



Precision Measurements and Parton Distribution Functions

C.-P. Yuan Michigan State University May 8, 2009 @ Berkeley Workshop

I thank my collaborators for providing many useful slides. Special thanks to Qing-Hong Cao, Chuan-Ren Chen, Joey Huston, Hung-Liang Lai, Jon Pumplin, Pavel Nadolsky, and Wu-Ki Tung.







- passed away on March 30, 2009
- the founder of "The Coordinated Theoretical-Experimental Project on Quantum Chromodynamics" (CTEQ) Collaboration.
- a founding member of Overseas Chinese Physics Association (OCPA)
- The last publication by himself is an invited article on Bjorken scaling in the new on-line "Scholarpedia" web site, sent in less than a month before his death.

http://www.scholarpedia.org/article/Bjorken_scaling



Remembering Wu-Ki



Reminded by my colleague Chih-Yung Chien (at JHU)

Two most famous sentences from Wu-Ki:



Of Course How do I know

I will tell you some of those stories (O and H) in this talk.

CTEQ

Timeline of CTEQ PDFs









 Most precise measurement of W boson mass was done at Tevatron.

 Most precise measurement of Top quark mass was done at Tevatron.







 Precision measurements at Tevatron Run-2 and LHC: W/Z Physics

 Impact of New CTEQ Parton Distribution Functions to LHC Phenomenology: W/Z, Top and Higgs Physics





W-boson physics

- W-boson production and decay at hadron collider
- 2 How to measure W-boson mass and width?
- High order radiative corrections:
 - **QCD** (NLO, NNLO, Resummation)
 - EW (QED-like, NLO)
- **4** ResBos-A and its predictions

CTEQ Theory requirements for Tevatron Run-II and LHC:



- Theory framework for Tevatron Run-I
 - $O(\alpha_S)$ (NLO-QCD) corrections
 - $O(\alpha)$ (QED) corrections
- Run-II experimental targets: $\delta \sigma_{tot} / \sigma_{tot} \sim 2 - 3\%$ $\delta M_W \sim 30 \text{ MeV}$
- Many factors contribute at a percent level:
 - $O(\alpha_s^2)$ (NNLO-QCD) corrections
 - $O(\alpha)$ (NLO-EW) corrections
 - uncertainties of parton distributions
 - power corrections to resummed cross sections

Adequate for comparison to Run-I data

Task: consistent and efficient implementation of these effects

Theory Calculations

There are a variety of programs available for comparison of data to theory and/or predictions.

- Tree level (Alpgen, CompHEP, Grace, Madgraph...)
 Les Houches accord
- Parton shower Monte Carlos (Herwig, Pythia,...
 MC@NLO
- NⁿLO (EKS, Jetrad, Dyrad, Wgrad, Zgrad,...

recover NLO (NNLO?) normalization

Resummed (ResBos)

Important to know strengths/weaknesses of each.

NLO Electroweak Calculations

- O(α) QED corrections to W/Z lepton decays
 F.A. Berends *et al.* Z. Physik C27 (1985) 155,365
- Electroweak corrections to W production
 - ***** Pole approximation ($\sqrt{\hat{s}} = M_W$)

D. Wackeroth and W. Hollik, Phys. Rev. D55 (1997) 6788

U. Baur, S. Keller, D. Wackeroth, Phys. Rev. D59 (1999) 013002 WGRAD

\star Complete $\mathcal{O}(\alpha)$ corrections

 V.A. Zykunov, Eur. P. J. C3 (2001) 9, Phys. Atom. Nucl. 69 (2006) 1522

 S. Dittmaier and M. Krämer, Phys. Rev. D65 (2002) 073007
 DK

 U. Baur and D. Wackeroth, Phys. Rev. D70 (2004) 073015
 WGRAD2

 A. Arbuzov et al., Eur. Phys. J. C46 (2006) 407
 SANC

 C.M. Carloni Calame et al., JHEP 12 (2006) 016
 HORACE

Electroweak corrections to Z production

 $\star \mathcal{O}(\alpha)$ photonic corrections

U. Baur, S. Keller, W.K. Sakumoto, Phys. Rev. D57 (1998) 199 ZGRAD

\star Complete $\mathcal{O}(\alpha)$ corrections

U. Baur et al., Phys. Rev. D65 (2002) 033007

ZGRAD2

C.-P. Yuan (MSU) Precision Electroweak Physics at Hadron Colliders

Multiple Photon Emissions

- Higher-order (real+virtual) QED corrections to W/Z production
 - → HORACE (Pavia): QED Parton Shower + NLO electroweak corrections to W/Z production (Z production available soon)

