

# Exotic Decays of $h(125)$



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on behalf of the CMS and ATLAS Collaborations

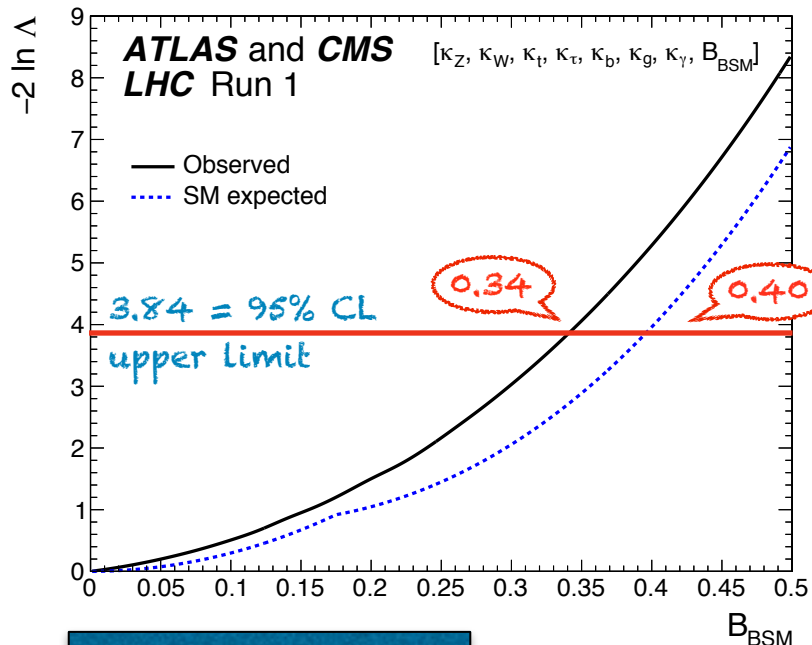
Precision theory for precise measurements at LHC and future colliders  
Quy Nhon, Vietnam (25 Sep to 1 Oct 2016)



# Exotic decay modes : Why?

- > Standard Model (SM) successfully describe particles and interactions but doesn't address the hierarchy problem, fine tuning, dark matter ... → **need to go beyond the SM**
  - The discovered Higgs at 125 GeV can play a crucial role in probing BSM physics
- > Combined ATLAS and CMS couplings measurements constrains  $BR(H \rightarrow BSM) < 0.34$  (0.4) at 95% CL from Run-1 data (7 and 8 TeV)

- **Still room for “New Physics”!**



JHEP 08 (2016) 045

- > Many BSM theories such as SUSY, 2HDM, EWS (etc.) predict such decays, e.g.
  - Higgs → invisible particles
  - Higgs → light (pseudo-)scalars
  - LFV Higgs
- > CMS and ATLAS experiments are actively working on the full Run-2 data to cover large number of BSM Higgs searches
- > **Is it the time for BSM era?**

# Exotic decay modes : Which?



Theoretical models include :

more details given by W. Jiawei

- > **Two Higgs Doublet Models (2HDM)** extend beyond the SM Higgs sector by including two complex Higgs doublets, which, after symmetry breaking, lead to five physical states

$H^+$ ,  $H$ ,  $A$  (CP-odd),  $H^0$ ,  $h$  (CP-even)

- e.g.  $h \rightarrow AA$ ,  $H^0 \rightarrow hh/AA$ , LFV of the Higgs
- an additional scalar singlet (**2HDM+S**) — CP-even ( $h_1, h_2, h_3$ ), CP-odd ( $a_1, a_2$ ),  $H^+$ ,  $H^-$
- > **Minimal Supersymmetric Standard Model (MSSM)** describes solution to hierarchy problem and dark matter (DM) candidates
  - e.g.  $h \rightarrow \chi_i \chi_j$  (i.e. Higgs to invisible searches)
- > **Next-to-MSSM (NMSSM)** provides larger possibilities for the Higgs decays to other (pseudo-) scalars as well as the neutralinos sectors
- > Other models such as **Little Higgs model**, include Higgs as a composite particle, or Higgs decays to valley particles which in turn decay to SM particles in **Hidden Valley models**
  - e.g. LFV of the Higgs,  $h \rightarrow$  dark sector

# Exotic decay modes : Which?



Experimental results so far...

## **$h(125) \rightarrow$ (pseudo)scalars**

- > CMS results currently cover  $h \rightarrow aa \rightarrow \mu\mu\mu\mu, \mu\mu bb, \mu\mu\tau\tau, \tau\tau\tau\tau$
- > ATLAS results currently cover  $h \rightarrow aa \rightarrow \gamma\gamma\gamma\gamma, \mu\mu\tau\tau$  and  $Wh \rightarrow aa \rightarrow bbbb$

## **Lepton Flavor Violating (LFV) of $h(125)$**

- > CMS and ATLAS results both cover **LFV  $h \rightarrow e\tau, \mu\tau$  and  $e\mu$**

## **$h(125) \rightarrow$ dark sector (invisible, dark photons, ...)**

not covered here

- > gluon-gluon fusion (ggF) : events with ISR jet (Monojet search)
- > vector boson fusion (VBF) : events with two tagged jets
- > associated production with W/Z (VH) : events with leptons/hadrons from W/Z
  - $Z \rightarrow ll, Z \rightarrow bb, V \rightarrow jj$

see talk given by L. Truong

**$h(125) \rightarrow aa$**

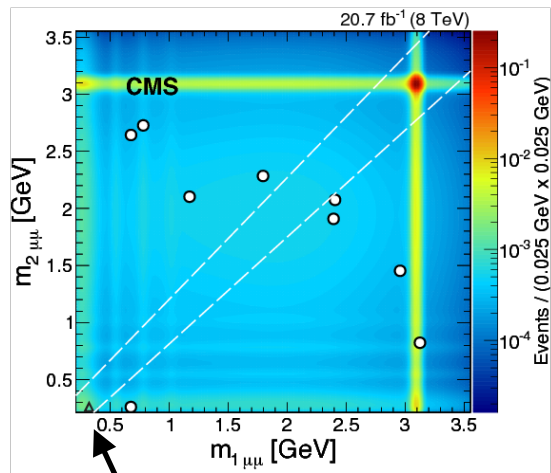
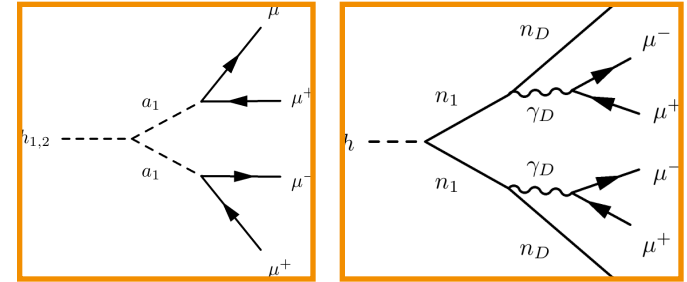
# $h \rightarrow aa \rightarrow 4\mu$



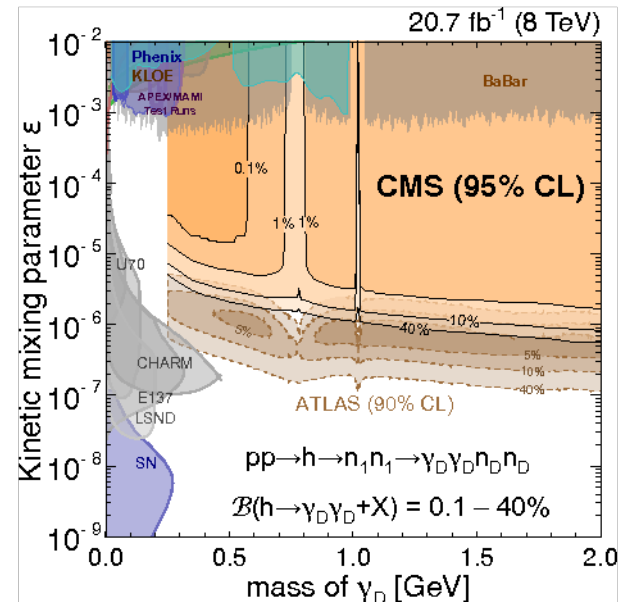
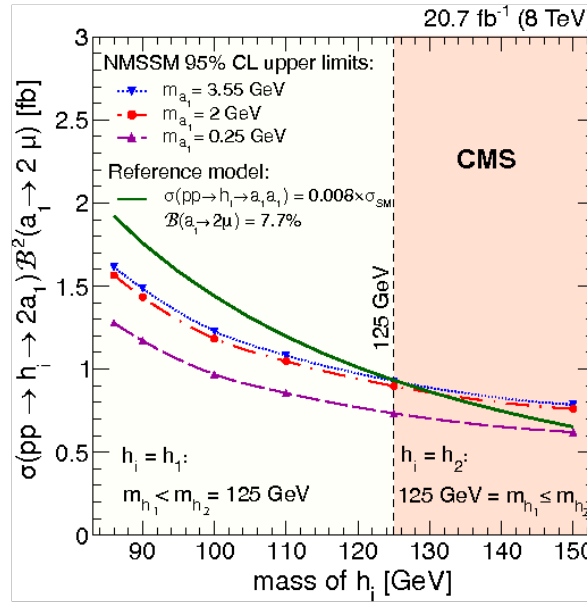
8 TeV 20 fb<sup>-1</sup>

Phys. Lett. B 752(2016)146-168

- Two models interpretation
  - NMSSM benchmark  $h \rightarrow aa \rightarrow 4\mu$  ( $2m_\mu \leq m_a \leq 2m_\tau$ )
  - Dark SUSY benchmark  $h \rightarrow 2n_1 \rightarrow 2n_D + 2\gamma_D \rightarrow 4\mu$
- Very small mass range  $m_a \in 0.25$  to  $3.55$  GeV
- Main backgrounds from  $bb$ ,  $J/\Psi$  and  $pp \rightarrow 4\mu$
- No excess data is observed
  - diagonal signal region :  $m_{\mu\mu 1} \approx m_{\mu\mu 2}$



observed 1 event w.r.t  $2.2 \pm 0.7$  SM background



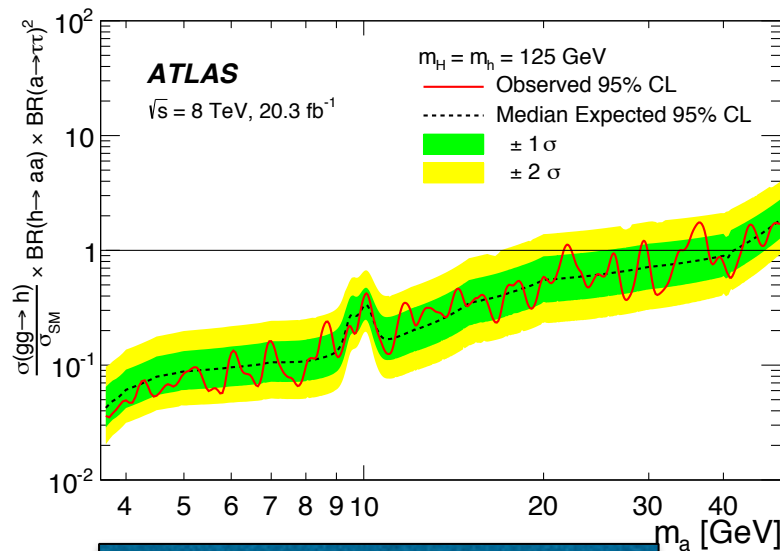
# $h \rightarrow aa \rightarrow \mu\mu\tau\tau$



