

Introduction to meeting

(some personal thoughts)

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University of Oxford

2nd LHC Dark Matter WG public meeting,
19-20 September 2016, CERN

Outcome of 1st meeting

[Boveia et al., 1603.04156]

16v1 [hep-ex] 14 Mar 2016

Recommendations on presenting LHC searches for missing transverse energy signals using simplified s -channel models of dark matter

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 Jan Heisig,¹² Valerio Ippolito,¹³ Felix Kahlhoefer,^{14,*}
 Valentin V. Khoze,¹⁵ Suchita Kulkarni,¹⁶ Greg Landsberg,¹⁷
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 Tristan du Pree,¹ Antonio Riotto,¹¹ David Salek,^{19,22}
 Kai Schmidt-Hoberg,¹⁴ William Shepherd,²³ Tim M.P. Tait,^{24,*}
 Lian-Tao Wang,²⁵ Steven Worm²⁶ and Kathryn Zurek²⁷

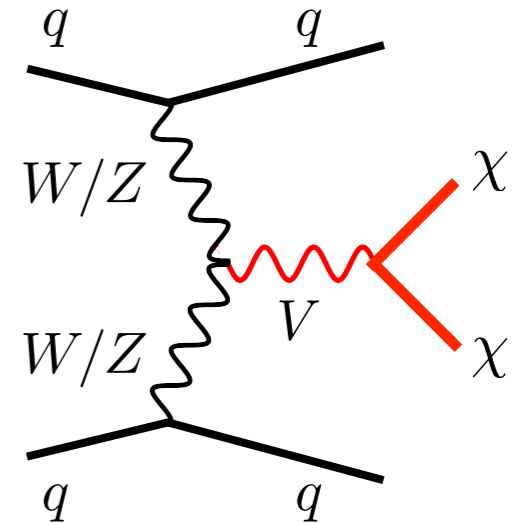
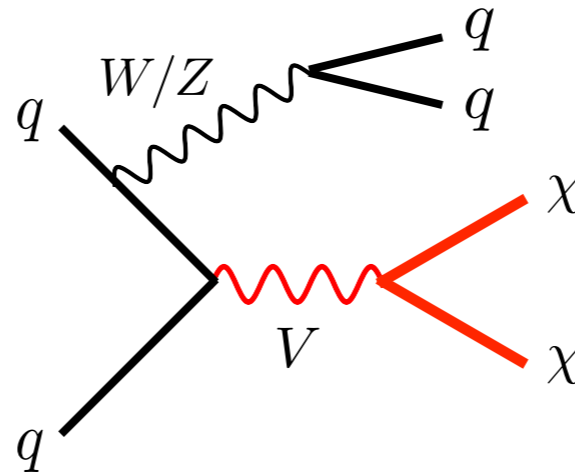
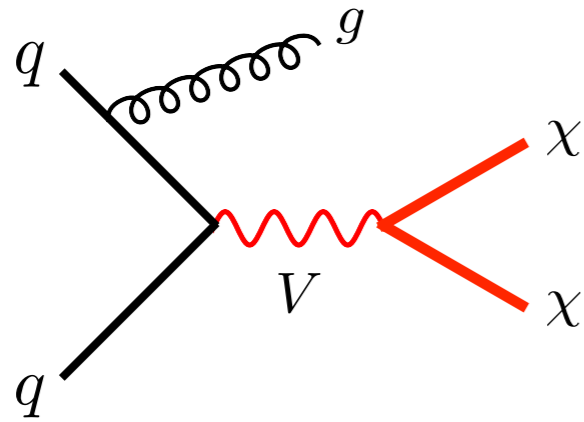
Document summarises proposal of LHC DMWG on how-to present LHC results on s -channel simplified DM models & to compare them to direct (indirect) detection experiments

Scope of 2nd meeting

Main focus of meeting on experimental & theoretical questions dealing with DM searches at LHC:

- (i) complementarity & interplay of mediator searches leading to $E_{T, \text{miss}}$ & non- $E_{T, \text{miss}}$ signatures
- (ii) limitations of existing s-channel simplified DM models & possible improvements
- (iii) review of progress in t-channel, spin-2 DM & gluphilic models
- (iv) discussion about experimental & theoretical issues concerning SM backgrounds relevant for $E_{T, \text{miss}}$ searches

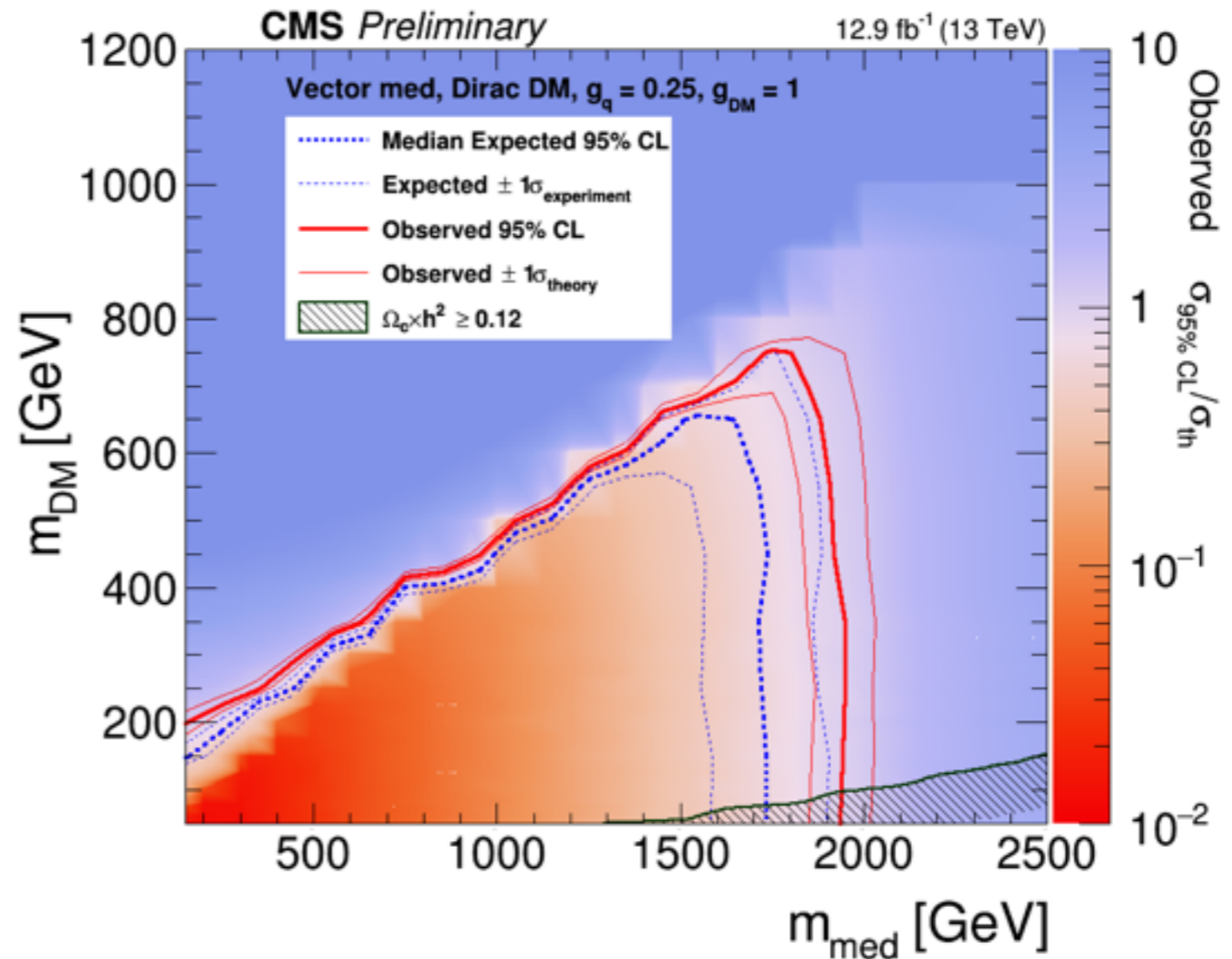
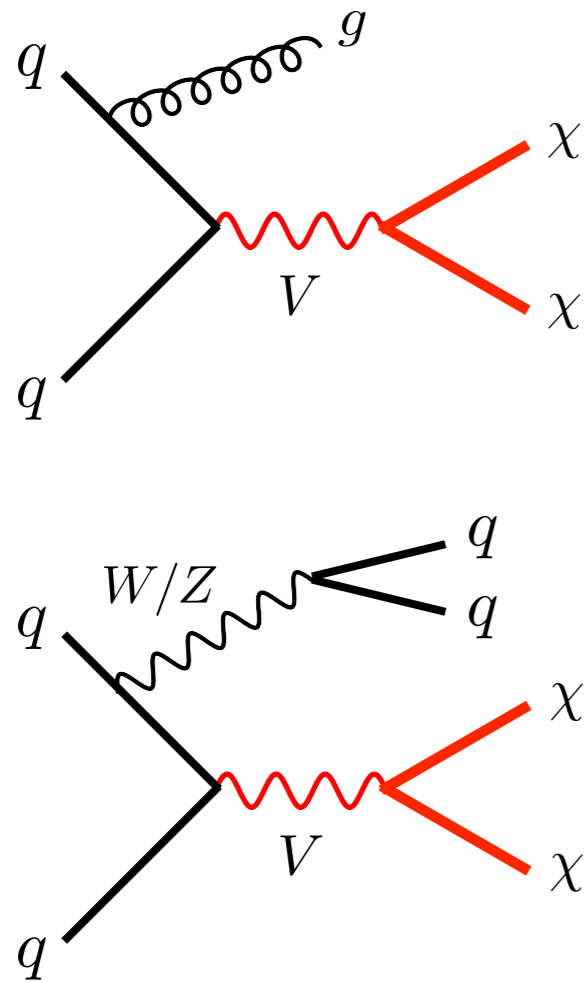
Mono-jet searches at 13 TeV



Latest mono-jet searches are more complex than simple cut & count analyses of Run I. A jet veto is not imposed anymore & hence searches sensitive to both initial state radiation (ISR) as well as gauge boson induced scatterings. Signal models need to correctly describe all possible $E_{T,miss} + \text{jets}$ production topologies

Spin-1 simplified models: 13 TeV limits

[CMS PAS EXO-16-037]

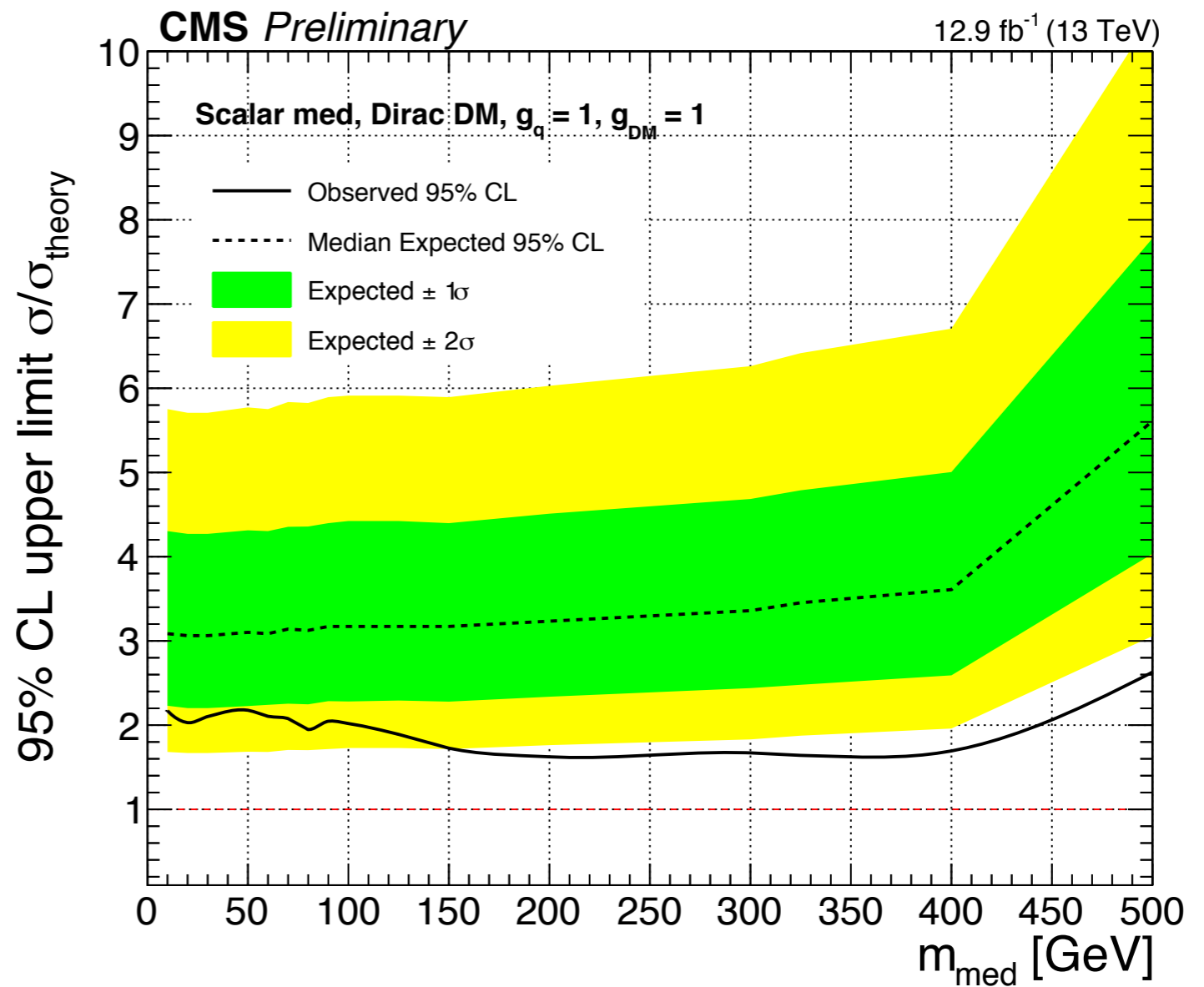
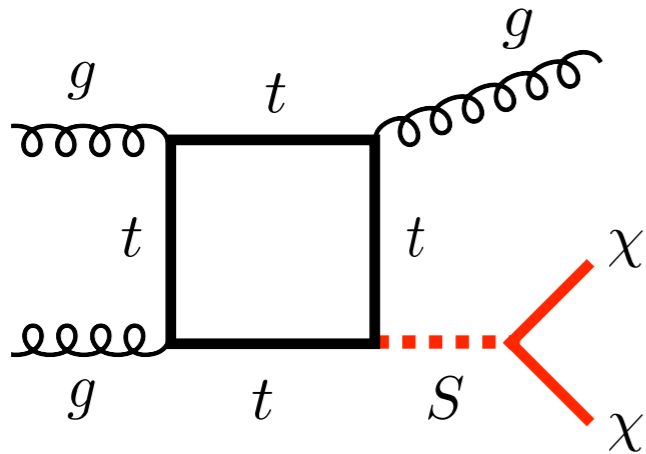


Latest $E_{T, \text{miss}} + \text{jets}$ searches exclude mediator masses up to close to 2 TeV for both vector & axialvector exchange if $g_q = 0.25, g_\chi = 1$

[details in talks by Caterina, Zeynep, Antonio & Tristan]

Spin-0 simplified models: 13 TeV limits

[CMS PAS EXO-16-037]

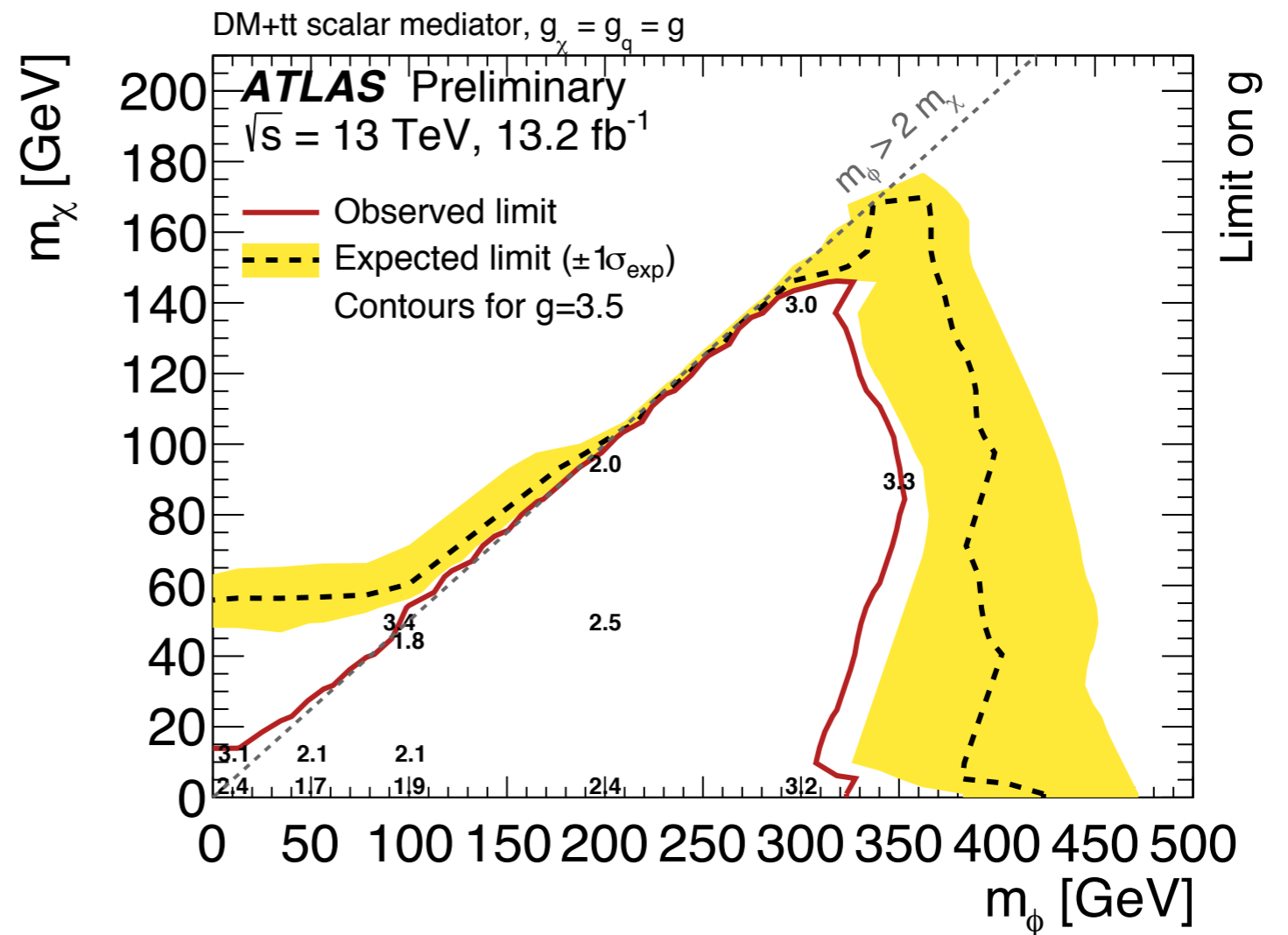
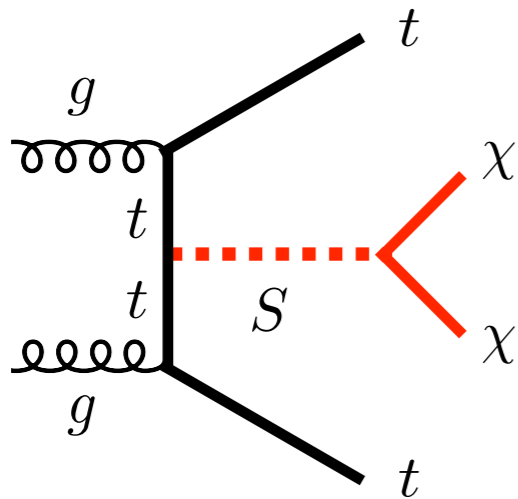