C.M. Carloni Calame *et al.*, Phys. Rev. **D69** (2004) 037301 C.M. Carloni Calame *et al.*, JHEP **05** (2005) 019; JHEP **12** (2006) 016

- → WINHAC (Cracow): YFS exponentiation + electroweak corrections to W decay S. Jadach and W. Placzek, Eur. Phys. J. C29 (2003) 325
- Perfect agreement between HORACE and WINHAC on multiphoton corrections to all W observables

C.M. Carloni Calame et al., Acta Phys. Pol. B35 (2004) 1643

- Recent effort to improve the treatment of multiphoton radiation in HERWIG (with SOPHTY via YFS) and PHOTOS (via QED Parton Shower)
 K. Hamilton and P. Richardson, JHEP 0607 (2006) 010
 P. Golonka and Z. Was, Eur. Phys. J. C45 (2006) 97
- ★ W-mass shift due to multiphoton radiation is about 10% of that caused by one photon emission → non-negligible for precision W mass measurements!

C.M. Carloni Calame et al., Phys. Rev. D69 (2004) 037301

Higher Order QCD Corrections

NLO/NNLO corrections to W/Z total production rate

G. Altarelli, R.K. Ellis, M. Greco and G. Martinelli, Nucl. Phys. B246 (1984) 12

R. Hamberg, W.L. van Neerven, T. Matsuura, Nucl. Phys. B359 (1991) 343

NLO calculations for W, Z + 1, 2 jets (DYRAD, MCFM ...)

W.T. Giele, E.W.N. Glover and D.A. Kosower, Nucl. Phys. B403 (1993) 633

J.M. Campbell and R.K. Ellis, Phys. Rev. D65 (2002) 113007

• resummation of leading/next-to-leading p_{\perp}^W/M_W logs (ResBos)

C. Balazs and C.P. Yuan, Phys. Rev. D56 (1997) 5558

NLO corrections merged with HERWIG Parton Shower (MC@NLO)

S. Frixione and B.R. Webber, JHEP 0206 (2002) 029

 Multi-parton matrix elements Monte Carlos (ALPGEN, SHERPA...) matched with vetoed Parton Showers

> M.L. Mangano *et al.*, JHEP 0307 (2003) 001 F. Krauss *et al.*, JHEP 0507 (2005) 018

• fully differential NNLO corrections to W/Z production (FEWZ)

C. Anastasiou *et al.*, Phys. Rev. **D69** (2004) 094008 K. Melnikov and F. Petriello, Phys. Rev. Lett. **96** (2006) 231803, Phys. Rev. **D74** (2006) 114017

C.-P. Yuan (MSU) Precision Electroweak Physics at Hadron Colliders

Combine QCD and Electroweak

 First attempt: combination of soft-gluon resummation with NLO final-state QED corrections

Q.-H. Cao and C.-P. Yuan, Phys. Rev. Lett. 93 (2004) 042001 ResBos-A

 Electroweak and QCD corrections can be combined in factorized form to arrive at

$$\left[\frac{d\sigma}{d\mathcal{O}}\right]_{\mathsf{QCD}\otimes\mathsf{EW}} = \left\{\frac{d\sigma}{d\mathcal{O}}\right\}_{\mathsf{QCD}} + \left\{\left[\frac{d\sigma}{d\mathcal{O}}\right]_{\mathsf{EW}} - \left[\frac{d\sigma}{d\mathcal{O}}\right]_{\mathsf{LO}}\right\}_{\mathsf{HERWIG}\;\mathsf{PS}}$$

