

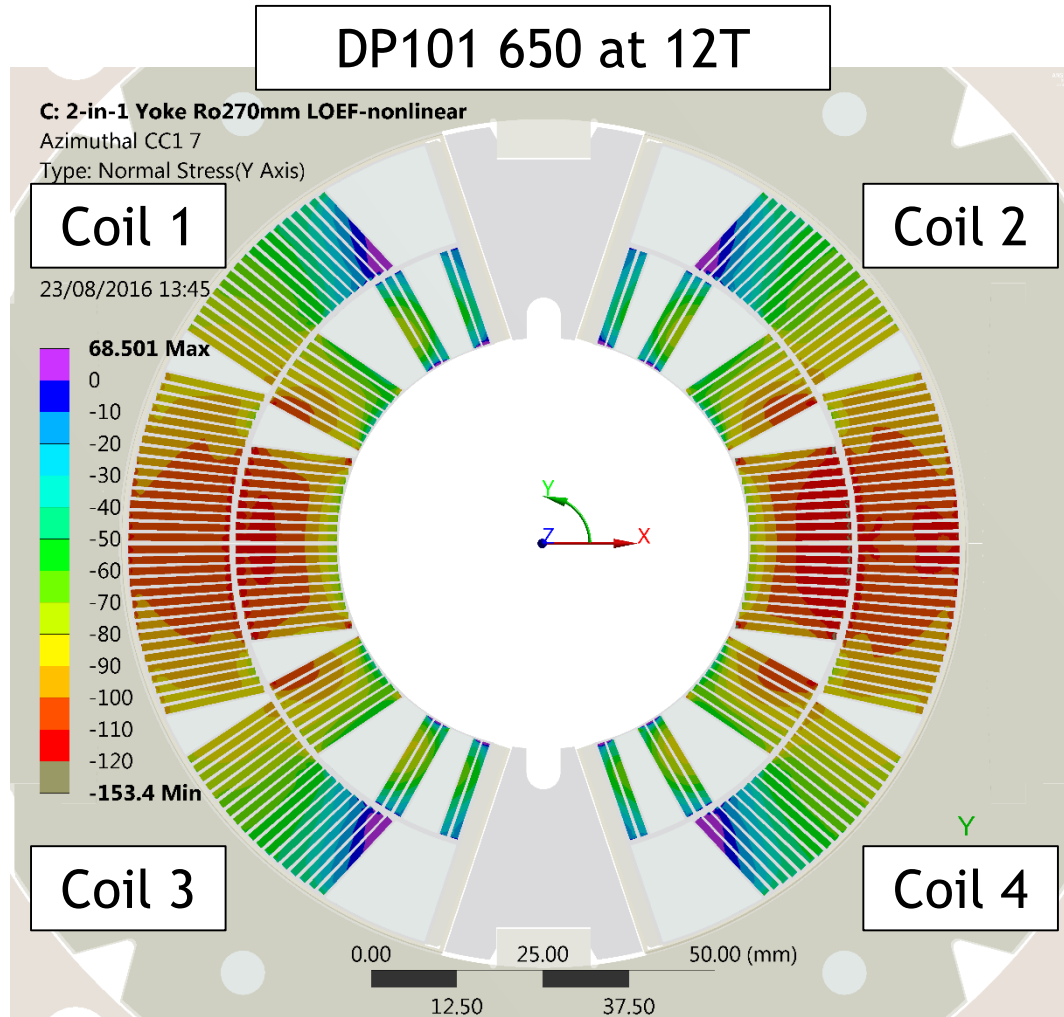
MBHSP104 - Stress analysis – Focus on mid-plane stresses

