



Plasma Wakefield Acceleration and Beam-Plasma Physics

Patric Muggli AWAKE collaboration

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**MAX-PLANCK-INSTITUT
FÜR PHYSIK**

1/30

✧ Advanced WAKefield Experiment

AWAKE collaboration: 22 institutes world-wide

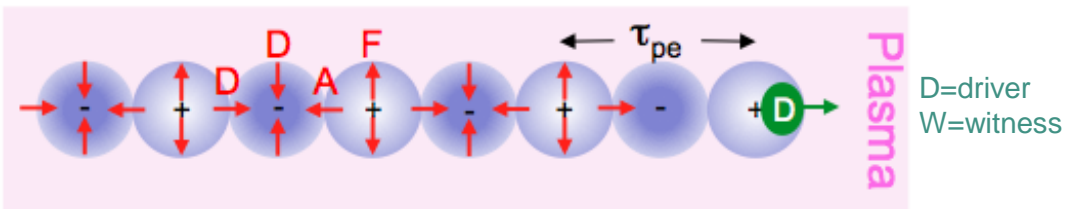
- CERN, Geneva, Switzerland
- University of Manchester, Manchester, UK
- Cockcroft Institute, Daresbury, UK
- Lancaster University, Lancaster, UK
- Oxford University, UK
- Max Planck Institute for Physics, Munich, Germany
- Max Planck Institute for Plasma Physics, Greifswald, Germany
- UCL, London, UK
- UNIST, Ulsan, Republic of Korea
- Philipps-Universität Marburg, Marburg, Germany
- Heinrich-Heine-Universität of Düsseldorf, Düsseldorf, Germany
- University of Liverpool, Liverpool, UK
- ISCTE – Instituto Universitário de Lisboa, Lisbon, Portugal
- Budker Institute of Nuclear Physics SB RAS, Novosibirsk, Russia
- Novosibirsk State University, Novosibirsk, Russia
- GoLP/Instituto de Plasmas e Fusão Nuclear, Instituto Superior Técnico, Universidade de Lisboa, Lisbon, Portugal
- TRIUMF, Vancouver, Canada
- Ludwig-Maximilians-Universität, Munich, Germany
- University of Wisconsin, Madison, US
- Uppsala University, Uppsala, Sweden
- Wigner Institute, Budapest, Hungary
- Swiss Plasma Center group of EPFL, Lausanne, Switzerland

Vancouver
Madison



Experiment @





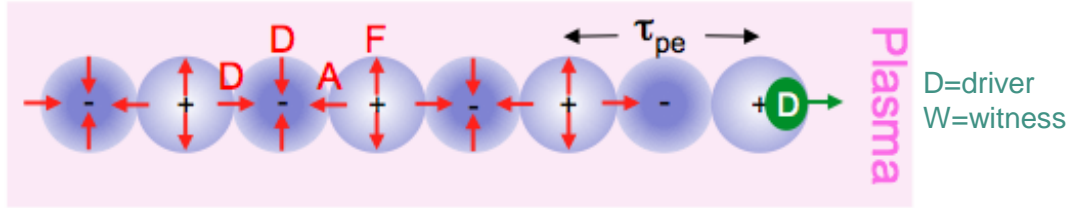
⇔ Relativistic Bunch ⇔ Radial Space Charge Field ⇔ Plasma Screening

⇔ Azimuthal Magnetic Field ⇔ Plasma Return Current

⇔ High Frequency Regime ⇔ Time $\sim 1/\omega_{pe}$ ⇔ Space $\sim c/\omega_{pe} = 1/k_{pe}$, $\lambda_{pe} = 2\pi/k_{pe}$, $v_b \sim c$, $\gamma \gg 1$, (ω_{pi})

$$\omega_{pe} = \left(\frac{n_{e0} e^2}{\epsilon_0 m_e} \right)^{1/2} \gg \omega_{pi}$$

RELATIVISTIC PARTICLE BUNCH MEETS PLASMA



⇧ Relativistic Bunch ⇧ Radial Space Charge Field ⇧ Plasma Screening

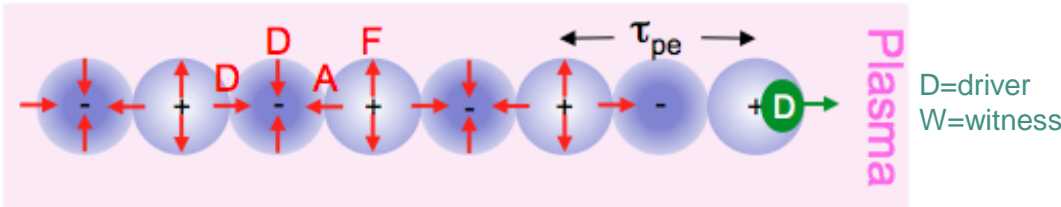
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⇧ Screening ⇧ Plasma Wakefields (Langmuir Wave, E_z) ⇧ Self-Modulation and Hosing Instabilities ⇧ Accelerators

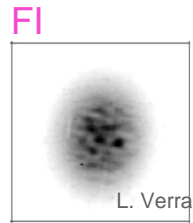
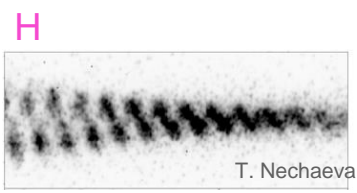
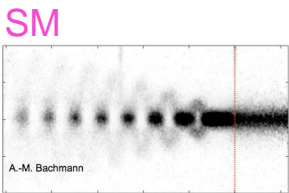
⇧ Return Current ⇧ Filamentation Instability (\sim Weibel Instability), Generation of Magnetic Fields ⇧ Astrophysics



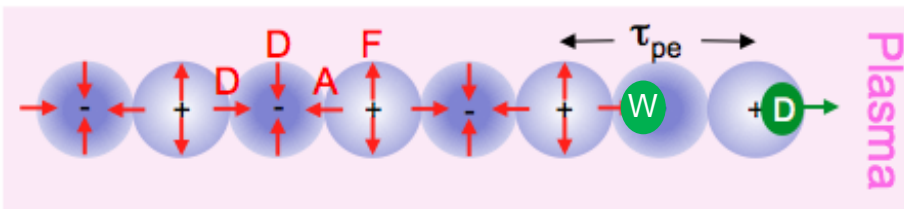
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RELATIVISTIC PARTICLE BUNCH MEETS PLASMA



D=driver
W=witness

⇨ Relativistic Bunch ⇨ Radial Space Charge Field ⇨ Plasma Screening

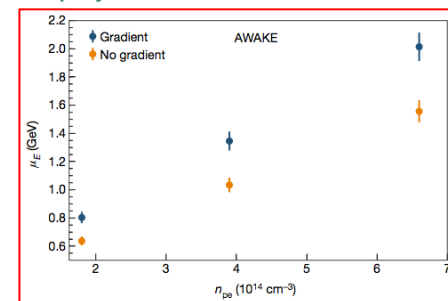
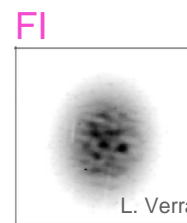
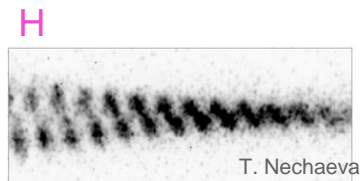
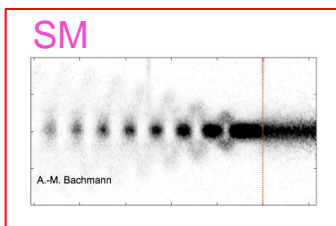
⇨ Azimuthal Magnetic Field ⇨ Plasma Return Current

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⇨ Screening ⇨ Plasma Wakefields (Langmuir Wave, E_z) ⇨ Self-Modulation and Hosing Instabilities ⇨ Accelerators

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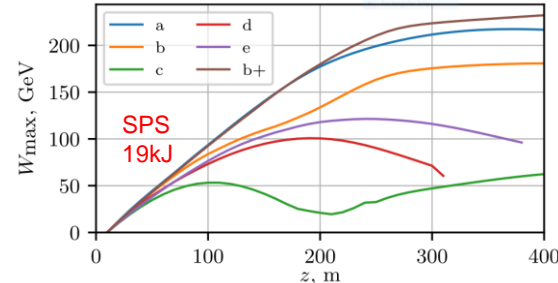
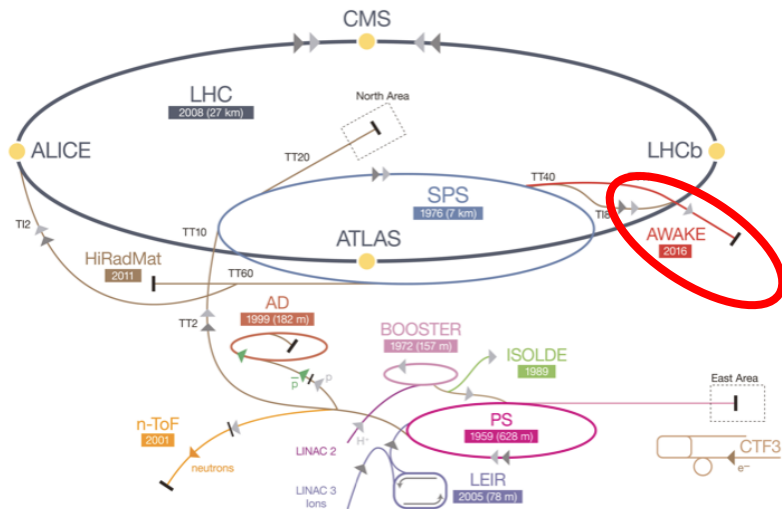


Main motivation:

⇨ Produce high-energy e^- bunches (200GeV, 5TeV), in a high-gradient (1GeV/m) plasma-based accelerator (PWFA) driven by a p^+ bunch, for particle physics applications (dark photon searches, very-high-energy ep collider)

- ✧ Drive wakefields in plasma with a proton (p^+) bunch
- ✧ Accelerate externally-injected electrons (e^-) to GeV (SPS) to TeV (LHC) energy scale
- ✧ Relativistic proton (p^+) bunches with tens to hundreds of kJ are available

- ✧ Driving wakefields in plasma with a proton (p^+) bunch
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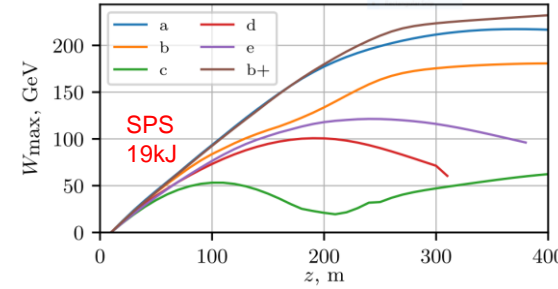
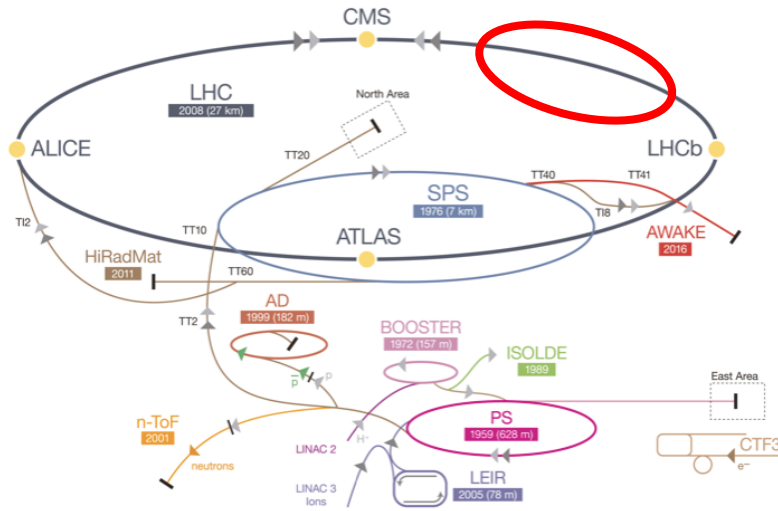
SPS driver (19kJ):
~200GeV in ~200m
~ $10^9 e^-$

P. Tuev, K. V. Lotov, PPFC 63, 125027 (2021)

2D numerical simulation results



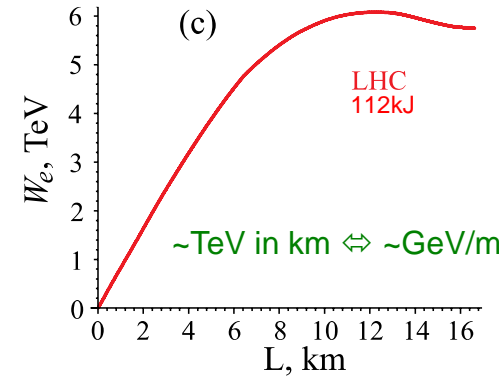
- ✧ Driving wakefields in plasma with a proton (p^+) bunch
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P. Tuev, K. V. Lotov, PPFC 63, 125027 (2021)

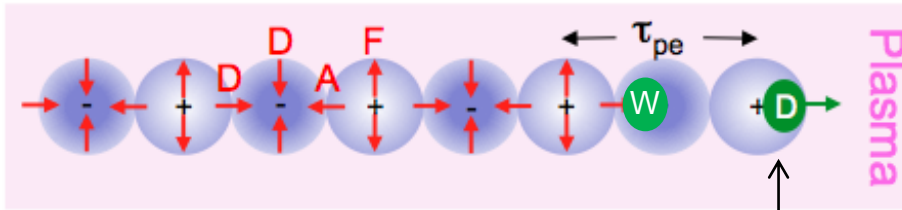
2D numerical simulation results



LHC driver (119kJ):
~5TeV in ~7km
~ $10^9 e^-$

1GeV/m!

Short driver (e⁻), $\sigma_t \leq 1/\omega_{pe}$, $\sigma_r \sim c/\omega_{pe}$, “resonant”



~Langmuir wave in 1D, on axis

Scaling:

$$\sigma_t, \tau \leq 1/\omega_{pe} \propto n_{e0}^{-1/2}$$

$$\sigma_r \leq c/\omega_{pe} \propto n_{e0}^{-1/2}$$

$$E_{WB} = \frac{m_e c}{e} \omega_{pe} \propto n_{e0}^{1/2}$$

$$\omega_{pe} = \left(\frac{n_{e0} e^2}{\epsilon_0 m_e} \right)^{1/2}$$

$$c/\omega_{pe}$$

Plasma e⁻ angular frequency

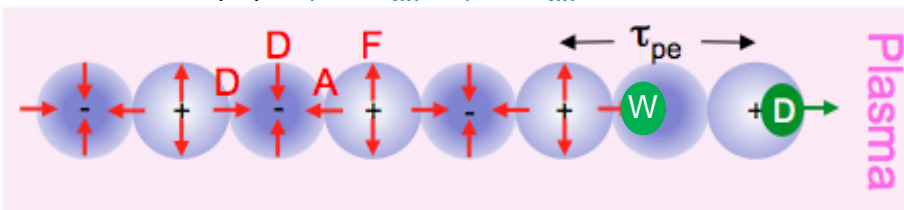
Plasma skin depth

fit within the “structure”, “bubble”

Short and Narrow

$$\underbrace{k_{pe} \sigma_z = \sqrt{2} \quad k_{pe} \sigma_r \sim 1}_{n_{e0}, k_{pe}, c/\omega_{pe}}$$

Short driver (e^-), $\sigma_t \leq 1/\omega_{pe}$, $\sigma_r \sim c/\omega_{pe}$, “resonant”



Short and Narrow

$$k_{pe} \sigma_z = \sqrt{2}$$

$$k_{pe} \sigma_r \sim 1$$

~Langmuir wave in 1D, on axis

PWFA, short e^- bunch

Scaling:

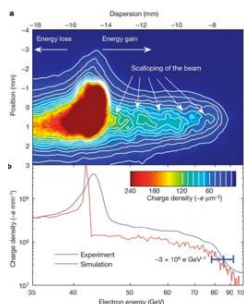
$$\sigma_t, \tau \leq 1/\omega_{pe} \propto n_{e0}^{-1/2}$$

$$\sigma_r \leq c/\omega_{pe} \propto n_{e0}^{-1/2}$$

$$E_{WFB} = \frac{m_e c}{e} \omega_{pe} \propto n_{e0}^{1/2}$$

$$\omega_{pe} = \left(\frac{n_{e0} e^2}{\epsilon_0 m_e} \right)^{1/2}$$

$$c/\omega_{pe}$$



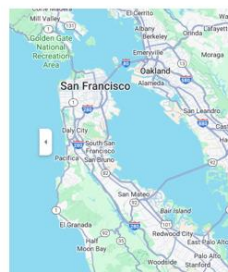
Blumenfeld, Nature 445, 741 (2007)

$n_{e0} = 2.7 \times 10^{17} \text{cm}^{-3}$
60fs e^- bunch
2x10¹⁰ e^- , 42GeV, ~50J
~42GeV energy gain
~52GeV/m, 85cm

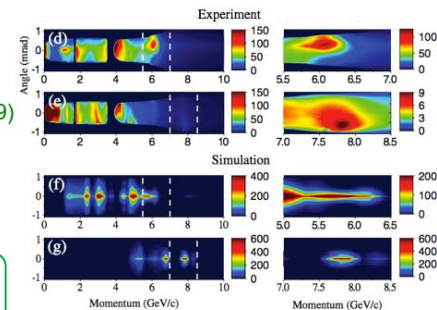


Gonsalves, PRL 122, 084801 (2019)

$n_{e0} = 3 \times 10^{17} \text{cm}^{-3}$
~40fs laser pulse
~40J, 1PW
~8GeV energy gain
~39GeV/m, 20cm



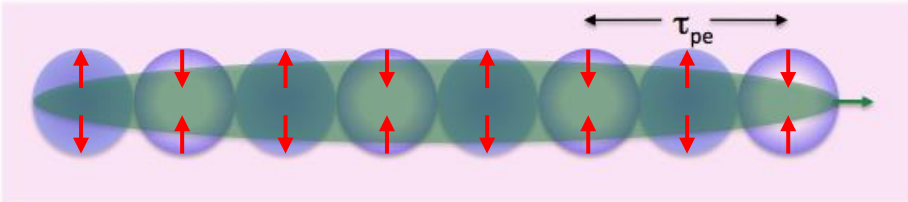
LWFA, short laser pulse



High energy gain & gradient!!

Long driver (p⁺), $\sigma_t \gg 1/\omega_{pe}$, $\sigma_r \sim c/\omega_{pe}$, initially non-resonant

N. Kumar et al., Phys. Rev. Lett. 104, 255003 (2010)



Short and Narrow → Long and Narrow

$$k_{pe} \sigma_z = \sqrt{2}$$

$$k_{pe} \sigma_r \sim 1$$

$$k_{pe} \sigma_z \gg 1$$

$$k_{pe} \sigma_r \sim 1$$



$$n_{e0}, k_{pe}, c/\omega_{pe}$$

Blumenfeld, Nature 445, 741 (2007)

Gonsalves, PRL 122, 084801 (2019)

$$n_{e0} = 2.7 \times 10^{17} \text{cm}^{-3}$$

60fs e⁻ bunch

$$2 \times 10^{10} \text{e}^-, 42 \text{GeV} \sim 50 \text{J}$$

~42GeV energy gain

~52GeV/m, 85cm



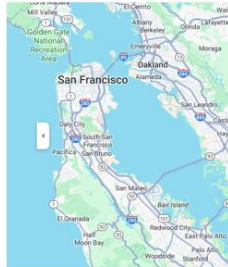
$$n_{e0} = 3 \times 10^{17} \text{cm}^{-3}$$

~40fs laser pulse

$$\sim 40 \text{J}, 1 \text{PW}$$

~8GeV energy gain

~39GeV/m, 20cm



p⁺ bunch, CERN:

SPS: 400GeV, $3 \times 10^{11} \rightarrow 19 \text{kJ}$

LHC: 7TeV, $1 \times 10^{11} \rightarrow 119 \text{kJ}$

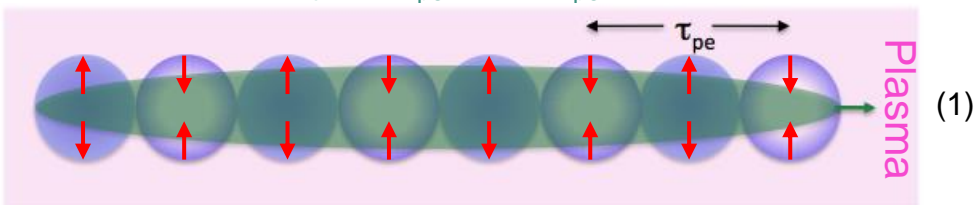
~200ps

$$E_{WB} = \frac{m_e c \sqrt{2}}{e \sigma_r} \propto n_{e0}^{1/2}$$

10-100J → 10-100kJ!

SELF-MODULATION

Long driver (p⁺), $\sigma_t \gg 1/\omega_{pe}$, $\sigma_r \sim c/\omega_{pe}$, initially non-resonant



$$\omega_{pe} = \left(\frac{n_{e0} e^2}{\epsilon_0 m_e} \right)^{1/2}$$

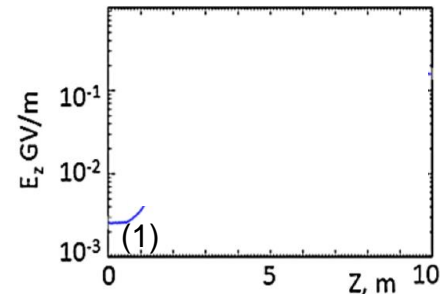
Plasma e⁻ angular frequency

Initial (transverse) wakefields



Periodic focusing/defocusing (1)

Pukhov, PRL107 145003 (2011)

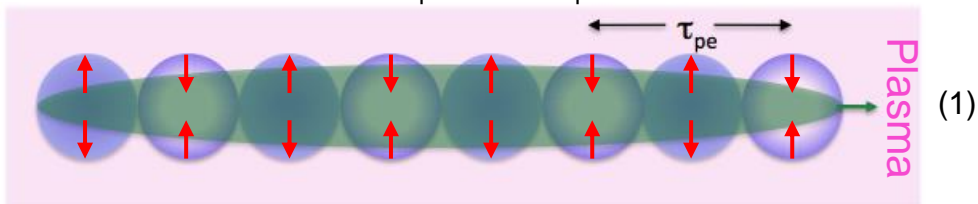


✧ E_z-field along the plasma

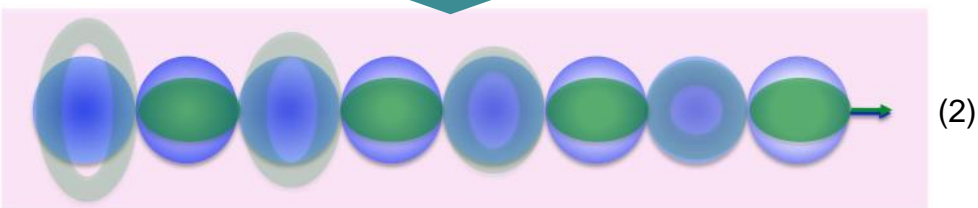
Relativistic particles do not (appreciably) dephase!
SM ⇔ transverse effect!

SELF-MODULATION

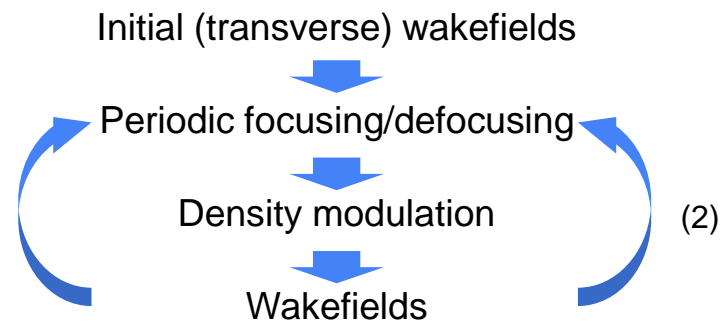
Long driver (p⁺), $\sigma_t \gg 1/\omega_{pe}$, $\sigma_r \sim c/\omega_{pe}$, initially non-resonant



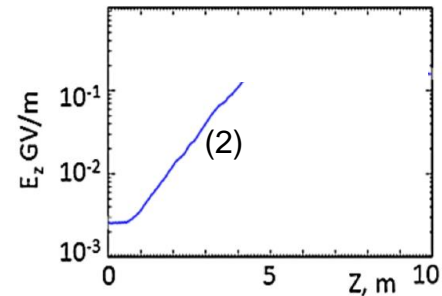
Self-modulation



Growth mechanism:



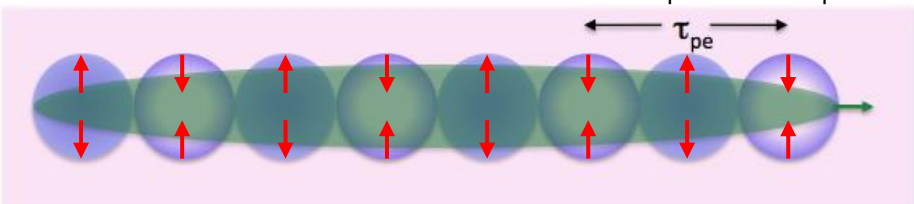
Pukhov, PRL107 145003 (2011)



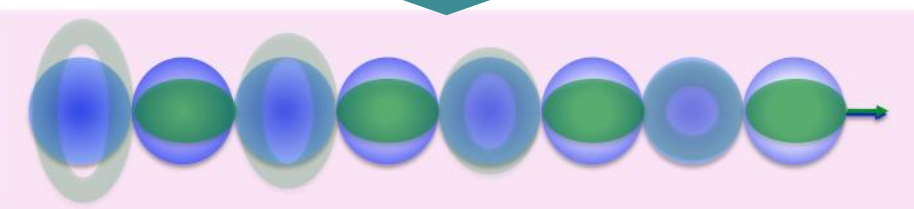
Growth along the bunch and plasma!

