

NLO QCD+EW for Dark Matter Backgrounds



**Universität
Zürich^{UZH}**

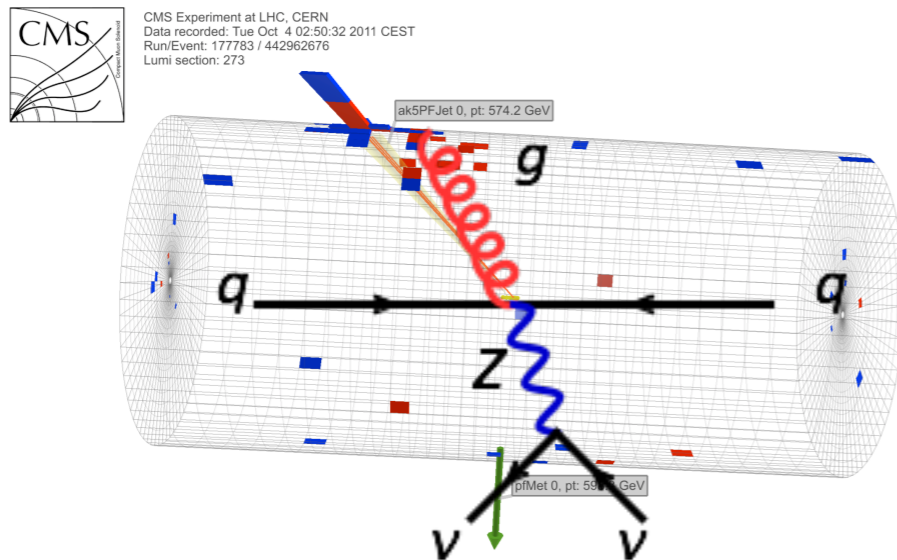
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work in collaboration with:

S. Kallweit, P. Maierhöfer, S. Pozzorini, M. Schönherr

LHC Dark Matter WG, CERN, 20.09.2016

V+jets backgrounds in monojet/MET + jets searches



irreducible background:

$$pp \rightarrow Z(\rightarrow \nu\bar{\nu}) + \text{jets} \Rightarrow \text{MET} + \text{jets}$$

$$pp \rightarrow W(\rightarrow l\nu) + \text{jets} \Rightarrow \text{MET} + \text{jets} \text{ (lepton lost)}$$

► can be determined from $Z(\rightarrow l\bar{l}) + \text{jets}$, $W(\rightarrow l\nu) + \text{jets}$ or $\gamma + \text{jets}$ measurements (combination!)

- hardly any systematics (just QED dressing)
- but: limited statistics at large p_T

- fairly large data samples at large p_T

► need theory input, i.e. predictions at (N)NLO QCD+NLO EW:

$$R_{ZZ}(dp_T) = \frac{d\sigma(Z \rightarrow \nu\bar{\nu} + \text{jets})/dp_T}{d\sigma(Z \rightarrow l\bar{l} + \text{jets})/dp_T} \quad R_{ZW}(dp_T) = \frac{d\sigma(Z \rightarrow \nu\bar{\nu} + \text{jets})/dp_T}{d\sigma(W \rightarrow l\nu + \text{jets})/dp_T} \quad R_{Z\gamma}(dp_T) = \frac{d\sigma(Z \rightarrow \nu\bar{\nu} + \text{jets})/dp_T}{d\sigma(\gamma + \text{jets})/dp_T}$$

Z/γ + 1 jet: exclusive

Setup:

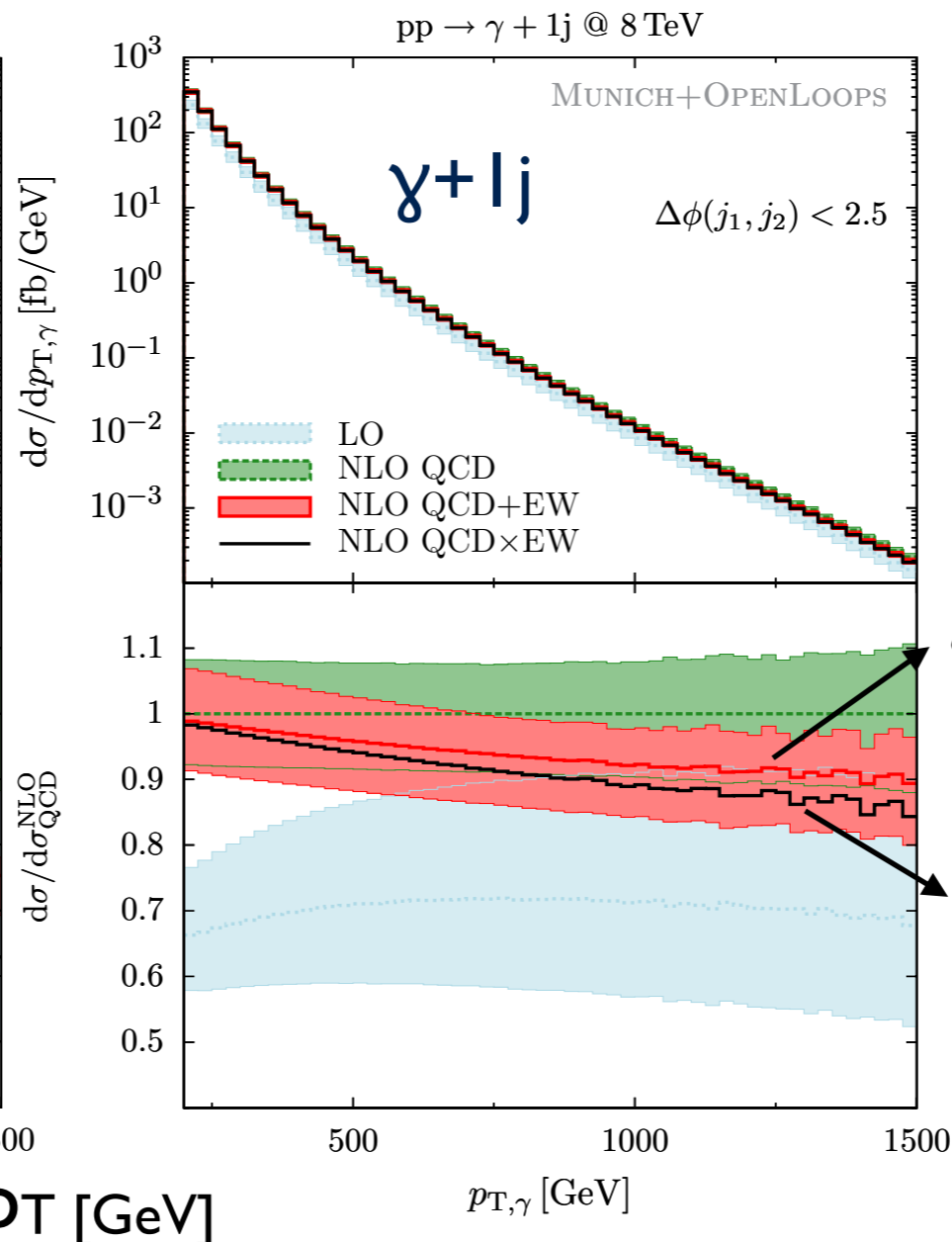
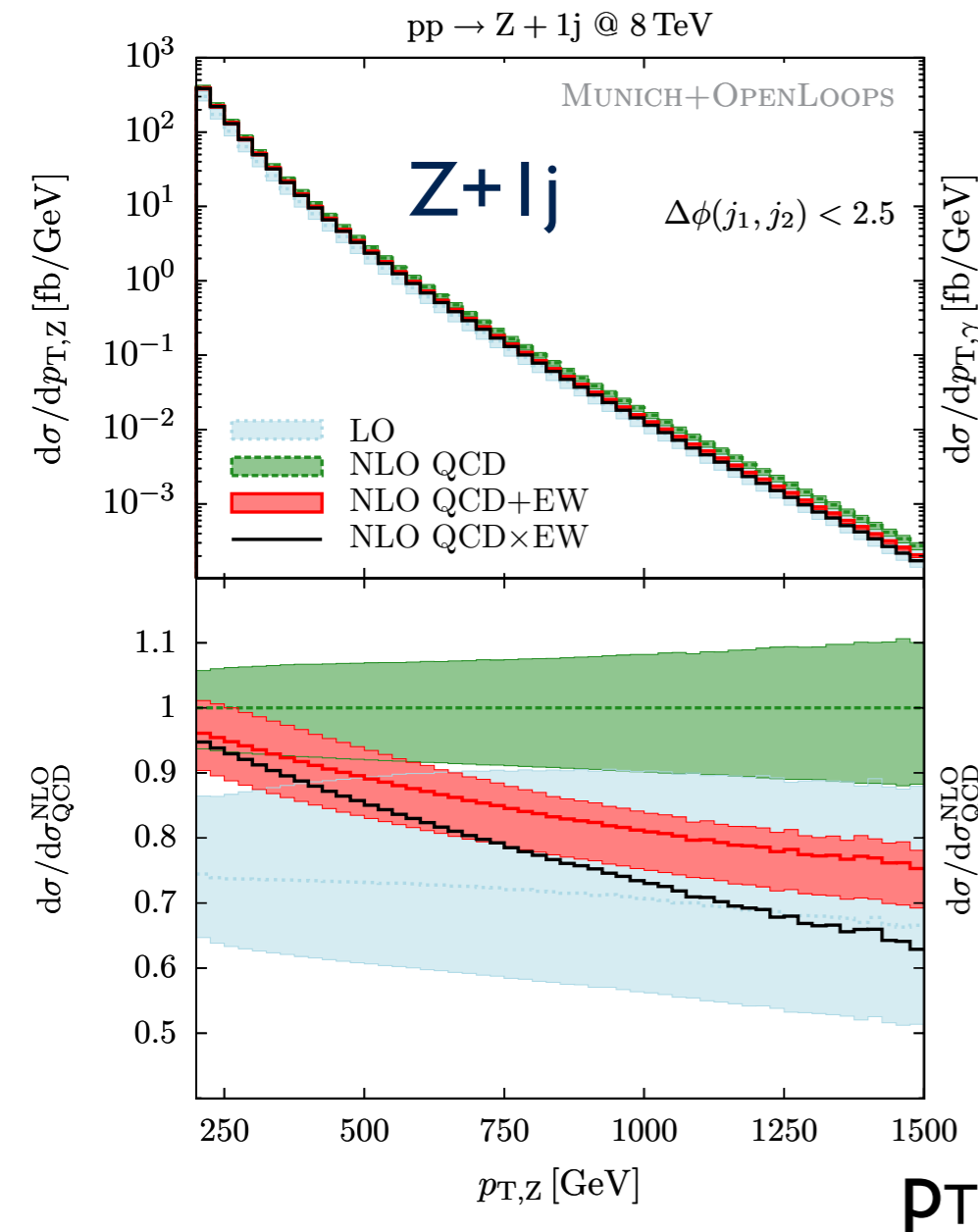
$$\sqrt{S} = 8 \text{ TeV}$$

$$p_{T,j} > 110 \text{ GeV}, \quad |\eta_j| < 2.4$$

$$\mu_0 = \hat{H}_T/2 \text{ (+ 7-pt. variation)}$$

$$\Delta\phi_{j_1 j_2} < 2.5$$

Frixione-Isolation with $dR=0.3$



$$\sigma_{\text{QCD+EW}}^{\text{NLO}} = \sigma^{\text{LO}} + \delta\sigma_{\text{QCD}}^{\text{NLO}} + \delta\sigma_{\text{EW}}^{\text{NLO}}$$

$$\sigma_{\text{QCD}\times\text{EW}}^{\text{NLO}} = \sigma_{\text{QCD}}^{\text{NLO}} \left(1 + \frac{\delta\sigma_{\text{EW}}^{\text{NLO}}}{\sigma^{\text{LO}}} \right) = \sigma_{\text{EW}}^{\text{NLO}} \left(1 + \frac{\delta\sigma_{\text{QCD}}^{\text{NLO}}}{\sigma^{\text{LO}}} \right)$$

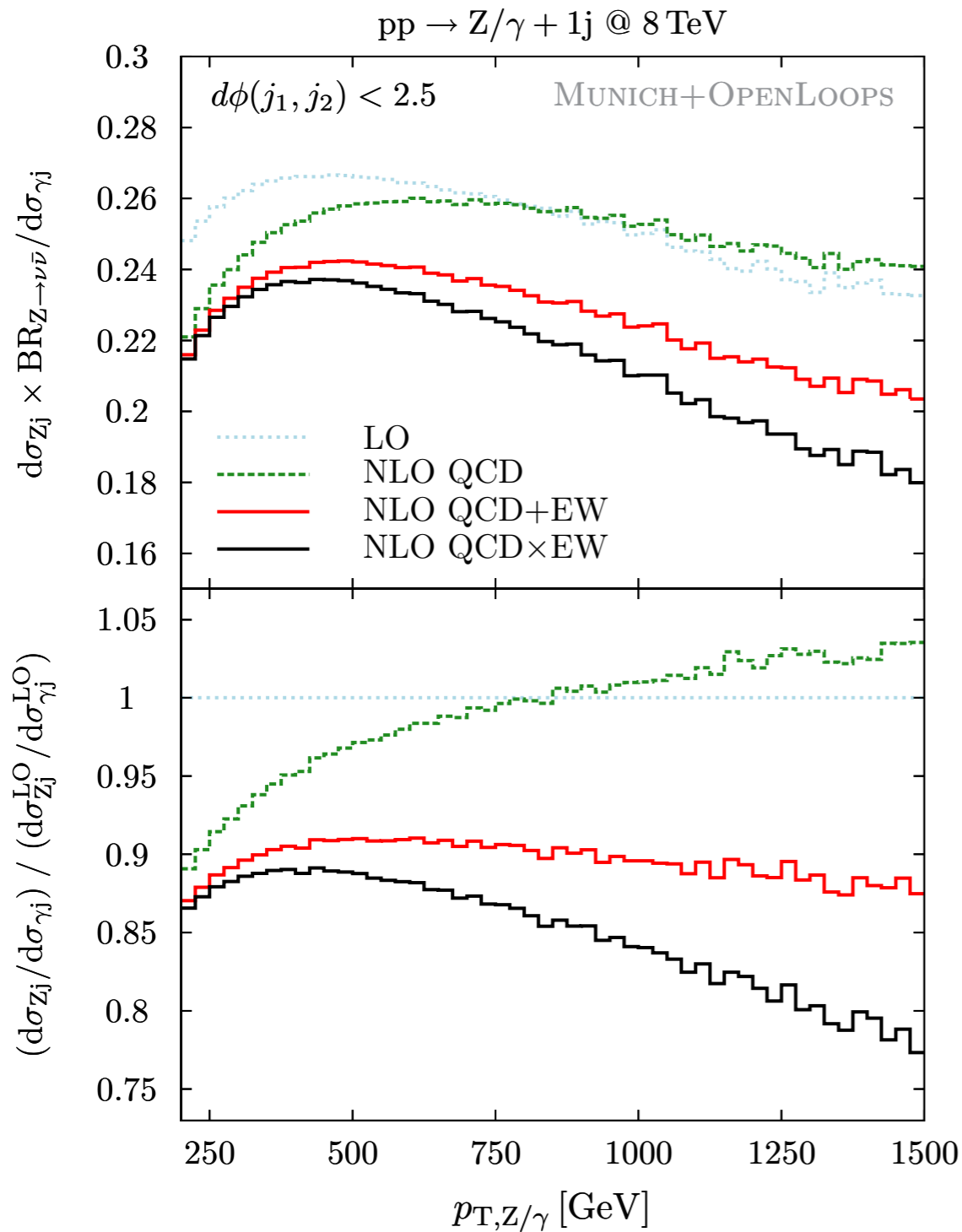
QCD corrections

- ▶ mostly moderate and stable QCD corrections
- ▶ (almost) **identical QCD corrections in the tail**, sizeable differences for small p_T (mass effects)