Christian Löffler 23-08-2016

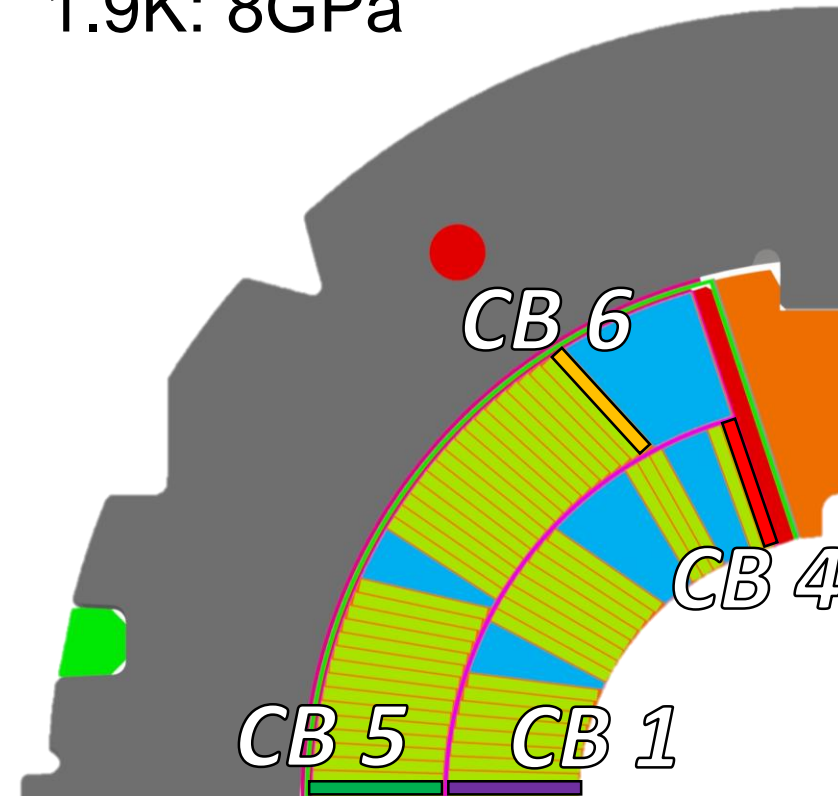
SP104 –midplane mechanics

- The stress on the collars and the bullet gauges had been discussed in the previous debriefing
- Bullet gauges behave very similar to previous models
- Strain Gauges on the collars show 25% more stress in the collared coil

Midplane stresses

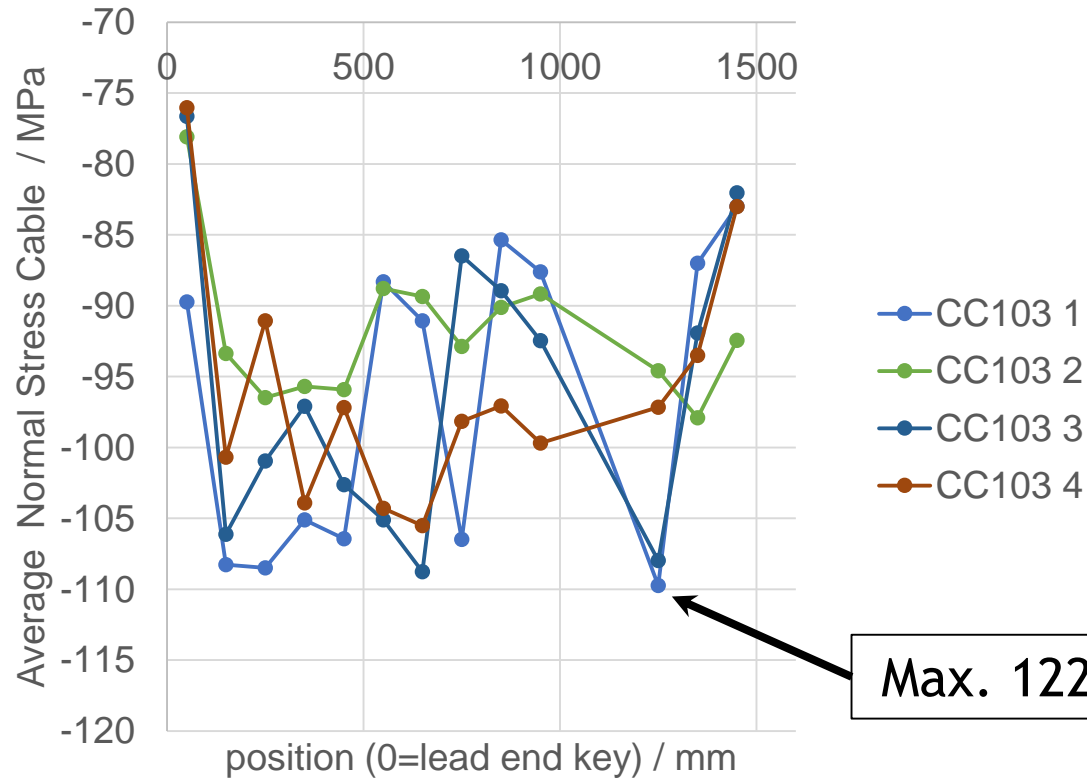


- Stresses will be shown as an average over one full cable
- Cable RT: 129GPa;
1.9K: 104GPa [2]
- Insulation RT: 6GPa;
1.9K: 8GPa