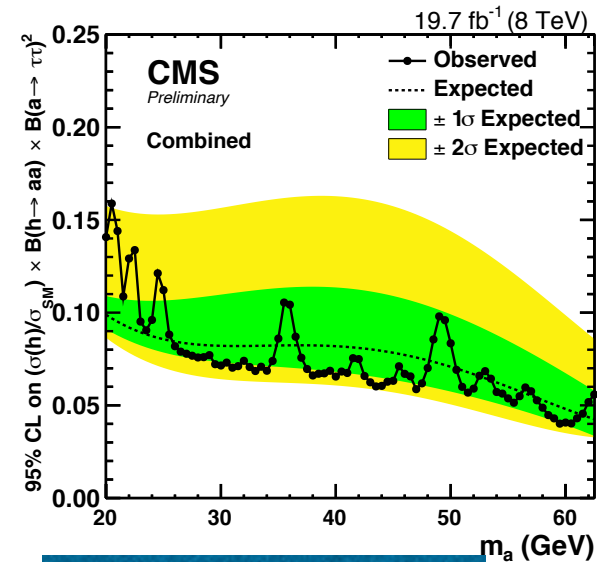
8 TeV 20 fb<sup>-1</sup>

- > Well-motivated by **2HDM+S**, especially type-3 at large  $\tan\beta$  and type-4 at small  $\tan\beta$
- > Reconstructed events with 2 muons (good resolution) plus 2 taus
  - CMS combined 5 final states  $\rightarrow \mu\mu\tau_e\tau_e, \mu\mu\tau_e\tau_\mu, \mu\mu\tau_e\tau_h, \mu\mu\tau_\mu\tau_h$  and  $\mu\mu\tau_h\tau_h$
  - ATLAS considered two  $\mu$  + one lepton ( $e, \mu$ ) and tracks
- > Limits are set on  $\text{Br}(h \rightarrow aa) \times \text{Br}(a \rightarrow \tau\tau)^2$  from an unbinned fit of  $m_{\mu\mu}$  distributions
  - CMS placed upper limits between 4-15% for  $m_{\mu\mu} \in 20$  to 62.5 GeV
  - ATLAS provided the most stringent limit at 3.5% for  $m_{\mu\mu}$  3.75 GeV over 3.7 to 50 GeV

> No significant excess of data over SM backgrounds



Phys.Rev.D92 (2015) 052002



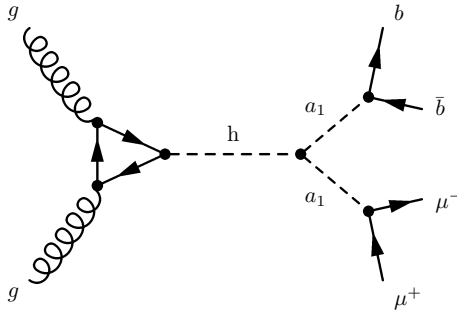
CMS PAS HIG-15-011



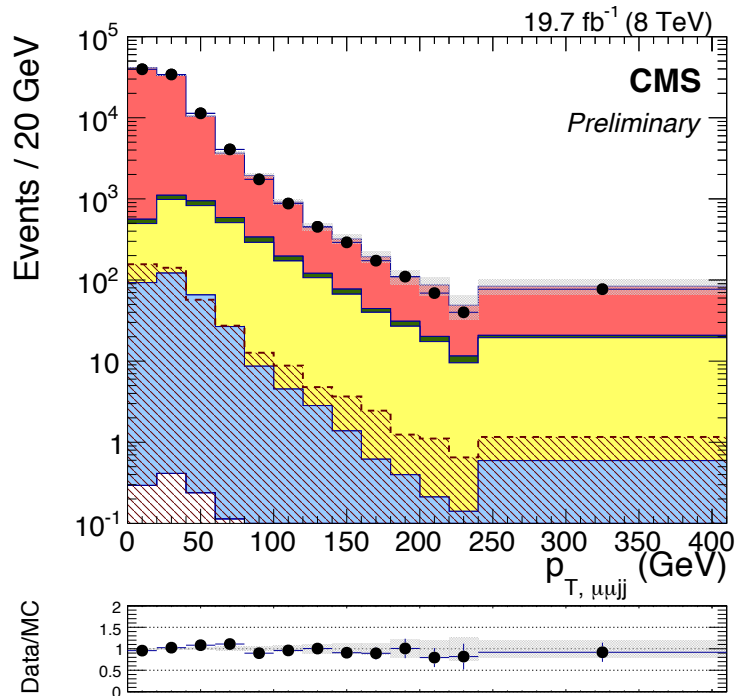
# $h \rightarrow aa \rightarrow \mu\mu bb$



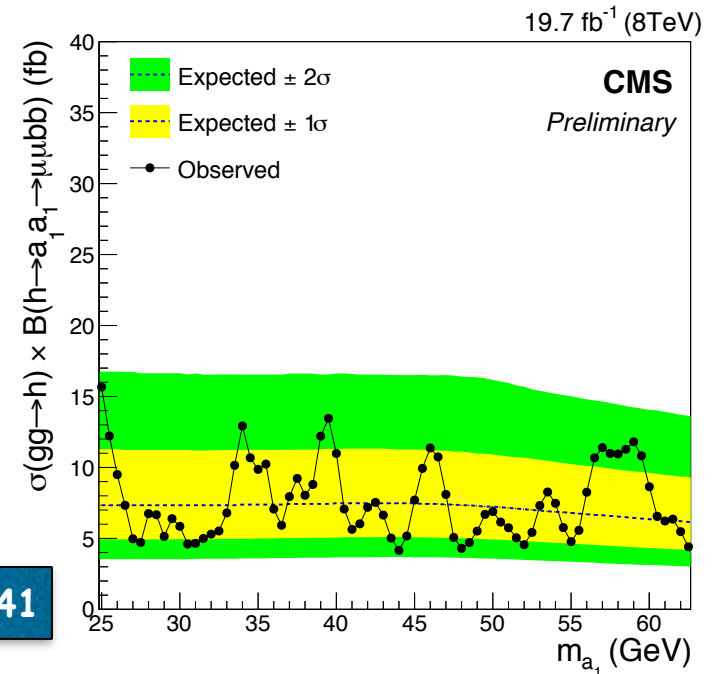
8 TeV 20 fb<sup>-1</sup>



- > Interpretation of **NMSSM** and even more generic **2HDM+S**
- > Advantage of the higher rate and lower background contamination in comparison with the 4 $\mu$  and 4b final states
- > **No significant excess is observed**
  - upper limits are set on  $\sigma_{\text{ggF}} \times \text{Br}(h \rightarrow aa \rightarrow \mu^+\mu^-bb)$  with ranging between 4 to 12 fb for  $m_{\mu\mu} \in 25$  to 65 GeV



CMS PAS HIG-14-041



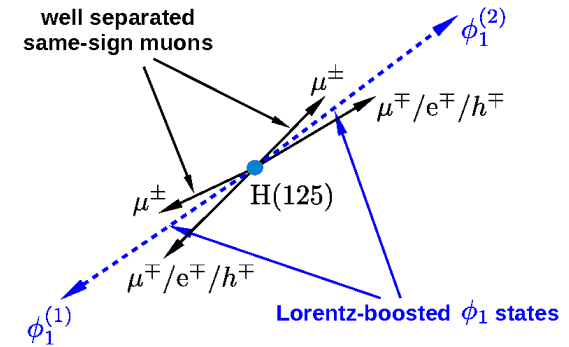


# $h \rightarrow aa \rightarrow 4\tau$ (1)

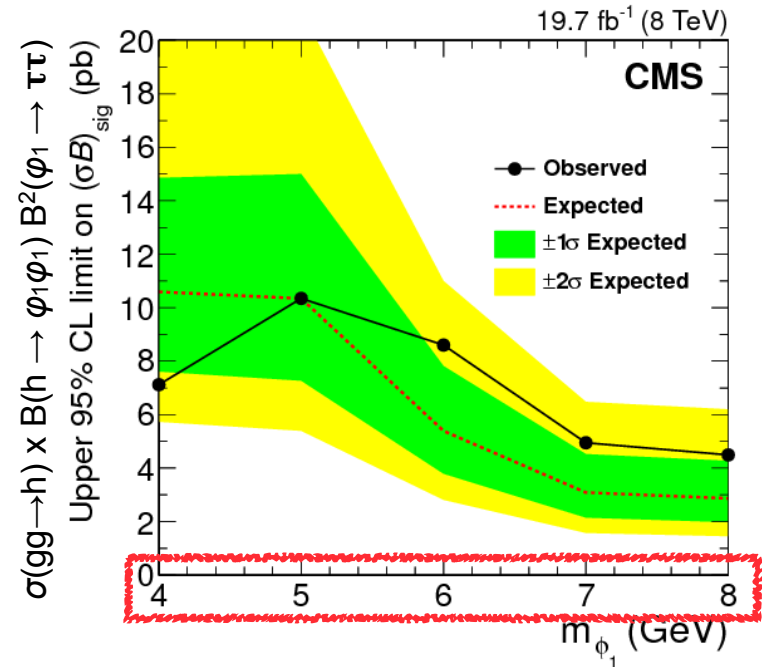
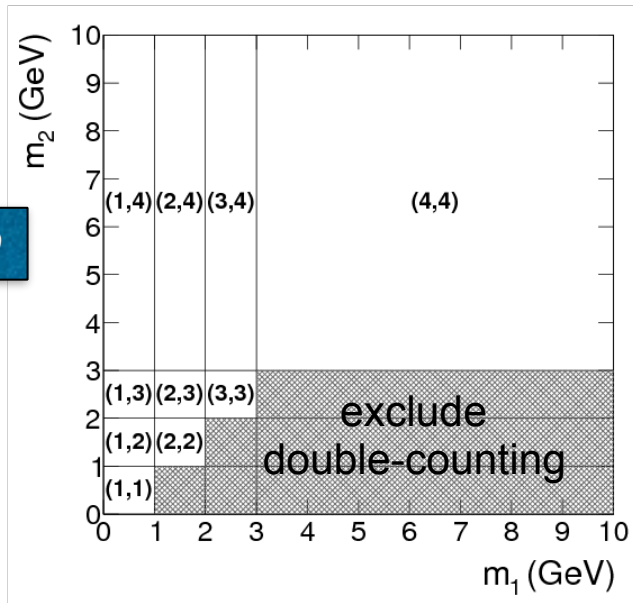


8 TeV 20 fb<sup>-1</sup>

- > Focus  $gg \rightarrow aa \rightarrow 4\tau$  within the framework of **NMSSM**
  - same-sign di-muon events with large angular separation plus one nearby opposite-sign track ( $\mu$ +track)
- > Signal extracted with binned maximum likelihood fit to the 2D distribution of  $(m_{\mu\text{track}1}, m_{\mu\text{track}2})$
- > **No excess data is observed**
  - upper limits range from 4.5 pb at  $m_{a_1}(m_{h_1}) = 8\text{GeV}$  to 10.3 pb at  $m_{a_1}(m_{h_1}) = 5\text{GeV}$