SELF-MODULATION

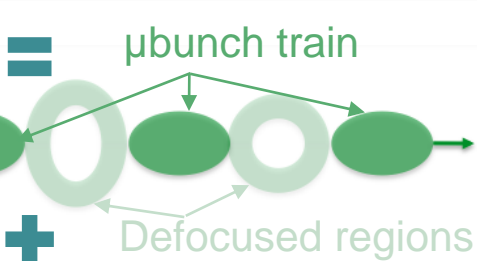
Long driver (p^+), dense plasma, $\sigma_t \gg 1/\omega_{pe}$, $\sigma_t \sim c/\omega_{pe}$



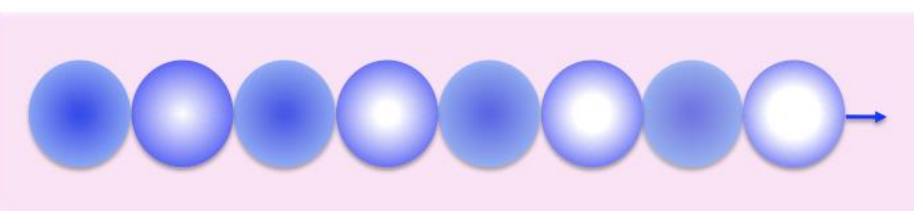
Self-modulation



Self-modulated bunch



Plasma wakefields



Growth mechanism:

Initial (transverse) wakefields

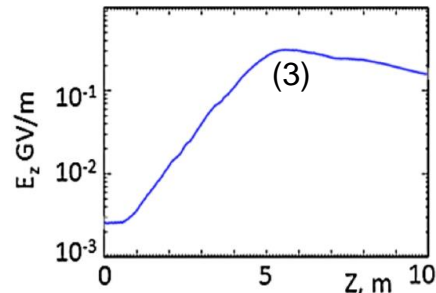
Periodic focusing/defocusing

Density modulation

Wakefields

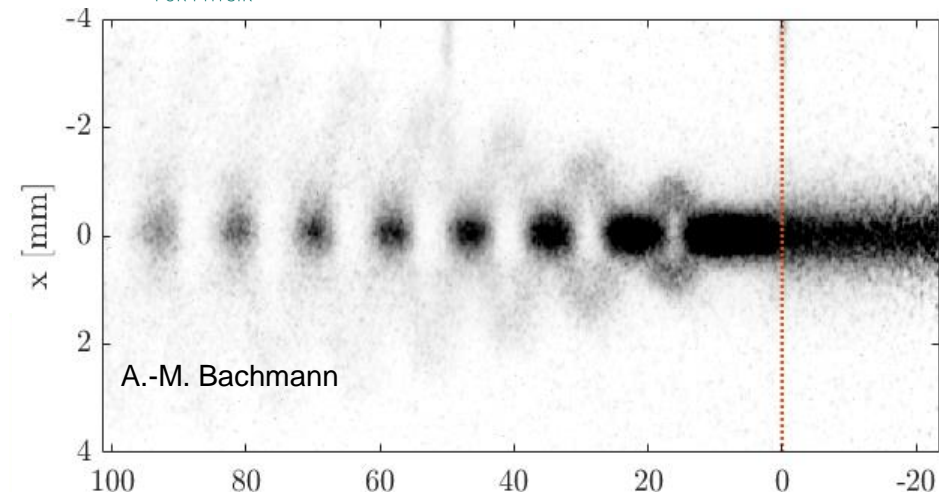
Full modulation - bunch train (3)

Pukhov, PRL107 145003 (2011)

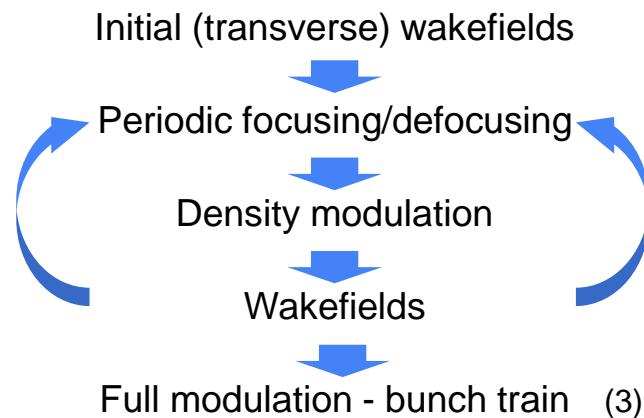


- (3) \diamond Train period $\sim \tau_{pe} = 2\pi/\omega_{pe}$
- \diamond μ bunch length $< \tau_{pe}$
- \diamond Resonantly drives wakefields to large amplitude
- \diamond Self-modulation necessary to drive \sim GV/m accelerating fields in $\sim 10^{14}$ cm $^{-3}$ density plasma

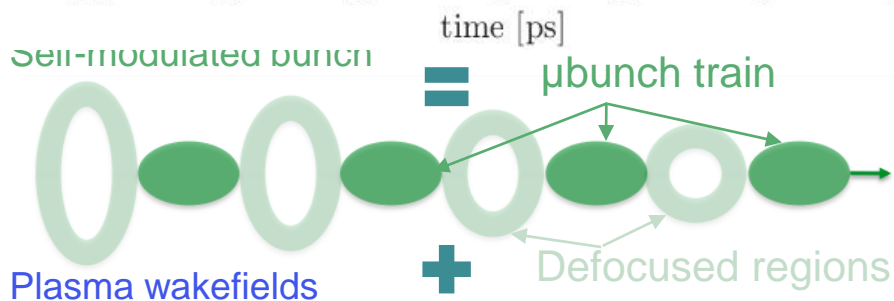
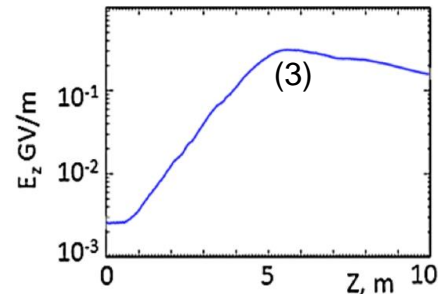
SELF-MODULATION



Growth mechanism:

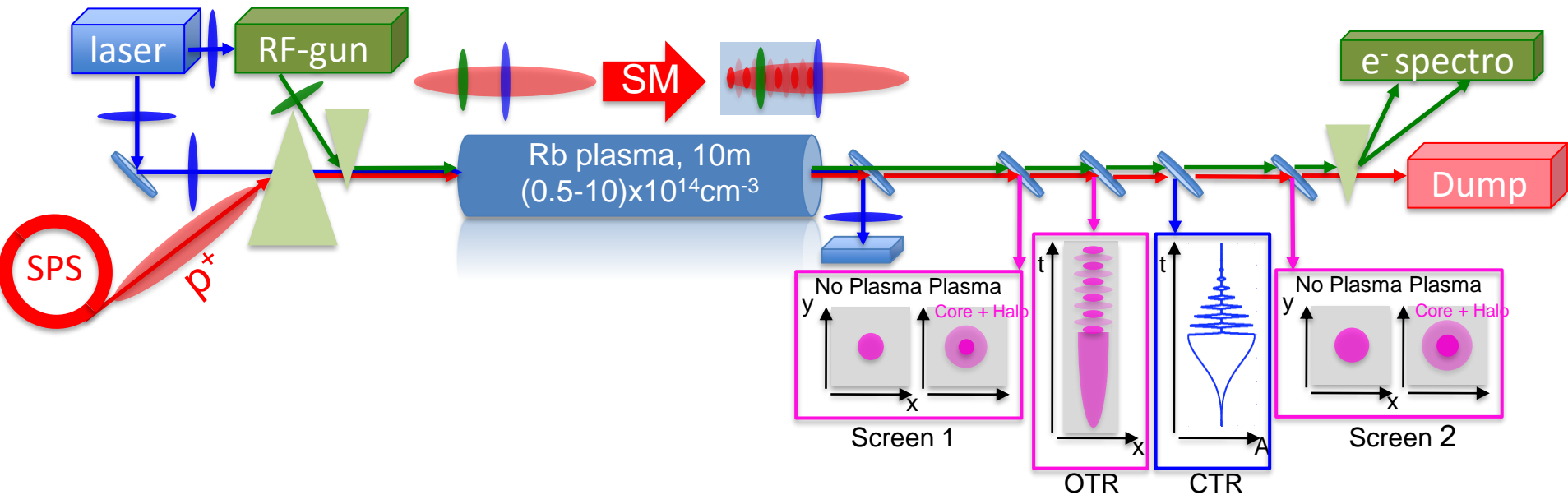


Pukhov, PRL107 145003 (2011)



- (3) ✧ Train period $\sim \tau_{pe} = 2\pi/\omega_{pe}$
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- ✧ Resonantly drives wakefields to large amplitude
- ✧ Self-modulation necessary to drive \sim GV/m accelerating fields in $\sim 10^{14}$ cm $^{-3}$ density plasma

AWAKE EXPERIMENTAL SETUP



$E=400\text{GeV}$
 $\sigma_z=6\text{cm}!!$

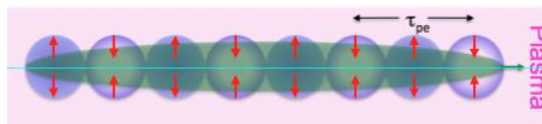
Long

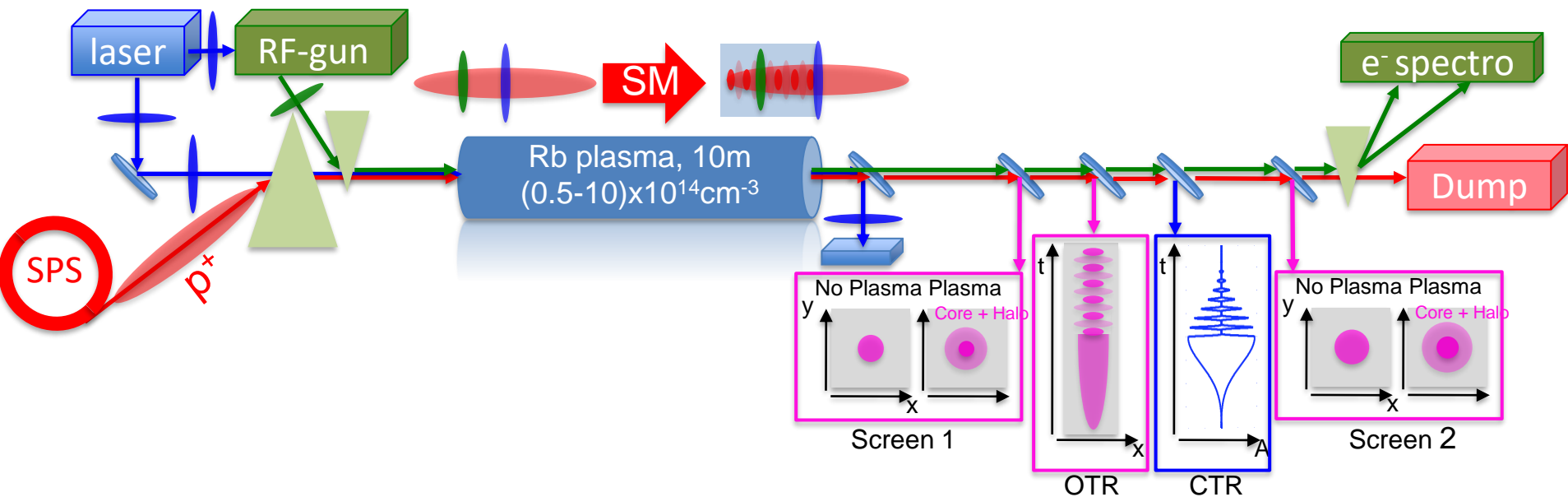
$N=(1-3) \times 10^{11} p^+$
 $\sigma_r=200\mu\text{m}$

Narrow

✧ Plasma density from σ_r

SM regime ...



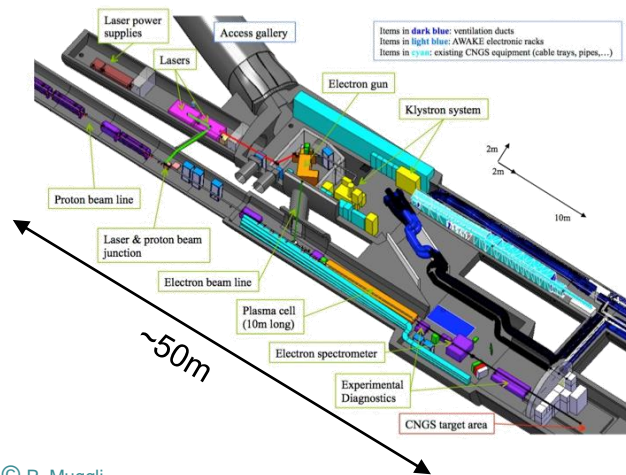
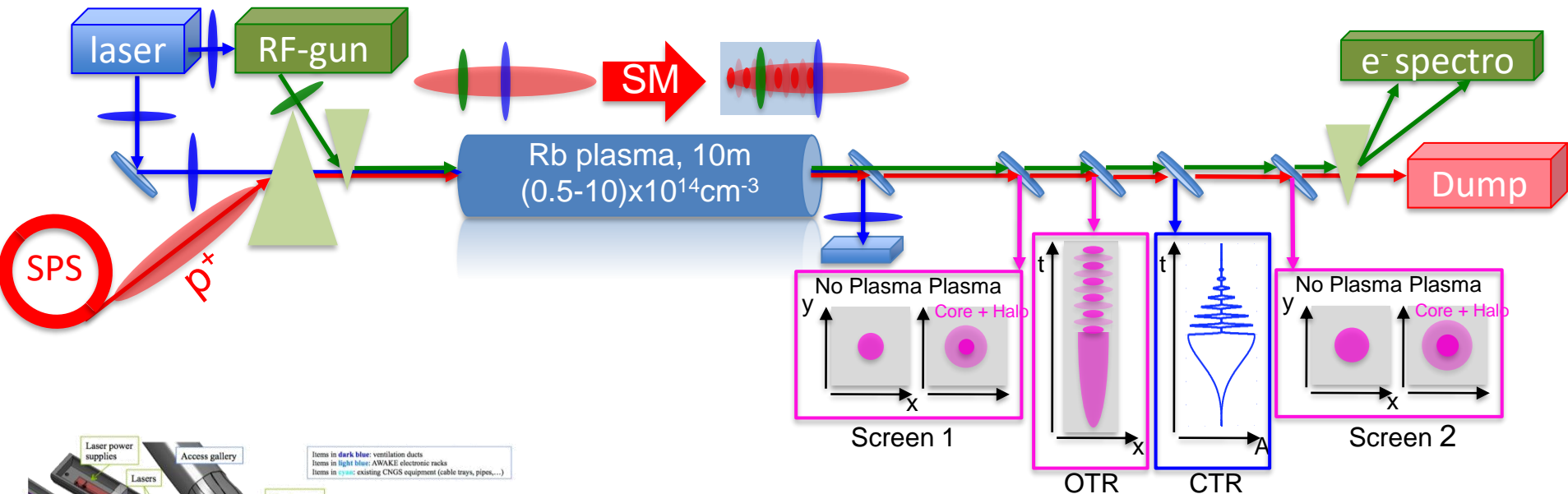


$E=400\text{GeV}$
 $\sigma_z=6\text{cm}!!$
 $c/\omega_{pe} \approx \sigma_r \Leftrightarrow$

$N=(1-3) \times 10^{11} p^+$
 $\sigma_r=200\mu\text{m}$
 $n_e \sim 7 \times 10^{14} \text{cm}^{-3}$
 $\lambda_{pe} \sim 1.3\text{mm} \ll \sigma_z$
 $f_{pe} \sim 240\text{GHz}$
 $E_{WB} \sim 2.5\text{GV/m}$
 $L_p \sim 10\text{m} \sim 2\beta^*$

✧ Plasma density from σ_r

➡ SM ~ 1GeV/m



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$$\sigma_z=6\text{cm!!}$$

$$c/\omega_{pe} \approx \sigma_r \Leftrightarrow$$

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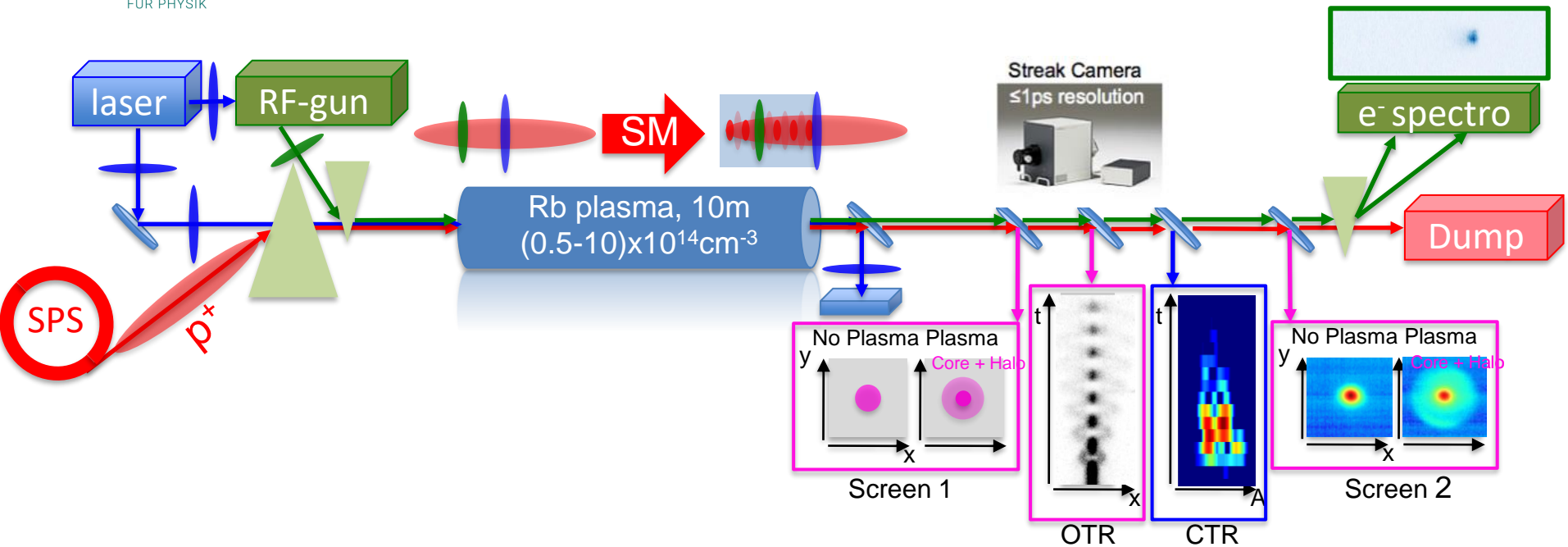
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$$L_p \sim 10\text{m} \sim 2\beta^*$$

✧ Plasma density from σ_r

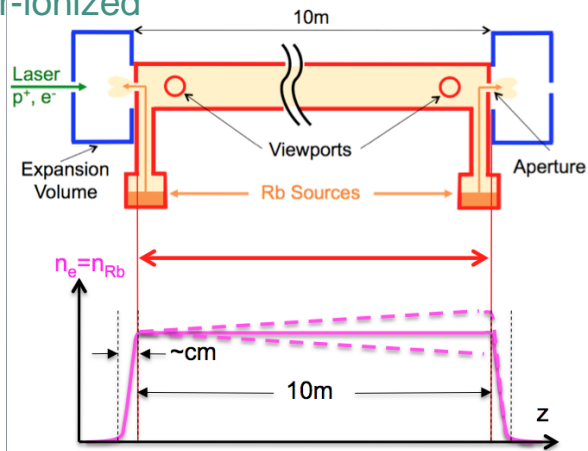
➡ SM ~ 1GeV/m

AWAKE EXPERIMENTAL SETUP



✧ Rubidium vapor source $0.5 < n_{e0} < 10 \cdot 10^{14} \text{cm}^{-3}$

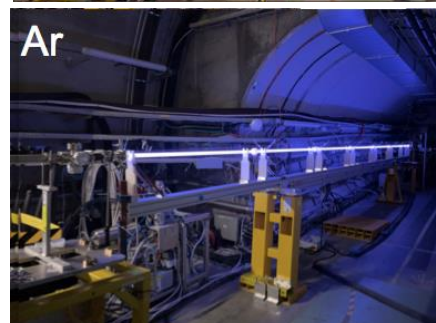
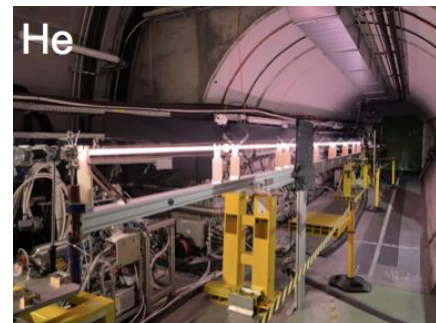
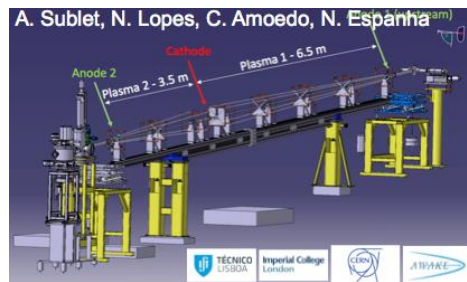
✧ Laser-ionized



Oz, Nucl. Instr. Meth. Phys. Res. A 740(11), 197 (2014)
Plyushchev, J. Phys. D: Applied Physics, 51(2), 025203 (2017)



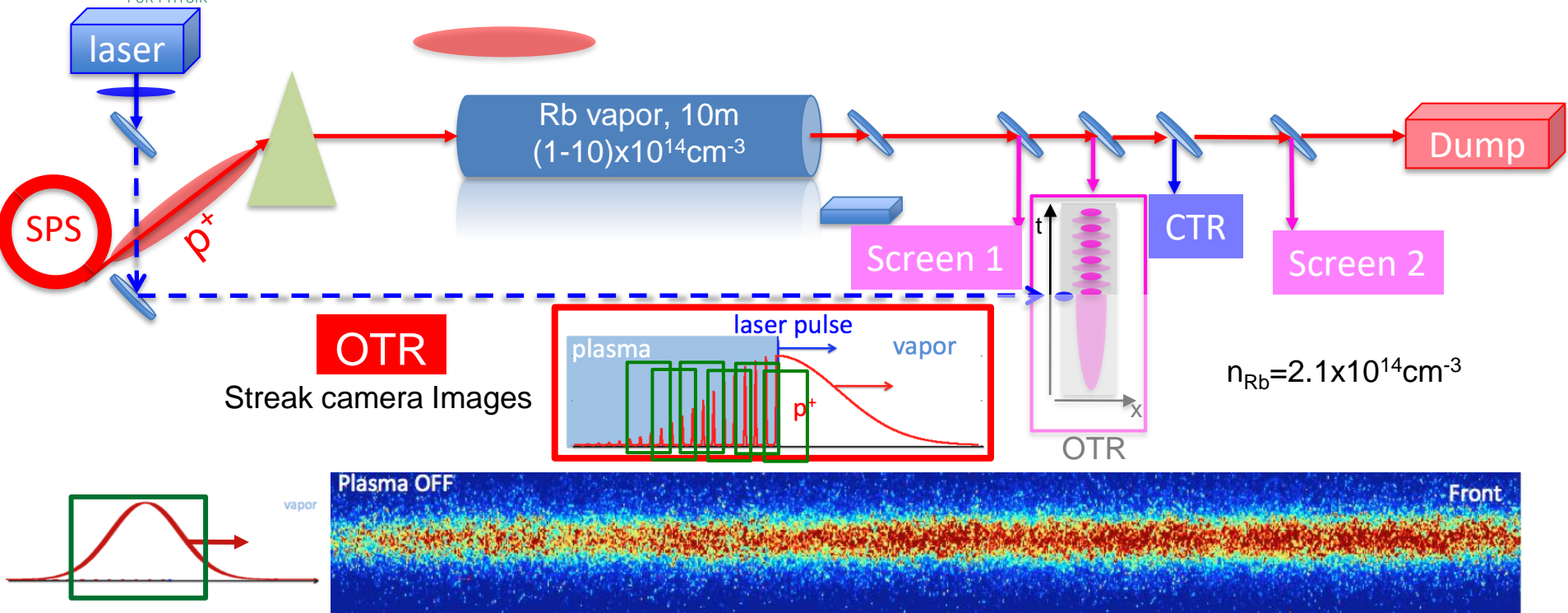
✧ Discharge plasma source



✧ Flexibility:

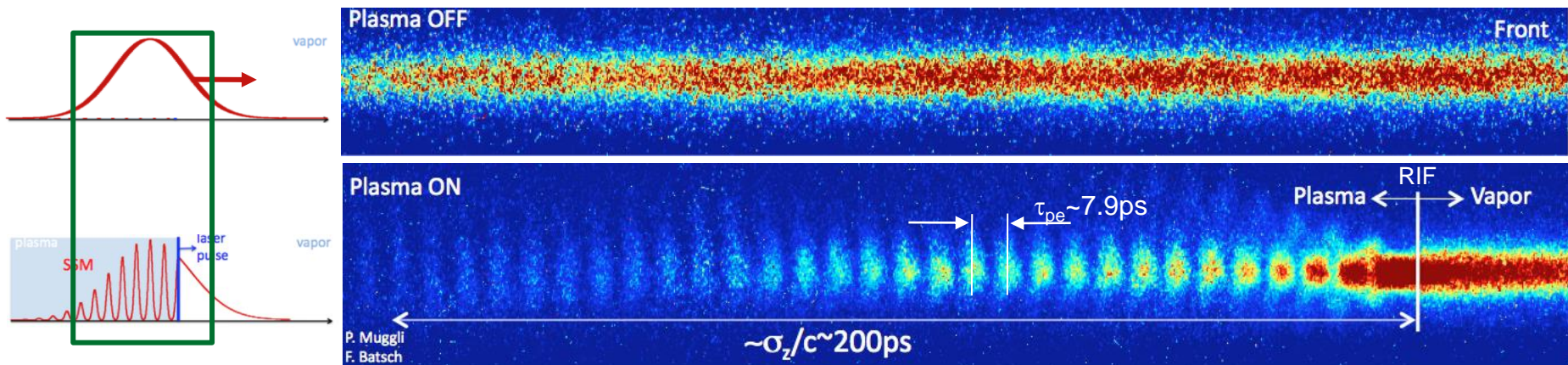
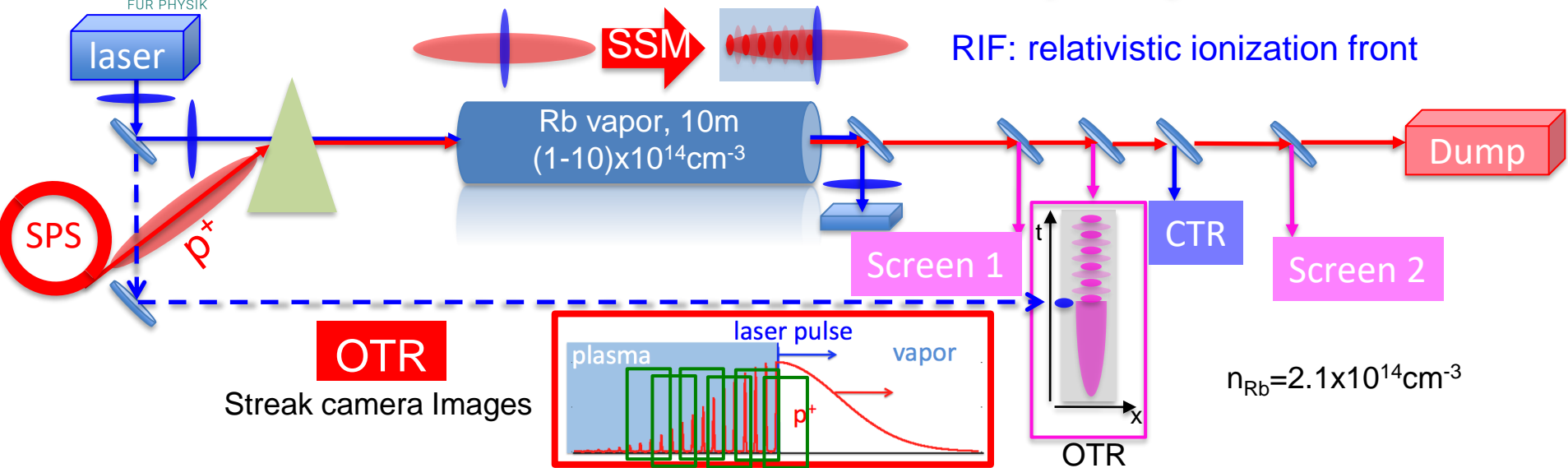
- ✧ Plasma length: 3.5, 6.5, 10m
- ✧ Density $0.1 - 20 \cdot 10^{14} \text{cm}^{-3}$
- ✧ Gas-ion mass: He, Ar, Xe (ω_{pi})
- ✧ Access to plasma light