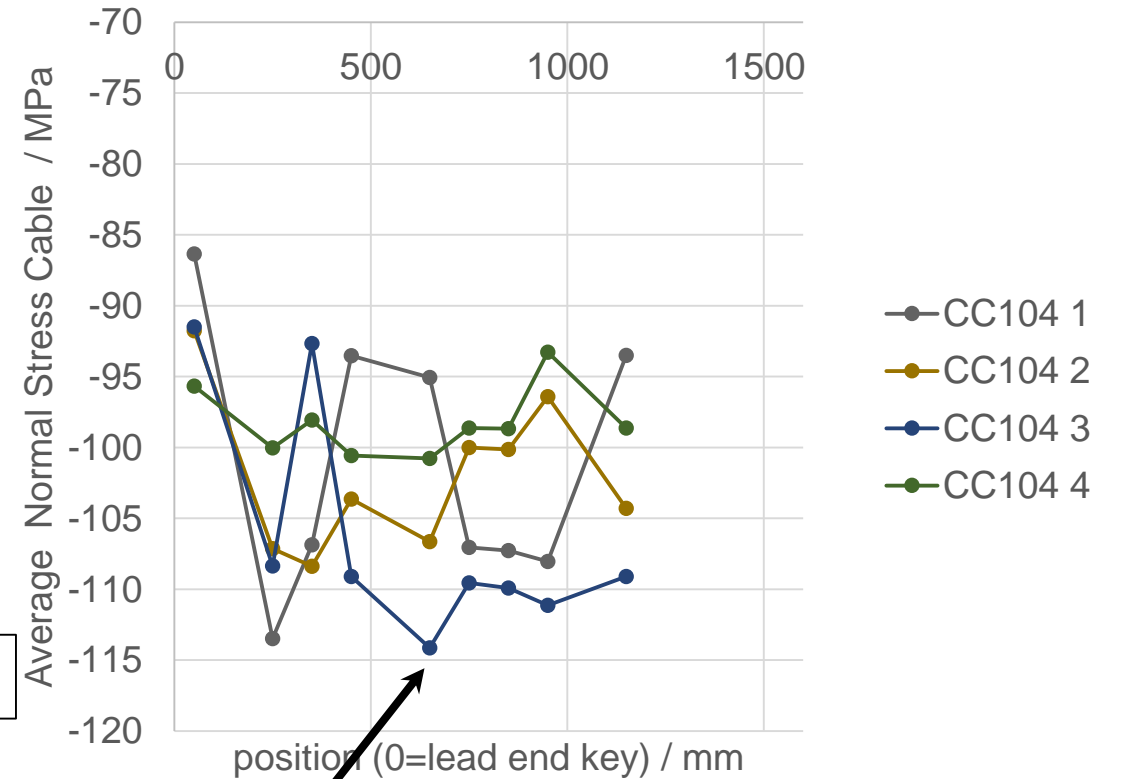


Midplane stresses at 12T / average over midplane cable CB1

Average stress midplane cable coil block 1 ,
SP103

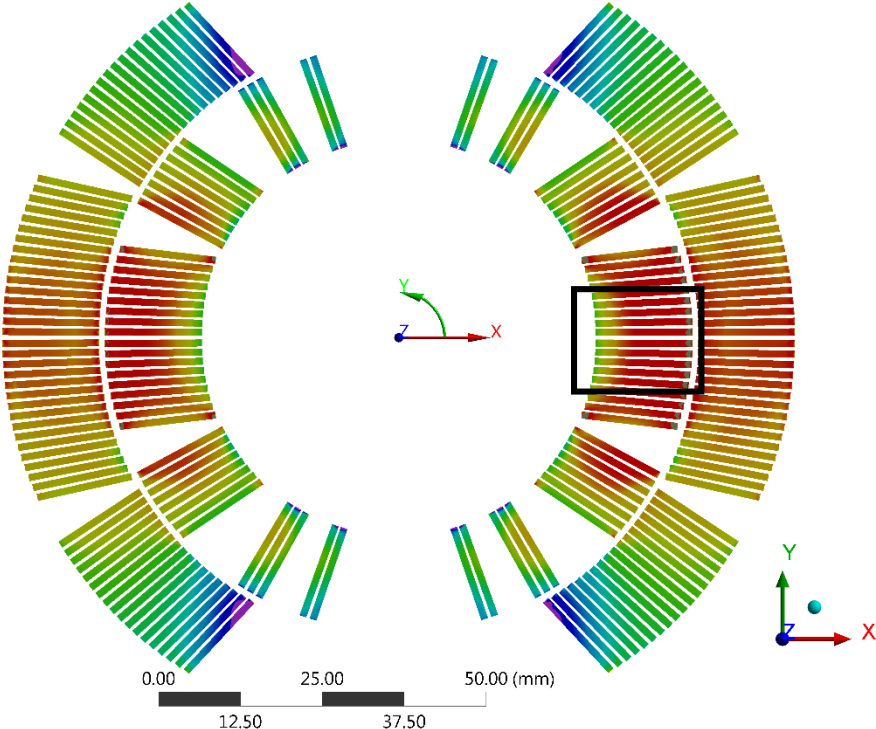
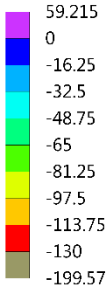