Mono-jet searches not yet sensitive to scalar models with weak couplings

[details in talks by Caterina, Zeynep, Antonio & Tristan]

Spin-0 simplified models: 13 TeV limits

[ATLAS-CONF-2016-050]

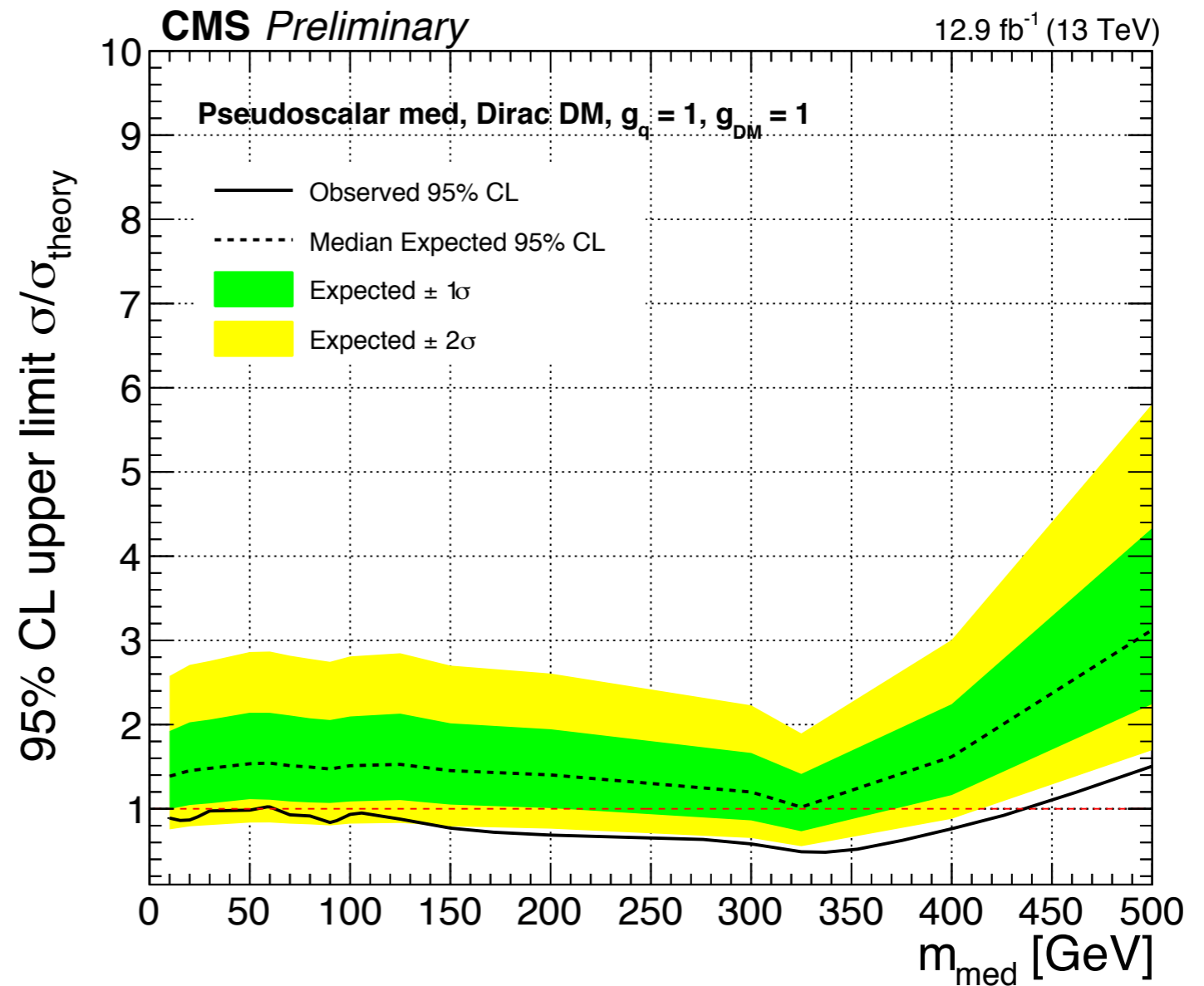
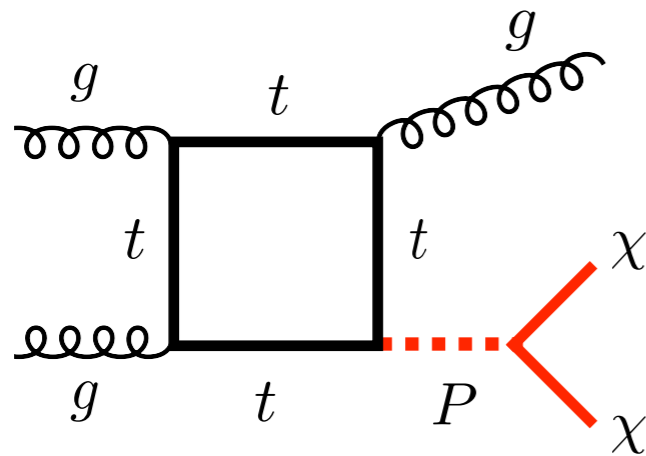


Strongly-coupled scalar models with mediator masses of 300 GeV can be tested via $E_{T,\text{miss}} + t\bar{t}$. Mediator broad in large parts of parameter space

[details in talks by Johanna, Eitan & Kevin]

Spin-0 simplified models: 13 TeV limits

[CMS PAS EXO-16-037]

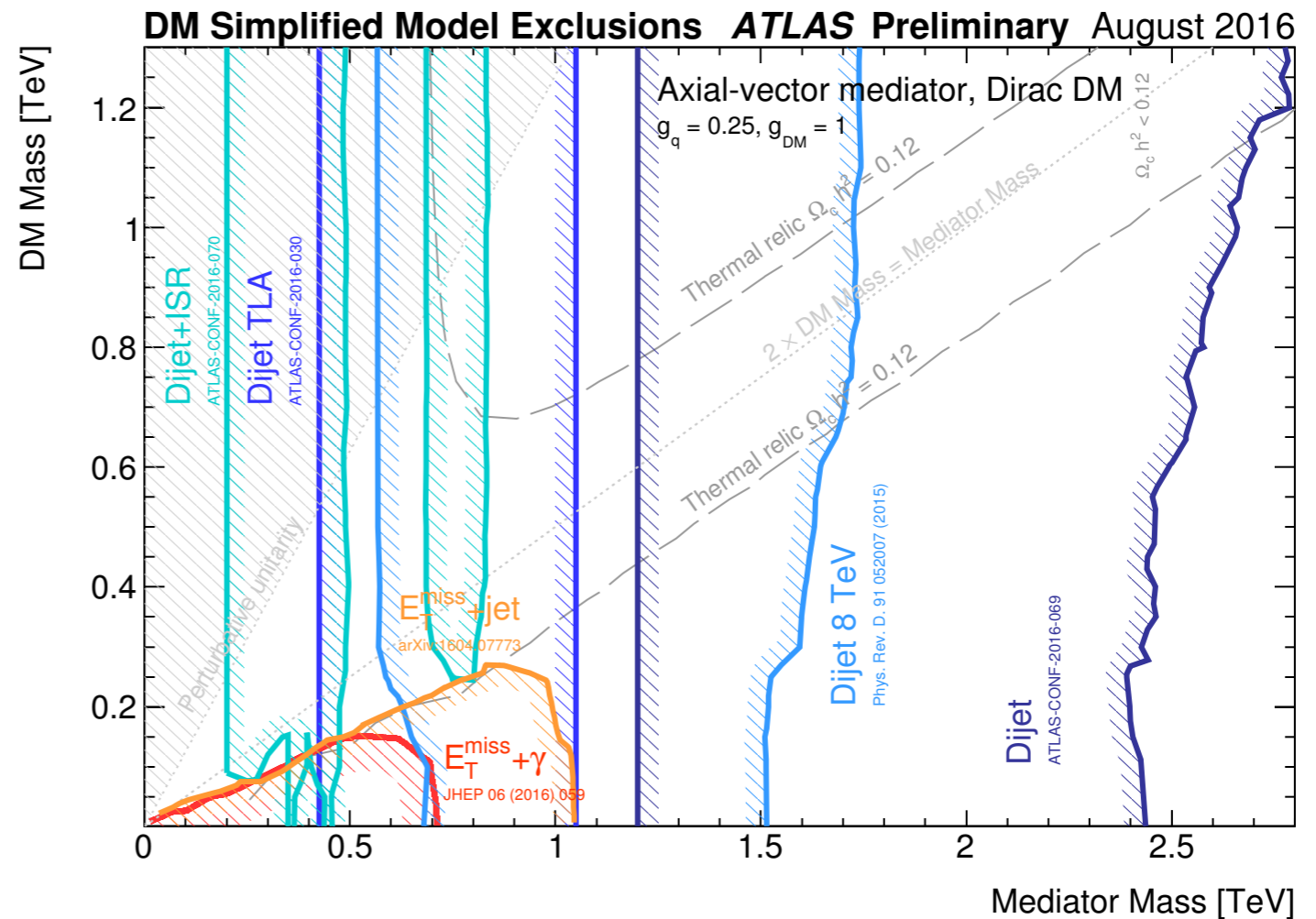
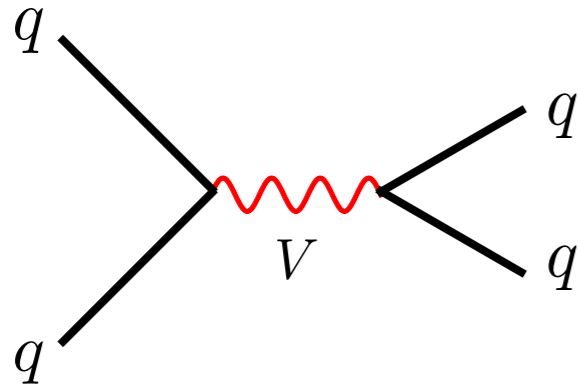


Since pseudoscalar production enhanced by a factor of more than 2,
mediator masses close to 450 GeV are excluded for $g_q = g_\chi = 1$

[details in talks by Caterina, Zeynep, Antonio & Tristan]

Spin-1 simplified models: di-jet limits

[<https://twiki.cern.ch/twiki/bin/view/AtlasPublic/ExoticsPublicResults>]

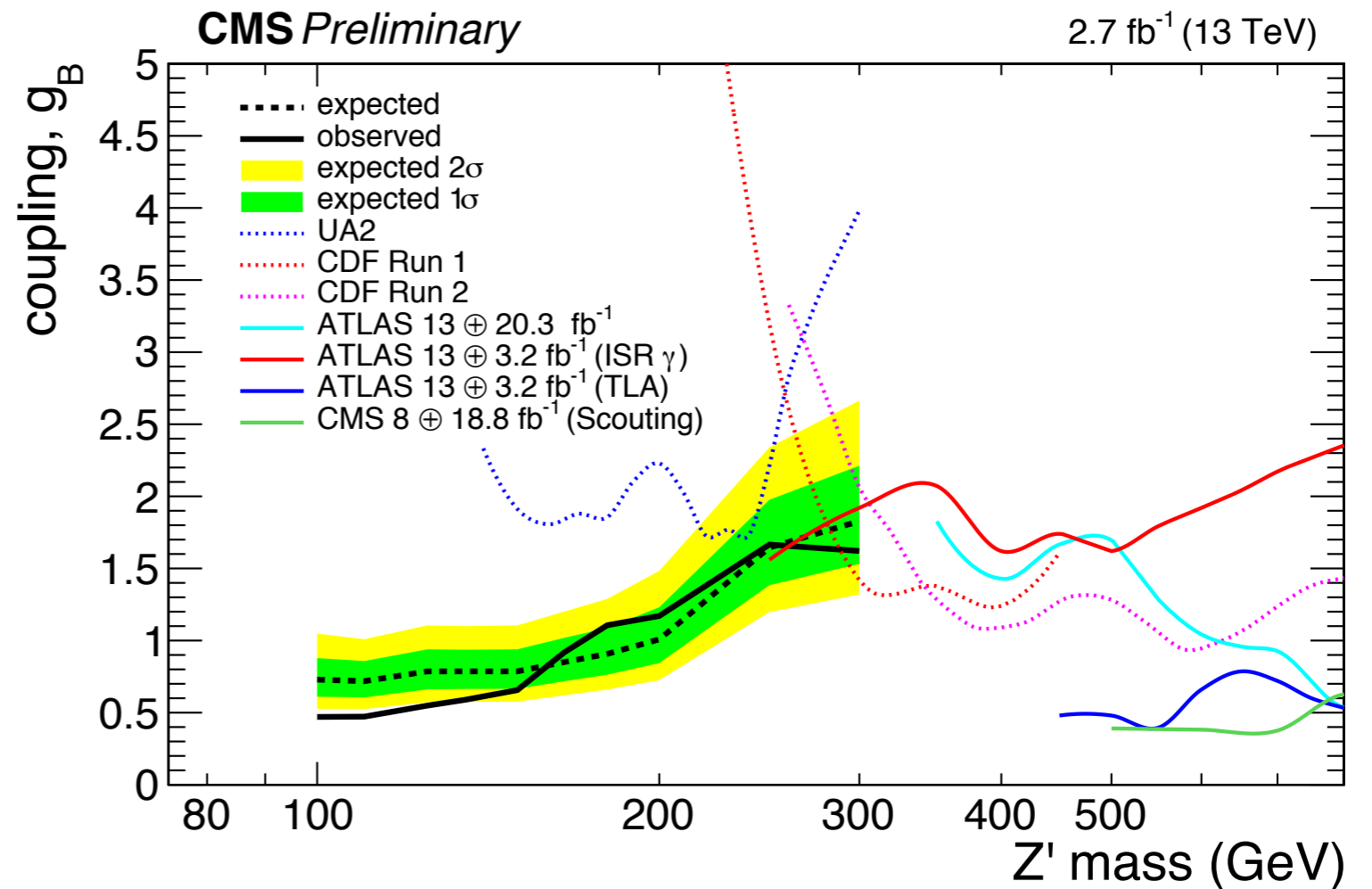
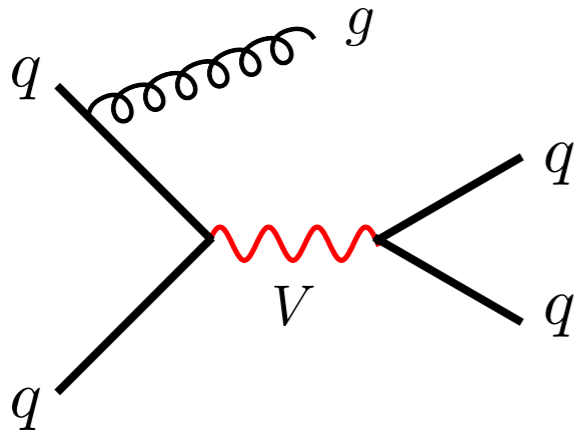


For coupling choice $g_q = 0.25, g_\chi = 1$ di-jet searches provide complementary constraints & exclude mediator masses from 200 GeV to 2.8 TeV

[details in talks by Caterina, Zeynep, Antonio & Tristan]