- QCD ⇒ ResBos, MC@NLO, ALPGEN (with CKKW-MLM Parton Shower matching and standard matching parameters), FEWZ, ...
- EW
 ⇒ Electroweak + multiphoton corrections from HORACE convoluted with HERWIG QCD Parton Shower
 - ★ NLO electroweak corrections are interfaced to QCD Parton Shower evolution ⇒ O(αα_s) corrections not reliable when hard non-collinear QCD radiation is important
 - * Beyond this approximation, a full two-loop $\mathcal{O}(\alpha \alpha_s)$ calculation is needed (unavailable yet) J.H. Kühn *et al.*, hep-ph/0703283 NLO/NNLO_{EW} to $pp \rightarrow Wj$



- Cannot describe data with small q_T of W-boson.
- Cannot precisely determine m_W at hadron colliders without knowing the transverse momentum of W-boson. Most events fall in the small q_T region.















W-boson production and decay How to measure W mass and width High order radiative corrections ResBos-A and its predictions

Theory requirements for Run-II High order QCD corrections (NLO, NNLO, Resum) High order EW corrections ResBos-A and its predictions

What is QCD resummation ?

All order quantum corrections



Resummation is to reorganize the results in terms of the large Log's.

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W-boson production and decay How to measure W mass and width High order radiative corrections ResBos-A and its predictions Theory requirements for Run-II High order QCD corrections (NLO, NNLO, Resum) High order EW corrections ResBos-A and its predictions

What is QCD resummation ?

reorganization of logs



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CSS resummation formalism

[Non-perturbative functions] are functions of (b,Q,x_A,x_B) which include QCD effects beyond Leading Twist.

W-boson production and decay How to measure W mass and width High order radiative corrections ResBos-A and its predictions Theory requirements for Run-II High order QCD corrections (NLO, NNLO, Resum) High order EW corrections ResBos-A and its predictions

Resummation effects agree with data very well

$P\bar{P} \rightarrow Z$ @ Tevatron



A fortran program that includes the effect of multiple soft gluon emission on the production of W and Z bosons in hadron collisions.



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• Difference between u(x) and d(x) in proton cause $u\bar{d} \to W^+$ and $\bar{u}d \to W^-$ to be boosted in opposite directions

$$A(y_{W}) = \frac{d\sigma(W^{+})/dy_{W} - d\sigma(W^{-})/dy_{W}}{d\sigma(W^{+})/dy_{W} + d\sigma(W^{-})/dy_{W}}$$

$$A(y_{W}) \approx \frac{u(x_{1})d(x_{2}) - d(x_{1})u(x_{2})}{u(x_{1})d(x_{2}) + d(x_{1})u(x_{2})}$$
Rapidity charge asymmetry is sensitive to $d(x)/u(x)$ ratio at high-x
 \rightarrow primary interest of PDF fitters.
• cannot reconstruct y_w directly
• measure charged lepton only
$$A(\eta_{l}) = \frac{d\sigma(l^{+})/d\eta_{l} - d\sigma(l^{-})/d\eta_{l}}{d\sigma(l^{+})/d\eta_{l} + d\sigma(l^{-})/d\eta_{l}}$$

$$(\mu_{l}) = \frac{d\sigma(l^{+})/d\eta_{l} - d\sigma(l^{-})/d\eta_{l}}{d\sigma(l^{+})/d\eta_{l} + d\sigma(l^{-})/d\eta_{l}}$$



Rapidity Distribution

C T E Q





ResBos needed for Rapidity

Charged lepton asymmetry (from W decay)

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All recent CTEQ and MSTW PDF fits include the effects of soft gluon resummation predicted by ResBos.





• The complete NLO EW correction to W and Z boson production in hadron collisions are known.

• The NLO QED corrections to the decay of W and Z bosons can be factored out from the complete NLO EW corrections in a gauge invariant way.



