

Resummation in Heavy Particle Production

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Berkeley Workshop on Early LHC Physics, 5/7/09

Outline

- quarkonium production near kinematic endpoints

color-octet mechanism in photoproduction, $e^+e^- \rightarrow J/\psi + X$

S.Fleming, A. Leibovich, TM, PRD68:094011(2003), PRD74:114004(2003)

- threshold effects in $t\bar{t}$ pair production

threshold resummation $t\bar{t}$ production

Y. Kiyo, et.al. Eur.Phys. J. C60:375(2009)

resummed cross sections for NP particles

A. Idilbi, C. Kim, & T.M., arXiv:0903.3668[hep-ph]

A. Kulesza and L. Motyka, arXiv:0807.2405[hep-ph]

U. Langenfeld and S.O. Moch, arXiv:0901.0802[hep-ph]

Quarkonium Production Near Kinematic Endpoints

Review of NRQCD

- EFT for nonrelativistic $Q\bar{Q}$ ($J/\psi, \Upsilon, B_c$)
- Factorization Theorem for cross sections, decay rates:
(Bodwin, Braaten and Lepage)

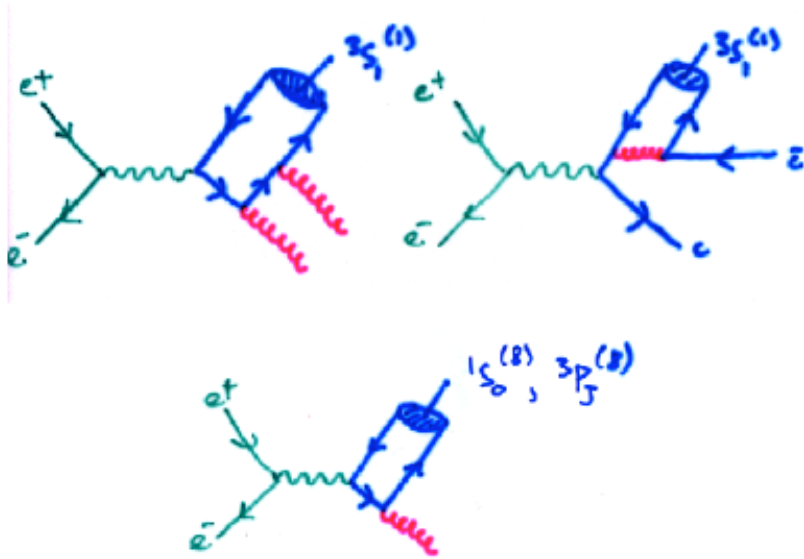
$$d\sigma = \sum_n c_n(\alpha_s) \langle O_n \rangle, \quad \langle O_n \rangle \sim v^n$$

- double expansion in α_s, v
- color-singlet model (J/ψ) lowest order in v expansion
- color-octet mechanisms v suppressed but often important

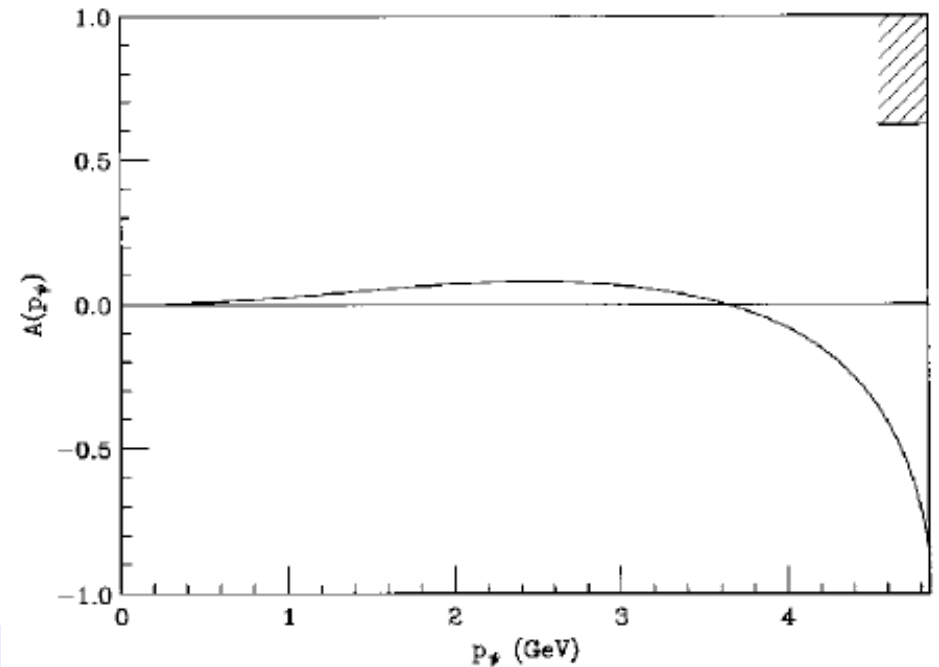
Quarkonium Production Near Kinematic Endpoints

- Color-Octet Signal in $e^+e^- \rightarrow J/\psi + X$

(Braaten, Chen)



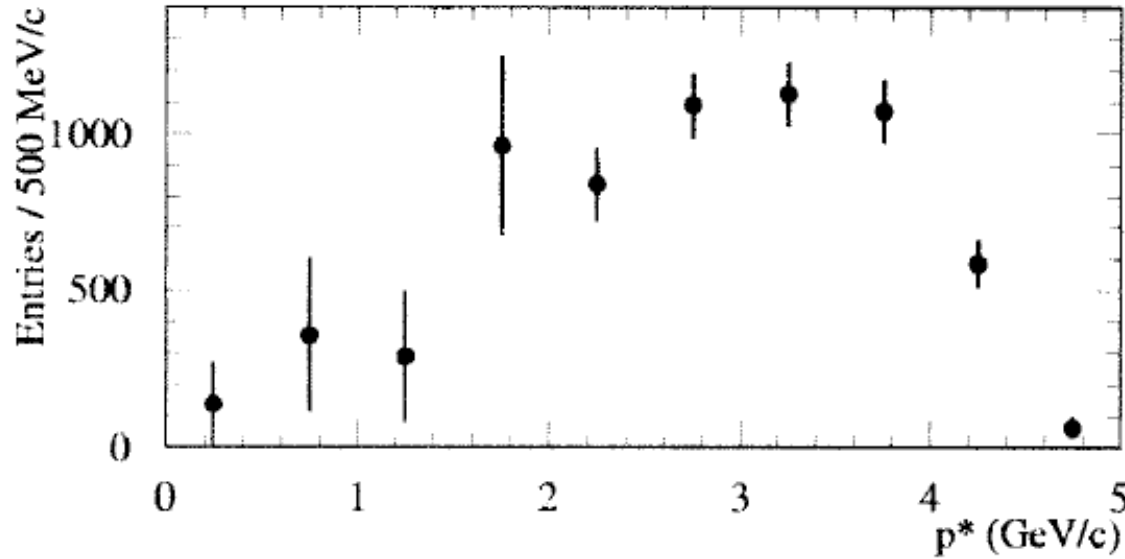
$$\sigma^{\text{LO}}[e^+e^- \rightarrow J/\psi c\bar{c}] \sim 0.1 \sigma^{\text{LO}}[e^+e^- \rightarrow J/\psi gg]$$



- Large (~ 1 pb) CO contribution near endpoint (total CS 0.4-0.9 pb)
- angular distribution ($\cos \theta$ – angle between J/ψ and beam)

$$\frac{d\sigma}{dp d\cos\theta} = S(p)(1 + A(p)\cos^2\theta)$$

- BaBar (J/ψ cross section)



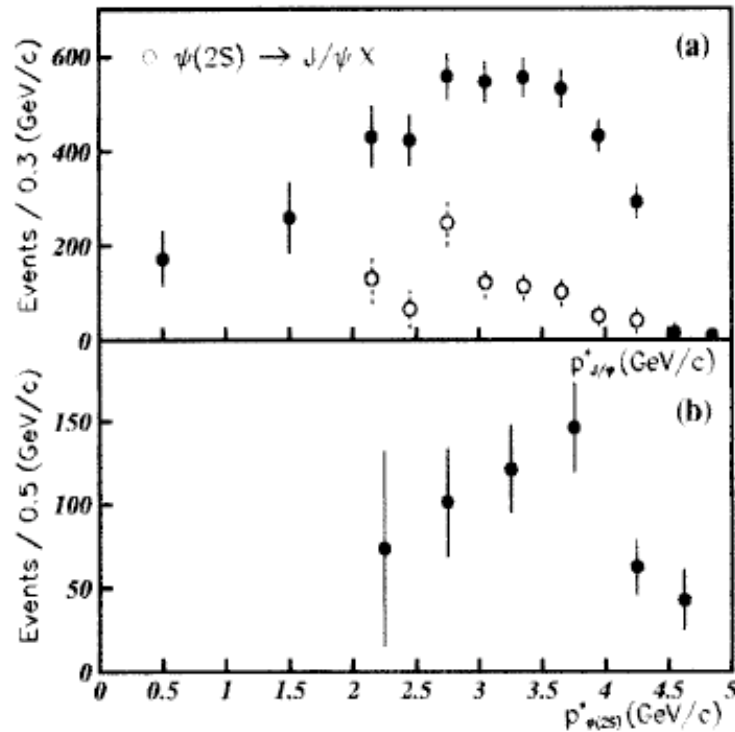
- $\sigma_{\text{tot}} = 2.52 \pm 0.21 \pm 0.21 \text{ pb}$

$$A(p) = \begin{cases} 0.05 \pm 0.22 & p < 3.5 \text{ GeV} \\ 1.5 \pm 0.6 & p > 3.5 \text{ GeV} \end{cases}$$

- Total cross section in excess of CSM, $A(p) \sim 1$ for large p

- Where is color-octet contribution at endpoint?

