

Offshell Higgs production and interference effects at NLO

Raoul Röntsch

KARLSRUHE INSTITUTE OF TECHNOLOGY

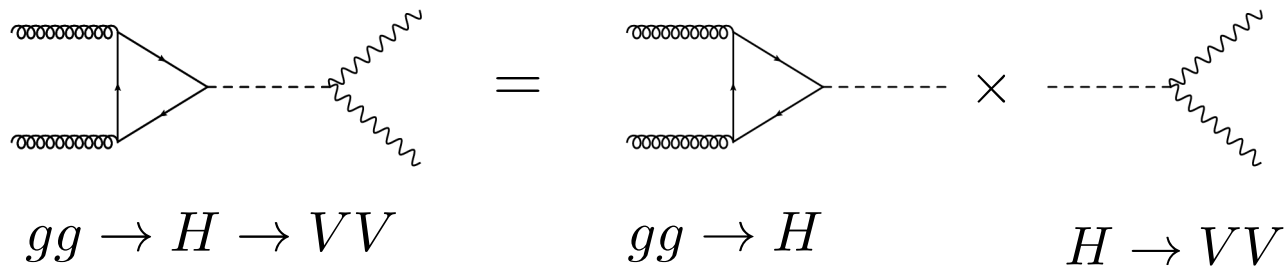
Precision theory for precise measurements at LHC and future colliders

Quy Nhơn, Vietnam

29 September 2016

Higgs on- and offshell

- Higgs properties mostly probed using **onshell Higgs**
 - Factorize production and decay



- Treat signal and background separately

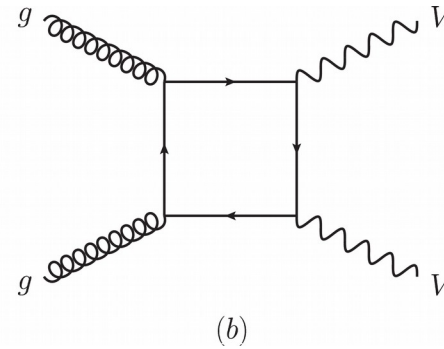
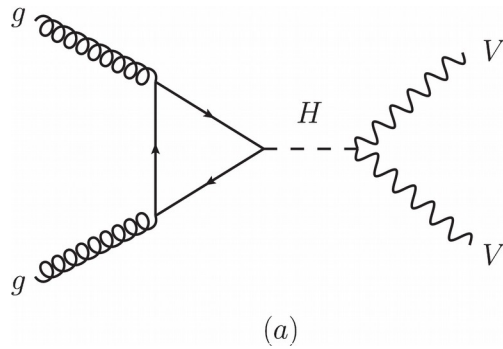
BUT: 10% of events in $H \rightarrow VV$ **above $2m_V$ threshold**

(Kauer, Passarino '12)

➡ NWA **not sufficient** to describe behavior of $H \rightarrow VV$

Offshell interference

Consistent treatment in **high mass region** requires both **signal** and **background** amplitudes



