

# **Testing neutrino mass generation mechanisms from the lepton flavor violating decay of the Higgs boson**

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**Mayumi AOKI (Kanazawa U.)**

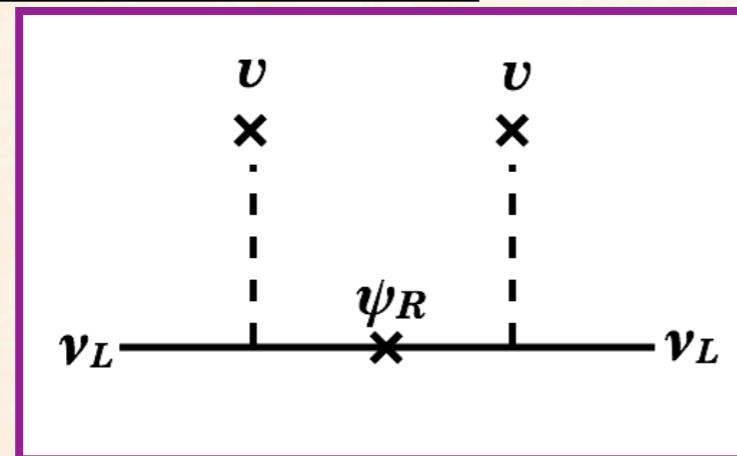
**S. Kanemura, K. Sakurai, H. Sugiyama (U. of Toyama)  
Phys.Lett. B763 (2016) 352**

# Introduction

- Neutrino mass scale is much smaller than the  $q$  and  $\ell$  masses.  
 $m_\nu \sim 0.1 \text{ eV} \ll m_q, m_\ell$
- The origin of the neutrino mass might be different from that of  $q$  and  $\ell$ .

## Seesaw Mechanism

Type-I



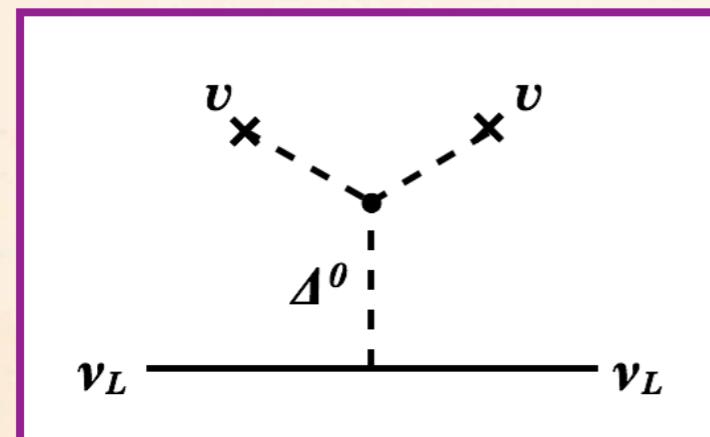
$\psi_R$  : Right-handed neutrino

$$m_\nu \simeq \frac{v^2 y^2}{2M}$$

- $y \sim \mathcal{O}(1)$ ,  $M \sim 10^{14} \text{ GeV}$
- $y \sim y_e$ ,  $M \sim 100 \text{ GeV}$

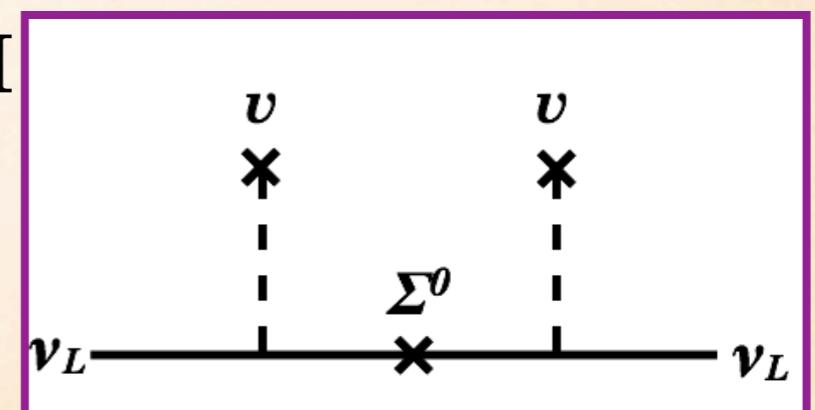
Far from experimental reach

Type-II



$\Delta$ : SU(2) triplet scalar

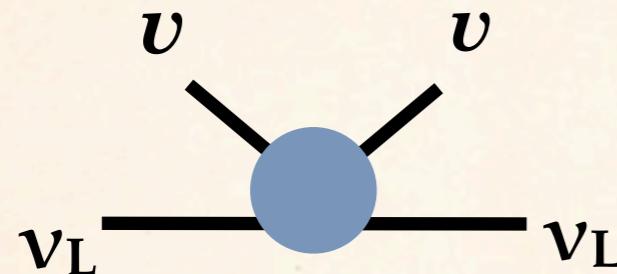
Type-III



$\Sigma$ : SU(2) triplet fermion

# Introduction

## Radiative Seesaw Mechanism



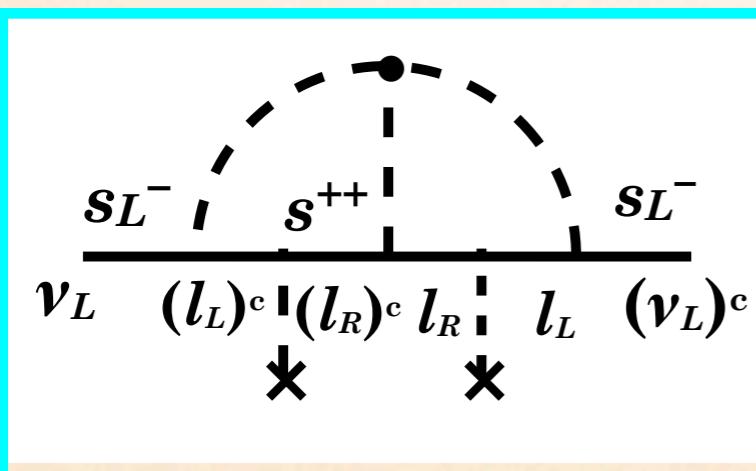
$$\text{N-loop: } m_\nu^{ij} = \left( \frac{1}{16\pi^2} \right)^N \frac{f_{ij}}{\Lambda} \langle \phi^0 \rangle^2$$

- Neutrino masses are generated via the radiative effect.
- Due to the loop suppression factor, the neutrino masses would be explained in a natural way by the TeV-scale dynamics with the unsuppressed couplings.