• **ResBos-A**: improved **ResBos** by including final state NLO QED corrections



to W and Z production and decay

hep-ph/0401026 Qing-Hong Cao and CPY

• and

denote FQED radiation corrections, which dominates the W mass shift.





 p_T^e is sensitive to q_T^W







W Boson q_T @ D0 Run-2

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Z-boson physics

- Help to improve the measurement of W-boson
 - 🖙 calibrate detector
 - indirect measurement of W-boson width
- **2** ResBos-A and its predictions
 - effective Born approximation
 - various kinematical distributions

CTEQ

Precision measurement of Z-boson



R help to calibrate detector



detector response to hadronic recoil energy Combine lepton and neutrino p_{τ} to form transverse mass $(m_{ au})$ for best statistical power

Additional information from v p_{τ} (inferred through measurement of

muon

neutrino





- 1. We are entering the era of precision measurement at hadron colliders.
- 2. For precision measurement of W mass, it is needed to include both QCD and EW corrections consistently and efficiently.

As the first step toward this goal, ResBos-A includes both the initial state multiple soft gluon resummation effect and final state QED corrections (which dominates the W mass shift).

3. Precision measurement of Z boson, via the ratio method, can improve W-boson mass measurement and provide indirect measurement of W-boson width.



ResBos ResBos-A

IncludeInitial state QCD soft gluon resummationandFinal state QED corrections

For Drell-Yan, W, Z, Higgs, di-photon pairs, etc.

In collaboration with Csaba Balazs, Pavel Nadolsky, Qing-Hong Cao, Jian-Wei Qiu (Michigan State, Iowa State)

ResBos:http://hep.pa.msu.edu/resum/hep-ph/9704258ResBos-A:including final state QED correctionshep-ph/0401026Plotter:on-line plotting package (by P. Nadolsky)





Impact of New CTEQ Parton Distribution Functions to LHC Phenomenology:

W/Z, Top and Higgs Physics

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New Physics signal found?



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LHC Parton Kinematics





 $\mathbf{C} \mathbf{T} \mathbf{E} \mathbf{Q}$

Wu-Ki's O and H will be continued



Recent CTEQ activities

Preliminary CT09 fit (PN.)

- effect of the Tevatron Run-2 jet and W asymmetry data on CT09 PDF's
- \blacktriangleright CT09 strangeness at small x
- Combined fit of PDF's and Drell-Yan p_T distributions (H.-L Lat)
- PDF's for leading-order Monte-Carlo programs (H.-L. Lat)









Figure 1: Gluon distributions and uncertainties: CT09G (solid red); fit using CDF run II jets only (short dash blue); fit using D0 run II jets only (long dash green). (A larger weight factor x^4 is used in the right-hand figure to accentuate the large-x behavior.)

hep-ph/0904.2424



CT09 vs CTEQ6.6





Comparison of CT09 and CTEQ6.6 gluon PDF uncertainties at Q=2 GeV. MSTW08 central fit is also shown.



CT09 vs CTEQ6.6





Comparison of CT09 and CTEQ6.6 gluon PDF uncertainties at Q=85 GeV. MSTW08 central fit is also shown.



Precision measurement and combined global analysis of PDF including P_T resummation theory and data

In collaboration with

Hung-Liang Lai, Pavel Nadolsky, and Jon Pumplin



New Inputs:

- Experimentally: include not only rapidity (y) but also p_T of Drell-Yan pairs and Z bosons
- > Theoretically: include p_T Resummation formalism to account for the soft physics that entangle with multi-scale measurements

New Outputs:

> F_{NP} of non-perturbative function is simultaneously determined, In addition to the PDF $f_a(x,\mu)$.





Preliminary results



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Measurement of g2 from D0





DØ Note 5755-CONF

Version: 1.5

A Study of $Z \to e^+e^-$ and $Z \to \mu^+\mu^-$ Events Produced at Low Transverse Momentum Using a Novel Technique

The Z boson transverse momentum, p_T^Z , can be decomposed into two components, a_T and a_L , that are transverse and parallel, respectively, to the di-lepton thrust axis. Using the a_T distribution of Z decays observed with the DØ detector, we measure g_2 , a phenomenological parameter in the BLNY non-perturbative form factor. In a combined measurement with di-muon and di-electron decay channels, using approximately 2 fb⁻¹ of data, we measure $g_2 = 0.63 \pm 0.02 \pm 0.04 \text{ GeV}^2$ The first uncertainty is experimental and the second uncertainty is due to the PDF dependence of the theoretical prediction.