Spin-1 simplified models: tri-jet limits

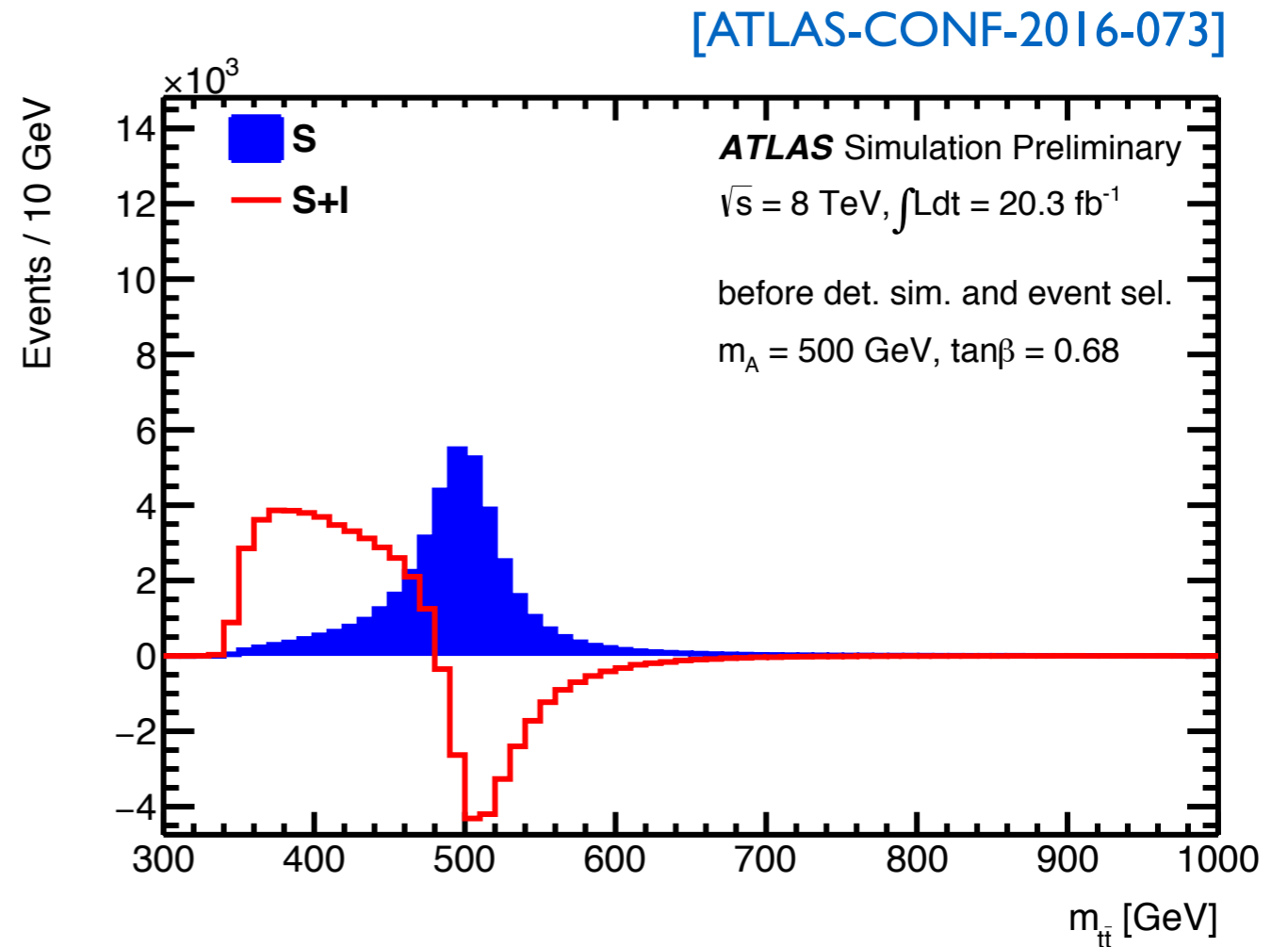
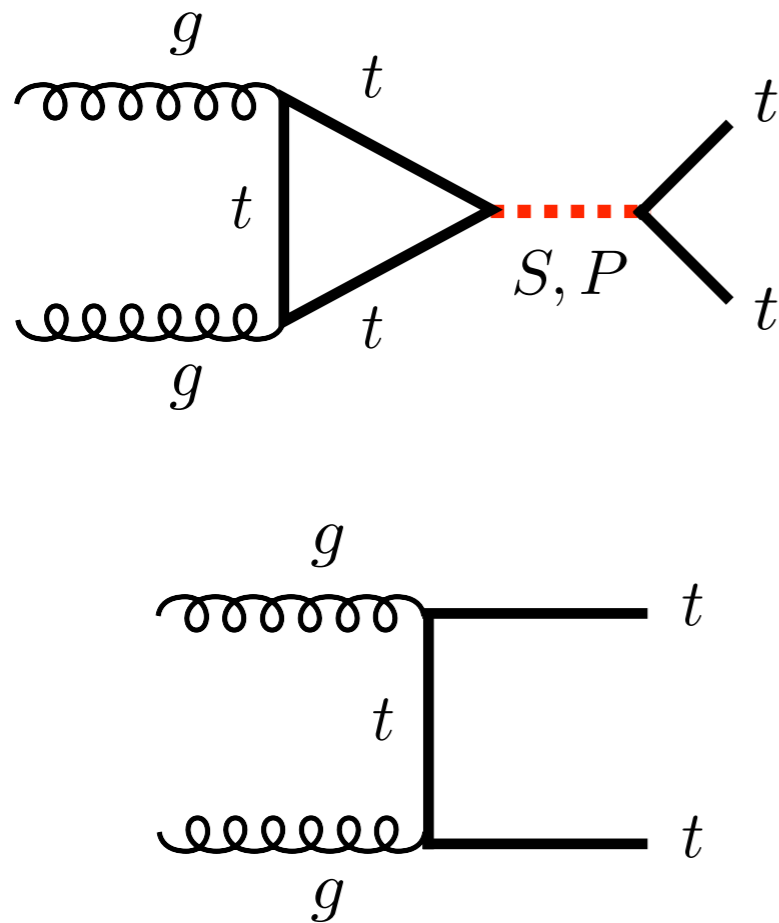
[CMS PAS EXO-16-030]



Mediators with mass down to 100 GeV can be tested by considering tri-jet events where one jet is hard & comes from ISR

[di-lepton limits on spin-1 models discussed by Bryan, Felix & Stefan]

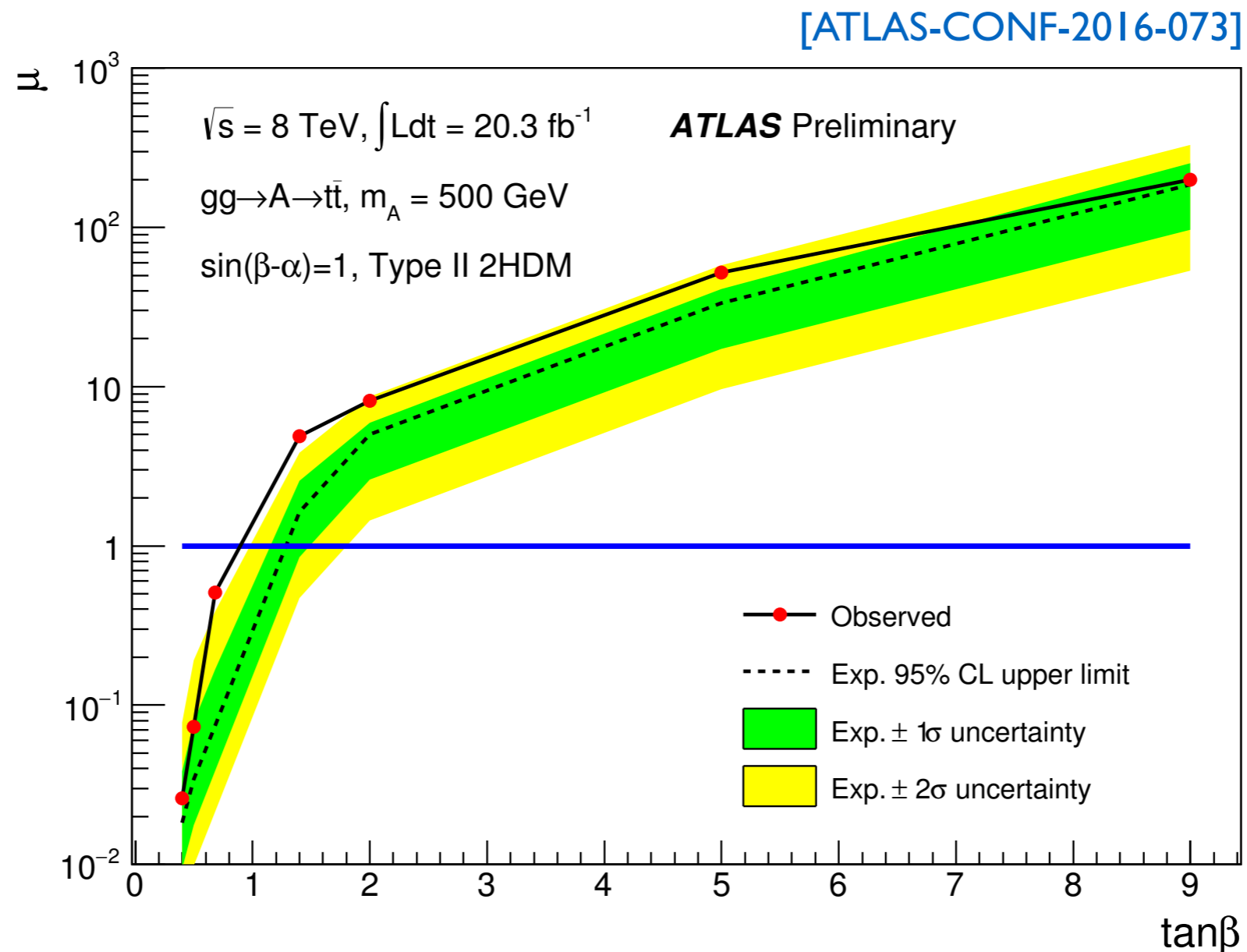
Spin-0 simplified models: di-top limits



Spin-0 di-top resonances interfere maximal with SM background, which leads to a peak-dip structure in $m_{t\bar{t}}$ invariant mass spectrum

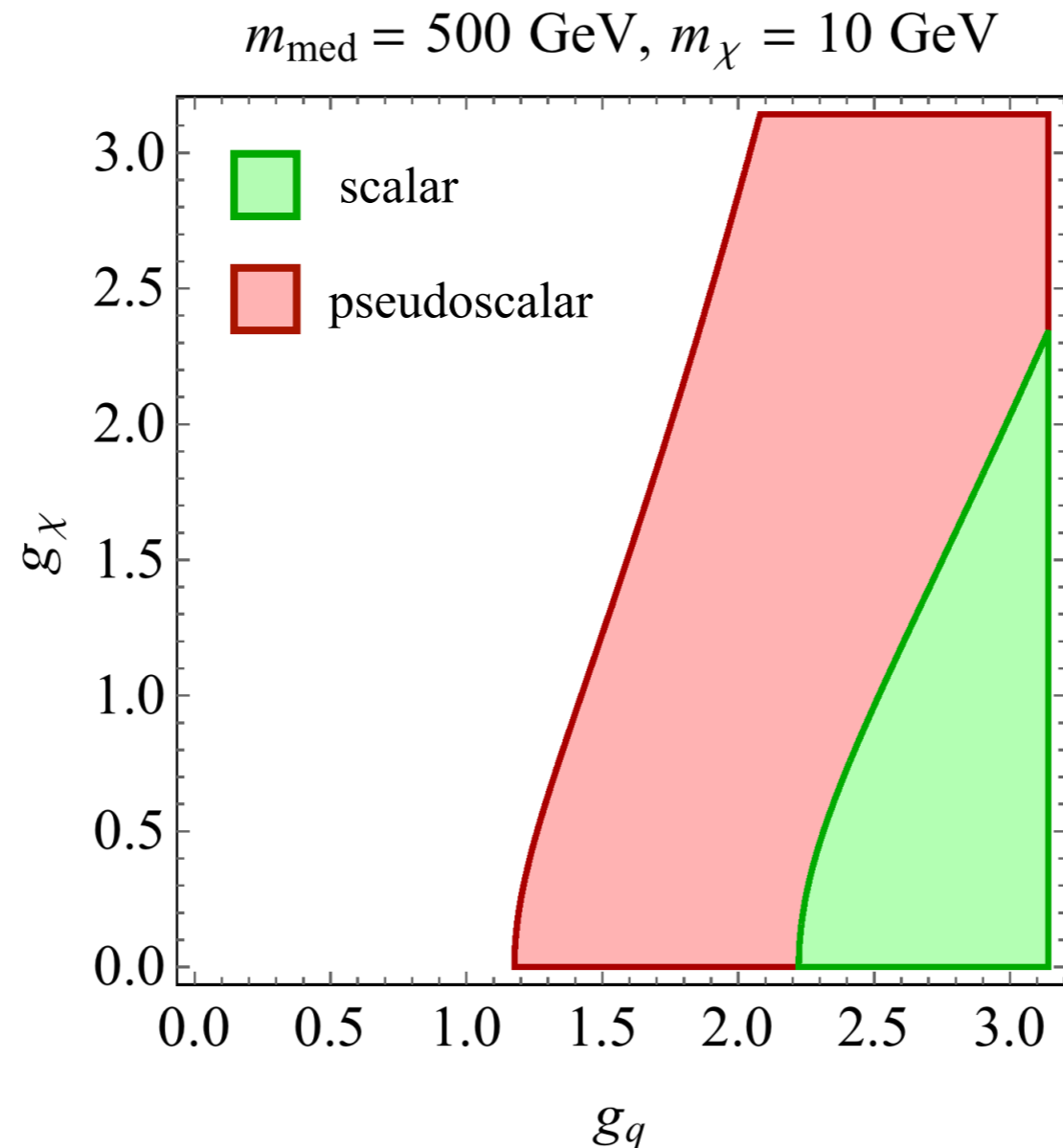
[Dicus et al., 9404359; Frederix & Maltoni, 0712.2355; Craig et al., 1504.04630; Bernreuther et al., 1511.05584; ...]

Spin-0 simplified models: di-top limits



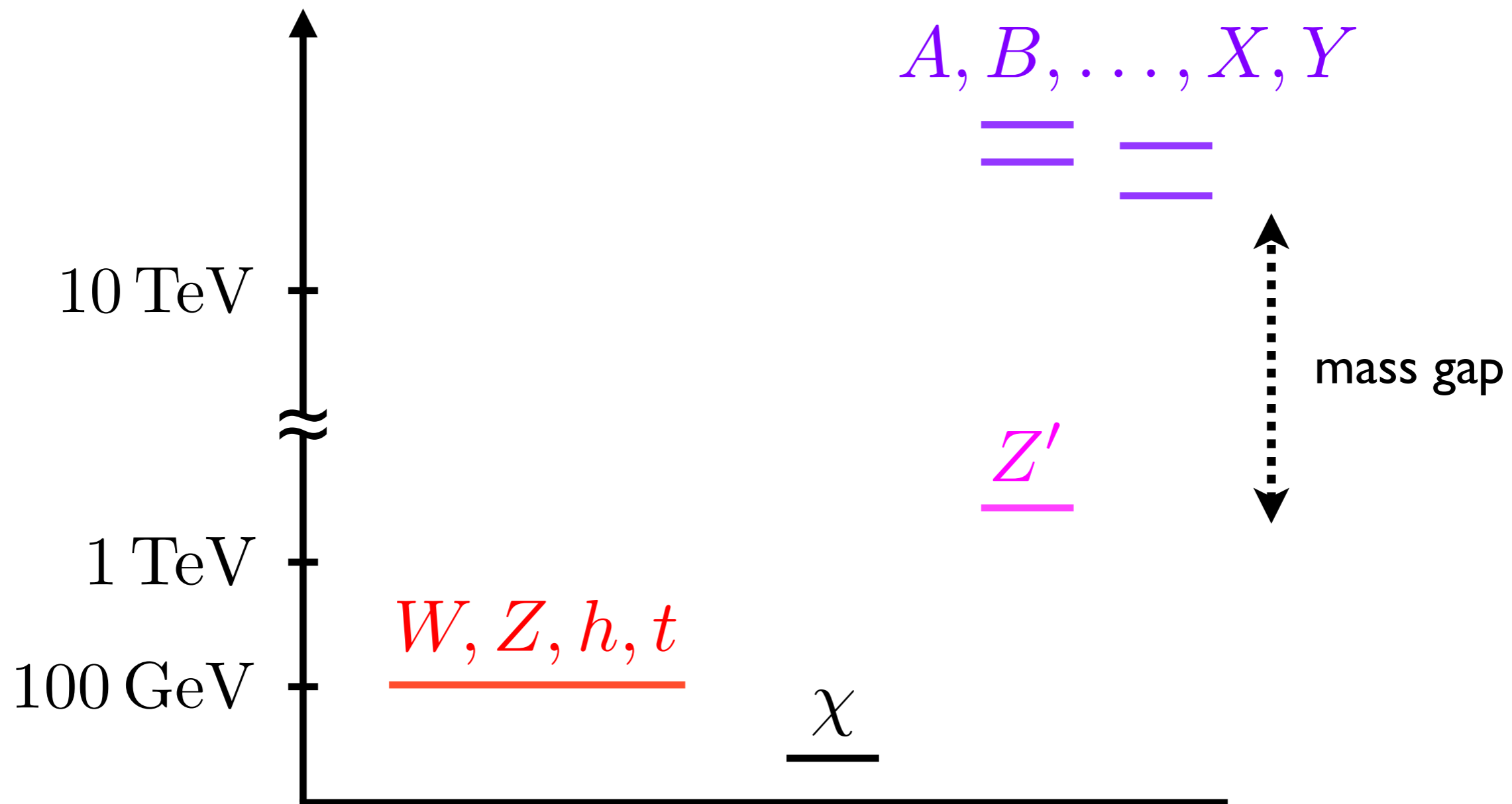
For a pseudoscalar (scalar) of 500 GeV, values of $\tan\beta < 0.85$ ($\tan\beta < 0.45$) are excluded at 95% CL in type II 2-Higgs doublet model (2HDM-II)

Spin-0 simplified models: di-top limits



Easy to recast ATLAS limits to spin-0 simplified model parameter space. For light DM & mediator masses close to $t\bar{t}$ threshold get sensitivity to couplings close to 2 (1) in scalar (pseudoscalar) case

Cartoon of simplified model



Are DM simplified models perfect?

By construction DM & mediator only relevant degrees of freedom at LHC energies. SM- & DM-mediator couplings are treated as free parameters & mechanism that provides mass to DM & mediator is unspecified

In ultraviolet (UV) complete model such as SM, couplings are usually not random but fixed by for example gauge invariance & anomalies. Higgs mechanism also an important ingredient in SM

To UV complete simplified models have to add more structure to them & question is whether effects of new particles decouple or in fact change LHC phenomenology

How-to spot potential problems?