JHEP 01(2016)079



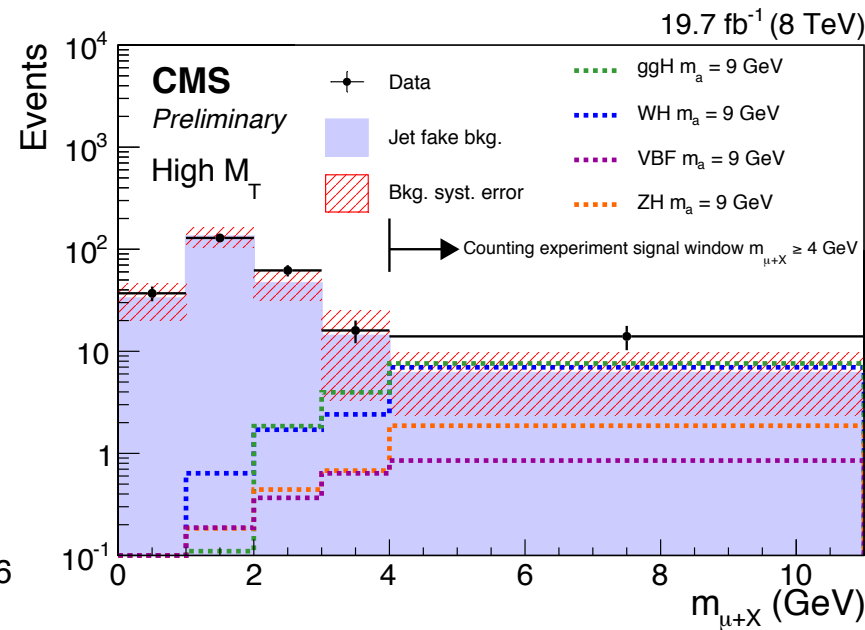
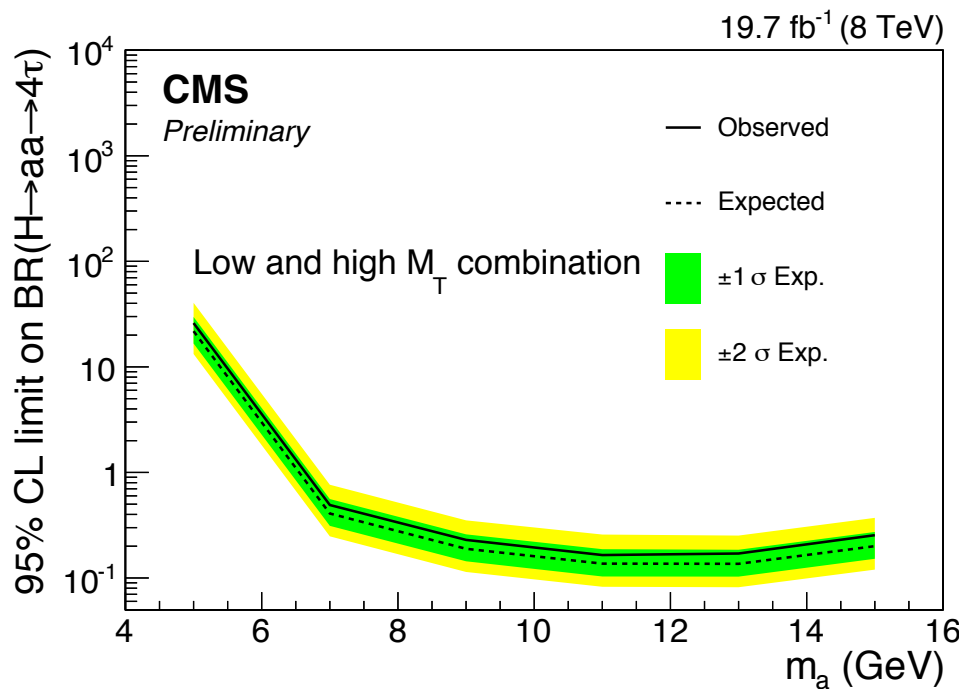
# $h \rightarrow aa \rightarrow 4\tau$ (2)



8 TeV 20 fb<sup>-1</sup>

- Different approach ( $\mu$ +jet) within the context of **NMSSM and 2HDM+S**
  - including ggH, WH, ZH and VBF production modes of h(125)
  - higher mass region covered  $m_a \in 5$ -15 GeV
- Simple counting experiment
- No excess of events above the SM backgrounds is found
  - upper limits on  $BR(H \rightarrow aa/hh)BR^2(a/h \rightarrow \tau\tau)$  are set assuming SM cross-sections for all Higgs production modes

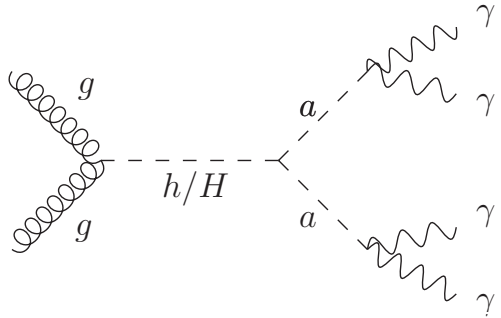
CMS PAS HIG-14-022



# $h \rightarrow aa \rightarrow 4\gamma$

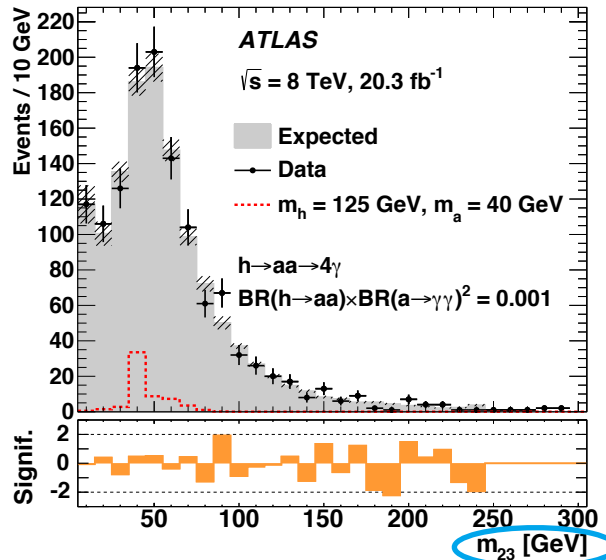


8 TeV 20 fb<sup>-1</sup>

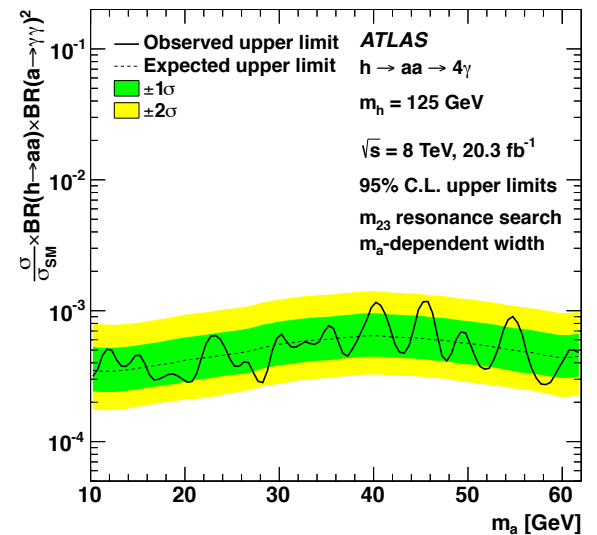
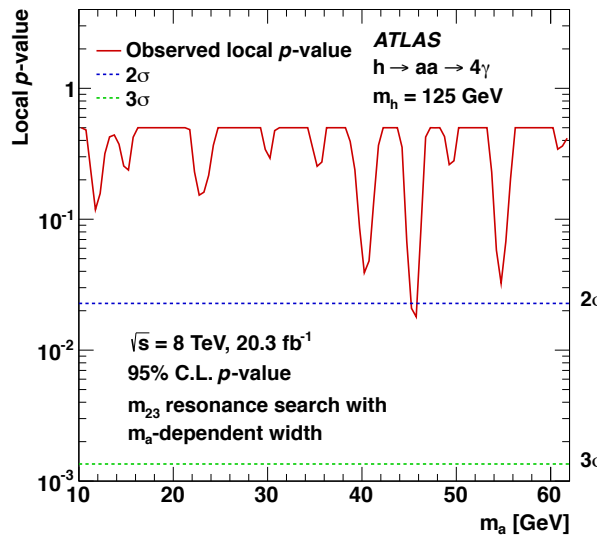


EPJC 76(4)1-26(2016)

- > Inclusive three photons search interpreted in **NMSSM** context
  - select events have  $\geq 3\gamma$  with  $p_T > 22, 22, 17$  GeV
- > Main backgrounds estimated from MC and data
  - irreducible multi-photon processes by MC
  - photons+jet (jet fakes) from data
- > No excess above SM backgrounds is detected
  - Limits are found to be  $\sigma \times \text{BR}(h \rightarrow aa) \times \text{BR}(a \rightarrow \gamma\gamma)^2 < 10^{-3} \sigma_{\text{SM}}$  for  $m_a \in 10-62$  GeV



2<sup>nd</sup>+3<sup>rd</sup> leading  $p_T$  photon



# Wh $\rightarrow$ aa $\rightarrow$ 4b



13 TeV 3.2 fb<sup>-1</sup>

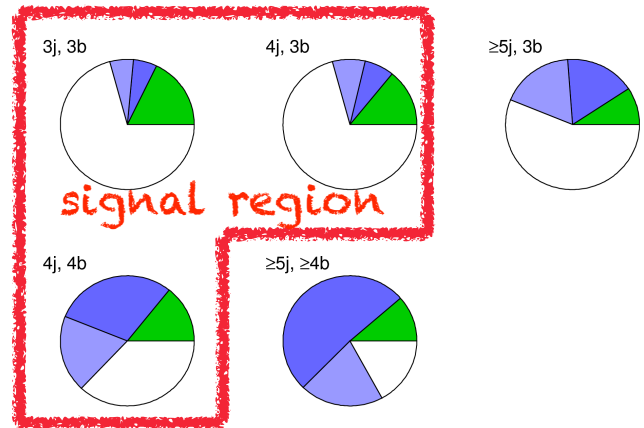
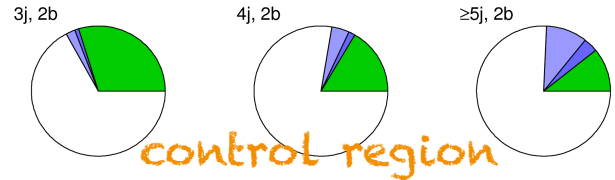
arXiv:1606.08391

- > First published result from 13 TeV data at the LHC
- > Associated production of h(125) with W boson
  - charged lepton from W provides efficient trigger and background reduction
  - final states contain e/ $\mu$  + E<sub>T,miss</sub> + multi-jets ( $\geq 2$  b-tagged)
- > In the framework of **NMSSM** covered  $m_a \in 20\text{-}60$  GeV
- > 8 categories from  $N_{\text{jets}}$  (3,4, $\geq 5$ ) mixed with  $N_{\text{b-tagged}}$  (2,3, $\geq 4$ )
  - 3 signal regions (3j,3b), (4j,3b), (4j,4b)
  - 5 control regions — tt background constraint
- > The Boosted Decision Tree (**BDT**) is trained to discriminate between signal events with an  $m_a$  of 60 GeV and tt events