Average stress midplane cable coil block 1 ,
SP104

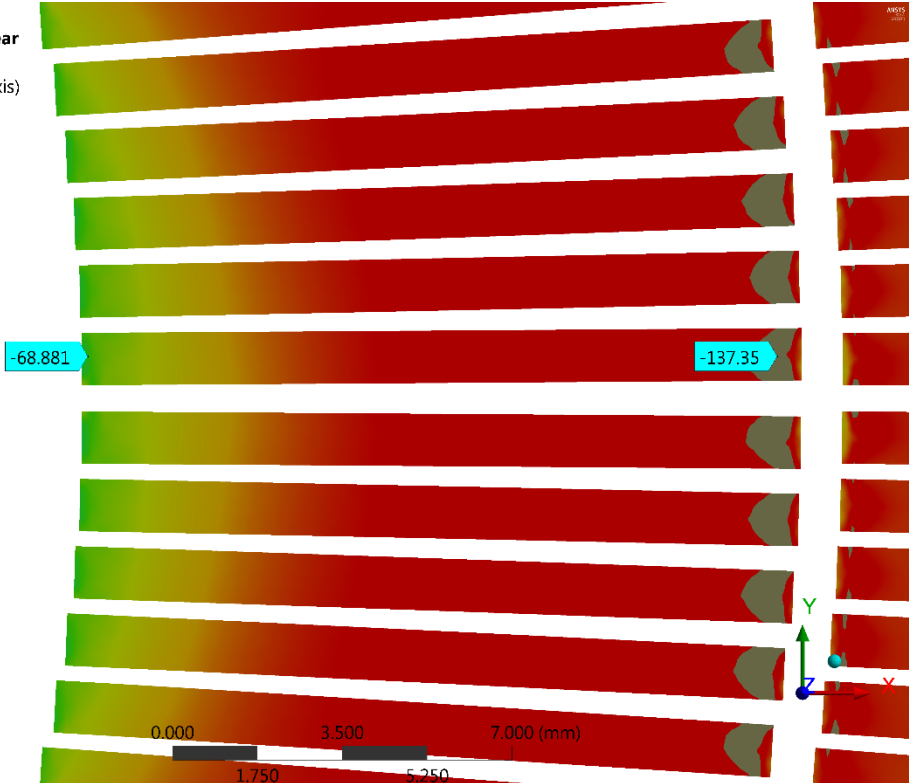
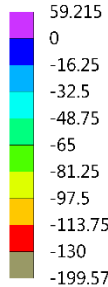


SP104 z=650mm at 12T

C: DS11T-1in1-non-linear
 Azimuthal Y-Stress-12T
 Type: Normal Stress(Y Axis)
 Unit: MPa
 Cylindrical system
 Time: 7
 Custom
 Max: 59.215
 Min: -199.57
 24/08/2016 08:27



C: DS11T-1in1-non-linear
 Azimuthal Y-Stress-12T
 Type: Normal Stress(Y Axis)
 Unit: MPa
 Cylindrical system
 Time: 7
 Custom Obsolete
 Max: 59.215
 Min: -199.57
 24/08/2016 08:35



Applying the scaling law from Bernardo

$$I_1 = \varepsilon_1 + \varepsilon_2 + \varepsilon_3$$

$$J_2 = \frac{1}{6}[(\varepsilon_1 - \varepsilon_2)^2 + (\varepsilon_2 - \varepsilon_3)^2 + (\varepsilon_3 - \varepsilon_1)^2]$$

$$s(\boldsymbol{\varepsilon}) = \frac{e^{-C_1 \frac{J_2+3}{J_2+1} J_2} + e^{-C_1 \frac{I_1^2+3}{I_1^2+1} I_1^2}}{2}$$

$$s(\boldsymbol{\varepsilon}) \equiv \frac{B_{c2}(0, \boldsymbol{\varepsilon})}{B_{c2}(0, 0)}$$

Assumption:

$$C_1 = 0.875$$

From:

An exponential scaling law for the strain dependence of the Nb 3 Sn critical current density, B Bordini and P Alknes and L Bottura and L Rossi and D Valentinis, Superconductor Science and Technology 2013

SP104 z=650mm at 12T

C: DS11T-1in1-non-linear

$$S_e = (e^{(-C1*J2*((J2+3)/(J2+1)))} + e^{(-C1*I1^2*((I1^2+3)/(I1^2+1)))})/2 - 7. s^2$$

$$\text{Expression: } (e^{(-C1*J2*((J2+3)/(J2+1)))} + e^{(-C1*I1^2*((I1^2+3)/(I1^2+1)))})/2$$

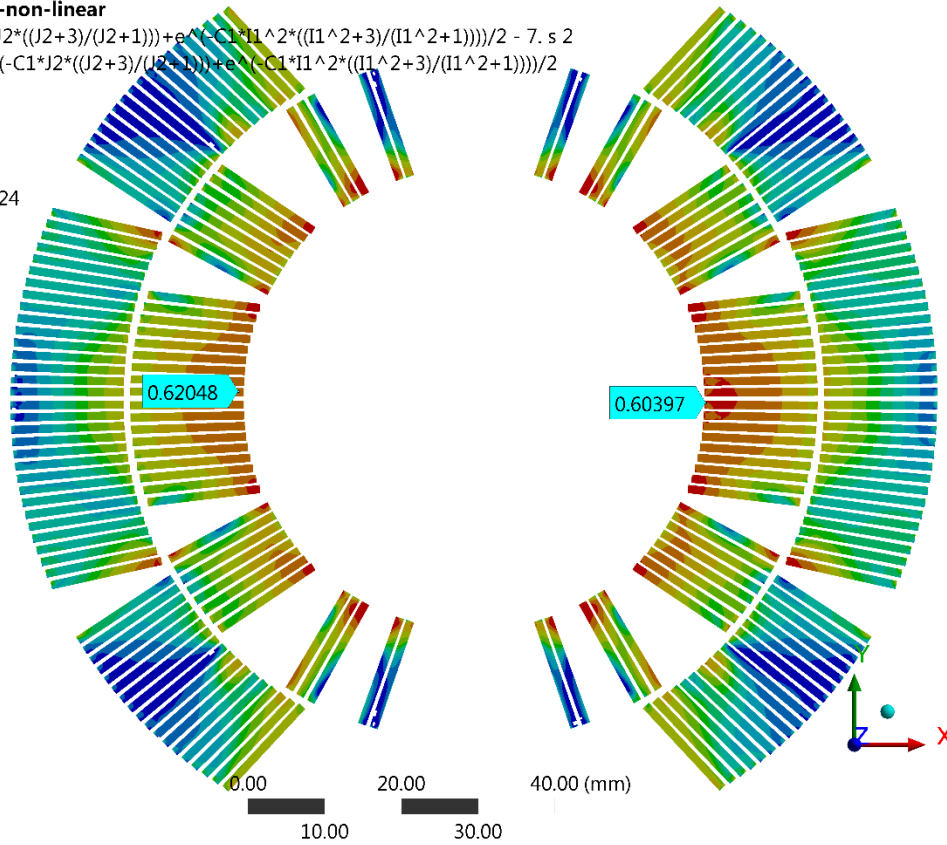
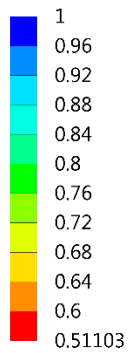
Unit: mm/mm