There are at least two ways to figure out if use of simplified model is viable at LHC:

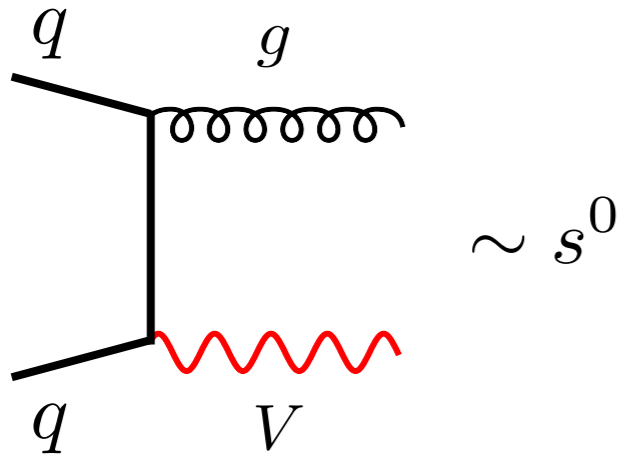
- (i) take simplified model as is & see if scattering amplitudes relevant to DM searches violate perturbative unitarity at LHC energies

[see for instance Englert et al., [1604.07975](#)]

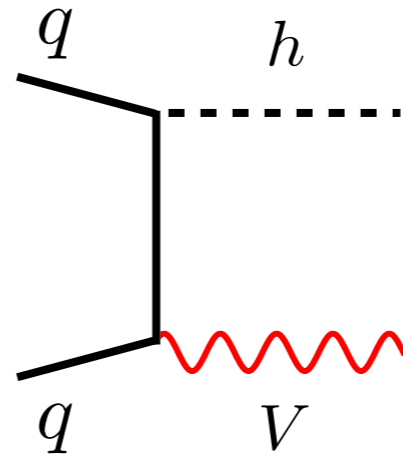
- (ii) extend simplified model by a dark Higgs sector, new fermion sector, etc. & study if additional particle content modifies existing signals or leads to new signatures

[see for instance Kahlhoefer et al., [1510.02110](#); Duerr et al., [1606.07609](#)]

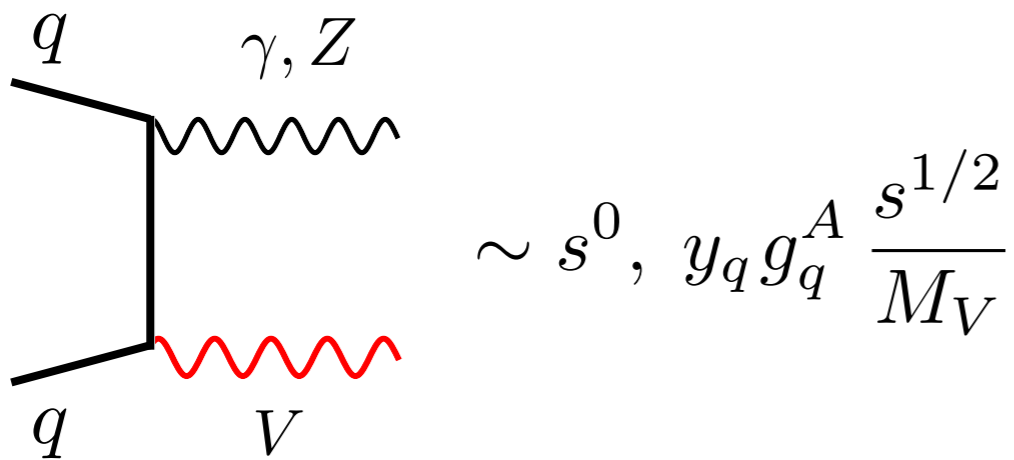
Spin-1 mono-X amplitudes



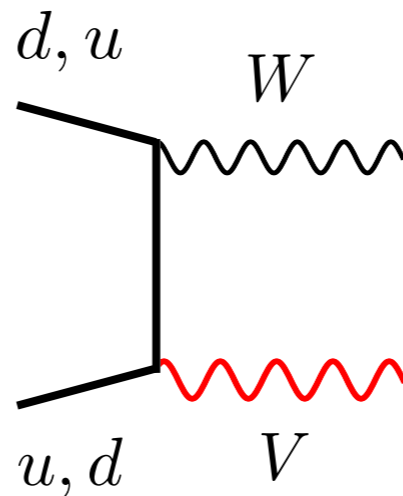
$$\sim s^0$$



$$\sim y_q g_q^A \frac{s^{1/2}}{M_V}$$



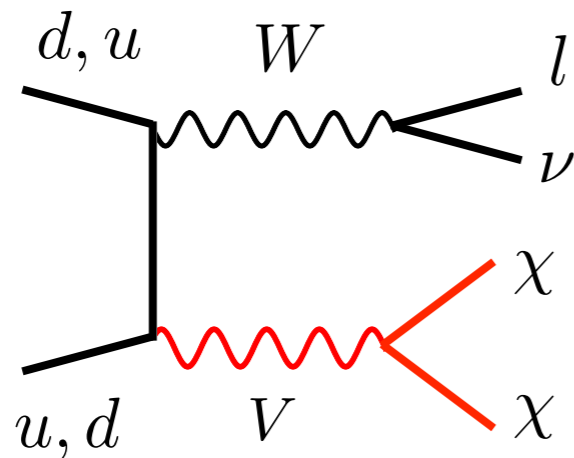
$$\sim s^0, y_q g_q^A \frac{s^{1/2}}{M_V}$$



$$\sim (g_u^L - g_d^L) \frac{s}{M_W M_V}$$

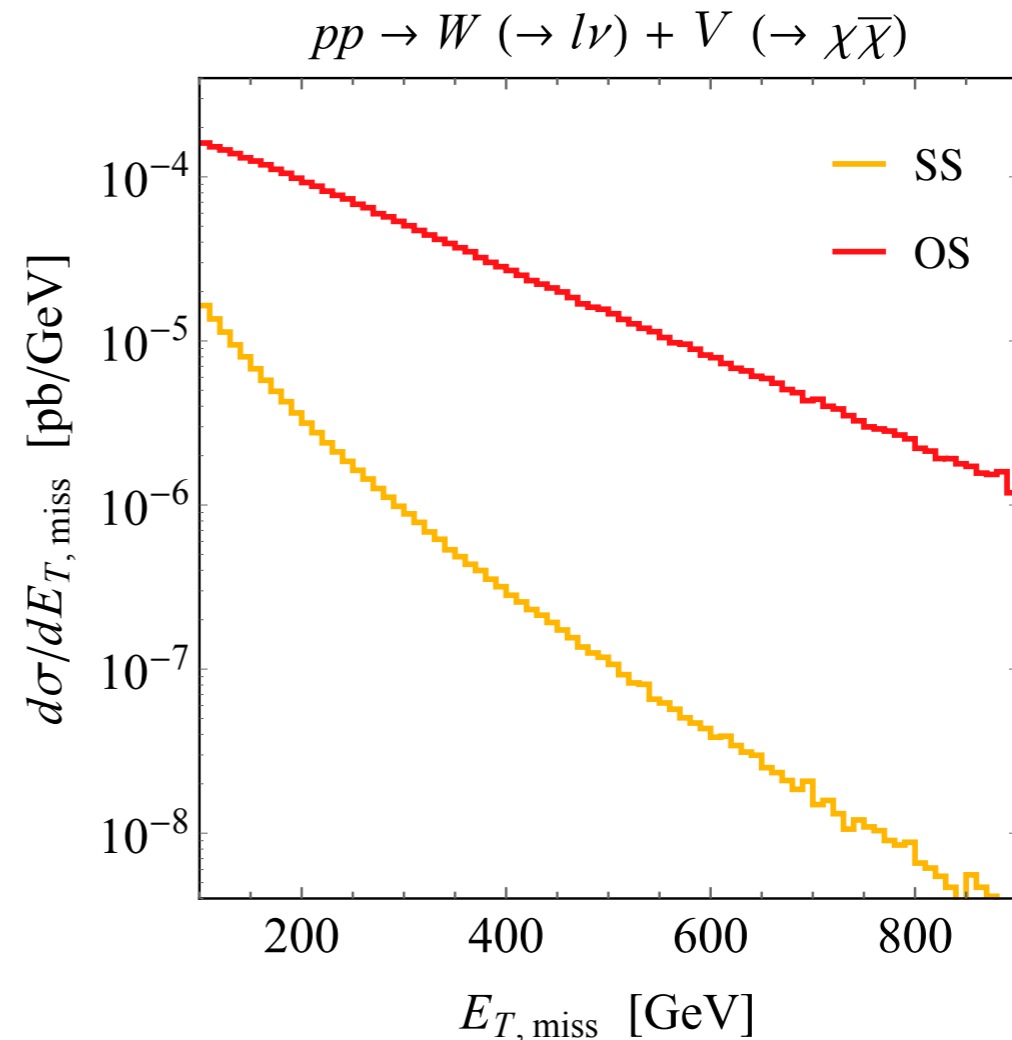
$E_{T,\text{miss}}$ spectra in mono- W sample

[UH, Kahlhoefer & Tait, 1603.01267]



same-sign (SS): $g_u = g_d$

opposite-sign (OS): $g_u = -g_d$



For OS couplings $E_{T,\text{miss}}$ spectrum significantly harder than in SS case. This is an artefact of unitarity violation & thus unphysical

[see also Bell et al., 1503.07874, 1512.00476]

Cures & consequences

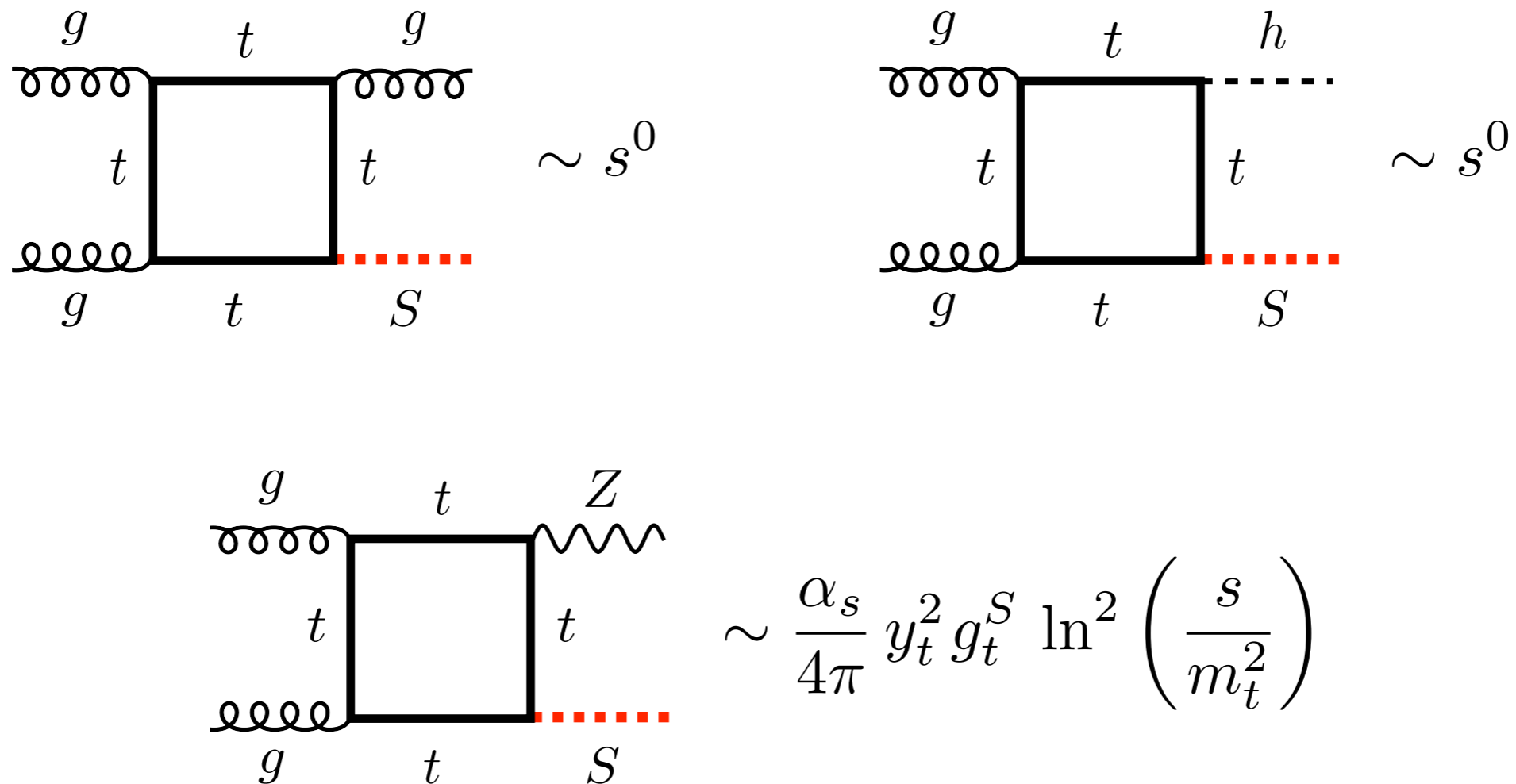
There are several ways to tame unitarity problem in $pp \rightarrow E_{T,\text{miss}} + W$:

- (i) formulate couplings between u, d & V in gauge-invariant way
- (ii) add a WWV vertex to spin-1 simplified model
- (iii) implement interactions of quarks & V via dimension-6 operators

Irrespectively of how issue is resolved, sensitivity of mono-jet searches will always exceed that of mono- W channel in modified theory. Same verdict has been reached in EFT case & t-channel simplified DM models with coloured scalar exchange

[see backup slides for details & Bell et al., 1503.07874, 1512.00476 for EFT & t-channel discussions]

Spin-0 mono-X amplitudes



1-loop $gg \rightarrow Z+S$ amplitude diverges for $s \rightarrow \infty$. Naively, numerical effect small unless coupling g_t^S large & centre-of-mass energy $s^{1/2} \gg 13 \text{ TeV}$

Structure of spin-0 simplified model

Since left- & right-handed SM fermions have different quantum numbers, interaction of form

$$\mathcal{L}_S \supset \sum \frac{g_q y_q}{\sqrt{2}} \bar{q} q S = \sum \frac{g_q y_q}{\sqrt{2}} (\bar{q}_L q_R + \bar{q}_R q_L) S$$

not $SU(2)_L \times U(1)_Y$ gauge invariant

Given that S is a SM singlet, terms like

$$S|H|^2, S^2|H|^2, S^3, S^4$$

not forbidden by EW symmetry. Why are such couplings not included?

Extensions of spin-0 simplified model

$$\mathcal{L} \supset \mu s H^\dagger H$$



Two physical spin-0 states h, S
& single mixing angle Θ



Model predicts universal suppression of Higgs couplings as modifications of gauge-scalar & fermion-scalar couplings fully correlated. If kinematically allowed new Higgs decays $h \rightarrow \chi\bar{\chi}$ & $h \rightarrow SS$ present. All $E_{T,\text{miss}}$ cross sections are changed. In particular, $V+E_{T,\text{miss}}$ as well as $\text{VBF}+E_{T,\text{miss}}$ contributions arise

Extensions of spin-0 simplified model

$$\mathcal{L} \supset i\mu a H_u^\dagger H_d + \text{h.c.}$$



Six physical spin-0 states h, H, A, H^\pm, P & three mixing angle α, β, Θ



Can decouple gauge-scalar & fermion-scalar couplings which allows to avoid Higgs constraints. Besides invisible & exotic Higgs decays, also neutral & charged Higgs searches & flavour physics constrain parameter space. In alignment/decoupling limit, $E_{T,\text{miss}}$ signatures driven by fermionic contributions while $V+E_{T,\text{miss}}$ & $VBF+E_{T,\text{miss}}$ channels necessarily small

Mono-jet backgrounds at 8 TeV

[CMS, 1408.3583]

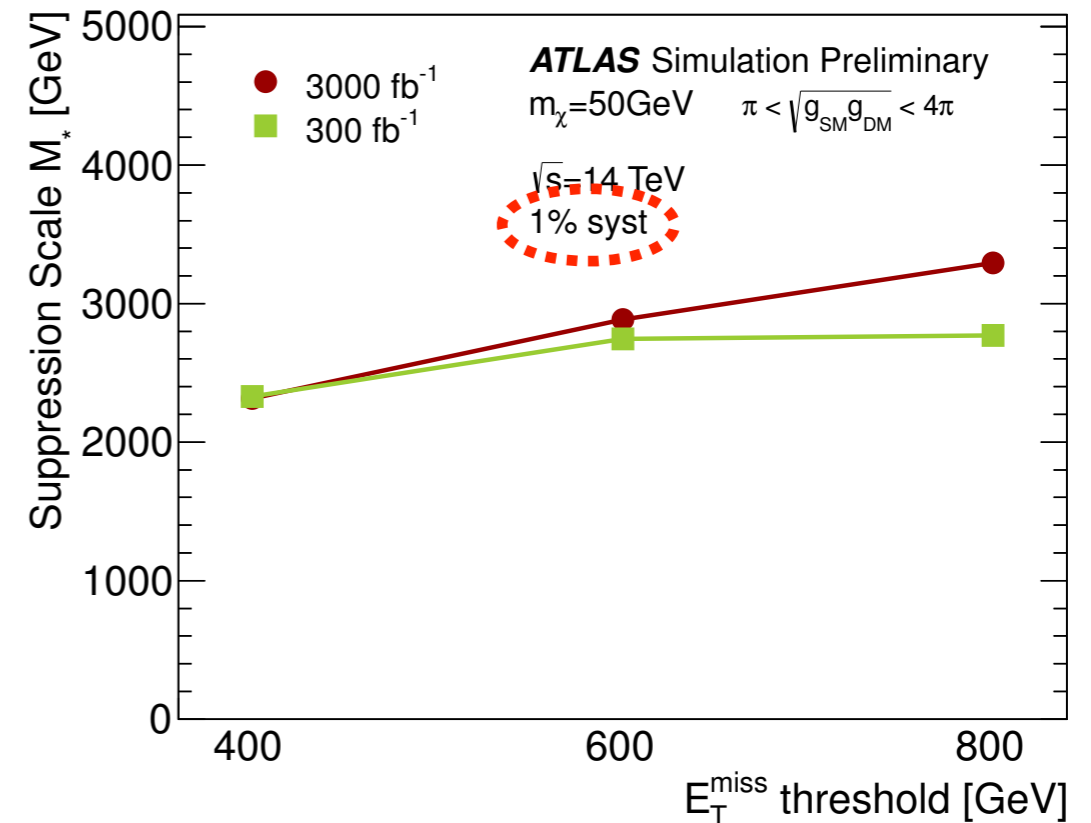
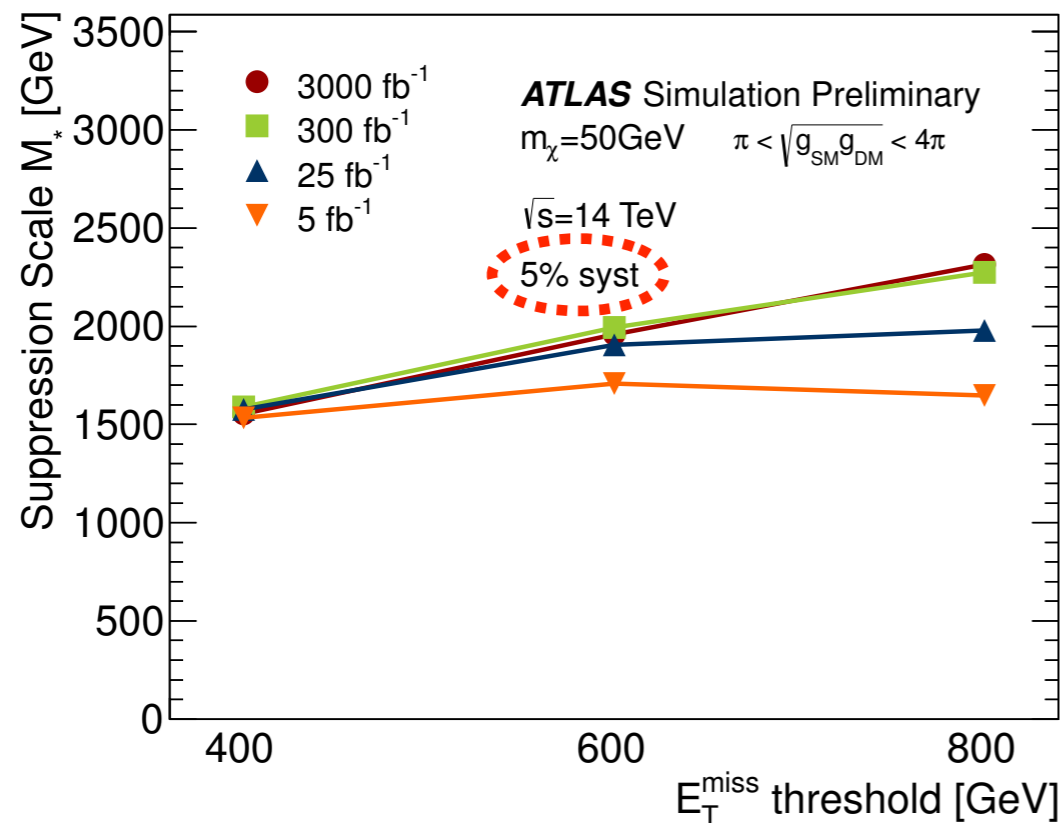
relative
uncertainty

