



Introduction to Particle Accelerators

Pedro F. Tavares – MAX IV Laboratory

CAS – Vacuum for Particle Accelerators
Örenäs Slott – Glumslöv, Sweden June 2017

Introduction to Particle Accelerators

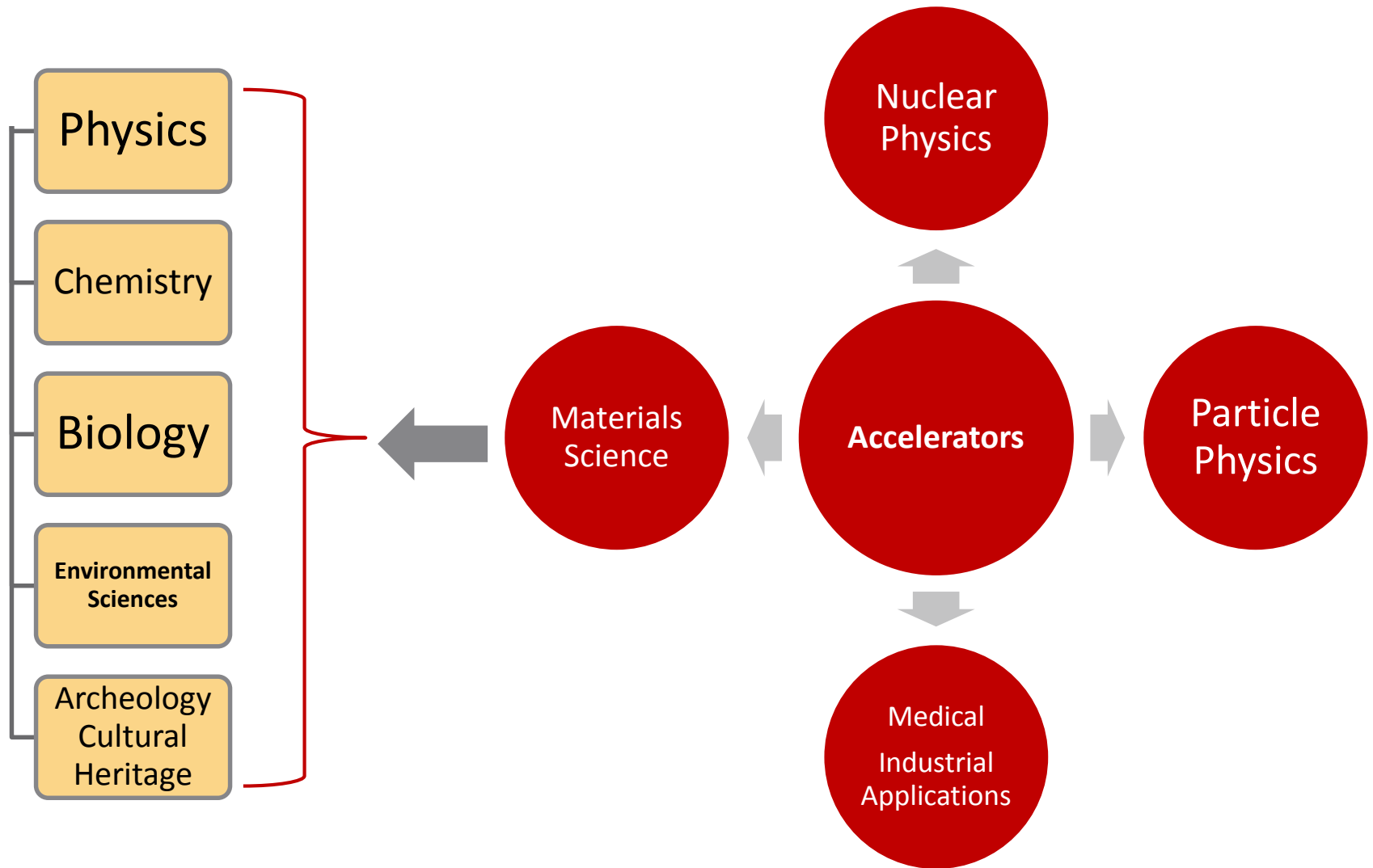
- ❑ Pre-requisites: classical mechanics & electromagnetism + matrix algebra at the undergraduate level.
- ❑ No specific knowledge of accelerators assumed.
- ❑ Objectives
 - Provide motivations for developing and building particle accelerators
 - Describe the basic building blocks of a particle accelerator
 - Describe the basic concepts and tools needed to understand how the vacuum system affects accelerator performance.

Caveat: I will focus the discussion/examples on one type of accelerator, but most of the discussion can be translated into other accelerator models.

Outlook

- Why Particle Accelerators ?
 - Why Synchrotron Light Sources ?
- Storage Ring Light Sources: *accelerator building blocks*
- Basic Beam Dynamics in Storage Rings.
 - Transverse dynamics: twiss parameters, betatron functions and tunes, chromaticity.
 - Longitudinal dynamics: RF acceleration, synchrotron tune
 - Synchrotron light emission, radiation damping and emittance
- How vacuum affects accelerator performance.

Why Particle Accelerators ?



Beams for Materials Research

Photon
Sources

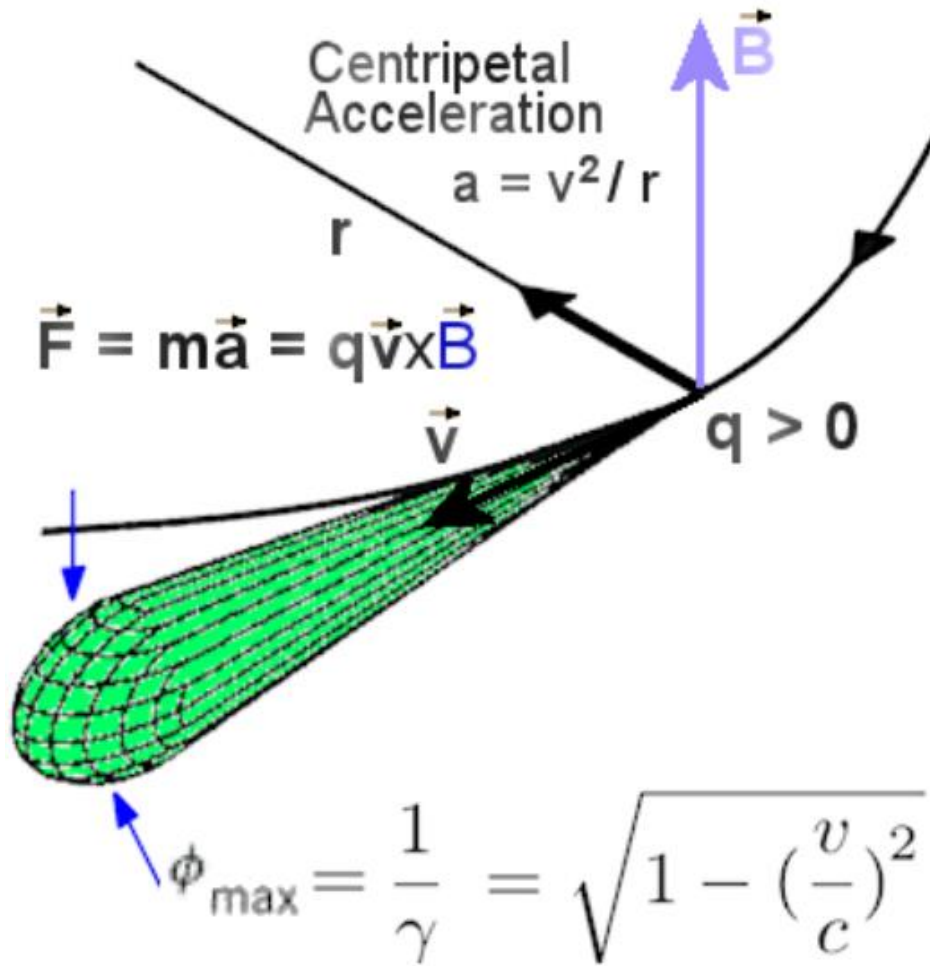
Neutron
Sources

MAX IV



ESS

What is Synchrotron Light ?