Time: 7

Max: 0.99829

Min: 0.51103

23/08/2016 17:24



C: DS11T-1in1-non-linear

Equivalent Total Strain - Coil - 7. s

Type: Equivalent Total Strain

Unit: mm/mm

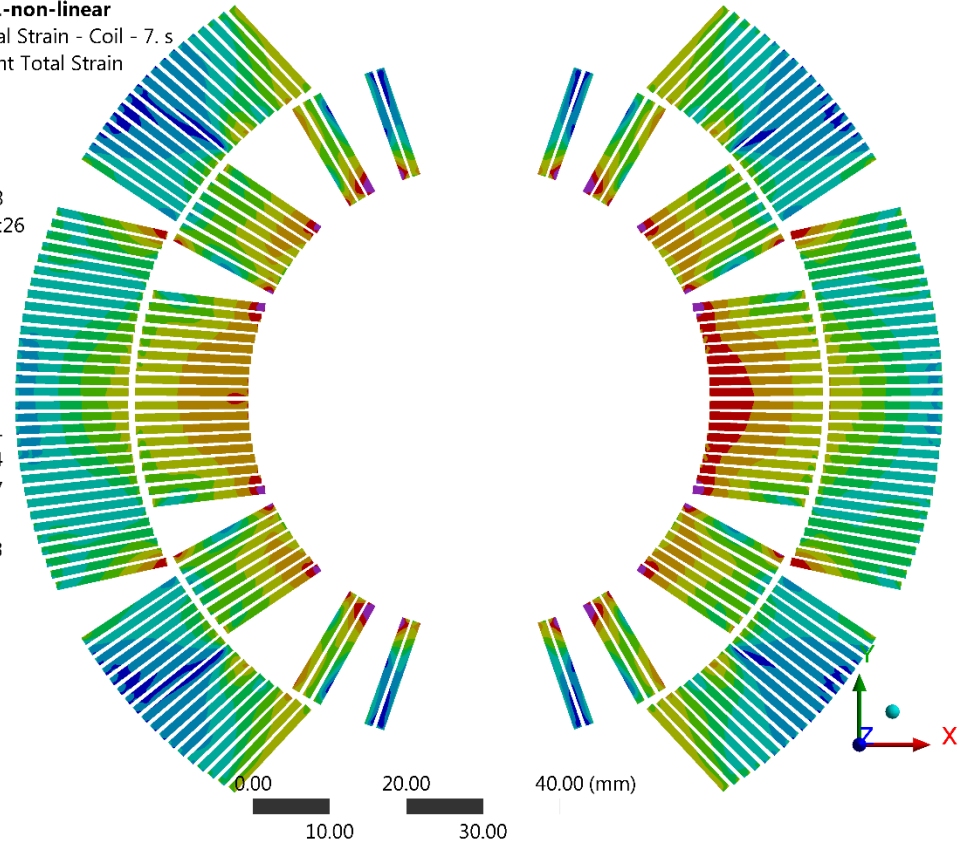
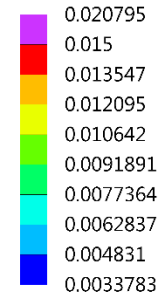
Time: 7