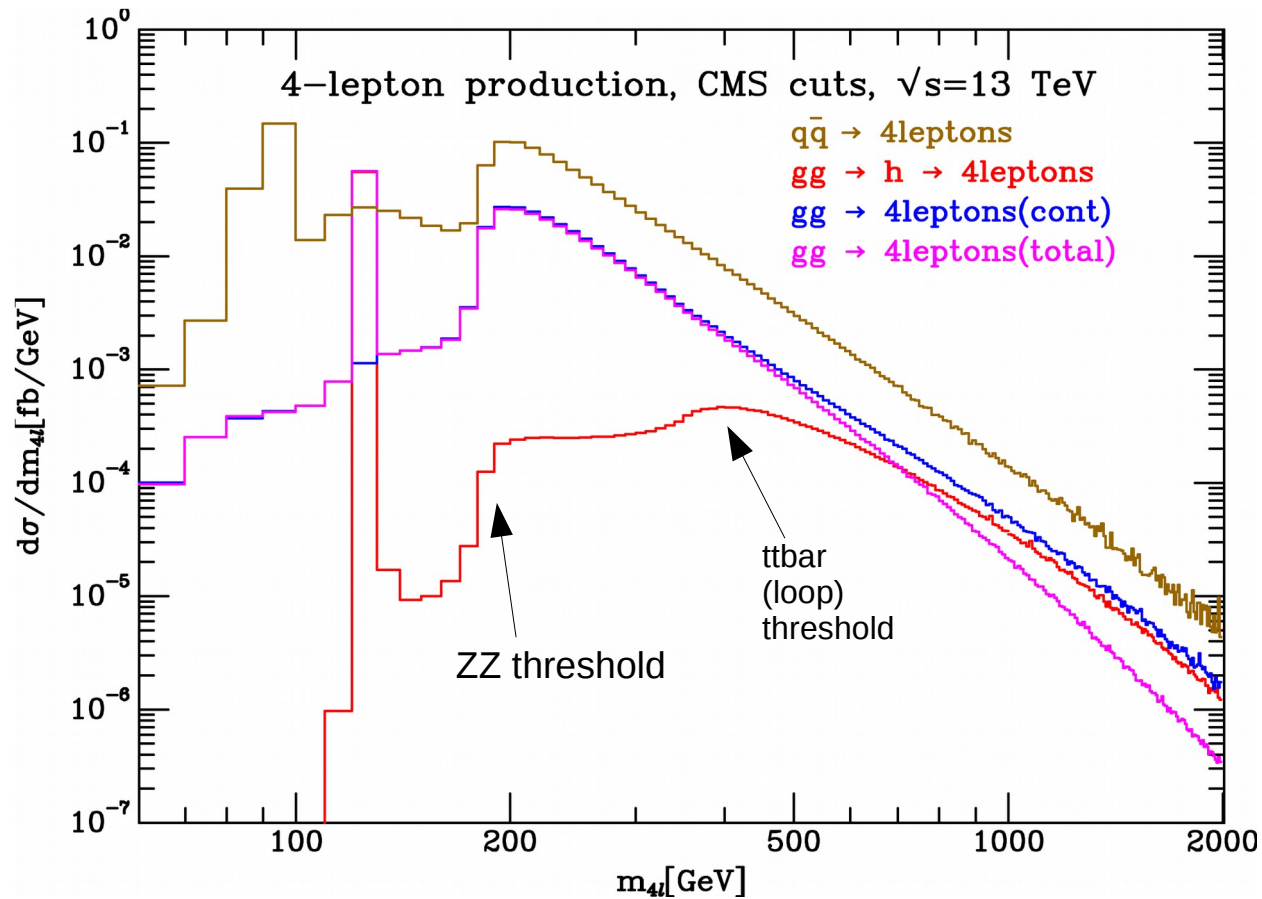
“signal” A_H

“background” A_b

$$|A_{ZZ}|^2 = |A_H|^2 + |A_b|^2 + 2\text{Re}[A_H A_b^*]$$

$$\rightarrow \sigma_{\text{full}} = \sigma_{\text{sigl}} + \sigma_{\text{bkgd}} + \sigma_{\text{intf}}$$

Interference effect and line shape

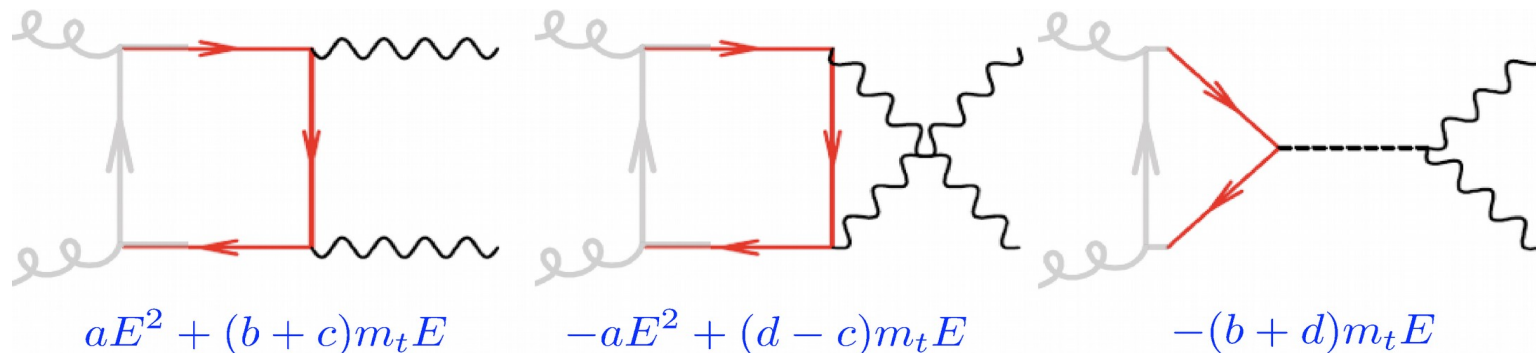


Interference is **strong** and **destructive**, especially at high invariant mass

Campbell, Ellis, Williams '13

Understanding high energy behavior

Cut open top loop – have $t\bar{t} \rightarrow VV$



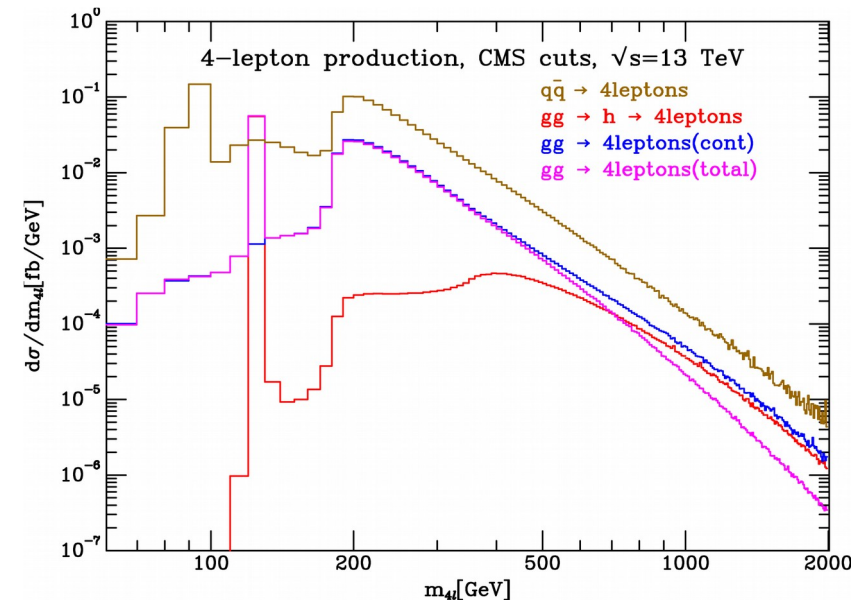
J. Campbell

- **Signal** and **background** amplitudes-squared grow like E^2
- **Interference** grows like $-E^2 \rightarrow$ cancels E^2 terms of signal and background
- **Higgs unitarizing massive scattering amplitude** – connected to its role in EWSB and mass generation

Using off-shell Higgs

We have **a new tool** for studying Higgs physics!