Properties:

Wide band

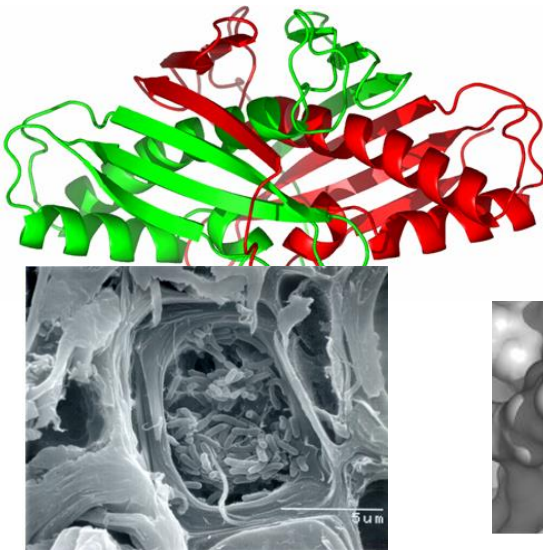
High intensity/Brightness

Polarization

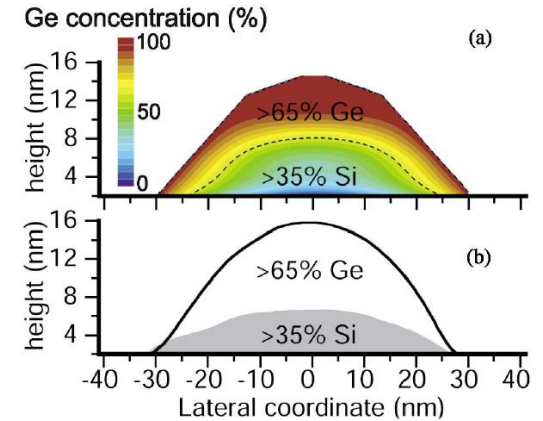
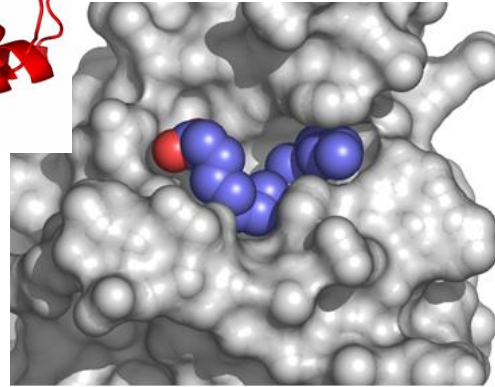
Time structure

Picture: <https://universe-review.ca/I13-15-pattern.png>

Why Synchrotron Light ?



A. Malachias et al, *3D Composition of Epitaxial Nanocrystals by Anomalous X-Ray Diffraction*, PRL **99**, 17 (2003)



OLIVEIRA, M. A. et al. *Crystallization and preliminary X-ray diffraction analysis of an oxidized state of Ohr from Xylella fastidiosa*. Acta Crystallographica. Section D, Biological Crystallography, v. D60, p. 337-339, 2004

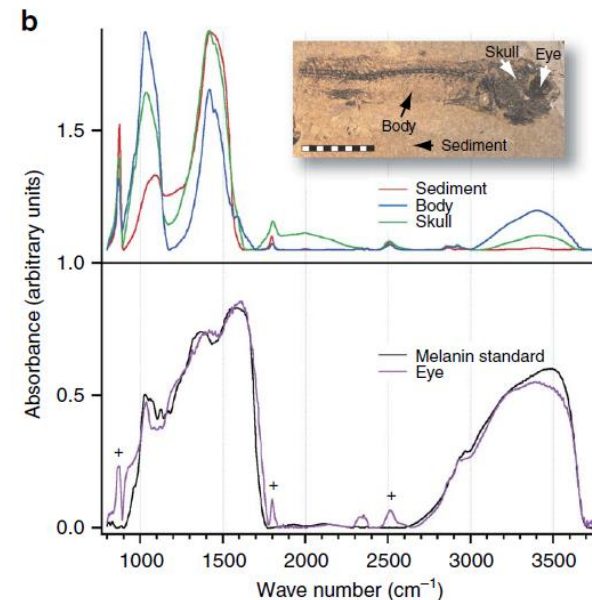
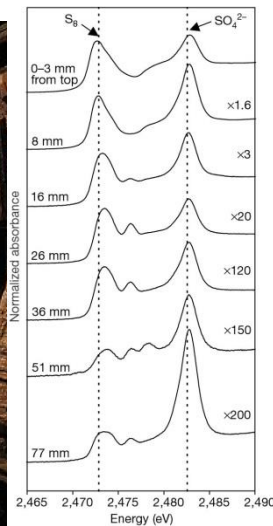


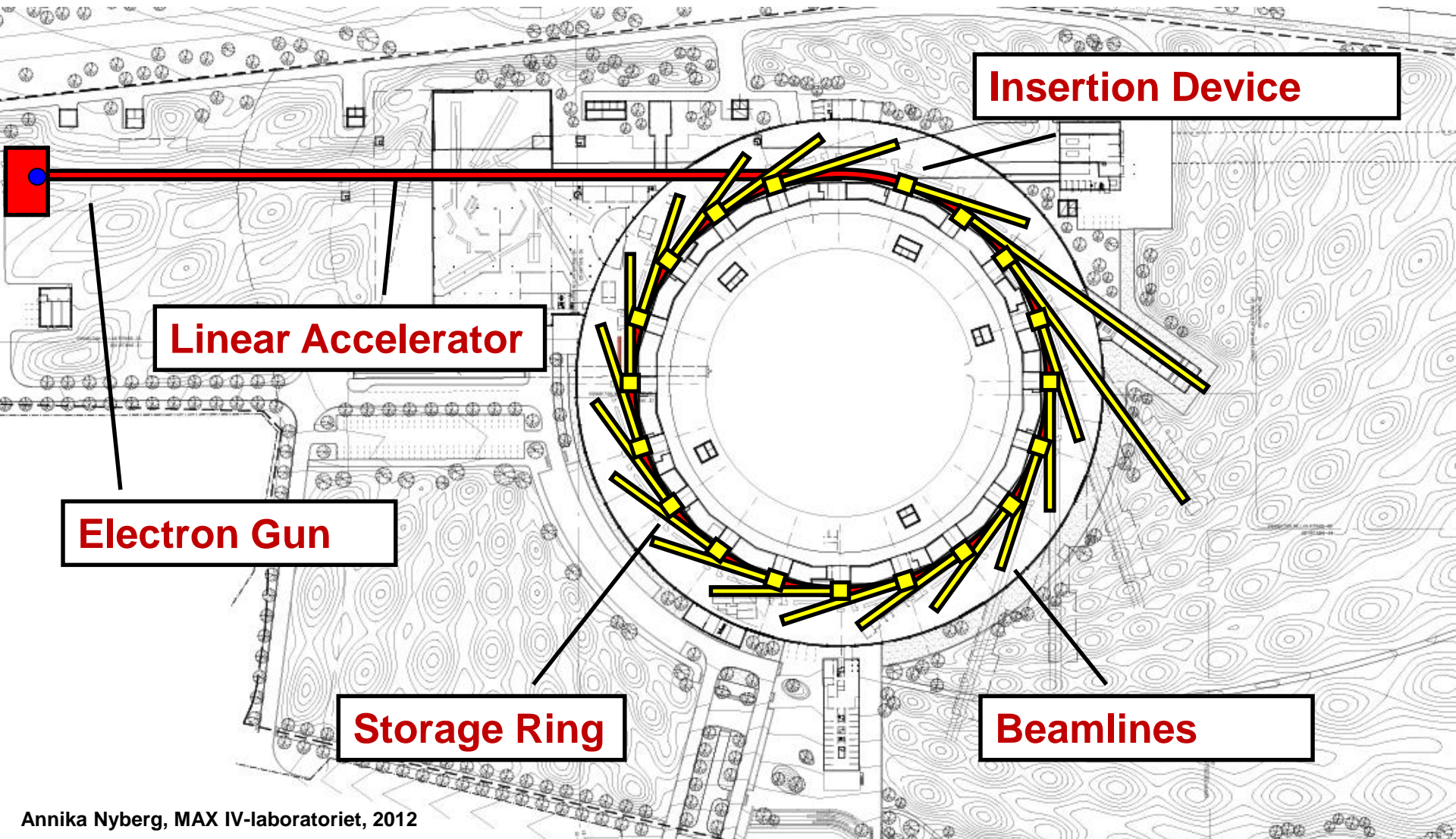
Photo: Vasa Museum



Sandstrom, M. et al. *Deterioration of the seventeenth-century warship vasa by internal formation of sulphuric acid*. Nature **415**, 893 - 897 (2002)