E_T^{miss} (GeV)	>250	...	>550	
Z($\nu\nu$)+jets	32100 \pm 1600	...	362 \pm 64	13%
W+jets	17600 \pm 900	...	123 \pm 13	3%
t \bar{t}	446 \pm 220	...	2.8 \pm 1.4	
Z(ll)+jets	139 \pm 70	...	1.0 \pm 0.5	
Single t	155 \pm 77	...	—	
QCD multijets	443 \pm 270	...	0.5 \pm 0.3	
Diboson	980 \pm 490	...	20 \pm 10	2%
Total SM	51800 \pm 2000	...	509 \pm 66	
Data	52200	...	519	

At 8 TeV SM background to mono-jet searches has an error of $O(10\%)$

Mono-jet prospects at 14 TeV

[ATL-COM-PHYS-2014-549]



At high-luminosity LHC, systematic uncertainties will limit reach of mono-jet searches. How far can one push these uncertainties down? 1% seems like a big challenge for both experiment & theory

I am looking forward ...

to 19 presentations & two days of lively discussions about the future of DM searches at the LHC

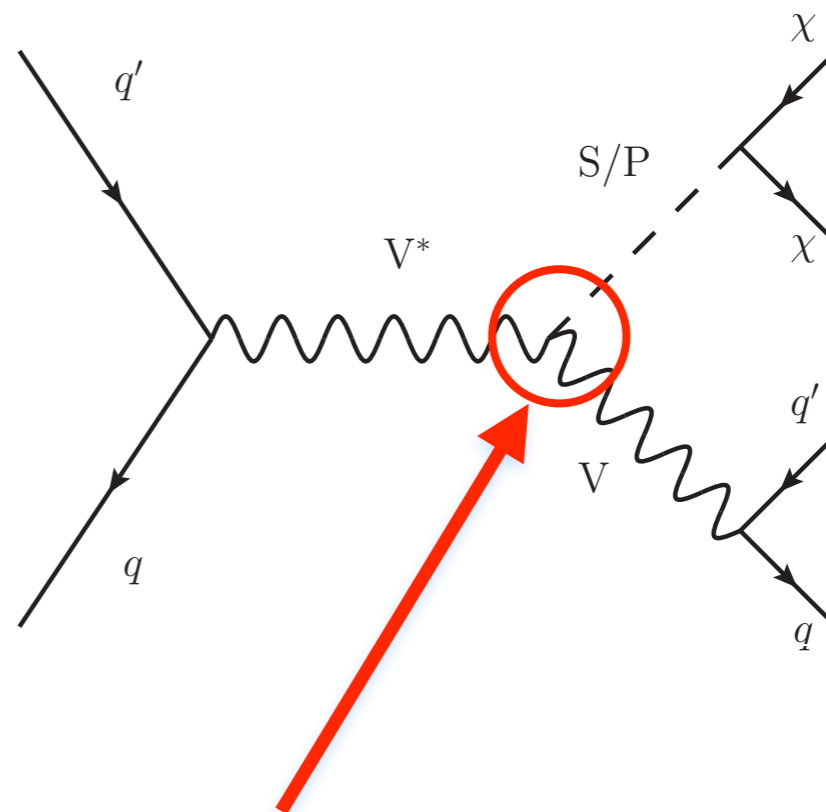
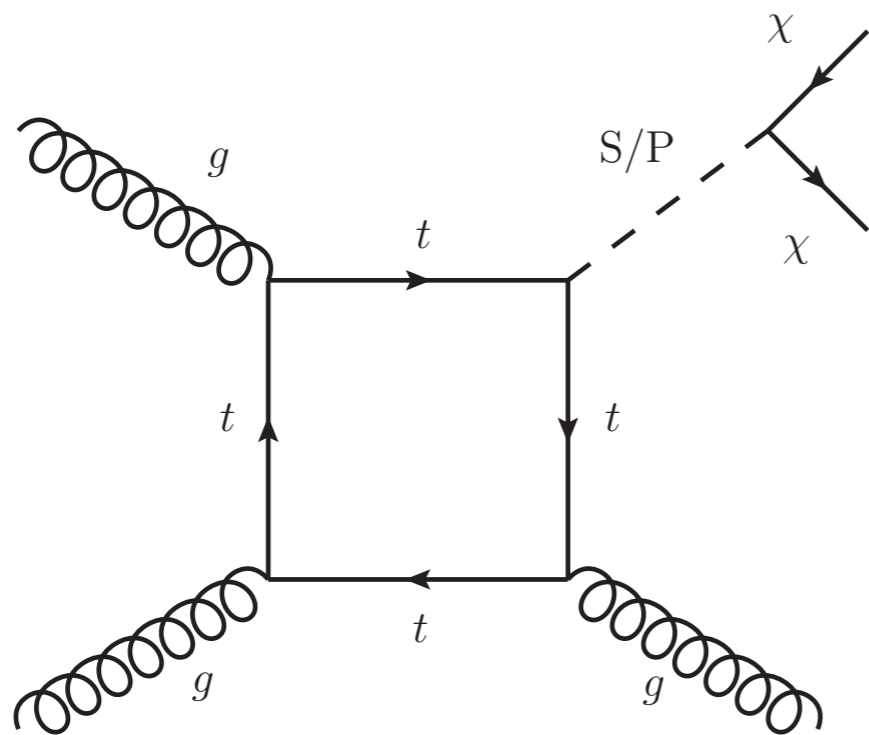
Backup



CMS, 1607.05764

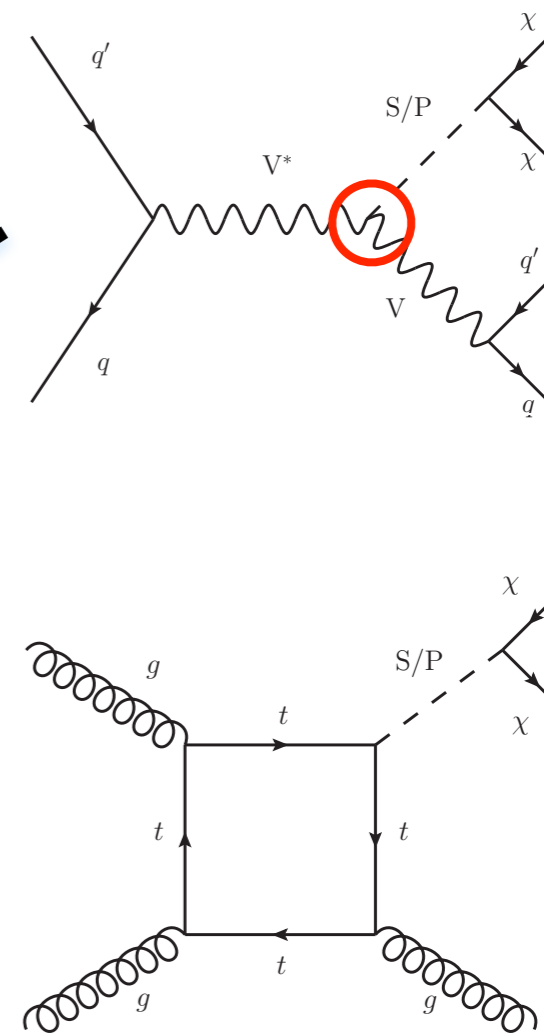
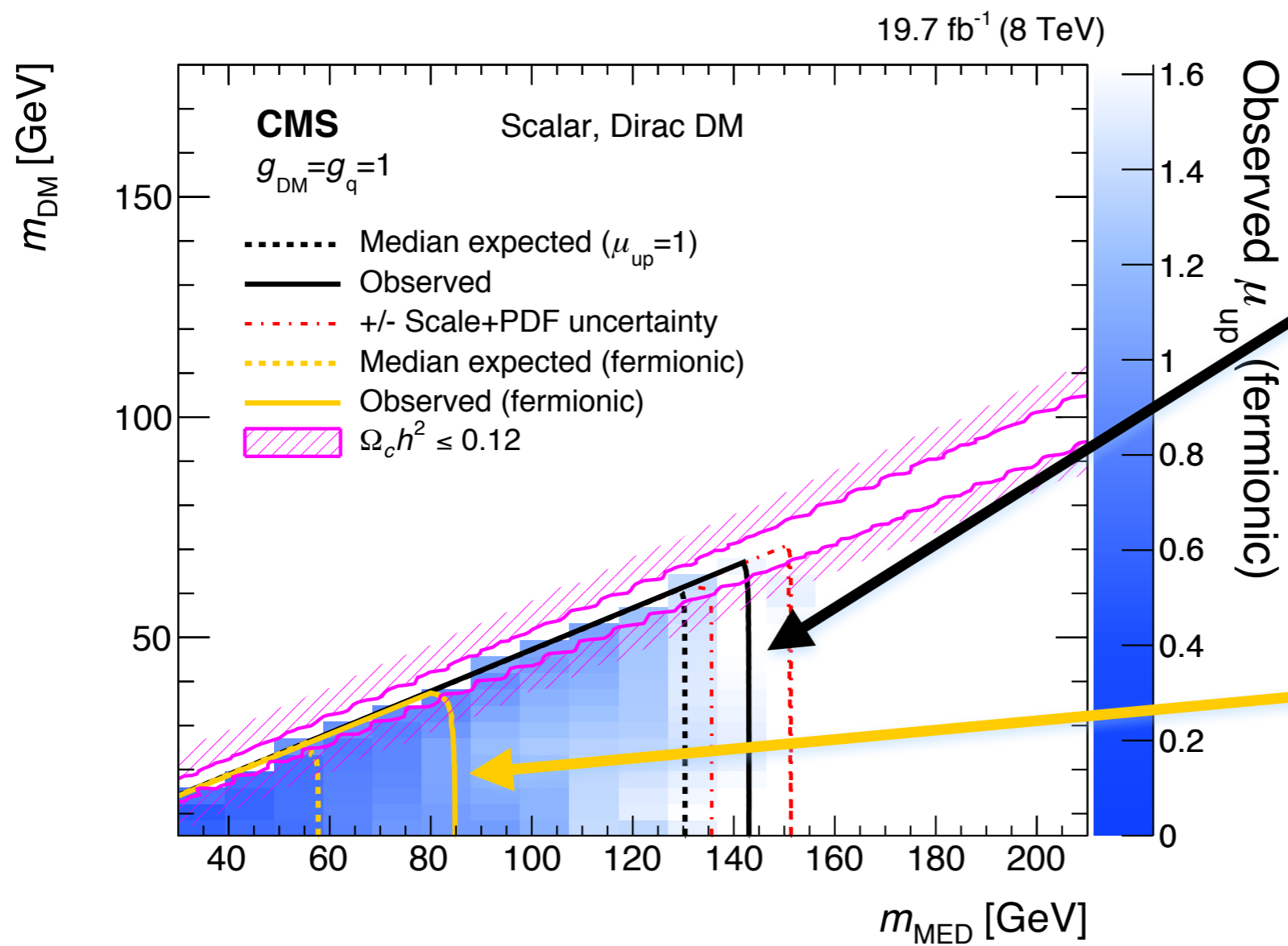
$$\mathcal{L}_{\text{scalar}} \supset -\frac{1}{2}m_{\text{MED}}^2 S^2 - g_{\text{DM}} S \bar{\chi} \chi - g_q \sum_{q=b,t} \frac{m_q}{v} S \bar{q} q - m_{\text{DM}} \bar{\chi} \chi,$$

$$\mathcal{L}_{\text{pseudoscalar}} \supset -\frac{1}{2}m_{\text{MED}}^2 P^2 - ig_{\text{DM}} P \bar{\chi} \gamma^5 \chi - ig_q \sum_{q=b,t} \frac{m_q}{v} P \bar{q} \gamma^5 q - m_{\text{DM}} \bar{\chi} \chi,$$

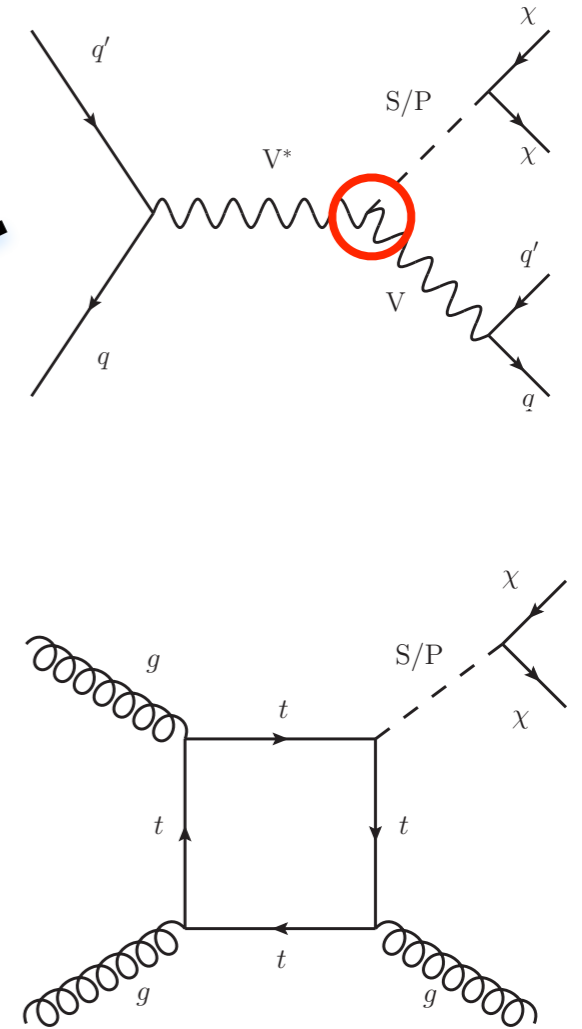
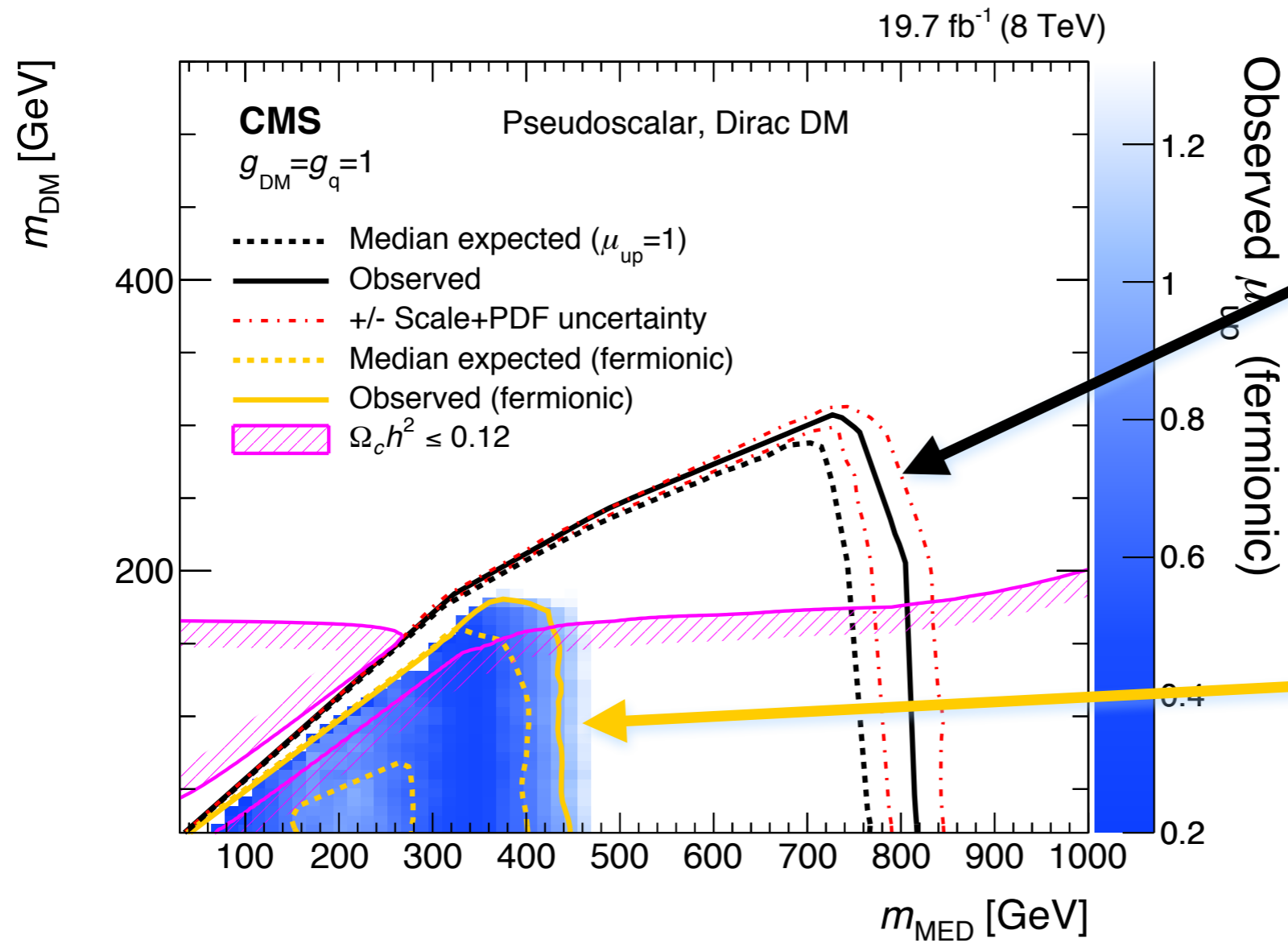


where does this vertex come from?