- High mass behavior probes **unitarization properties** of Higgs
 - **As important** as measuring Higgs couplings for understanding EWSB
 - Cross sections small \rightarrow HL-LHC
- Higgs couplings **more sensitive to NP** at high energies



Campbell, Ellis, Williams '13

Using off-shell Higgs: indirect width constraints

- Observation of Caola & Melnikov:

$$\sigma_{\text{on}} \propto g_i^2 g_f^2 / \Gamma_H \quad \sigma_{\text{off}} \propto g_i^2 g_f^2$$

$$\Rightarrow \Gamma_H \propto \frac{\sigma_{\text{off}}}{\sigma_{\text{on}}} \quad \longrightarrow \quad \text{indirect constraint on width}$$

- CMS: $\Gamma_H < 13 \text{ MeV}$ ATLAS: $\Gamma_H < 23 \text{ MeV}$
- Direct constraints $\sim 1 \text{ GeV}$
- Compare with SM value: $\Gamma_H \approx 4 \text{ MeV}$

Indirect Higgs width constraint: *caveat emptor*

Indirect constraints not model-independent:

- **Assume same couplings on- & off-shell**
- Can construct models with $\Gamma_H > \Gamma_H^{\text{SM}}$ but no sensitivity from off-shell measurements (Englert, Spannowsky '14)
- Possible option:
 - Introduce energy-dependent couplings in κ -framework / EFT (Englert, Soreq, Spannowsky '14)
 - Constrain couplings and width simultaneously
 - Highly non-trivial dependence of **signal**, **background** and **interference** on these couplings! (see e.g. Azatov, Grojean, Paul, Salvioni '16)
 - CMS: simultaneous constraints on width & HVV coupling (hep-ex/1507.06656)

Impact of higher order corrections

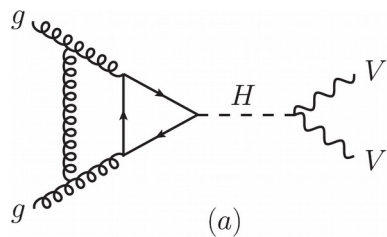
- Signal (incl. top mass effects) known at **NLO**
 - **NLO corrections large**, k-factor ~ 1.7
- Experimental analyses use background and interference at **LO only**
 - NLO corrections approximated by corrections from signal
→ **adds uncertainties to analysis**
- Recent work has extended background and interference to **NLO**

Campbell, Czakon, Ellis, Kirchner, hep-ph/1605.01380

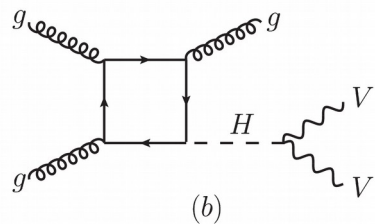
Caola, Dowling, Melnikov, R.R., Tancredi, hep-ph/1605.04610

Higgs Interference Effects at NLO

Known

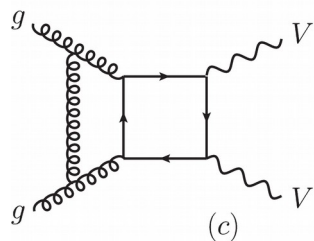


Known



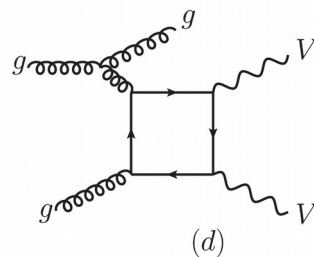
Massless: known

Massive: extremely difficult / impossible

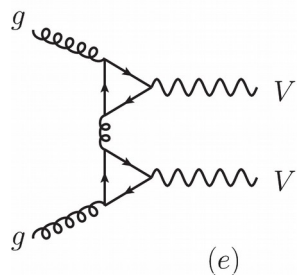


Massless: easy

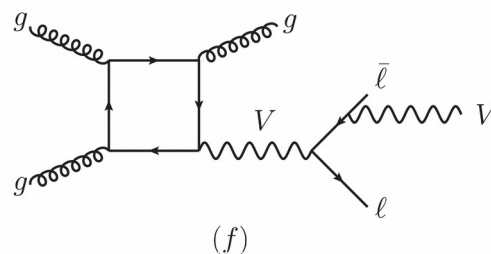
Massive: moderate



Known



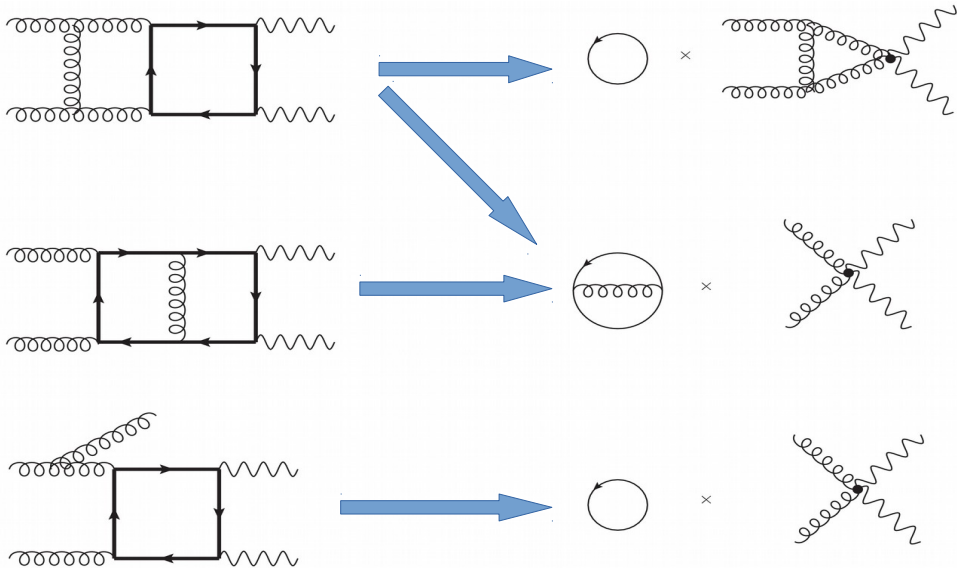
Known



Spira, Djouadi, Graudenz, Zerwas '95; Harlander, Kant '05; Aglietti, Bonciani, Degrassi, Vicini '07;
 Ellis, Hinchliffe, Soldate, v.d. Bij '88;
 Caola et al '15, v. Manteuffel, Tancredi '15
 Hagiwara, Kuruma, Yamada '91; Campbell, Ellis, Zanderighi '07;
 v.d. Bij, Glover '89;