- Belle



$$\sigma_{\text{tot}} = 1.47 \pm 0.10 \pm 0.13 \text{ pb}$$

$$A(p) = \begin{cases} 0.3^{+0.5}_{-0.4} & 2.0 < p < 2.6 \text{ GeV} \\ 1.1^{+0.4}_{-0.3} & 2.6 < p < 3.4 \text{ GeV} \\ 1.1^{+0.4}_{-0.3} & 3.4 < p < 4.9 \text{ GeV} \end{cases}$$

- Other Puzzles: $\frac{\sigma(e^+e^- \rightarrow J/\psi c\bar{c})}{\sigma(e^+e^- \rightarrow J/\psi X)} = 0.59^{+0.15}_{-0.13} \pm 0.12 \quad (2002)$

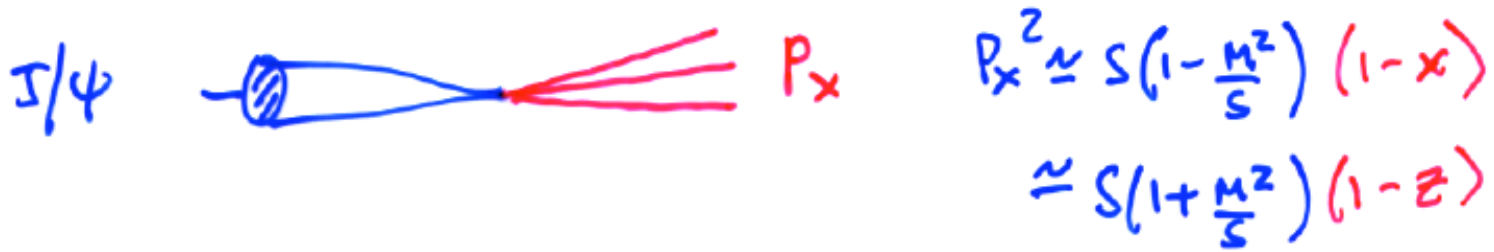
Recent Data

BELLE, arXiv:0901.2775 [hep-ex]

$$\sigma[e^+e^- \rightarrow J/\psi + c\bar{c} + X] = 0.74 \pm 0.08^{+0.09}_{-0.08} \text{ pb}$$

$$\sigma[e^+e^- \rightarrow J/\psi + X(\text{non-}c\bar{c})] = 0.43 \pm 0.09 \pm 0.09$$

- Near endpoint $c\bar{c}$ recoiling against low mass energetic jet



$$x = \frac{E + p_z}{\sqrt{s}}$$

$$z = E^\psi / E_{\max}^\psi$$

- Large perturbative, nonperturbative corrections

(Beneke, Rothstein, and Wise)

$$\alpha_s \frac{\ln(1-x)}{1-x} \quad \frac{v^2}{1-x}$$

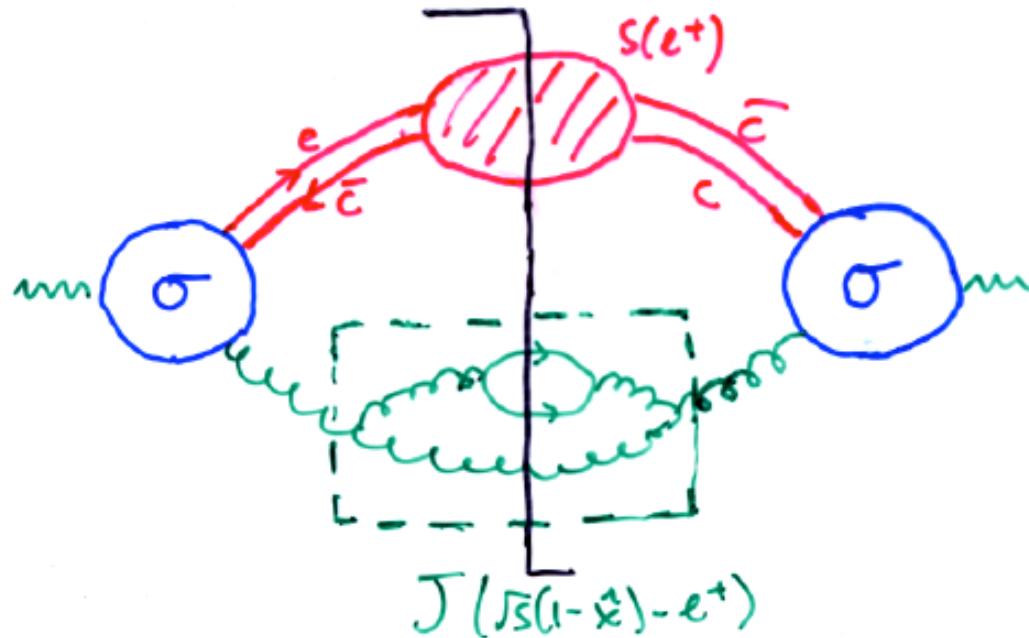
- $1 - \hat{x} \sim \Lambda_{\text{QCD}}/M \longrightarrow p_\psi \approx 3 \text{ GeV}$

$$(p_\psi)_{\max} \approx 4.8 \text{ GeV}$$

- as $x \rightarrow 1$ need a new factorization theorem

(Fleming, Leibovich, T.M.)

$$\frac{d\sigma}{dx} = \sigma(\mu) \int dl^+ S(l^+) J(\sqrt{s}(1 - \hat{x}) - l^+)$$



- resum large logs using RGE's for $S(l^+)$, $J(\sqrt{s}(1 - \hat{x}) - l^+)$
- nonperturbative corrections incorporated in **shape function** $S(l^+)$

Soft Collinear Effective Theory

(Bauer, Fleming, Luke, Pirjol, Stewart)

- Inclusive process Hard Scale $\sim Q$

- Degrees of Freedom

$$n^\mu = (1, 0, 0, 1), \quad \bar{n}^\mu = (1, 0, 0, -1)$$

collinear $(\bar{n} \cdot p, n \cdot p, p_\perp) \sim Q(1, \lambda^2, \lambda)$

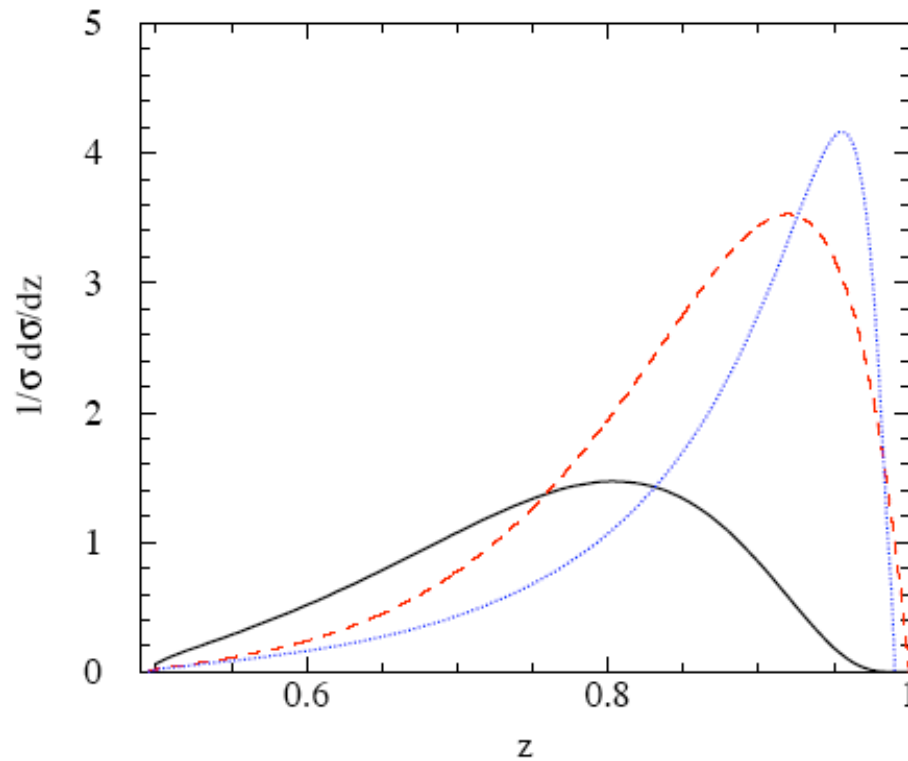
usoft $(\bar{n} \cdot p, n \cdot p, p_\perp) \sim Q(\lambda^2, \lambda^2, \lambda^2)$

- $e^+e^- \rightarrow J/\psi + X$ $Q \sim \sqrt{s} \sim 2m_c$ $\lambda \sim \sqrt{\Lambda_{\text{QCD}}/Q} \sim \sqrt{1-x}$

collinear gluons $J(\sqrt{s}(1 - \hat{x}) - \ell^+)$

usoft gluons, heavy quarks $S(\ell^+)$

- **Not Predictive** - depends on unknown **universal** $S(\ell^+)$
test universality in photo-, electroproduction ?