J. Lindgren et al, *Molecular preservation of the pigment melanin in fossil melanosomes*, Nature Communications DOI: 10.1038/ncomms1819 (2012)

Building Blocks of a SR based Light Source



Annika Nyberg, MAX IV-laboratoriet, 2012

Insertion Devices

Undulator

Periodic arrays of magnets cause the beam to “undulate”

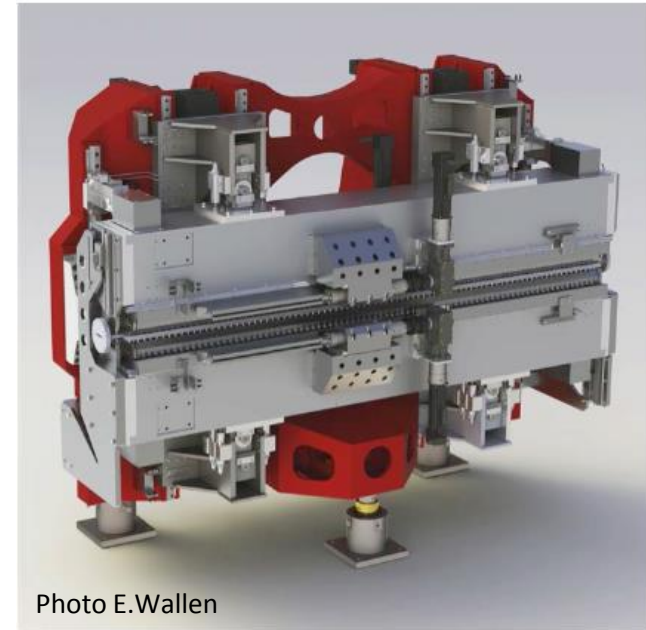
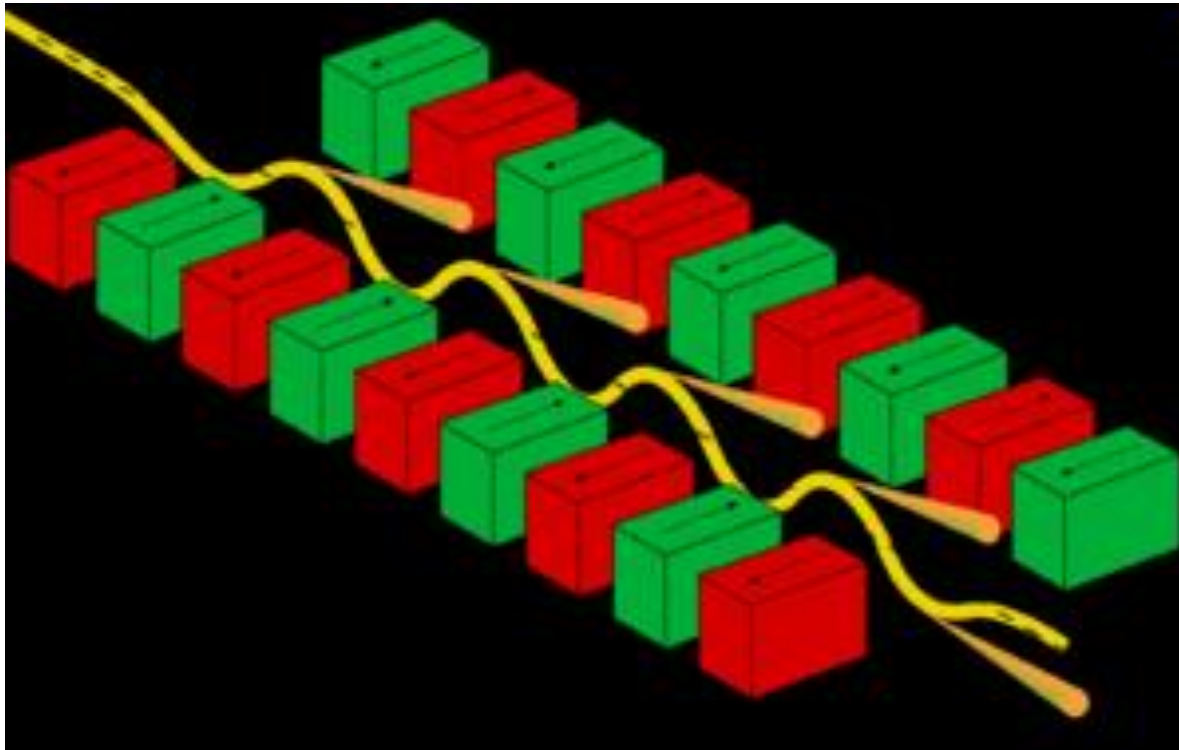
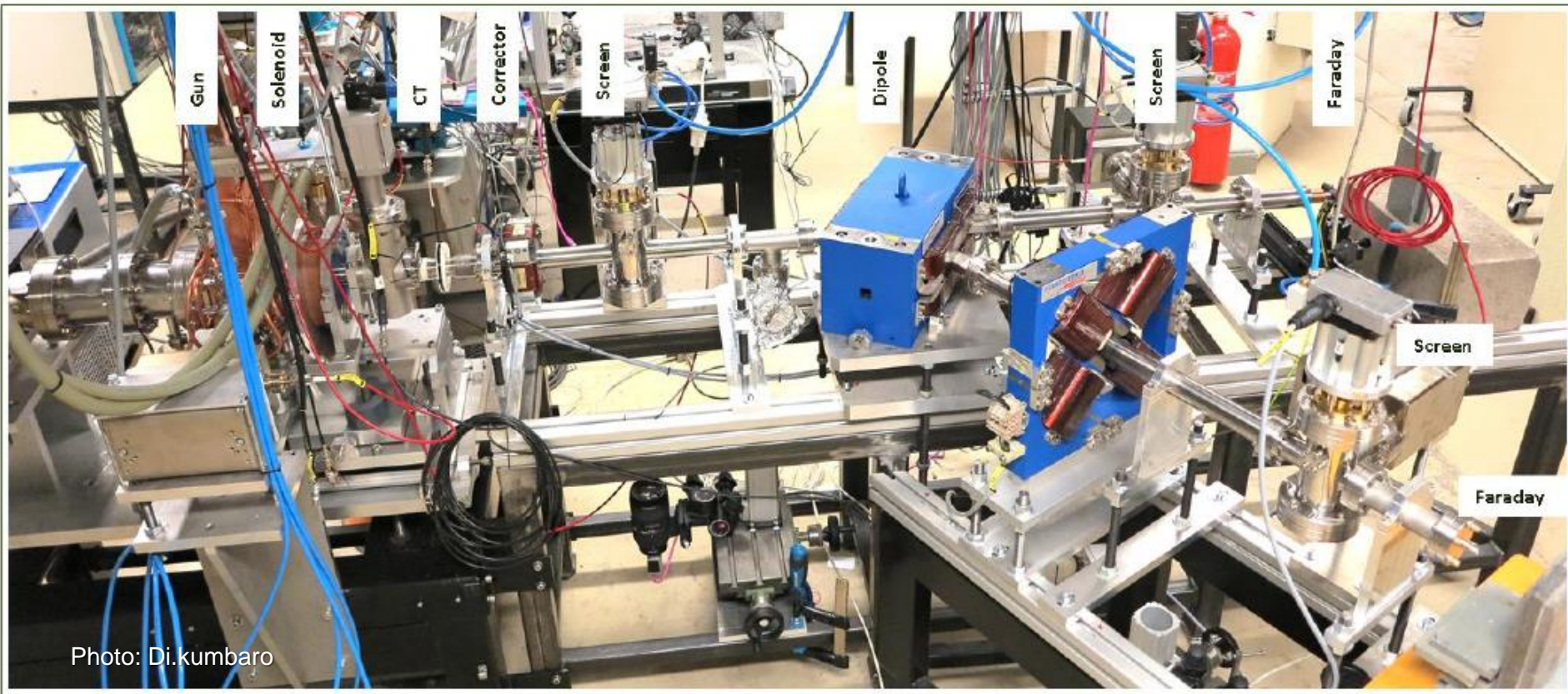