$gg \rightarrow (H) \rightarrow ZZ$: Top Mass Expansion

Expand in s/m_t^2



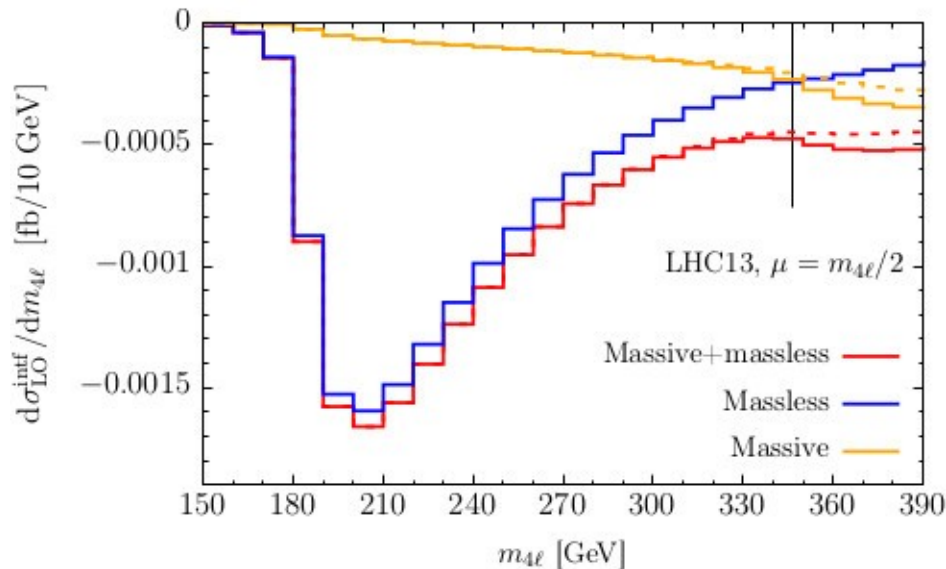
- Keep terms to $(s/m_t^2)^4$
- Expect to be valid for partonic energies

$$s \lesssim 4m_t^2$$

Dowling, Melnikov '15

Validity of top mass expansion

Can check validity at LO – Interference for exact m_t dependence vs mass expansion



Good approximation below $2m_t$ threshold

Restricted to
 $m_{4\ell} \leq 2m_t$
 $p_{T,j} < 150 \text{ GeV}$

- Cannot probe unitarization effects :(

- Large window $150 \text{ GeV} \lesssim m_{4\ell} \leq 2m_t$ where Higgs is off-shell and we can study **interference effects at NLO**

Parameters

- $gg \rightarrow ZZ \rightarrow e^+e^-\mu^+\mu^-$ at 13 TeV LHC
- Dynamical scale $\mu_F = \mu_R = \{m_{4\ell}/4, m_{4\ell}/2, m_{4\ell}\}$
- Minimal cuts:
 - $150 \text{ GeV} \leq m_{4\ell} \leq 340 \text{ GeV}$
 - $p_{T,j} < 150 \text{ GeV}$
 - $60 \text{ GeV} \leq m_{\ell\ell} \leq 120 \text{ GeV}$

$gg \rightarrow (H) \rightarrow ZZ$ Results: Cross Sections

$$\sigma_{\text{LO}}^{\text{signal}} = 0.043_{-0.009}^{+0.012} \text{ fb}, \quad \sigma_{\text{NLO}}^{\text{signal}} = 0.074_{-0.008}^{+0.008} \text{ fb}$$

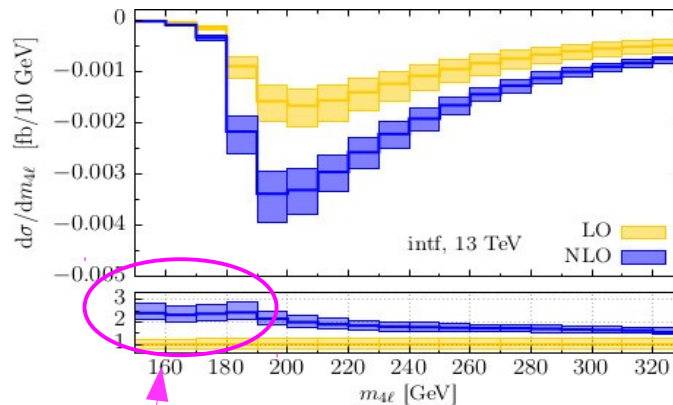
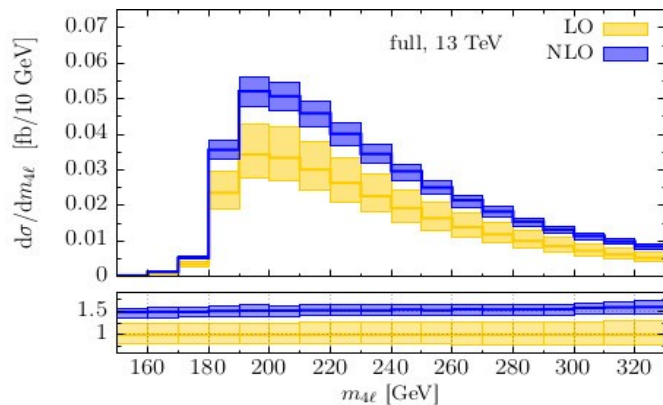
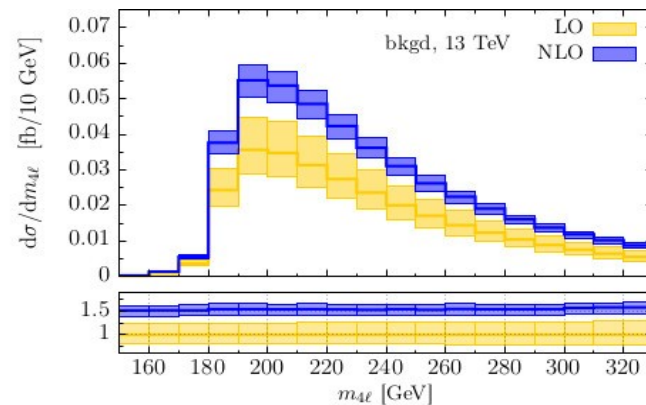
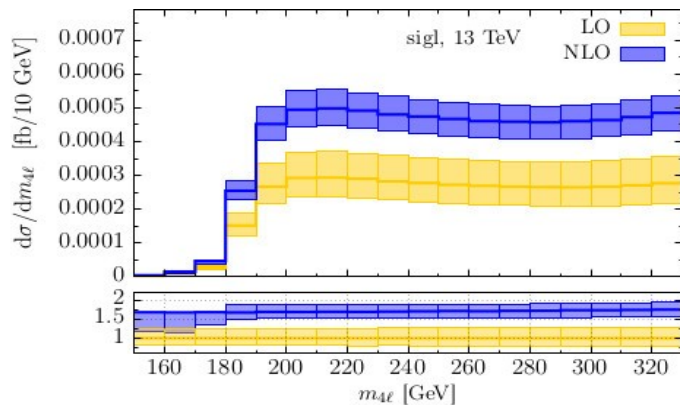
$$\sigma_{\text{LO}}^{\text{bkgd}} = 2.90_{-0.58}^{+0.77} \text{ fb}, \quad \sigma_{\text{NLO}}^{\text{bkgd}} = 4.49_{-0.38}^{+0.34} \text{ fb}$$