Translated to F_{NP} : $F_{NP}(M_Z)/b^2 = 2.51 \pm 0.15$



Preliminary results



	CTEQ66	CTEQ66	g2c	g2l	g2h
	(BLNY)	(refit g's)			
g_1	.210	.234	.294	.409	.219
g ₂	.680	.600	.566	.415	.660
$g_{1} g_{3}$	126	174	194	194	194
$F_{NP}(M_Z)/b^2$	2.68	2.51	2.49	2.10	2.73
χ^2_{pt} (111 Pts)	403	165	135	155	155
$\Delta \chi^2_{pt}$	267	30	0	20	20

(This range of 2.10 to 2.75 shall be compared to D0's 2.36 to 2.66.)





Impact of New CTEQ Parton Distribution Functions to LHC Phenomenology:

W/Z, Top and Higgs Physics







CTEQ6.6 PDF's, heavy flavors and PDF induced correlations between LHC observables

hep-ph/0802.0007

In collaboration with

Pavel Nadolsky, Hung-Liang Lai, Qing-Hong Cao, Joey Huston, Jon Pumplin, Dan Stump, Wu-Ki Tung



- NLO calculations using ResBos, WTTOT, MCFM
- CTEQ6.5 and CTEQ6.6 cross sections are qualitatively same
- At LHC, $\sigma_{W,Z}$ (CTEQ6.6M) $\approx 1.06\sigma_{W,Z}$ (CTEQ6.1M)
 - ► reflects a 6% increase in light quark luminosities $\mathcal{L}_{q_i\bar{q}_i}(x_1, x_2, Q) = q_i(x_1, Q)\bar{q}_j(x_2, Q)$ at relevant x and Q

finer differences with CTEQ6.5 in precision predictions for W, Z production, strange-quark scattering

Стео Correlation analysis for collider observable

A technique based on the Hessian method

For 2N PDF eigensets and two cross sections X and Y:

$$\Delta X = \frac{1}{2} \sqrt{\sum_{i=1}^{N} \left(X_i^{(+)} - X_i^{(-)} \right)^2}$$

$$\cos \varphi = \frac{1}{4\Delta X \, \Delta Y} \sum_{i=1}^{N} \left(X_i^{(+)} - X_i^{(-)} \right) \left(Y_i^{(+)} - Y_i^{(-)} \right)$$

 $X_i^{(\pm)}$ are maximal (minimal) values of X_i tolerated along the *i*-th PDF eigenvector direction; N = 22 for the CTEQ6.6 set

For CT09 PDFs, N=24.

сте Q Correlation analysis for collider observables

Correlation angle φ

Determines the parametric form of the X - Y correlation ellipse $X = X_0 + \Delta X \cos \theta$ $Y = Y_0 + \Delta Y \cos(\theta + \varphi)$ $\cos\varphi\approx 1$ $\cos \varphi \approx -1$ $\cos \varphi \approx 0$ δY δY X_0, Y_0 : best-fit values δX δX δX $\Delta X, \Delta Y$: PDF errors $\cos\varphi \approx \pm 1$: tight Measurement of X imposes constraints on Y $\cos\varphi \approx 0$: loose

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For cross section of Z boson at the LHC_10 TeV

For cross section of W+ boson at the LHC_10 TeV

CTEQ





For cross section of W- boson at the LHC_10 TeV

W+/W- vs. u/d at the LHC_10 TeV



CT09 vs CTEQ6.6





Comparison of CT09 and CTEQ6.6 u and d PDF uncertainties at Q=85 GeV. MSTW08 central fit is also shown.

Correlations (CT09 PDFs) @ LHC_10





Cross section of a 500 GeV Higgs boson at the LHC_10 TeV

CTEQ

Top quark pair cross section at the LHC_10 TeV

Correlations (CT09 PDFs) @ LHC_10





CT09: σ_{tot} correlation

Higgs (500 GeV) vs top quark pair

CTEQ

W+ vs Z







Correlation of Z Rapidity distribution at LHC_10 TeV to CT09 PDFs

Sensitive to different parton flavors at different rapidity.