## e.g.) 2-loop model

### Zee-Babu model

Zee (1986); Babu (1988)



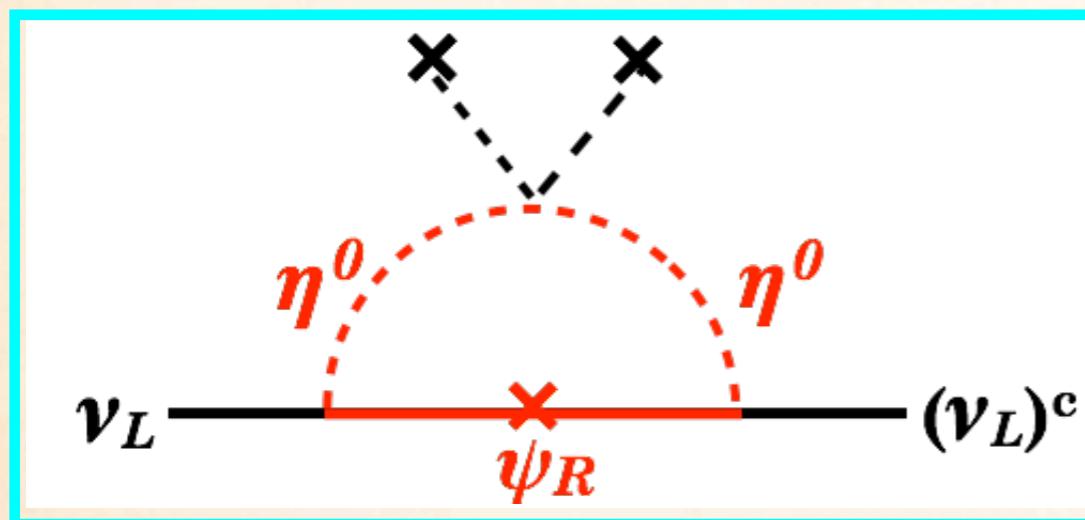
- New particles:  $s_L^-$ ,  $s^{++}$
- $f \sim O(1)$ ,  $M \sim 10^3 \text{ GeV}$

# Introduction

## Model with dark matter particle

e.g.) Ma model

Ma (2006)



- $Z_2$  symmetry is introduced.
- New particles:  $Z_2$  odd  $\psi_R$ ,  $\eta$

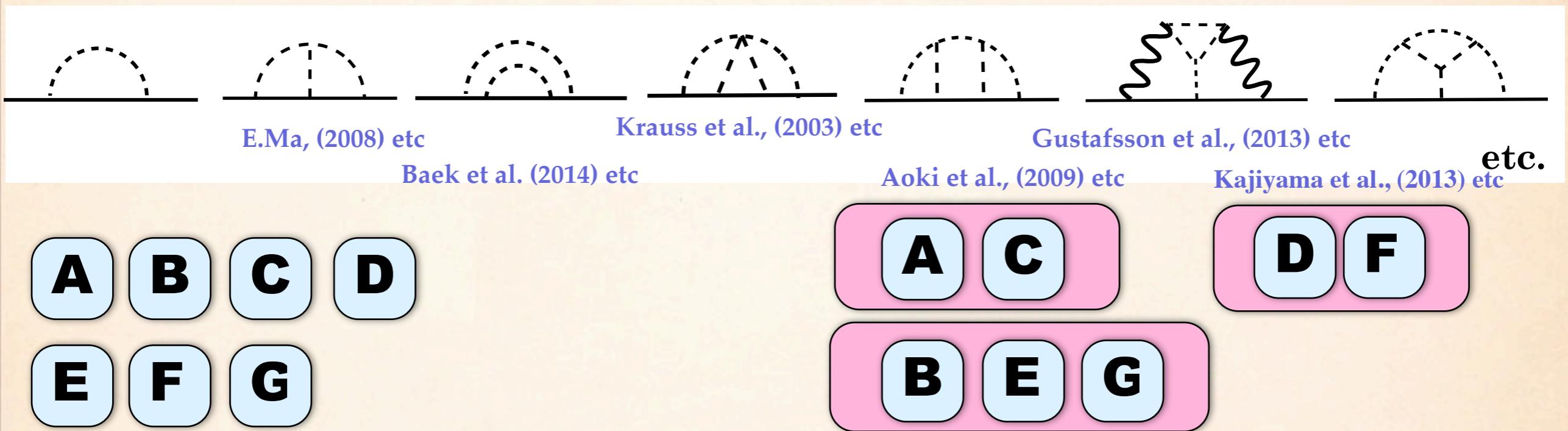
$\eta$ : Inert doublet scalar

$$\eta = \begin{pmatrix} \eta^+ \\ (\eta_R^0 + i\eta_I^0)/\sqrt{2} \end{pmatrix}, \quad \langle \eta \rangle = 0$$

- The  $Z_2$  symmetry forbids the Dirac  $\nu$  mass term and guarantees the stability of DM.
- DM candidates :  $\psi_R$ ,  $\eta^0_R$ ,  $\eta^0_I$
- The framework would explain the neutrino mass and the DM.

# Introduction

## Many variety of radiative seesaw models



- Classification of models into several groups by some common features enables us to test neutrino mass generation mechanisms.

### Our work

- The models are classified by focusing on the combinations of new Yukawa coupling.
- The mechanisms are tested by LFV phenomena.  
**charged LFV, LFV decays of the Higgs boson**

# Introduction

- LFV decays of the Higgs boson  $h \rightarrow ll'$

$$\text{BR}(h \rightarrow ll') \equiv \text{BR}(h \rightarrow l\bar{l}') + \text{BR}(h \rightarrow \bar{l}l')$$

**BR( $h \rightarrow \mu\tau$ )**

CMS 8TeV

$< 1.51 \%$

Best Fit

$0.84^{+0.39}_{-0.37} \%$  **2.4 $\sigma$  excess**

13TeV

$< 1.20 \%$

$-0.76^{+0.81}_{-0.84} \%$  **No excess observed**

ATLAS 8TeV

$< 1.43 \%$

$0.53^{+0.51}_{-0.51} \%$

Future colliders  $\rightarrow O(0.01) \%$

[Han and Marfatia \(2001\)](#), [Kanemura et.al. \(2004\)](#)

**BR( $h \rightarrow e\mu$ )**

CMS 8TeV  $< 3.5 \times 10^{-2} \%$

**BR( $h \rightarrow e\tau$ )**

CMS 8TeV  $< 6.9 \times 10^{-1} \%$

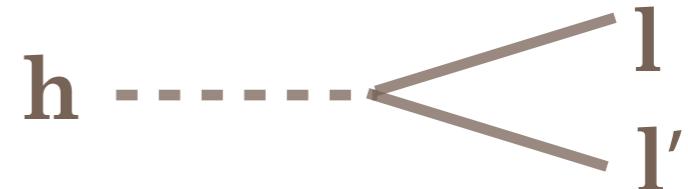
- We discuss impact of future discoveries of  $h \rightarrow ll'$  on the mechanisms to generate neutrino masses.

# Introduction

$$h \rightarrow ll'$$

- Tree-level LFV

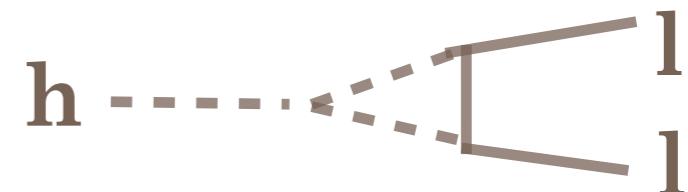
e.g) Type III two Higgs doublet model  $\mathcal{L}_Y = y_{ij}^1 \bar{\psi}_i \psi_j \Phi_1 - y_{ij}^2 \bar{\psi}_i \psi_j \Phi_2$



We consider the FCNC interactions at the tree level are absent.