$$\sigma_{\text{LO}}^{\text{intf}} = -0.154_{-0.04}^{+0.031} \text{ fb}, \quad \sigma_{\text{NLO}}^{\text{intf}} = -0.287_{-0.037}^{+0.031} \text{ fb}$$

$$\sigma_{\text{LO}}^{\text{full}} = 2.79_{-0.56}^{+0.74} \text{ fb}, \quad \sigma_{\text{NLO}}^{\text{full}} = 4.27_{-0.35}^{+0.32} \text{ fb},$$

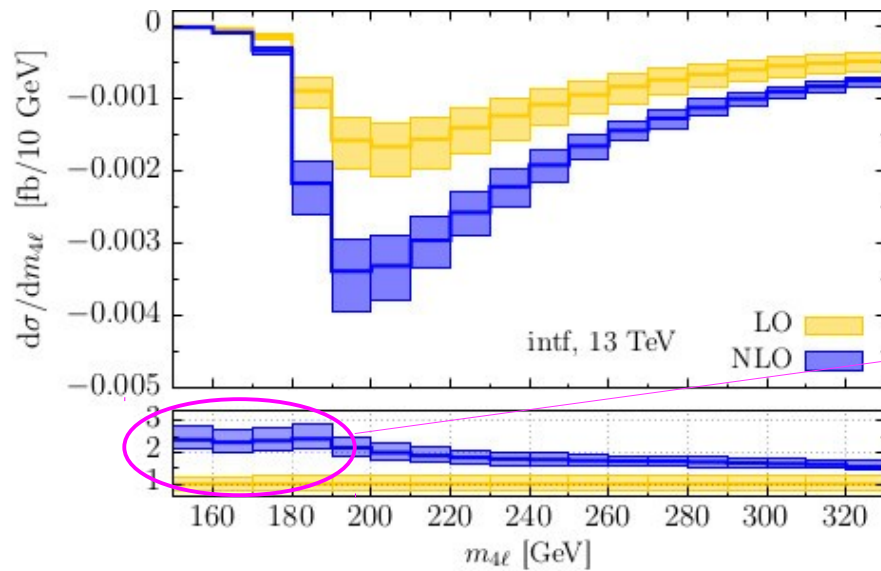
- $\sim 13\text{k}$ events at HL-LHC (3 ab^{-1})
- **Destructive interference** $\sim 5\%$
 - ~ 4 x larger than signal, order of magnitude smaller than background
 - Can use specialized cuts needed to enhance relative to signal and background
- Scale uncertainty: **20%-30% at LO**, **10% at NLO**
- $K_{\text{sigl}} = 1.72$ $K_{\text{bkgd}} = 1.55$ $K_{\text{intf}} = 1.65 \simeq \sqrt{K_{\text{sigl}} K_{\text{bkgd}}}$

$gg \rightarrow (H) \rightarrow ZZ$ Results: Mass distributions

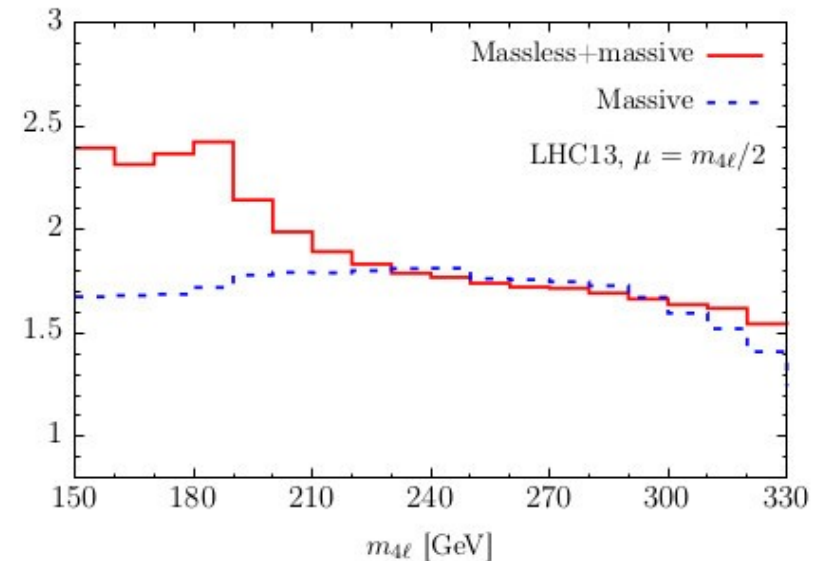


- Differential k-factors **relatively flat**...
- Except for interference near $2m_Z$ threshold