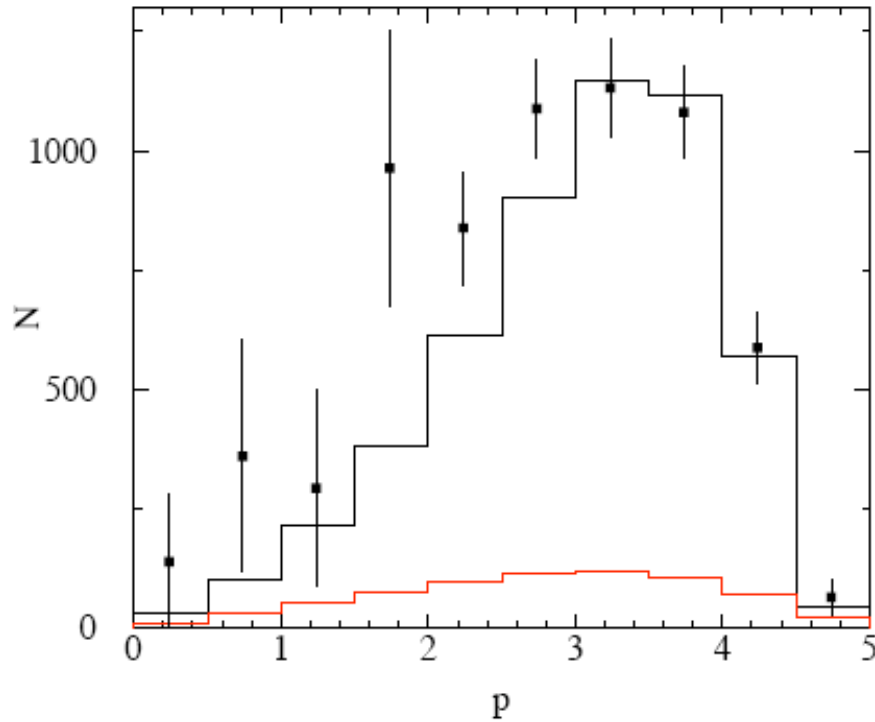


Dotted - resummation only
Dashed - shape function only
Solid - both

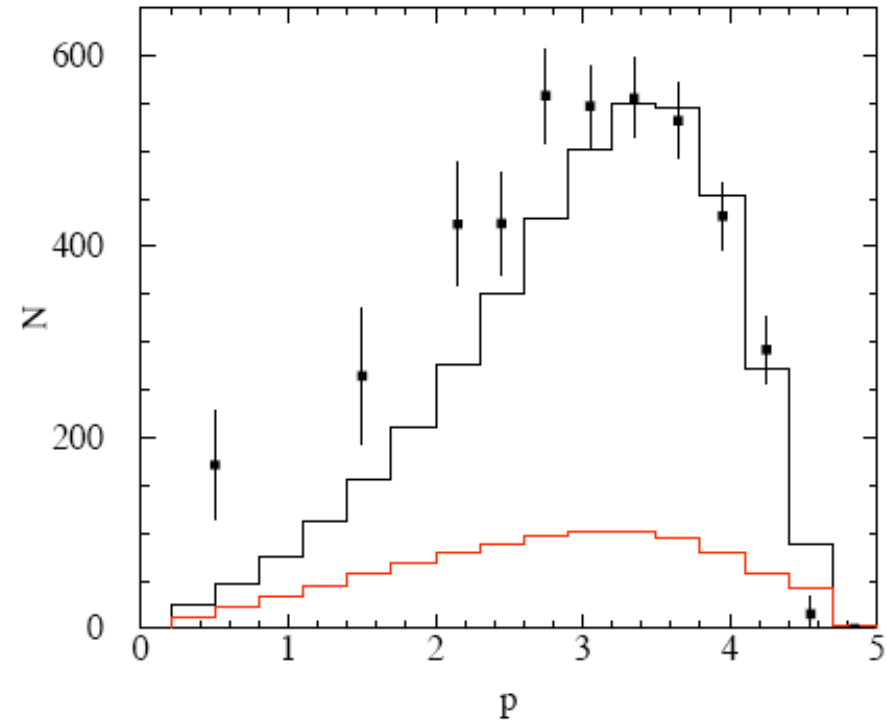
- NRQCD scaling rules:

$$S_N = \int d\hat{\ell}^+ (\hat{\ell}^+)^N S(\hat{\ell}^+) \sim (2m_c v^2)^N \sim \Lambda_{\text{QCD}}^N; N \geq 1$$

- **Comparison with Data** (Different normalization)



BaBar



Belle

- **Absence of color-octet peak near endpoint understood**

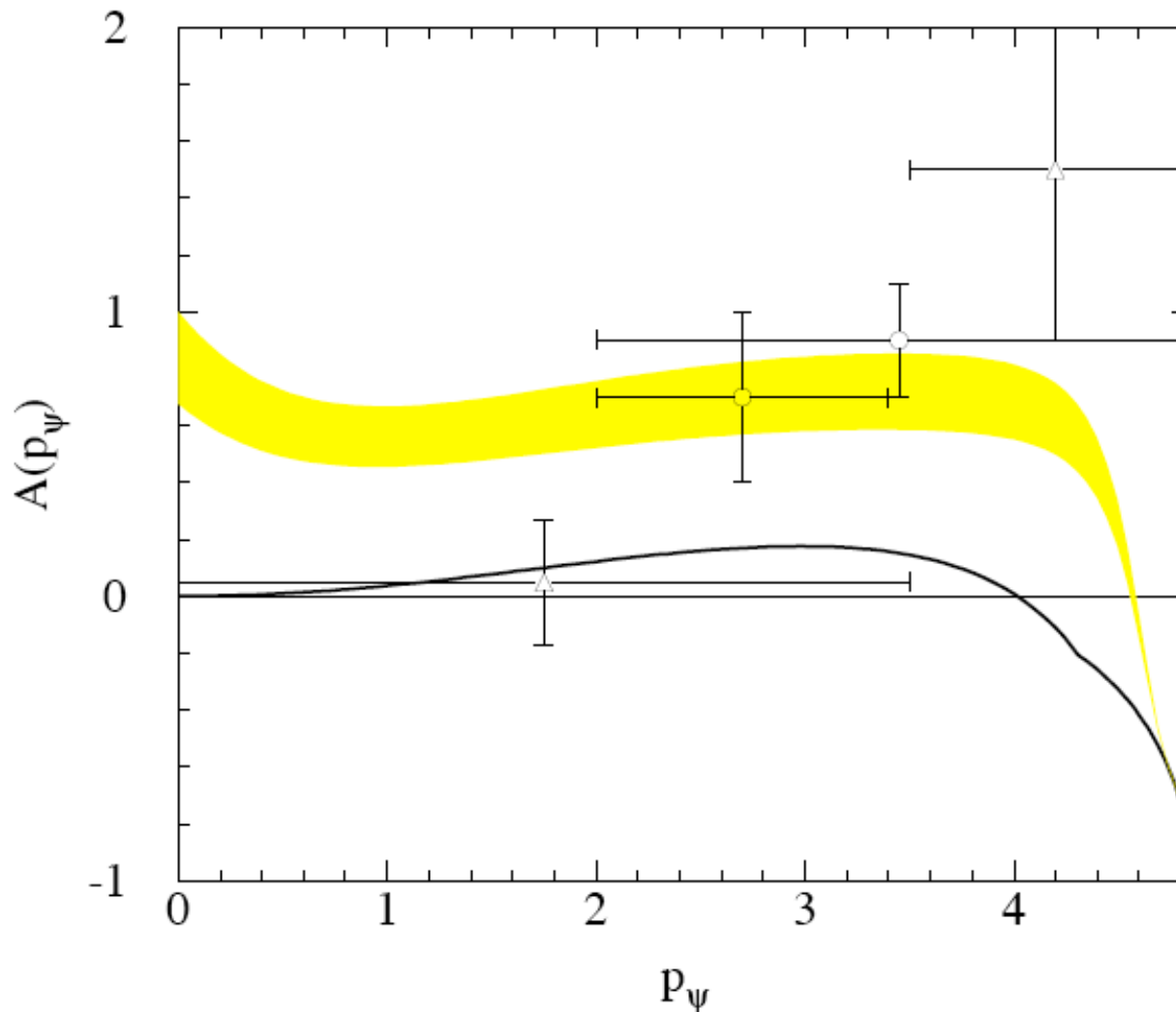
- $\frac{\sigma(e^+e^- \rightarrow J/\psi c\bar{c})}{\sigma(e^+e^- \rightarrow J/\psi X)}$ still unexplained, NLO effects close gap slightly

$$\sigma^{\text{NLO}}[e^+e^- \rightarrow J/\psi c\bar{c}] \approx 1.8 \sigma^{\text{LO}}[e^+e^- \rightarrow J/\psi c\bar{c}] \quad \text{Y.-J.Zhang \& K.-T. Chao, PRL 98:092003 (2007)}$$

$$\sigma^{\text{NLO}}[e^+e^- \rightarrow J/\psi gg] \approx 1.2 \sigma^{\text{LO}}[e^+e^- \rightarrow J/\psi gg] \quad \text{B. Gong \& J.-X. Wang, PRL 98:092003 (2007)}$$

feeddown from ψ'

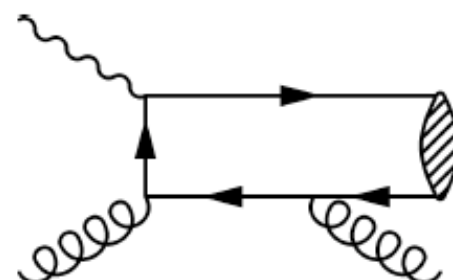
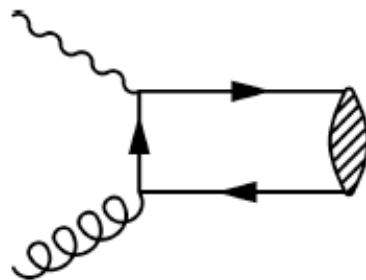
- Angular distribution



Solid line - Color-Singlet Model, Yellow Band - Resummed Color-Octet

$A(p_\psi) \approx 1$ at large p_ψ (don't believe resummation at small p_ψ)