Custom

Max: 0.020795

Min: 0.0033783

23/08/2016 17:26



$S(\epsilon)$

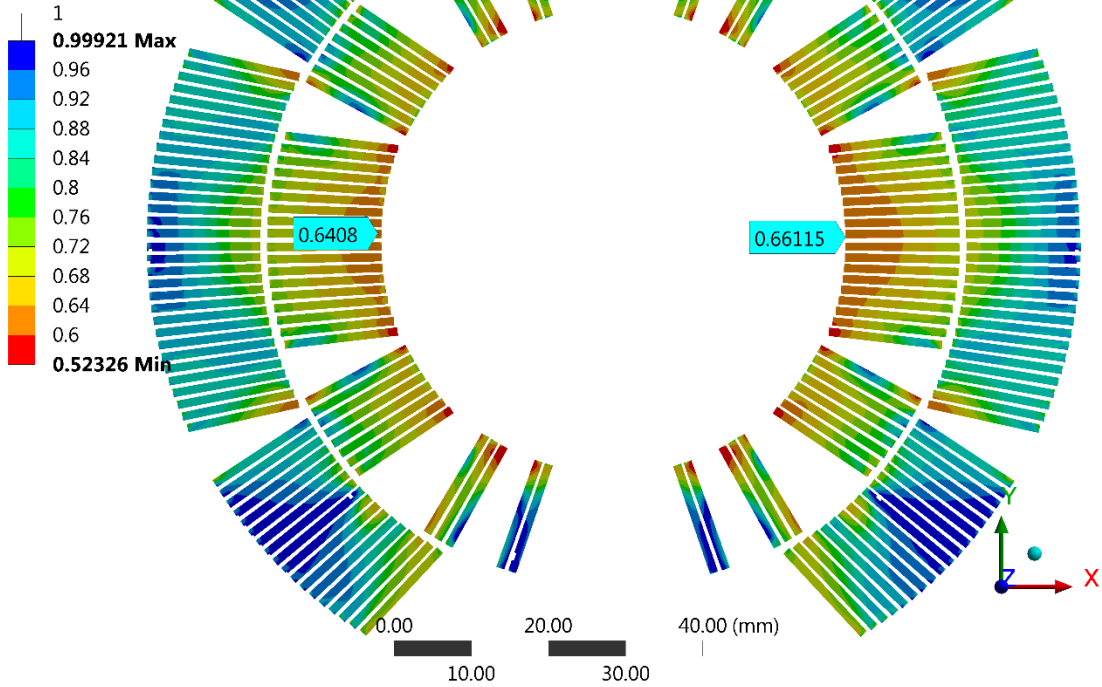
Equivalent Total Strain



SP103 z=650mm at 12T

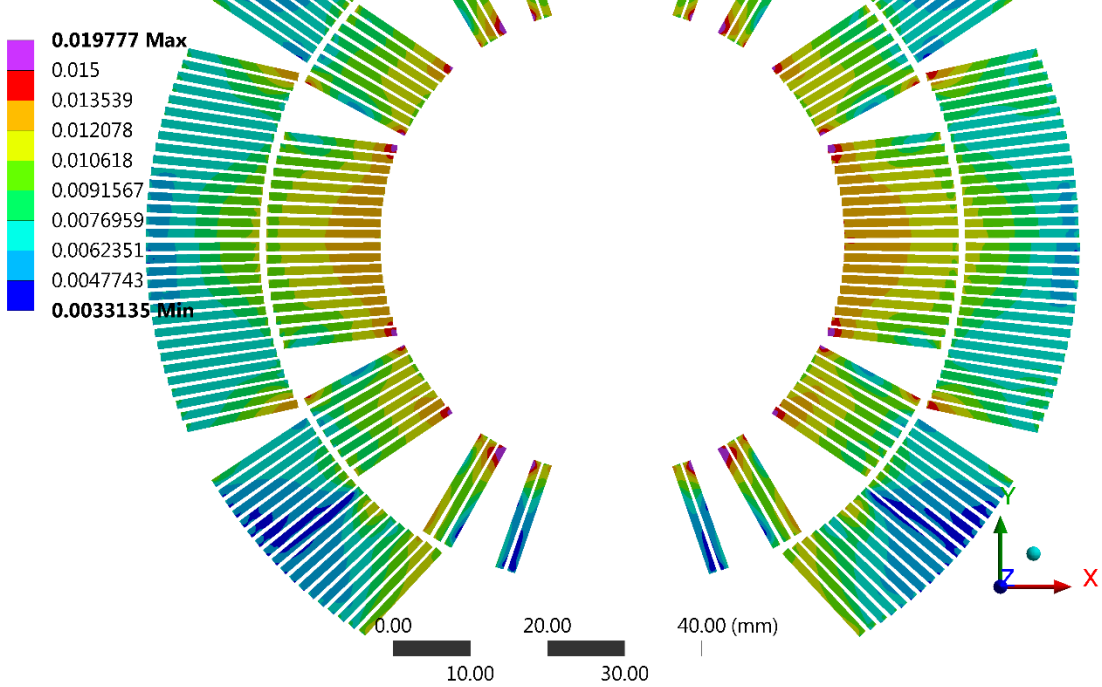
C: DS11T-1in1-non-linear

$S_e = (e^{(-C1 \cdot J2 \cdot ((J2+3)/(J2+1)))} + e^{(-C1 \cdot I1^2 \cdot ((I1^2+3)/(I1^2+1)))})/2 - 7. s$
 Expression: $S_e = (e^{(-C1 \cdot J2 \cdot ((J2+3)/(J2+1)))} + e^{(-C1 \cdot I1^2 \cdot ((I1^2+3)/(I1^2+1)))})/2$
 Unit: mm/mm
 Time: 7
 23/08/2016 17:50



C: DS11T-1in1-non-linear

Equivalent Total Strain - Coil - 7. s
 Type: Equivalent Total Strain
 Unit: mm/mm
 Time: 7
 23/08/2016 17:51