## 8 event categories

ATLAS  
13 TeV, 3.2 fb<sup>-1</sup>

Legend:  
■ Non-tt  
■ tt + bb  
■ tt + c $\bar{c}$   
■ tt + light



## kinematic variables for BDT

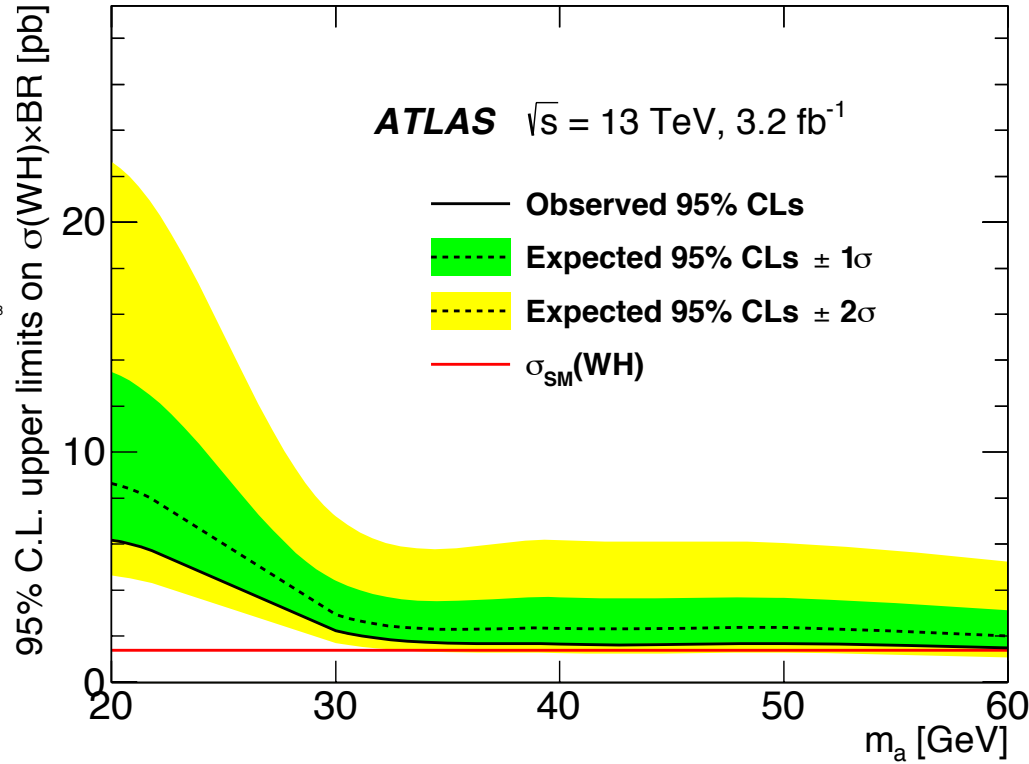
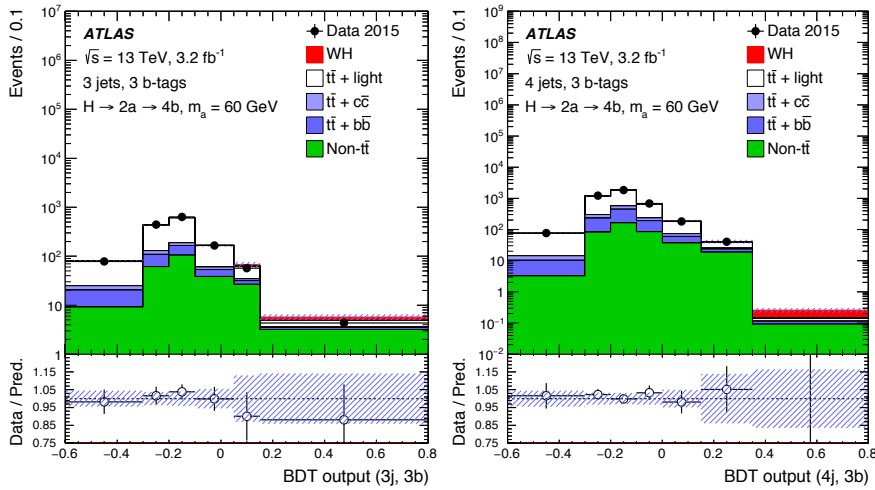
Region	$m_{bbb}$	$m_{bbbb}$	$\Delta m_{\text{min}}^{bb}$	$H_T$	$p_T^W$	$\Delta R_{\text{av}}^{bb}$	$\Delta R_{\text{min}}^{lb}$	$m_{bbj}$	$m_{T2}$
Signal	(3j, 3b)	✓		✓	✓	✓	✓		
	(4j, 3b)	✓		✓	✓	✓		✓	
	(4j, 4b)		✓	✓	✓	✓			✓
Control				✓					

# Wh $\rightarrow$ aa $\rightarrow$ 4b



13 TeV 3.2 fb<sup>-1</sup>

arXiv:1606.08391



Process	(3j, 3b)	(4j, 3b)	(4j, 4b)
$t\bar{t}$ + light	1089 $\pm$ 76	2940 $\pm$ 180	53 $\pm$ 16
$t\bar{t}$ + $c\bar{c}$	70 $\pm$ 28	280 $\pm$ 110	21 $\pm$ 11
$t\bar{t}$ + $b\bar{b}$	172 $\pm$ 55	610 $\pm$ 160	74 $\pm$ 15
$t\bar{t}$ + $\gamma$ /W/Z	0.8 $\pm$ 0.1	4 $\pm$ 1	0.4 $\pm$ 0.1
W + jets	93 $\pm$ 31	129 $\pm$ 40	2 $\pm$ 1
Z + jets	18 $\pm$ 12	14 $\pm$ 10	-
Single-top-quark	135 $\pm$ 13	208 $\pm$ 17	8 $\pm$ 1
Multijet	48 $\pm$ 20	67 $\pm$ 28	4 $\pm$ 2
Dibosons	4 $\pm$ 1	9 $\pm$ 1	0.6 $\pm$ 0.4
$t\bar{t}$ + H	0.7 $\pm$ 0.1	4 $\pm$ 1	0.8 $\pm$ 0.2
<b>Total</b>	<b>1640 <math>\pm</math> 58</b>	<b>4270 <math>\pm</math> 130</b>	<b>165 <math>\pm</math> 15</b>
Data	1646	4302	166
<i>WH, H <math>\rightarrow</math> 2a <math>\rightarrow</math> 4b</i>			
$m_a = 60$ GeV	10 $\pm$ 2	9 $\pm$ 1	3 $\pm$ 1
$m_a = 40$ GeV	11 $\pm$ 2	10 $\pm$ 2	2 $\pm$ 1
$m_a = 20$ GeV	6 $\pm$ 1	5 $\pm$ 1	0.7 $\pm$ 0.2

> The observed (expected) 95% CL upper limits range from 6.2 (8.6) pb for  $m_a = 20$  GeV, to 1.5 (2.0) pb for  $m_a = 60$  GeV

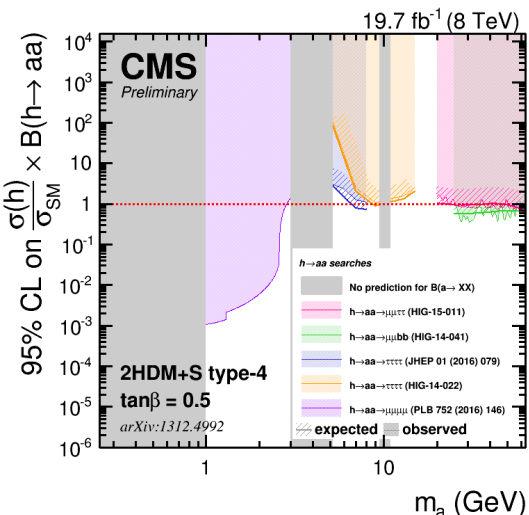
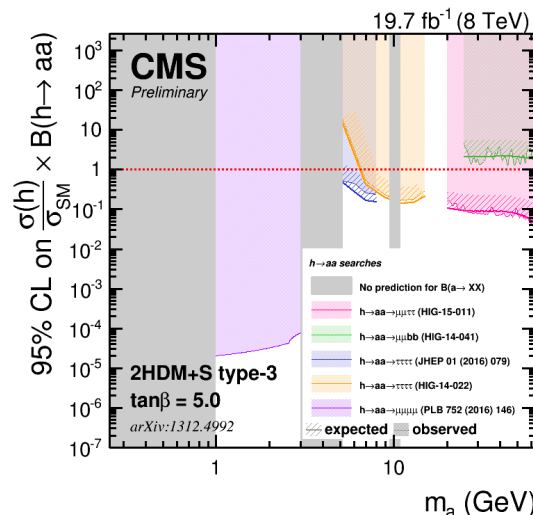
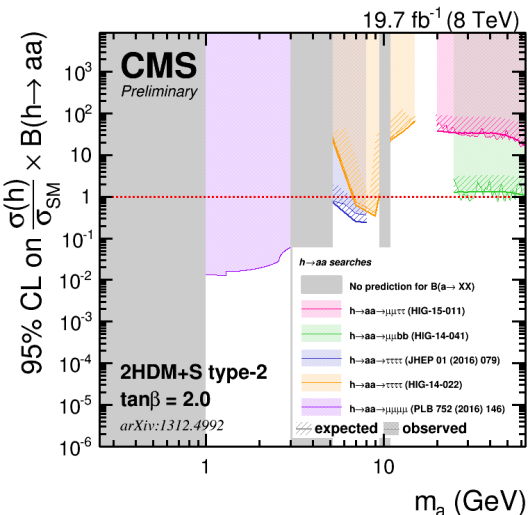
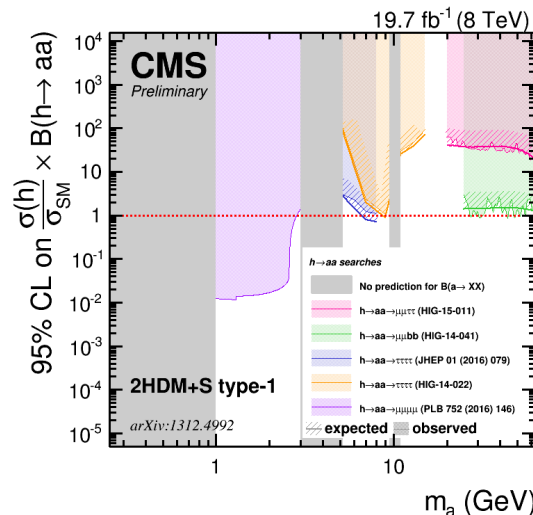
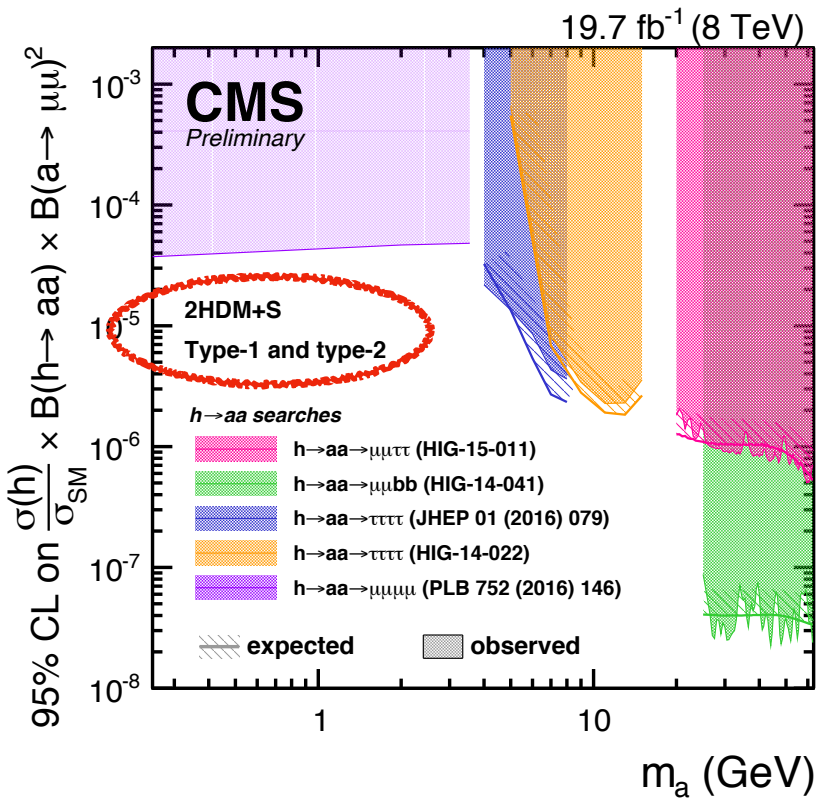
# $h \rightarrow aa$ in 2HDM+S