Correlations (CT09 PDFs) for Higgs (120 GeV)



At Tevatron

CTEQ

At LHC 10 TeV



Different sensitivity to partons at various x values lead to different PDF induced uncertainty in cross sections.

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Top Quark Pair production rates





CTEQ











• What's the top mass in a full event generator, such as PYTHIA?

NOBODY KNOWS

Parton showers generate some higher order corrections in the event shape, but with approximations.





Effect of pQCD Resummation:

Higgs Signal and Background





- new pdf : cteq 6.6M
- matching NNLO ($\alpha_{s}{}^{4})$ in high p_{T} region

Q.-H. Cao, C.-R. Chen, C.R. Schmidt and CPY, in progress.

• Including K factors in
$$\frac{d\sigma}{dQ^2 dy dQ_T}$$
 grids :

$$k_{pert} = [pert(\alpha_s^3) + pert(\alpha_s^4)] / pert(\alpha_s^3)$$

$$k_{Y} = \left[Y(\alpha_{s}^{3}) + Y(\alpha_{s}^{4})\right] / Y(\alpha_{s}^{3})$$

Total cross section of $gg \rightarrow H \rightarrow WW \rightarrow \ell^+ \ell^- \nu \nu$

M _H -100 Gev						
	cteq 6.1M (α_s^3)	cteq 6.6M (α_s^3)	cteq 6.6M (α_s^4)			
@Tevatron	2.37 fb	2.26 fb	2.60 fb			
@LHC	174 fb	172 fb	205 fb			

M = 160 CoV/



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Higgs search Background: Direct di-photon production



The search for Higgs resonance relies on good understanding of the large QCD background



It is useful to apply the likelihood analysis to fully **differential distributions** of the signal and background

- I resummation is needed for logarithmic corrections of several types from all orders in α_s
 - ▶ e.g., $\alpha_s^n \ln^k(Q_T/Q)$ at $Q_T \ll Q$

Signal and background in $H \to \gamma \gamma$

global aspects, such as calibration of collider luminosity and detectors, will affect precision of the measurement of Higgs cross sections pQCD Resummation Calculation







Di-Phootn Production



Direct diphotons

The dominant production mode; evaluated up to NLO in α_s

Balazs, Berger, Nadolsky, Yuan, 2006



$q\bar{q} + qg$ channel

- NLO matrix elements: Aurenche et al.; Bailey, Owens, Ohnemus
- qq̄ scattering dominates at the Tevatron
- qg scattering is strongly enhanced at the LHC by photon radiation off final-state quarks





 $\mathcal{O}(\alpha_S)$ resummed cross section

Hep-ph/0603049

Simplified ACOT scheme was used

 $\therefore M_H \neq 0$ only in the gluon-initiated channels

 $S^{pert}(b,Q)$ and functions $\mathcal{C}^{in}_{jq}(x,b\mu_F), \mathcal{C}^{out}_{bj}(z,b\mu_F)$ do not depend on the mass

Only $C_{jg}^{in}(x, b, M, \mu_F)$ retains mass



The effect from initial state heavy parton mass is included in perturbative Wilson coefficient function, using CSS resummation fromalism in the general-mass variable-flavor number scheme.

This effect has been included in the **ResBos** code.





Figure 2: Transverse momentum distribution of on-shell Higgs bosons in the $b\bar{b} \rightarrow \mathcal{H}$ channel at (a) the Tevatron and (b) LHC. The solid (red) lines show the q_T distribution in the massive (S-ACOT) scheme. The dashed (black) lines show the distribution in the massless ("ZM-VFN") scheme. The numerical calculation was performed using the programs Legacy and ResBos [29, 30] with the CTEQ5HQ1 parton distribution functions [31]. The bottom quark mass is taken to be $m_b = 4.5$ GeV.



 Precision measurements demand higher order calculations
 NLO, NNLO, Resummation

PDFs need to be refined using the early LHC (W, Z and top) data
 to reliably predict New Physics signal.





Backup Slides



Run-2 W Lepton Asymmetry Data





W-Lepton Asymmetry





W-Lepton Asymmetry [Ratio^{*} = (DatAsy-0.5)/(ThyAsy-0.5)]