Photo E. Wallen

Wiggler



Electron Sources



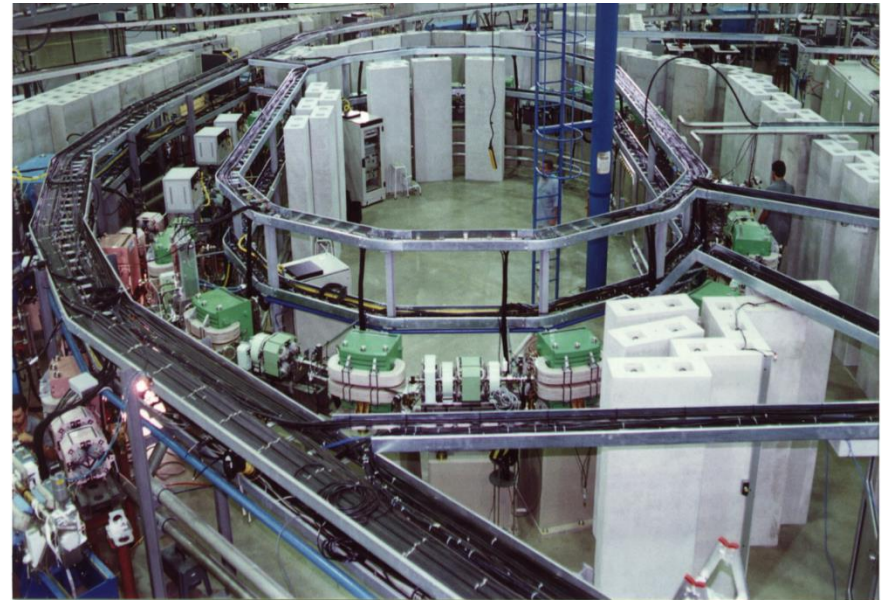
Injector Systems

Linear Accelerator



MAX IV Full Energy Injector LINAC

LINAC + Booster



LNLS -
Brazil

Storage Ring Subsystems

Accumulate and maintain particles circulating stably for many turns

- Magnet System : *Guiding and Focussing*
 - DC
 - Pulsed
- Radio-Frequency System: *Replace lost energy*
- Diagnostic and Control System: *Measure properties, feedback if necessary*
- Vacuum System: *Prevent losses and quality degradation*

The magnet Lattice

Guiding - Dipoles

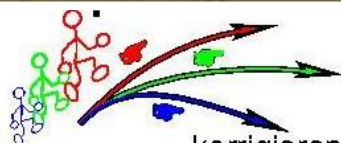


MAX IV Magnet block. Photo: M.Johansson

corr x,y
OXX

SDend corr x OYY DIPm QDend OXY QFend

Note: Many functions can be integrated into a single magnet block



Correction of Chromatic aberrations Sextupoles

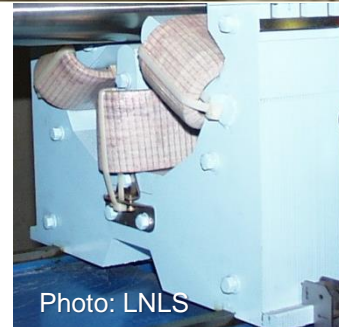
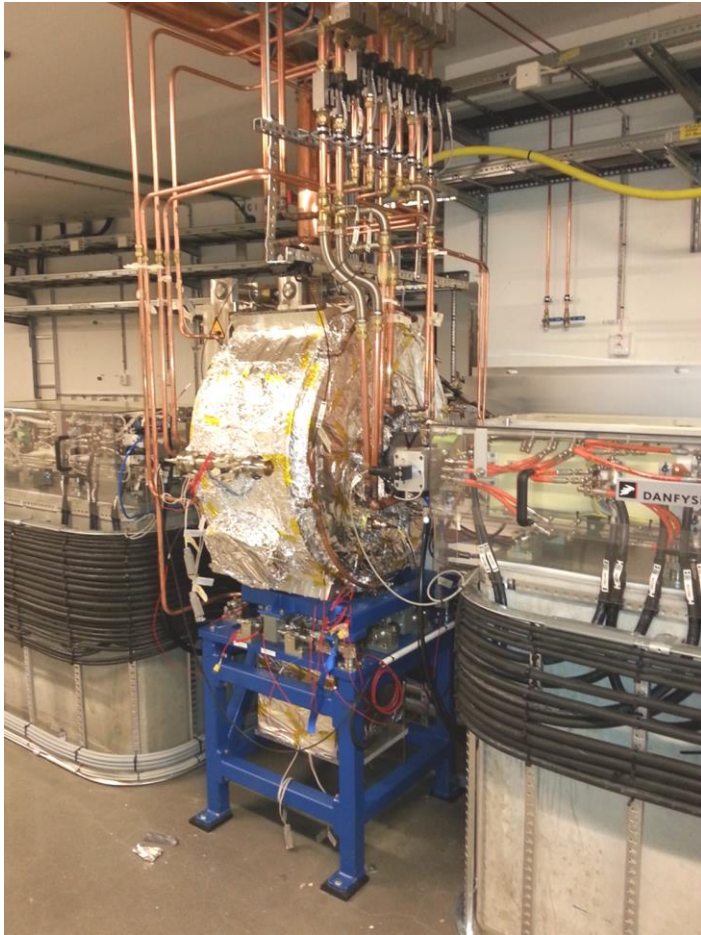