(by imposing the softly-broken  $Z_2$  symmetry)

- Loop-level LFV



Model with new Yukawa interaction between new scalar and lepton.

Dimension- 4 and -6 operators

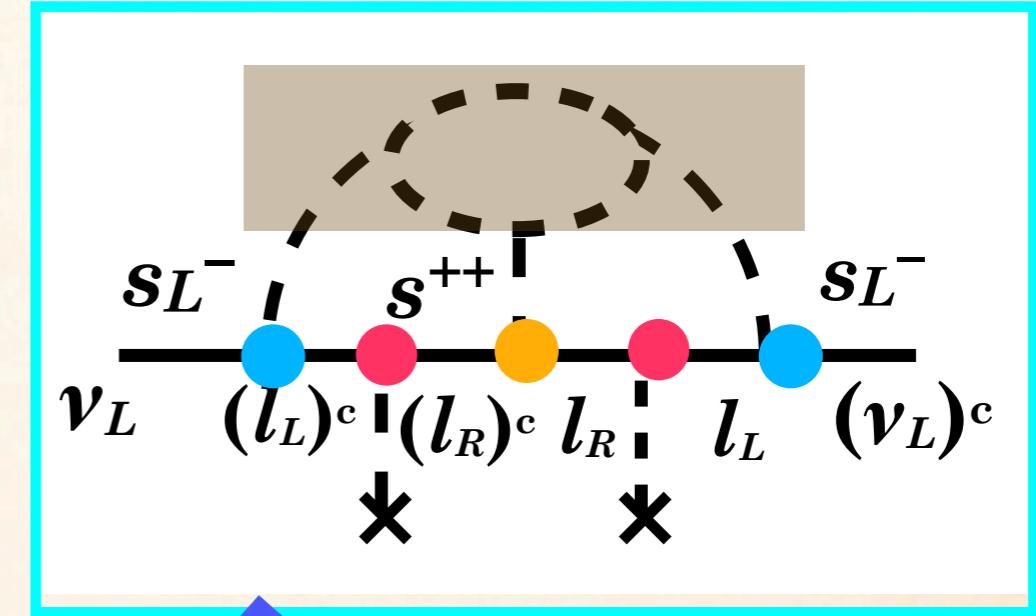
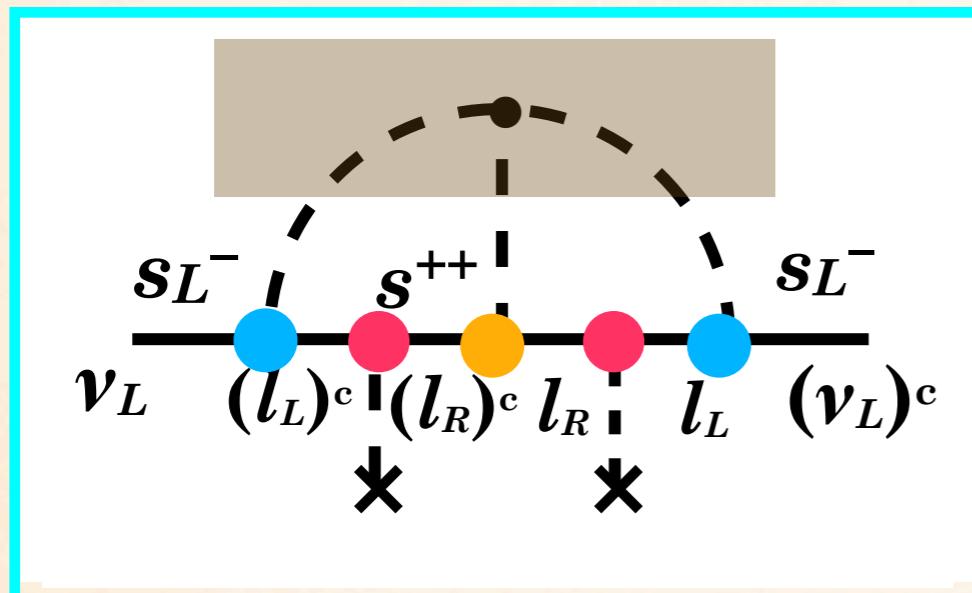
$$\begin{aligned}\mathcal{L} &= Y [\bar{L} \Phi \ell'_R] + \frac{Y_6}{\Lambda^2} [\bar{L} \Phi \ell'_R (\Phi^\dagger \Phi)] \\ &\rightarrow \left( \frac{v}{\sqrt{2}} Y + \frac{v^3}{2\Lambda^2} Y_6 \right) [\ell_L \ell'_R] + \left( \frac{1}{\sqrt{2}} Y + \boxed{3} \frac{v^2}{2\Lambda^2} Y_6 \right) [\ell_L \ell'_R h]\end{aligned}$$

Misalignment

1. Introduction
2. Classification of models
3.  $h \rightarrow ll'$
4. Summary

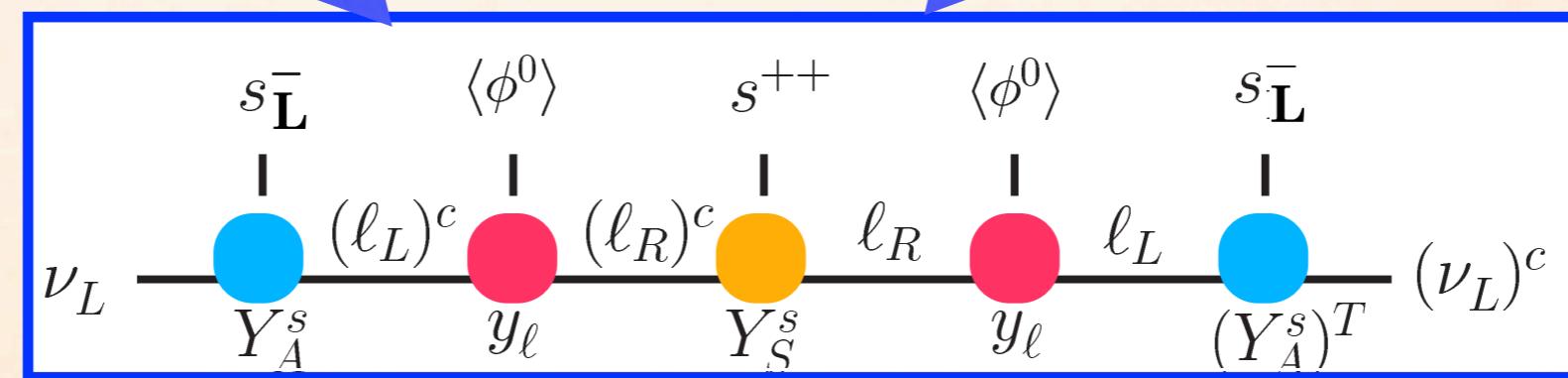
# Classification of Models

- We classify the models by focusing only on the combinations of Yukawa coupling matrices.