SEEDED SELF-MODULATION (SSM)

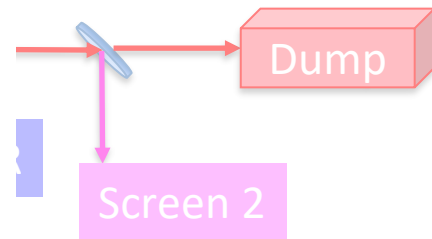
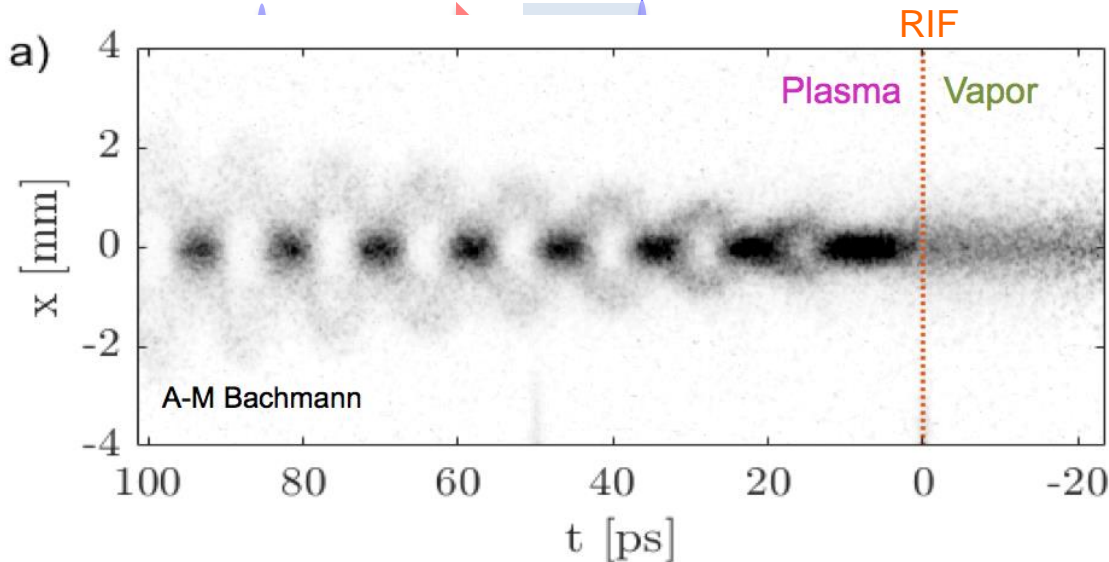
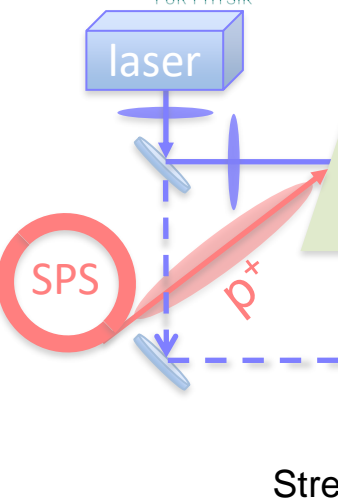


- ✧ No plasma
- ✧ No density modulation
- ✧ No centroid position oscillation

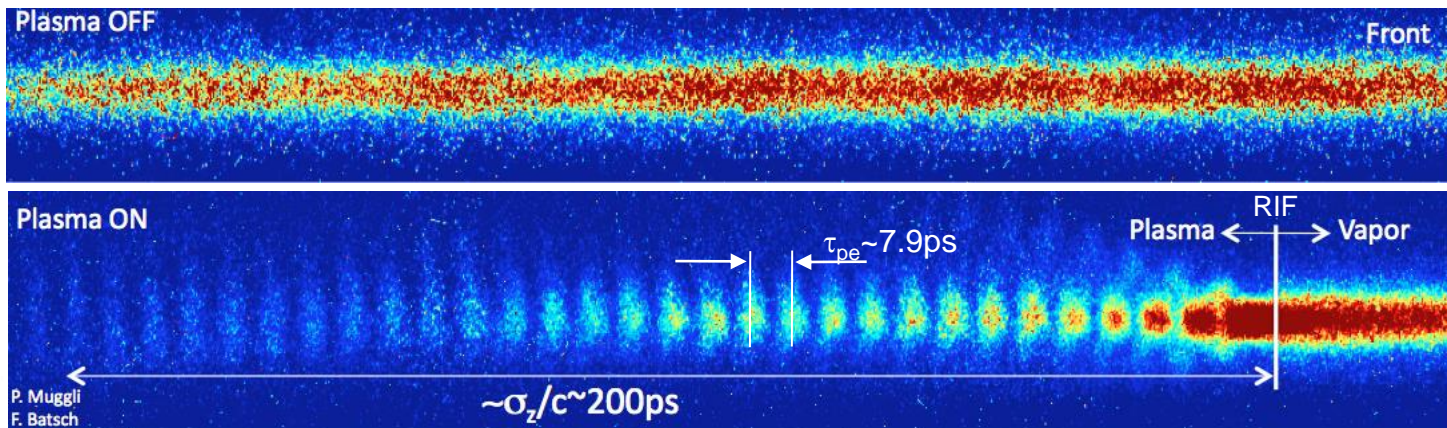
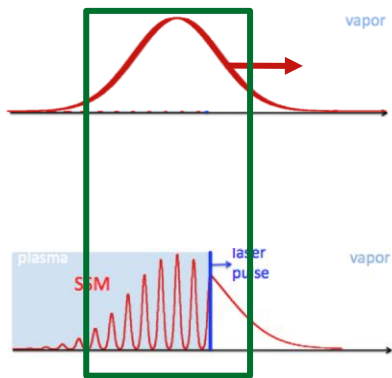
SEEDED SELF-MODULATION (SSM)



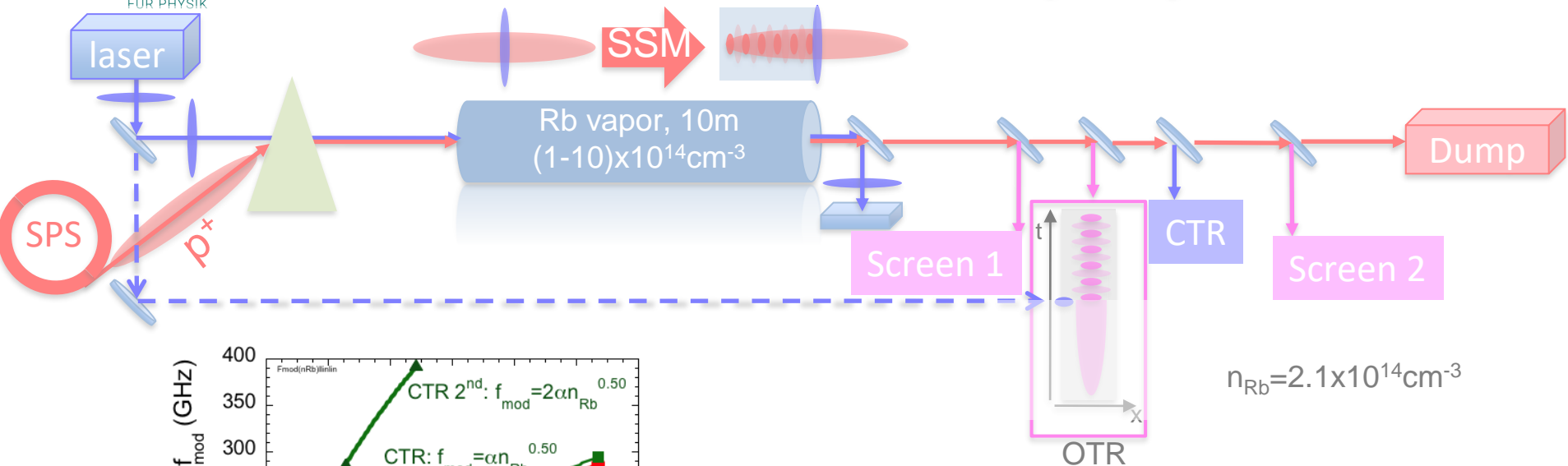
SEEDED SELF-MODULATION (SSM)



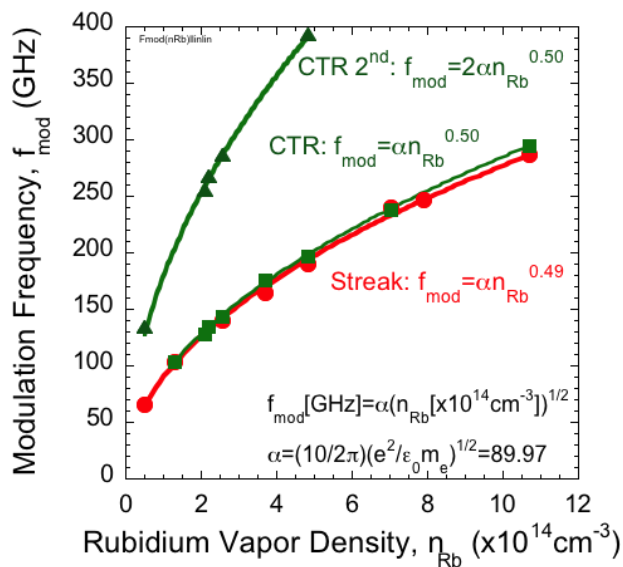
$$n_{Rb} = 2.1 \times 10^{14} \text{ cm}^{-3}$$



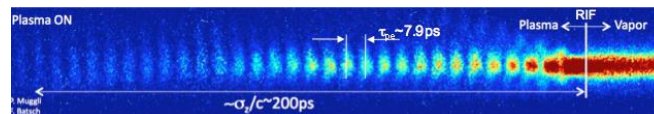
SEEDED SELF-MODULATION (SSM)



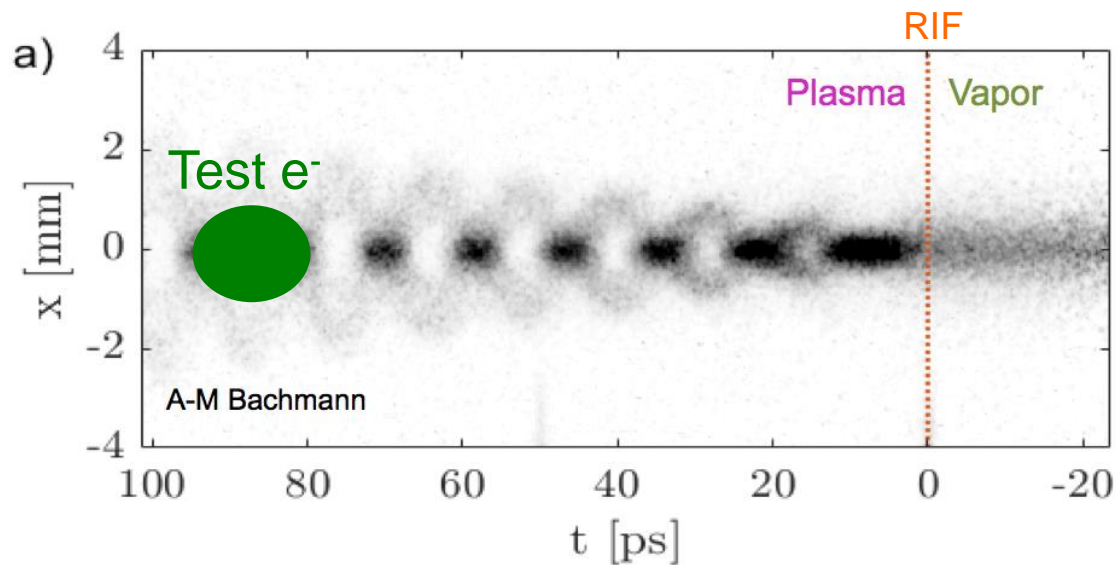
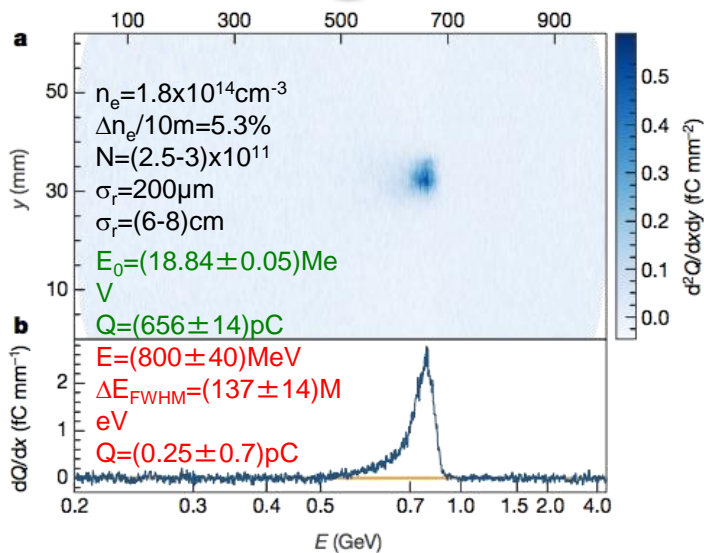
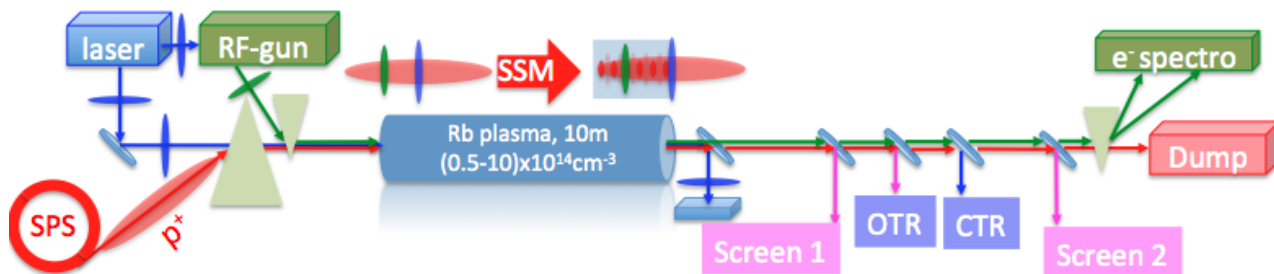
$n_{Rb} = 2.1 \times 10^{14} \text{cm}^{-3}$



✧ Modulation frequency = f_{pe}

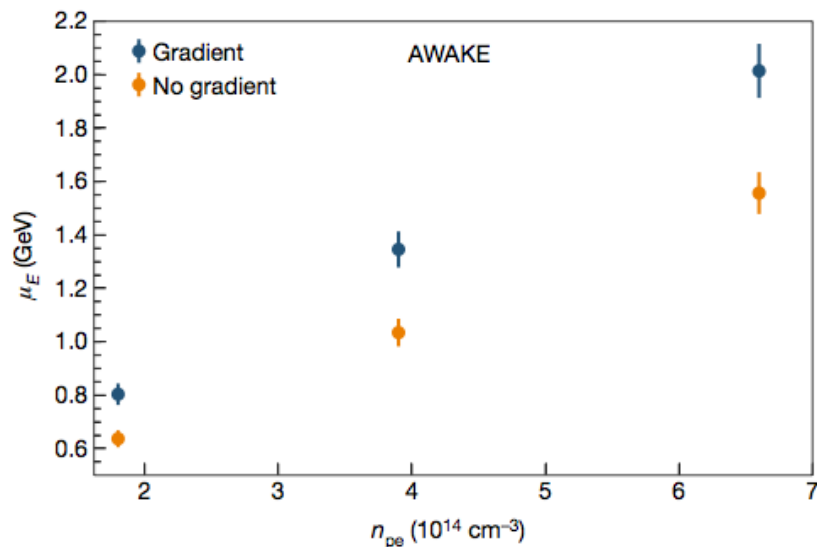
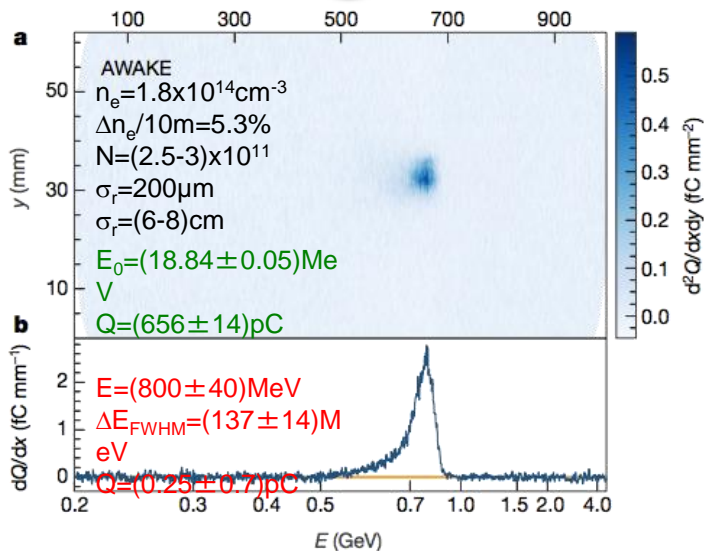
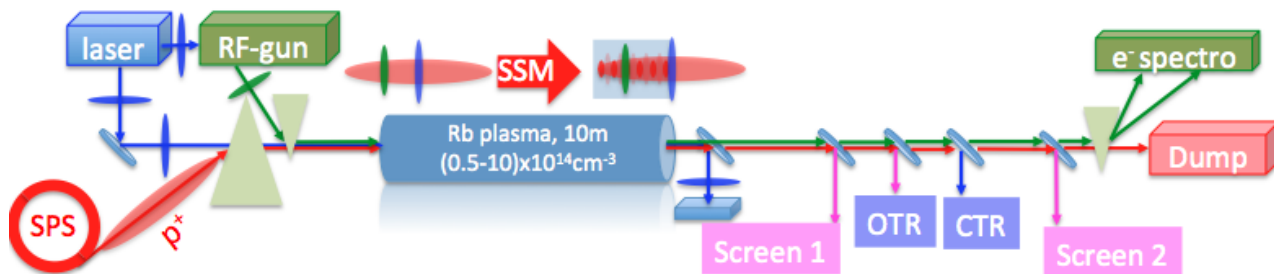


ACCELERATION EXTERNALLY-INJECTED e^-

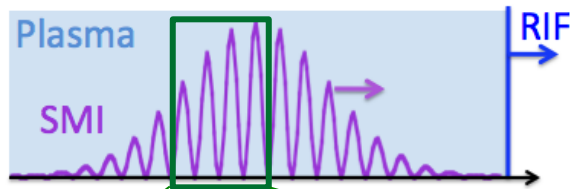


- ✧ Injection test e^- at an angle ($\sim 1-3 \text{mrad}$)
- ✧ Finite $\Delta E/E$

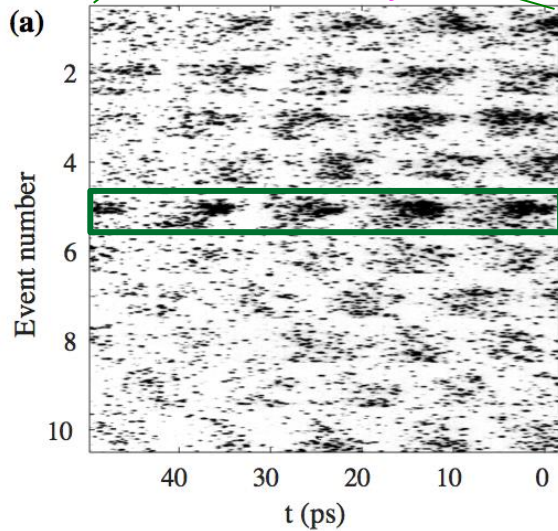
ACCELERATION EXTERNALLY-INJECTED e^-



- ✧ Injection test e^- at an angle ($\sim 1-3 \text{mrad}$)
- ✧ Finite $\Delta E/E$
- ✧ Up to 2 GeV energy gain (from $\sim 19 \text{MeV}$)
- ✧ Captured charge: $\sim \text{pC}$



SMI - Instability

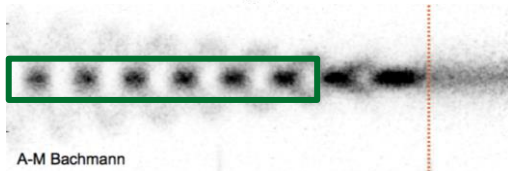


μ -bunches
@ varying times

10 events

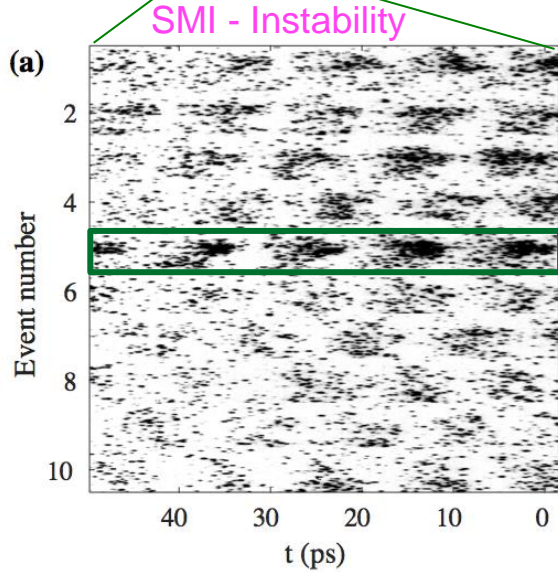
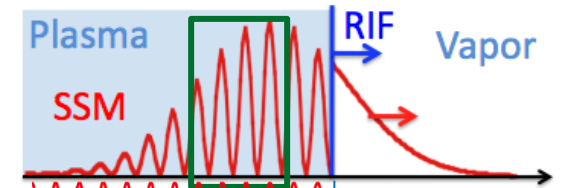
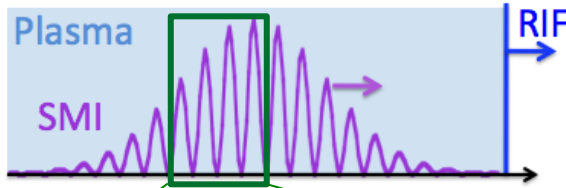
$$n_{e0} = 10^{14} \text{cm}^{-3}$$

$$N_{p+} = 3 \times 10^{11}$$



A-M Bachmann

SEEDED SELF-MODULATION (SSM)

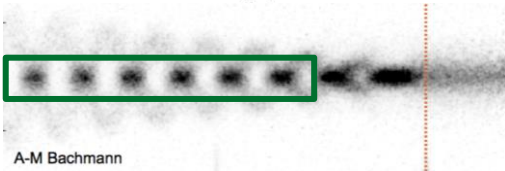


μ -bunches
@ varying times

10 events

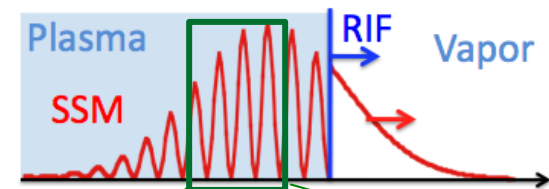
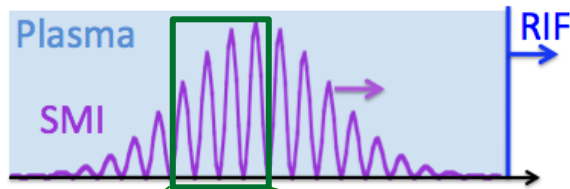
Wakefields
start
here!