EW corrections

- ▶ **correction in $p_T(\text{Z}) >$ correction in $p_T(\gamma)$**
- ▶ -20/-8% EW for Z/γ at 1 TeV
- ▶ EW corrections $>$ QCD uncertainties for $p_{T,Z} > 350 \text{ GeV}$

Z/γ + 1 jet: pT-ratio



Overall

- ▶ mild dependence on the boson pT

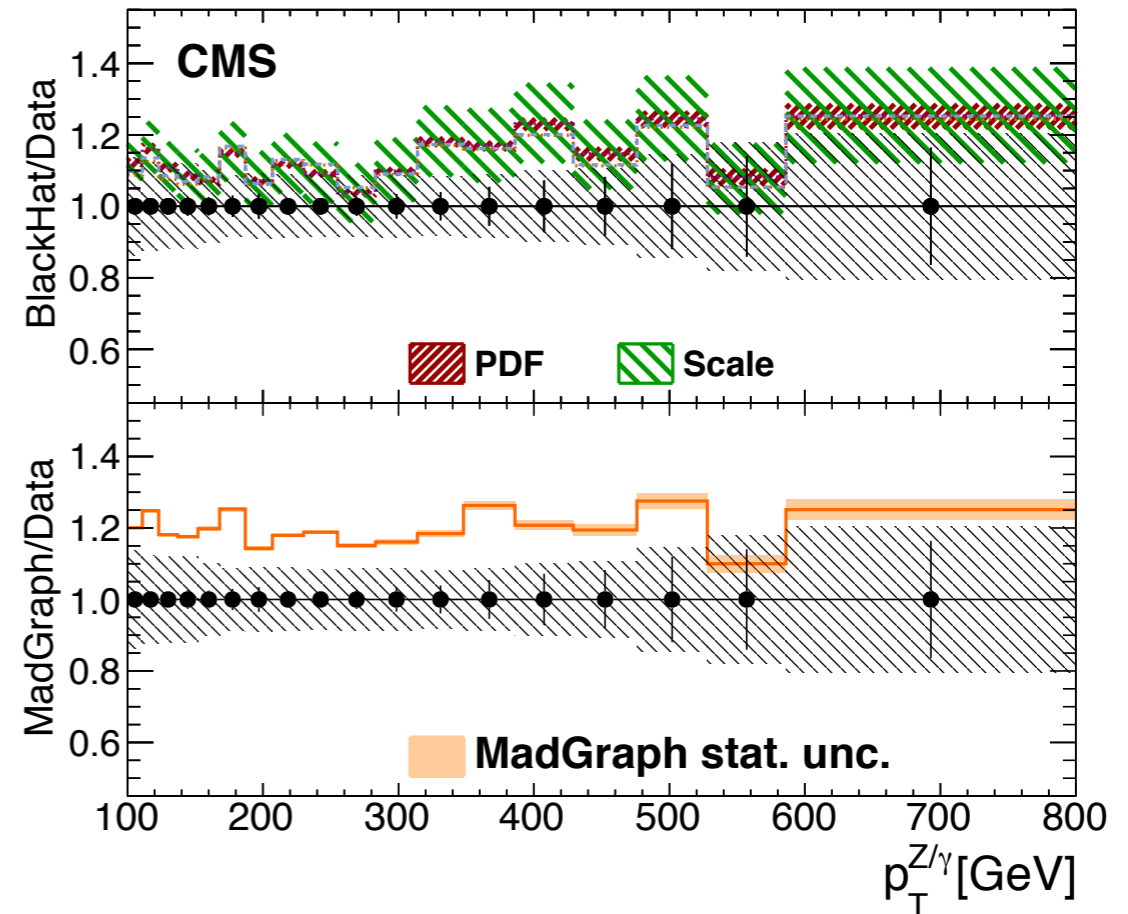
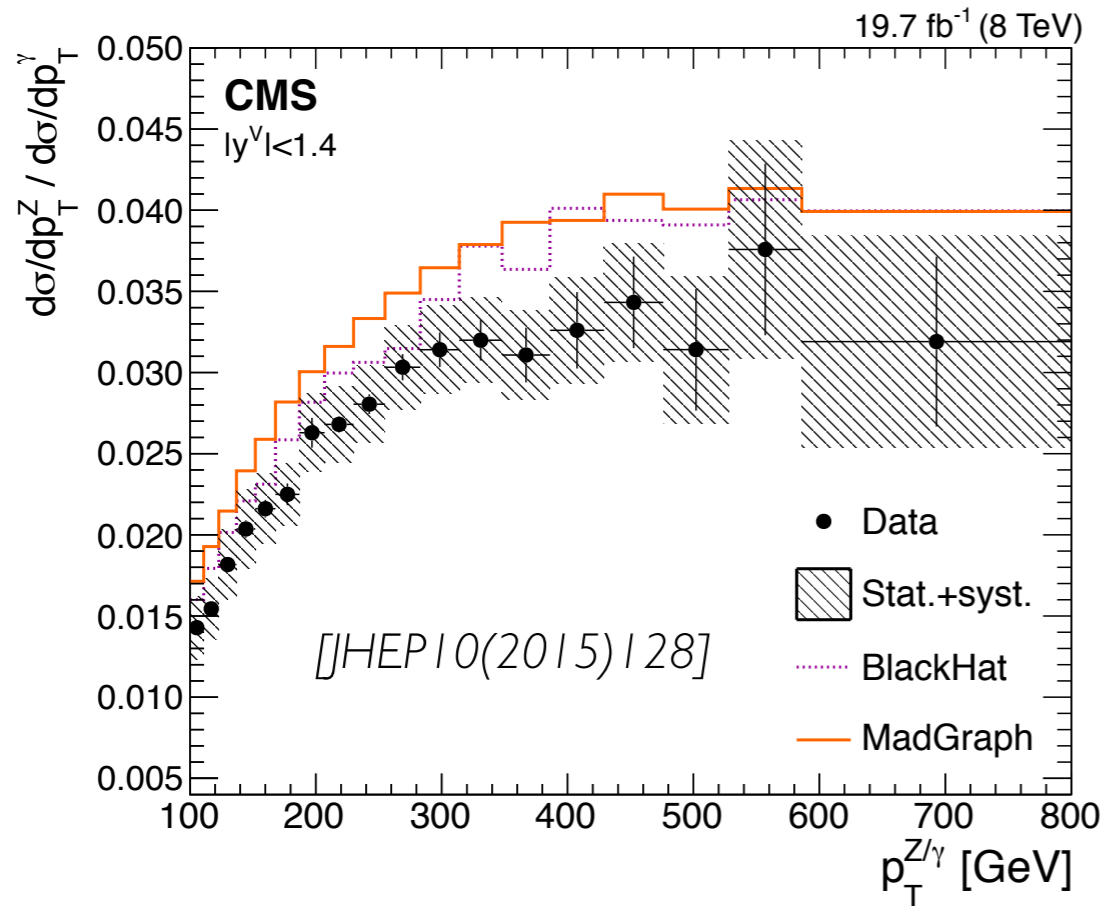
QCD corrections

- ▶ 10-15% below 250 GeV
- ▶ $\approx 5\%$ above 350 GeV

EW corrections

- ▶ sizeable difference in EW corrections results in 10-15% corrections at several hundred GeV
- ▶ $\sim 5\%$ difference between NLO QCD+EW and NLO QCD×EW

Compare against data

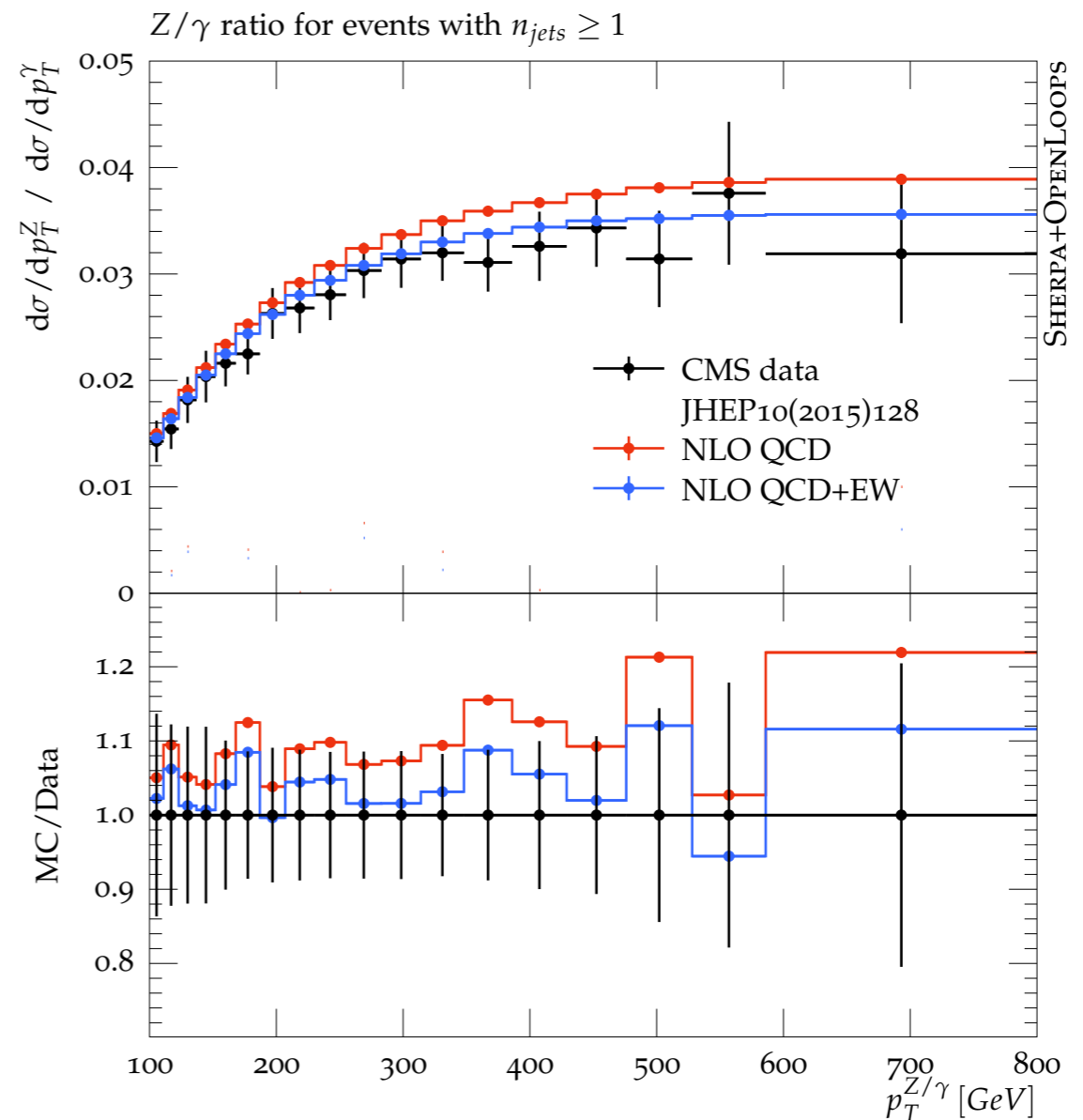
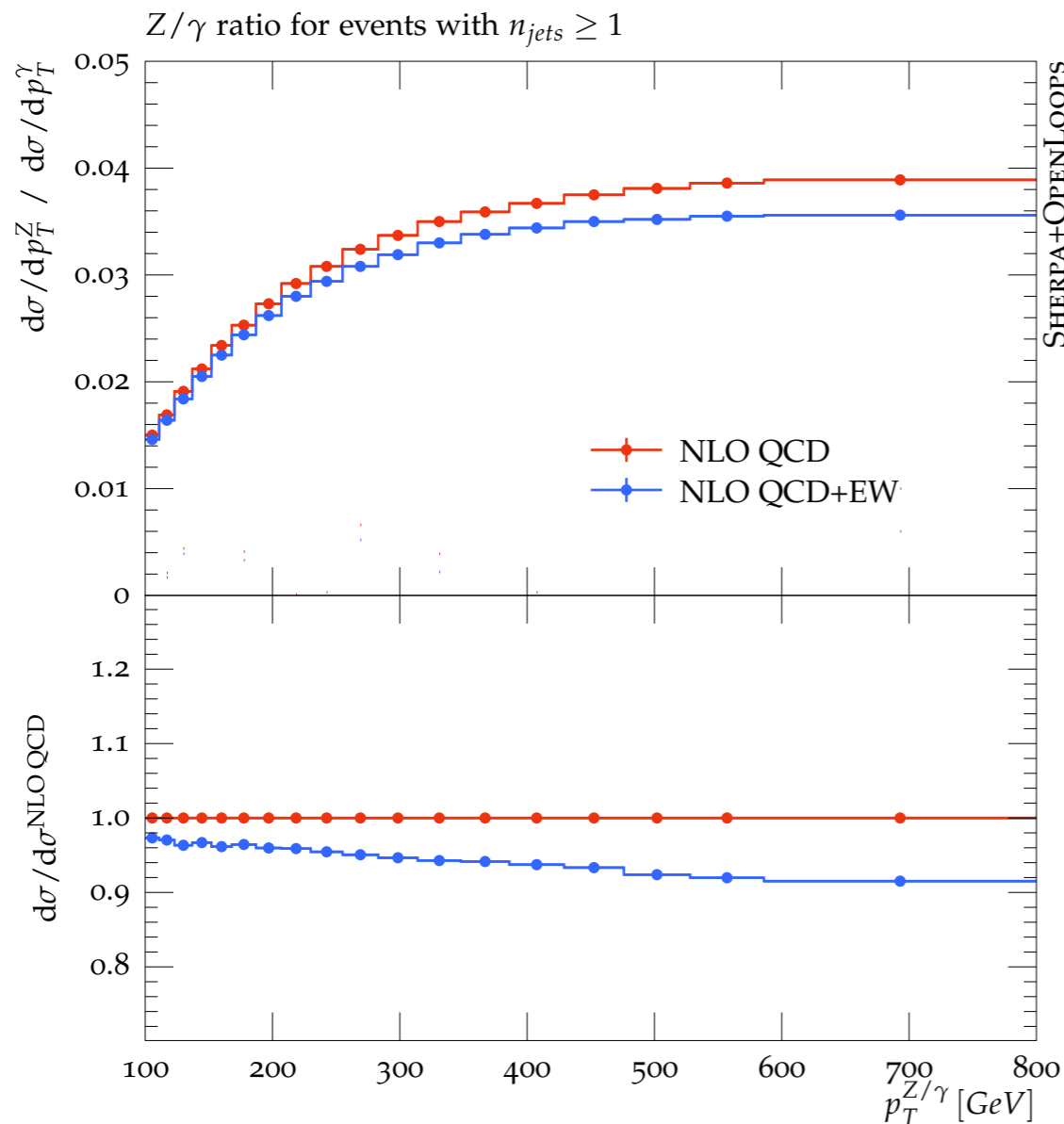