“Mechanism”

M1



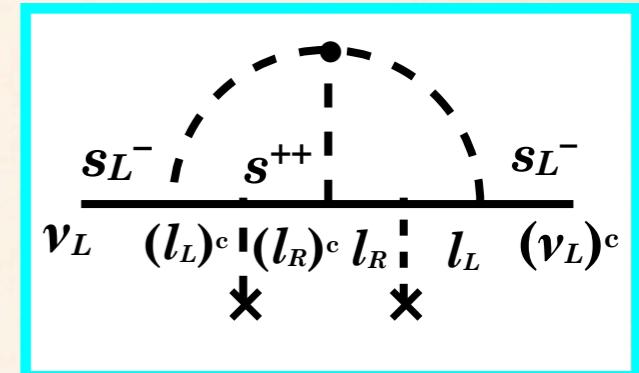
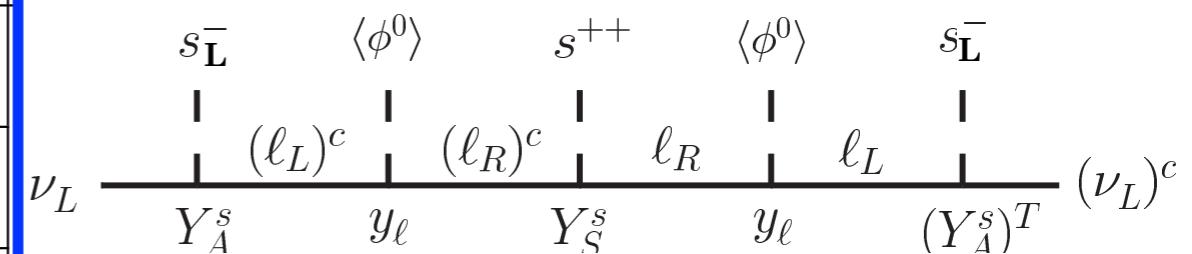
# Majorana Neutrino

Kanemura, Sugiyama (2016)

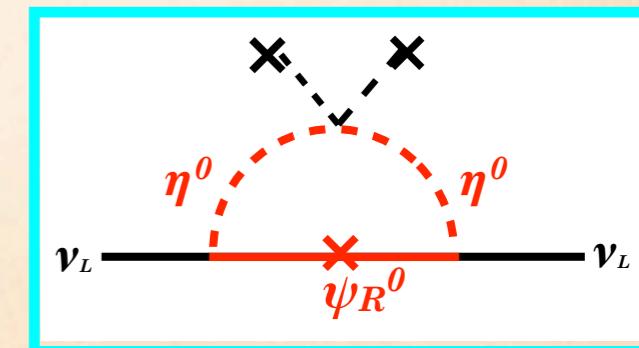
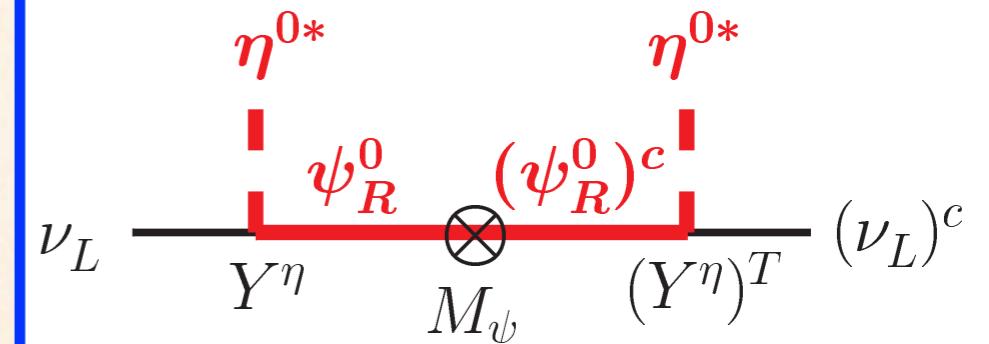
Scalar with leptonic Yukawa int.

	$s_L^+$	$s^{++}$	$\Phi_2$	$\Delta$	$s_2^+$	$\eta$
SU(2) <sub>L</sub>	$\underline{1}$	$\underline{1}$	$\underline{2}$	$\underline{3}$	$\underline{1}$	$\underline{2}$
U(1) <sub>Y</sub>	1	2	1/2	1	1	1/2
Unbroken $Z_2$	+	+	+	+	-	-
M1	✓	✓				
M2		✓	✓			
M3		✓				
M4				✓		
M5	✓				✓	
M6			✓		✓	
M7					✓	
M8						✓

**M1**



**M8**

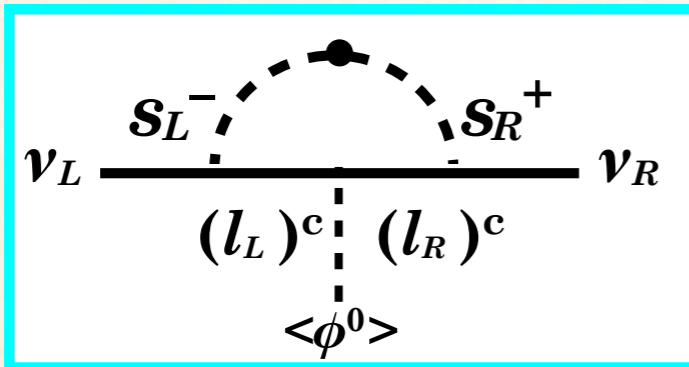


# Classification of Models

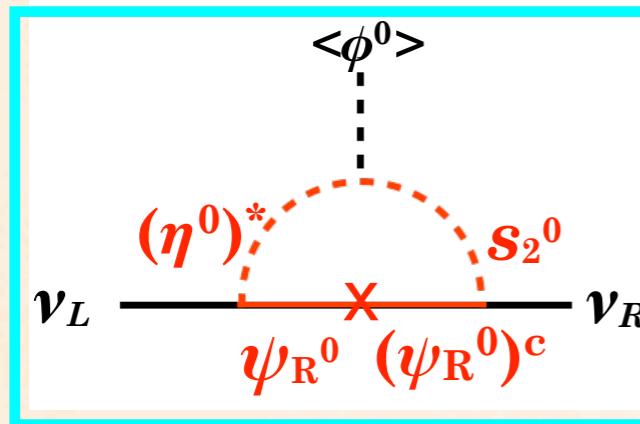
## Dirac Neutrino

- Dirac masses can be generated at the the loop level.