8 TeV 20 fb<sup>-1</sup>

CMS PAS HIG-16-015

Combined upper limits from different  $h \rightarrow aa$  searches in the context of "2HDM+S"



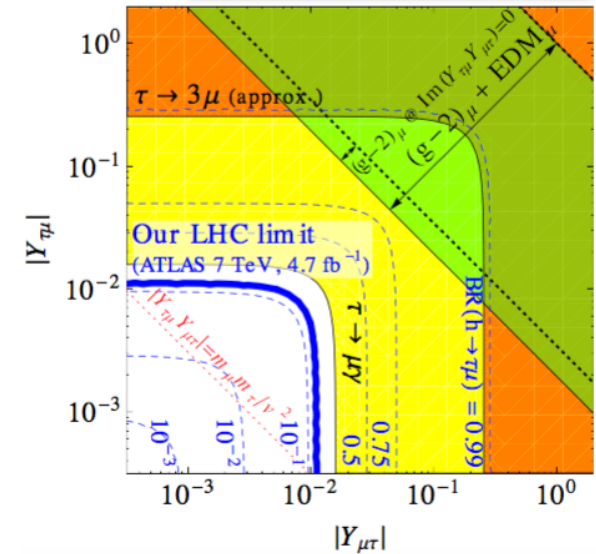
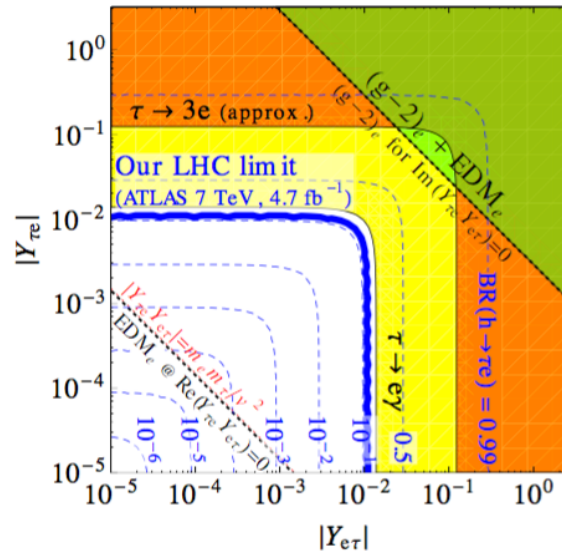
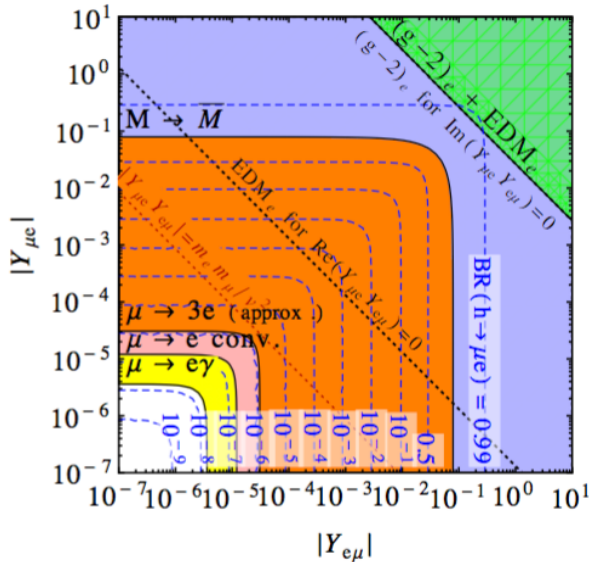
# Lepton-Flavor-Violating decays of $h(125)$



# LFV Higgs decays

- LFV Higgs couplings allow  $\mu \rightarrow e$ ,  $\tau \rightarrow \mu$ ,  $\tau \rightarrow e$  to proceed via a virtual Higgs boson
- **Indirect constraints** to branching ratios of  $H \rightarrow e\mu$ ,  $H \rightarrow e\tau$ ,  $H \rightarrow \mu\tau$  (theoretical approach by re-interpretation ATLAS 7 TeV results)

JHEP 03 (2013) 026



Stringent constraints from  $\mu \rightarrow e\gamma$   
 Indirect upper limit at 95% CL  
 **$Br(H \rightarrow \mu e) < O(10^{-8})$**

Bounds from  $\tau \rightarrow \mu\gamma$  and  $\tau \rightarrow e\gamma$  indirectly  
 provide upper limit at 95% CL  
 **$Br(H \rightarrow \mu\tau)$  and  $Br(H \rightarrow e\tau) < O(10\%)$**

# LFV Higgs (Run-1)



8 TeV 20 fb<sup>-1</sup>

## CMS results :

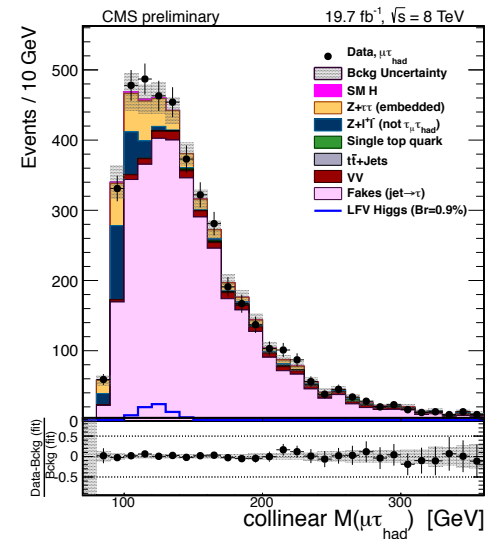
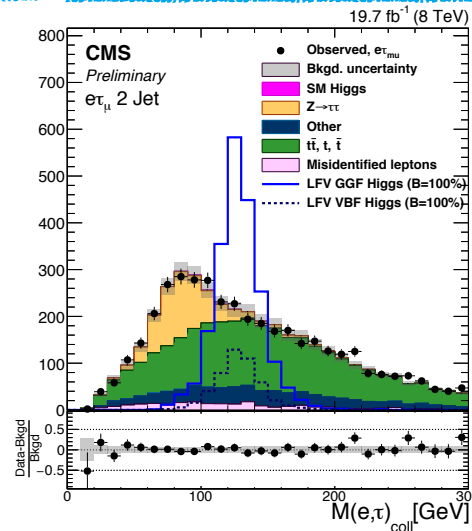
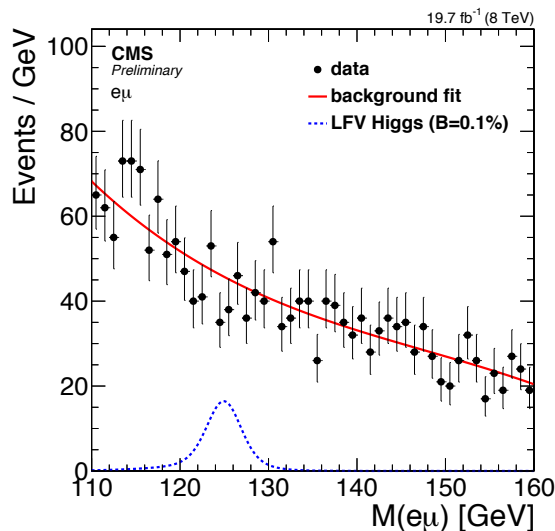
- > Similar signature to the SM  $H \rightarrow \tau\tau$  and  $\mu\mu$  searches but significant kinematic differences
- > Provide direct constraints on the off-diagonal Higgs Yukawa couplings

### $H \rightarrow e\mu$

- > Very clean but branching ratio strongly constrained!
- > 10 channels (barrel/endcap leptons mix with 0-1-2 jets)
- > unbinned likelihood fit to  $M_{e\mu}$  distribution

### $H \rightarrow e\tau$ and $\mu\tau$

- > 3 categories (0,1,2 jets) from both  $\tau_{had}$  and  $\tau_{lep}$
- > large background leads to high systematic uncertainties
- > binned likelihood fit to the distributions of  $M_{col}$  ( $m_H$  estimated with collinear approx.)

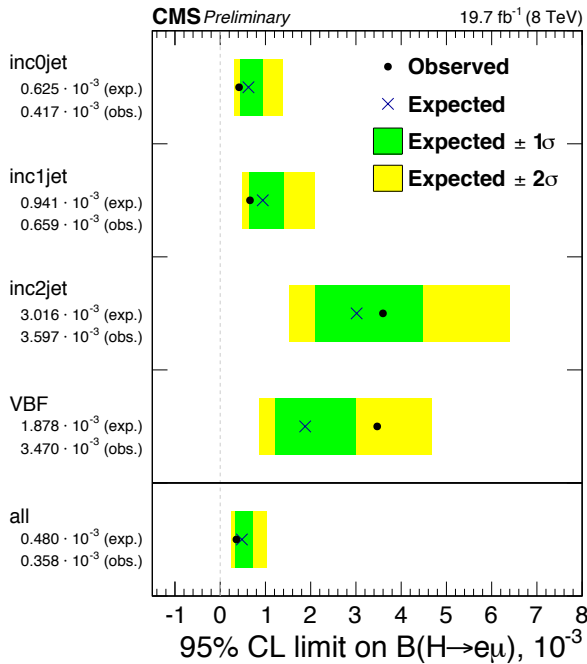


# LFV Higgs (Run-1)



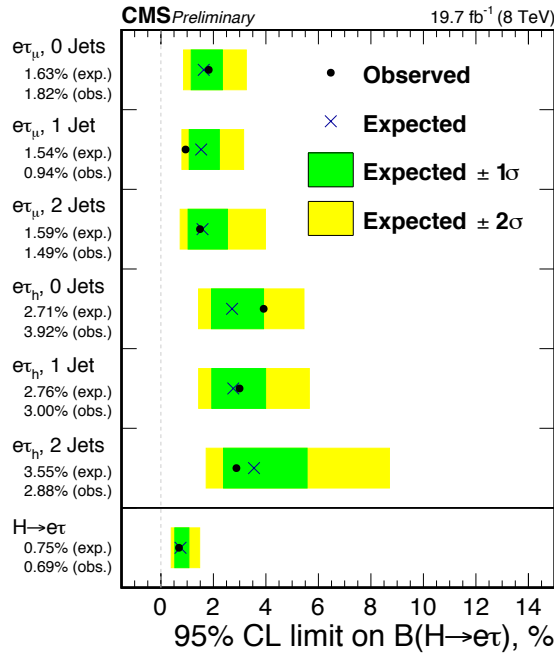
8 TeV 20 fb<sup>-1</sup>

CMS results :