CMS, 1607.05764

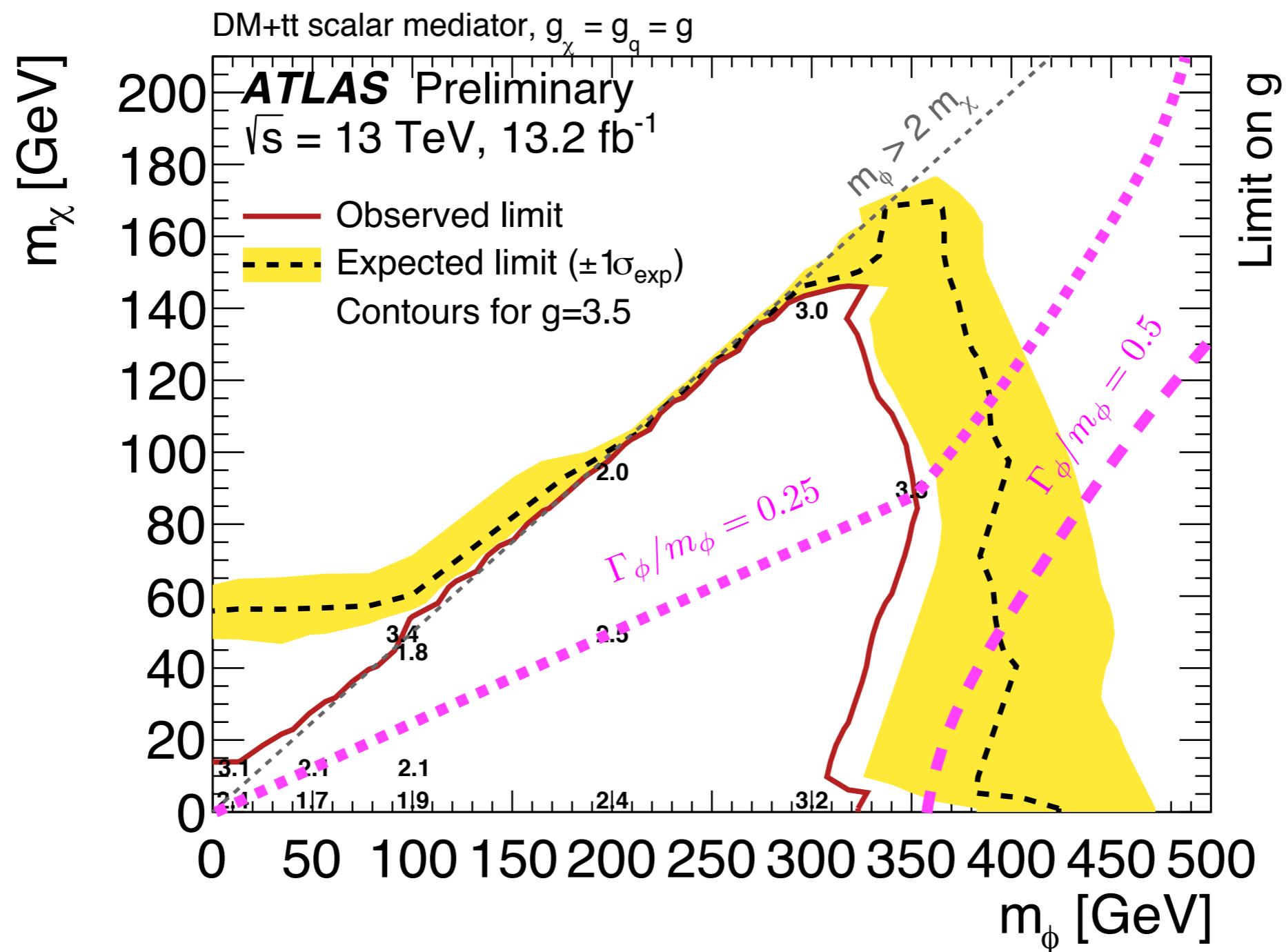


CMS, 1607.05764



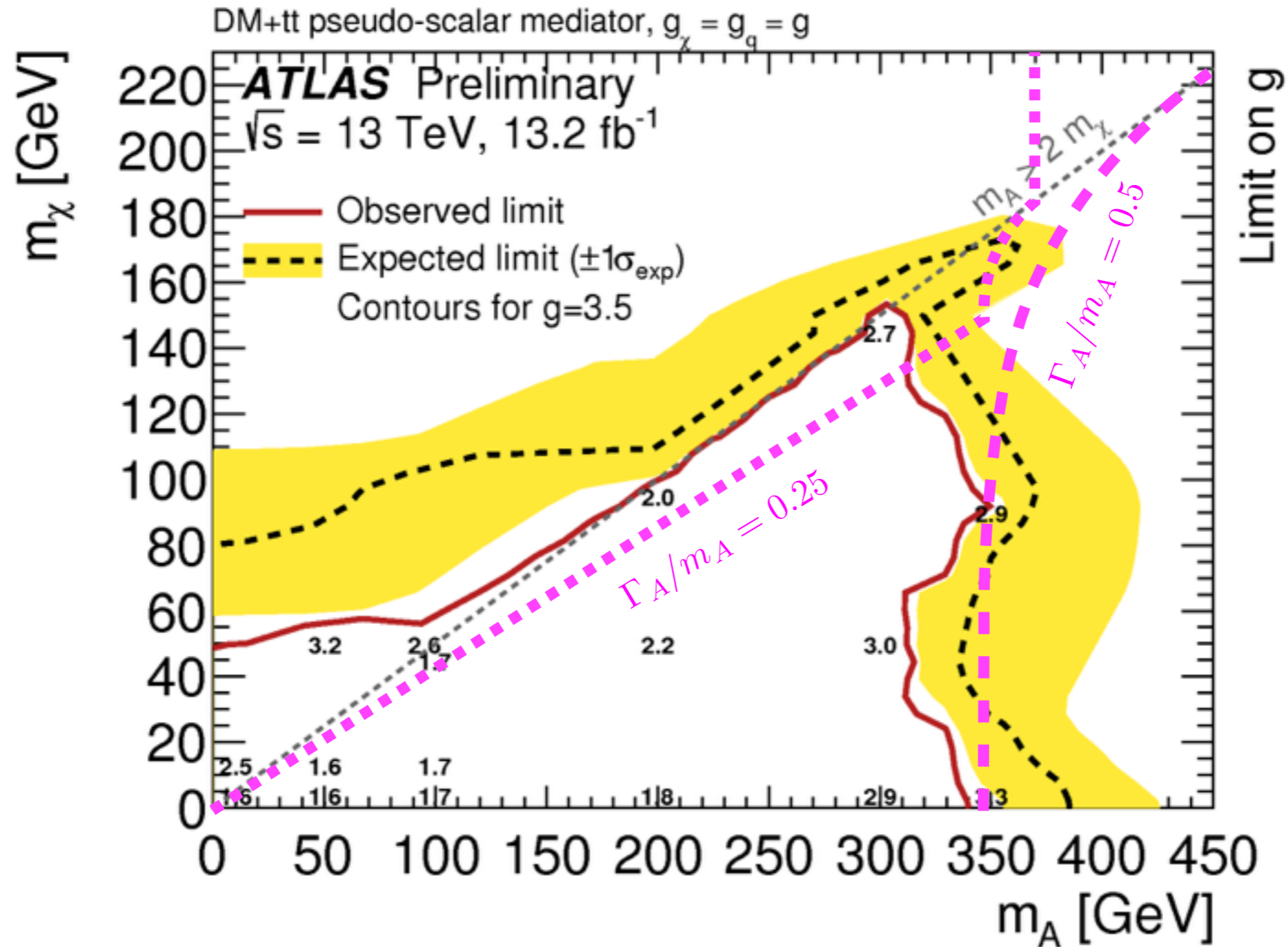
13 TeV limits on $E_{T,miss} + t\bar{t}$

[ATLAS-CONF-2016-050]



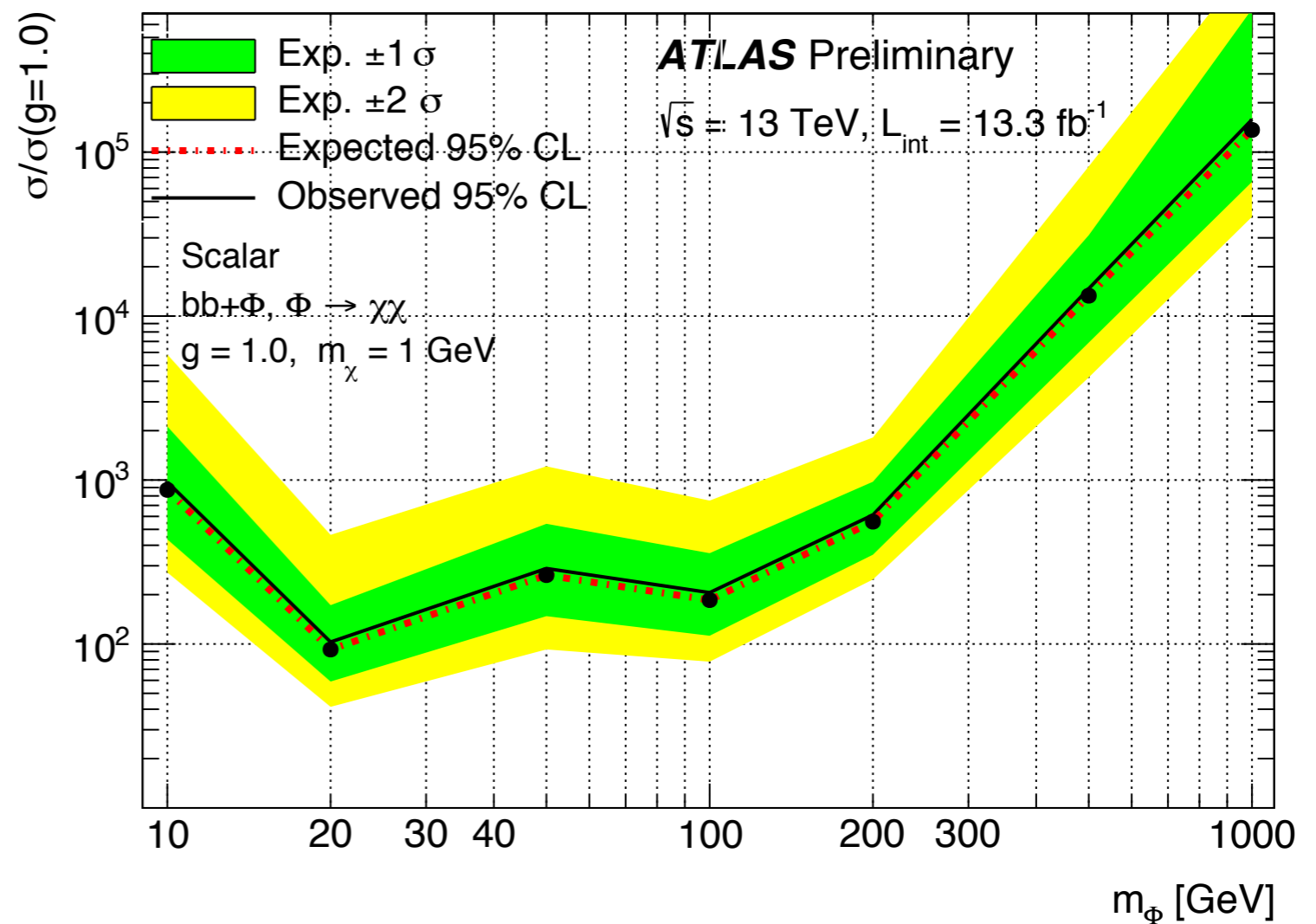
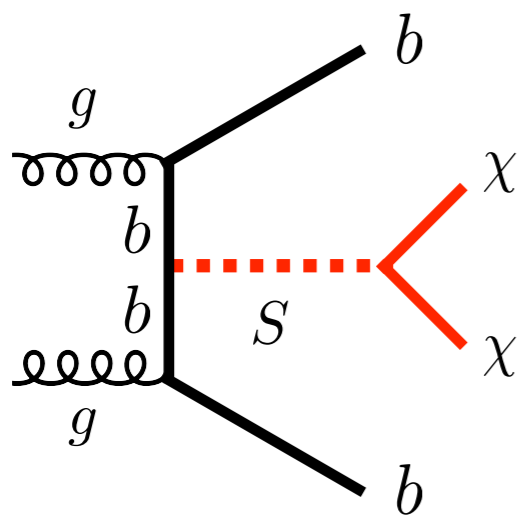
13 TeV limits on $E_{T,miss} + t\bar{t}$

[ATLAS-CONF-2016-050]



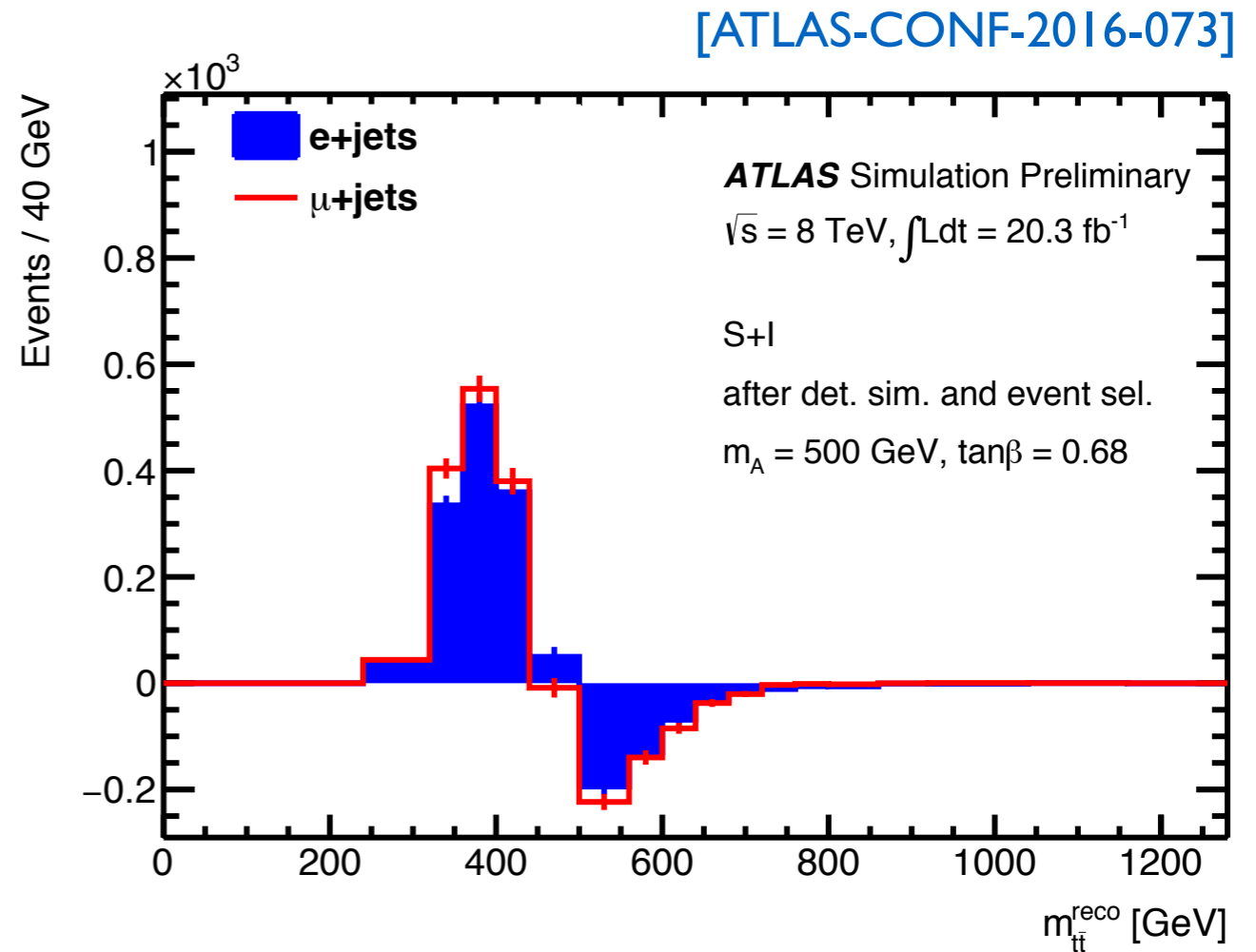
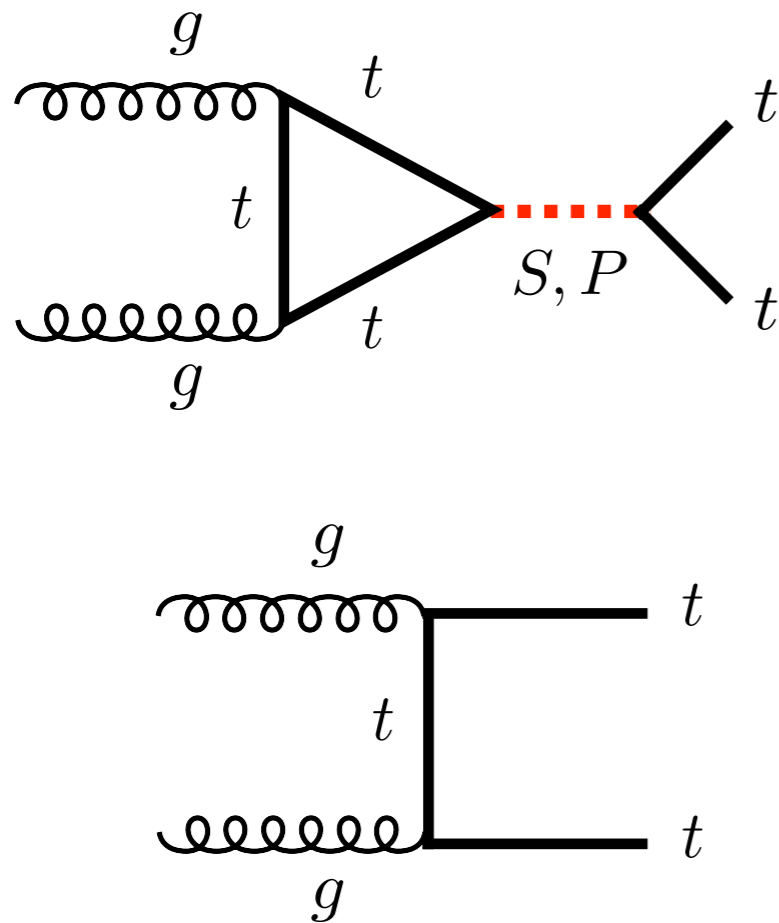
13 TeV limits on $E_{T,miss} + b\bar{b}$