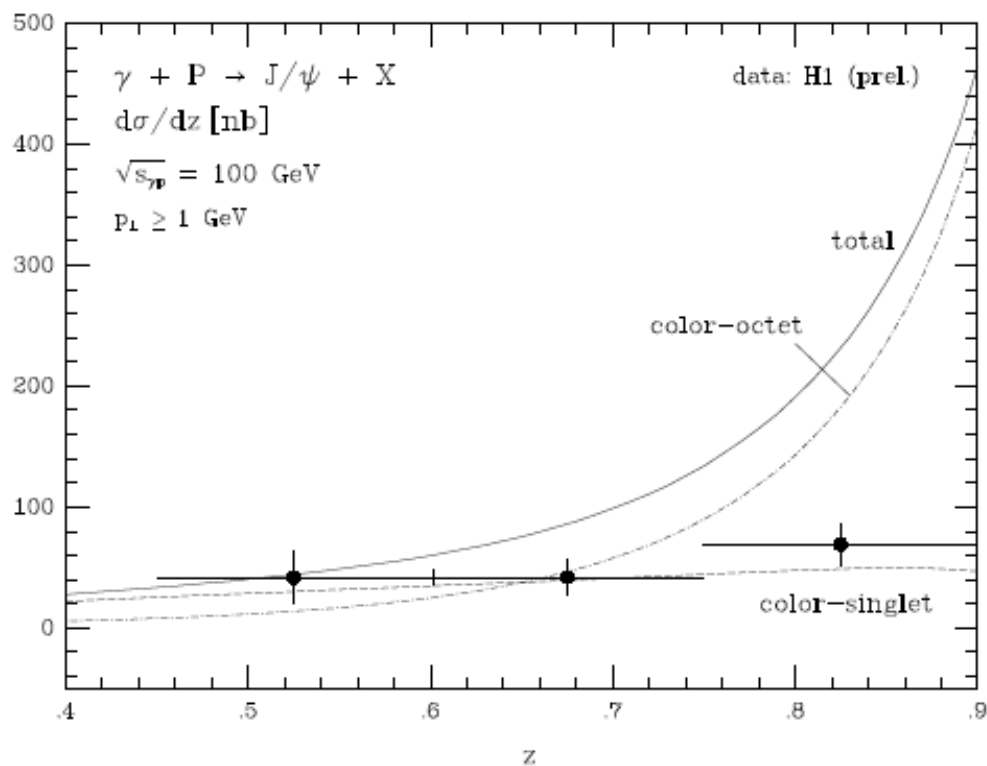
● Photoproduction



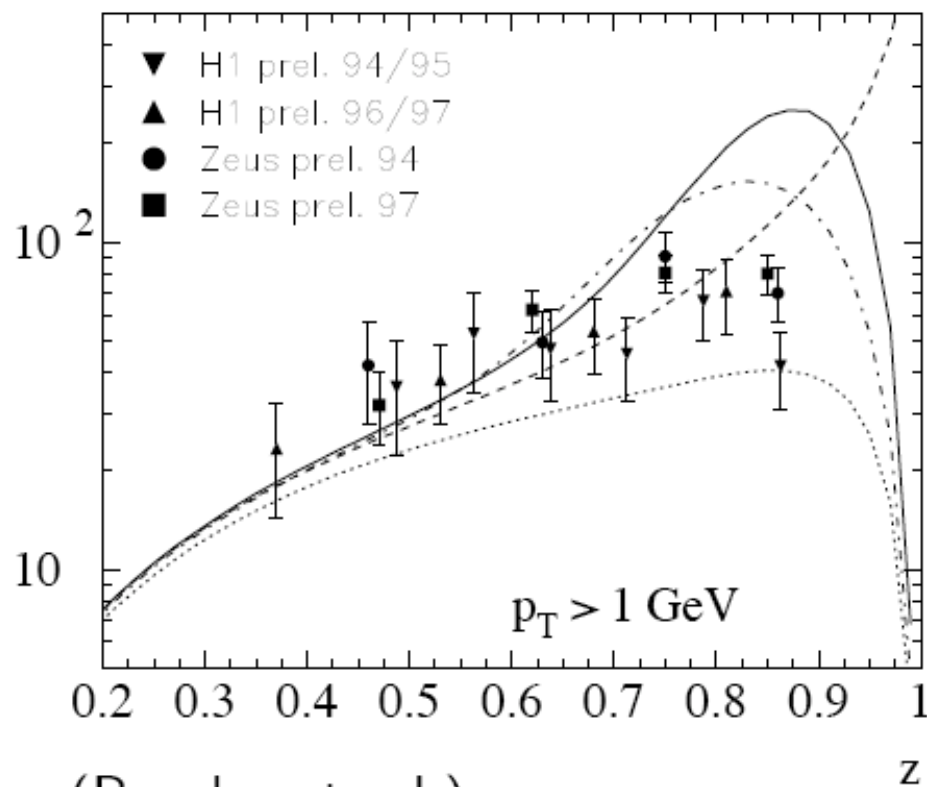
$$z = E^\psi / E_{\max}^\psi$$

$$\sigma_0 \delta(1 - z)$$

$$- \sigma_0 \frac{C_A \alpha_s}{\pi} \frac{\ln(1 - z)}{1 - z} + \dots$$



$d\sigma(\gamma p \rightarrow J/\psi X)/dz$ [nb]



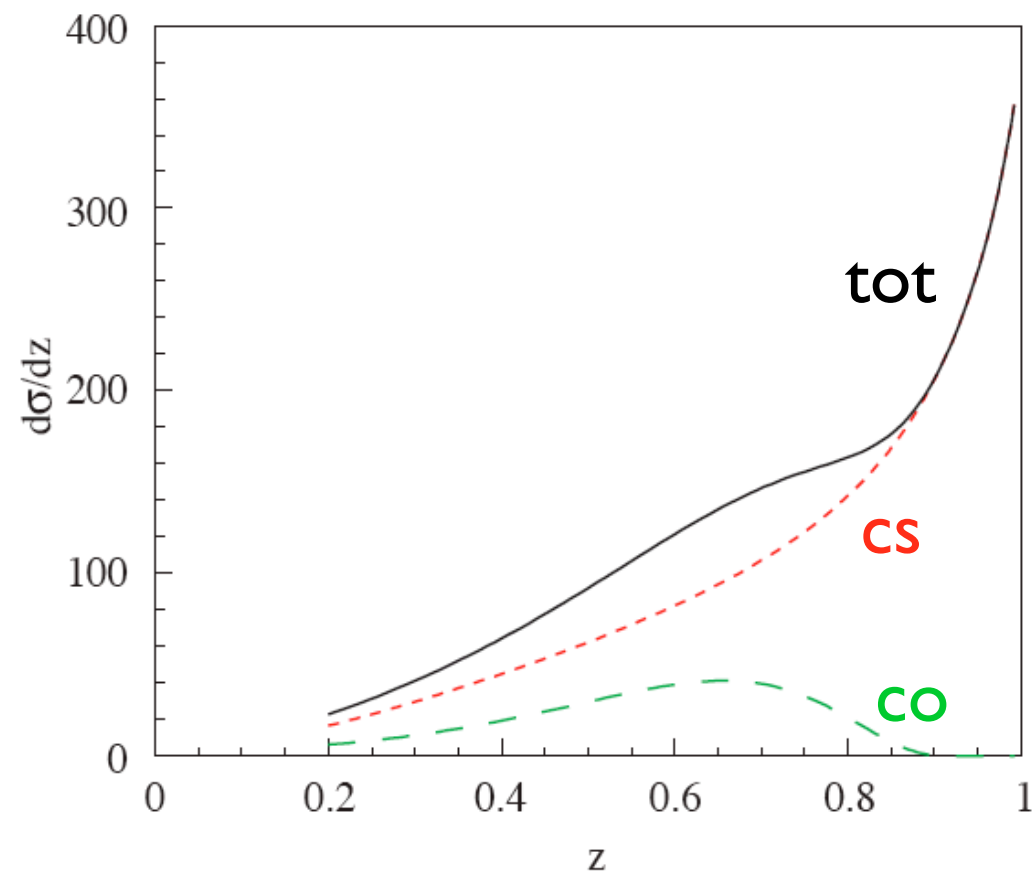
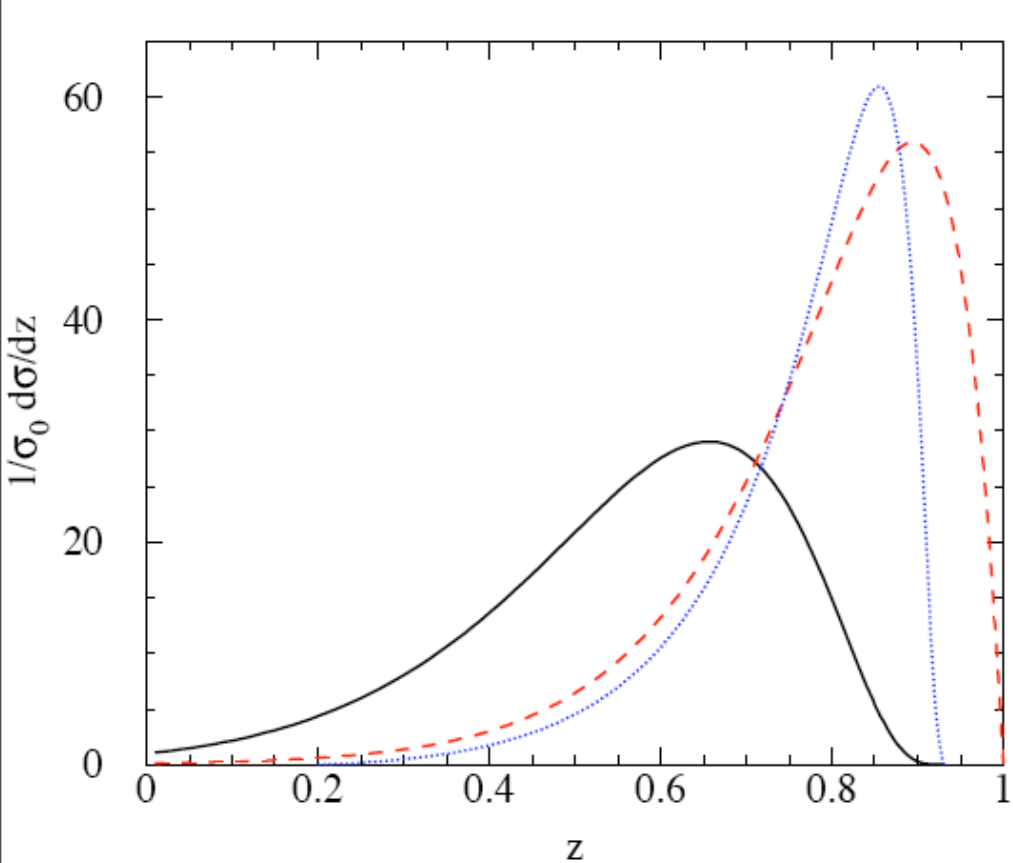
(Cacciari, Kramer)

(Beneke, et. al.)

NLO CO

includes shape function, no resum.

- Resummed Cross Section



- Peak shifted from $z \sim 0.9$ to $z \sim 0.7$
- nonperturbative and perturbative resummation required
- CO matrix element is ~ 10 times smaller than Tevatron!