$gg \rightarrow (H) \rightarrow ZZ$ Results: Differential k-factor



K_{intf}



- **Massless loop** dominates near $2m_Z$ threshold, **drives k-factor behavior**

Comparison with similar work

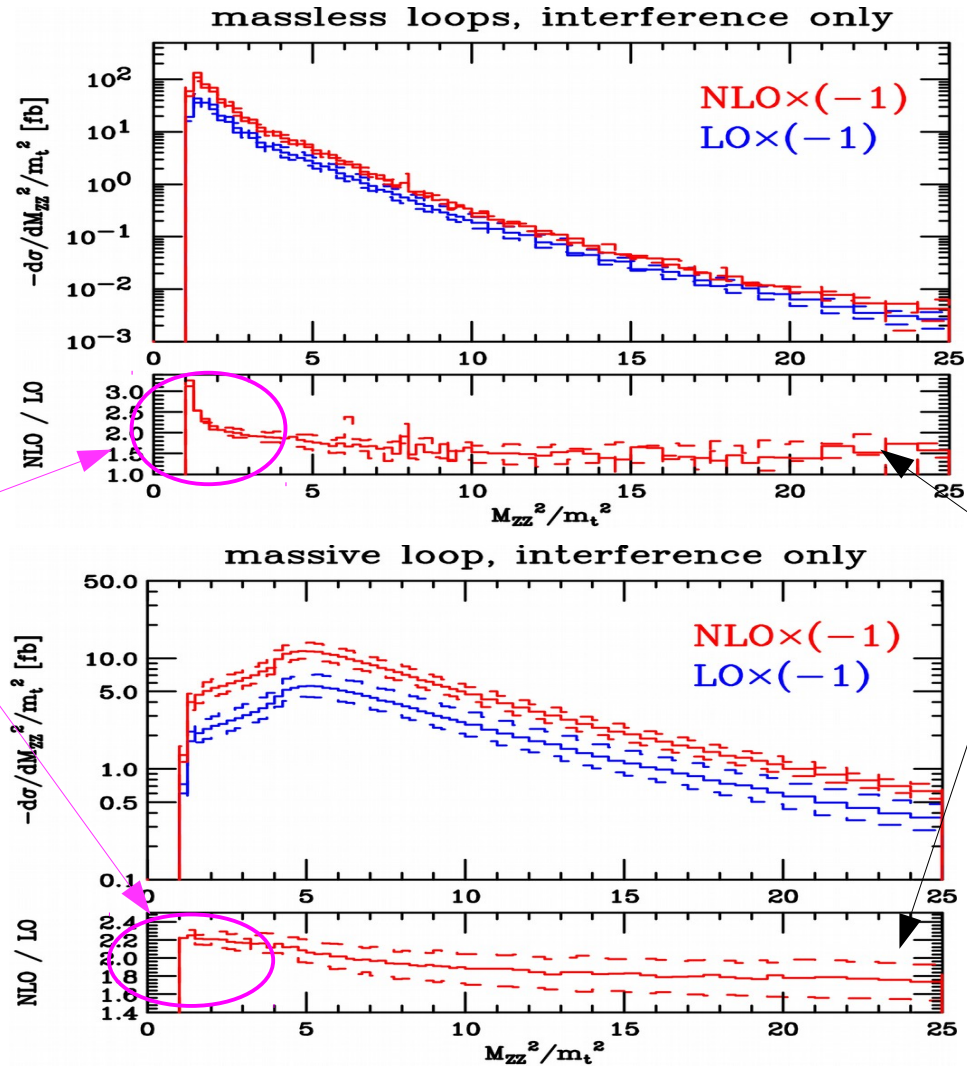
Campbell, Czakon, Ellis, Kirchner, hep-ph/1605.01380

- Only **interference** contribution considered
- On-shell Z bosons, so $m_{ZZ} > 2m_Z$
- Massive two-loop amplitudes computed in mass expansion to $(s/m_t^2)^6$
- Massive real emission amplitudes computed exactly – no need for jet cut
- **Results extended beyond $2m_t$ threshold using Padé approximations – look at high-mass tail**

Comparison with similar work

Campbell, Czakon, Ellis,
Kirchner, hep-ph/1605.01380

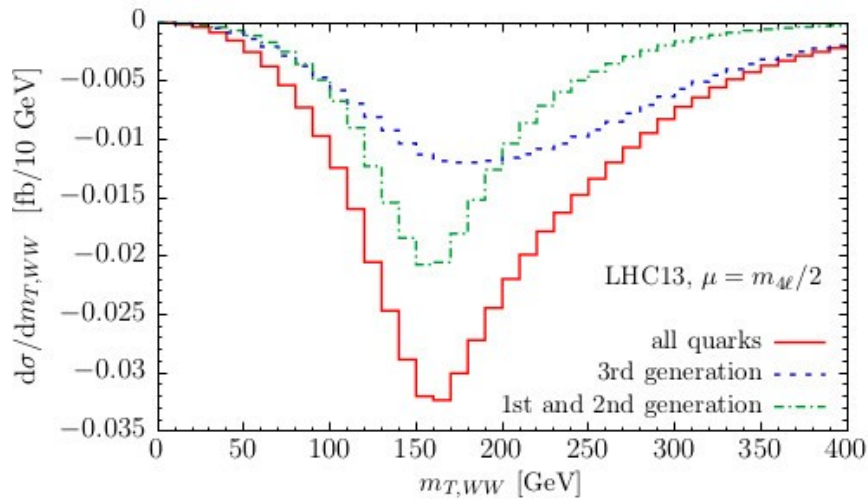
Qualitatively similar
behavior of k-factors
near $2m_Z$ threshold