Photo: LNLS

**Focusing -
Quadrupoles**

The Radio-Frequency System

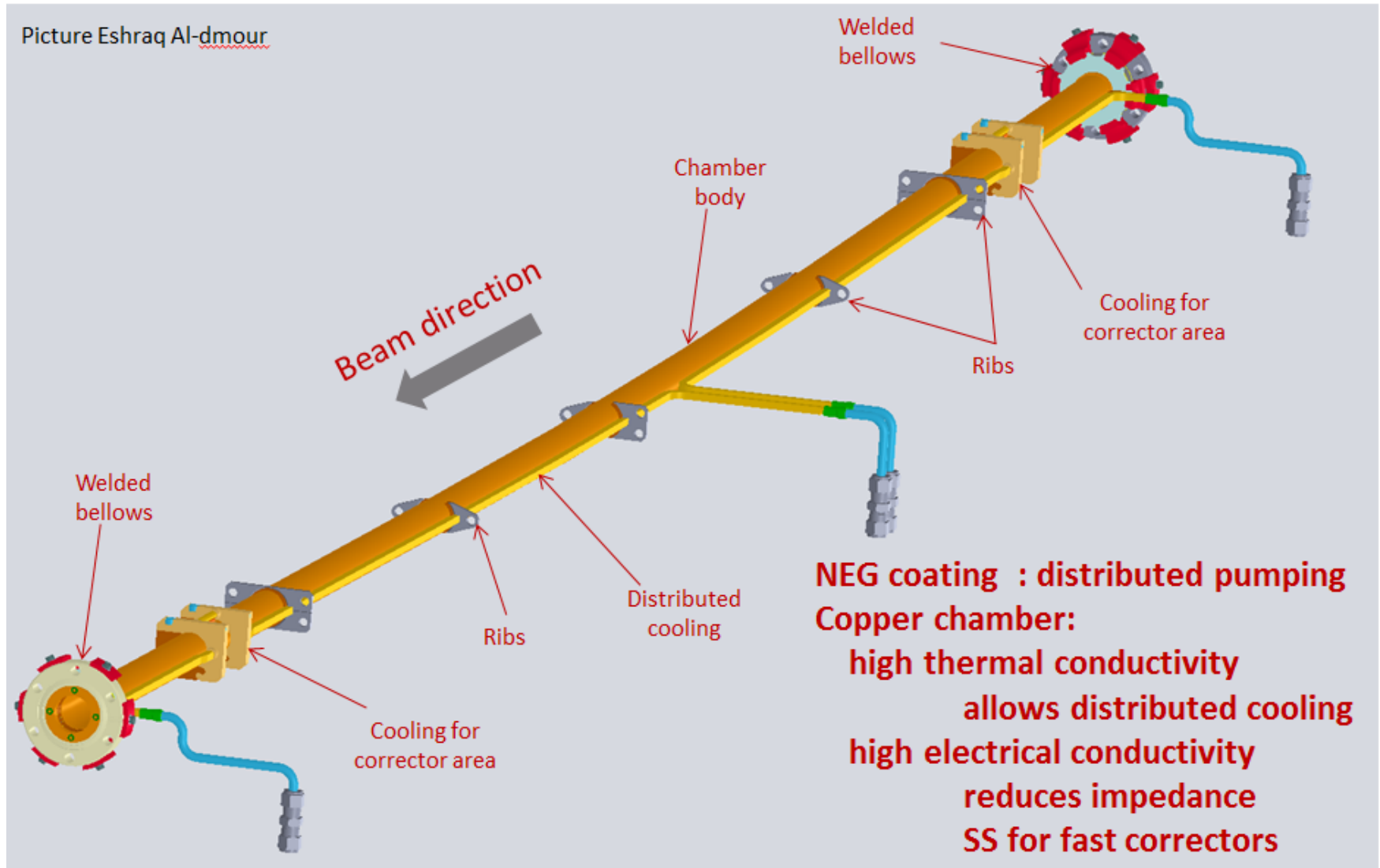


100 MHz Copper Cavities



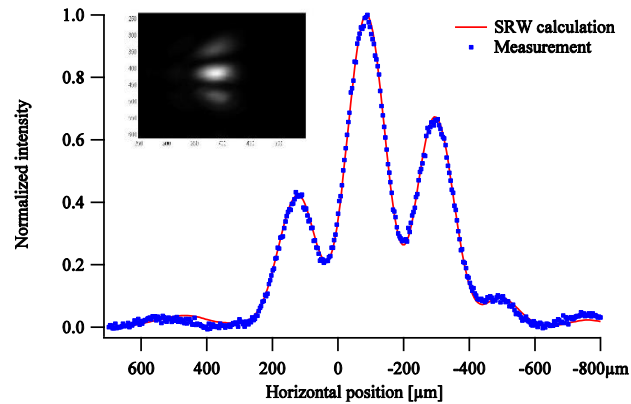
Solid State UHF Amplifiers

The Vacuum System



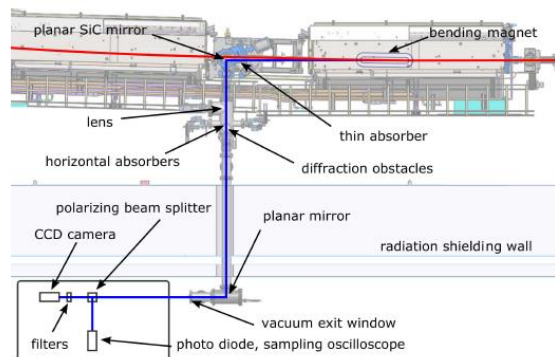
Diagnostics and Controls

Optical Diagnostics

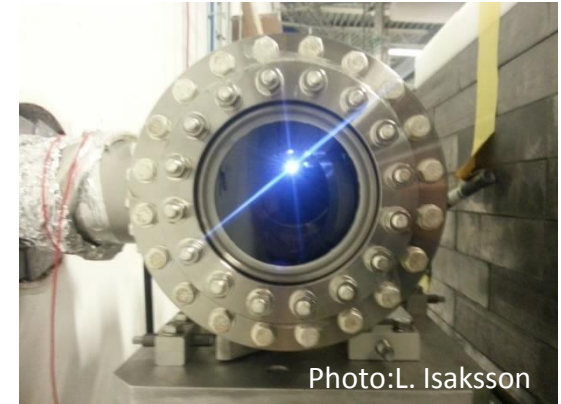


$$\sigma_x = 20.86 \pm 0.14 \mu\text{m} \text{ (fit uncertainty)}$$

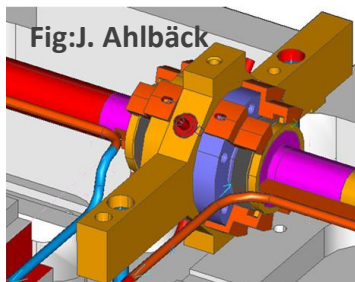
$$\sigma_y = 15.70 \pm 0.15 \mu\text{m} \text{ (fit uncertainty)}$$



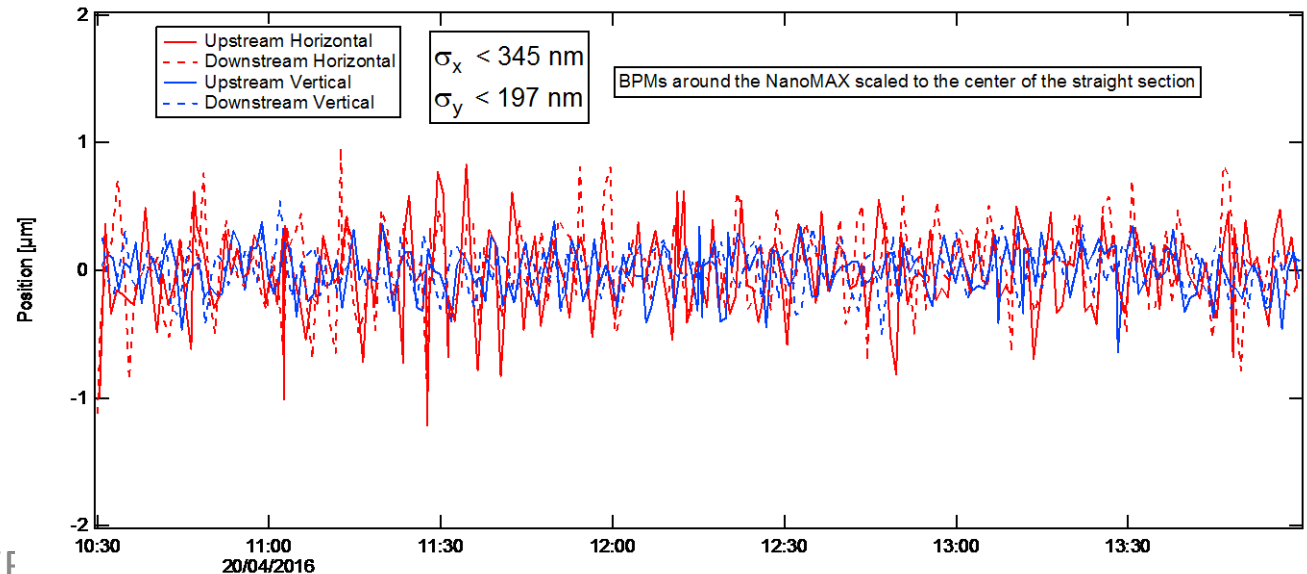
B320B diagnostic beamline
(visible SR radiation)



Electrical Diagnostics and Controls



RF BPMs



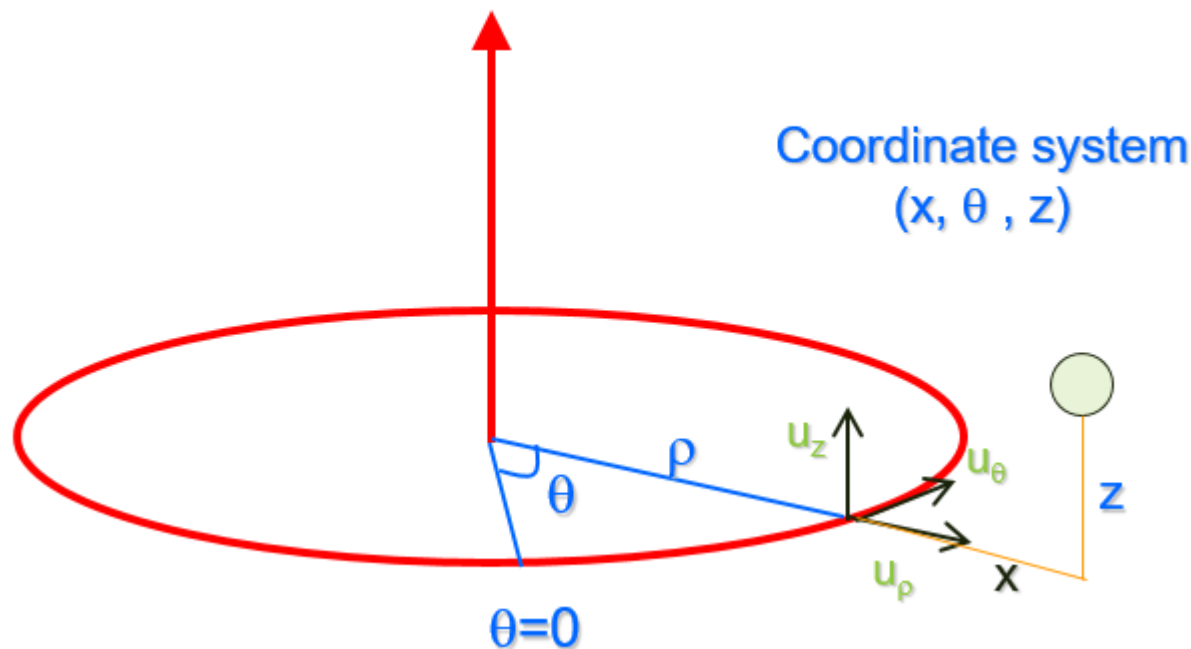
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Storage Ring Beam Dynamics