- ◇ Relativistic ionization front (RIF)
- ◇ Abrupt ($\ll 1/\omega_{pe}$) start beam/plasma interaction
- ◇ Seed wakefields



A-M Bachmann

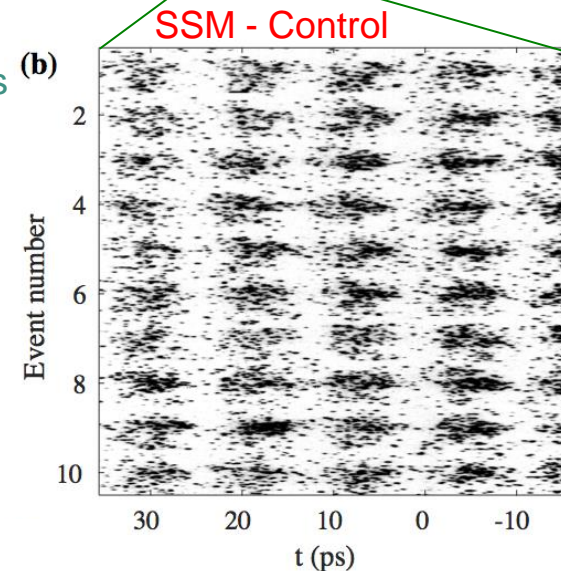
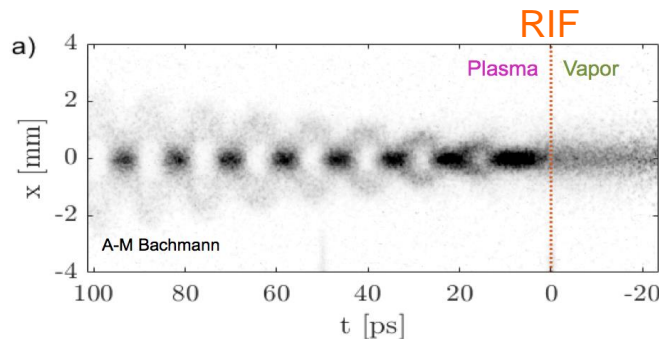
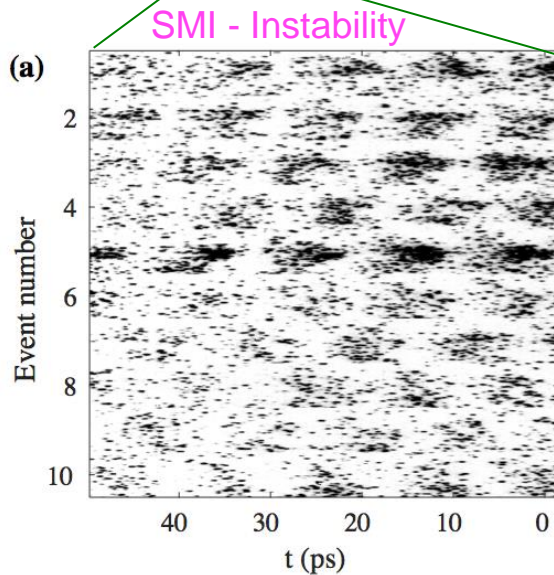
SEEDED SELF-MODULATION (SSM)



Relativistic Ionization Front
(RIF)
Seeding

μ -bunches @ varying times \rightarrow μ -bunches @ fixed times

REPRODUCIBLE!



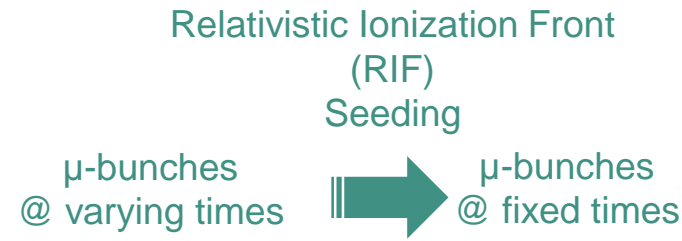
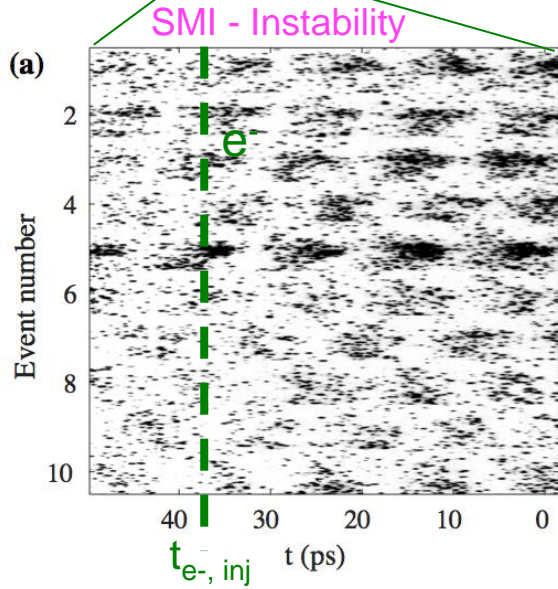
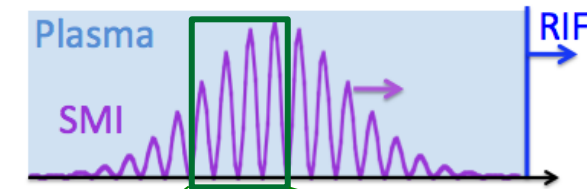
- Transition from SMI to SSM
- SSM, RIF seeding: $\Delta\Phi/2\pi \leq 8\%$
- SMI – SSM transition:

$$t_{\text{RIF}} \sim 2\sigma_{p^+}$$

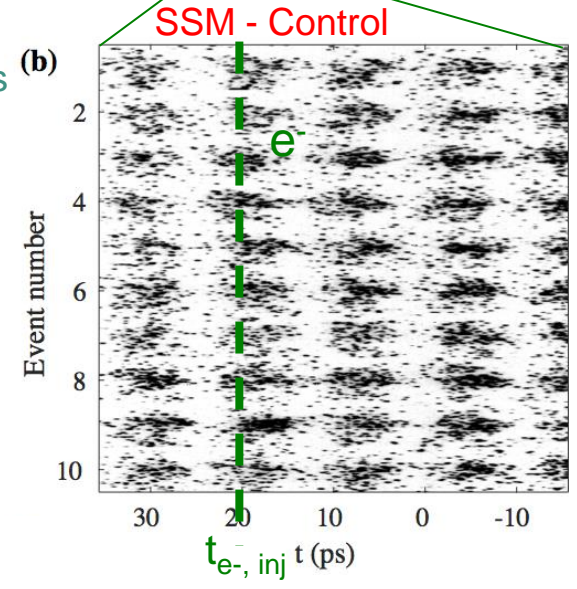
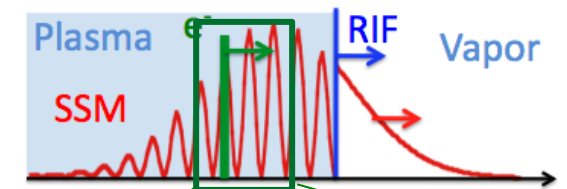
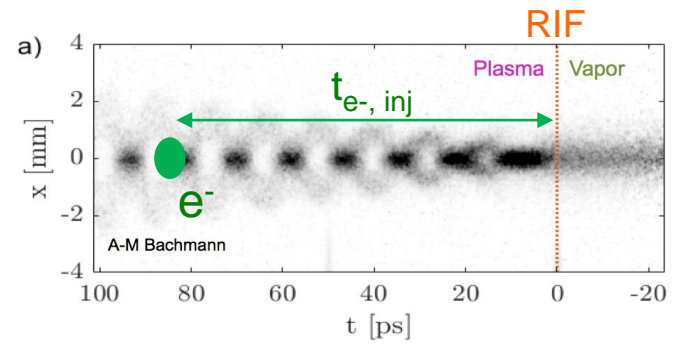
$$2.8\text{MV/m} \leq E_{z,\text{seed}} \leq 4\text{MV/m} @ n_e = 10^{14}\text{cm}^{-3}$$

- Summed image confirms reproducibility
- Wakefields start at the RIF

SEEDED SELF-MODULATION (SSM)

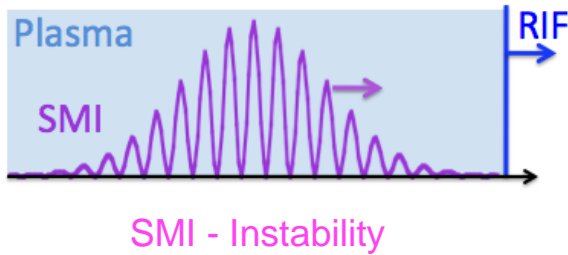


REPRODUCIBLE!

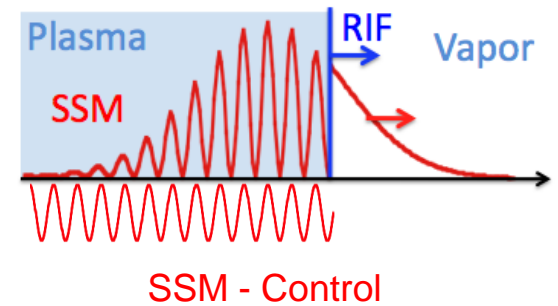


- ✧ Reproducibility essential for deterministic injection/acceleration
- ✧ $t_{e^-, inj}$ fixed!

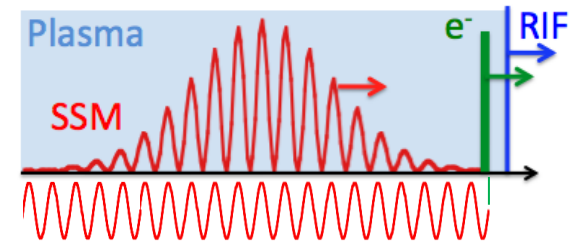
SEEDED SELF-MODULATION (SSM)



Relativistic Ionization Front
(RIF)
Seeding



e-bunch
Seeding



L. Verra et al., Phys. Rev. Lett. 129, 024802 (2022)

PHYSICAL REVIEW LETTERS

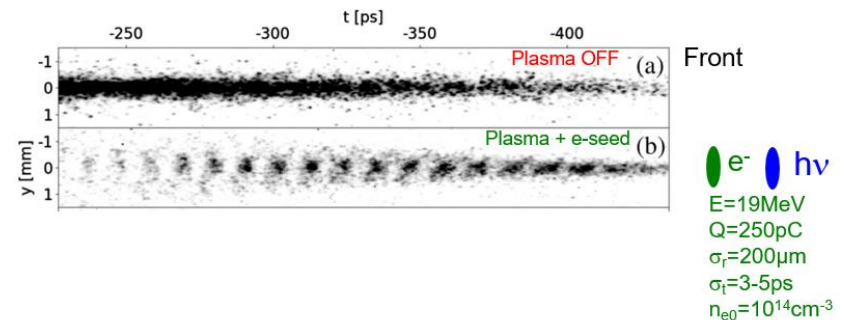
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Featured in Physics Editors' Suggestion Open Access

Controlled Growth of the Self-Modulation of a Relativistic Proton Bunch in Plasma

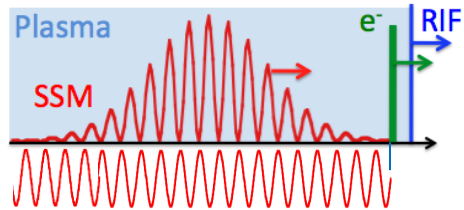
L. Verra et al. (AWAKE Collaboration)
Phys. Rev. Lett. 129, 024802 – Published 6 July 2022

PhysiCS See synopsis: [Controlling Instabilities in a Plasma Particle Accelerator](#)

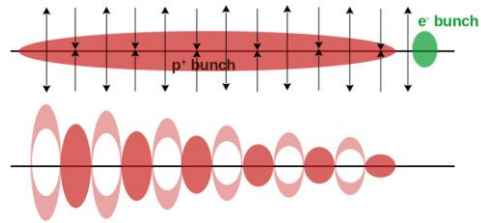


- ◇ SSM seeded by wakefields of e-bunch
- ◇ Same reproducibility as RIF-seeding
- ◇ SSM of entire bunch
- ◇ Independent control of seed (e^-) and growth (p^+ , n_{e0}) parameters

✧ e-bunch seeding of SM

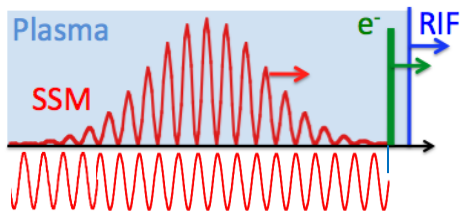


✧ e^- and p^+ aligned ...

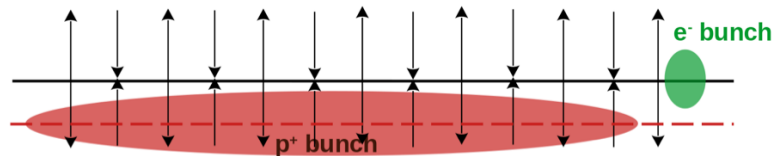


✧ ... axi-symmetric SM

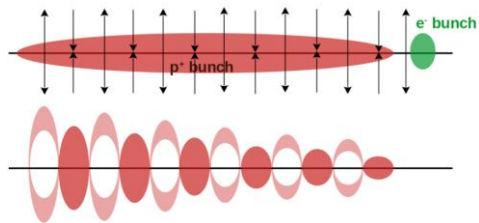
✧ e-bunch seeding of SM



✧ e⁻ and p⁺ mis-aligned ...



✧ e⁻ and p⁺ aligned ...

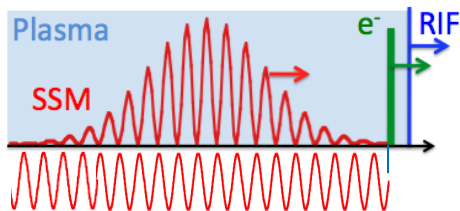


✧ ... non-axi-symmetric hosing (mis-alignment plane)

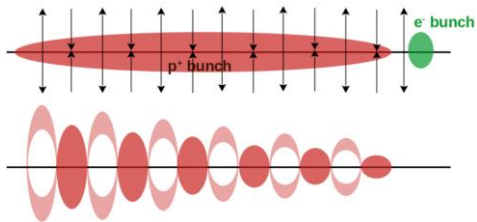
✧ ... and SM in the perpendicular plane (“no misalignment” plane)

✧ ... axi-symmetric SM

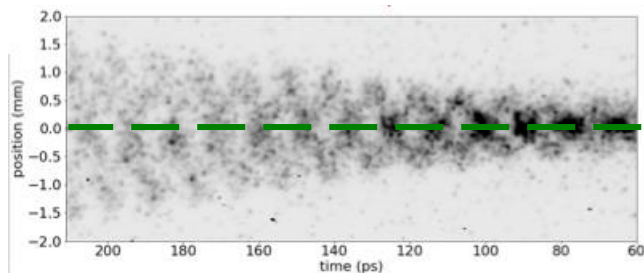
✧ e-bunch seeding of SM



✧ e⁻ and p⁺ aligned ...



✧ ... axi-symmetric SM



Front

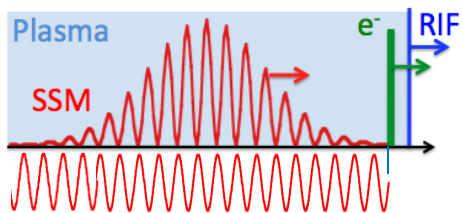
- ✧ e⁻/p⁺ aligned
- ✧ Self-modulation
- ✧ Symmetric

T. Nechaeva

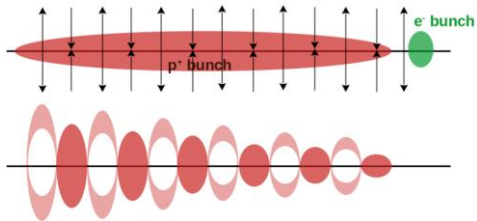
$$n_{e0} = 10^{14} \text{cm}^{-3}$$

$$N_{p+} = 3 \times 10^{11}$$

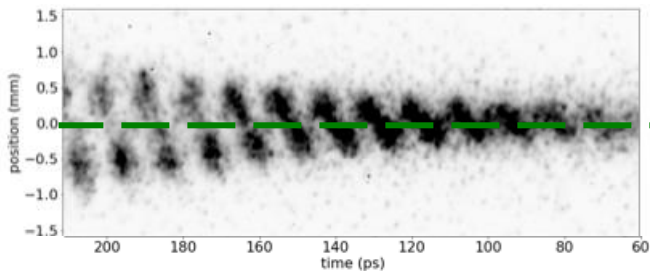
✧ e-bunch seeding of SM



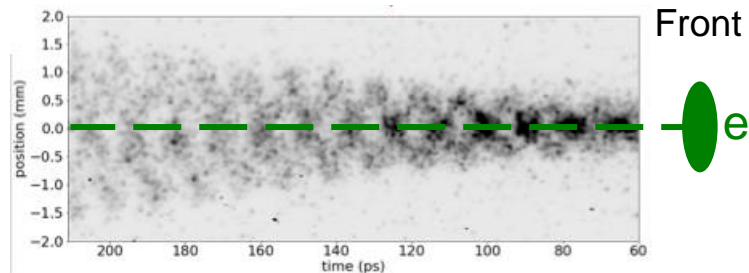
✧ e⁻ and p⁺ aligned ...



✧ ... axi-symmetric SM

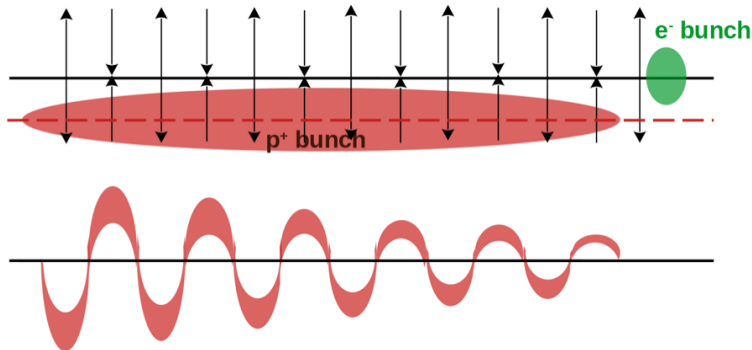


- ✧ e⁻/p⁺ mis-aligned
- ✧ Hosing
- ✧ Centroid oscillation



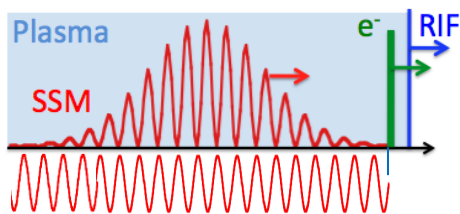
- ✧ e⁻/p⁺ aligned
- ✧ Self-modulation
- ✧ Symmetric

T. Nechaeva

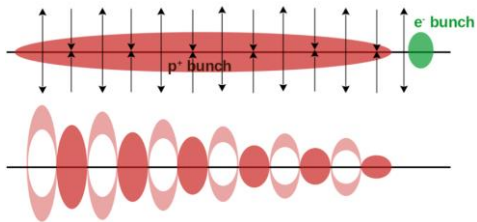


- ✧ SM and HI together
- ✧ $f_{HI} \sim f_{SM} \sim f_{pe}$
- ✧ Induced by wakefields

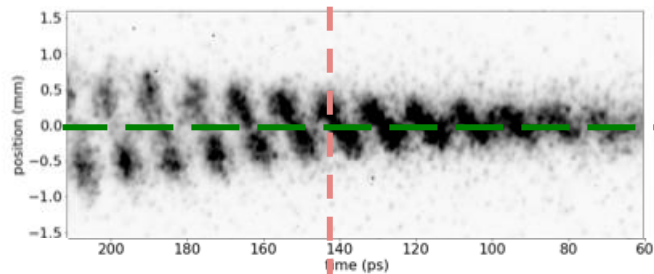
✧ e-bunch seeding of SM



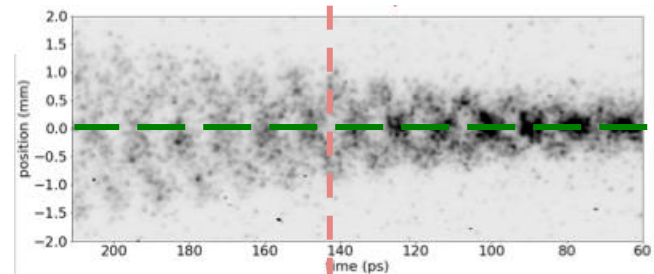
✧ e⁻ and p⁺ aligned ...



✧ ... axi-symmetric SM



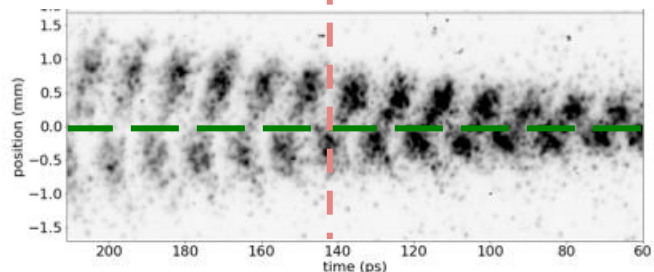
- ✧ e⁻/p⁺ mis-aligned
- ✧ Hosing
- ✧ Centroid oscillation



Front

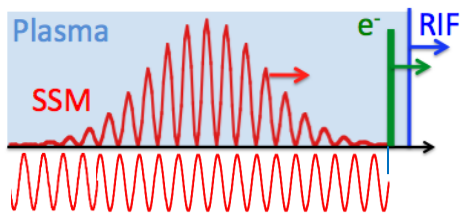
- ✧ e⁻/p⁺ aligned
- ✧ Self-modulation
- ✧ Symmetric

T. Nechaeva

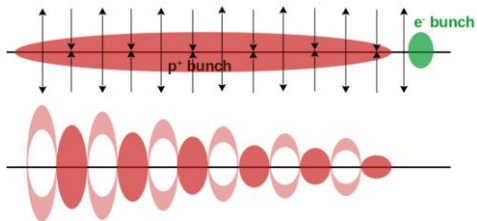


- ✧ e⁻/p⁺ mis-aligned
- ✧ Hosing
- ✧ Reversed!

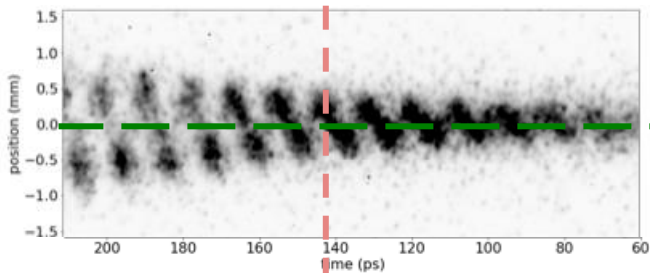
✧ e-bunch seeding of SM



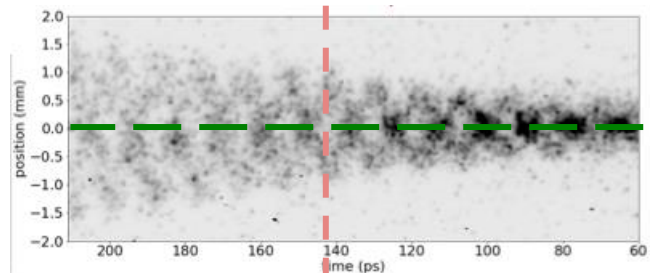
✧ e⁻ and p⁺ aligned ...



✧ ... axi-symmetric SM



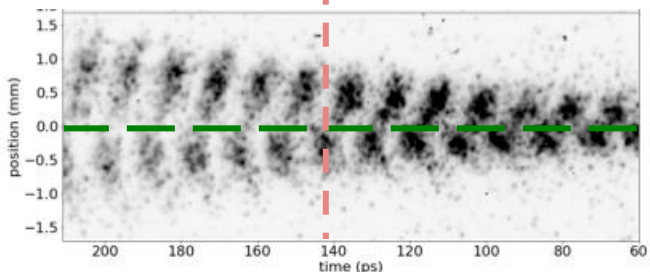
- ✧ e⁻/p⁺ mis-aligned
- ✧ Hosing
- ✧ Centroid oscillation



Front

- ✧ e⁻/p⁺ aligned
- ✧ Self-modulation
- ✧ Symmetric

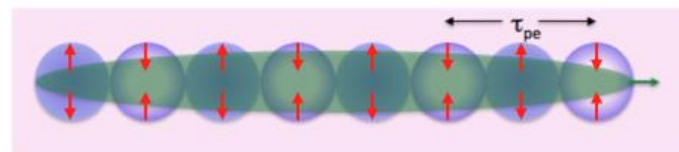
T. Nechaeva



- ✧ e⁻/p⁺ mis-aligned
- ✧ Hosing
- ✧ Reversed!

FILAMENTATION INSTABILITY

✧ $\sigma_{r0} < c/\omega_{pe}$: ($k_{pe}\sigma_{r0} < 1$) optimum for wakefield generation ...



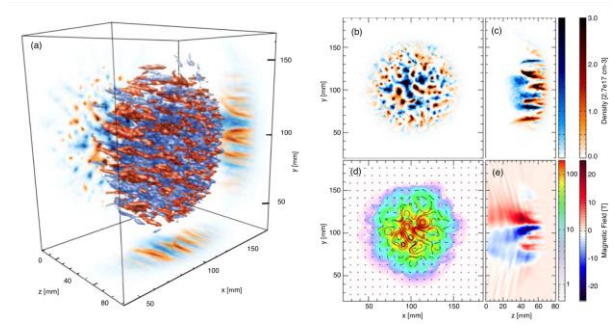
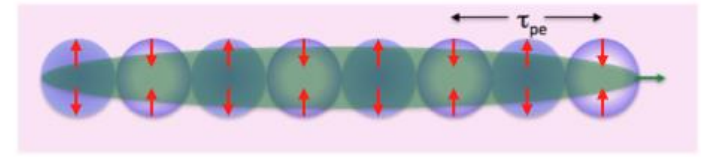
Return current outside the bunch
Wakefields can develop

FILAMENTATION INSTABILITY

- ✧ $\sigma_{r0} < c/\omega_{pe}$: ($k_{pe}\sigma_{r0} < 1$) optimum for wakefield generation ...
- ✧ $\sigma_{r0} \gg c/\omega_{pe}$: ($k_{pe}\sigma_{r0} \gg 1$) filamentation instabilities can develop ...
 - ✧ Equal streams: current filamentation instability (CFI)
 - ✧ Unequal streams: oblique modes, wakefields, ...

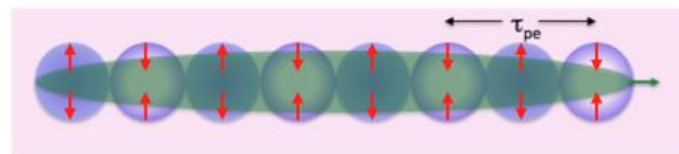
$$n_b \ll n_{e0} \quad \rightarrow \quad \vec{k} = \vec{k}_\perp + \vec{k}_\parallel$$

$$v_{p+} \gg v_e$$



Shukla, J. Plasma Phys. 84(3) 905840302 (2018)
 Allen, Phys. Rev. Lett. 109, 185007 (2012)

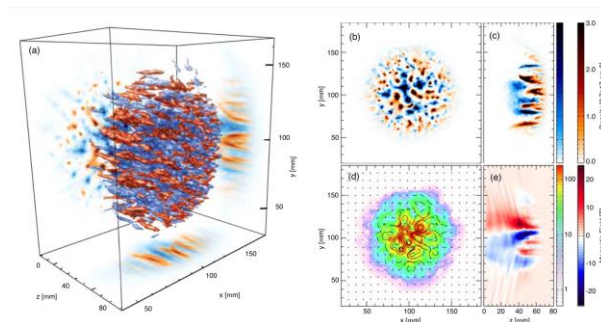
- ✧ $\sigma_{r0} < c/\omega_{pe}$: ($k_{pe}\sigma_{r0} < 1$) optimum for wakefield generation ...
- ✧ $\sigma_{r0} \gg c/\omega_{pe}$: ($k_{pe}\sigma_{r0} \gg 1$) filamentation instabilities can develop ...