k-factor flat
in high-
energy tail

$gg \rightarrow (H) \rightarrow WW$

- Analogous to $gg \rightarrow (H) \rightarrow ZZ$
- Mass expansion more complicated since **top and bottom quarks mix** in loop
- \rightarrow neglect 3rd generation altogether
 - **Comparable** to massless contribution at low-intermediate $m_{T,WW}$
 - **Dominate** at high $m_{T,WW}$
- **Partial results only**



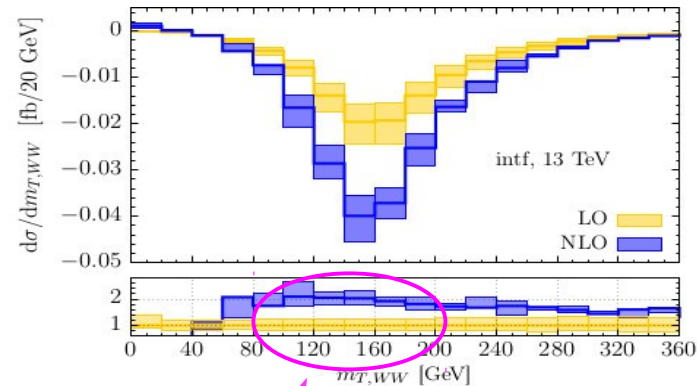
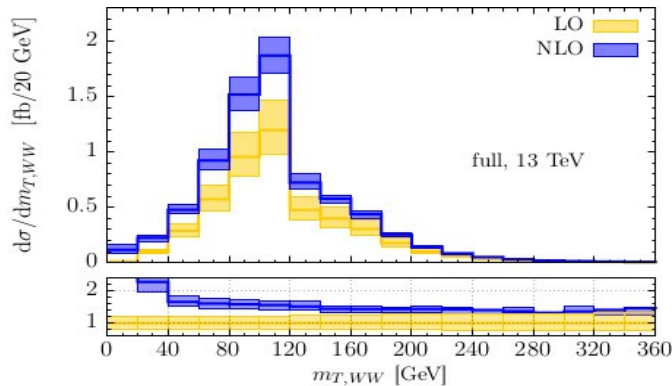
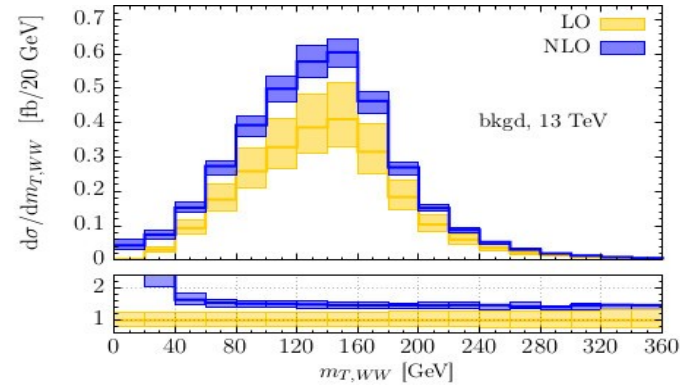
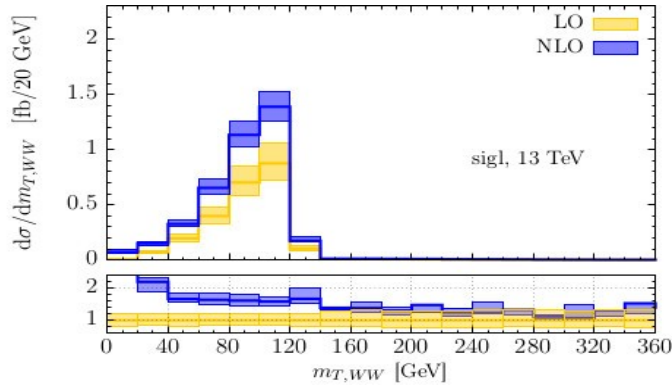
- $gg \rightarrow W^+W^- \rightarrow \nu_e e^+ \mu^- \bar{\nu}_\mu$
- No kinematic cuts imposed
- Scales as for ZZ

$gg \rightarrow (H) \rightarrow WW$ Results: Cross Sections

$$\begin{aligned} \sigma_{\text{LO}}^{\text{signal}} &= 48.3_{-8.4}^{+10.4} \text{ fb}, & \sigma_{\text{NLO}}^{\text{signal}} &= 81.0_{-8.2}^{+10.5} \text{ fb} \\ \sigma_{\text{LO}}^{\text{bkgd}} &= 49.0_{-9.7}^{+12.8} \text{ fb}, & \sigma_{\text{NLO}}^{\text{bkgd}} &= 74.7_{-6.2}^{+5.5} \text{ fb} \\ \sigma_{\text{LO}}^{\text{intf}} &= -2.24_{-0.59}^{+0.44} \text{ fb}, & \sigma_{\text{NLO}}^{\text{intf}} &= -4.15_{-0.54}^{+0.47} \text{ fb} \\ \sigma_{\text{LO}}^{\text{full}} &= 95.0_{-17.6}^{+22.6} \text{ fb}, & \sigma_{\text{NLO}}^{\text{full}} &= 151.6_{-13.9}^{+15.4} \text{ fb}. \end{aligned}$$