Goals:

- To determine necessary conditions for the beam to circulate stably for many turns, while optimizing photon beam parameters – larger intensity and brilliance.
- We want to study motion close to an *ideal* or *reference* orbit: Only small deviations w.r.t this reference are considered.
- Understand the behaviour of a system composed of a large number ($\sim 10^{10}$ particles) of ***non-linear coupled oscillators governed by both classical and quantum effects.***



Symmetry conditions for the Field

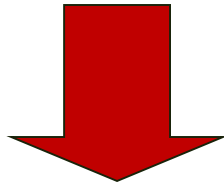
$$B_z(x, \theta, z) = B_z(x, \theta, -z)$$

$$B_x(x, \theta, z) = -B_x(x, \theta, -z)$$

$$B_\theta(x, \theta, z) = 0$$

■ Only transverse components (no edge effects)

■ Only vertical component on the symmetry plane



$$B_z(x, \theta, z) = B_0 - g x$$

$$B_x(x, \theta, z) = -g z$$

First order expansion for the field close to the design orbit

Equations of Motion

$$\vec{F} = -e_0 \vec{v} \times \vec{B}$$

Lorentz Force

$$\gamma m \frac{d\vec{v}}{dt} = -e_0 \vec{v} \times \vec{B}$$

$$\vec{r}(t) = r\vec{u}_r + z\vec{u}_z$$

$$\vec{v}(t) = \dot{r}\vec{u}_r + r\dot{\theta}\vec{u}_\theta + \dot{z}\vec{u}_z$$

$$\frac{d\vec{v}}{dt} = (\ddot{r} - r\dot{\theta}^2)\vec{u}_r + (2\dot{r}\dot{\theta} + r\ddot{\theta})\vec{u}_\theta + \ddot{z}\vec{u}_z$$

$$\vec{v} \times \vec{B} = r\dot{\theta}B_z\vec{u}_r + (\dot{z}B_r - \dot{r}B_z)\vec{u}_\theta - r\dot{\theta}B_r\vec{u}_z$$

$$= r\dot{\theta}(B_0 - gx)\vec{u}_r + (-\dot{z}gz - \dot{r}(B_0 - gx))\vec{u}_\theta + r\dot{\theta}gz\vec{u}_z$$

Paraxial Approximation

■ Azimuthal velocity \gg transverse velocity

■ Small deviations

■ Independent variable $t \Rightarrow s$

$$r = \rho + x$$

$$x \ll \rho$$

$$p = p_0 + \Delta p$$

$$\Delta p \ll p_0$$

$$x''(s) + \left[1 / \rho(s)^2 - K(s) \right] x(s) = \frac{1}{\rho} \frac{\Delta p}{p_0} \quad K = \frac{e_0 g}{p_0}$$

$$z''(s) + K(s) z(s) = 0 \quad \rho = \frac{p_0}{e_0 B_0}$$

$K(s)$ periodic

Oscillatory (stable) solutions

$$s = \theta \rho$$

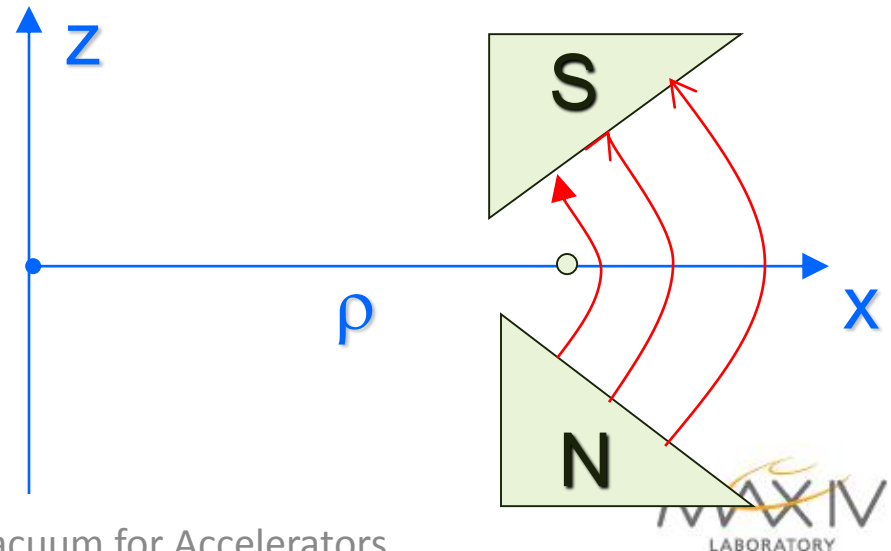
How to guarantee stability ?

Weak focussing

Azimuthally symmetric machine: $y''(s) + Ky(s) = 0$ Oscillatory requires $K > 0$

$$K_x = \frac{1}{\rho^2} - K > 0 \quad \Rightarrow \quad 0 < K < \frac{1}{\rho^2}$$
$$K_z = K > 0$$

*Combined function
magnets*



Weak Focusing Limitations

- Magnet apertures scale with machine energy and become impractical

SOLUTION

Alternating Gradient Courant/Snyder

Eliminate azimuthal symmetry and
alternate field gradients of opposite signs

On-Energy - General Solution

$$x(s) = x_0 C(s) + x'_0 S(s) \quad \text{On-energy particles} \quad \frac{\Delta p}{p_0} = 0$$

$$C(0) = 1 \quad S(0) = 0$$

$$C'(0) = 0 \quad S'(0) = 1$$

Particular solutions

$$\begin{pmatrix} x \\ x' \end{pmatrix}_s = \begin{pmatrix} C(s) & S(s) \\ C'(s) & S'(s) \end{pmatrix} \begin{pmatrix} x \\ x' \end{pmatrix}_0$$

Matrix Solution

$$\begin{pmatrix} x \\ x' \end{pmatrix}_s = M(s) \begin{pmatrix} x \\ x' \end{pmatrix}_0$$

Combining elements means
multiplying matrices

Transfer Matrices - Examples

$$x''(s) = 0$$

$$C(s) = 1$$

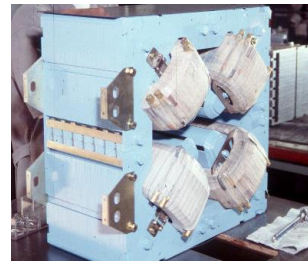
$$S(s) = s$$

$$M = \begin{pmatrix} 1 & L \\ 0 & 1 \end{pmatrix}$$

$$x(L) = x_0 + x'_0 L$$

Field-Free Straight section

Transfer Matrices - Examples



Focussing Quad $x''(s) + Kx(s) = 0$

$$C(s) = \cos(\sqrt{K}s)$$

$$S(s) = \frac{1}{\sqrt{K}} \sin(\sqrt{K}s)$$

$$M = \begin{pmatrix} \cos(\sqrt{K}L) & \frac{1}{\sqrt{K}} \sin(\sqrt{K}L) \\ -\sqrt{K} \sin(\sqrt{K}L) & \cos(\sqrt{K}L) \end{pmatrix}$$

Thin Lens
Approximation

$$M = \begin{pmatrix} 1 & 0 \\ -\frac{1}{f} & 1 \end{pmatrix} \quad \begin{matrix} L \rightarrow 0 \\ KL \rightarrow \frac{1}{f} \end{matrix}$$