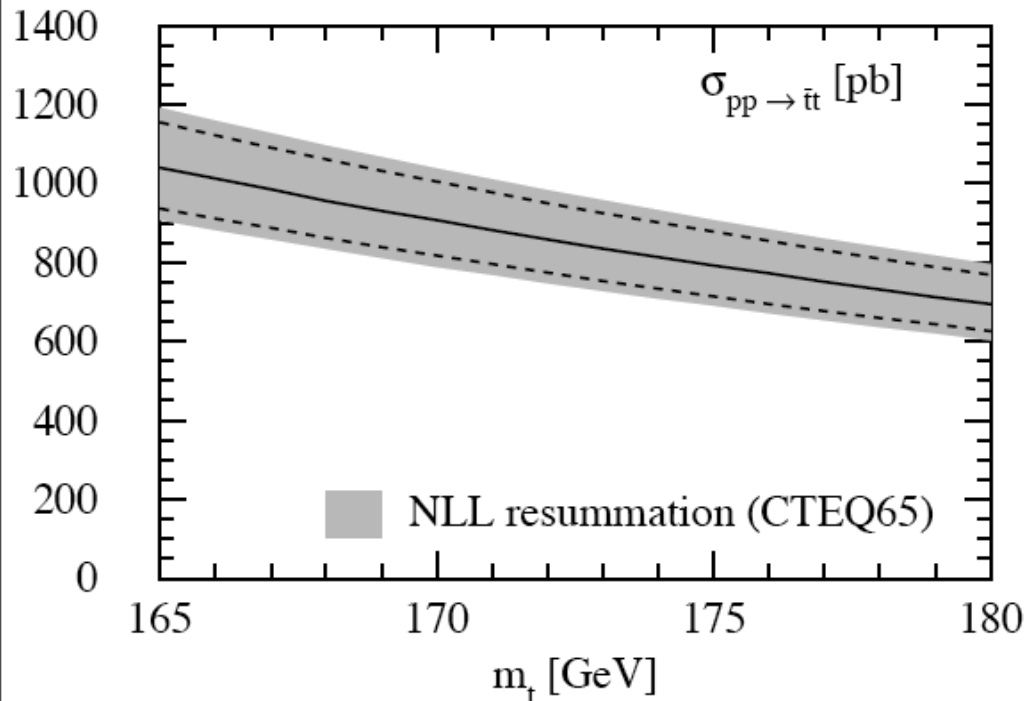
$t \bar{t}$ pair production

Top quark pair production

- dominant production mechanism - gluon-gluon fusion



- include NLO QCD correction, NLL resummation



$$\sigma_{\text{tot}} \approx 900 \text{ pb}, \sqrt{s} = 14 \text{ TeV}$$
$$\approx 400 \text{ pb}, \sqrt{s} = 10 \text{ TeV}$$

Scale, pdf uncertainty ~10-15%

reduce to ~5% w/ full NNLO

only partial NNLO available now

Physics Goals

- measure m_t
- anomalous couplings

$$-\frac{g_W}{\sqrt{2}}\varepsilon^{*\mu}\bar{u}_b \left[(V_{tb}^* + f_L)\gamma_\mu P_L + f_R\gamma_\mu P_R + i\sigma_{\mu\nu}q^\nu \left(\frac{g_L}{m_W}P_L + \frac{g_R}{m_W}P_R \right) \right] u_t$$

indirect bounds from $B \rightarrow X_s \gamma$

$$\begin{aligned}
 -0.13 < f_L < 0.03 \\
 -7 \cdot 10^{-3} < f_R < 2.5 \cdot 10^{-3} \\
 -1.5 \cdot 10^{-3} < g_L < 4 \cdot 10^{-4} \\
 -0.15 < g_R < 0.57
 \end{aligned}$$

B. Grzadkowski & M. Misiak, 0802.1413 [hep-ph]

- probe Higgs mechanism

top important source of longitudinal W bosons!

F_λ^W - fraction of W with helicity λ (assuming V-A coupling)

$$F_0^W \sim 0.7, \quad F_-^W \sim 0.3, \quad F_+^W \sim 0$$

measured through angular distribution in $W^+ \rightarrow \ell^+ \nu_\ell$

- new physics, e.g. $t\bar{t}$ resonances

Threshold Resummation

- LHC: 80% of cross section $2m_t \leq \sqrt{\hat{s}} < 600 \text{ GeV}$

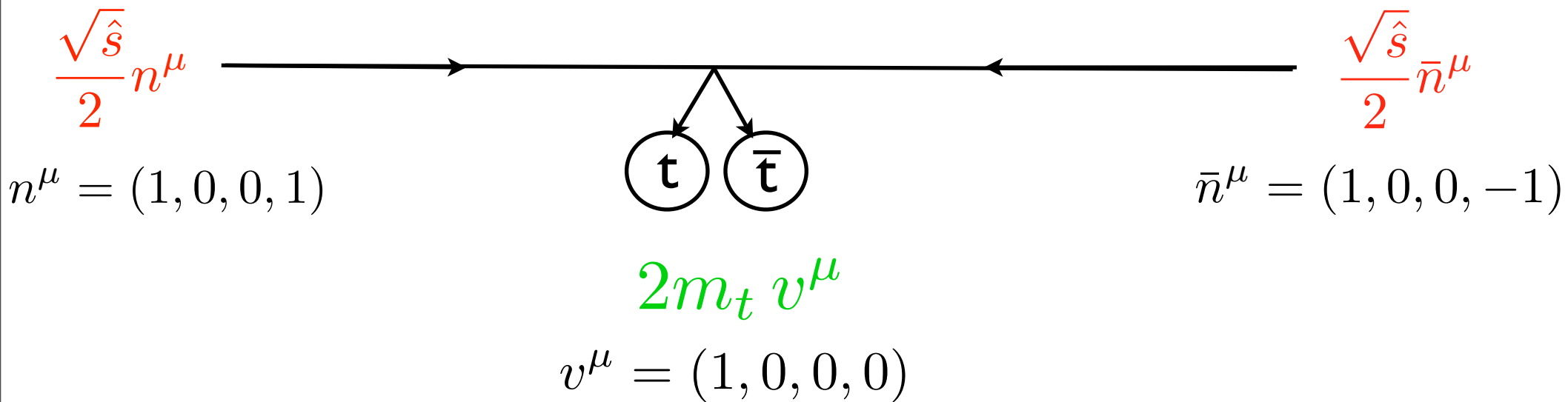
- fixed order calculations exhibit large logs $M^2 = (p_t + p_{\bar{t}})^2$

$$\frac{d\sigma}{dM} = \sum_{ij} \tau \int_{\tau}^1 d\tau C_{ij}(M, z) F_{ij}(\tau/z) \quad F_{ij}(y) = \int \frac{dx}{x} f_{i/p}(x) f_{j/p}(x/y)$$

$$C_{ij}(M, z) \propto \alpha_s \left(\frac{\ln(1-z)}{1-z} \right)_+ , \alpha_s \left(\frac{1}{1-z} \right)_+ \ln \left(\frac{M^2}{\mu_f^2} \right) \quad z = \frac{M^2}{\hat{s}}$$

- associated with soft-collinear radiation in threshold region
- fixed NLO, NLL resummation differ by ~5%
resummation reduces scale uncertainty
- relevant to Drell-Yan, Higgs, heavy particle production

- kinematics in threshold region



- soft radiation sees light-like (time-like) Wilson-line sources due to energetic (heavy) particles

- Factorization Theorem

$$\sigma(pp \rightarrow t\bar{t}X) = \tau H(M, \mu_f) \int_{\tau}^1 \frac{dz}{z} S(M(1-z), \mu_f) F(\tau/z, \mu_f)$$

- Parton densities (SCET collinear modes)

$$F(x, \mu_f) = \int_y^1 \frac{dy}{y} f_{g/P}(y, \mu_f) f_{g/p}(x/y, \mu_f)$$

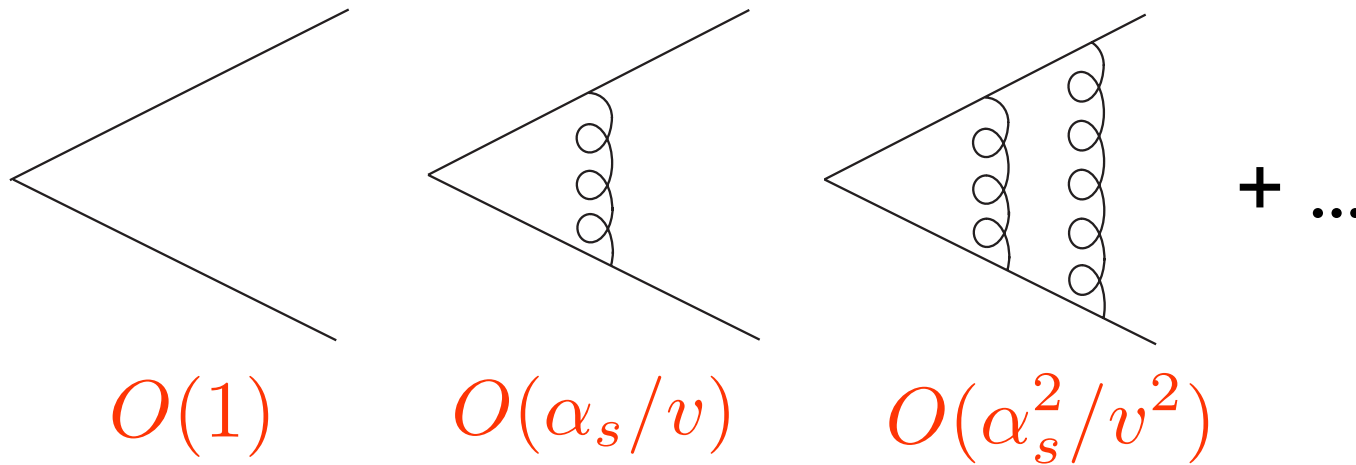
- Soft function (SCET soft modes) $S(M(1-z), \mu_f)$

- Hard function (SCET matching coefficient)