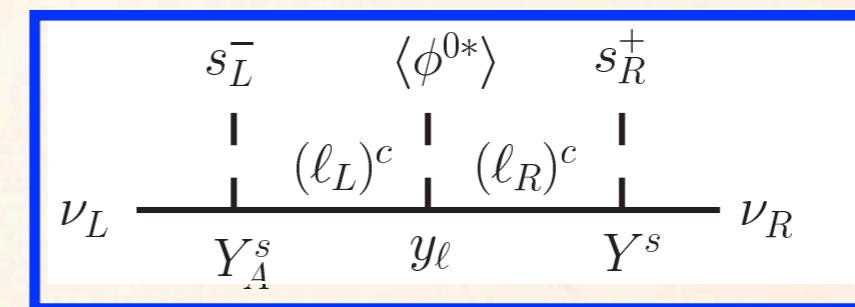
Nasri, Moussa (2002)



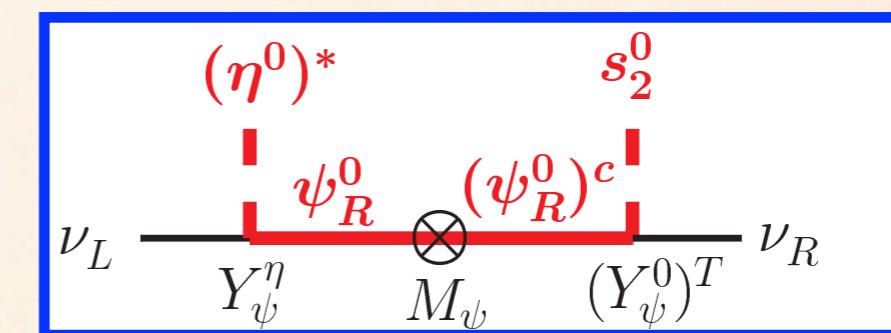
Gu, Sarkar (2008)



D1



D18



- In order to forbid the  $L\Phi\nu_R$ , the softly-broken  $Z_2$  symmetry ( $Z_2'$ ) is introduced.

$\nu_R$  :  $Z_2'$  odd

# Dirac Neutrino

Scalar with leptonic Yukawa int.

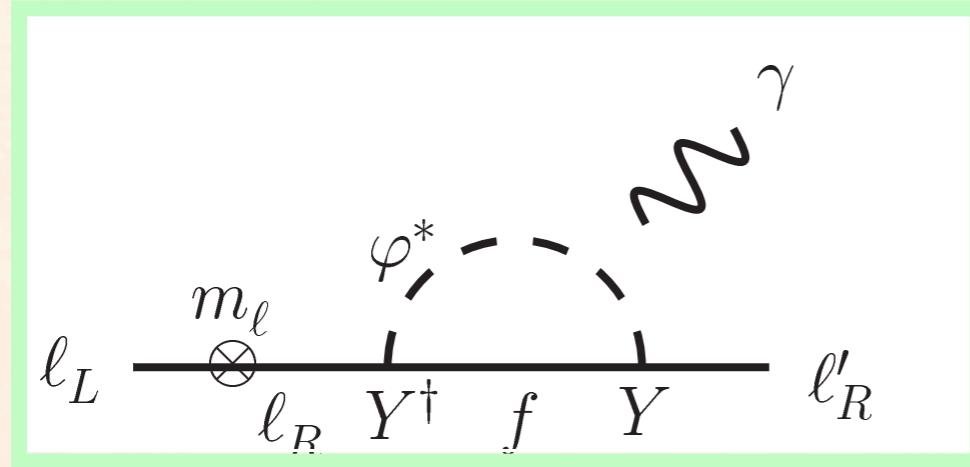
	$s^0$	$s_L^+$	$s_R^+$	$s^{++}$	$\Phi_\nu$	$\Phi_2$	$\Delta$
SU(2) <sub>L</sub>	$\underline{\mathbf{1}}$	$\underline{\mathbf{1}}$	$\underline{\mathbf{1}}$	$\underline{\mathbf{1}}$	$\underline{\mathbf{2}}$	$\underline{\mathbf{2}}$	$\underline{\mathbf{3}}$
U(1) <sub>Y</sub>	0	1	1	2	1/2	1/2	1
Lepton number	-2	-2	-2	-2	0	0	-2
$Z'_2$	+	+	-	+	-	+	+
D1		✓	✓				
D2			✓				✓
D3			✓	✓		✓	
D4			✓	✓			
D5	✓		✓			✓	
D6	✓		✓				
D7					✓		

	$s^0$	$s_L^+$	$s_R^+$	$s^{++}$	$\Phi_\nu$	$\Phi_2$	$\Delta$	$s_2^0$	$s_2^+$	$\eta$
SU(2) <sub>L</sub>	$\underline{\mathbf{1}}$	$\underline{\mathbf{1}}$	$\underline{\mathbf{1}}$	$\underline{\mathbf{1}}$	$\underline{\mathbf{2}}$	$\underline{\mathbf{2}}$	$\underline{\mathbf{3}}$	$\underline{\mathbf{1}}$	$\underline{\mathbf{1}}$	$\underline{\mathbf{2}}$
U(1) <sub>Y</sub>	0	1	1	2	1/2	1/2	1	0	1	1/2
Lepton number	-2	-2	-2	-2	0	0	-2	-1	-1	-1
$Z'_2$	+	+	-	+	-	+	+	-	+	+
D8				✓					✓	✓
D9								✓	✓	✓
D10					✓					✓
D11					✓		✓			✓
D12					✓					✓
D13					✓		✓			✓
D14					✓				✓	
D15						✓		✓	✓	✓
D16									✓	✓
D17					✓				✓	✓
D18								✓		✓

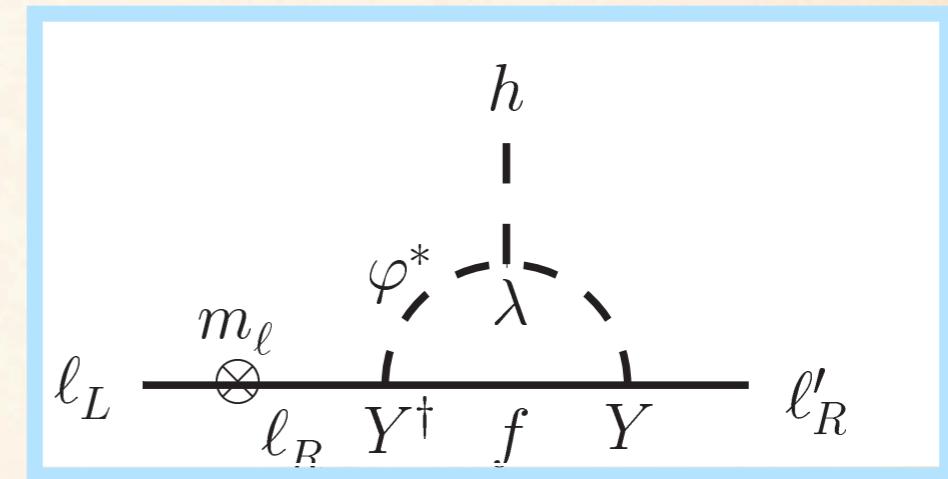
1. Introduction
2. Classification of models
3.  $h \rightarrow ll'$
4. Summary

$$h \rightarrow ll'$$

$$l \rightarrow l'\gamma$$



$$h \rightarrow ll'$$



$$\text{BR}(l \rightarrow l'\gamma) \sim 0.1 \frac{\lambda^2}{(2 - 3Q_\varphi)^2} \text{BR}(h \rightarrow ll')$$

- Under the constraint from the cLFV, the BR of  $h$  LFV decay is too small to be observed if it is radiatively produced.