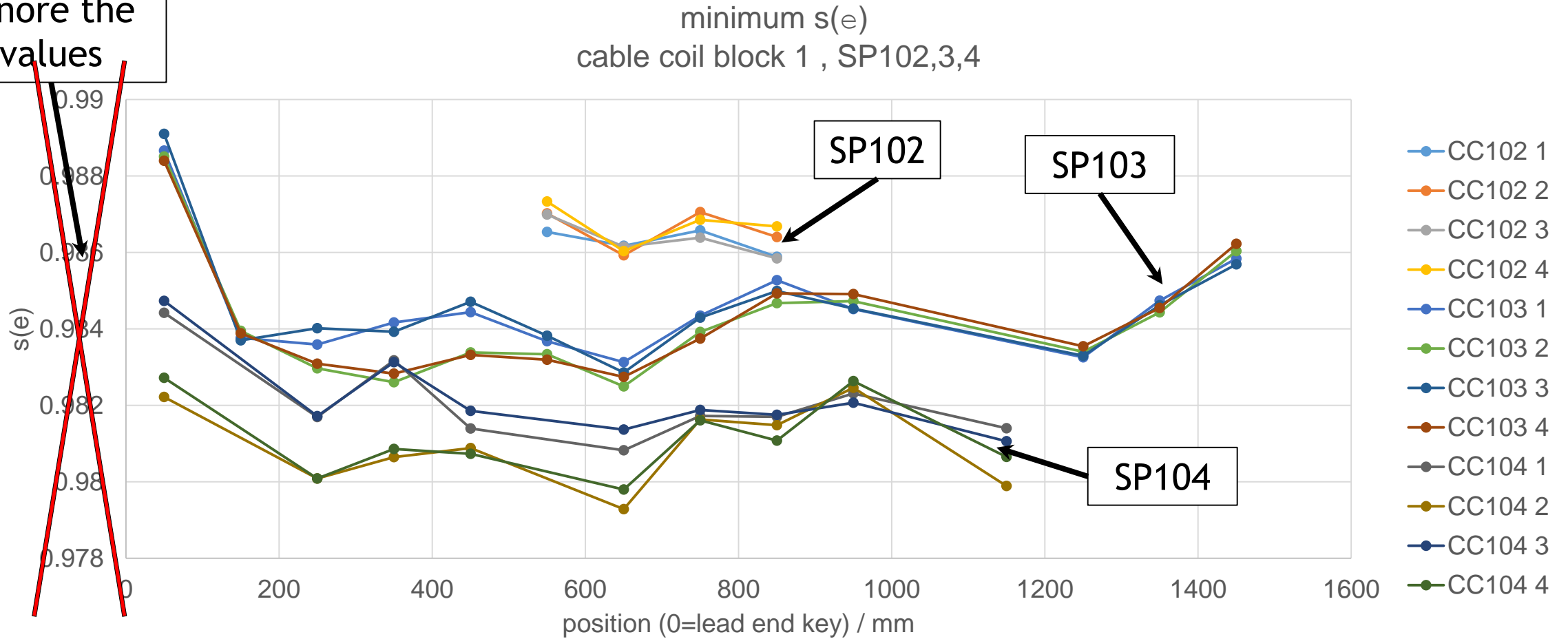


$S(\epsilon)$

Equivalent Total Strain

Scaling law on midplane cable – plot only qualitative

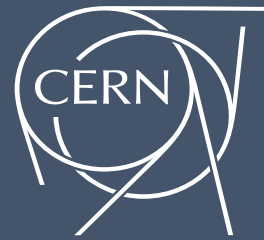
Ignore the values



Comparing SP103 and SP104

- The Maximum $s(e)$ for SP103 is **0.64** at the midplane
- For SP104 it is **0.6**
- Applying the scaling law to a full magnet model is a rather new method
- The cable is modeled as a smeared property of Nb3Sn and Copper, material data is based on [2]
Elastic Anisotropy in Multifilament Nb3Sn Superconducting Wires

C. Scheuerlein, B. Fedelich, P. Alknes, G. Arnau, R. Bjoerstad, and B. Bordini



Stress in collars after test

- SP102 = -111MPa
 - SP103 = -116MPa
 - SP104 = -165MPa
- Also after the cold-test SP104 is the model with the most pre-stress in the collar

[1] material

Table 2.2. Properties of the different spring materials and of a typical Nb₃Sn wire.

Material	Thermal expansion 293–4 K (%)	Young's modulus at 4 K [293 K] (GPa)	Poisson's ratio at 4 K [293 K]	Elastic limit at 4 K [293 K] (%)
Titanium -4Al-6V	-0.174 ^a	130 ^b [110]	[0.31] ^b	1.3 ^c [1.0] ^d
Copper-beryllium (TH04)	-0.317 ^a	132 [119] ^e	[0.27] ^b	1.0 [0.9] ^c
Brass (C27200)	-0.370 ^e	[105] ^f	[0.34] ^f	[0.4] ^f
Stainless steel 316L	-0.300 ^a	208 ^a [193] ^f	0.28 [0.29] ^g	[0.1] ^f
Nb ₃ Sn wire	-0.28 ^{g,h}	25–100 ^{g,i}	—	~0 [~0] ^g
Copper	-0.334 ^g	137 [128] ^g	[0.31] ^f	0.04 [0.02] ^g
Nb ₃ Sn	-0.16 ^j	100 [135] ^g	0.4 ^j	—

^a Reference⁵⁵. Stainless steel data is for type 316.