SCET RGE's for $S(M(1-z), \mu_f)$ $H(M, \mu_f)$ $F(x, \mu_f)$

resum large logarithms

- v-enhanced corrections in threshold region



- leading contribution comes from Coulomb gluons

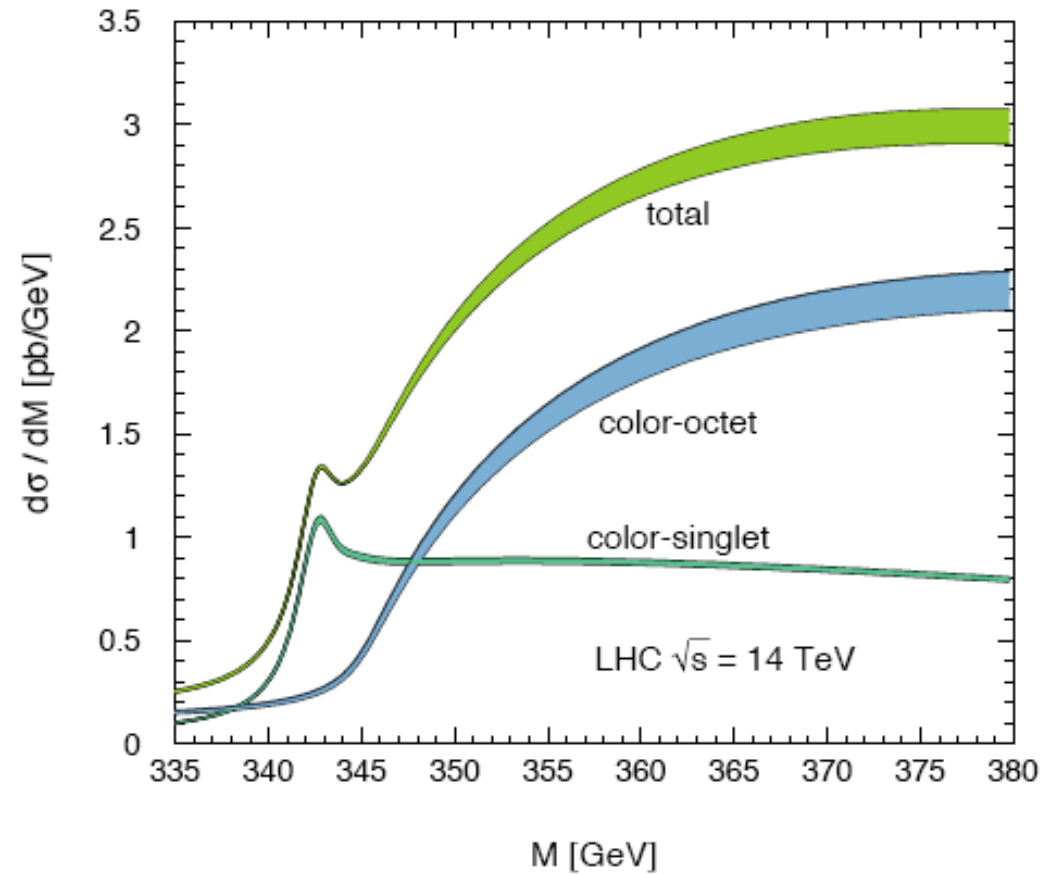
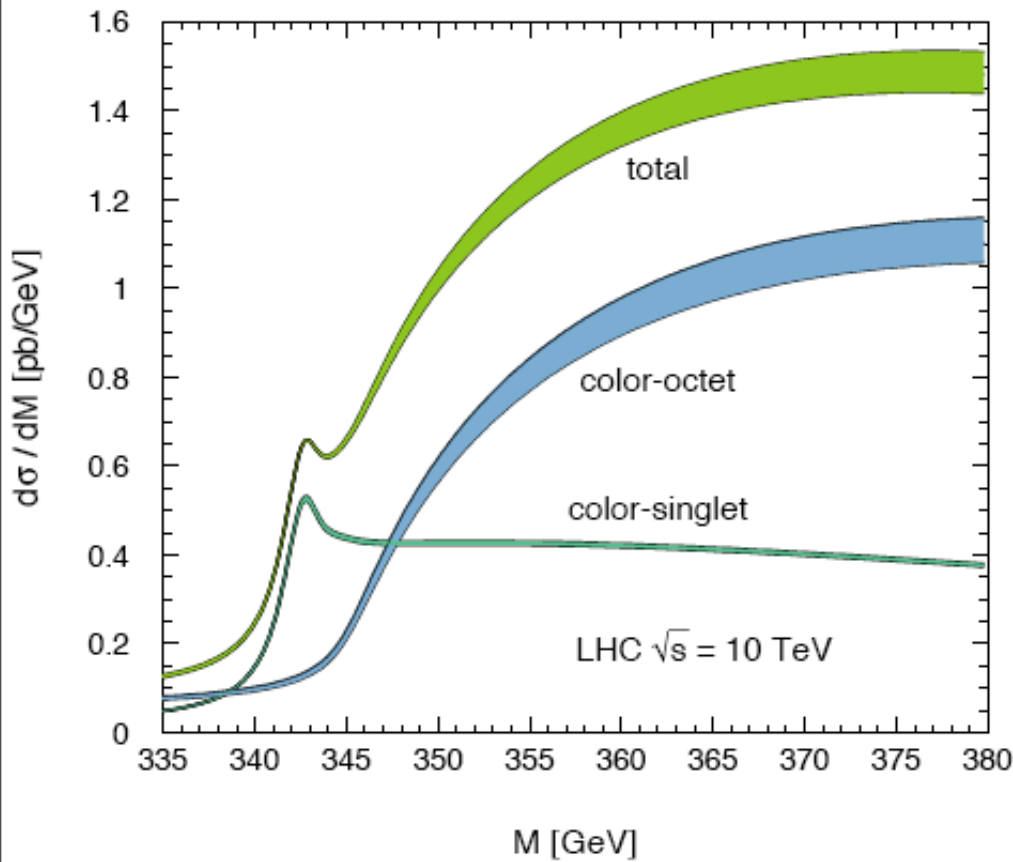
when $v \sim \alpha_s$ sum to all orders using Schroedinger Eq.

$$\left| \begin{array}{c} \text{Diagram with two vertical lines and a triangle containing gluon lines} \end{array} \right|^2 \propto \text{Im } G^{(1,8)}(\vec{0}; M + i\Gamma_t)$$

$$\left\{ 2m_t + \left[\frac{(-i\nabla)^2}{m_t} + V_C^{[1,8]}(\vec{r}) \right] - (M + i\Gamma_t) \right\} G^{[1,8]}(\vec{r}; M + i\Gamma_t) = \delta^{(3)}(\vec{r})$$

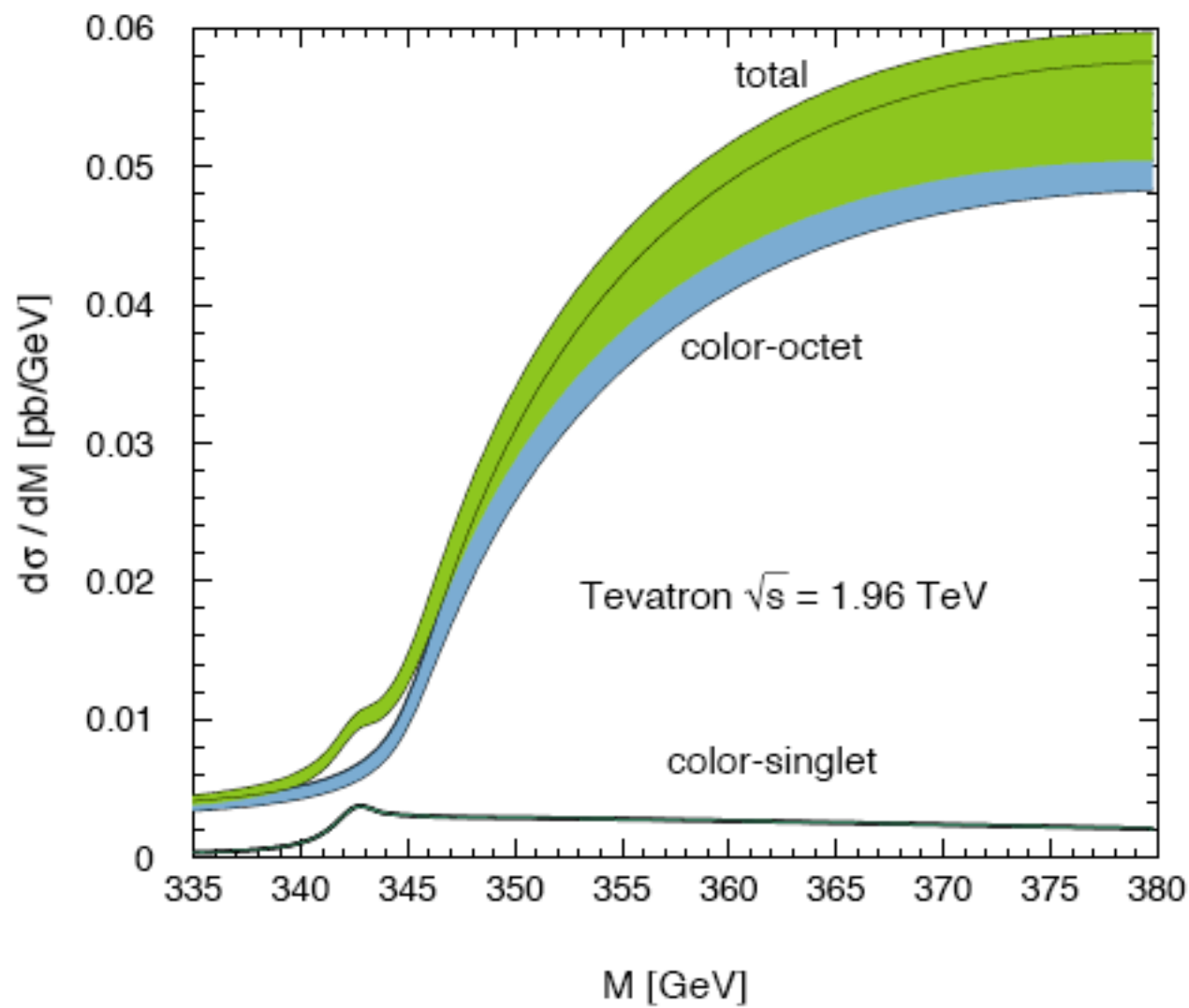
- including all threshold effects

(Y. Kiyo, et. al., Eur. Phys. J. C60:375 (2009))