[ATLAS-CONF-2016-086]



$E_{T,miss} + b\bar{b}$ searches not yet sensitive to spin-0 models with weak couplings

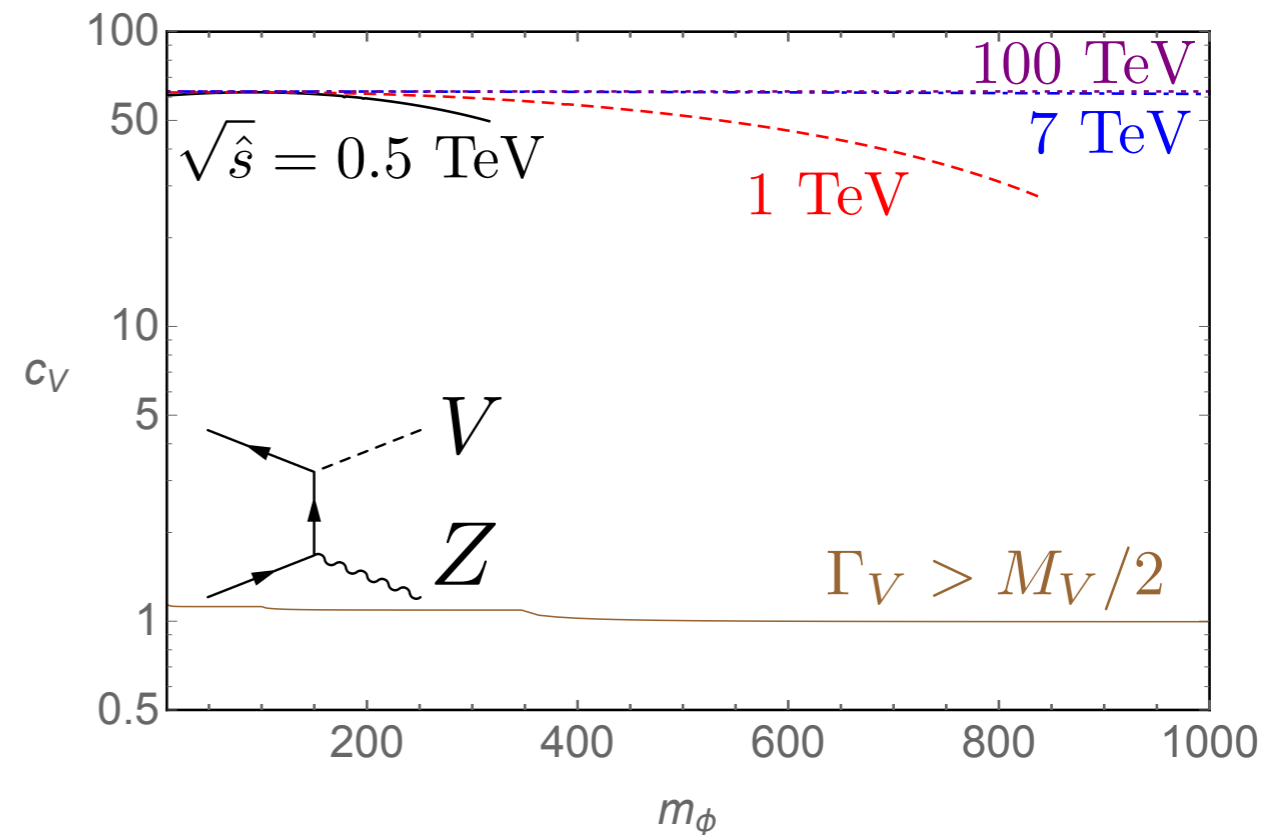
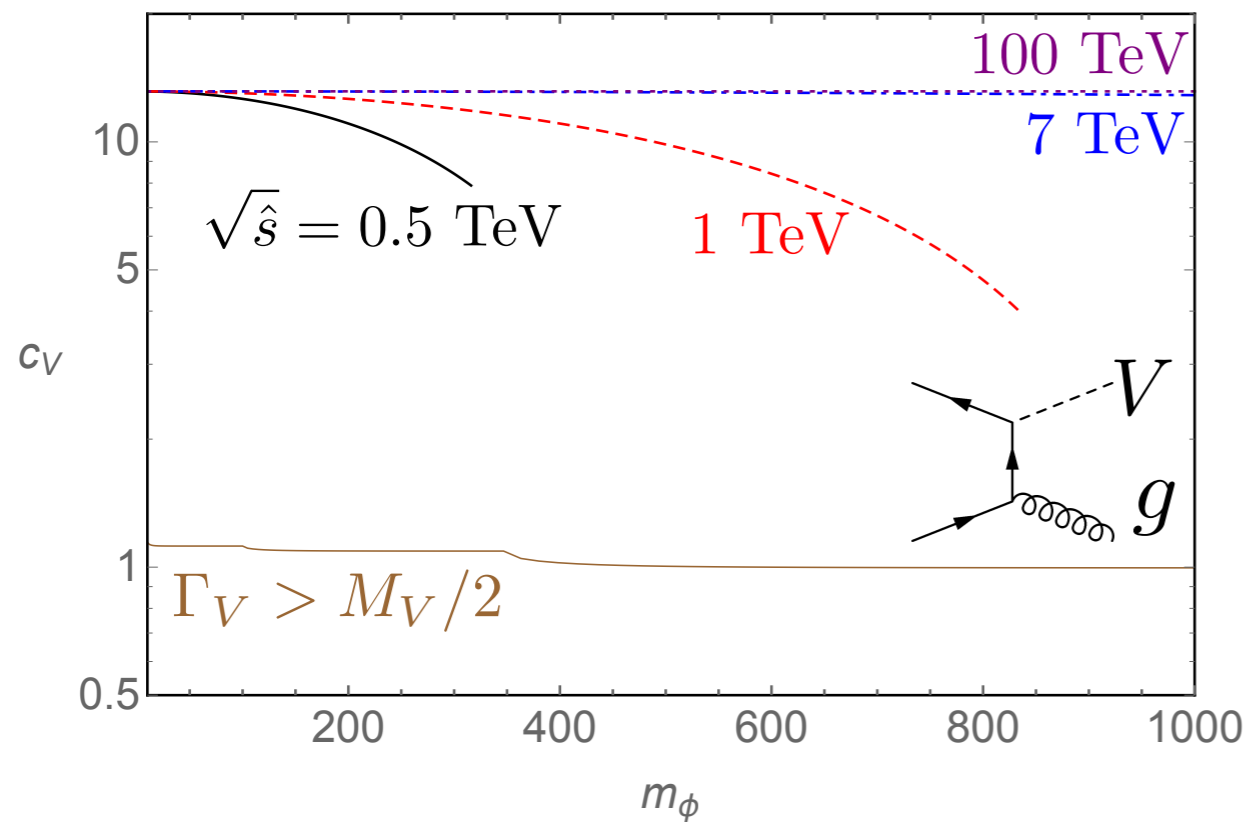
Di-top limits



Compared to parton-level spectra, reconstructed distributions with narrower resonances are more strongly distorted due detector resolution

Unitarity: $E_{T,\text{miss}+\text{jet}}$, Z , h searches

[Englert et al., 1604.07975]

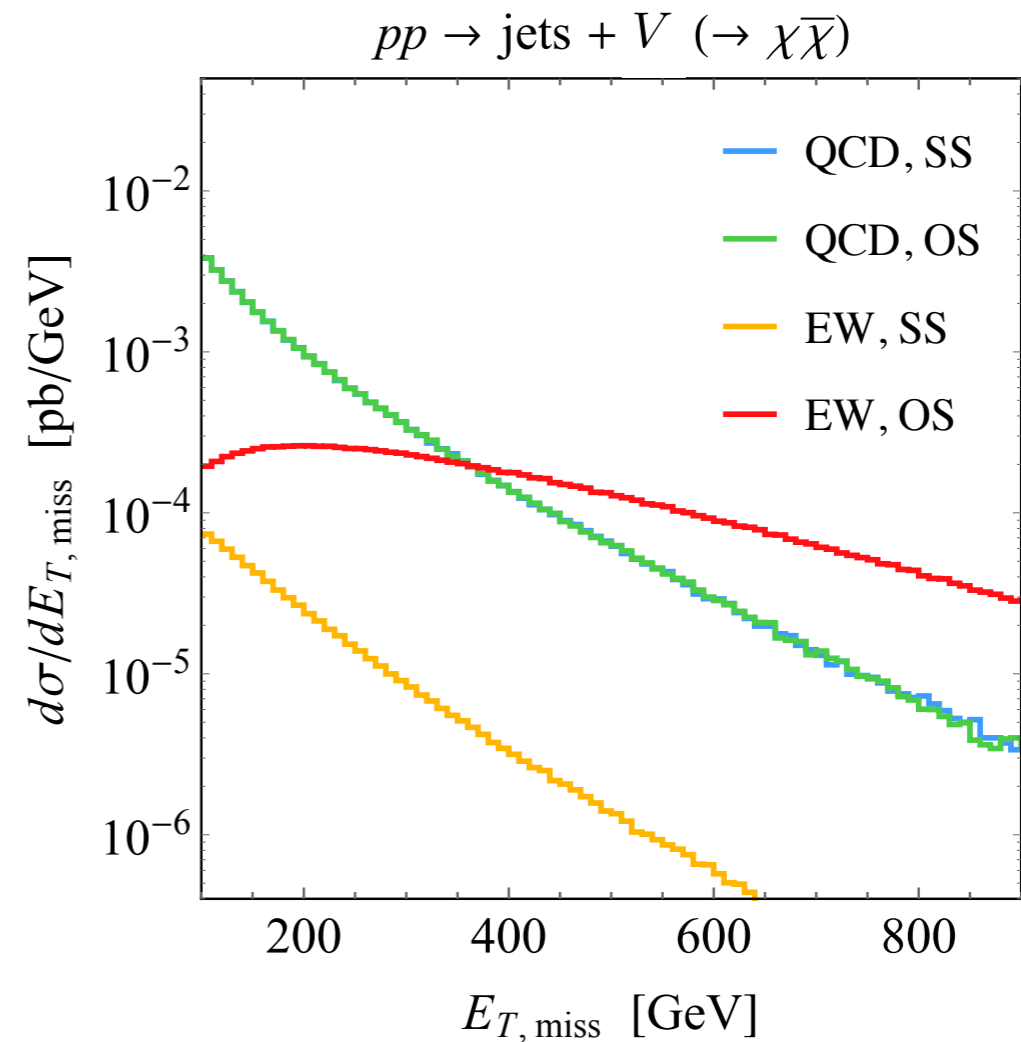
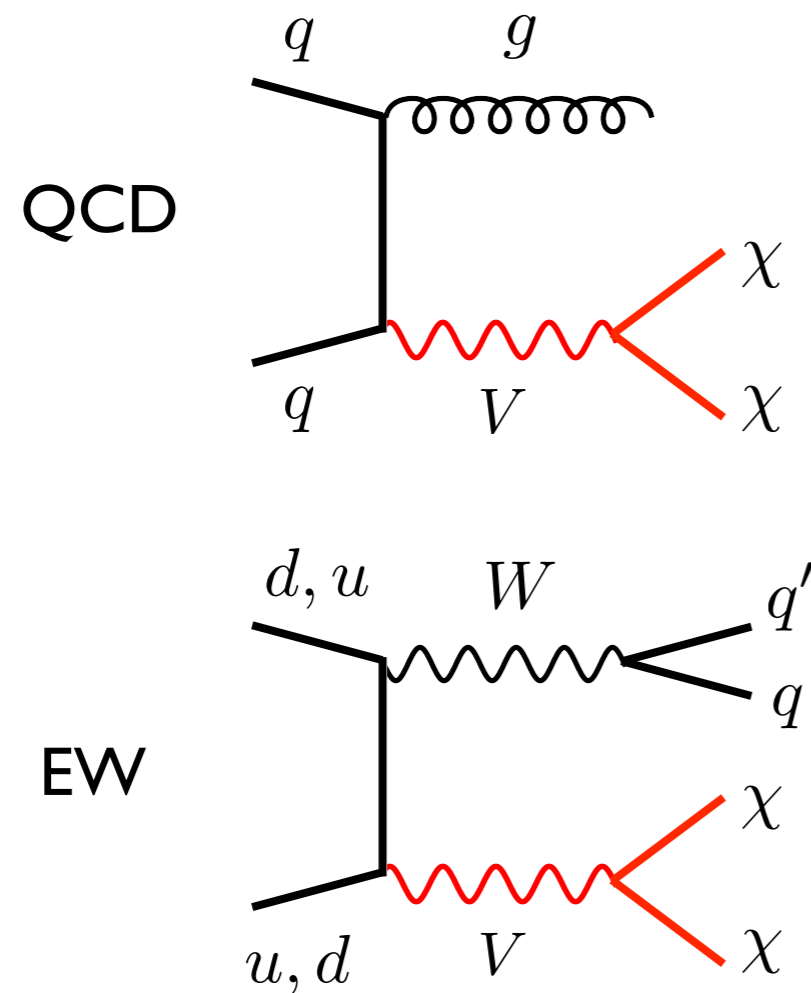


$E_{T,\text{miss}+\text{jet}}$, Z , h amplitudes in spin-1 models have no problem with unitarity at LHC energies & beyond unless DM-mediator couplings are non-perturbative[†]

[†]For such couplings, one always has $\Gamma_V > M_V$ & simple particle description breaks down

$E_{T,miss}$ spectra in mono-jet sample

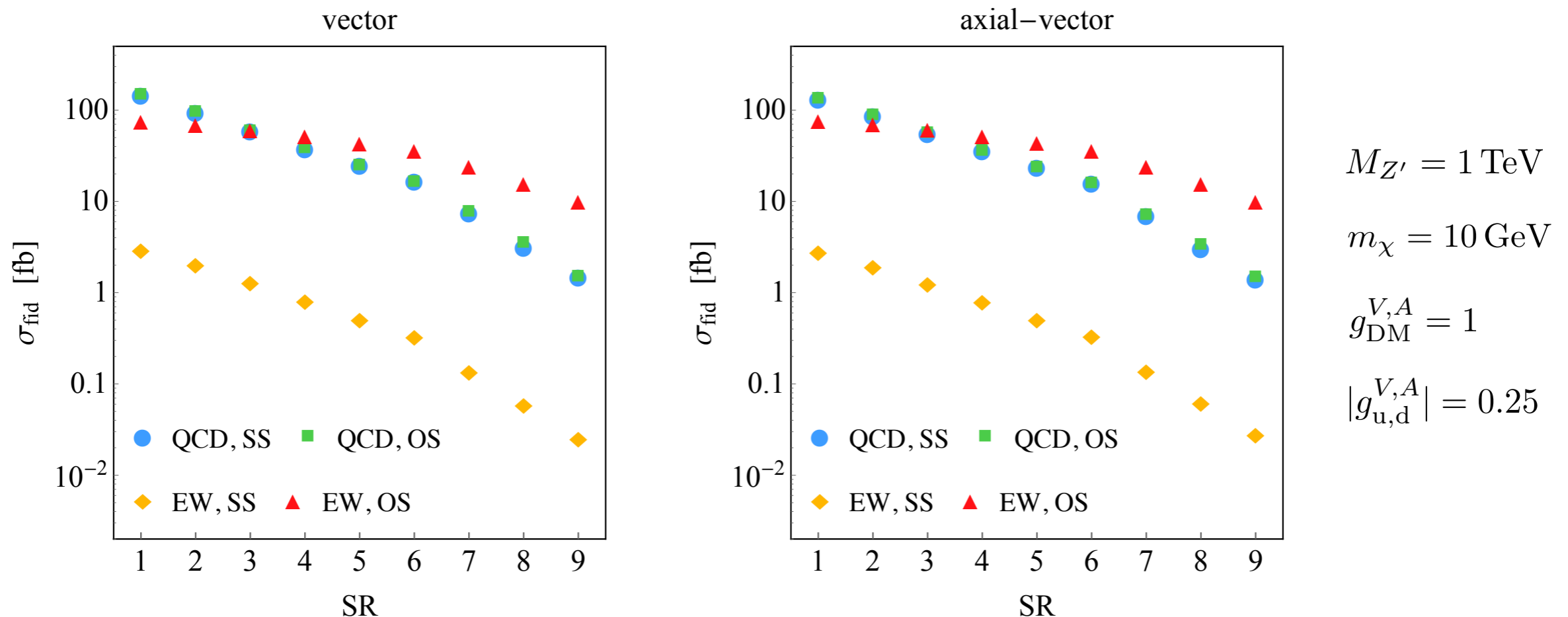
[UH, Kahlhoefer & Tait, 1603.01267]