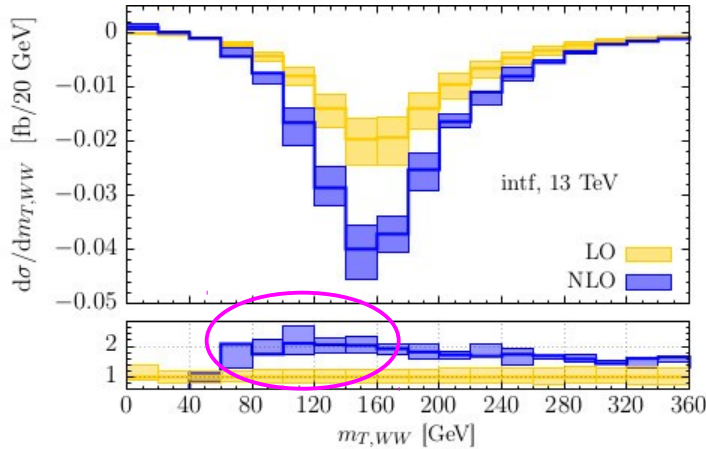
- **Destructive interference** ~ 2%
 - Higgs peak present → interference smaller than signal and background
- Scale uncertainty reduced by factor ~ 2
- $K_{\text{sigl}} = 1.68$ $K_{\text{bkgd}} = 1.53$ $K_{\text{intf}} = 1.85$
 - slightly above geometric mean

$gg \rightarrow (H) \rightarrow WW$ Results: Mass distributions



- Differential k-factors **relatively flat...**
- ... except for interference near $2m_W$ threshold – as in ZZ case

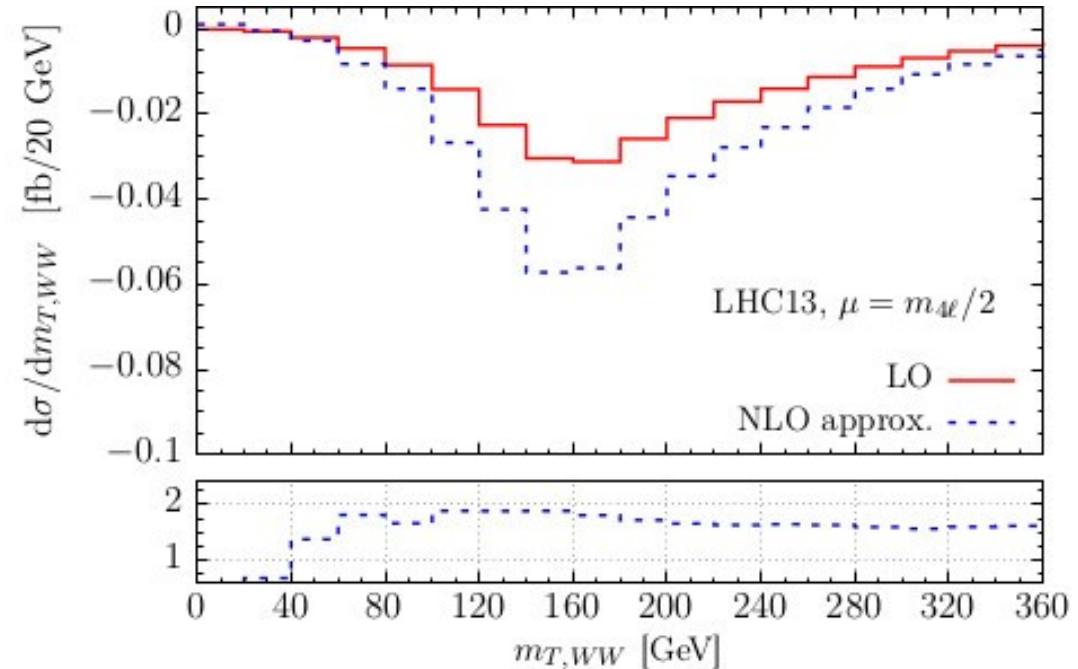
$gg \rightarrow (H) \rightarrow WW$ Results: Estimating effect of 3rd generation



- As in ZZ case, enhancement from **massless loops**
- **3rd generation loops** give relatively flat differential k-factor

→ estimate by using LO results scaled by approximate k-factor

$$\sqrt{K_{\text{sigl}} K_{\text{bkgd}}}$$



Nice job...

Impact of NLO calculation on width constraints:

- K-factor known, can remove systemic uncertainty
- **Exact impact not obvious** – will wait for experimental analysis

...but is it good enough?

- NLO is known to be insufficient for onshell Higgs – **is it okay for offshell?**
 - NLO results lie **outside** LO scale uncertainty bands
 - Do we trust the **NLO scale uncertainty?**
 - **Offshell NNLO** impossible at present
 - Use NNLO results for infinite m_t to get **approximate NNLO** k-factor offshell?
- Can we understand effectiveness of Padé approximants (e.g. how well do they do for HH production)?

Conclusions

- Higgs off-shell behavior provides a rich environment to study Higgs physics:
 - Probe **unitarizing behavior** of the Higgs
 - **Indirect constraints** on Higgs width
 - **Test couplings** at high energies
- NLO corrections to **interference** in $gg \rightarrow ZZ$ and $gg \rightarrow WW$, are now known, at least below $2m_t$ threshold
- Difficulty of computing two-loop massive corrections
 - **top mass expansion** for ZZ
 - **neglect 3rd generation** for WW
- ZZ in window $150 \text{ GeV} \leq m_{4\ell} \leq 340 \text{ GeV}$
 - Moderate k-factors $\sim 1.6-1.7$
 - $K_{\text{intf}} \simeq \sqrt{K_{\text{sigl}} K_{\text{bkgd}}}$ **except near $2m_z$ threshold** – driven by massless amplitudes
- WW :
 - Interference k-factor slightly larger than signal and background k-factors
 - Effect of 3rd generation at NLO approximated assuming uniform contribution to k-factor

THANK YOU!