- ✧ Equal streams: current filamentation instability (CFI)
- ✧ Unequal streams: oblique modes, wakefields, ...

$$n_b \ll n_{e0} \quad \longrightarrow \quad \vec{k} = \vec{k}_\perp + \vec{k}_\parallel$$

$$v_{p+} \gg v_e$$



- ✧ Astrophysics: generation of magnetic fields in the universe?

- ✧ Collision: neutral, expanding supernova plasma – interstellar plasma

- ✧ CFI :

- ✧ Generates magnetic fields

- ✧ Converts kinetic energy of the expanding plasma into B-field energy and plasma kinetic energy

- ✧ Evolution: filaments -> coalescence -> shock formation

- ✧ Study FI with relativistic particle bunch (p^+) or “fireball” ($e^- e^+$) beam

- ✧ “Astrophysics in the lab”



Core-collapse, or type II supernovas, are caused by the impllosion of massive stars like red supergiants. (Supplied: ESA/Hubble, C. Carozzi)

FILAMENTATION INSTABILITY

Transverse Filamentation: $\sigma_{r0} \sim 200 \Rightarrow 550 \mu\text{m} \gg c/\omega_{pe}$ AND $\sigma_z \gg c/\omega_{pe}$

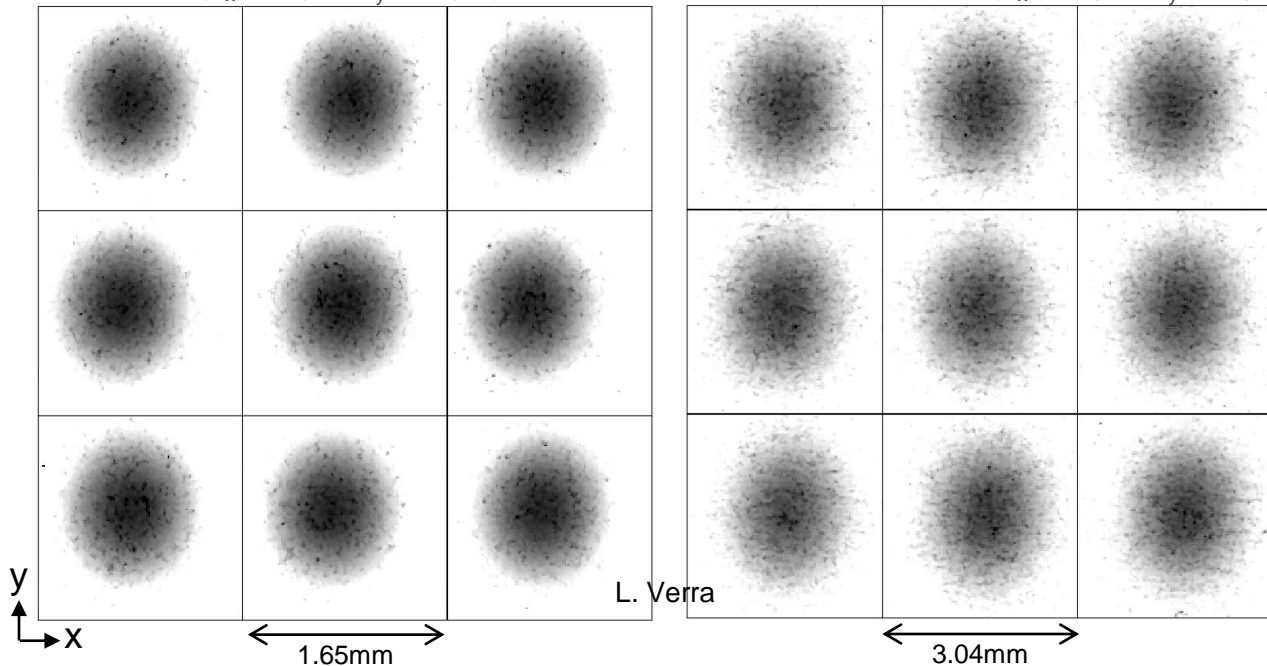


FILAMENTATION INSTABILITY

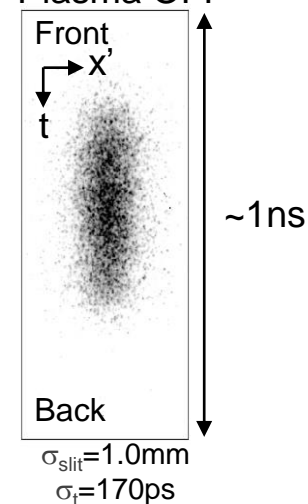
Transverse Filamentation: $\sigma_{r0} \sim 200 \Rightarrow 550 \mu\text{m} \gg c/\omega_{pe}$ AND $\sigma_z \gg c/\omega_{pe}$

Entrance ($\sigma_x = 480 \mu\text{m}$, $\sigma_y = 520 \mu\text{m}$)

Exit: Plasma OFF ($\sigma_x = 810 \mu\text{m}$, $\sigma_y = 870 \mu\text{m}$)



Plasma OFF

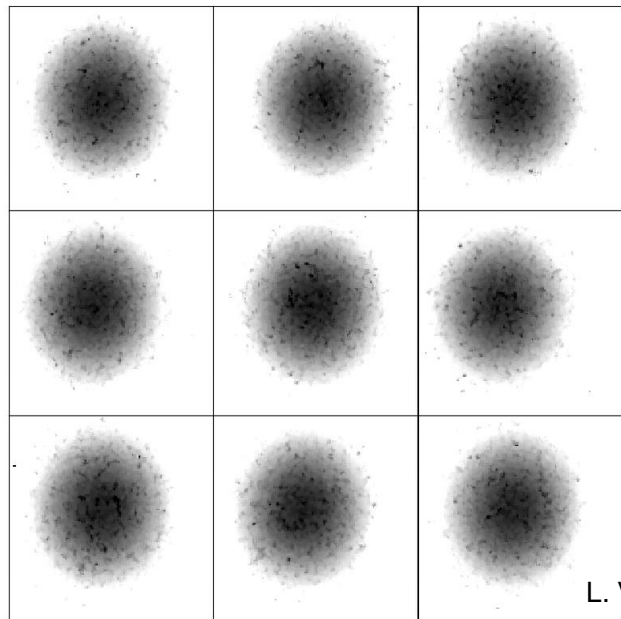


✧ Incoming bunch without transverse features (Gaussian)

FILAMENTATION INSTABILITY

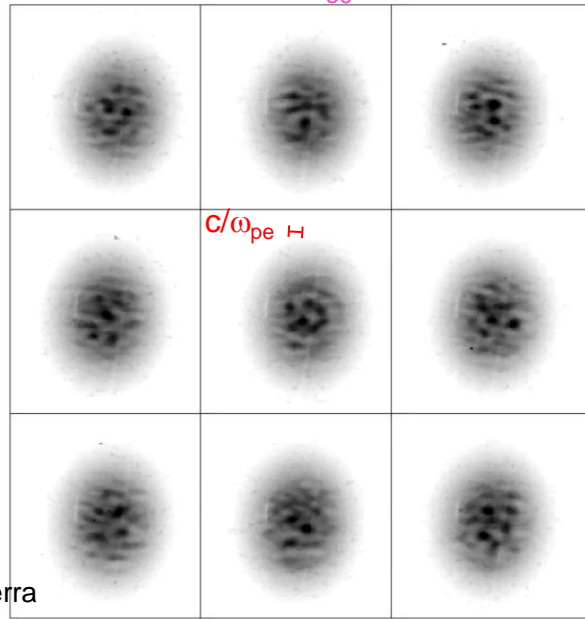
Transverse Filamentation: $\sigma_{r0} \sim 550 \mu\text{m} \sim 3.2c/\omega_{pe}$ AND $\sigma_z \gg c/\omega_{pe}$

Entrance



1.65mm

Exit: Plasma ON, $n_{e0} = 9 \times 10^{14} \text{cm}^{-3}$



3.04mm

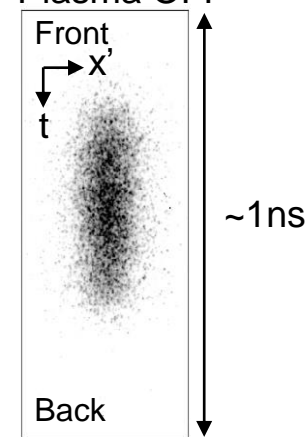
L. Verra



✧ Incoming bunch without transverse features (Gaussian)

✧ Filaments with plasma

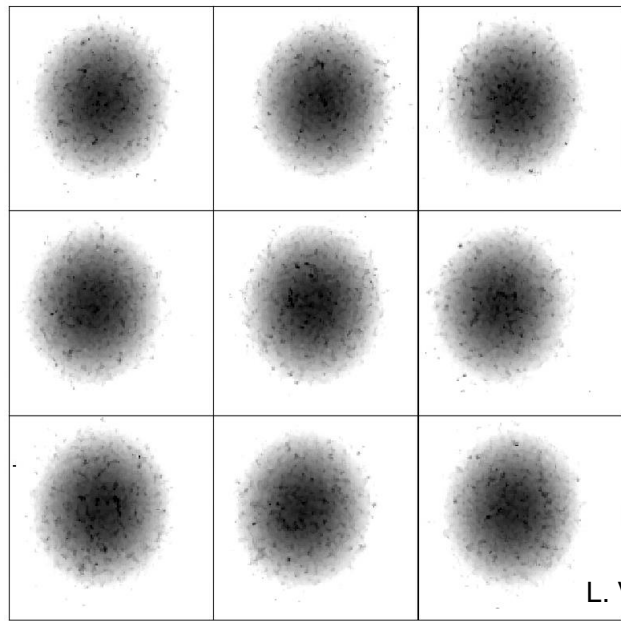
Plasma OFF



FILAMENTATION INSTABILITY

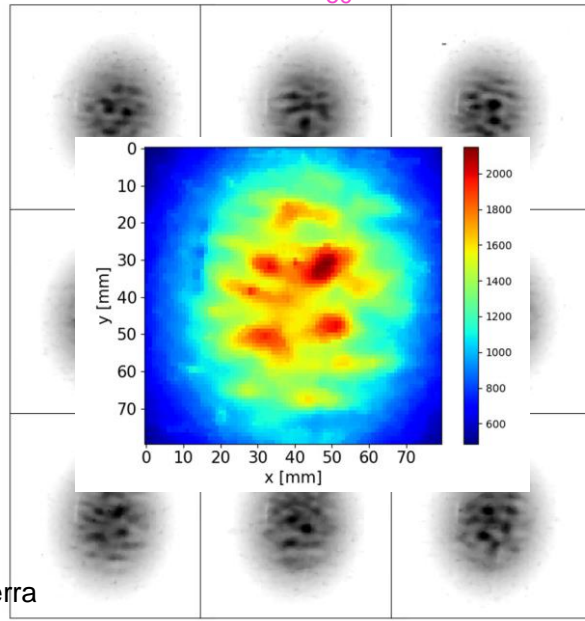
Transverse Filamentation: $\sigma_{r0} \sim 550 \mu\text{m} \sim 3.2c/\omega_{pe}$ AND $\sigma_z \gg c/\omega_{pe}$

Entrance



1.65mm

Exit: Plasma ON, $n_{e0} = 9 \times 10^{14} \text{cm}^{-3}$

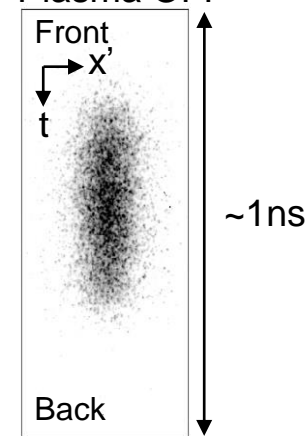


3.04mm

L. Verra



Plasma OFF



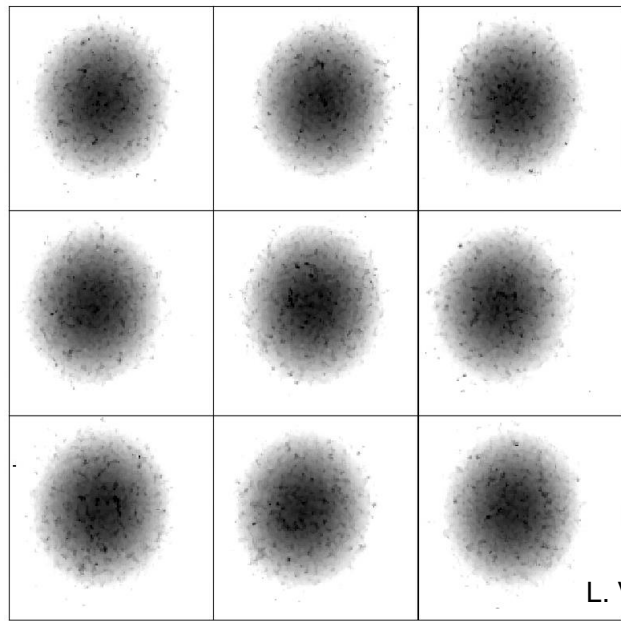
✧ Incoming bunch without transverse features (Gaussian)

✧ Filaments with plasma

FILAMENTATION INSTABILITY

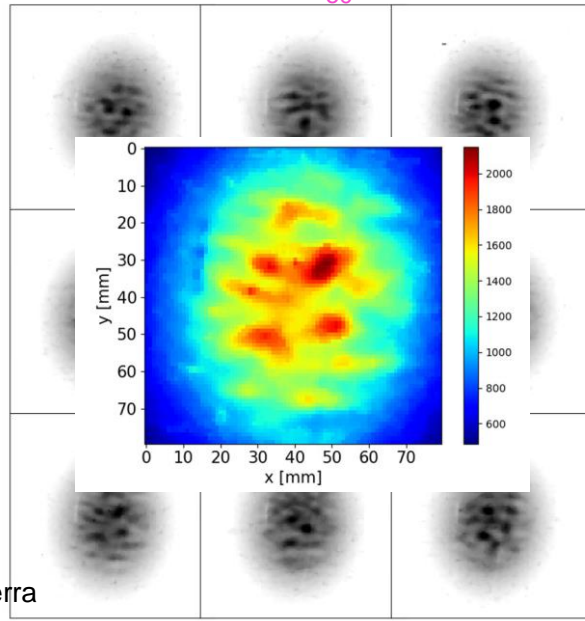
Transverse Filamentation: $\sigma_{r0} \sim 550 \mu\text{m} \sim 3.2c/\omega_{pe}$ AND $\sigma_z \gg c/\omega_{pe}$

Entrance



1.65mm

Exit: Plasma ON, $n_{e0} = 9 \times 10^{14} \text{cm}^{-3}$

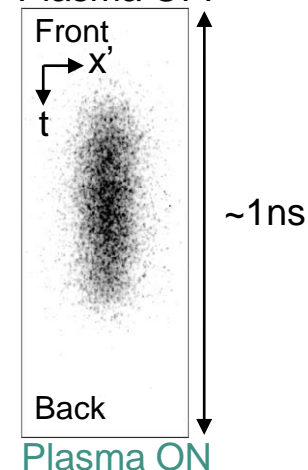


3.04mm

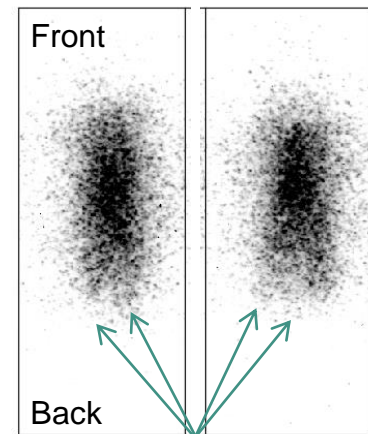
L. Verra



Plasma OFF



Plasma ON



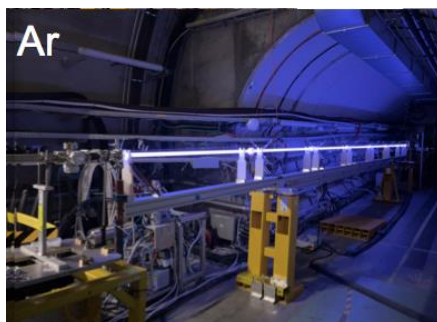
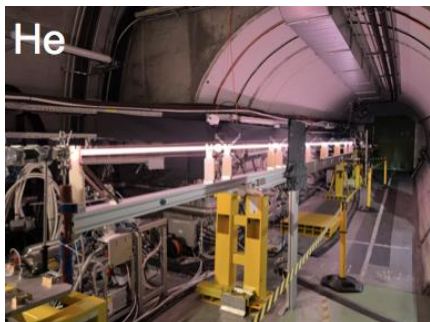
Filament?

✧ Incoming bunch without transverse features (Gaussian)

✧ Filaments with plasma, late along the bunch, early stage?

L. Verra et al., AWAKE Collaboration, Phys. Rev. E 109, 055203 (2024)

DISCHARGE PLASMA SOURCE



✧ $A_{\text{He}}=4$

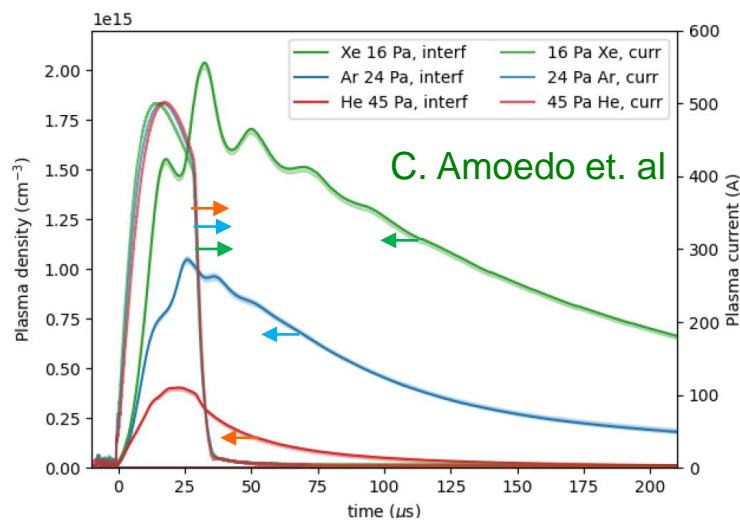
✧ $A_{\text{Ar}}=40$

✧ $A_{\text{Rb}}=85$

✧ $A_{\text{Xe}}=131$

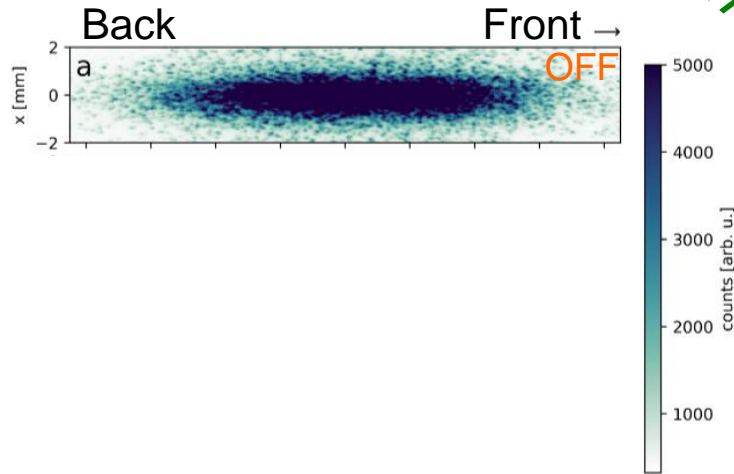
Discharge plasma source (DPS):

- ✧ Quick change of density
- ✧ Reach high plasma densities $>10^{15}\text{cm}^{-3}$
- ✧ Change ion species: He, Ar, Xe
- ✧ No alignment ($r_p \sim 10\text{mm}$)



Effect of ion motion on:

- ✧ Accelerated bunch quality
- ✧ Acceleration process



Preliminary

ξ [ps]

M. Turner

Long, low density bunch:

Plasma:

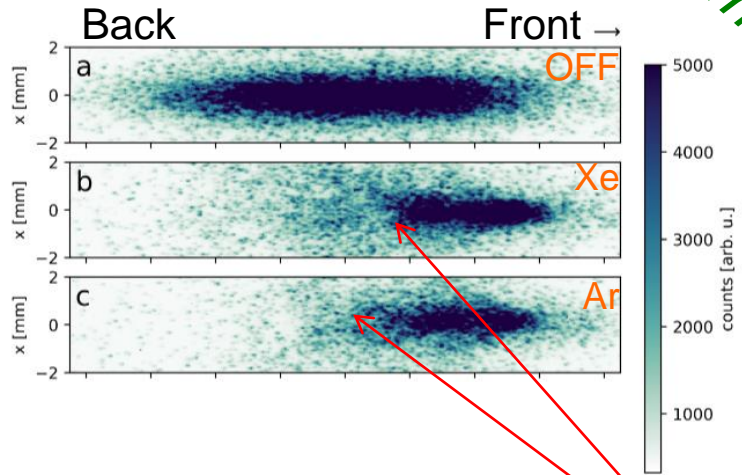
- ✧ Light, mobile electrons
- ✧ Heavy ($m_i \geq 1832m_e$) immobile ions
 - ✧ $\omega_{pe} \gg \omega_{pi}$
 - ✧ ps \leftrightarrow ns
- ✧ Large force, ions move at ω_{pe} scale?
- ✧ Not seeded: SMI

ION MOTION?

Effect of ion motion on:

- ✧ Accelerated bunch quality
- ✧ Acceleration process

Preliminary

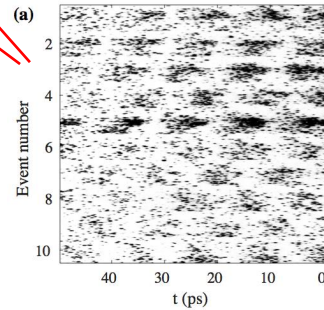


No!

M. Turner

Long, low density bunch:

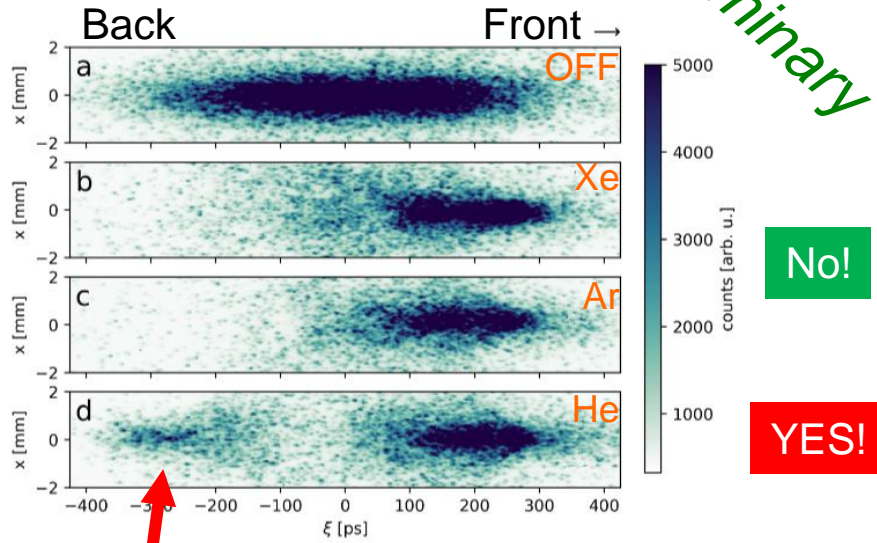
- ✧ Typical SMI (Xe, Ar)



Effect of ion motion on:

- ✧ Accelerated bunch quality
- ✧ Acceleration process

Preliminary



M. Turner

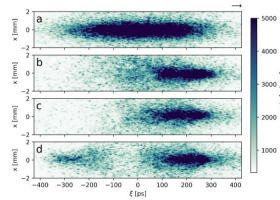
Long, low density bunch:

- ✧ Typical SMI (Xe, Ar)
- ✧ “Tail” appear in the back of the bunch (He)

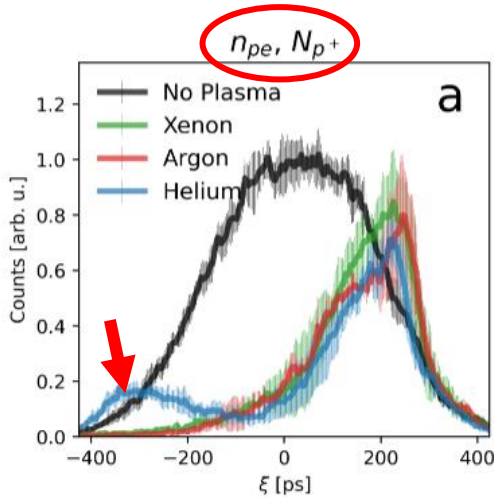
ION MOTION

Effect of ion motion on:

- Accelerated bunch quality
- Acceleration process



M. Turner



“Tail” with He, not with Ar, Xe

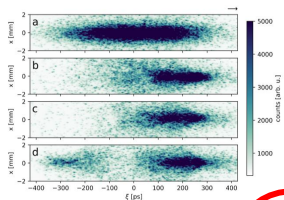
Long, low density bunch:

- Typical SMI (Xe, Ar)
- “Tail” appear in the back of the bunch (He)

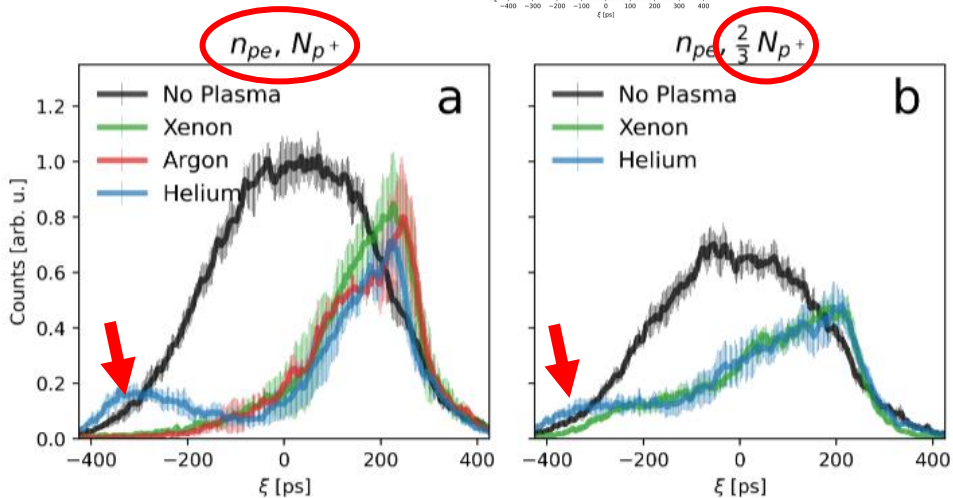
Preliminary

Effect of ion motion on:

- Accelerated bunch quality
- Acceleration process



M. Turner



“Tail” with He, not with Ar, Xe

Lower wakefield amplitude, less tail

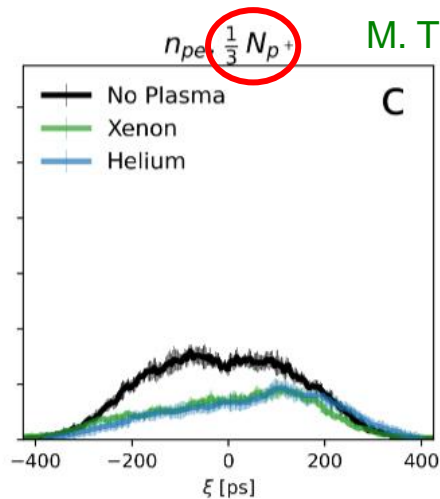
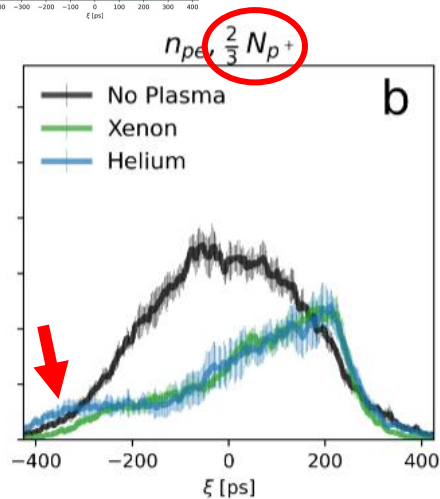
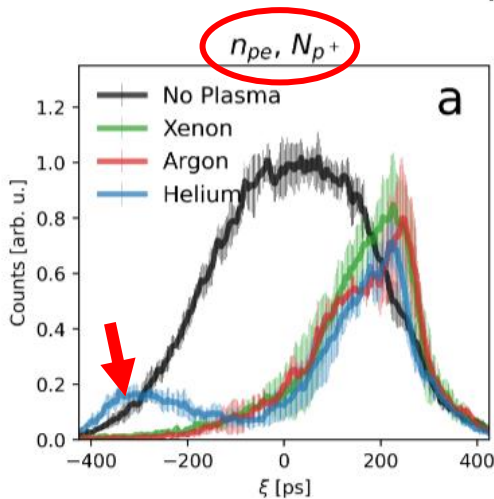
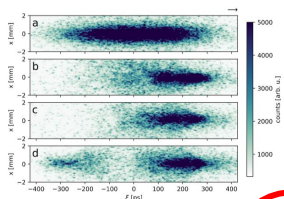
Long, low density bunch:

- Typical SMI (Xe, Ar)
- “Tail” appear in the back of the bunch (He)

Preliminary

Effect of ion motion on:

- Accelerated bunch quality
- Acceleration process



M. Turner

“Tail” with He, not with Ar, Xe

Lower wakefield amplitude, less tail

Even less

Long, low density bunch:

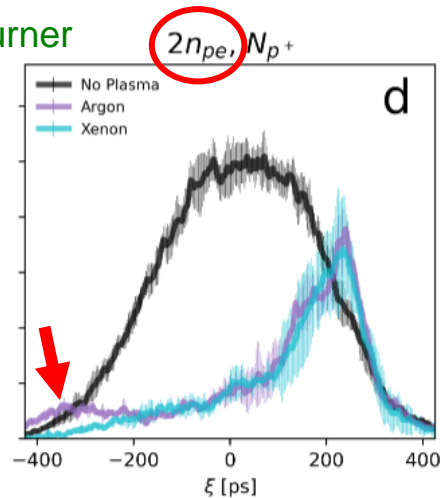
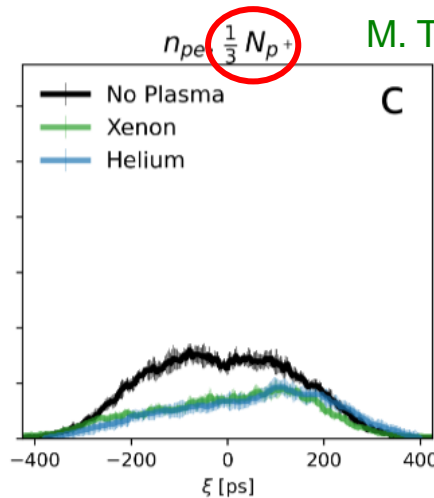
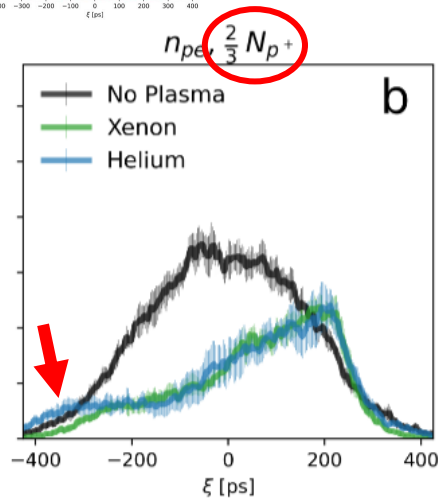
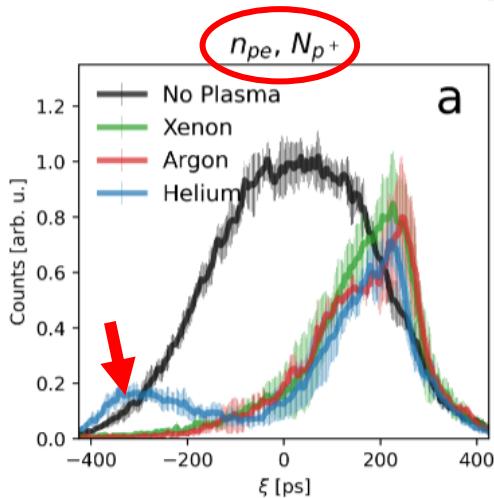
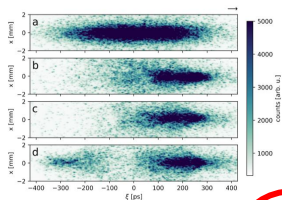
Typical SMI (Xe, Ar)

“Tail” appear in the back of the bunch (He)

Preliminary

Effect of ion motion on:

- Accelerated bunch quality
- Acceleration process



M. Turner

“Tail” with He, not with Ar, Xe

Lower wakefield amplitude, less tail

Even less

Higher wakefield amplitude, tail with Ar, but not with Xe

Long, low density bunch:

Typical SMI (Xe, Ar)

“Tail” appear in the back of the bunch (He)

More “tail” with lighter ion (He), larger wakefield amplitude (N_{p+}, n_{e0}) (Ar)

Preliminary

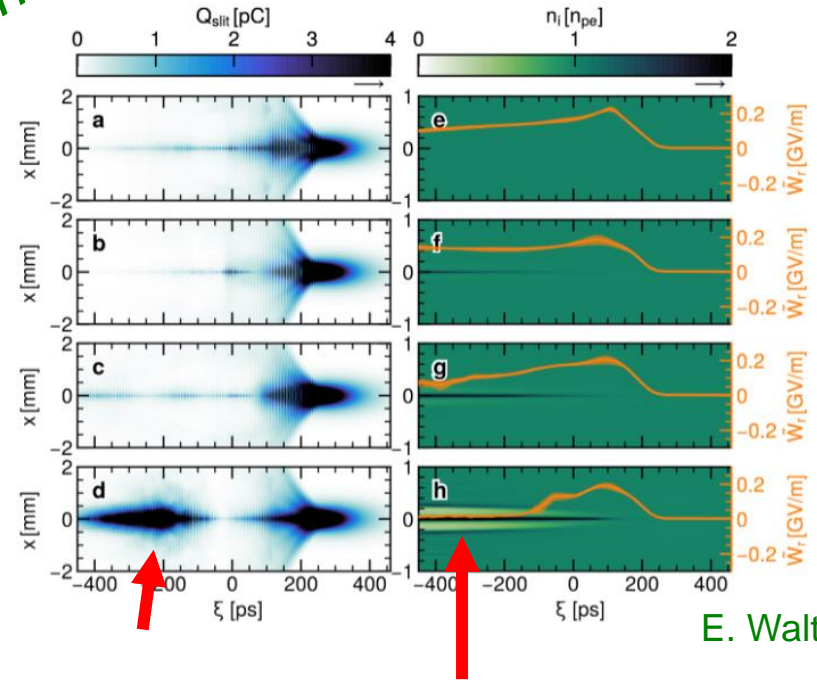
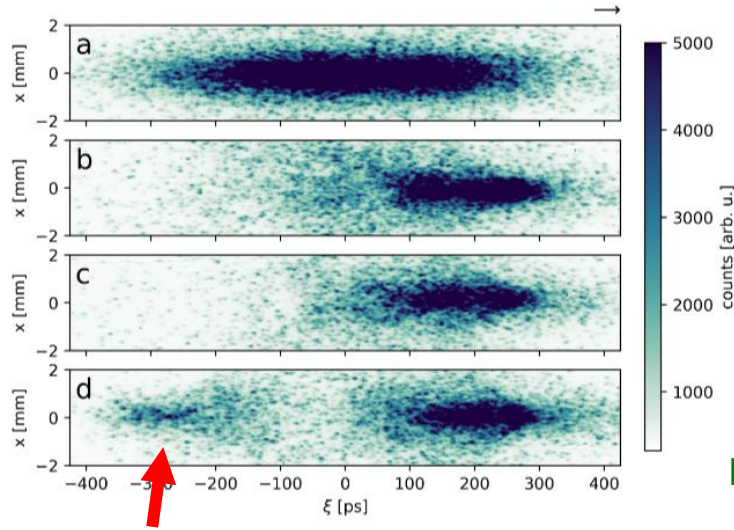
Preliminary

M. Turner

E. Walter

Effect of ion motion on:

- Accelerated bunch quality
- Acceleration process



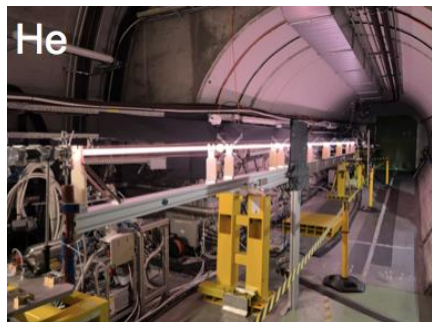
Long, low density bunch:

- Typical SMI (Xe, Ar)
- “Tail” appear in the back of the bunch (He)
- More “tail” with lighter ion (He), larger wakefield amplitude (N_{p+} , n_{e0}) (Ar)
- Numerical simulations confirm: ion motion because of ponderomotive force of the wakefields

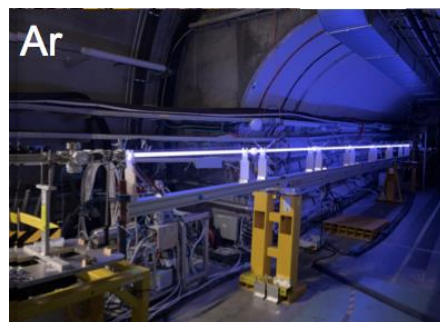
$$F_p \cong -\frac{e^2}{4m_e\omega_{pe}^2} \nabla W_r^2$$



DISCHARGE PLASMA SOURCE



◇ $A_{\text{He}}=4$



◇ $A_{\text{Ar}}=40$



◇ $A_{\text{Rb}}=85$

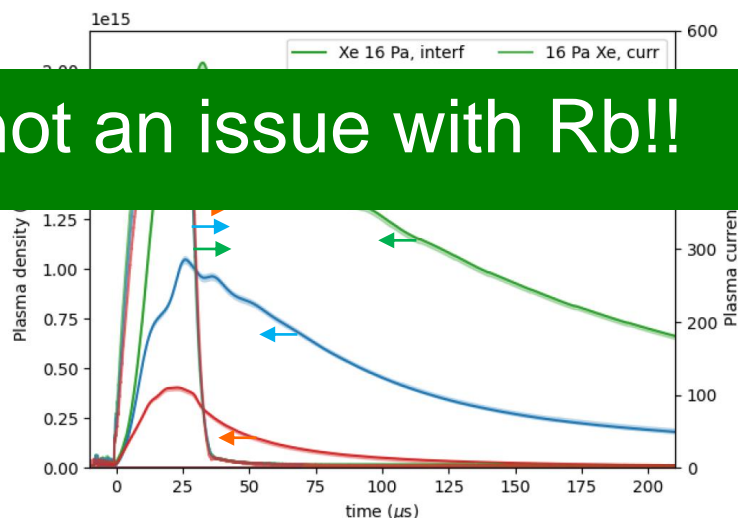


◇ $A_{\text{Xe}}=131$

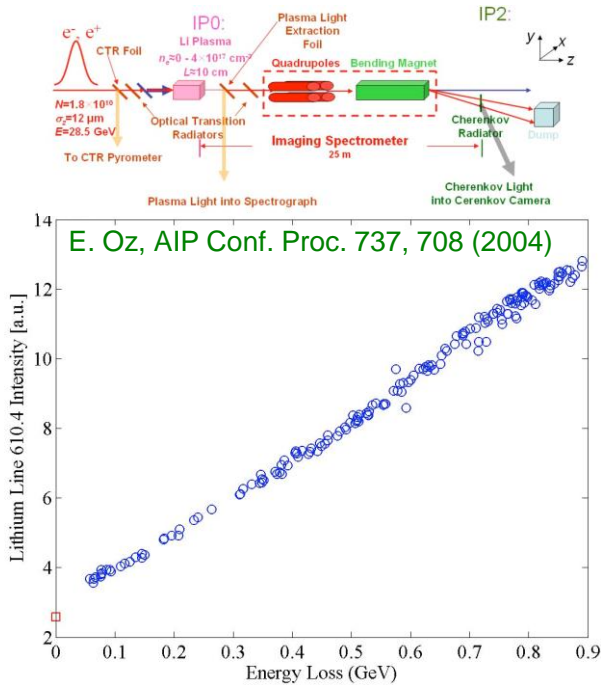
Discharge plasma source (DPS):

- ◇ Quick change
- ◇ Reach high
- ◇ Change ion species: He, Ar, Xe
- ◇ No alignment ($r_p \sim 10\text{mm}$)

Ion motion not an issue with Rb!!

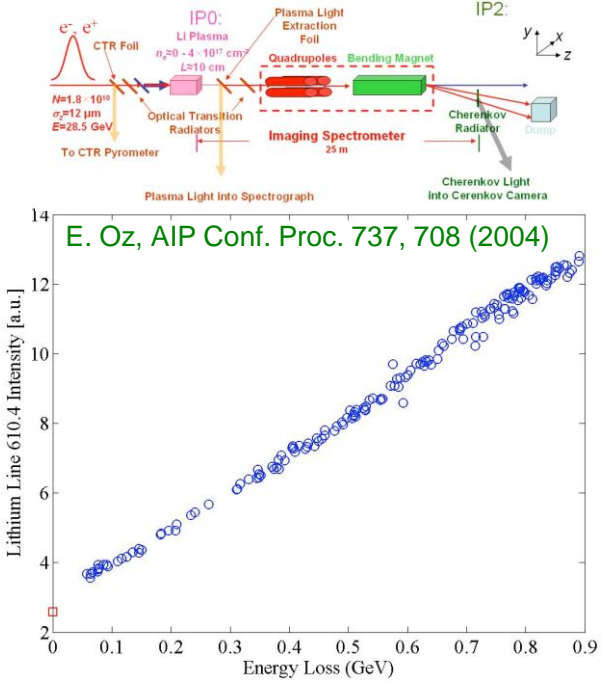


- ✧ Wakefields \Leftrightarrow energy deposited into plasma e^-
- ✧ Energy must dissipate
- ✧ Dissipation of wakefields produces “wakefield light” (atomic line radiation)



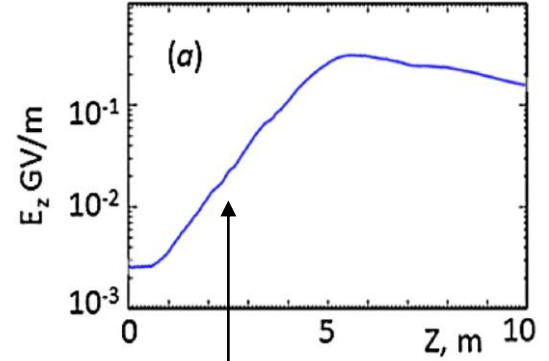
✧ Light from wakefields
proportional to energy deposited

- ✧ Wakefields \Leftrightarrow energy deposited into plasma e^-
- ✧ Energy must dissipate
- ✧ Dissipation of wakefields produces “wakefield light” (atomic line radiation)

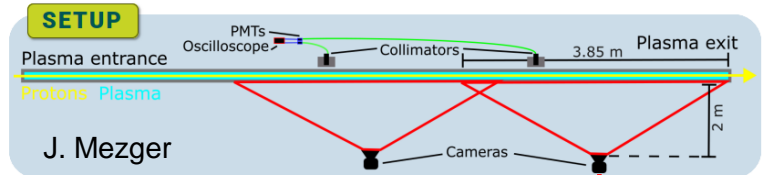


✧ Light from wakefields proportional to energy deposited

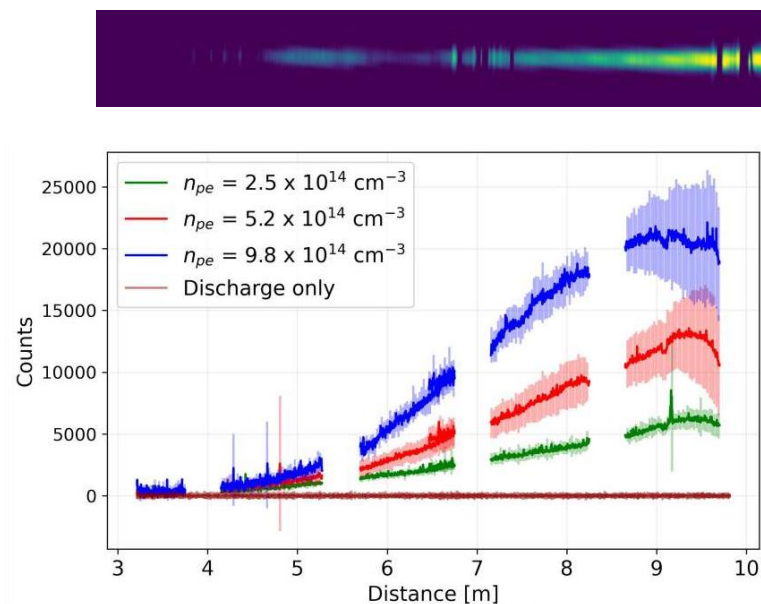
Pukhov, PRL107 145003 (2011)



- ✧ SM grows along the plasma
- ✧ Can the growth be observed?



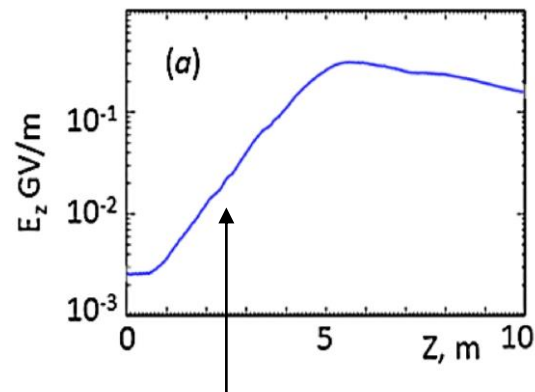
- ✧ Wakefields \Leftrightarrow energy deposited into plasma e^-
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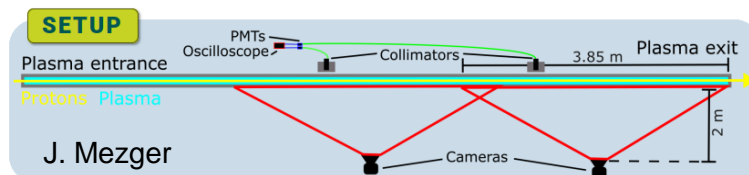
- ✧ Growth of SM along the plasma visible
- ✧ Measurement for growth rate?

J. Mezger

Pukhov, PRL107 145003 (2011)



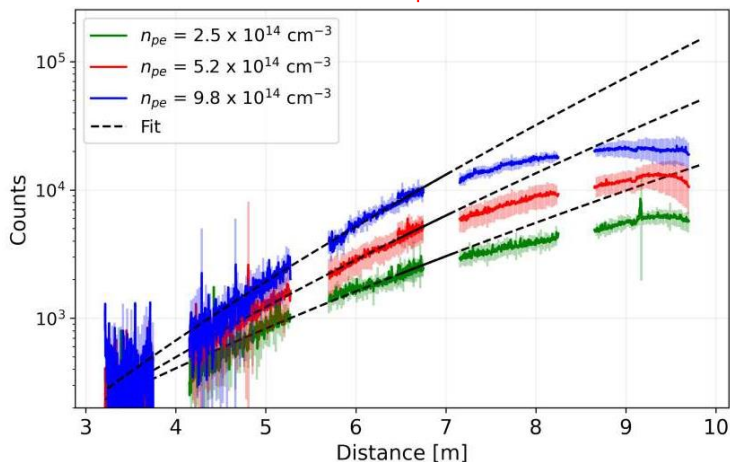
- ✧ SM grows along the plasma
- ✧ Can the growth be observed?



- ✧ Wakefields \Leftrightarrow energy deposited into plasma e^-
- ✧ Energy must dissipate
- ✧ Dissipation of wakefields produces “wakefield light” (atomic line radiation)

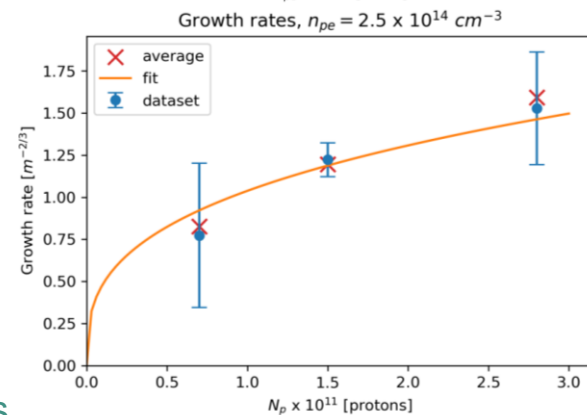
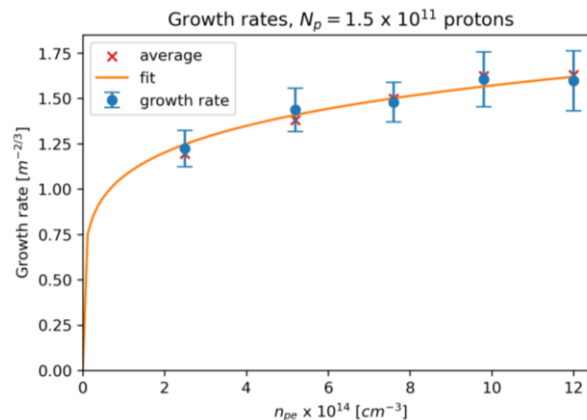
$$E = E_0 e^{z^{2/3} \Gamma} \quad \Gamma = \frac{3^{3/2}}{4} \left(\frac{m_e k_{pe}^3}{n_e m_p \gamma} \nu n_b(\zeta, r=0) \zeta \right)^{1/3}$$

$$\Gamma \sim n_b^{1/3} // n_{pe}^{-1/6}$$



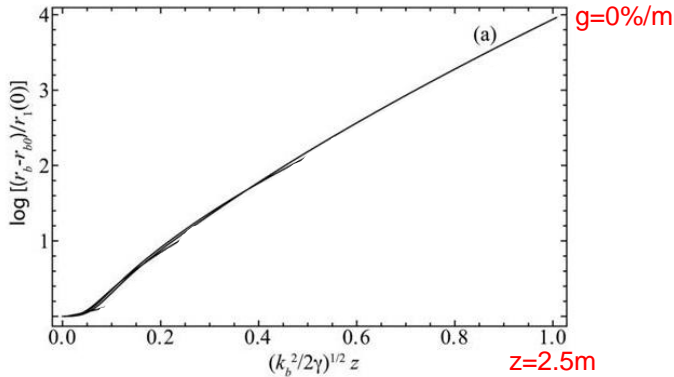
- ✧ Growth of SM along the plasma visible
- ✧ Measurement for growth rate?
- ✧ Measured growth rate consistent with n_{e0} and N_{p+} dependencies

J. Mezger



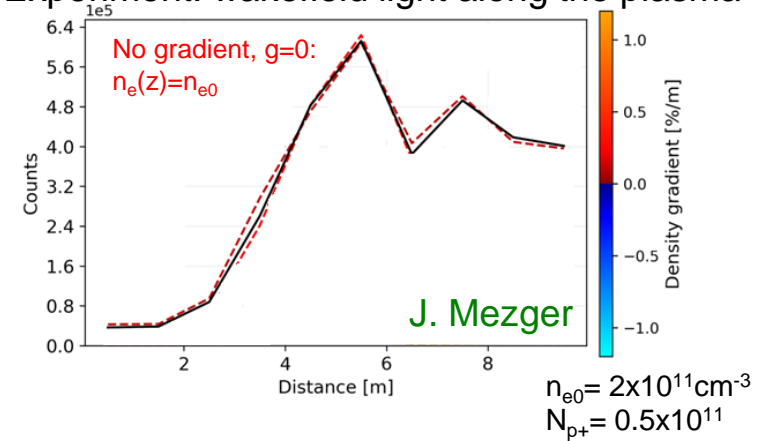
✧ Theory prediction: plasma density gradient suppressed SM

Theory: bunch radial modulation



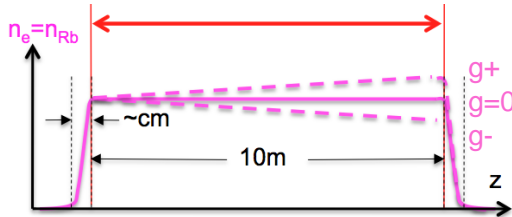
C. B. Schroeder, et al., *Phys. Plasmas* 19, 010703 (2012)