$$\text{BR}(\mu \rightarrow e\gamma) < 4.2 \times 10^{-13}, \quad \text{BR}(\tau \rightarrow l'\gamma) < 10^{-8}$$

- If  $h$  LFV decay is observed, we might take FCNC at the tree level or take some extension to suppress  $l \rightarrow l'\gamma$  by cancellation.

$$h \rightarrow ll'$$

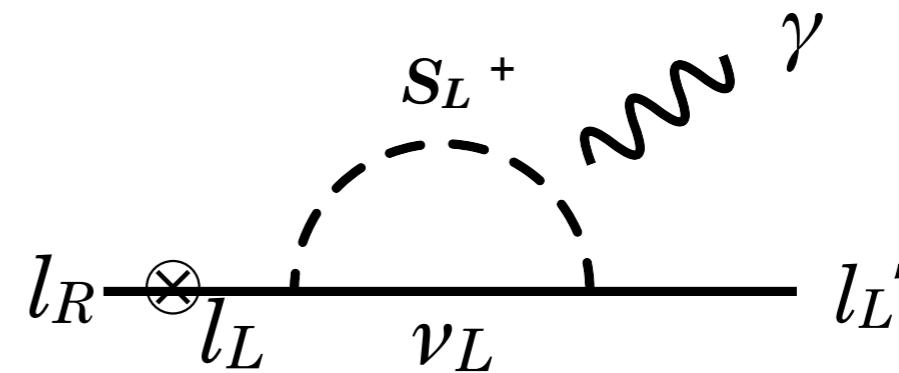
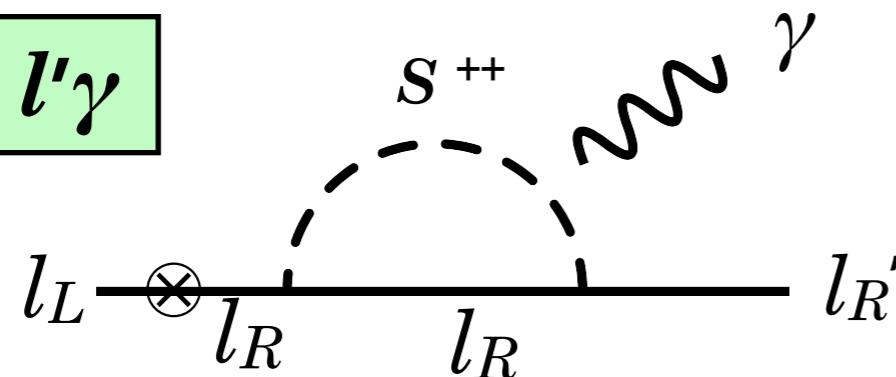
- Each of the Mechanisms has new Yukawa interactions, which can produce both  $l \rightarrow l'\gamma$  and  $h \rightarrow ll'$ .
- 14 Mechanisms will be excluded if  $h \rightarrow ll'$  is observed.
- All other Mechanisms have two kinds of new Yukawa interactions.
- In the Mechanisms-M1, M5, D1, D2, D8, D9 and D10, their effects to  $l \rightarrow l'\gamma$  cannot be cancelled with each other.

**M1**

$$(Y_S^s)_{\ell\ell'} \left[ (\overline{\ell_R})^c \ell'_R s^{++} \right]$$

$$(Y_A^s)_{\ell\ell'} \left[ \overline{L_\ell} \epsilon L_{\ell'}^* s_L^- \right]$$

$l \rightarrow l'\gamma$



Different chiralities of charged leptons

$$h \rightarrow ll'$$

- Some Mechanisms for Dirac neutrino masses can be compatible with the observation of  $h \rightarrow ll'$ .

	$s^0$	$s_L^+$	$s_R^+$	$s^{++}$	$\Phi_\nu$	$\Phi_2$	$\Delta$	$\ell \rightarrow \ell' \gamma$		
	$\ell'_L$	$\ell'_R$								
SU(2) <sub>L</sub>	<b>1</b>	<b>1</b>	<b>1</b>	<b>1</b>	<b>2</b>	<b>2</b>	<b>3</b>			
U(1) <sub>Y</sub>	0	1	1	2	1/2	1/2	1			
Lepton number	-2	-2	-2	-2	0	0	-2			
$Z'_2$	+	+	-	+	-	+	+			
D1		✓	✓					✓	✓	
D2			✓				✓	✓	✓	
D3			✓	✓		✓		✓✓		
D4			✓	✓				✓✓		
D5	✓		✓			✓		✓		
D6	✓		✓					✓		
D7					✓			✓		

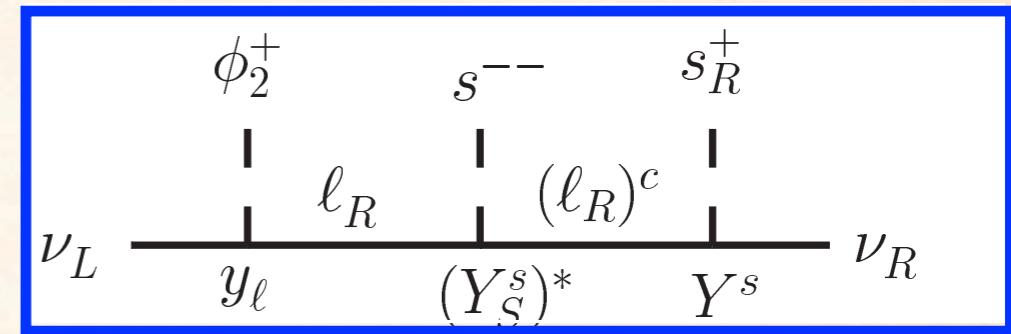
	$s^0$	$s_L^+$	$s_R^+$	$s^{++}$	$\Phi_\nu$	$\Phi_2$	$\Delta$	$s_2^0$	$s_2^+$	$\eta$	$\ell \rightarrow \ell' \gamma$
	$\ell'_L$	$\ell'_R$									
SU(2) <sub>L</sub>	<b>1</b>	<b>1</b>	<b>1</b>	<b>1</b>	<b>2</b>	<b>2</b>	<b>3</b>	<b>1</b>	<b>1</b>	<b>2</b>	
U(1) <sub>Y</sub>	0	1	1	2	1/2	1/2	1	0	1	1/2	
Lepton number	-2	-2	-2	-2	0	0	-2	-1	-1	-1	
$Z'_2$	+	+	-	+	-	+	+	-	+	+	
D8			✓					✓	✓		✓✓
D9								✓	✓	✓	✓✓
D10				✓						✓	✓✓
D11				✓			✓			✓	✓✓
D12				✓						✓	✓✓
D13				✓		✓		✓			✓
D14				✓					✓		✓
D15						✓		✓	✓		✓
D16								✓	✓		✓
D17			✓					✓	✓	✓	✓✓
D18								✓	✓	✓	✓