- ▶ constant off-set with respect to LO
- ▶ improved agreement at NLO QCD for small p_T

Compare against data

Frixione-Isolation with $\epsilon = 0.025$
 $\delta_0 = 0.4$

“a Frixione cone with these choices mimics the selections in the true on-shell photon definition at particle level”
[JHEP10(2015)128]



[Ciulli, Kallweit, JML, Pozzorini, Schönherr for **LH'15**]

- ▶ remarkable agreement with data at @ NLO **QCD+EW!**

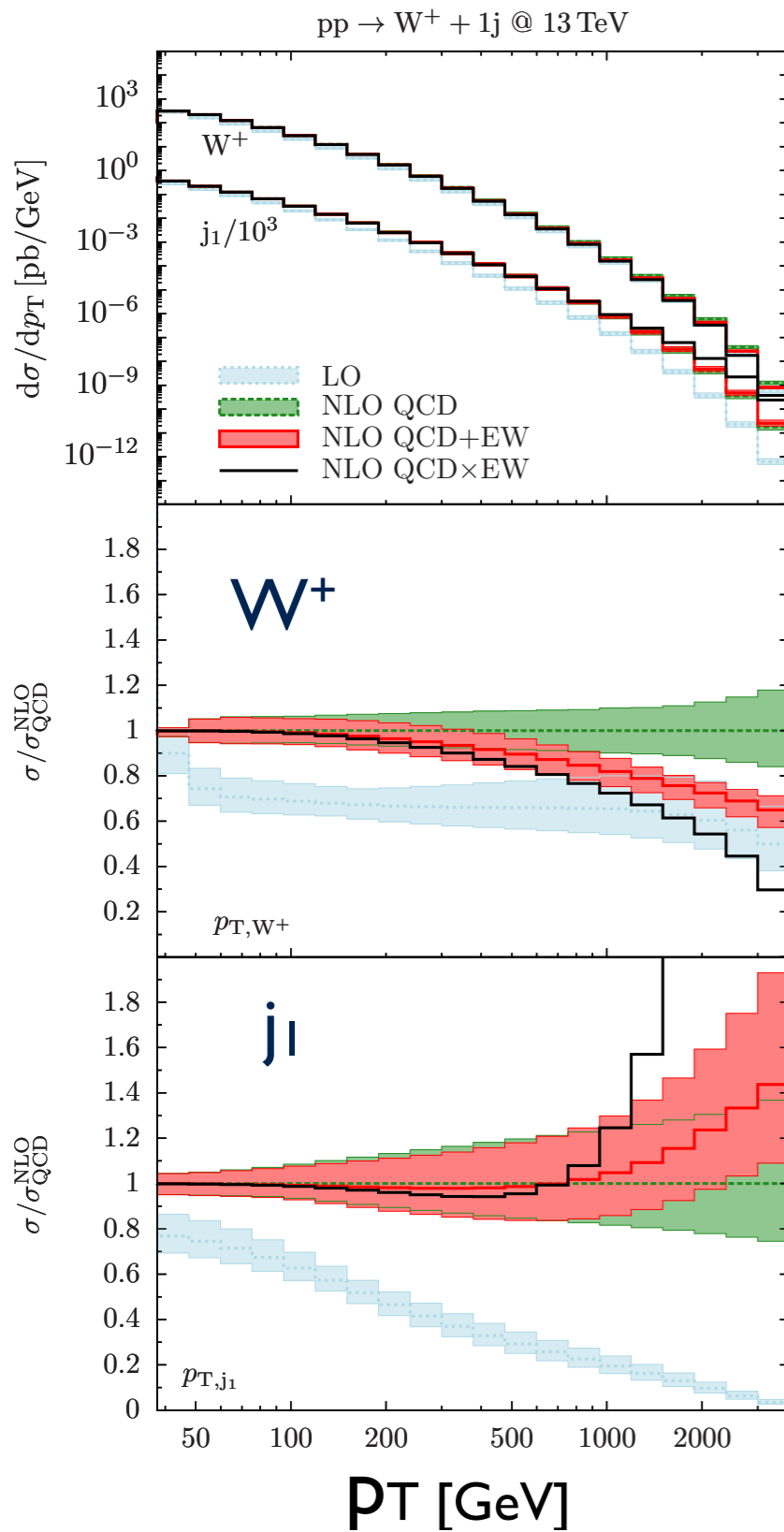
Open Questions

- Uncertainty of such a ratio?
(QCD uncertainties should be *fairly* correlated)
- Dependence on jet multiplicity?
- Impact of jet cuts?

... let's first discuss V+jets @ NLO QCD+EW on more general grounds!

$W^+ + 1 \text{ jet}$: inclusive

Setup:
 $\sqrt{S} = 13 \text{ TeV}$
 $p_{T,j} > 30 \text{ GeV}, \quad |\eta_j| < 4.5$
 $\mu_0 = \hat{H}_T/2 \text{ (+ 7-pt. variation)}$



inclusive

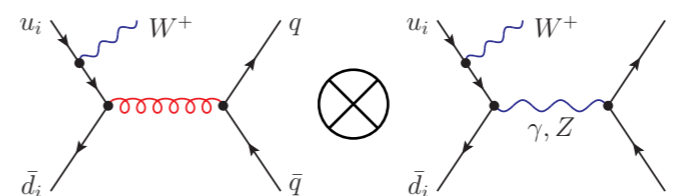
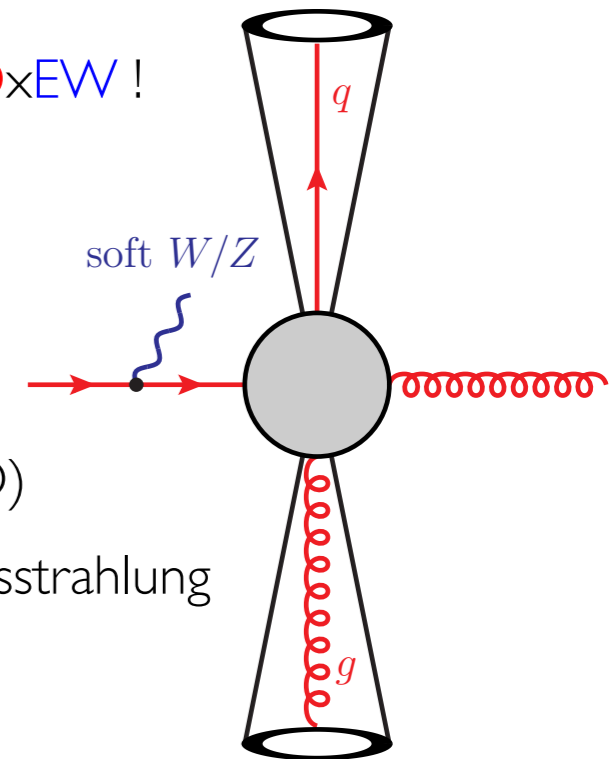
$\approx 1\%$ EW corrections

p_T of W-boson

- ▶ +100% **QCD** corrections in the tail
- ▶ large negative **EW** corrections due to **Sudakov behaviour**: -20–35% corrections at 1–4 TeV
- ▶ sizeable difference between **QCD+EW** and **QCDxEW**!

p_T of jet

- ▶ factor-10 NLO **QCD** corrections in the tail!
- ▶ dominated by **dijet configurations** (effectively LO)
- ▶ positive 10–50% EW corrections from quark bremsstrahlung



\Rightarrow pathologic with large uncertainties!

[Kallweit, Maierhöfer, JML, Pozzorini, Schönherr, '14]

$W^+ + 1 \text{ jet: exclusive}$

$$\Delta\phi_{j_1 j_2} < 3\pi/4$$

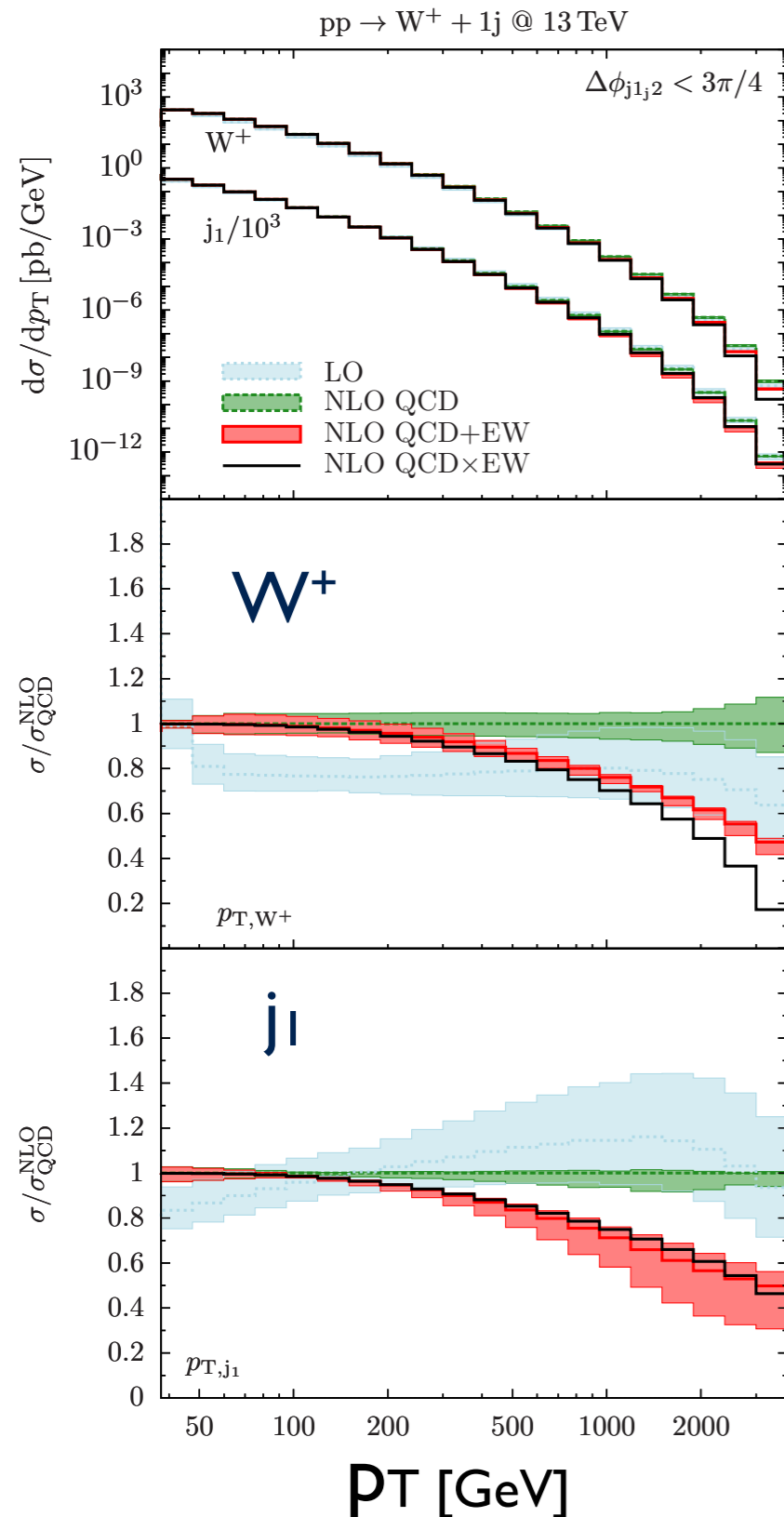
(veto on dijet configurations)