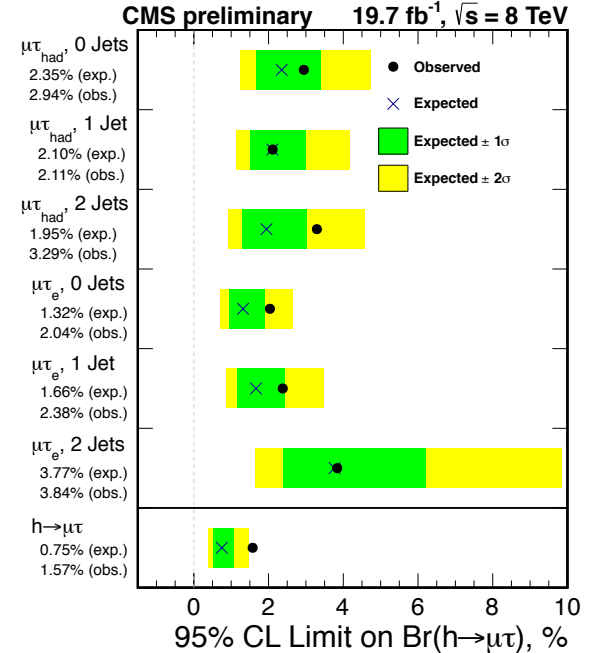
**BR(H → eμ) < 0.035%**  
(0.048% expected)

CMS PAS HIG-14-040  
arXiv:1607.03561



**BR(H → eτ) < 0.69%**  
(0.75% expected)

CMS PAS HIG-14-040  
arXiv:1607.03561



**BR(H → μτ) < 1.51%**  
(0.75% expected)

CMS PAS HIG-14-005  
arXiv:1502.07400

# LFV Higgs (Run-1)



8 TeV 20 fb<sup>-1</sup>

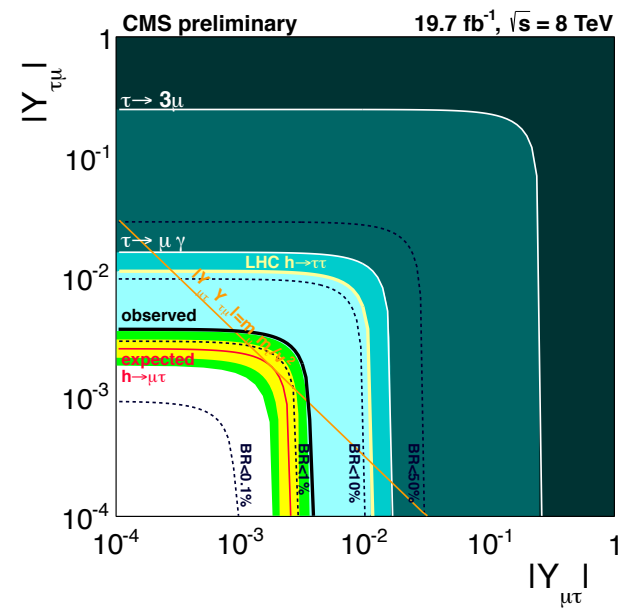
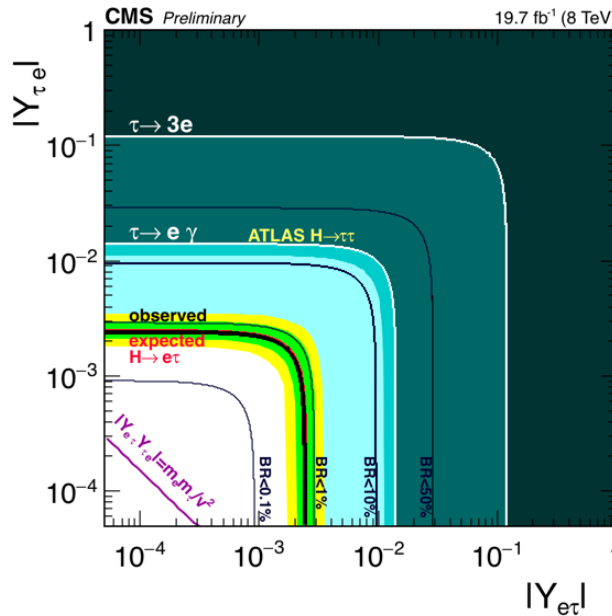
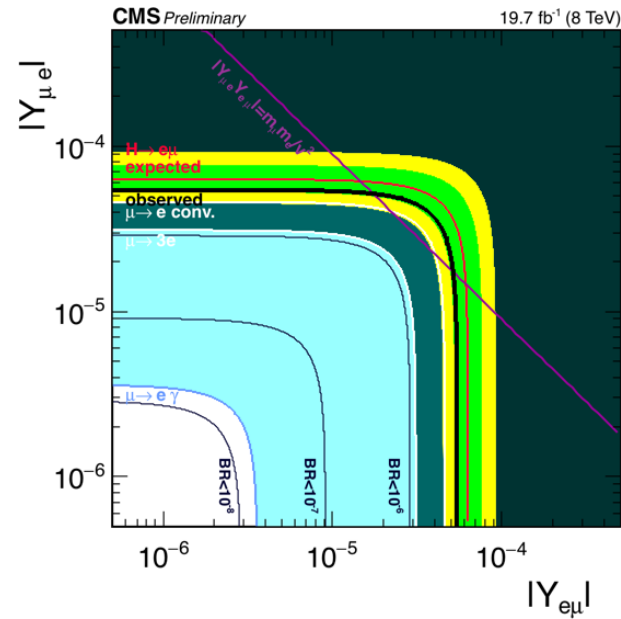
CMS results :

Bounds on the Higgs Yukawa couplings (theoretical no.)

$$H \rightarrow e\mu : \sqrt{|Y_{e\mu}|^2 + |Y_{\mu e}|^2} < 5.4 \times 10^{-4} (< 3.6 \times 10^{-6})$$

$$H \rightarrow e\tau : \sqrt{|Y_{e\tau}|^2 + |Y_{\tau e}|^2} < 0.0024 (< 0.014)$$

$$H \rightarrow \mu\tau : \sqrt{|Y_{\mu\tau}|^2 + |Y_{\tau\mu}|^2} < 0.0026 (< 0.016)$$



# LFV Higgs (Run-1)

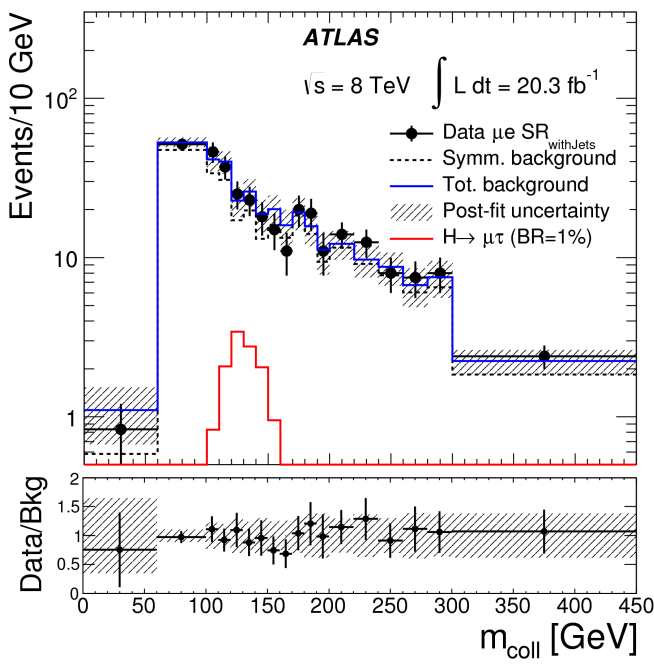
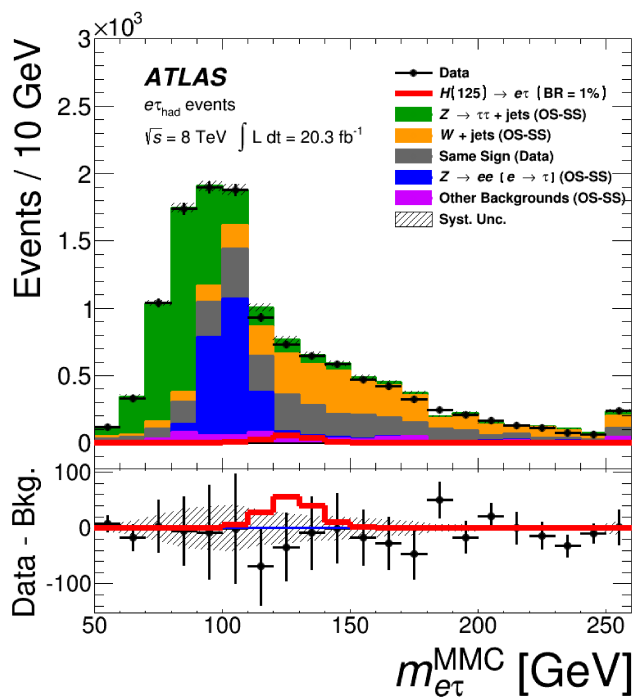
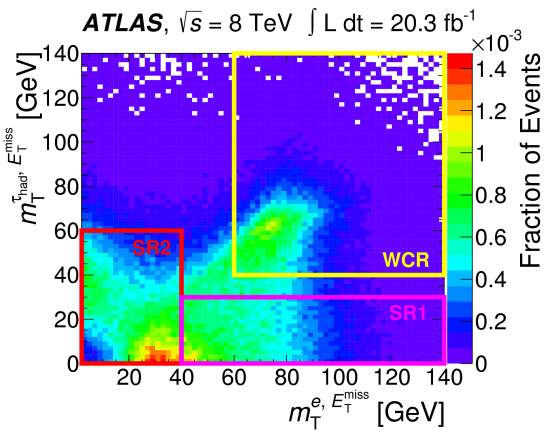


8 TeV 20 fb<sup>-1</sup>

## ATLAS results :

- Analyses performed for  $H \rightarrow e\tau$ ,  $H \rightarrow \mu\tau$  but slightly different for  $\tau_{had}$  and  $\tau_{lep}$ 
  - $e\tau_{had} + \mu\tau_{had}$  : opposite-sign, well-separated e/ $\mu$  with  $\tau_{had}$  plus  $E_{T,miss}$ ; two signal regions to fit missing mass calculator (MMC), reconstructed from e/ $\mu$ ,  $\tau_{had}$  and  $E_{T,miss}$
  - $e\tau_{\mu} + \mu\tau_e$  : opposite charge e+ $\mu$  with final discriminant of collinear mass ( $M_{col}$ )
- Binned likelihood fit on the distributions of MMC ( $\tau_{had}$ ) and  $M_{col}$  ( $\tau_{lep}$ )

JHEP 1511(2015)211  
arXiv:1604.07730



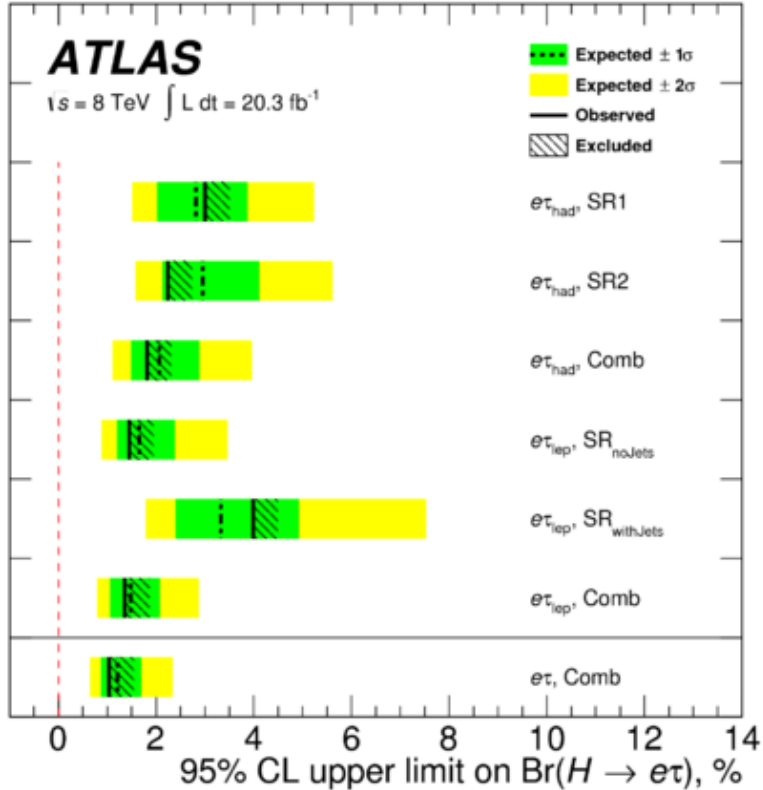
# LFV Higgs (Run-1)