# $h \rightarrow ll'$

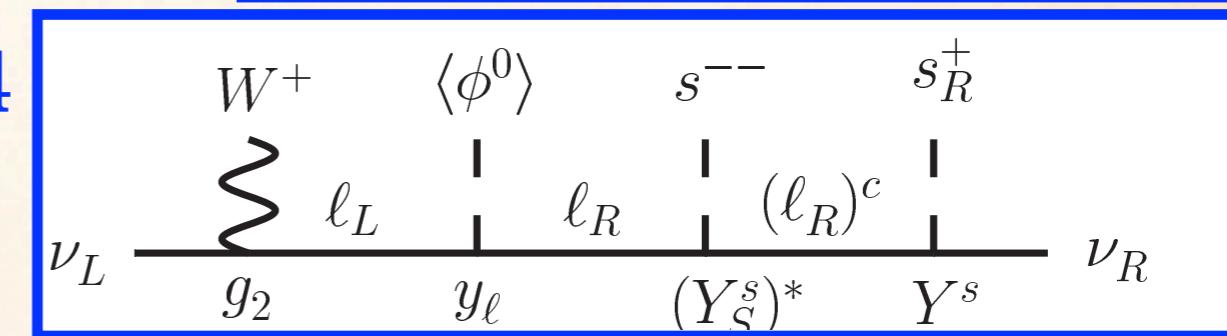
- Some Mechanisms for Dirac neutrino masses can be compatible with the observation of  $h \rightarrow ll'$ .

	$s^0$	$s_L^+$	$s_R^+$	$s^{++}$	$\Phi_\nu$	$\Phi_2$	$\Delta$	$\ell \rightarrow \ell' \gamma$	$\ell'_L$	$\ell'_R$
SU(2) <sub>L</sub>	<b>1</b>	<b>1</b>	<b>1</b>	<b>1</b>	<b>2</b>	<b>2</b>	<b>3</b>			
U(1) <sub>Y</sub>	0	1	1	2	1/2	1/2	1			
Lepton number	-2	-2	-2	-2	0	0	-2			
$Z'_2$	+	+	-	+	-	+	+			
D1		✓	✓						✓	✓
D2			✓				✓		✓	✓
D3			✓	✓		✓			✓✓	
D4			✓	✓					✓✓	
D5	✓		✓			✓				✓
D6	✓		✓							✓
D7					✓				✓	

**D3**



**D4**



- The singlet scalars  $s_R^+$  and  $s^{++}$  interact with  $\ell_R$ .

**$s_R^+$**

$$(Y^s)_{\ell i} \left[ \overline{(\ell_R)^c} \nu_{i R} s_R^+ \right]$$

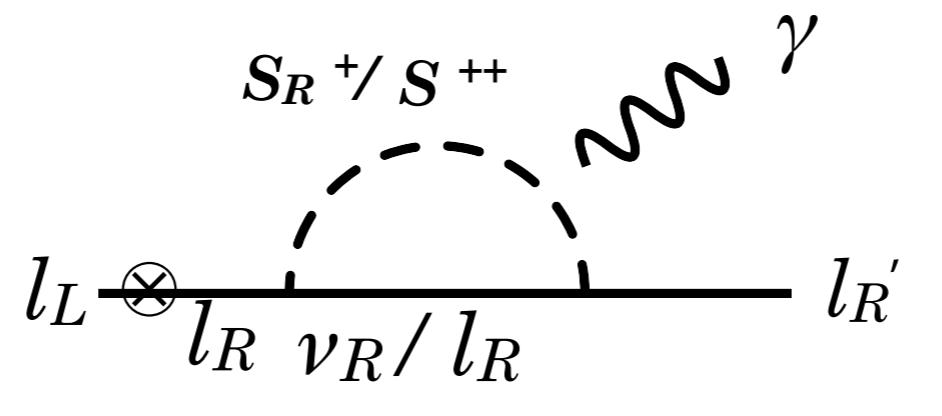
**$s^{++}$**

$$(Y_S^s)_{\ell \ell'} \left[ \overline{(\ell_R)^c} \ell'_{R'} s^{++} \right]$$

$$h \rightarrow ll'$$

D3, D4

$$l \rightarrow l'\gamma$$



- Contributions of these scalars to  $\ell \rightarrow \ell_R \gamma$  can be destructive.

$$\text{BR}(\ell \rightarrow \ell'\gamma) \propto \left| \frac{(Y^{s\dagger} Y^s)_{\ell\ell'}}{m_{s_R^+}^2} + 16 \frac{(Y_S^{s\dagger} Y_S^s)_{\ell\ell'}}{m_{s^{++}}^2} \right|^2 \ll \left| \frac{(Y^{s\dagger} Y^s)_{\ell\ell'}}{m_{s_R^+}^2} \right|^2,$$

- The  $10^{-3}$  tuning of two amplitudes is required for the cancellation to satisfy  $\text{BR}(l \rightarrow l'\gamma) < 10^{-8}$ , since  $\text{BR}(h \rightarrow \mu\tau) \sim 10^{-3}$  naively corresponds to  $\text{BR}(\tau \rightarrow \mu\gamma) \sim 10^{-2}$ .

$$h \rightarrow ll'$$

- The contributions of  $s_R^+$  and  $s^{++}$  to  $h \rightarrow ll'$  can be constructive.