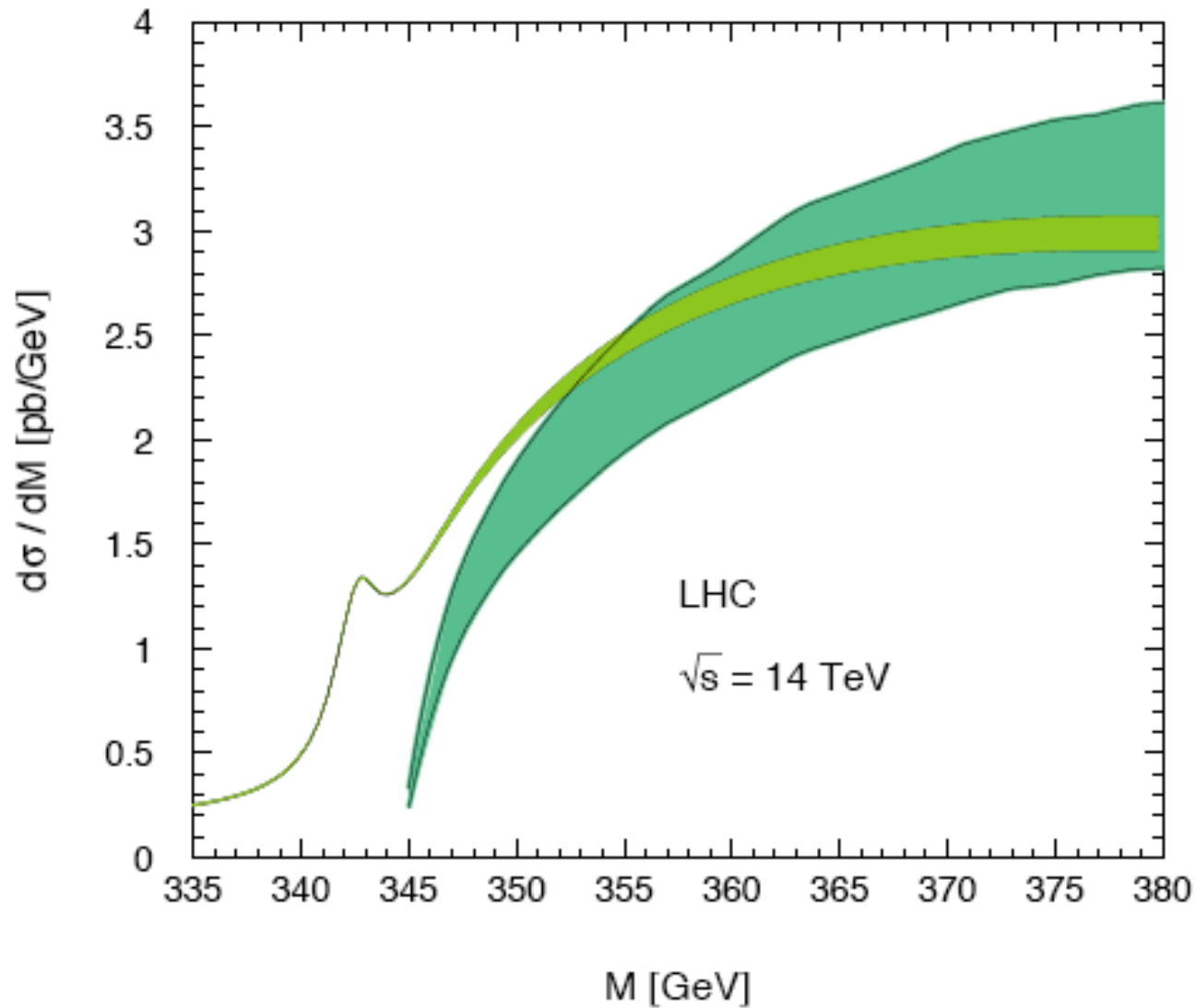


- Strong Coulombic attraction gives visible bump below threshold in color-singlet channel!

- contrast with $d\sigma/dM$ at Tevatron



- comparison w/ fixed order calculation



- bound state corrections large when $340 \text{ GeV} < M < 360 \text{ GeV}$

- interesting to consider relativistic corrections $0 < v^2 < 0.1$

fact. theorem: $\sigma(tt̄) = \sigma^{\text{resum}}(tt̄) \times \text{Im } G^C$ leading term as $v \rightarrow 0$

Top Quark Mass

- current measurements of “ m_t^{pole} ” combine:
 - tree-level matrix elements
 - parton showers
 - hadronization modelsfit to invariant mass of decay products (jets and leptons)
errors 1-2 GeV (CDF, ATLAS, CMS)

- **Ambiguities**

- color recombination with other particles in final state
 - renormalon pole ambiguity in definition of m_t^{pole}

- Prefer observable computed in terms of short-distance quantities

$$O^{\text{phys}}(\alpha_s(\bar{m}_t), \bar{m}_t(\bar{m}_t), \dots)$$

where $\bar{m}_t(\mu_r)$ is MS or other short distance mass

$$O^{\text{phys}} : d\sigma/dM_{t\bar{t}}, \langle M_{t\bar{t}} \rangle, \dots?$$

Threshold Resummation for New Physics

$\sigma(gg \rightarrow S^A)$ color-octet scalars in Manohar-Wise model

A. Idilbi, C. Kim, & T.M., arXiv:0903.3668[hep-ph]

$\sigma(\tilde{g}\tilde{g}), \sigma(\tilde{q}\tilde{q})$ in SUSY

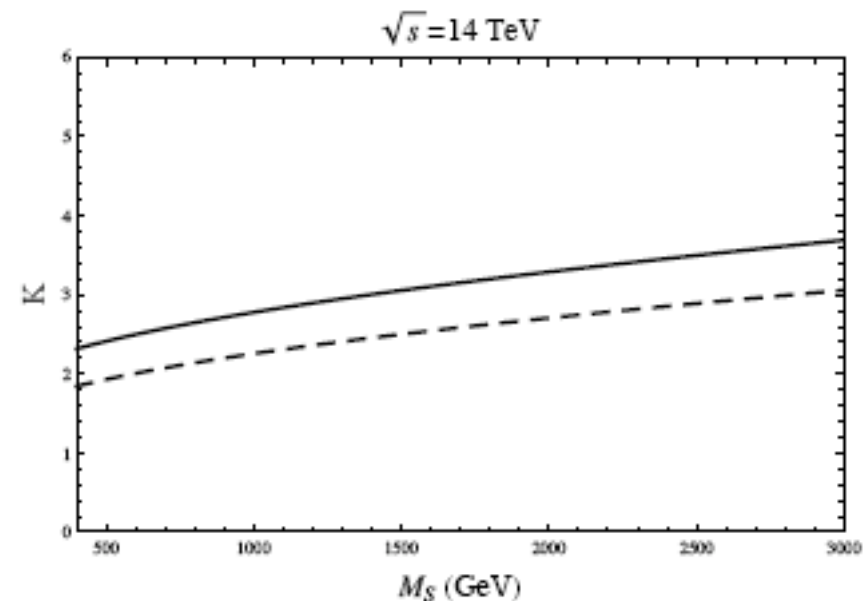
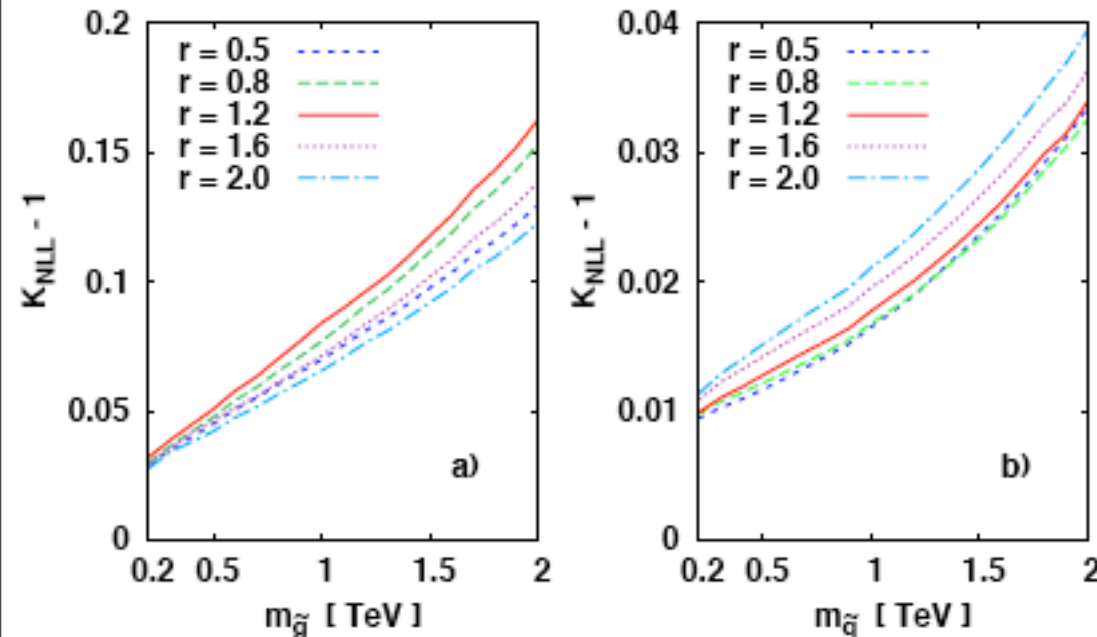
A. Kulesza and L. Motyka, arXiv:0807.2405[hep-ph]

U. Langenfeld and S.O. Moch, arXiv:0901.0802[hep-ph]

- more important as masses get bigger!

$\sigma(\tilde{g}\tilde{g}), \sigma(\tilde{q}\tilde{q})$

$\sigma(gg \rightarrow S^A)$



- bound state effects have not been considered!

Conclusion

- J/ψ photoproduction, $e^+e^- \rightarrow J/\psi + X$

large logs, nonperturbative effects near kinematic endpoints

qualitatively change expectations from fixed order CO calc.

analysis resumed CO + NLO color singlet needed!

most recent analysis of Belle data ignores $e^+e^- \rightarrow c\bar{c}({}^3S_1^{(8)}) + g$!