Experiment: wakefield light along the plasma



Preliminary

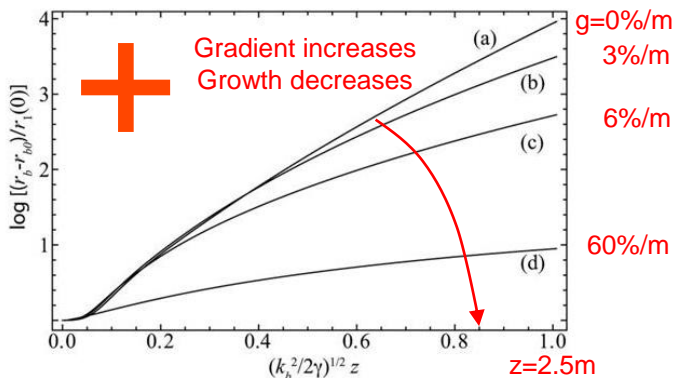
$$\text{Gradient: } g[\%/m] = 100(n_e(L=10m) - n_{e0})/n_{e0}$$



✧ Can apply positive/negative, linear plasma density gradients

✧ Theory prediction: plasma density gradient suppressed SM

Theory: bunch radial modulation

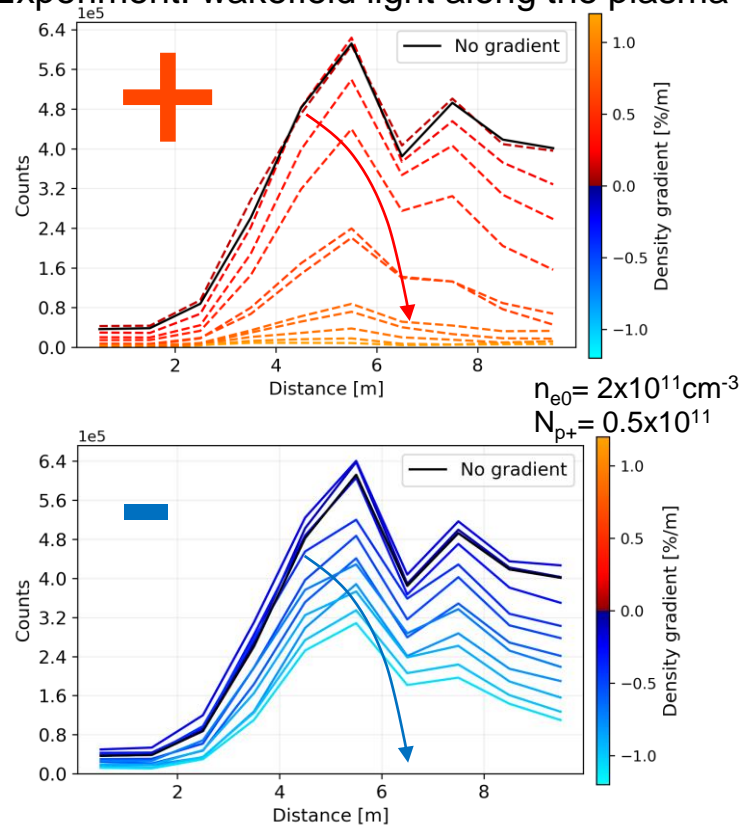


C. B. Schroeder, et al., *Phys. Plasmas* 19, 010703 (2012)

Preliminary

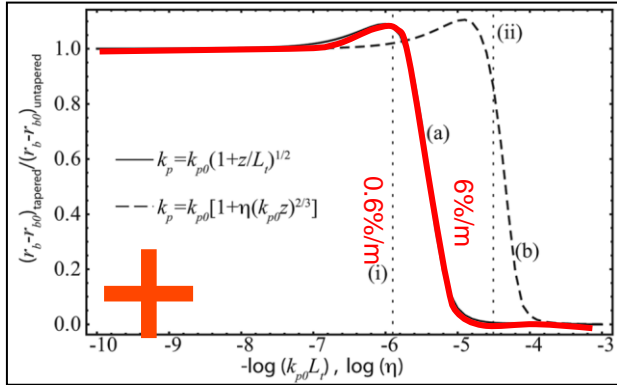
- ✧ Positive and negative gradient suppression of SM
- ✧ Consistent with predictions ...
- ✧ Observe also for negative gradients ...

Experiment: wakefield light along the plasma



✧ Theory prediction: more modulation of small positive gradient

Theory: bunch radial modulation

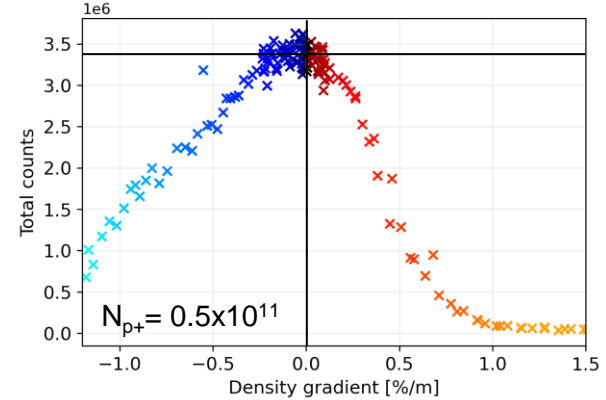


C. B. Schroeder, et al., *Phys. Plasmas* 19, 010703 (2012)

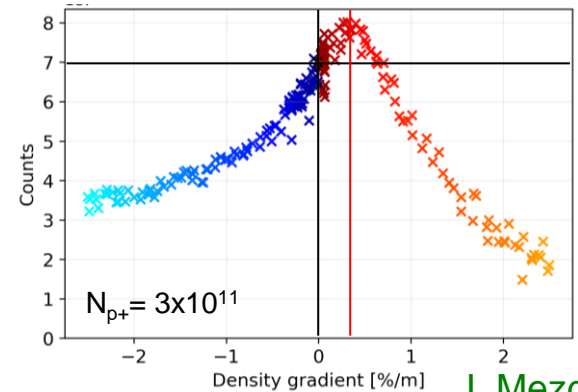
Preliminary

✧ In general: less light → “less wakefields”

Experiment: sum of wakefield light



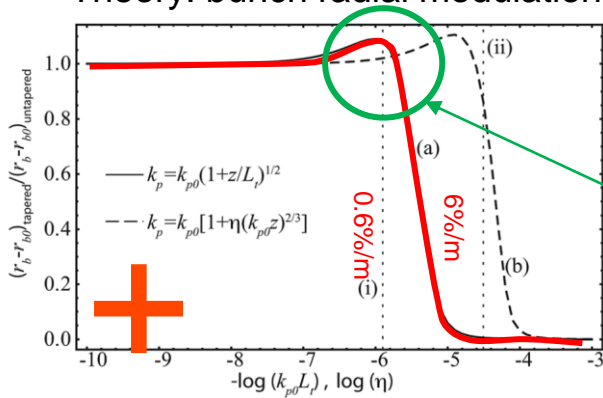
$n_{e0} = 2 \times 10^{11} \text{ cm}^{-3}$



J. Mezger 24/30

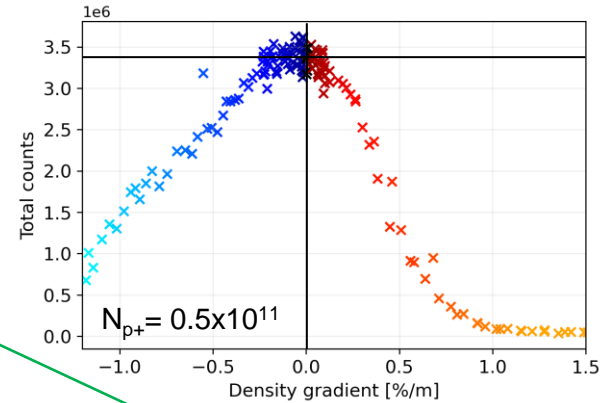
✧ Theory prediction: more modulation of small positive gradient

Theory: bunch radial modulation



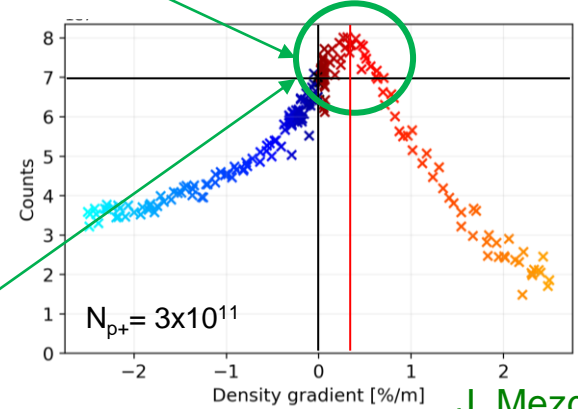
C. B. Schroeder, et al., *Phys. Plasmas* 19, 010703 (2012)

Experiment: sum of wakefield light

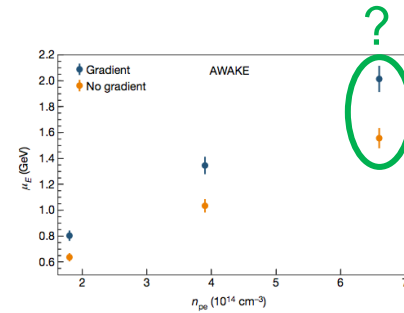


$n_{e0} = 2 \times 10^{11} \text{ cm}^{-3}$

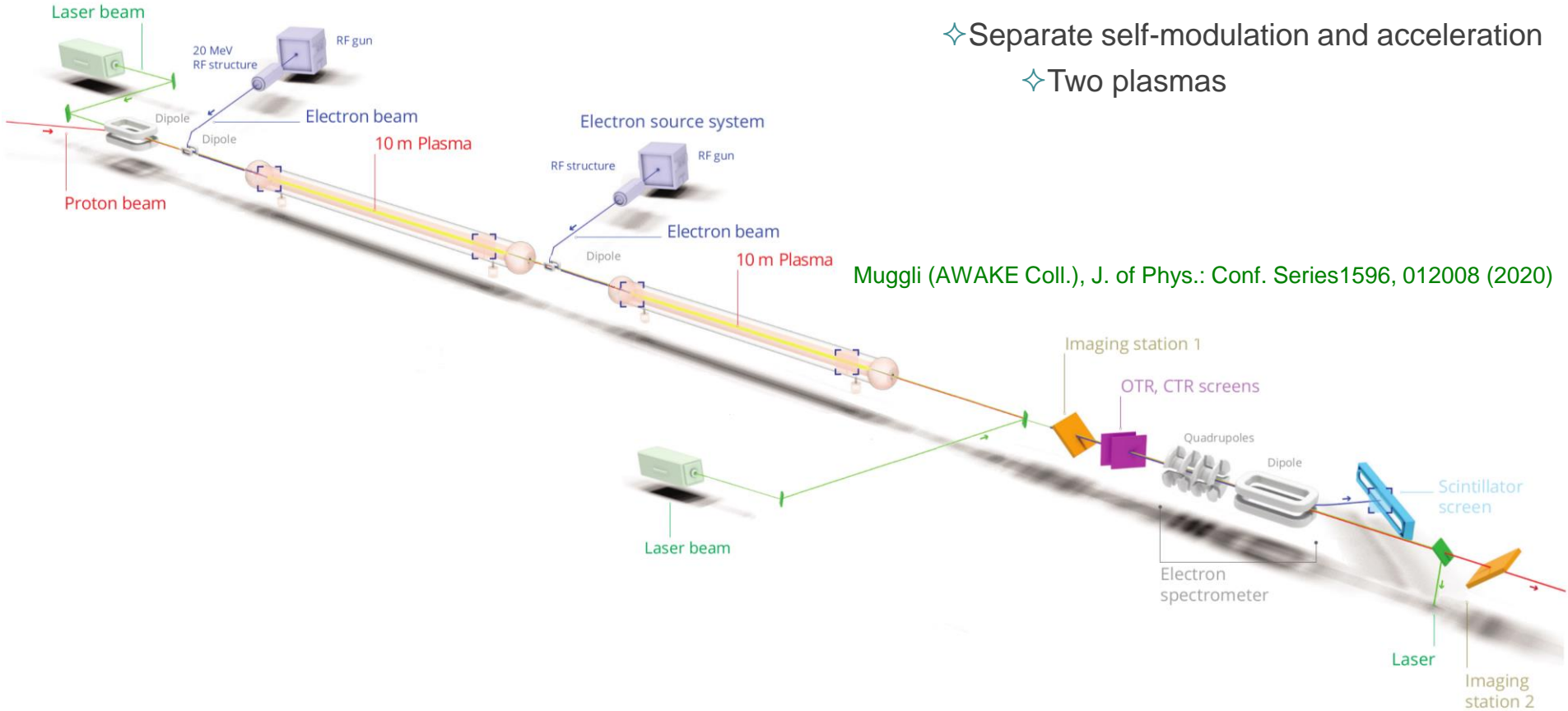
- ✧ In general: less light → “less wakefields”
- ✧ “More wakefields” with small gradient ($g \sim 0.5\%/m$)!
- ✧ Consistent with predictions ...



J. Mezger 24/30



RUN 2c,d: ACCELERATE e^- BUNCH, QUALITY

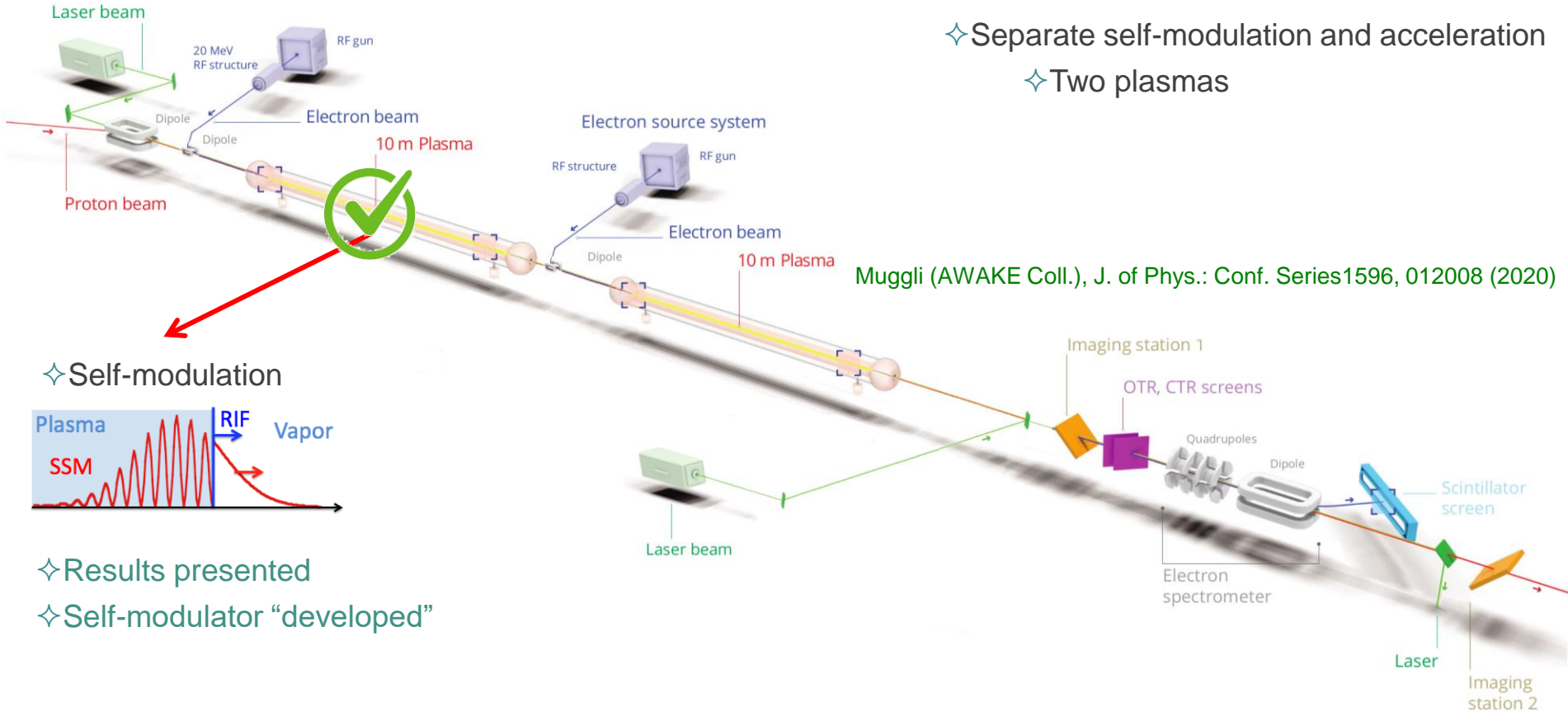


- ✧ Separate self-modulation and acceleration
- ✧ Two plasmas

Muggli (AWAKE Coll.), J. of Phys.: Conf. Series 1596, 012008 (2020)

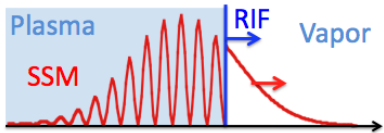
RUN 2c,d: ACCELERATE e^- BUNCH, QUALITY

- ✧ Separate self-modulation and acceleration
- ✧ Two plasmas



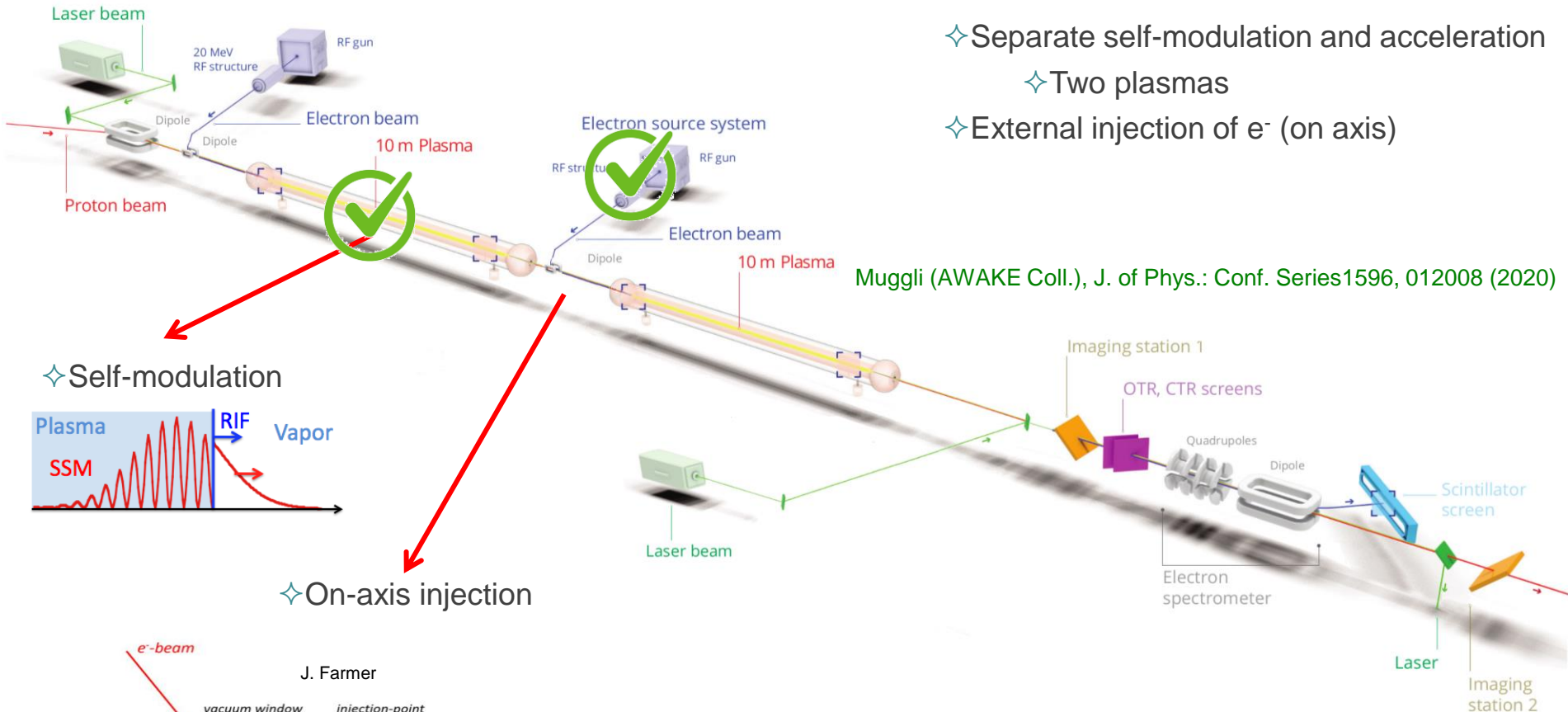
Muggli (AWAKE Coll.), J. of Phys.: Conf. Series 1596, 012008 (2020)

- ✧ Self-modulation



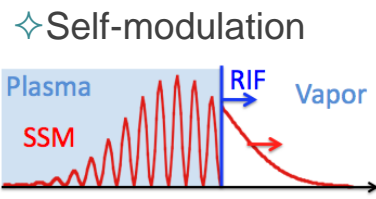
- ✧ Results presented
- ✧ Self-modulator “developed”

RUN 2c,d: ACCELERATE e^- BUNCH, QUALITY



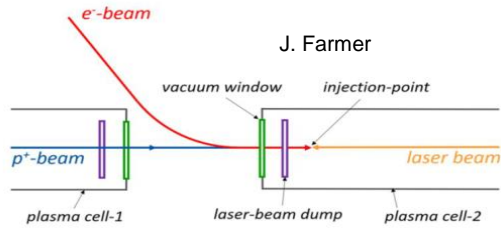
- ✧ Separate self-modulation and acceleration
- ✧ Two plasmas
- ✧ External injection of e^- (on axis)

Muggli (AWAKE Coll.), J. of Phys.: Conf. Series 1596, 012008 (2020)

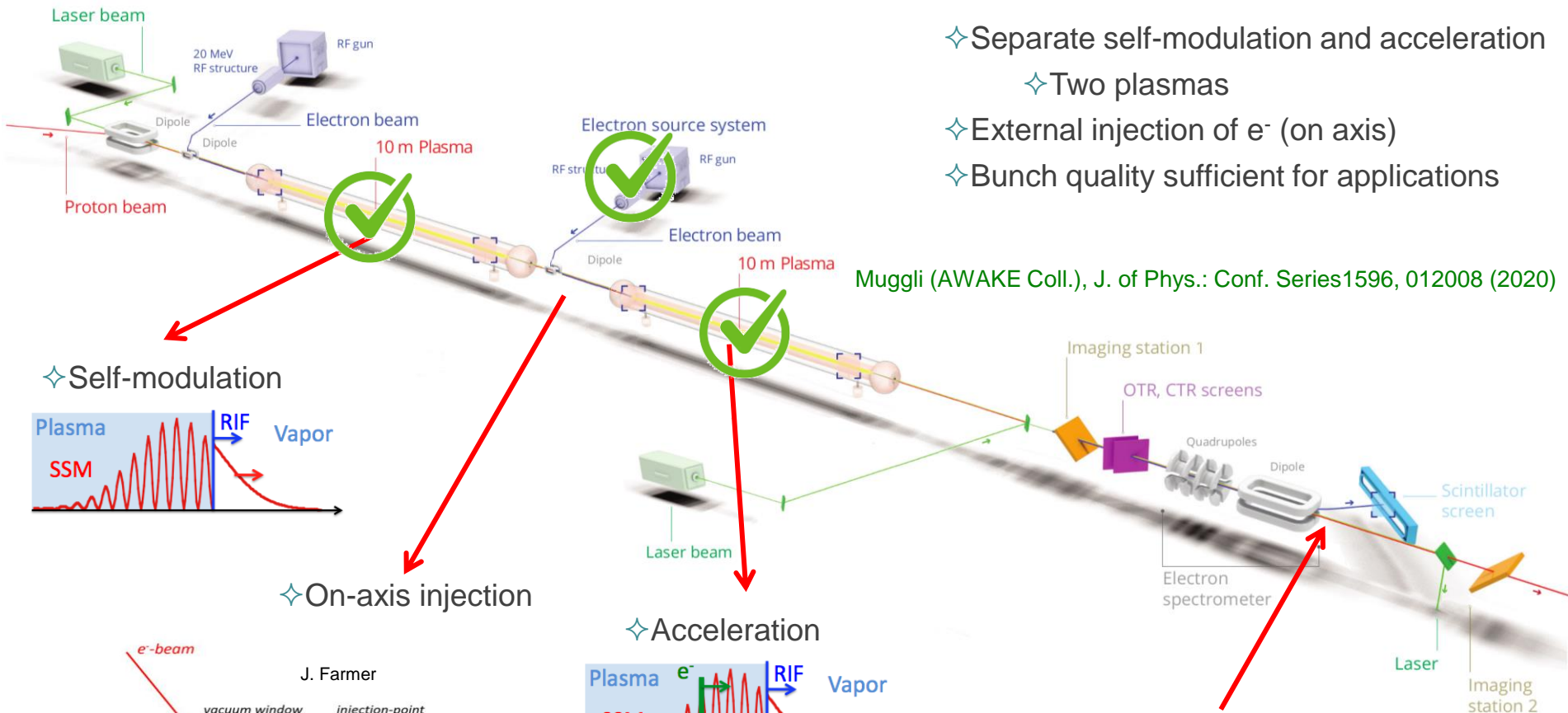


✧ Self-modulation

✧ On-axis injection



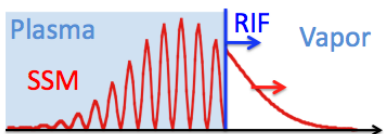
RUN 2c,d: ACCELERATE e^- BUNCH, QUALITY



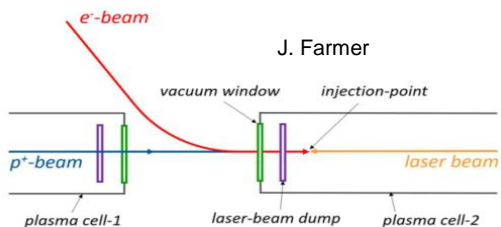
- ❖ Separate self-modulation and acceleration
- ❖ Two plasmas
- ❖ External injection of e^- (on axis)
- ❖ Bunch quality sufficient for applications

Muggli (AWAKE Coll.), J. of Phys.: Conf. Series 1596, 012008 (2020)

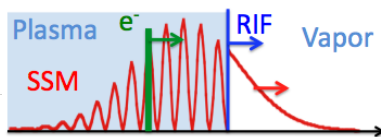
❖ Self-modulation



❖ On-axis injection

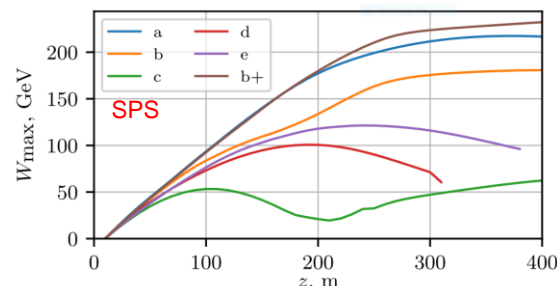
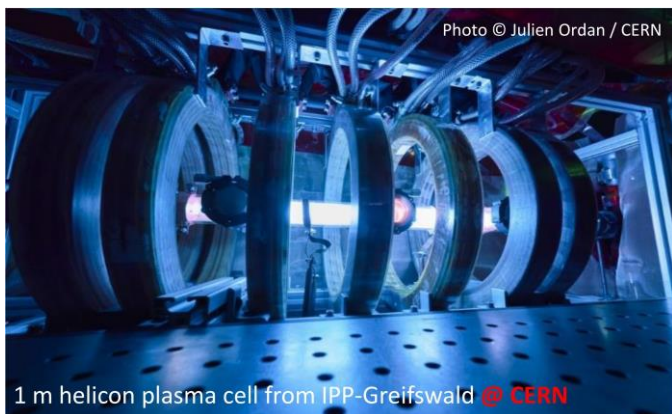


❖ Acceleration



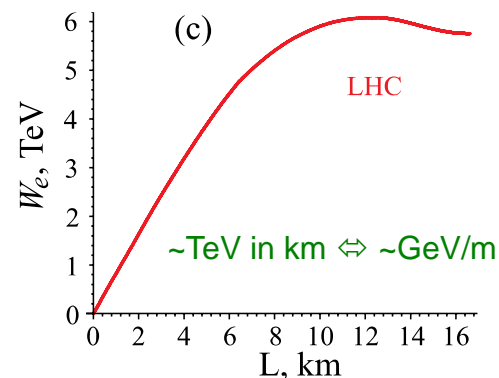
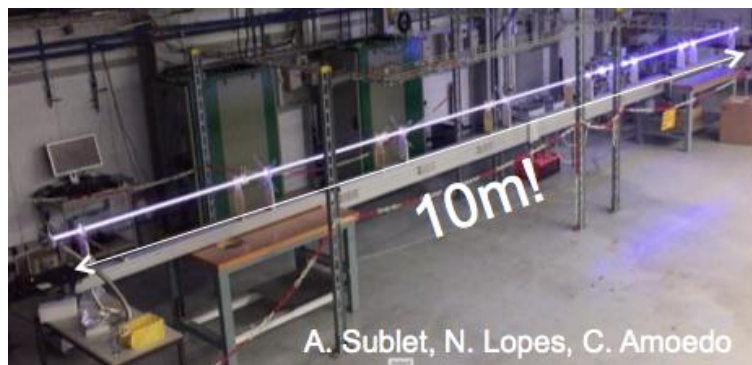
- ❖ Quality
- ❖ Particle Physics!