In fact, EW channel $pp \rightarrow W(\rightarrow q\bar{q}') + V(\rightarrow \chi\bar{\chi})$ even produces harder mono-jet events than QCD process $pp \rightarrow \text{jets} + V(\rightarrow \chi\bar{\chi})$

Mono-W problem in mono-jets

[UH, Kahlhoefer & Tait, 1603.01267]



Unitarity problem persists after parton shower, hadronisation corrections & detector effects. As a result, EW contribution gives rise to majority of events in high- $E_{T,\text{miss}}$ signal regions (SRs) of mono-jet searches[†] in OS case

[†]Plots show SRs as defined in ATLAS, 1502.01518

Mono-W problem: solution I

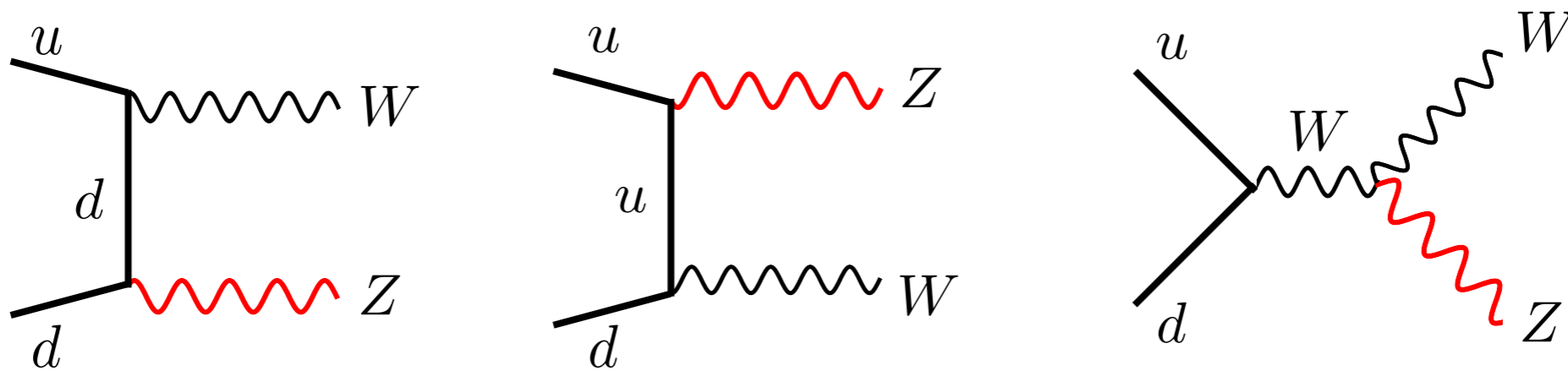
Since s-behaviour of $ud \rightarrow W+V$ amplitude proportional to $g_u^L - g_d^L$
 tree-level unitarity recovered for $g_Q = g_d^L = g_u^L$. Latter requirement
 automatically fulfilled, if quark couplings to V are written in a way
 that preserves EW symmetry:

$$\mathcal{L}_{Vq\bar{q}} = - \sum_{u,d} V_\mu (g_Q \bar{Q}_L \gamma^\mu Q_L + g_u \bar{u}_R \gamma^\mu u_R + g_d \bar{d}_R \gamma^\mu d_R)$$

$$Q_L = (u_L, d_L)^T$$

Mono-W problem: solution 2

Second solution obtained by thinking about how unitarity of $ud \rightarrow W+Z$ amplitude is realised within SM:



$$|\mathcal{M}|^2 = \frac{3g^4 c_w^2 |V_{ud}|^2}{32M_W^2} (d_1 + d_2 - 2d_3) s^2 \sin^2 \theta$$

Diagram with WWZ coupling cancels divergent s-behaviour of graphs with t-channel quark exchange. This is a result of gauge invariance

Mono-W problem: solution 2

SM result implies that even if

$$\Delta g = g_u^L - g_d^L \neq 0$$

unitarity violation avoided by adding following gauge-boson couplings to Lagrangian:

$$\Delta \mathcal{L} = i \Delta g \left\{ (\partial_\mu W_\nu^+ - \partial_\nu W_\mu^+) W^{\mu-} V^\nu - (\partial_\mu W_\nu^- - \partial_\nu W_\mu^-) W^{\mu+} V^\nu + \frac{1}{2} (\partial_\mu V_\nu - \partial_\nu V_\mu) (W^{\mu+} W^{\nu-} - W^{\mu-} W^{\nu+}) \right\}$$

Mono-W problem: solution 2

In fact, if V arises through mixing with a new vector field X , that is

$$X_\mu = N_{31} A_\mu + N_{32} Z_\mu + N_{33} V_\mu$$

& X has quark couplings of form

$$\mathcal{L}_{Xq\bar{X}} = - \sum_q X_\mu \bar{q} (f_q^V \gamma^\mu + f_q^A \gamma^\mu \gamma_5) q, \quad f_u^L \ominus f_d^L = 0$$

then relevant V couplings automatically obey

$$\Delta g = g_u^L \ominus g_d^L = g N_{23}, \quad g_{WWV} = g N_{23}$$

& modified theory unitary

Mono-W problem: solution 3

Quark-couplings of V can also be realised via dimension-6 operators:

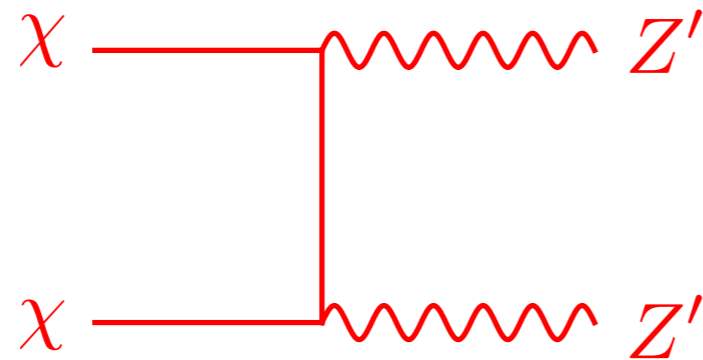
$$\mathcal{L}_{VQH} = - \sum_{u,d} V_\mu \left\{ \frac{1}{\Lambda_u^2} (\bar{Q}_L \tilde{H}) \gamma^\mu (\tilde{H}^\dagger Q_L) + \frac{1}{\Lambda_d^2} (\bar{Q}_L H) \gamma^\mu (H^\dagger Q_L) \right\}$$

In such a case $SU(2)_L$ breaking is however not $O(1)$, but given by[†]

$$\Delta g = g_u^L - g_d^L = \frac{v^2}{\Lambda^2}$$

In this model unitary at 13 TeV LHC requires either $|g_u^{V,A}| = |g_d^{V,A}| < 0.05$ or if $|g_u^{V,A}| = |g_d^{V,A}| = 0.25$ & $M_V = 1$ TeV is chosen, one has to employ truncation with $s^{1/2} \lesssim 6$ TeV. Both options reduce mono-W sensitivity

Unitarity violation: $\chi\bar{\chi} \rightarrow Z'Z'$



$$\sim g_{\chi}^A \frac{m_{\chi}}{M_{Z'}^2} s^{1/2}$$

$$s^{1/2} < \frac{\pi M_{Z'}^2}{(g_{\chi}^A)^2 m_{\chi}} \simeq \begin{cases} 5 \text{ TeV}, & g_{\chi}^A = 0.25, M_{Z'} = 1 \text{ TeV}, m_{\chi} = 10 \text{ GeV} \\ 0.5 \text{ TeV}, & g_{\chi}^A = 0.25, M_{Z'} = 1 \text{ TeV}, m_{\chi} = 100 \text{ GeV} \end{cases}$$

For $m_{\chi} = 10$ (100) GeV, new physics must appear before 5 (0.5) TeV to restore unitarity in DM annihilation to Z' pairs

Dark Higgs sector

Simplest way to restore unitarity is to generate mediator mass by Higgsing $U(1)'$ symmetry. Assuming that DM is Majorana particle (to avoid strong DD constraints due to vector coupling), one can write

$$\mathcal{L}_{\text{DM}} = \frac{i}{2} \bar{\psi} \not{\partial} \psi - \frac{1}{2} g_{\text{DM}}^A Z'^{\mu} \bar{\psi} \gamma_{\mu} \gamma_5 \psi - \frac{1}{2} y_{\text{DM}} \bar{\psi} (P_L S + P_R S^*) \psi$$

$$\mathcal{L}_S = \{(\partial^{\mu} + i g_S Z'^{\mu}) S\}^{\dagger} \{(\partial_{\mu} + i g_S Z'_{\mu}) S\} + \mu_s^2 S^{\dagger} S - \lambda_s (S^{\dagger} S)^2$$

Once S acquires vacuum expectation value (VEV) w , ψ & Z' get massive

$$m_{\text{DM}} = \frac{y_{\text{DM}} w}{\sqrt{2}}, \quad M_{Z'} \simeq 2g_{\text{DM}}^A w$$

Z' interactions

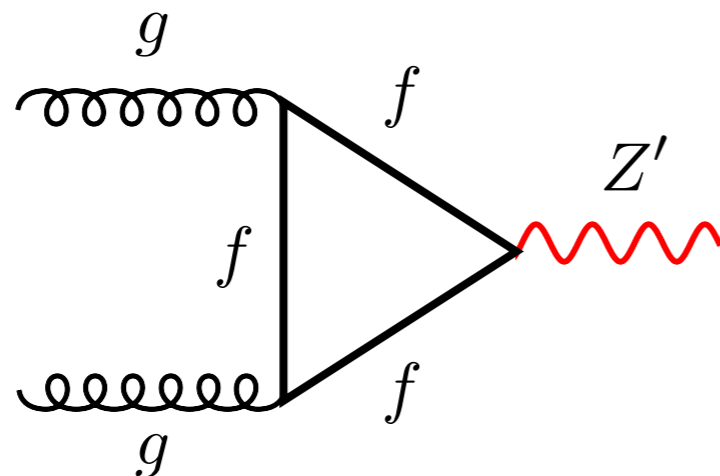
Interactions between SM states & Z' gauge boson can be written as

$$\begin{aligned} \mathcal{L}'_{\text{SM}} = & \left\{ (D^\mu H)^\dagger (-i g' q_H Z'_\mu H) + \text{h.c.} \right\} + g'^2 q_H^2 Z'^\mu Z'_\mu H^\dagger H \\ & - \sum_{f=q,\ell,\nu} g' Z'^\mu \left(\bar{q}_{fL} \bar{f}_L \gamma_\mu f_L + \bar{q}_{fR} \bar{f}_R \gamma_\mu f_R \right) \end{aligned}$$

Gauge invariance of SM Yukawa couplings requires that charges q are generation universal & must satisfy consistency conditions (CCs):

$$q_H = q_{qL} - q_{uR} = q_{dR} - q_{qL} = q_{eR} - q_{\ell L}$$

Implications of CCs



$$\sim 3 (2q_{qL} - q_{uR} - q_{dR})$$

For arbitrary charge assignments consistent with CCs, theory will have anomalies, but new fermions F do not need to be coloured since ggZ' anomaly vanishes automatically. This is a nice feature because masses of new fermions bounded by unitarity:

$$m_F < \sqrt{\frac{\pi}{2}} \frac{M_{Z'}}{g_F^A}$$

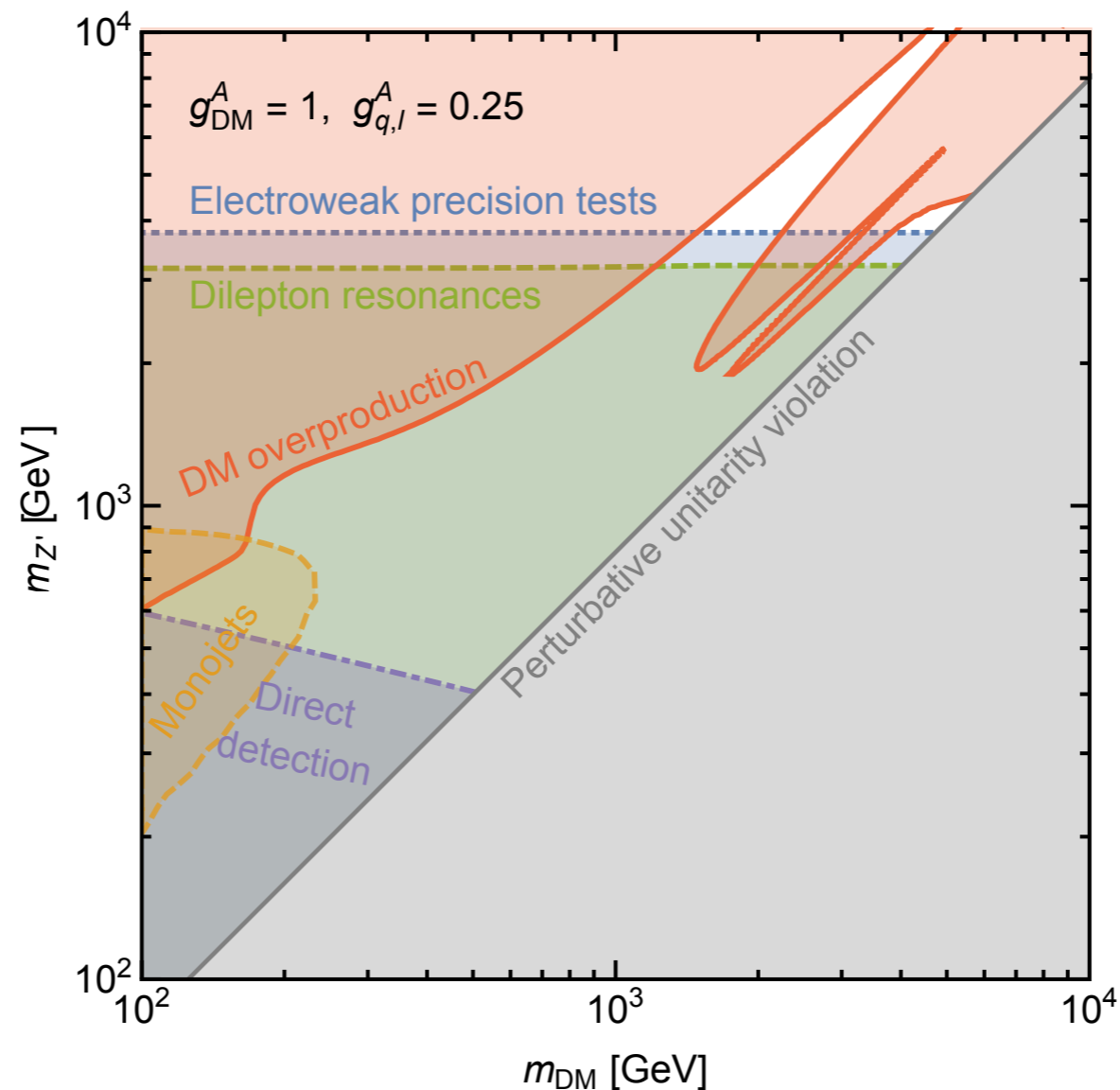
Implications of CCs

CCs also imply that for non-zero axialvector couplings to SM fermions, SM Higgs must carry $U(1)'$ charge. This has two important consequences:

- Z' must couple with same strength to quarks & leptons (assuming one Higgs doublet), resulting in stringent constraints from di-lepton resonance searches
- VEV of SM Higgs leads to $Z-Z'$ mixing, which is severely constrained by EW precision observables (EWPOs)

Axialvector Z' : constraints

[Kahlhoefer et al., 1510.02110]



In simplest UV completion of axialvector model, constraints from mono-jet & di-jet searches & DD not competitive with di-lepton searches & EWPOs

Fermion singlet DM

In fact, by adding

$$\mathcal{L}_s \supset y_\chi \bar{\chi} \chi s + \mu s |H|^2$$

to SM Lagrangian both issues can be addressed

As a result of portal coupling μ , SM Higgs h & singlet s mix, giving rise to mass eigenstates $h_{1,2}$:

$$\begin{pmatrix} h_1 \\ h_2 \end{pmatrix} = \begin{pmatrix} \cos \theta & \sin \theta \\ -\sin \theta & \cos \theta \end{pmatrix} \begin{pmatrix} h \\ s \end{pmatrix}, \quad \tan(2\theta) = \frac{2v\mu}{M_s^2 - M_h^2}$$

For small $\theta \ll 1$, h_1 (h_2) SM Higgs-like (singlet-like)

[Kim et al., 0803.2932; Baek et al., 1112.1847; Lopez-Honorez et al., 1203.2064; Fairbairn & Hogan, 1305.3452; ...]

Fermion singlet DM: vertices

$$\begin{array}{c} q \\ \diagdown \\ \text{---} \{h_1, h_2\} \\ \diagup \\ q \end{array} = \frac{y_q}{\sqrt{2}} \{\cos \theta, -\sin \theta\}$$

$$\begin{array}{c} W, Z \\ \diagdown \\ \text{---} \{h_1, h_2\} \\ \diagup \\ W, Z \end{array} = M_{W,Z} \{\cos \theta, -\sin \theta\}$$

$$\begin{array}{c} \text{---} \{h_1, h_2\} \\ \diagdown \\ \chi \\ \diagup \\ \chi \end{array} = y_\chi \{\sin \theta, \cos \theta\}$$

Fermion singlet DM: signatures

Compared to spin-0 simplified model LHC phenomenology is richer in fermion singlet DM scenario:

- (i) universal suppression of SM Higgs couplings by $\cos\Theta$ — LHC Run I data requires already $\sin\Theta \lesssim 0.4$
- (ii) new SM Higgs decay modes $h_1 \rightarrow \chi\bar{\chi}$ & $h_1 \rightarrow h_2 h_2$ if kinematically allowed
- (iii) $E_{T,\text{miss}}$ cross sections are changed & new signatures like $W/Z + E_{T,\text{miss}}$ & $\text{VBF} + E_{T,\text{miss}}$ arise — $E_{T,\text{miss}}$ processes involving EW bosons cannot be described consistently in spin-0 simplified model

Mono-jet vs. $W/Z, \text{VBF} + E_{T,\text{miss}}$ signal

$$M_{h_2} = 1 \text{ TeV}, m_\chi = 100 \text{ GeV}, \sin\theta = 0.1$$