(B. Gong + J.-X. Wang, arXiv:0904.1103[hep-ph])

Expectation: smaller values for COME relative to LO Tevatron fits

- $t\bar{t}$ production

resummation threshold effects, esp. Coulomb corrections to $d\sigma/dM$

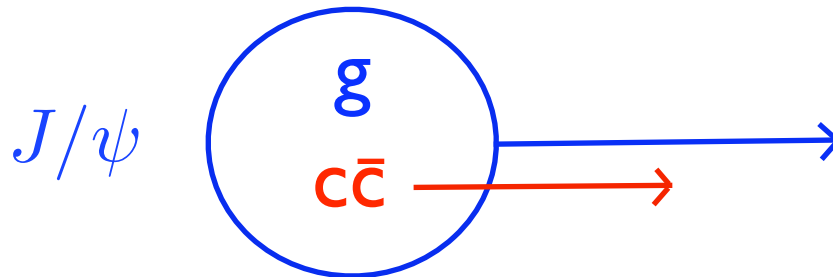
applications to new physics

Extra Slides

- Kinematics

$$n^\mu = (1, 0, 0, 1) \quad \bar{n}^\mu = (1, 0, 0, -1)$$

$$p_\psi^\mu = M_\psi v^\mu \quad v^\mu = \frac{M_\psi}{x\sqrt{s}} \frac{n^\mu}{2} + \frac{x\sqrt{s}}{M_\psi} \frac{\bar{n}^\mu}{2} \quad p_{c\bar{c}}^\mu = 2m_c v^\mu + \ell^\mu \quad \ell^\mu - \text{residual momentum}$$



$$\bar{n} \cdot \ell \sim \frac{M_\psi}{x\sqrt{s}} \Lambda_{QCD} \quad n \cdot \ell \sim \frac{x\sqrt{s}}{M_\psi} \Lambda_{QCD} \quad \ell_\perp^\mu \sim \Lambda_{QCD}$$

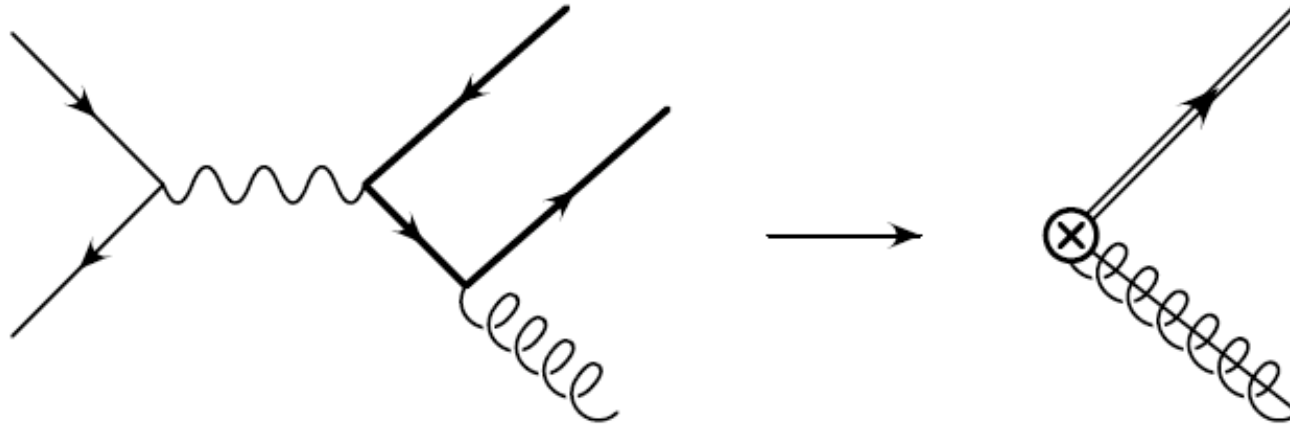
$$p_X^\mu = \frac{\sqrt{s}}{2} \left(1 - \frac{r}{\hat{x}}\right) n^\mu + \frac{\sqrt{s}}{2} (1 - \hat{x}) \bar{n}^\mu - \ell^\mu \quad r = \frac{M^2}{s} \quad \hat{x} = \frac{M}{M_\psi} x \quad M = 2m_c$$

- When $1 - \hat{x} \sim \Lambda_{QCD}/M$ cannot neglect $n \cdot \ell$!

- $1 - \hat{x} \sim \Lambda_{QCD}/M \longrightarrow p_\psi \approx 3 \text{ GeV} \quad (p_\psi)_{\max} \approx 4.8 \text{ GeV}$

Factorization for $e^+e^- \rightarrow J/\psi + X$ in SCET

- Matching current ($^1S_0^{(8)}$)



+ crossed diagram

$$J_\mu = \Gamma_{\alpha\mu}^8(-n \cdot v \bar{\mathcal{P}}, \mu) \psi_{-\mathbf{p}}^\dagger B_\perp^\alpha \chi_{\mathbf{p}}$$

- Collinear: $B_\perp^\alpha = \frac{1}{g_s} W^\dagger (\mathcal{P}_\perp^\alpha + g_s A_{n,q}^\alpha) W$ USoft: ψ_p^\dagger, χ_p

- Reparametrization Invariance: $-n \cdot v \bar{\mathcal{P}}$ (Manohar, T.M., Pirjol, Stewart)

- Decoupling usoft fields from collinear fields

$$A_{n,q}^\mu \rightarrow Y_n A_{n,q}^{(0)} Y_n^\dagger \quad B_\perp^\alpha \rightarrow Y_n B_\perp^{(0)\alpha} Y_n^\dagger$$

$$in \cdot D_{us} \rightarrow in \cdot \partial$$

- Factorization:

$$2E_\psi \frac{d\sigma}{d^3p_\psi} \propto L^{\mu\nu} \int d^4y e^{-iq \cdot y} \sum_X \langle 0 | J_\nu^\dagger(y) | J/\psi + X \rangle \langle J/\psi + X | J_\mu(0) | 0 \rangle$$

$$\langle J/\psi + X | J_\mu | 0 \rangle = 2\Gamma_{\alpha\mu}^8(s(1-r)/M, \mu) \langle J/\psi + X_{us} | \psi_{-p}^\dagger Y T^a Y^\dagger \chi_p | 0 \rangle \langle X_c | \text{Tr}[T^a B_\perp^{(0)\alpha}] | 0 \rangle$$

$$\frac{d\sigma}{dx} = \sigma(\mu) \int dl^+ S(l^+) J(\sqrt{s}(1-\hat{x}) - l^+)$$

$$J(k^+) \propto \text{Im} \left[i \int d^4y e^{ik^+ y^- / 2} \langle 0 | T \left(\text{Tr} \left[T^B B_\perp^{(0)\beta}(y) \right] \text{Tr} \left[T^B B_\perp^{(0)\beta}(0) \right] \right) | 0 \rangle \right]$$

$$S(l^+) = \frac{\langle 0 | \chi_{-p}^\dagger Y_n^\dagger T^B Y_n \psi_p a_\psi^\dagger a_\psi \delta(l^+ - in \cdot \partial) \psi_p^\dagger Y_n^\dagger T^B Y_n^\dagger \chi_{-p} | 0 \rangle}{4m_c \langle \mathcal{O}_8(^1S_0) \rangle}$$

- $J(\ell^+) : p_X^2 = s(1 - M^2/s)(1 - x) \sim Q\Lambda_{\text{QCD}}$ perturbative



Lowest order in perturbation theory: $J(\ell^+) \propto \delta(\ell^+)$

$$\frac{d\sigma}{dx} = \sigma(\mu) \int d\ell^+ S(\ell^+) J(\sqrt{s}(1 - \hat{x}) - \ell^+)$$

$$\rightarrow \sigma_0 S(\sqrt{s}(1 - \hat{x}))$$

- **Far from endpoint** $1 - \hat{x} > v^2$ $in \cdot \partial \sim \frac{\sqrt{s}}{M} Mv^2$

$$S(\ell^+) = \frac{\langle 0 | \chi_{-\mathbf{p}}^\dagger Y_n^\dagger T^B Y_n \psi_{\mathbf{p}} a_\psi^\dagger a_\psi \delta(\sqrt{s}(1 - \hat{x}) - in \cdot \partial) \psi_{\mathbf{p}}^\dagger Y_n T^B Y_n^\dagger \chi_{-\mathbf{p}} | 0 \rangle}{4m_c \langle \mathcal{O}_8(^1S_0) \rangle}$$

$$\rightarrow \delta(1 - \hat{x})$$

$$\frac{d\sigma}{dx} = \sigma_0 \delta(1 - \hat{x})$$

- Recover LO NRQCD differential cross section

- Usoft Wilson Lines in Color-Octet Operators

$$\langle \mathcal{O}_8(^1S_0) \rangle = \frac{\langle 0 | \chi_{-\mathbf{p}}^\dagger Y_n^\dagger T^B Y_n \psi_{\mathbf{p}} a_\psi^\dagger a_\psi \psi_{\mathbf{p}}^\dagger Y_n^\dagger T^B Y_n \chi_{-\mathbf{p}} | 0 \rangle}{4m_c}$$

- required in pQCD analysis for factorization

(Nayak, Sterman, Qiu)

analyze gluon fragmentation function

$$D_{H/i}(z, m_c, \mu) = \sum_n d_{i \rightarrow c\bar{c}[n]}(z, \mu, m_c) \langle \mathcal{O}_n^H \rangle$$

at two loops, find IR divergent matching coefficients unless Wilson lines are included in the color-octet operators

- appear automatically in SCET formalism

- Resummation

Moments $\sigma_N = \int dx x^N \frac{d\sigma}{dx}$ $\sigma_N = \sigma_\mu J_N S_N$

$$\frac{\ln(1-x)}{1-x} \rightarrow \frac{1}{2} \ln^2 \bar{N} \quad \frac{1}{1-x} \rightarrow -\ln \bar{N} \quad \bar{N} = N e^{\gamma_E}$$

- RGE's from SCET

$$\mu \frac{d}{d\mu} J_N(\mu) = \left[\frac{2C_A \alpha_s}{\pi} \log \left(\frac{\mu^2 \bar{N}}{s(1-r)} \right) + \frac{2\alpha_s}{\pi} \left(\frac{11}{12} C_A - \frac{n_f}{6} \right) \right] J_N(\mu)$$

$$\mu \frac{d}{d\mu} S_N(\mu) = \left[-\frac{2C_A \alpha_s}{\pi} \log \left(\frac{\mu \bar{N}}{M} \right) + \frac{\alpha_s C_A}{\pi} \right] S_N(\mu)$$

- Resummed moments

$$\sigma_N = \sigma_0 S_N e^{\log(N) g_1(\chi) + g_2(\chi)} \quad \chi = \log(N) \alpha_s(\mu_H) \beta_0 / 4\pi$$