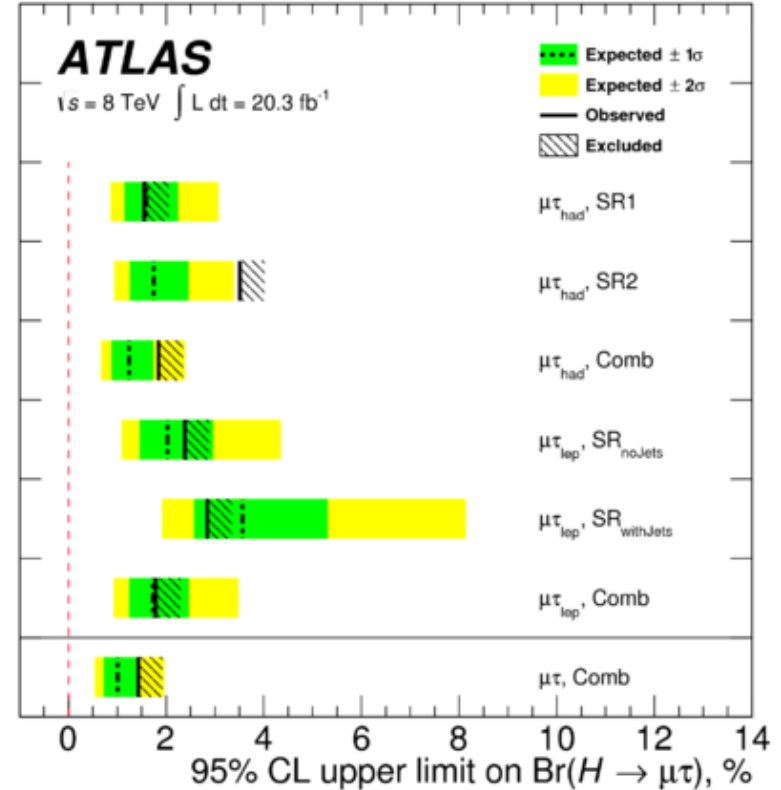
8 TeV 20 fb<sup>-1</sup>

ATLAS results :

arXiv:1604.07730



**Observed 95% CL upper limit**  
 $\text{BR}(H \rightarrow e\tau) < 1.04\%$   
 (1.21% expected)



**Observed 95% CL upper limit**  
 $\text{BR}(H \rightarrow \mu\tau) < 1.43\%$   
 (1.01% expected)



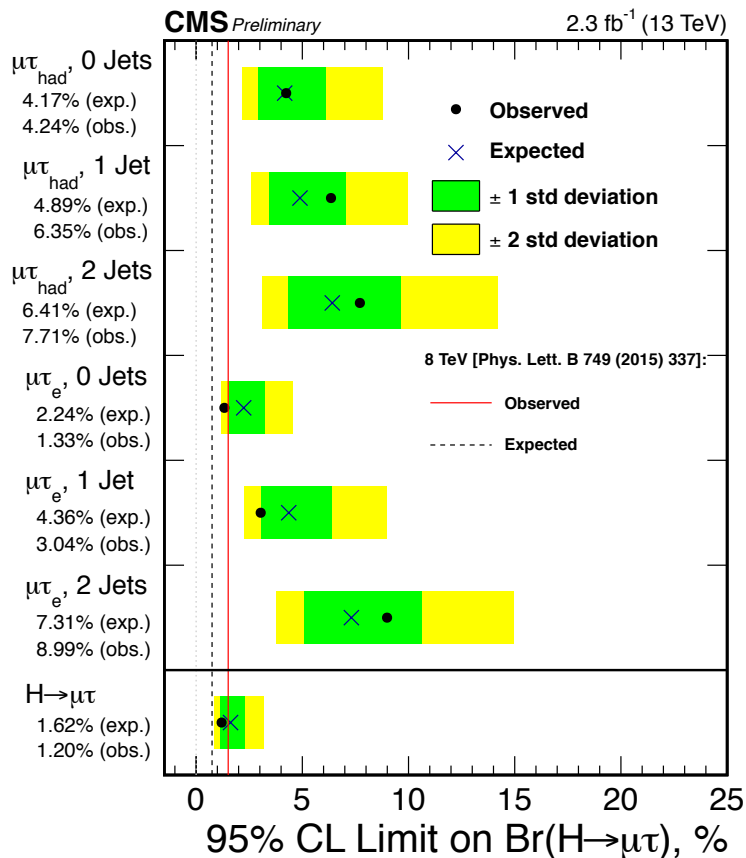
# LFV Higgs (Run-2)



13 TeV 2.3 fb<sup>-1</sup>

CMS results :

CMS PAS HIG-16-005



Expected limits				
	0-jet (%)	1-jet (%)	2-jets (%)	Combined (%)
$\mu\tau_h$	<4.17	<4.89	<6.41	<2.98
$\mu\tau_e$	<2.24	<4.36	<7.31	<1.96
$\mu\tau$	<1.62 %			

Observed limits				
	0-jet (%)	1-jet (%)	2-jets (%)	Combined (%)
$\mu\tau_h$	<4.24	<6.35	<7.71	<3.81
$\mu\tau_e$	<1.33	<3.04	<8.99	<1.15
$\mu\tau$	<1.20 %			

Best-fit branching fractions				
	0-jet (%)	1-jet (%)	2-jets (%)	Combined (%)
$\mu\tau_h$	$0.12^{+2.02}_{-1.91}$	$1.70^{+2.41}_{-2.52}$	$1.54^{+3.12}_{-2.71}$	$1.12^{+1.45}_{-1.40}$
$\mu\tau_e$	$-2.11^{+1.30}_{-1.89}$	$-2.18^{+1.99}_{-2.05}$	$2.04^{+2.96}_{-3.31}$	$-1.81^{+1.07}_{-1.32}$
$\mu\tau$	$-0.76^{+0.81}_{-0.84}$ %			

**BR(H→μτ) < 1.20% (1.62% expected)**  
**√|Y<sub>μτ</sub>|<sup>2</sup>+|Y<sub>τμ</sub>|<sup>2</sup> < 0.0032**

**No excess is observed**  
**(2.4σ at 8 TeV not confirmed but not excluded)**



# What next?



- > The discovery of the SM-like Higgs opens an era of **Precision Physics**
  - Exotic decays would be a strong sign of BSM physics
  - No excess is observed so far but significant results are found/provided
- > CMS and ATLAS enthusiastically broaden BSM Higgs searches to cover as many topics as possible using all 7, 8 and 13 TeV data
- > Keep your eyes peeled!
  - Stay tuned, many more physics results with Run-2 2016 full dataset ( $> 30 \text{ fb}^{-1}$ ) are on their ways ;-)
- > Enjoy the conference under sunny sky and nice beach :-)



# References



## > CMS Public Results

- <http://cms.web.cern.ch/org/cms-papers-and-results>
- <https://cds.cern.ch/collection/CMS%20Physics%20Analysis%20Summaries?ln=en>

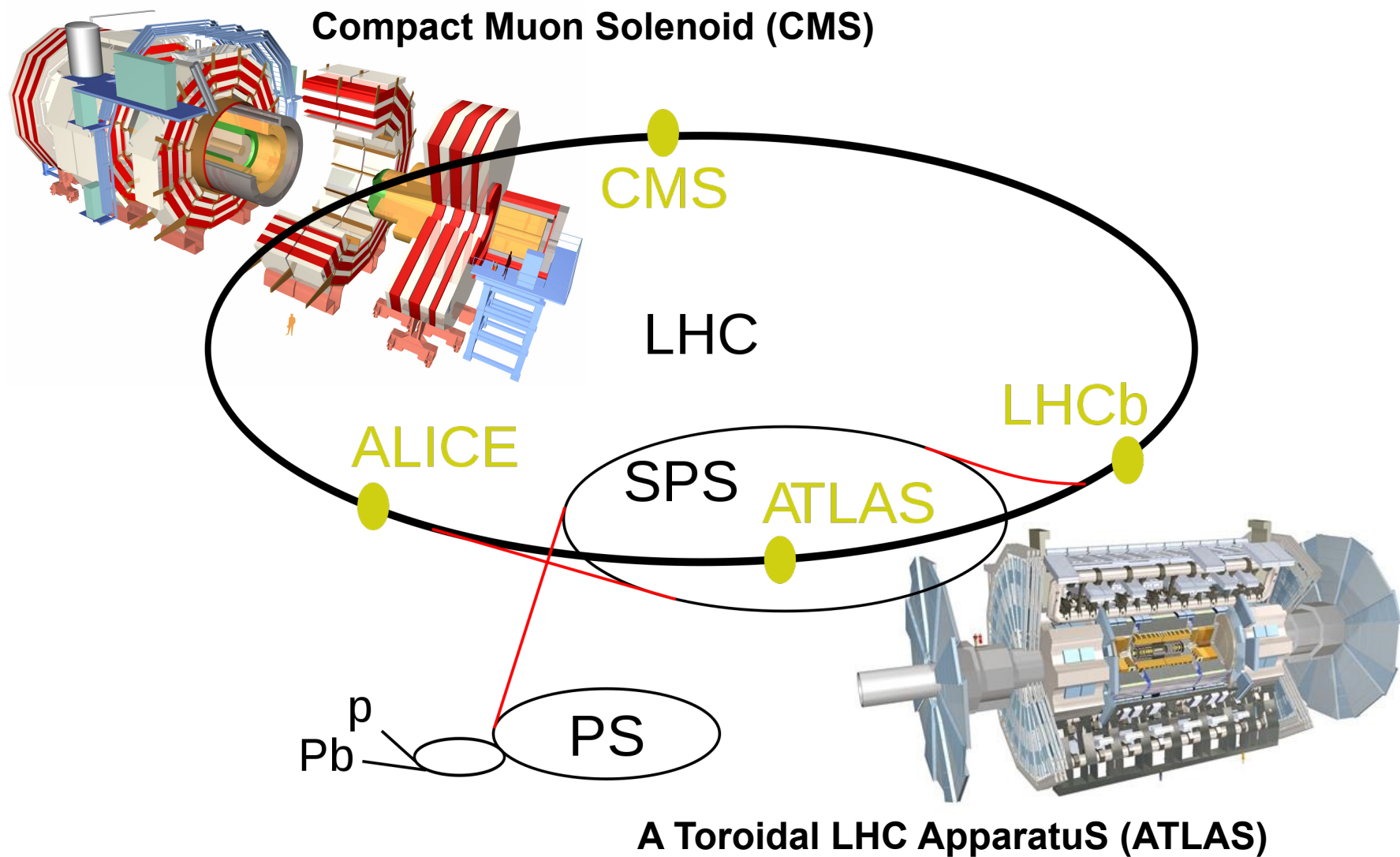
## > ATLAS Public Results

- <https://twiki.cern.ch/twiki/bin/view/AtlasPublic>
- <https://twiki.cern.ch/twiki/bin/view/AtlasPublic/CONFnotes>