Stability Analysis – Periodic Systems

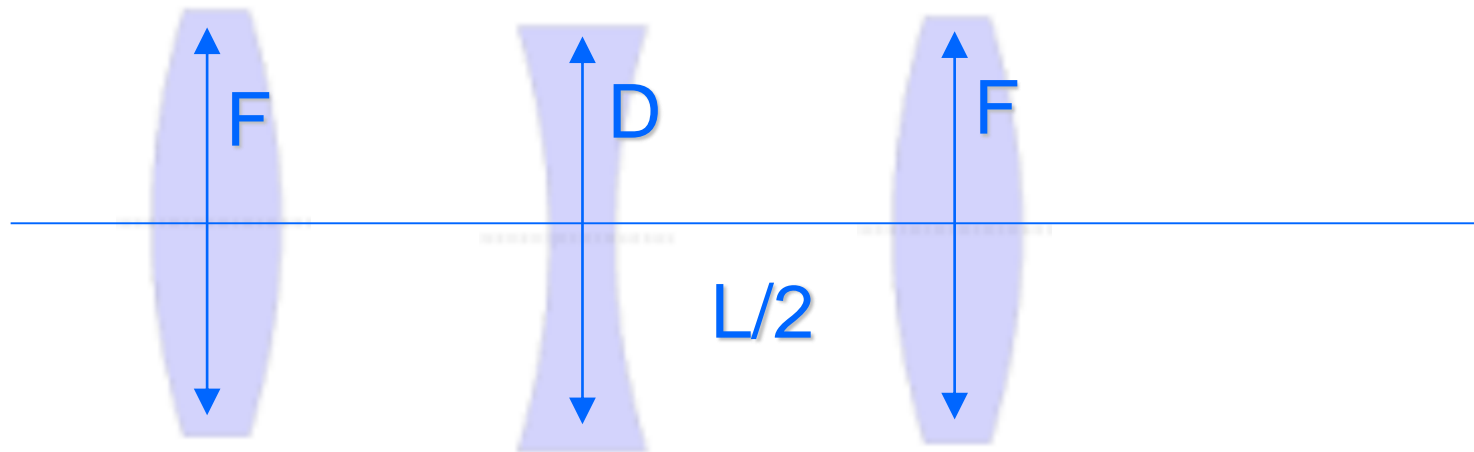
Transfer Matrix for a full period

$$M(s) = \begin{pmatrix} a & b \\ c & d \end{pmatrix}$$

Stability → matrix elements remain bounded

$$\begin{pmatrix} x \\ x' \end{pmatrix}_N = M^N \begin{pmatrix} x \\ x' \end{pmatrix}_0$$

Alternating Gradient: Stability



$$M = \begin{pmatrix} 1 & 0 \\ -\frac{1}{2f} & 1 \end{pmatrix} \begin{pmatrix} 1 & \frac{L}{2} \\ 0 & 1 \end{pmatrix} \begin{pmatrix} 1 & 0 \\ \frac{1}{f} & 1 \end{pmatrix} \begin{pmatrix} 1 & \frac{L}{2} \\ 0 & 1 \end{pmatrix} \begin{pmatrix} 1 & 0 \\ -\frac{1}{2f} & 1 \end{pmatrix}$$

$$M = \begin{pmatrix} 1 - \frac{L^2}{8f^2} & L \left(1 + \frac{L}{4f} \right) \\ -\frac{L}{4f^2} \left(1 - \frac{L}{4f} \right) & 1 - \frac{L^2}{8f^2} \end{pmatrix}$$

Stability Analysis

$$M = \begin{pmatrix} 1 - \frac{L^2}{8f^2} & L\left(1 + \frac{L}{4f}\right) \\ -\frac{L}{4f^2}\left(1 - \frac{L}{4f}\right) & 1 - \frac{L^2}{8f^2} \end{pmatrix} = \cos(\mu)I + \sin(\mu)J$$

$$\cos(\mu) = 1 - \frac{L^2}{8f^2}$$

$$\sin(\mu) = \frac{L}{2f} \sqrt{\left(1 - \frac{L}{4f}\right)\left(1 + \frac{L}{4f}\right)}$$

$$\beta = 2f \sqrt{\frac{\left(1 + \frac{L}{4f}\right)}{\left(1 - \frac{L}{4f}\right)}}$$

Stable if μ real

$$I = \begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}$$

$$J = \begin{pmatrix} 0 & \beta \\ -\frac{1}{\beta} & 0 \end{pmatrix}$$

$$I^2 = I$$

$$J^2 = -I$$

$$M^2 = \cos(2\mu)I + \sin(2\mu)J$$

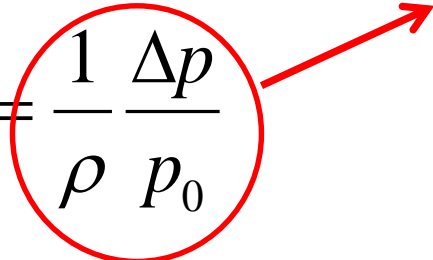
$$M^n = \cos(n\mu)I + \sin(n\mu)J$$

$$\left|1 - \frac{L^2}{8f^2}\right| < 1 \Rightarrow f > \frac{L}{4}$$

Off-Energy Particles

$$D''(s) + \left[1/\rho(s)^2 - K(s) \right] D(s) = \frac{1}{\rho} \frac{\Delta p}{p_0}$$

Non-homogeneous term



$D(s)$ can be obtained from the solution to the homogeneous eqs.

$$D(s) = S(s) \int_0^s \frac{ds'}{\rho(s')} C(s') - C(s) \int_0^s \frac{ds'}{\rho(s')} S(s')$$

Matrix Solution

$$\begin{pmatrix} x \\ x' \\ \frac{\Delta p}{p_0} \end{pmatrix}_s = M(s) \begin{pmatrix} x \\ x' \\ \frac{\Delta p}{p_0} \end{pmatrix}_{s=0} \quad M = \begin{pmatrix} C(s) & S(s) & D(s) \\ C'(s) & S'(s) & D'(s) \\ 0 & 0 & 1 \end{pmatrix}$$

Example: Sector Dipole Magnet

$$\left. \begin{array}{l} K(s) = 0 \\ \rho(s) = \rho_0 \end{array} \right\} \begin{array}{l} C(s) = \cos\left(\frac{s}{\rho_0}\right) \\ S(s) = \rho_0 \sin\left(\frac{s}{\rho_0}\right) \end{array} \rightarrow D(s) = \rho_0 \left\{ 1 - \cos\left(\frac{s}{\rho_0}\right) \right\}$$

$$M = \begin{pmatrix} C(s) & S(s) & D(s) \\ C'(s) & S'(s) & D'(s) \\ 0 & 0 & 1 \end{pmatrix} \approx \begin{pmatrix} 1 & s & \frac{s^2}{2\rho_0} \\ 0 & 1 & \frac{s}{\rho_0} \\ 0 & 0 & 1 \end{pmatrix}$$

Small bending angle

General pseudo-harmonic solution

$$\left\{ \begin{array}{l} x''(s) + \left[\frac{1}{\rho(s)^2} - K(s) \right] x(s) = \frac{1}{\rho} \frac{\Delta p}{p_0} \\ z''(s) + K(s) z(s) = 0 \end{array} \right.$$

Pseudo-harmonic solution

$$x(s) = \sqrt{\epsilon \beta(s)} \cos(\phi(s) - \phi_0) + \eta(s) \frac{\Delta p}{p}$$

Betatron Phase Advance

$$\phi(s) = \int_0^s \frac{ds'}{\beta(s')}$$

Betatron Function
Dispersion Function

Periodic

Betatron Tune

$$Q = \frac{\mu}{2\pi} = \frac{\phi(L)}{2\pi}$$

Equation for Betatron Function

$$\frac{1}{2} \beta(s) \beta''(s) - \frac{1}{4} \beta'^2(s) + \beta^2(s) K(s) = 1$$