Setup:

$$\sqrt{S} = 13 \text{ TeV}$$

$$p_{T,j} > 30 \text{ GeV}, \quad |\eta_j| < 4.5$$

$$\mu_0 = \hat{H}_T/2 \text{ (+ 7-pt. variation)}$$



QCD corrections

- ▶ mostly moderate and stable QCD corrections

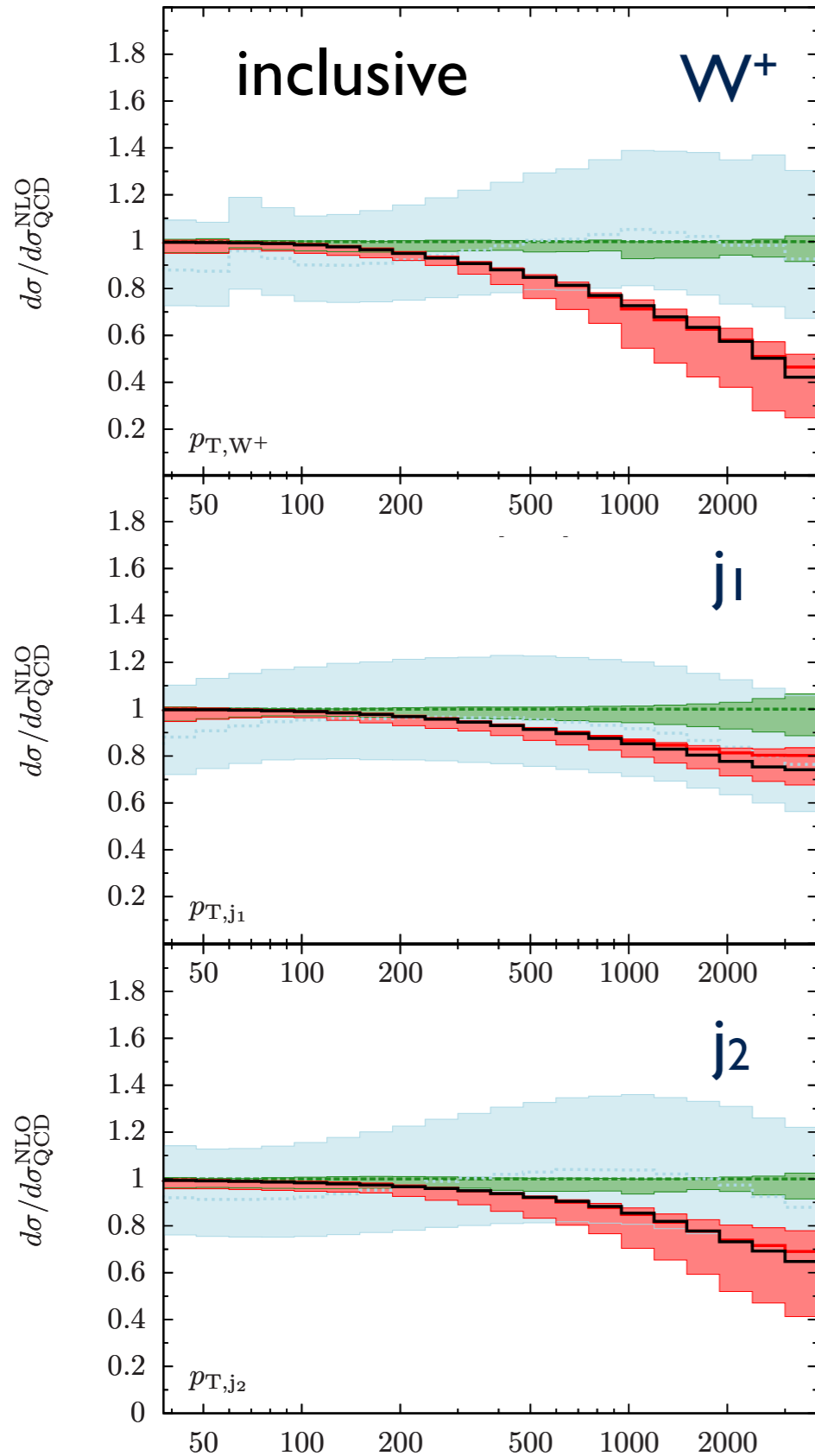
EW corrections

- ▶ **Sudakov behaviour** in both tails:
-20–50% EW corrections at 1–4 TeV
- ▶ EW corrections larger than QCD uncertainties for $p_{T,W^+} > 300 \text{ GeV}$

⇒ *exclusive* $W^+ 1 \text{ jet}$ ok!

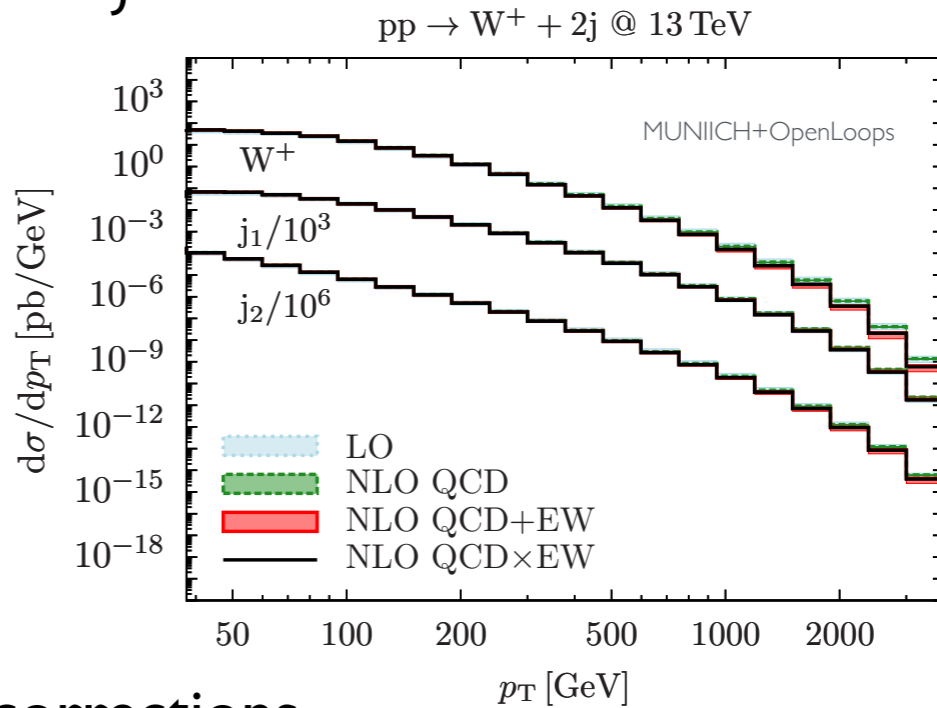
⇒ *inclusive* $W^+ 1 \text{ jet}$ requires $W^+ 2 \text{ jets}$ at NLO QCD+EW!

$W^+ + 2 \text{ jets}$



[Kallweit, Maierhöfer, JML, Pozzorini, Schönherr, '14]

p_T



QCD corrections

- ▶ small and very stable
- ▶ $\approx 10\%$ scale uncertainties

EW corrections

- ▶ **Sudakov behaviour** in all p_T tails:

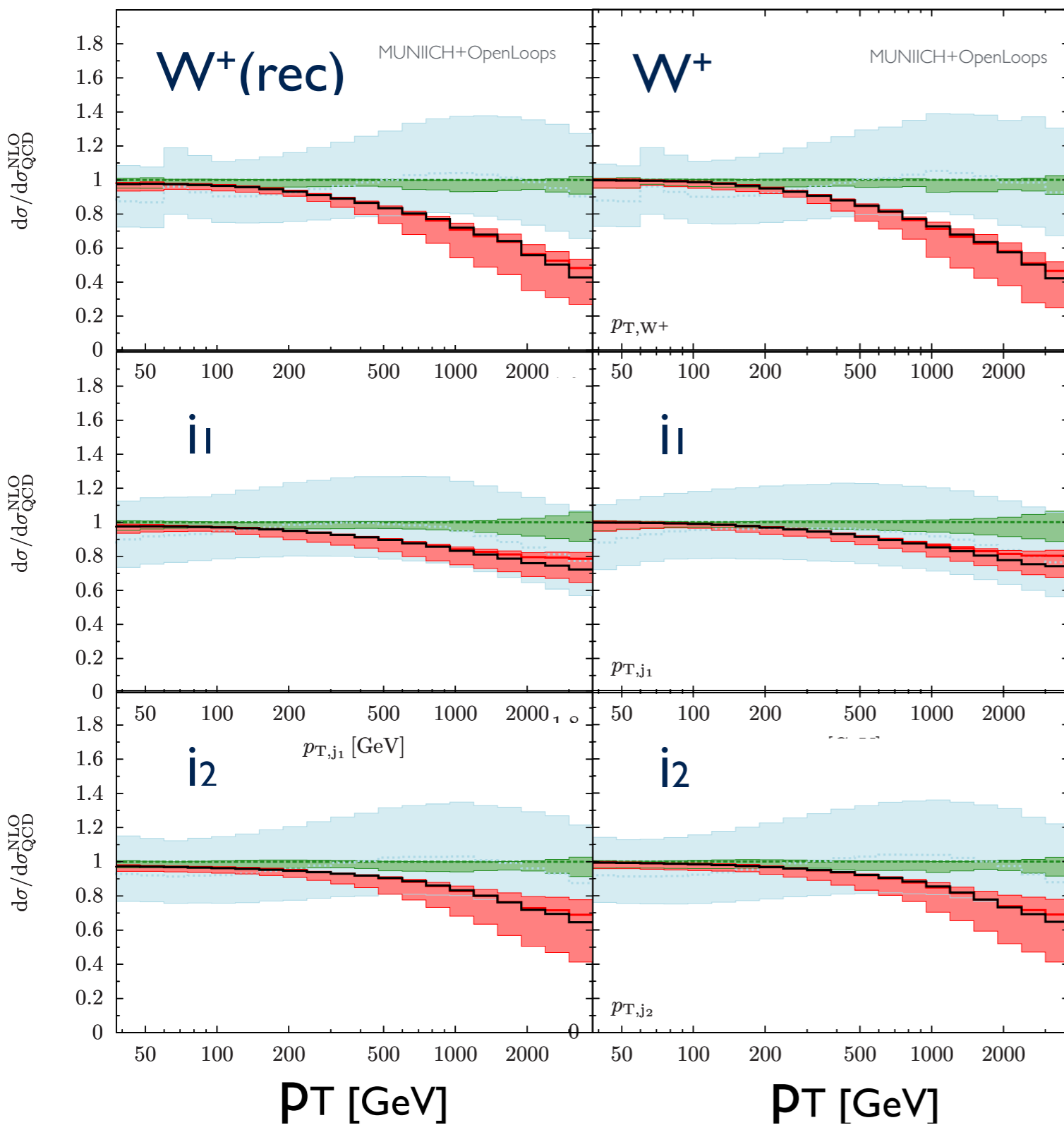
- -30–60% for W-boson at 1-4 TeV
- -15–25% for 1st and 2nd jet at 1-4 TeV

different!