- ❖ Laser ionization does not scale to long plasma lengths (100m-1km): laser pulse energy depletion!
- ❖ Plasma source development laboratory at CERN
- ❖ Helicon source: magnetized RF discharge **Buttenschön, PFC 60(7), 075005 (2018)**



P. Tuv, K. V. Lotov, PFC 63, 125027 (2021)

- ❖ Pulsed discharge **Torrado, IEEE-TPS 51(12) (2023)**



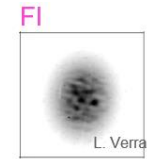
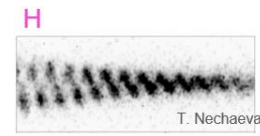
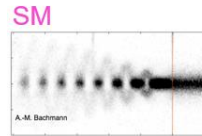
A. Caldwell, K. V. Lotov, Phys. Plasmas **18**, 13101 (2011)

- ❖ Challenge: plasma density uniformity!

$\Delta n_e/n_{e0} \ll 1/N_{ub}, N_{ub} \sim 100 \Rightarrow \Delta n_e/n_{e0} < 0.2\%$ P. Muggli, ECLIM, 16/09/2024

SUMMARY

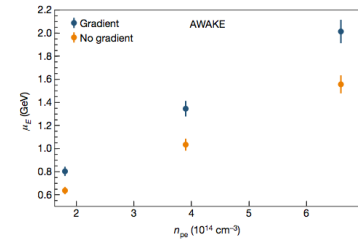
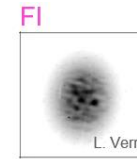
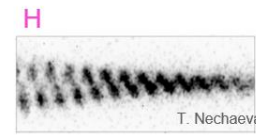
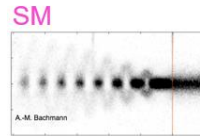
✧ Observed three instabilities, etc., etc.



SUMMARY

AWAKE:

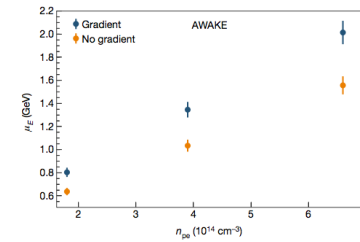
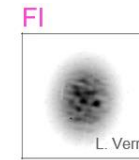
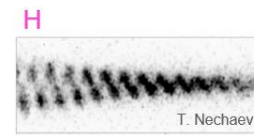
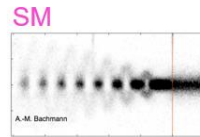
- Observed three instabilities, etc., etc.
- Seeded/controlled SM to accelerate e^- to GeV energy level



SUMMARY

AWAKE:

- Observed three instabilities, etc., etc.
- Seeded/controlled SM to accelerate e^- to GeV energy level
- Developing a self-modulator for a long p^+ bunch



SUMMARY

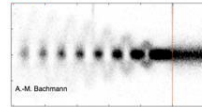
AWAKE:

- Observed three instabilities, etc., etc.
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- Clear plans for an accelerator: self-modulation, injection, acceleration

Large energy gain

Scalability to very large ..

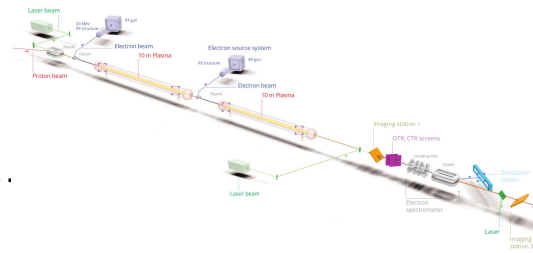
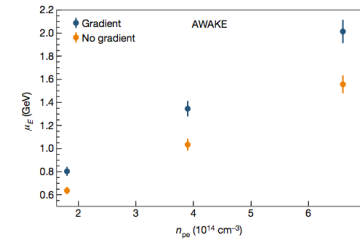
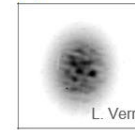
SM



H



FI

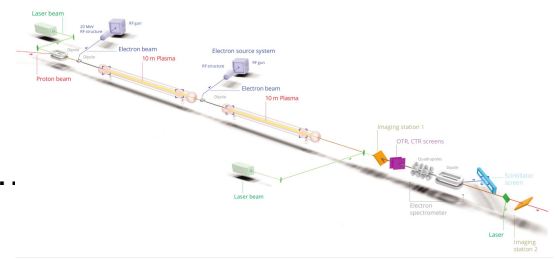
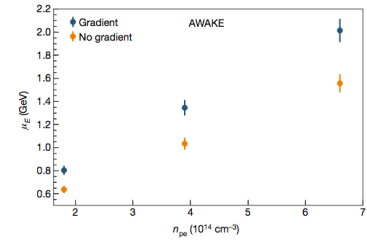
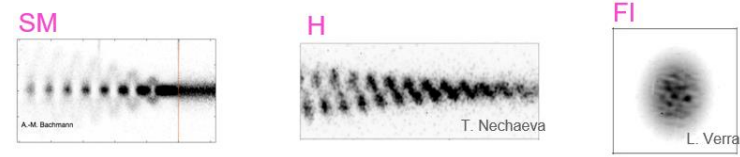


Muggli (AWAKE Coll.)
J. of Phys.: Conf. Series 1596, 012008 (2020).

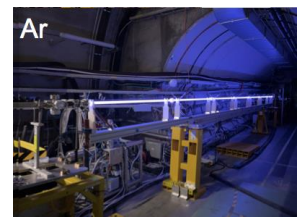
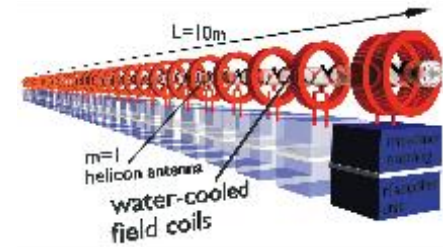
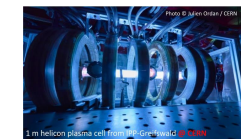
SUMMARY

AWAKE:

- Observed three instabilities, etc., etc.
- Seeded/controlled SM to accelerate e^- to GeV energy level
- Developing a self-modulator for a long p^+ bunch
- Clear plans for an accelerator: self-modulation, injection, acceleration
- Large energy gain
- Scalability to very large ..
- Development of scalable plasma sources



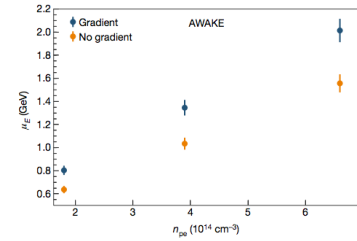
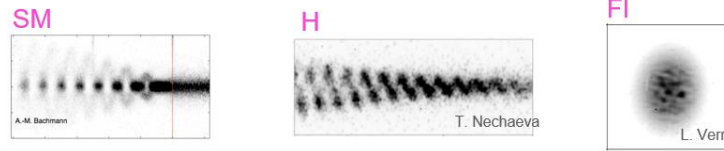
Muggli (AWAKE Coll.)
J. of Phys.: Conf. Series 1596, 012008 (2020).



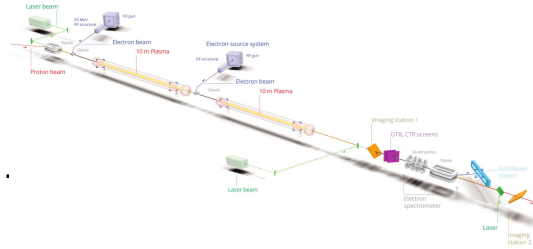
SUMMARY

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- Developing a self-modulator for a long p^+ bunch
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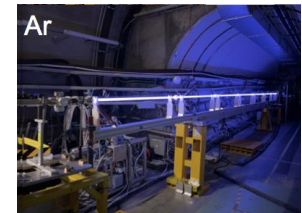
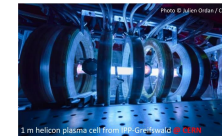
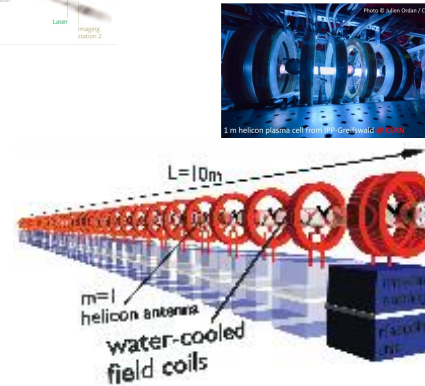


- Large energy gain
- Scalability to very large ..



Muggli (AWAKE Coll.)
J. of Phys.: Conf. Series 1596, 012008 (2020).

- Development of scalable plasma sources
- Propose particle physics experiments in the 2030's
- Dark photon search



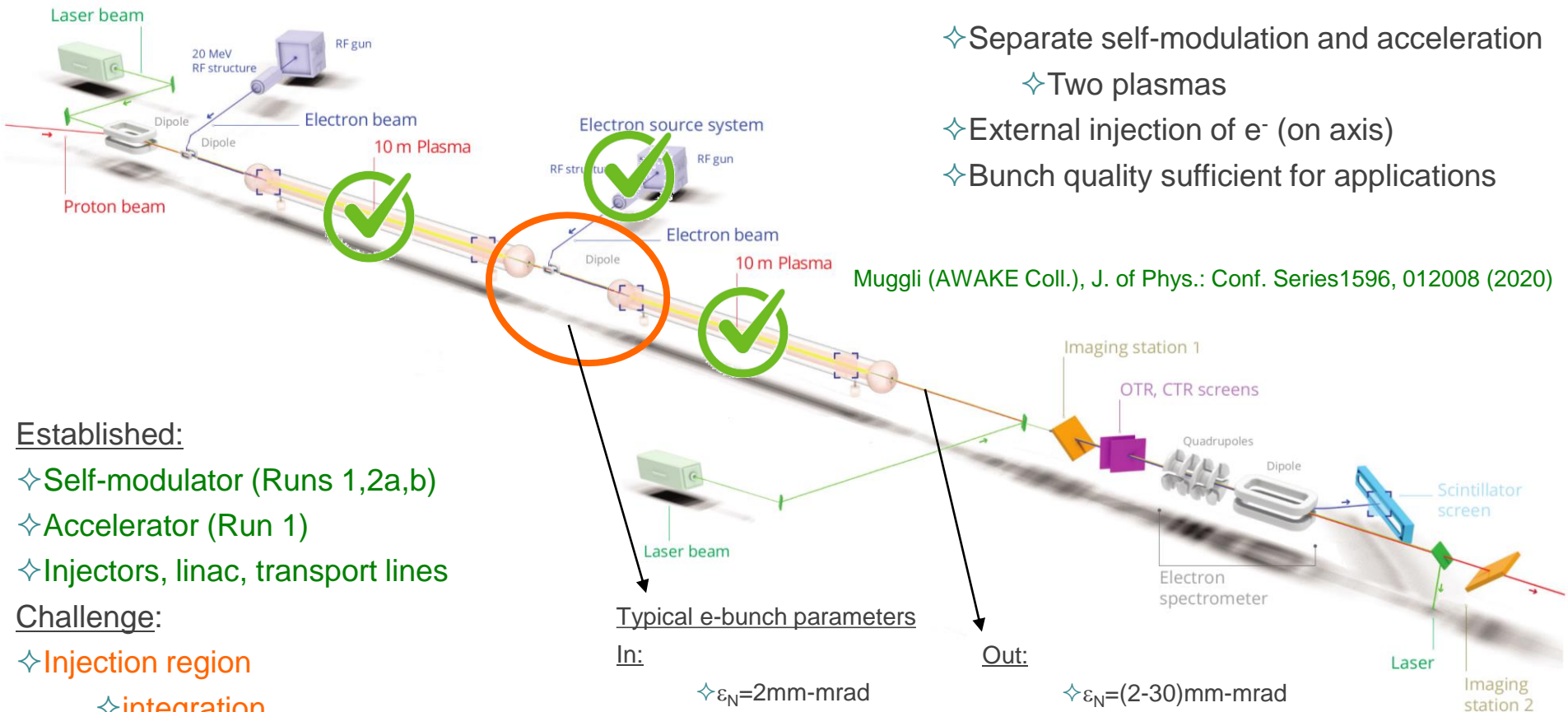
Thank you to my collaborators



Thank you!

<http://www.mpp.mpg.de/~muggli>

muggli@mpp.mpg.de



- ✧ Separate self-modulation and acceleration
- ✧ Two plasmas
- ✧ External injection of e⁻ (on axis)
- ✧ Bunch quality sufficient for applications

Established:

- ✧ Self-modulator (Runs 1,2a,b)
- ✧ Accelerator (Run 1)
- ✧ Injectors, linac, transport lines

Challenge:

- ✧ Injection region
 - ✧ integration
 - ✧ alignment, p⁺ and e⁻ beams
 - ✧ diagnostics

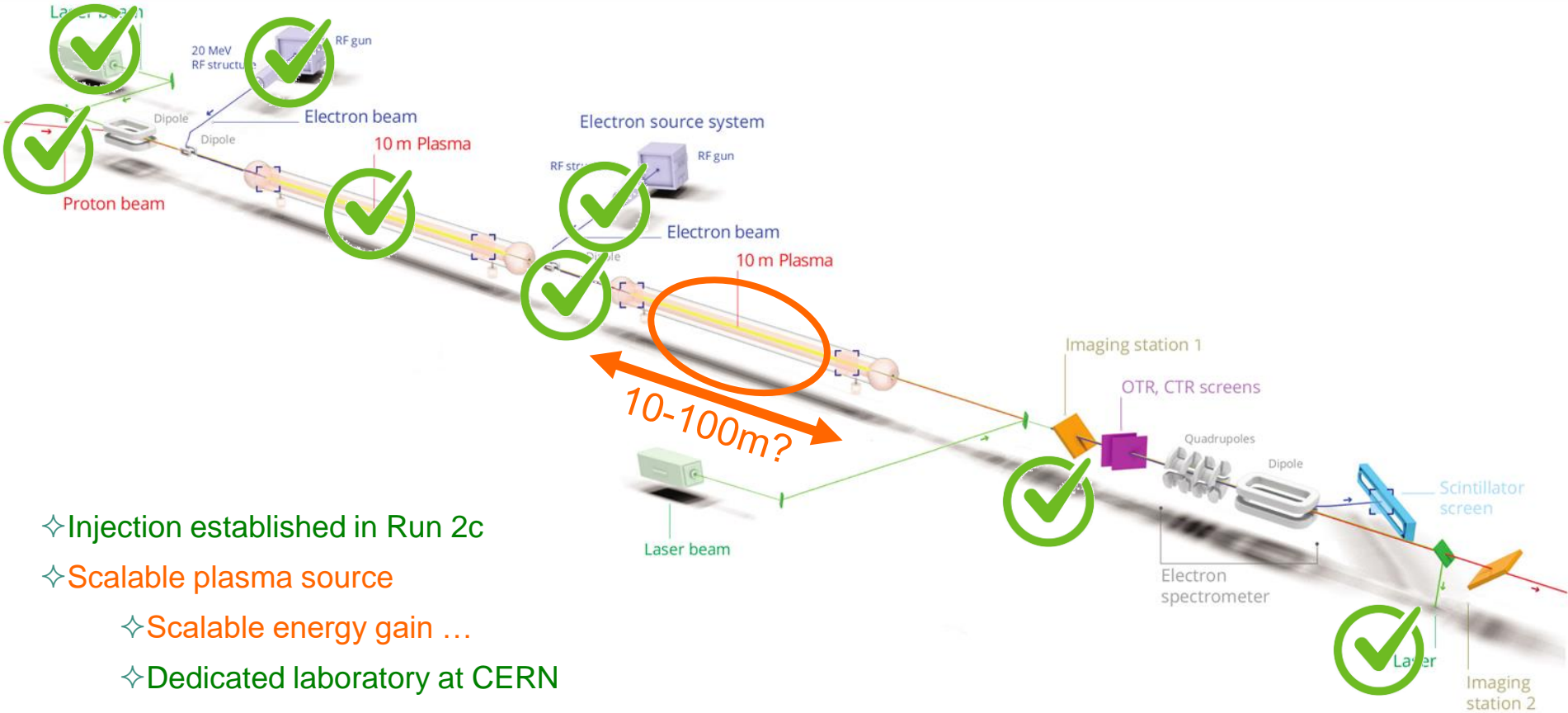
Typical e-bunch parameters

In:

- ✧ $\epsilon_N = 2 \text{ mm-mrad}$
- ✧ $Q = 100 \text{ pC}$, $N_e \sim 6 \times 10^9 e^-$
- ✧ 150 MeV
- ✧ $\sigma_t = 200 \text{ fs}$
- ✧ Jitter < 100 fs

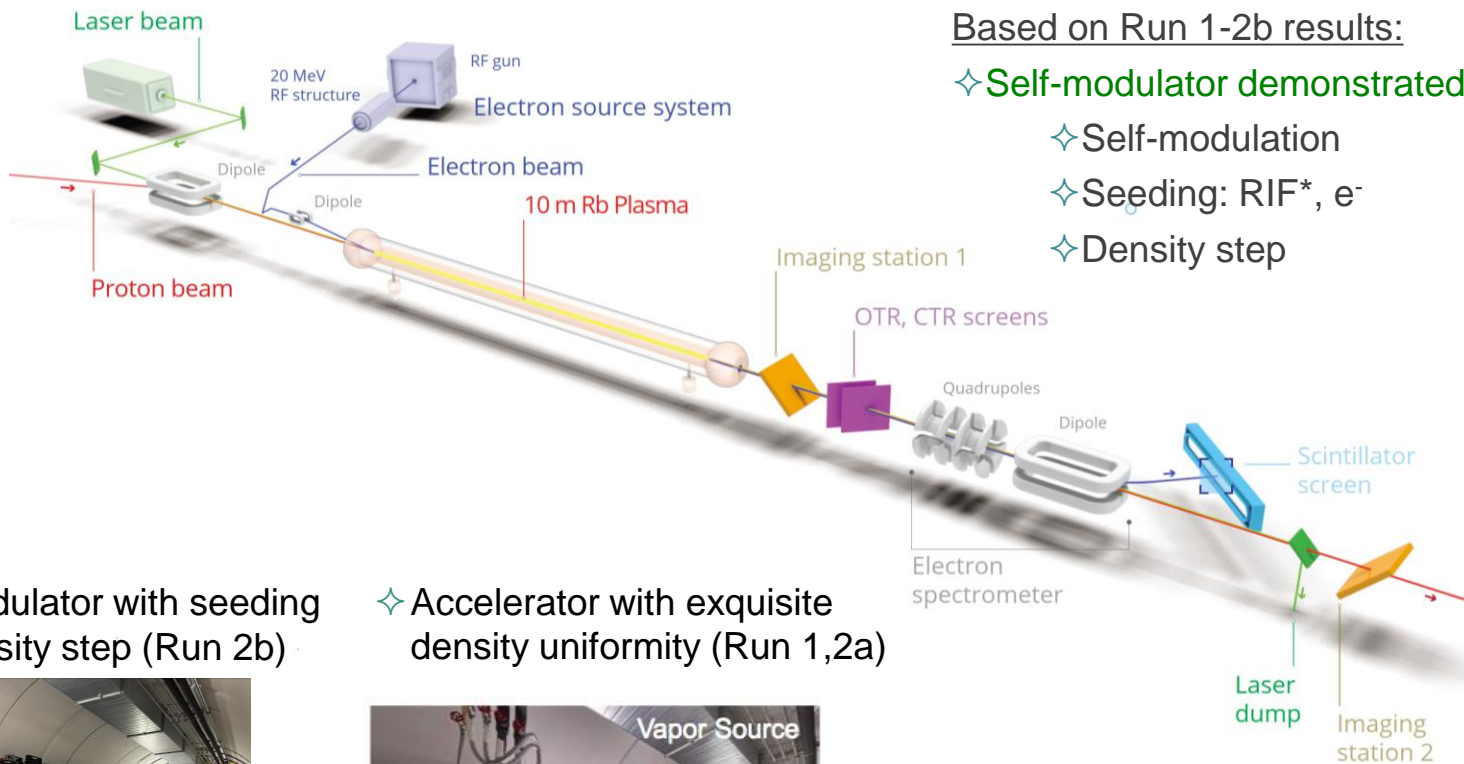
Out:

- ✧ $\epsilon_N = (2-30) \text{ mm-mrad}$
- ✧ $Q = 100 \text{ pC}$, $N_e \sim 6 \times 10^9 e^-$
- ✧ $\Delta E/E = 5-8\%$
- ✧ $E \sim 4-10^+ \text{ GeV}$



- ✧ Injection established in Run 2c
- ✧ Scalable plasma source
 - ✧ Scalable energy gain ...
- ✧ Dedicated laboratory at CERN

RUN 1,2a,b: SELF-MODULATOR FOR RUN 2c,d



Based on Run 1-2b results:

❖ Self-modulator demonstrated

❖ Self-modulation

❖ Seeding: RIF*, e⁻

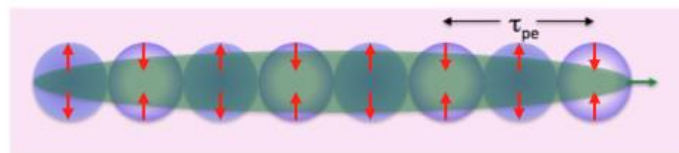
❖ Density step

❖ Self-modulator with seeding and density step (Run 2b)



❖ Accelerator with exquisite density uniformity (Run 1,2a)



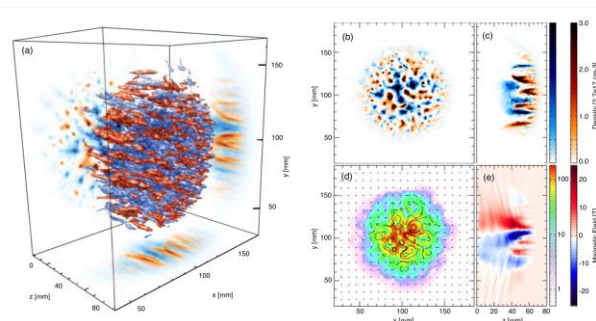


- ✧ $\sigma_{r0} < c/\omega_{pe}$: optimum for wakefield generation ...
- ✧ $\sigma_{r0} \gg c/\omega_{pe}$: filamentation instabilities can develop ...

- ✧ Equal streams: current filamentation instability (CFI)

- ✧ Unequal streams: oblique modes, wakefields, ...

$$\Gamma = \frac{\sqrt{3}}{2^{4/3}} \left(\frac{n_{b0} m_e}{n_{pe} m_p \gamma_p} \right)^{1/3} \omega_{pe} = \Gamma_e \left(\frac{m_e}{m_p} \right)^{1/3} \quad \vec{k} = \vec{k}_{\perp} + \vec{k}_{\parallel}$$



- ✧ Astrophysics: generation of magnetic fields in the universe?
- ✧ Collision: neutral, expanding supernova plasma – interstellar plasma
- ✧ CFI :

- ✧ Generates magnetic fields

- ✧ Converts kinetic energy of the expanding plasma into B-field energy and plasma kinetic energy

- ✧ Evolution: filaments -> coalescence -> shock formation

- ✧ Study FI with relativistic particle bunch (p^+)

- ✧ “Astrophysics in the lab”



Core-collapse, or Type II supernovas, are caused by the implosion of massive stars like red supergiants. (Supplied by ESA/Hubble/C. Cocchi)

Shukla, J. Plasma Phys. 84(3) 905840302 (2018)
Allen, Phys. Rev. Lett. 109, 185007 (2012)