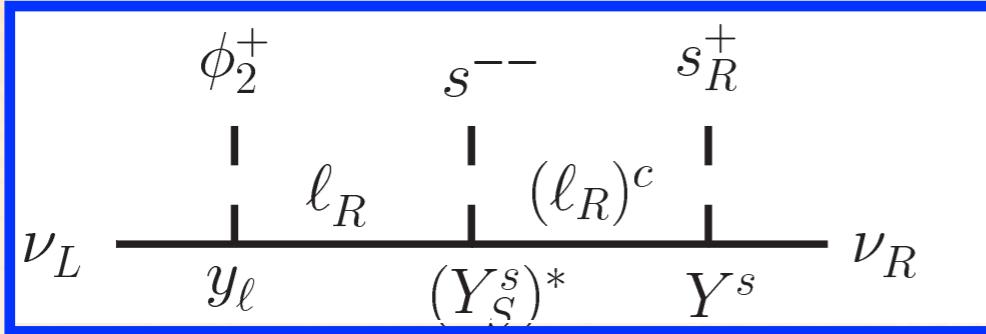
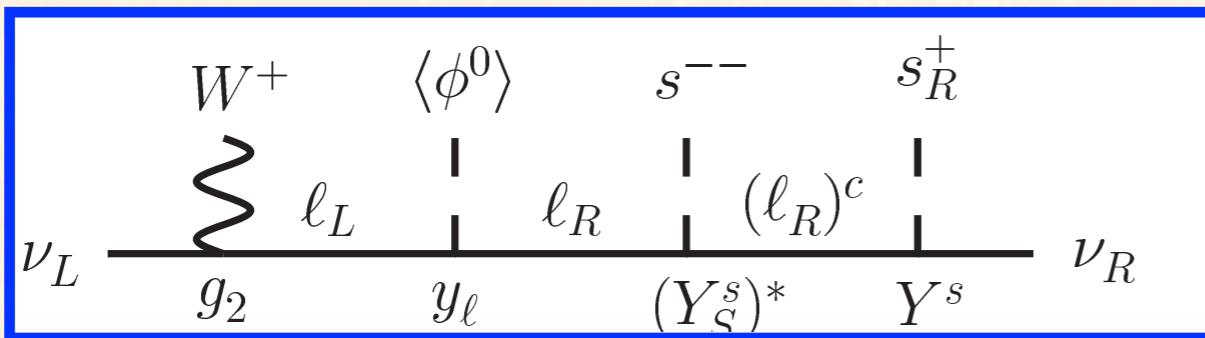
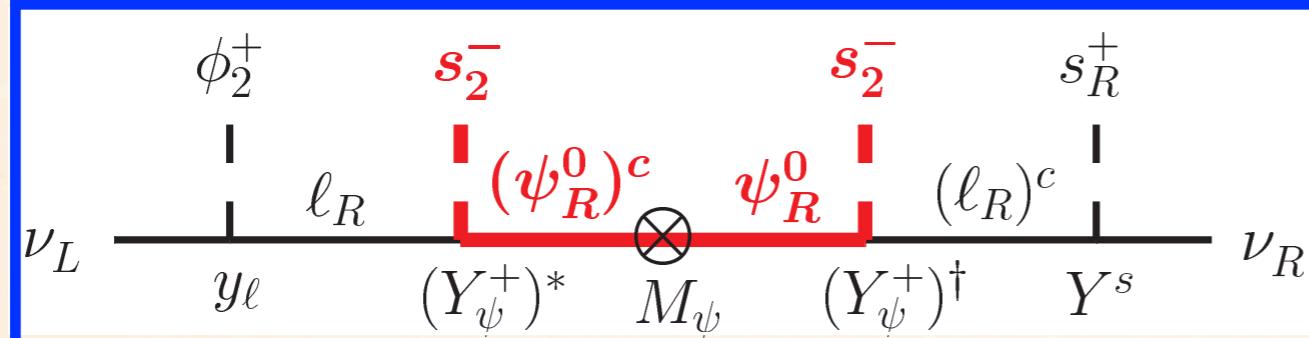
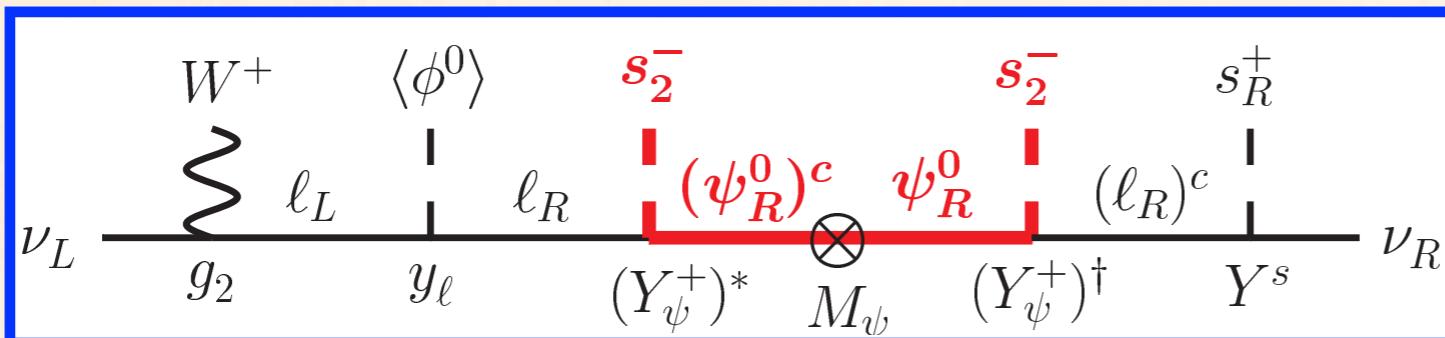
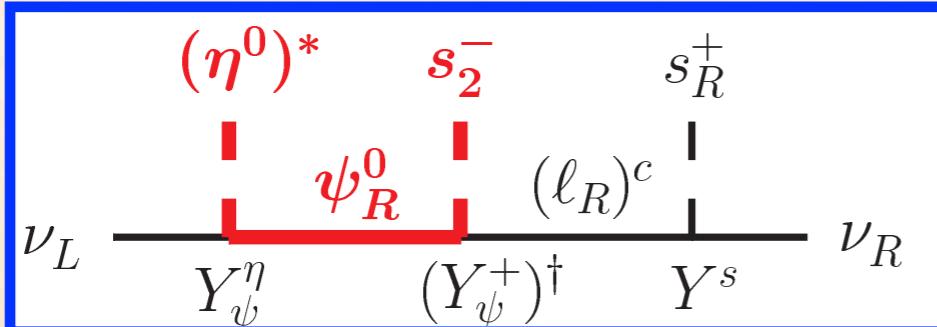
$$h \rightarrow ll'$$

$$\text{BR}(h \rightarrow \ell\ell') \propto \left| \lambda_{hs+} \frac{(Y^{s\dagger} Y^s)_{\ell\ell'}}{m_{s_R^+}^2} + 4\lambda_{hs++} \frac{(Y_S^{s\dagger} Y_S^s)_{\ell\ell'}}{m_{s^{++}}^2} \right|^2 \sim \left| \lambda_{hs+} \frac{(Y^{s\dagger} Y^s)_{\ell\ell'}}{m_{s_R^+}^2} \right|^2,$$

- The  $\lambda_{hs+}$  and  $\lambda_{hs++}$  should have the opposite sign.
- The scalar interactions  $\lambda_{hs+} v h |s_R^+|^2$ ,  $\lambda_{hs++} v h |s^{++}|^2$  are not used for the neutrino mass generation. They are free from constraints from neutrino oscillation experiments.

	(e.g.)	Kanemura, Sakurai, Sugiyama (2016)
D3		

- The Mechanisms-D3, D4, D11, D12, and D17 of the Dirac neutrino mass would be preferred when  $h \rightarrow ll'$  is observed.

**D3****D4****D11****D12****D17**

## Neutrino mass matrix

$$m_D \propto y_\ell X_{SR}^* Y^s$$

symmetric matrix

$$X_{SR} = \begin{cases} Y_S^s & \text{D3, D4} \\ (Y_\psi^+)^* M_\psi (Y_\psi^+)^{\dagger} & \text{D11, D12} \end{cases}$$

$$m_D \propto Y_\psi^\eta (Y_\psi^+)^{\dagger} Y^s$$

# Summary

- We have studied the LFV decay of the Higgs boson in a wide set of models for neutrino masses.
- The simple models of Majorana neutrinos are excluded if  $h \rightarrow ll'$  is discovered.
- The five Mechanisms for Dirac neutrinos can give a significant amount of  $h \rightarrow ll'$  with the suppressed  $l \rightarrow l'\gamma$  process.
  - Two kinds of scalar particles couple to  $l_R$ .
  - Their contributions to  $l \rightarrow l'\gamma$  can be cancelled with each other.

D3, D4

$S_R^+$ ,  $S^{++}$

D11, D12, D17

$S_R^+$ ,  $S_2^+$  (Z2 odd)

- Future discovery of the nonzero  $\text{BR}(h \rightarrow ll')$  shall be a strong probe of models for neutrino masses.