- ▶ Might need resummation of leading EW Sudakov logs

off-shell vs. on-shell production

$l^+ \nu + 2 \text{ jets}$ vs. $W^+ + 2 \text{ jets}$

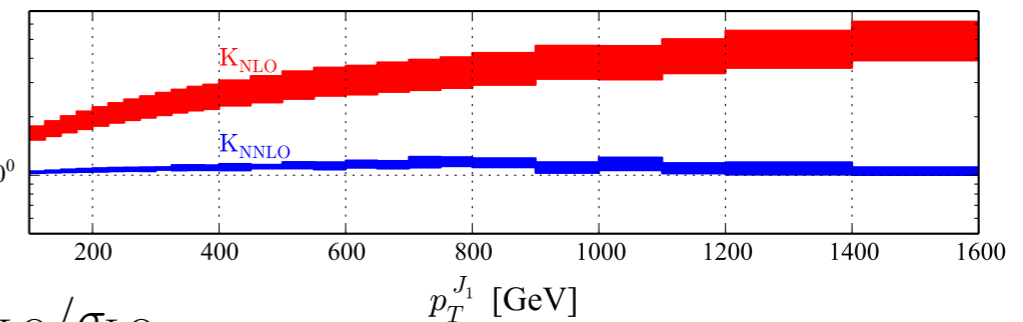
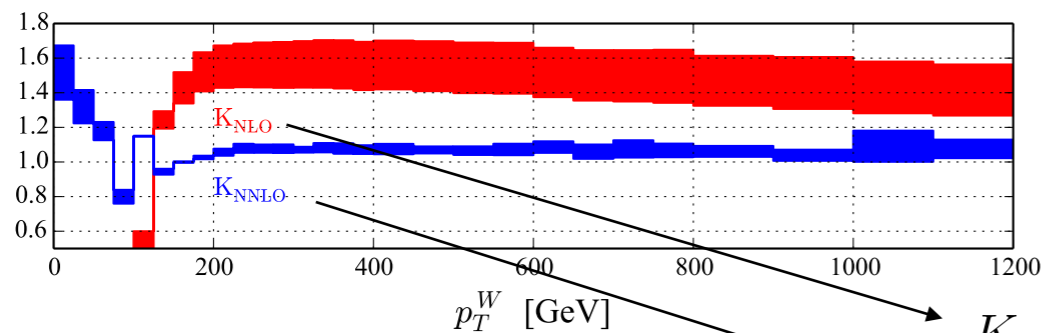
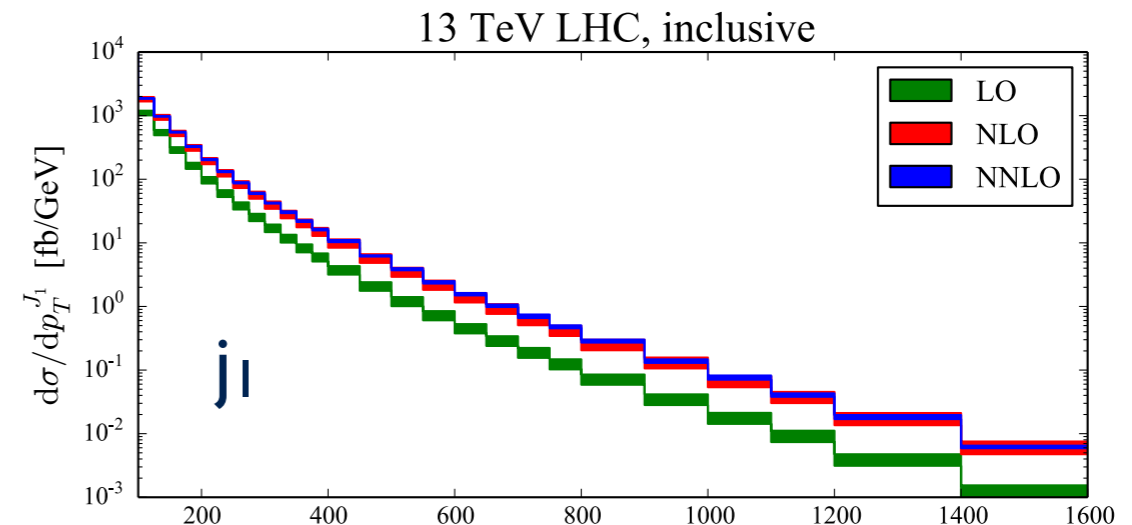
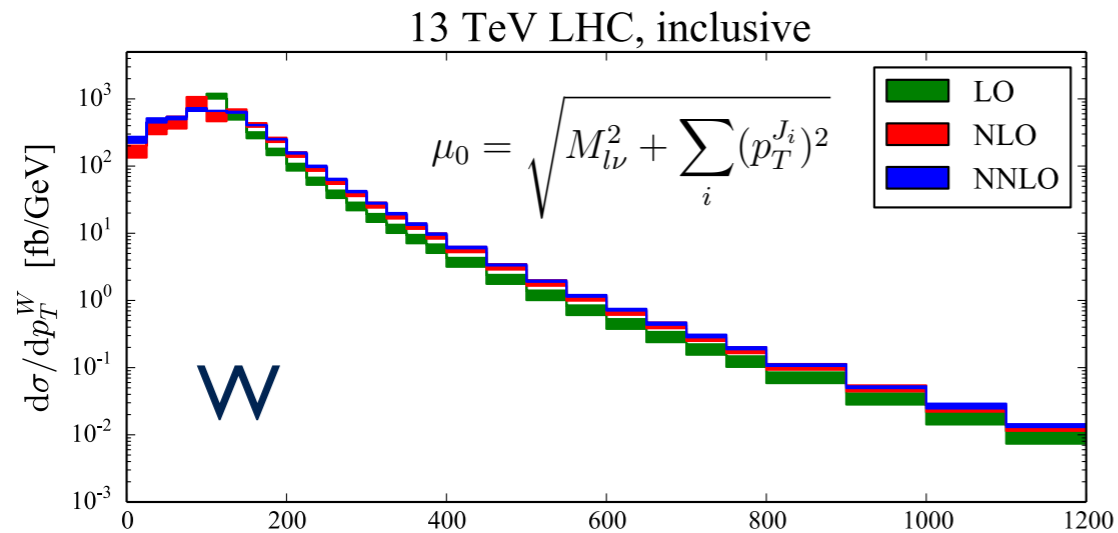


Effect of decays:

- ▶ Large Sudakov corrections unaffected
- ▶ However: needed for realistic experimental cuts

inclusive W + 1 jet @ NNLO QCD

[Boughezal, Liu, Petriello, '15, '16]



$$K_{\text{NLO}} = \sigma_{\text{NLO}} / \sigma_{\text{LO}}$$

$$K_{\text{NNLO}} = \sigma_{\text{NNLO}} / \sigma_{\text{NLO}}$$

- ▶ NNLO QCD: tiny remaining scale uncertainties (at the few % level)
- ▶ very small NNLO/NLO corrections in the tails

MEPS@NLO QCD+EW_{virt}

- ▶ Incorporate approximate EW corrections into MEPS@NLO framework [Höche, Krauss, Schönherr, Siegert; '13]
- ▶ **Idea:** integrate out real photon corrections (typical at the percent level for high-energy observables)

$$\tilde{B}_{n,\text{QCD}}(\Phi_n) \longrightarrow \tilde{B}_{n,\text{QCD+EW}}(\Phi_n) = \tilde{B}_n(\Phi_n) + V_{n,\text{EW}}(\Phi_n) + I_{n,\text{EW}}(\Phi_n) + B_{n,\text{mix}}(\Phi_n)$$

$$d\sigma = \underbrace{d\sigma(\alpha_S^2 \alpha)}_{\text{QCD}} + \underbrace{d\sigma(\alpha_S \alpha^2)}_{\text{EW}} + \underbrace{d\sigma(\alpha^3)}_{\text{QCD}} + \underbrace{d\sigma(\alpha^4)}_{\text{EW}}$$

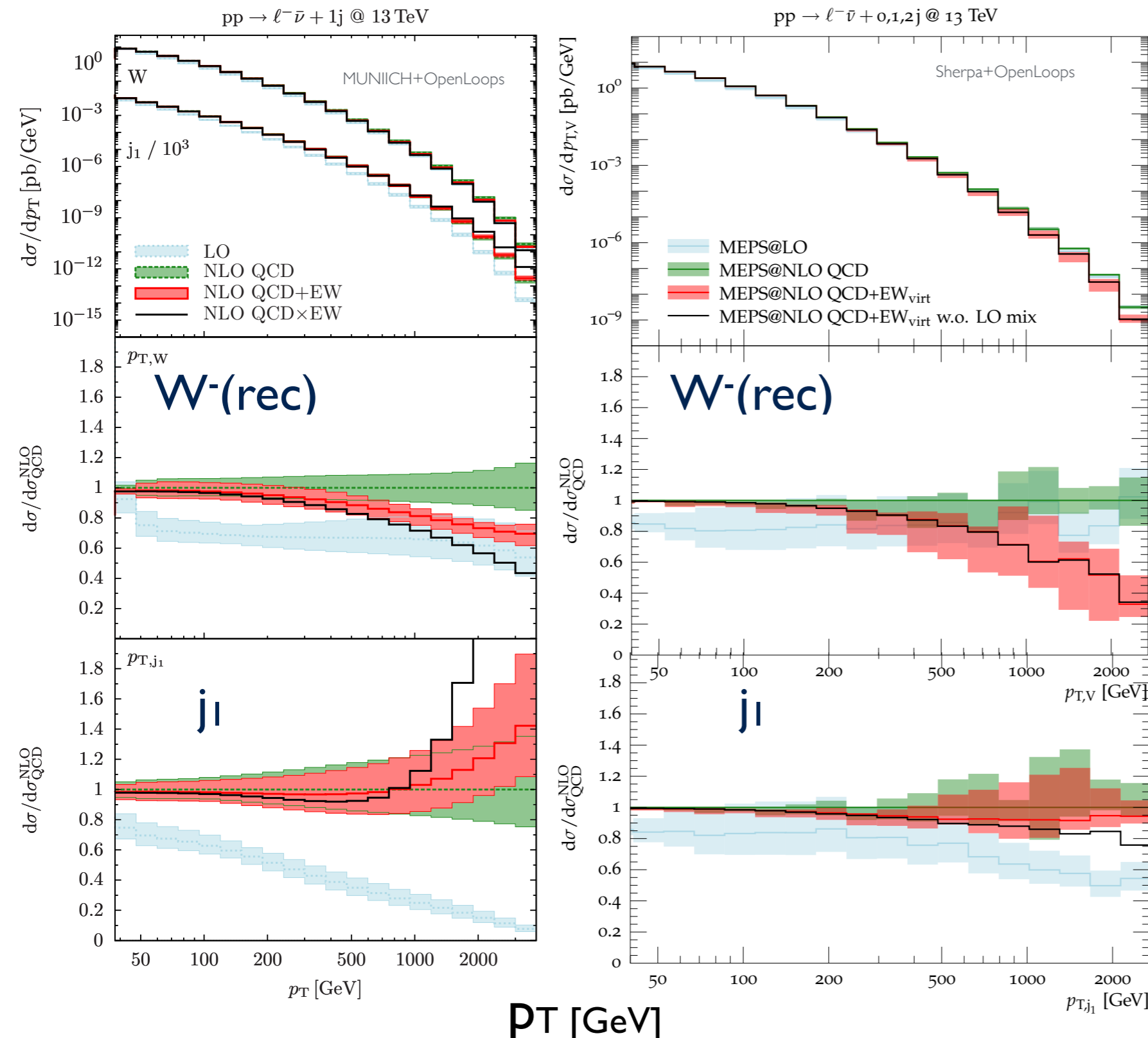
$$+ \underbrace{d\sigma(\alpha_S^3 \alpha)}_{\text{QCD}} + \underbrace{d\sigma(\alpha_S^2 \alpha^2)}_{\text{EW}} + \underbrace{d\sigma(\alpha_S \alpha^3)}_{\text{QCD}} + \underbrace{d\sigma(\alpha^4)}_{\text{EW}}$$

- ▶ Validated at fixed-order level (using exclusive sums for merging):
 - found to be reliable at the percent level
- ▶ exclusive QED corrections could be readded via QED parton shower
- ▶ use CKKW scale setting $\alpha_S^N(\mu_{\text{CKKW}}^2) = \alpha_S^{N-M}(\mu_{\text{core}}^2) \alpha_S(t_1) \dots \alpha_S(t_M)$ with EW clustering

and

$$\mu_{\text{core},\ell\ell} = m_{\ell\ell}, \quad \mu_{\text{core},Vj} = \frac{1}{2} E_{T,V} = \frac{1}{2} \sqrt{M_V^2 + p_{T,V}^2}, \quad \mu_{\text{core},jj} = \frac{1}{2} \left(\frac{1}{\hat{s}} - \frac{1}{\hat{t}} - \frac{1}{\hat{u}} \right)^{-\frac{1}{2}}$$

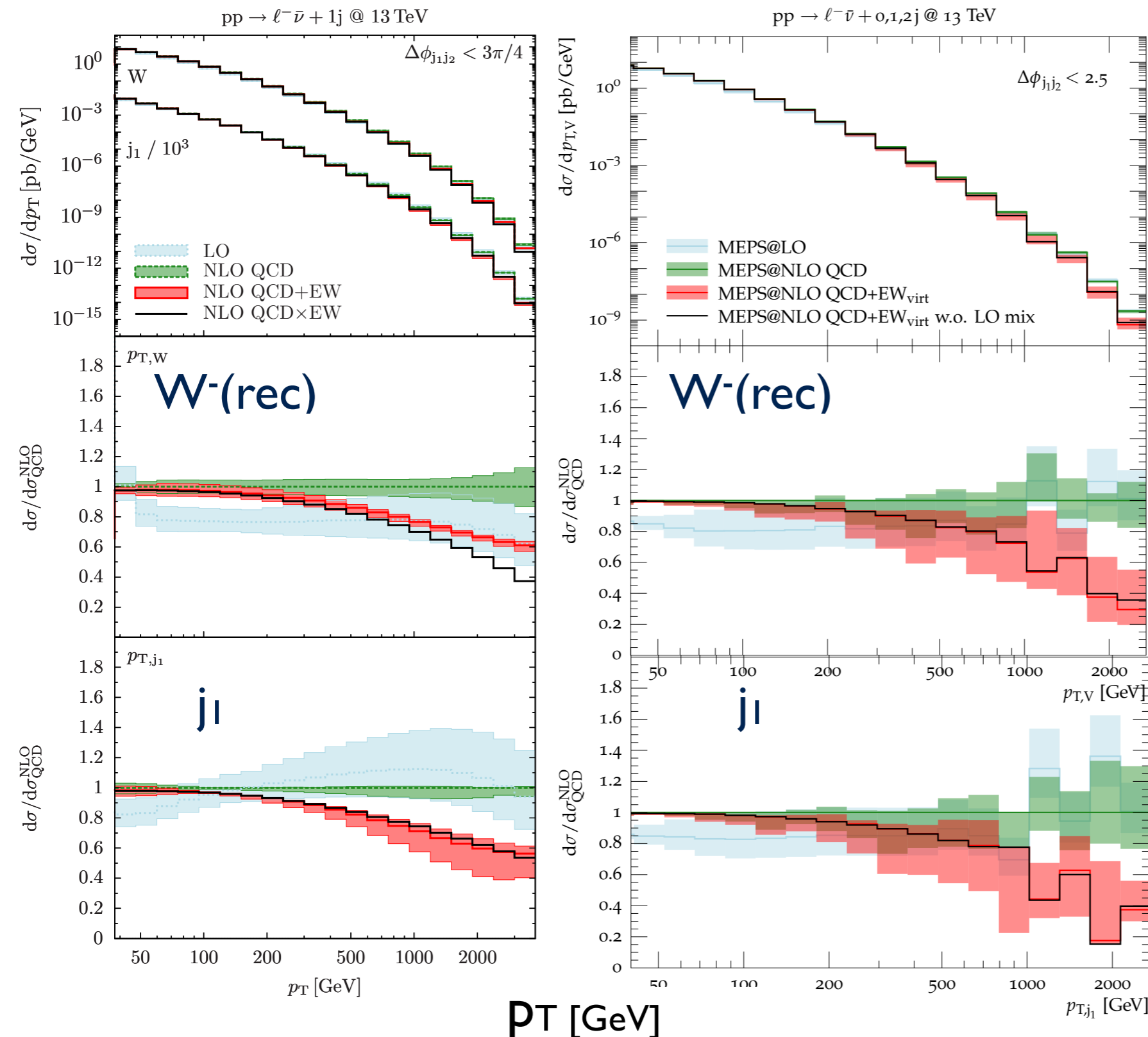
inclusive V+jets: MEPS@NLO QCD+EW_{virt}



- ▶ Stable NLO QCD+EW predictions in all of the phase-space...
- ▶ ...including Parton-Shower effects!
- ▶ $p_{T,V}$: MEPS@NLO QCD+EW in agreement with QCD×EW (fixed-order)
- ▶ p_{T,j_1} : compensation between negative Sudakov and quark-Bremsstrahlung (subleading Born for V+2 jet topology)