# Backup



# Experiments at the LHC

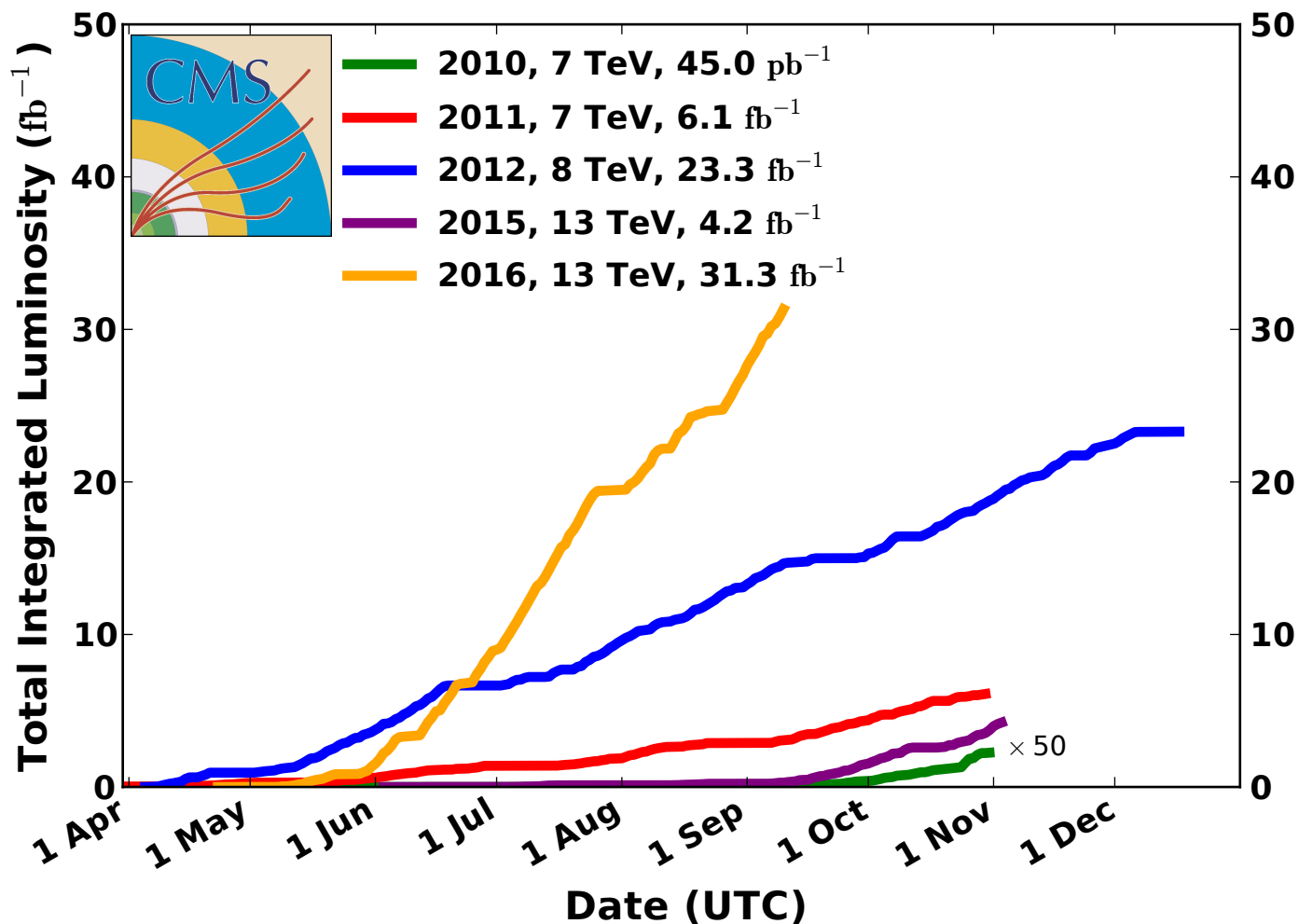


# Luminosity 2011-2016



## CMS Integrated Luminosity, pp

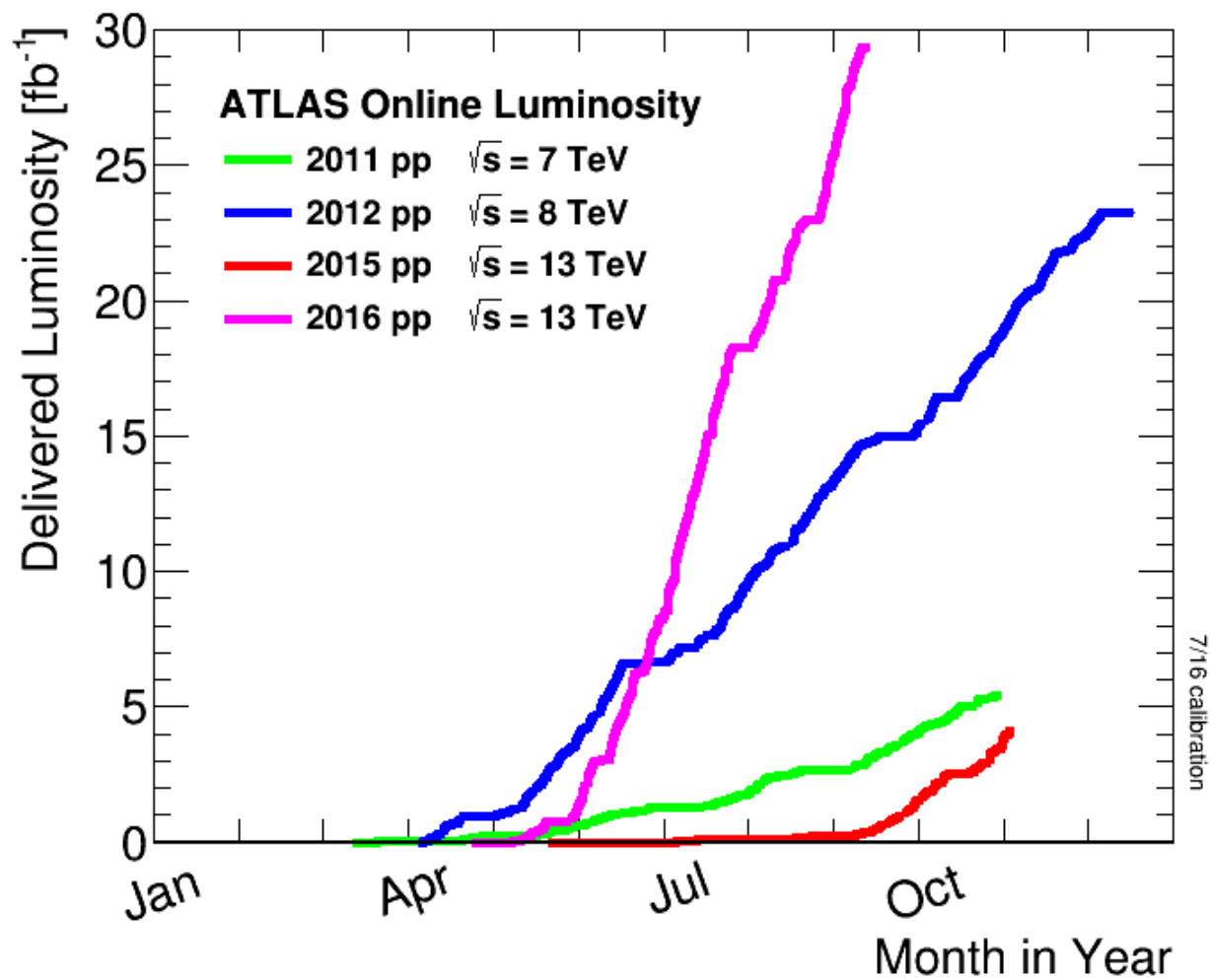
Data included from 2010-03-30 11:22 to 2016-09-09 22:19 UTC



# Luminosity 2011-2016



## ATLAS Integrated Luminosity, pp



# LFV indirect constraints



- Constraints on flavor violating Higgs couplings to  $e$ ,  $\mu$ ,  $\tau$  for a Higgs mass  $m_h = 125$  GeV and assuming that the flavor diagonal Yukawa couplings equal the SM values

Channel	Coupling	Bound
$\mu \rightarrow e\gamma$	$\sqrt{ Y_{\mu e} ^2 +  Y_{e\mu} ^2}$	$< 3.6 \times 10^{-6}$
$\mu \rightarrow 3e$	$\sqrt{ Y_{\mu e} ^2 +  Y_{e\mu} ^2}$	$\lesssim 3.1 \times 10^{-5}$
electron $g - 2$	$\text{Re}(Y_{e\mu}Y_{\mu e})$	$-0.019 \dots 0.026$
electron EDM	$ \text{Im}(Y_{e\mu}Y_{\mu e}) $	$< 9.8 \times 10^{-8}$
$\mu \rightarrow e$ conversion	$\sqrt{ Y_{\mu e} ^2 +  Y_{e\mu} ^2}$	$< 1.2 \times 10^{-5}$
$M-\bar{M}$ oscillations	$ Y_{\mu e} + Y_{e\mu}^* $	$< 0.079$
$\tau \rightarrow e\gamma$	$\sqrt{ Y_{\tau e} ^2 +  Y_{e\tau} ^2}$	$< 0.014$
$\tau \rightarrow 3e$	$\sqrt{ Y_{\tau e} ^2 +  Y_{e\tau} ^2}$	$\lesssim 0.12$
electron $g - 2$	$\text{Re}(Y_{e\tau}Y_{\tau e})$	$[-2.1 \dots 2.9] \times 10^{-3}$
electron EDM	$ \text{Im}(Y_{e\tau}Y_{\tau e}) $	$< 1.1 \times 10^{-8}$
$\tau \rightarrow \mu\gamma$	$\sqrt{ Y_{\tau\mu} ^2 +  Y_{\mu\tau} ^2}$	$0.016$
$\tau \rightarrow 3\mu$	$\sqrt{ Y_{\tau\mu} ^2 +  Y_{\mu\tau} ^2}$	$\lesssim 0.25$
muon $g - 2$	$\text{Re}(Y_{\mu\tau}Y_{\tau\mu})$	$(2.7 \pm 0.75) \times 10^{-3}$
muon EDM	$\text{Im}(Y_{\mu\tau}Y_{\tau\mu})$	$-0.8 \dots 1.0$
$\mu \rightarrow e\gamma$	$( Y_{\tau\mu}Y_{e\tau} ^2 +  Y_{\mu\tau}Y_{\tau e} ^2)^{1/4}$	$< 3.4 \times 10^{-4}$

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$$\Gamma(\text{H} \rightarrow \ell^\alpha \ell^\beta) = \frac{m_{\text{H}}}{8\pi} (|Y_{\ell^\beta \ell^\alpha}|^2 + |Y_{\ell^\alpha \ell^\beta}|^2),$$

$$B(\text{H} \rightarrow \ell^\alpha \ell^\beta) = \frac{\Gamma(\text{H} \rightarrow \ell^\alpha \ell^\beta)}{\Gamma(\text{H} \rightarrow \ell^\alpha \ell^\beta) + \Gamma_{\text{SM}}}.$$