^b Reference⁵⁶. Cryogenic data for Ti-6Al-4V at 20 K.

^c Reference¹⁹.

^d Reference⁴².

^e Reference⁵⁷. 70/30 Brass (C26000).

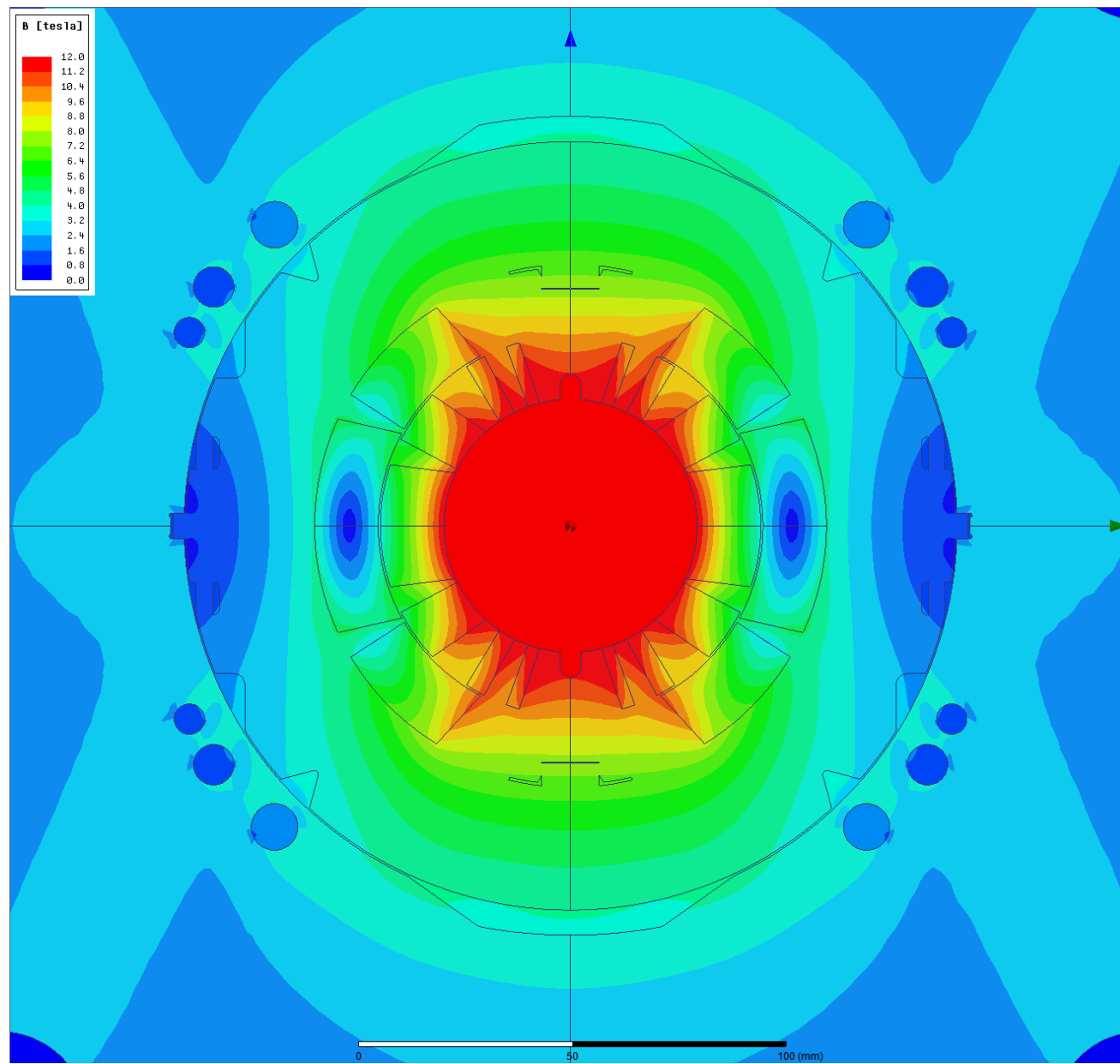
^f Reference⁵⁸.

^g Reference⁵⁹. Stainless steel data is for type 316LN.

^h Reference⁶⁰. Vacuumschmelze bronze-route wire.

ⁱ Reference⁶¹. A range of tangent modulus values are shown for the Nb₃Sn wire (which behaves plastically). Similar at 293 and 7 K.

^j Reference²².



1in1 12.8kA

- [1] Critical current measurements of TFMC-LMI and CSMC-VAC Nb₃Sn—measurements, FEA corrections and the scaling law parameterisation
 - DMJ Taylor, P Foley, HJ Niu and DP Hampshire
- [2] Elastic Anisotropy in Multifilament Nb₃Sn Superconducting Wires
 - C. Scheuerlein, B. Fedelich, P. Alknes, G. Arnau, R. Bjoerstad, and B. Bordini