[Kallweit, Maierhöfer, JML, Pozzorini, Schönherr, '15]

exclusive V+ 1jet: MEPS@NLO QCD+EW



- ▶ Stable NLO QCD+EW predictions in all of the phase-space...
- ▶ ...including Parton-Shower effects.
- ▶ p_{T,j_1} : recover large EW corrections (as in fixed-order)

[Kallweit, Maierhöfer, JML, Pozzorini, Schönherr, '15]

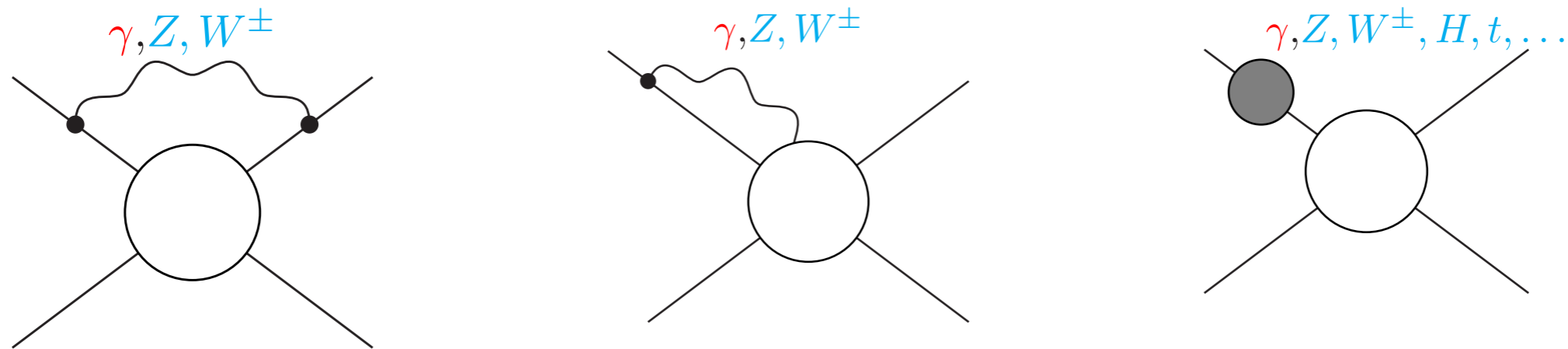
Conclusions

- ▶ monojet / MET+jets searches limited by systematics in transfer factors
- ▶ V + multijets @ NLO QCD+EW:
 - inclusion of EW corrections *crucial*
 - non-trivial interplay between QCD and EW
 - multi-jet final states genuinely different from V+1jet
 - merging essential for inclusive V+1jet
- ▶ Outlook:
 - $R_{ZZ}, R_{ZW} \text{ \& } R_{ZY}$ @ MEPS@NLO QCD+EW_{virt}
 - Goal: $(\text{MEPS@NLO QCD+EW}_{\text{virt}} / \text{MEPS@NLO QCD}) \times \text{NNLO QCD}$
 - few % accuracy for R-factors
 - Solid investigation of resulting theory uncertainty
 - MET + HF / V + HF

BACKUP

Virtual EW Sudakov logarithms

Originate from soft/collinear virtual EW bosons coupling to on-shell legs



Universality and factorisation similar as in QCD [Denner, Pozzorini; '01]

$$\delta_{\text{LL+NLL}}^{1\text{-loop}} = \frac{\alpha}{4\pi} \sum_{k=1}^n \left\{ \frac{1}{2} \sum_{l \neq k} \sum_{a=\gamma, Z, W^\pm} I^a(k) I^{\bar{a}}(l) \ln^2 \frac{s_{kl}}{M^2} + \gamma^{\text{ew}}(k) \ln \frac{s}{M^2} \right\}$$

- process-independent, simple structure, independent of \sqrt{S}
- 2-loop extension and resummation partially available
- typical size at $\sqrt{\hat{s}} = 1, 5, 10 \text{ TeV}$:

$$\delta_{\text{LL}} \sim -\frac{\alpha}{\pi s_W^2} \log^2 \frac{\hat{s}}{M_W^2} \simeq -28, -76, -104\%$$

$$\delta_{\text{NLL}} \sim +\frac{3\alpha}{\pi s_W^4} \log \frac{\hat{s}}{M_W^2} \simeq +16, +28, +32\%$$

➔ overall very large effect in the tail of distributions (relevant for BSM searches)

➔ large cancellations possible

Combination of NLO QCD and EW & Setup

Two alternatives:

$$\sigma_{\text{QCD}+\text{EW}}^{\text{NLO}} = \sigma^{\text{LO}} + \delta\sigma_{\text{QCD}}^{\text{NLO}} + \delta\sigma_{\text{EW}}^{\text{NLO}}$$

$$\sigma_{\text{QCD}\times\text{EW}}^{\text{NLO}} = \sigma_{\text{QCD}}^{\text{NLO}} \left(1 + \frac{\delta\sigma_{\text{EW}}^{\text{NLO}}}{\sigma^{\text{LO}}} \right) = \sigma_{\text{EW}}^{\text{NLO}} \left(1 + \frac{\delta\sigma_{\text{QCD}}^{\text{NLO}}}{\sigma^{\text{LO}}} \right)$$

Difference between the two approaches indicates uncertainties due to missing two-loop EW-QCD corrections of $\mathcal{O}(\alpha\alpha_s)$

Relative corrections w.r.t. NLO QCD:

$$\frac{\sigma_{\text{QCD}+\text{EW}}^{\text{NLO}}}{\sigma_{\text{QCD}}^{\text{NLO}}} = \left(1 + \frac{\delta\sigma_{\text{EW}}^{\text{NLO}}}{\sigma_{\text{QCD}}^{\text{NLO}}} \right)$$

suppressed by large NLO QCD corrections

$$\frac{\sigma_{\text{QCD}\times\text{EW}}^{\text{NLO}}}{\sigma_{\text{QCD}}^{\text{NLO}}} = \left(1 + \frac{\delta\sigma_{\text{EW}}^{\text{NLO}}}{\sigma^{\text{LO}}} \right)$$

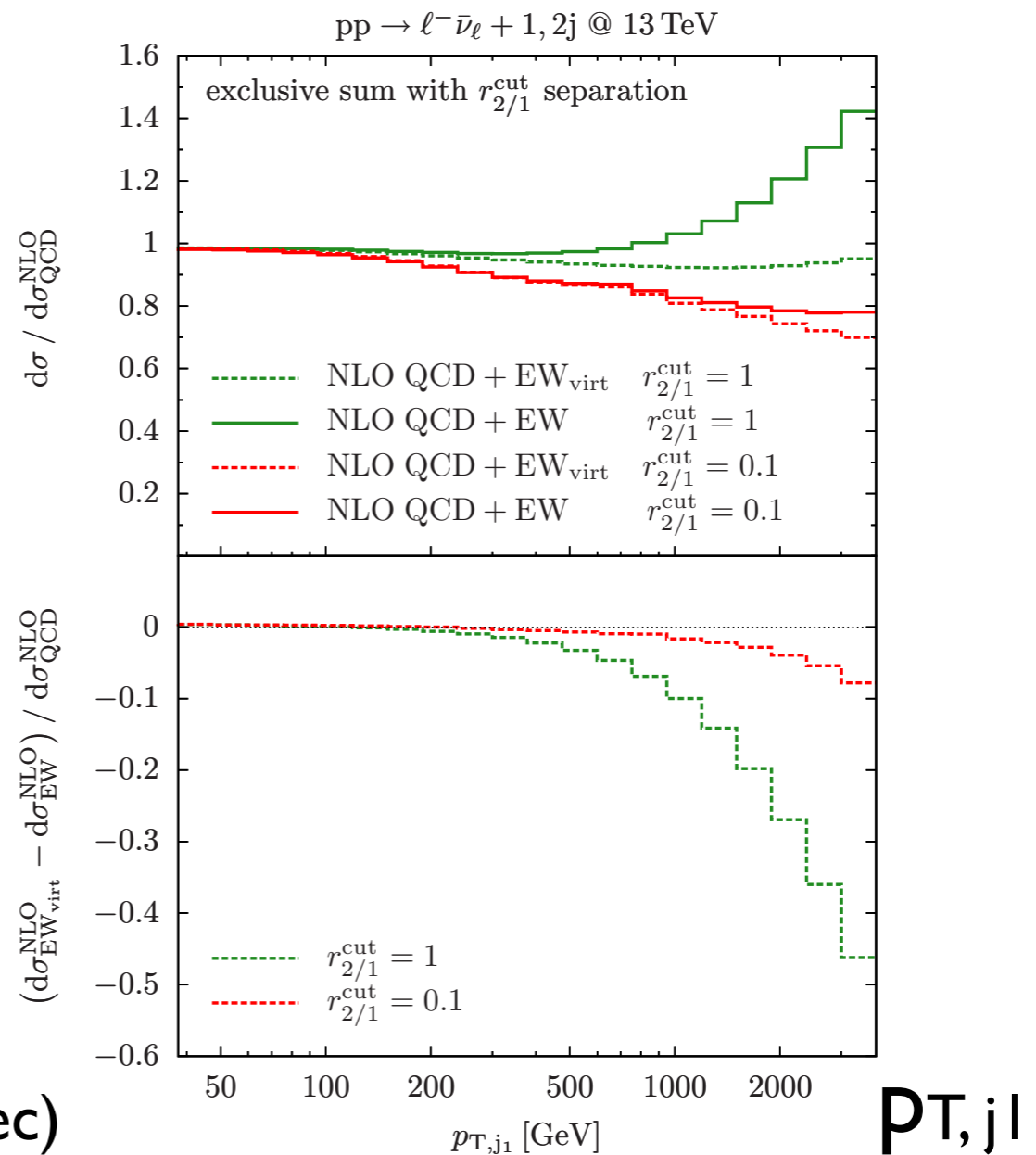
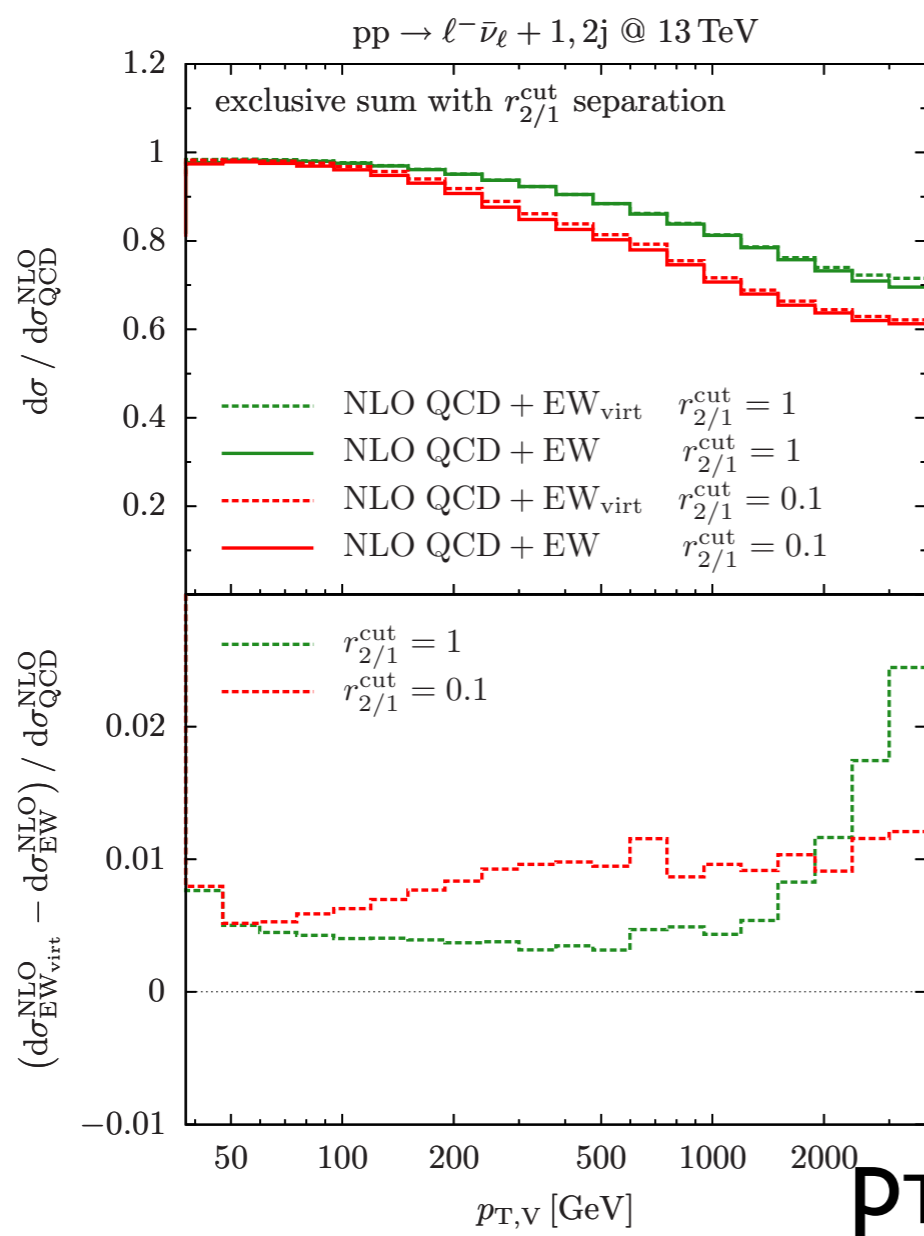
“usual” NLO EW w.r.t. LO

► $\alpha = \frac{\sqrt{2}}{\pi} G_\mu M_W^2 \left(1 - \frac{M_W^2}{M_Z^2} \right)$ in G_μ -scheme with $G_\mu = 1.16637 \times 10^{-5} \text{ GeV}^{-2}$

► PDFs: NNPDF 2.3QED with $\alpha_S(M_Z) = 0.118$ for LO and NLO QCD/EW

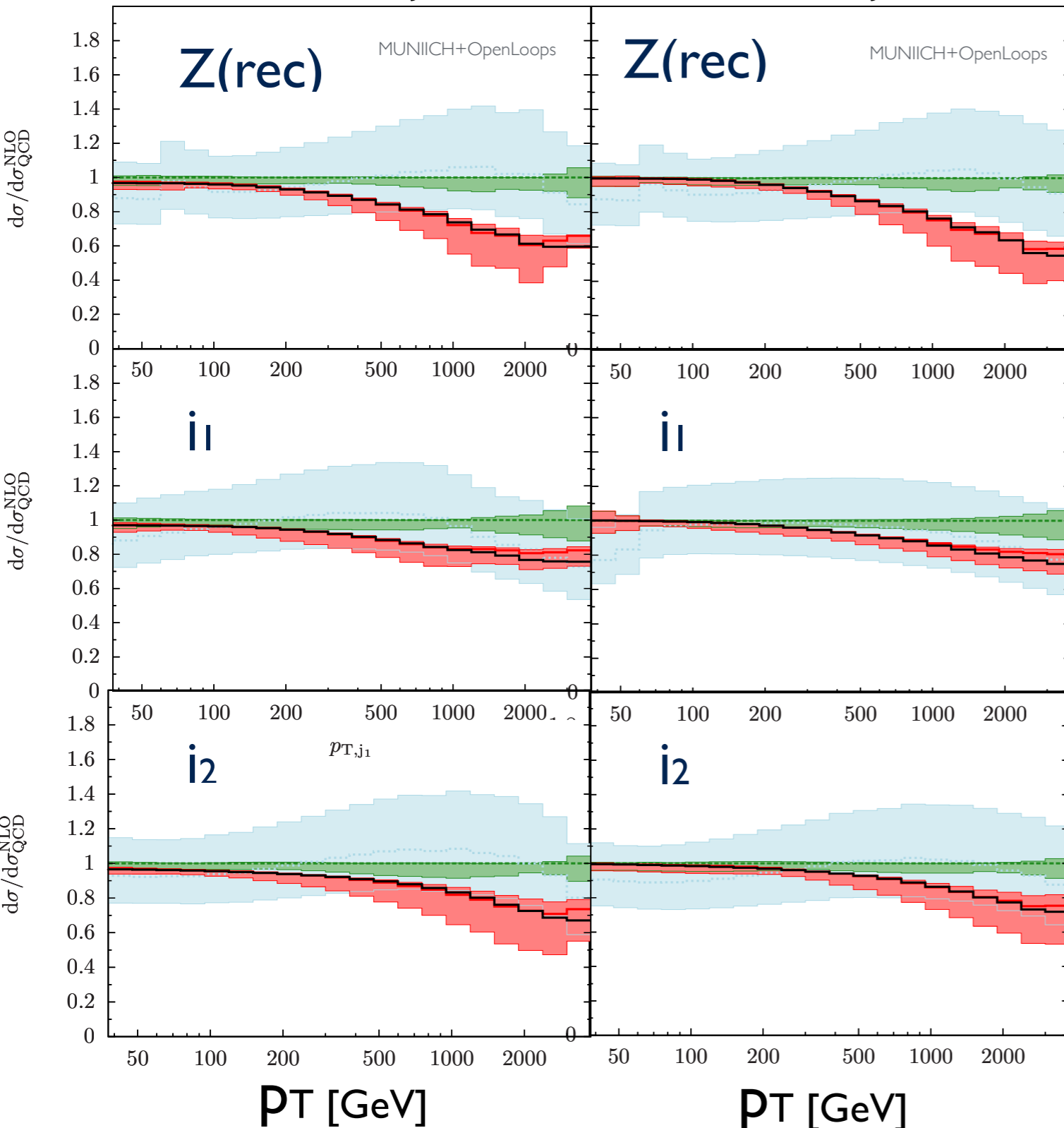
NLO EW_{virt} Approximation

- ▶ Goal: include dominant (Sudakov) corrections into PS Monte-Carlo & apply multi-jet merging (MEPS@NLO)
- ▶ Idea: $d\sigma_{n,\text{NLO EW}_{\text{virt}}} = \left[B_n(\Phi_n) + V_{n,\text{EW}}(\Phi_n) + I_{n,\text{EW}}(\Phi_n) \right] d\Phi_n$.
- ▶ Check: agreement within few percent (with $r_{2/1}^{\text{cut}} = 0.1$):



Dependence on decay mode

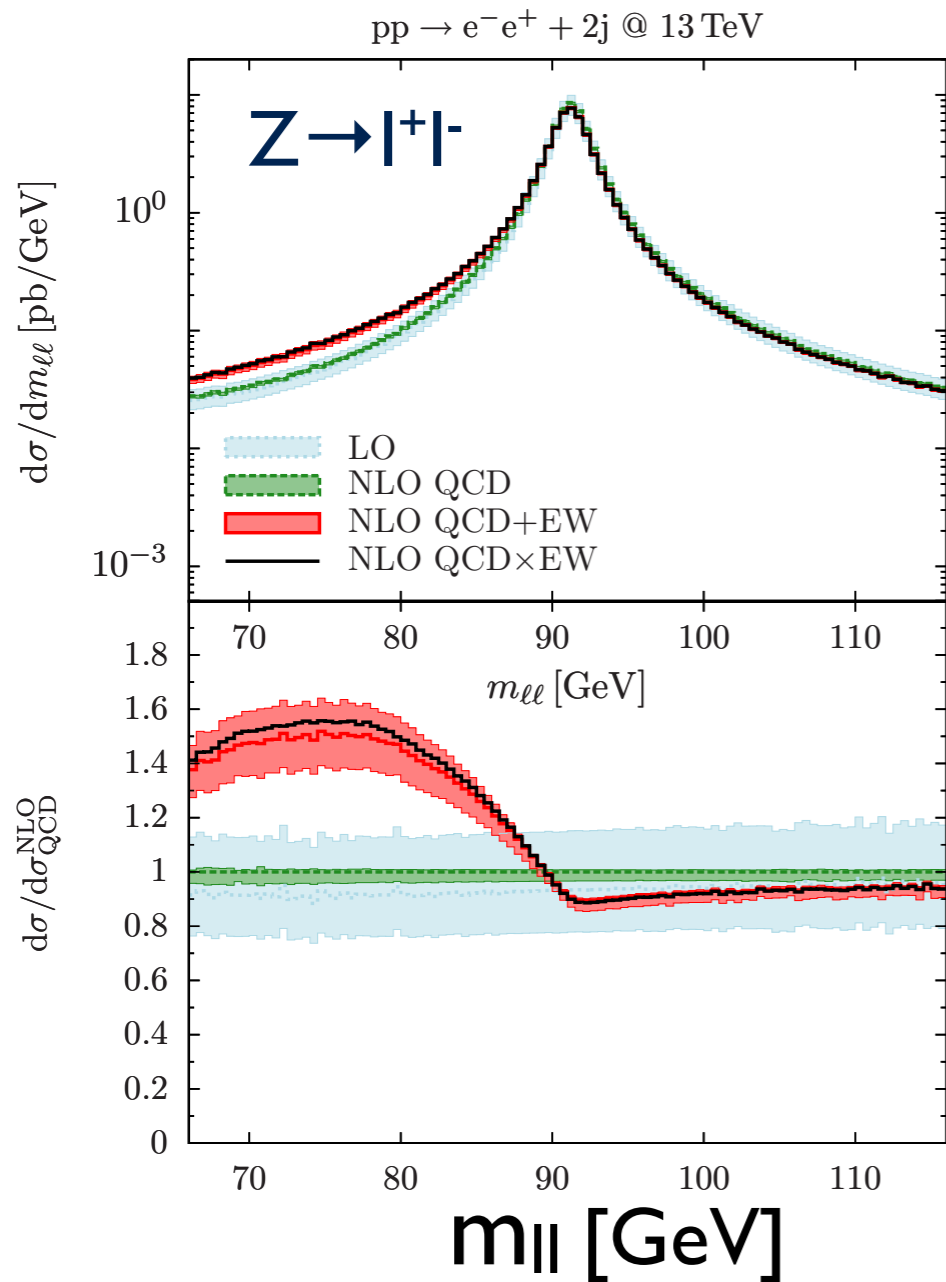
$l^+l^- + 2 \text{ jets}$ vs. $\nu\bar{\nu} + 2 \text{ jets}$



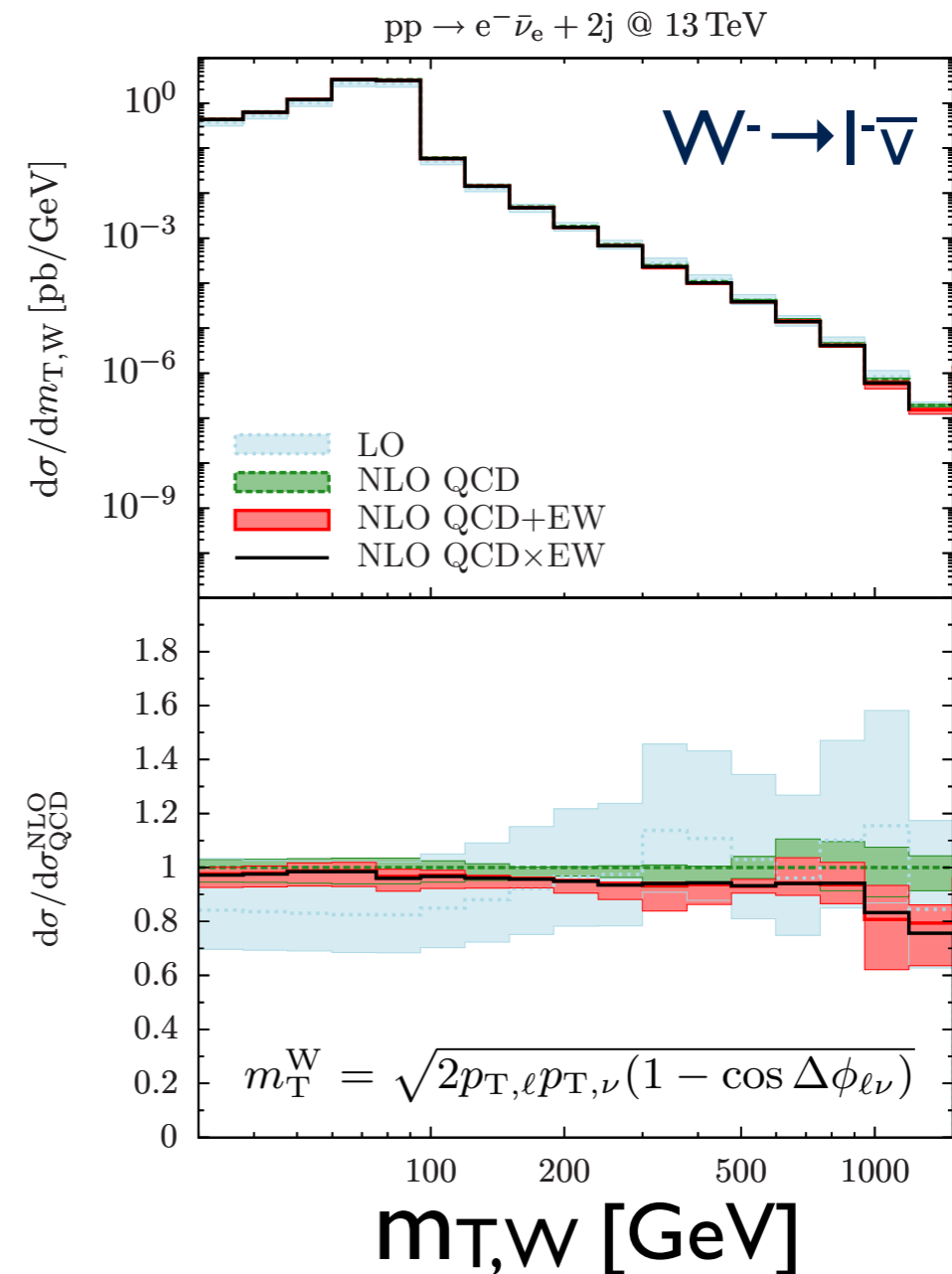
► Large EW Sudakov corrections independent of the decay mode (with inclusive lepton selections)

		$Z \rightarrow l^+l^-$	$Z \rightarrow \nu\bar{\nu}l$
l	\in	e, μ	e, μ, τ
p_{T,l^\pm} [GeV]	$>$	25	
\cancel{E}_T [GeV]	$>$		25
m_T^W [GeV]	$>$		
m_{l+l^-} [GeV]	\in	[66, 116]	
$ \eta_{l^\pm} $	$<$	2.5	
$\Delta R_{l^\pm j}$	$>$	0.5	
ΔR_{l+l^-}	$>$	0.2	

Leptonic observables

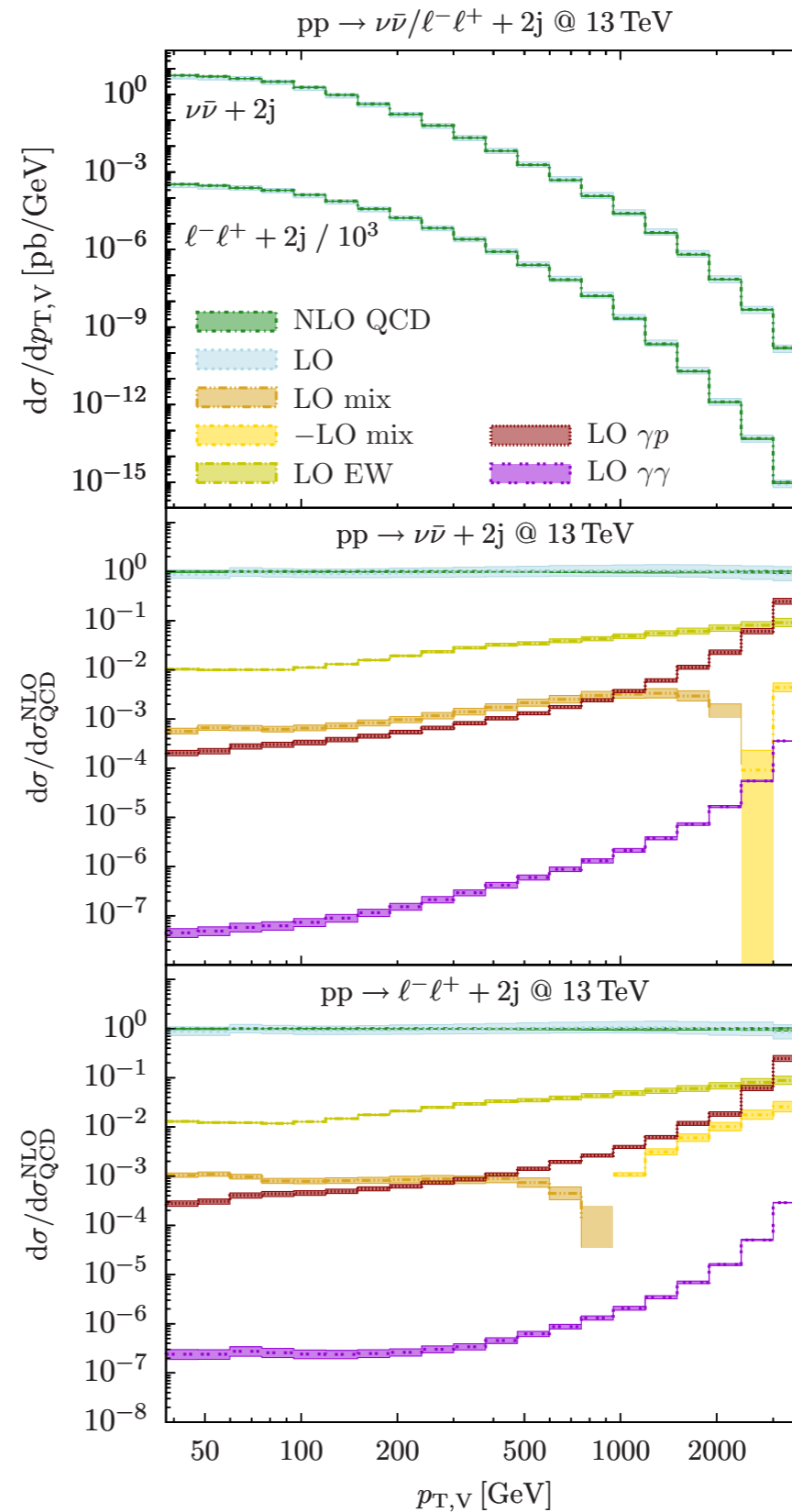
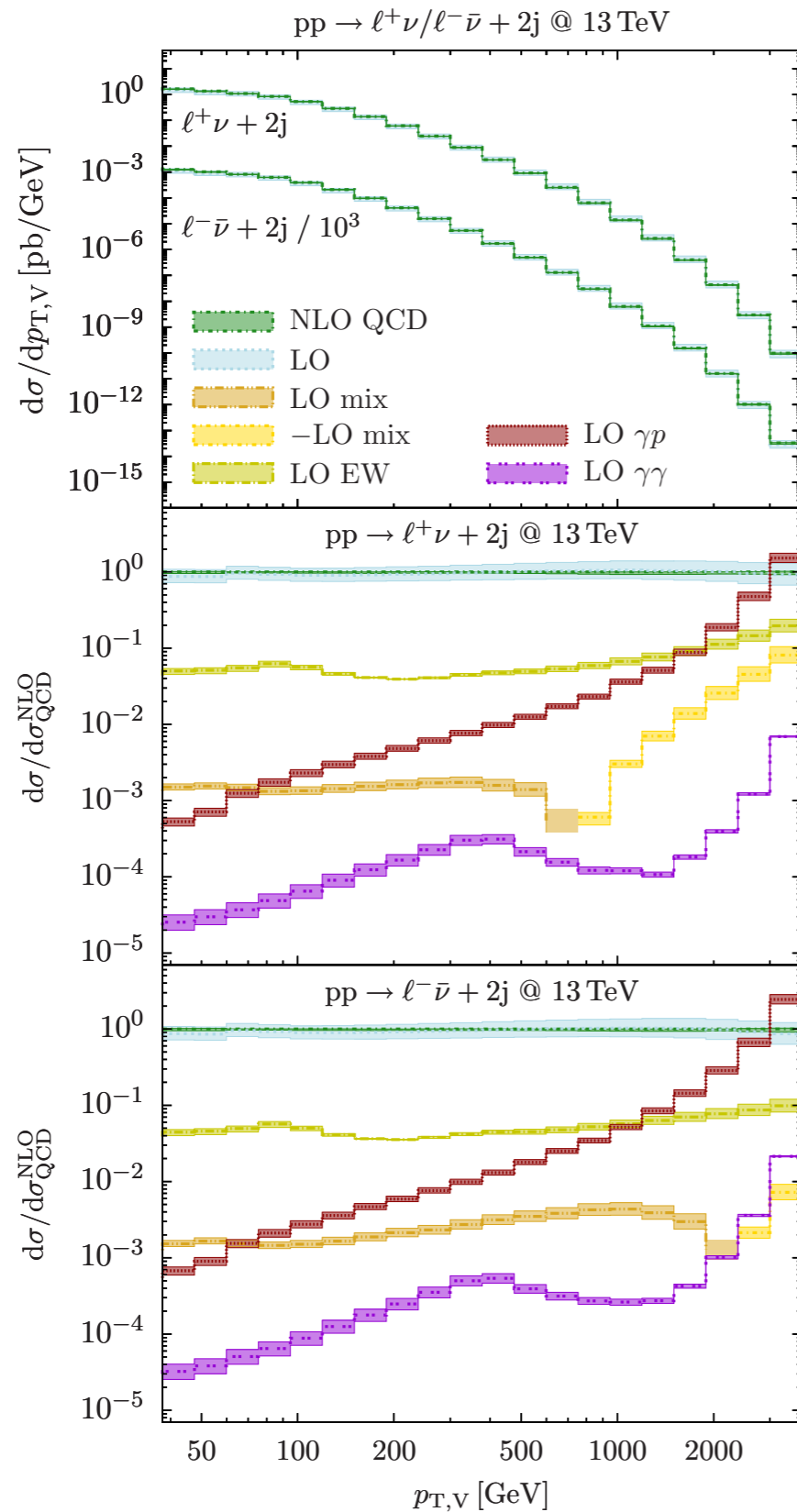


- ▶ up to 50% from QED Bremsstrahlung.
- ▶ Similar shape as for NC DY

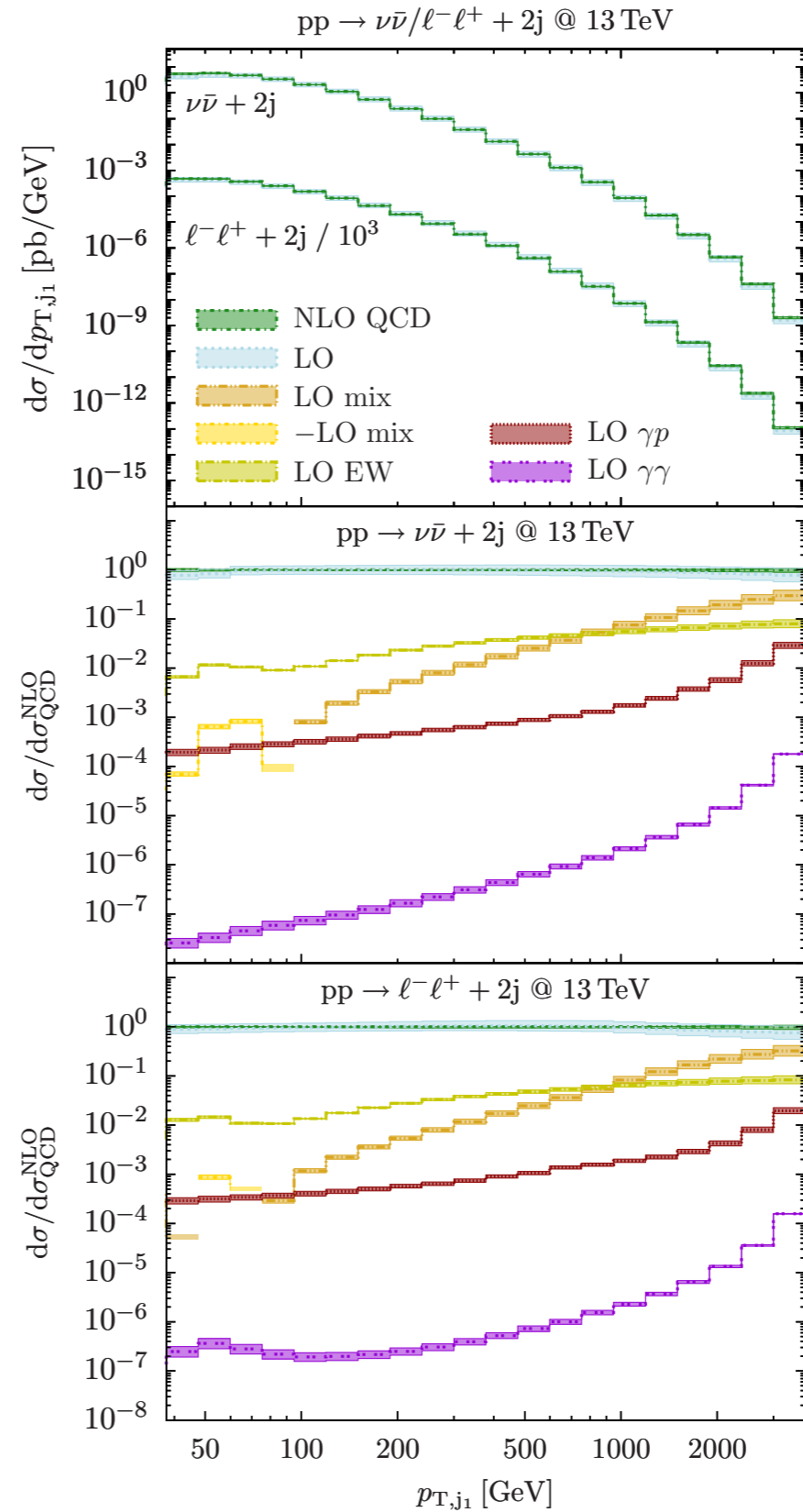
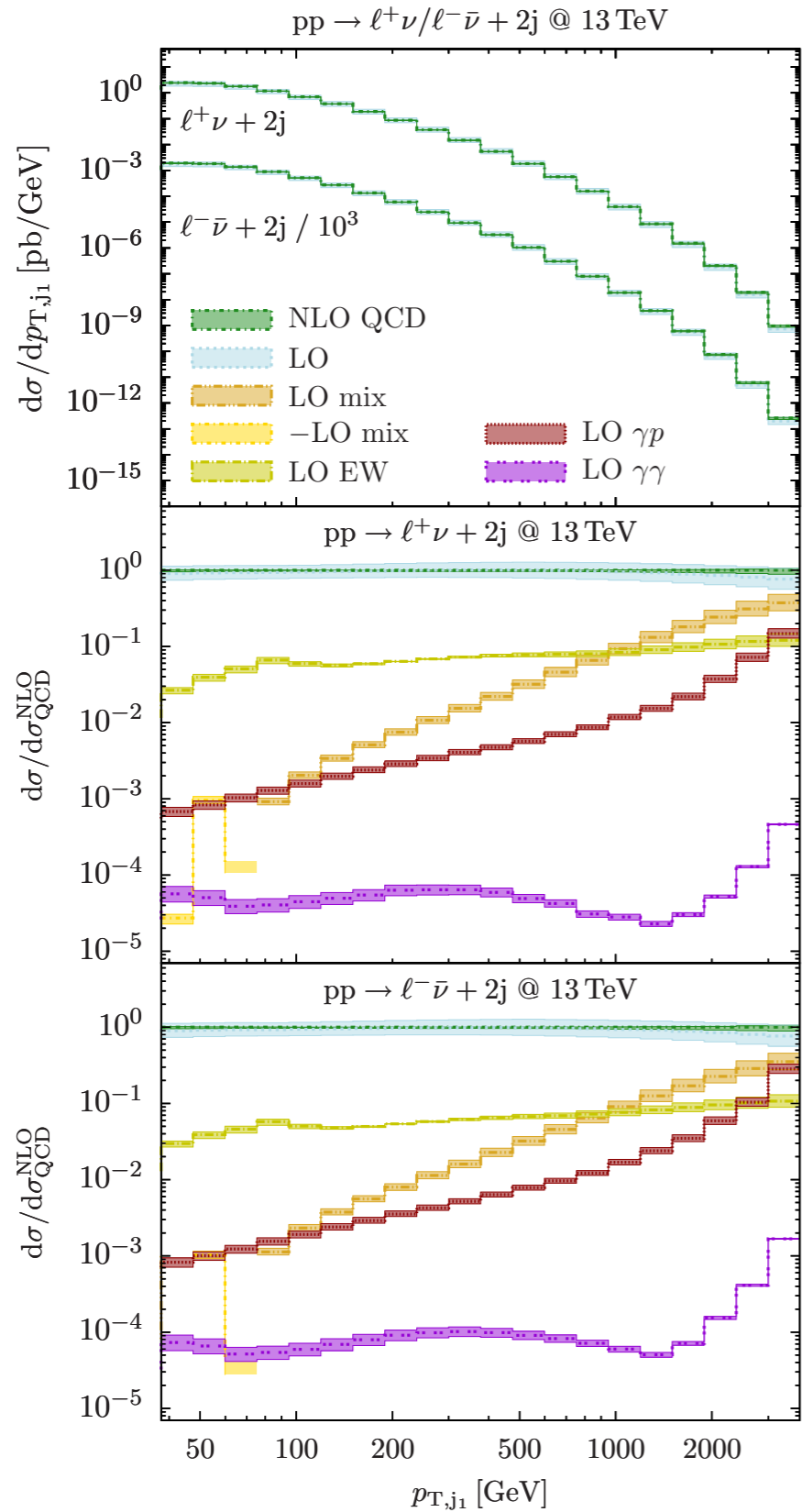


- ▶ moderate EW corrections at large $m_{T,W}$
- ▶ no (strong) Sudakov enhancement

Subleading Born: $p_{T,V}$



Subleading Born: $p_{T,j1}$



Photon PDF comparison at 10^4 GeV^2