Twiss Parameters

$$\beta(s)$$

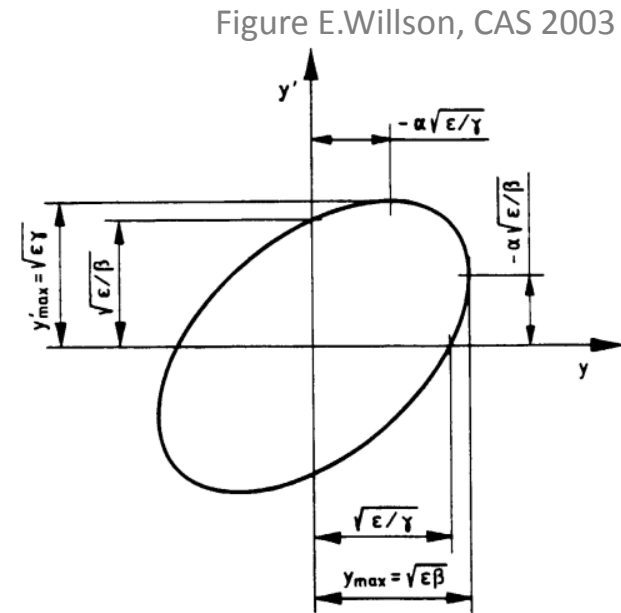
$$\alpha(s) = -\frac{1}{2}\beta'(s)$$

$$\gamma(s) = \frac{1 + \alpha^2(s)}{\beta(s)}$$

Courant Snyder Invariant

$$\varepsilon = \gamma(s)x^2(s) + 2\alpha(s)x(s)x'(s) + \beta(s)x'^2(s)$$

These are properties of the ring, defined by how the focussing is distributed along the accelerator and give us a convenient way to describe any trajectory (in linear approximation)



Twiss Parameters and Beam sizes

Equilibrium beam parameters: Emittance, Energy Spread

$\epsilon_x, \epsilon_y, \sigma_\delta$

$$\sigma_x(s) = \sqrt{\epsilon_x \beta_x(s) + \sigma_\delta^2 \eta(s)^2}$$

$$\sigma_{x'}(s) = \sqrt{\epsilon_x \gamma_x(s) + \sigma_\delta^2 \eta'(s)^2}$$

$$\sigma_y(s) = \sqrt{\epsilon_y \beta_y(s)}$$

$$\sigma_{y'}(s) = \sqrt{\epsilon_y \gamma_y(s)}$$

Twiss Parameters and Perturbations

- Localized dipole error (θ) – perturbation of the *closed orbit* (periodic solution)

$$\Delta x_{c.o.}(s) = \frac{\sqrt{\beta(s)\beta_0}\theta_0\cos(\phi(s) - \pi Q)}{2\sin(\pi Q)}$$

- Localized quadrupole error (ΔKL) – perturbation of the tune and beta function

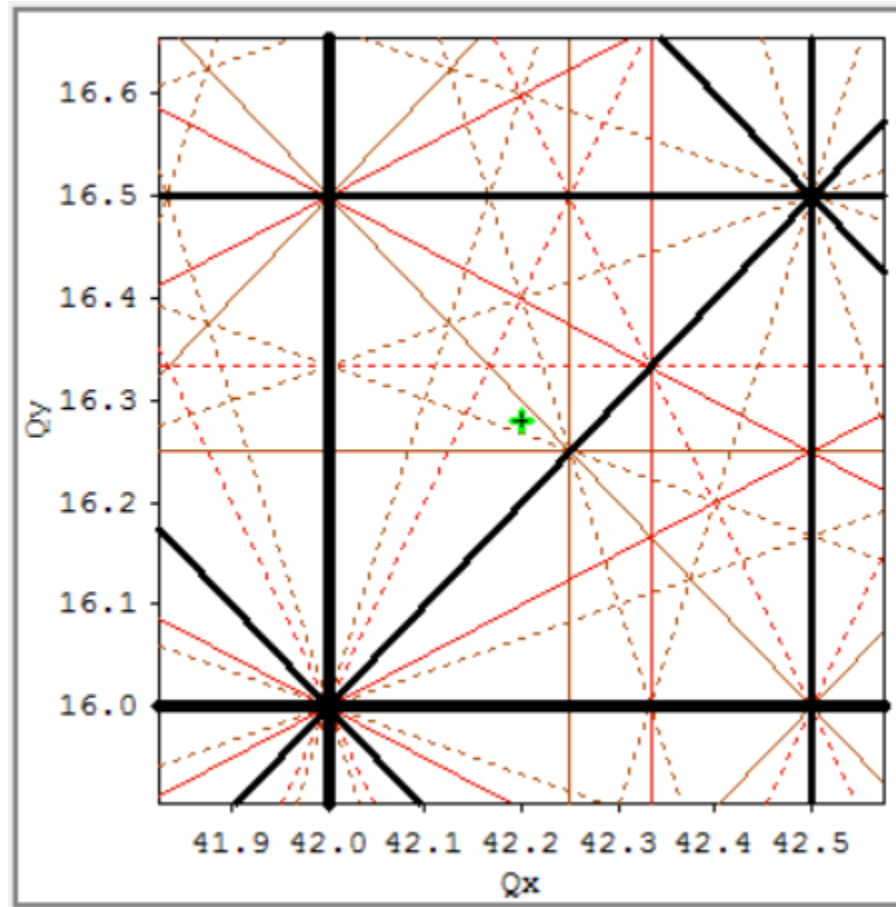
$$\frac{\Delta\beta(s)}{\beta(s)} = \frac{\beta_0}{2\sin(2\pi Q)}\cos(2\phi(s) - 2\pi Q)\Delta KL$$

Perturbations

Some freqs. (tunes) must be avoided to prevent resonances.

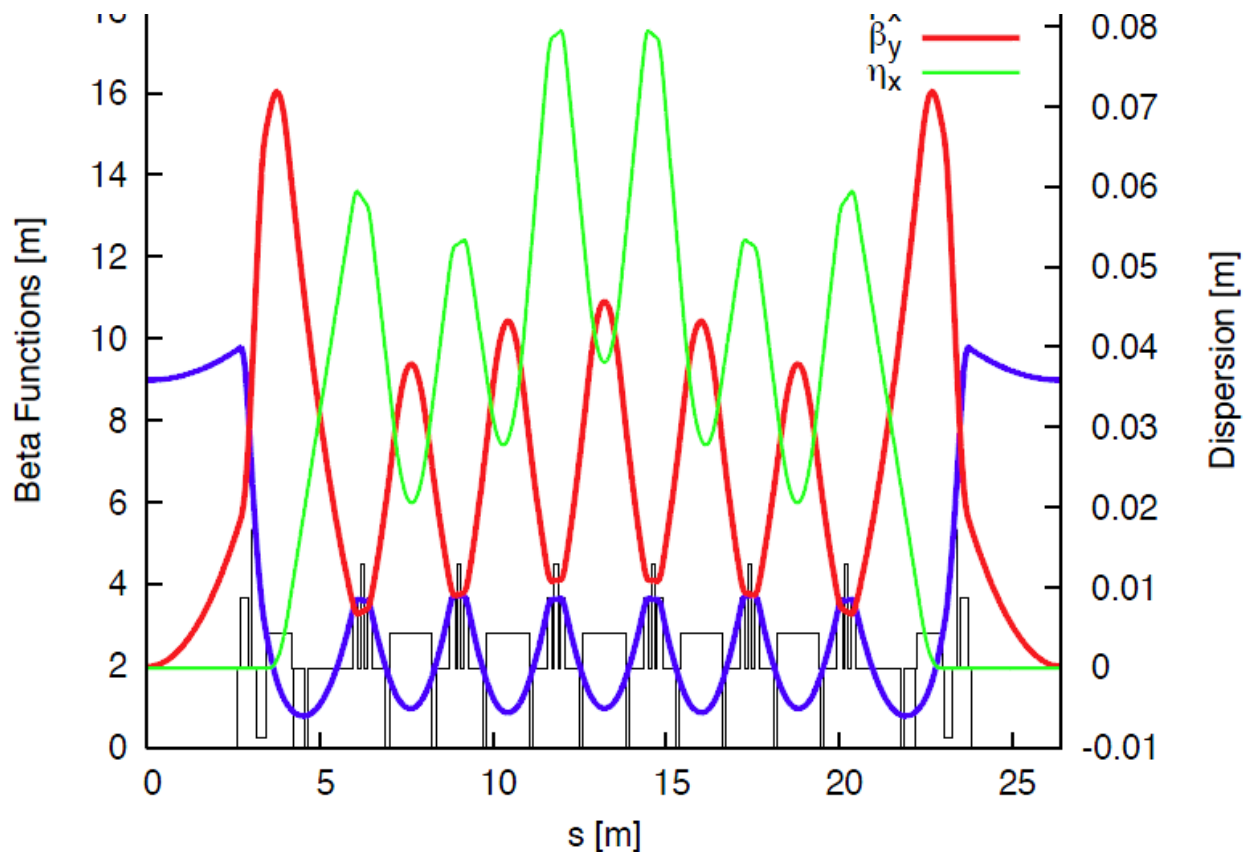
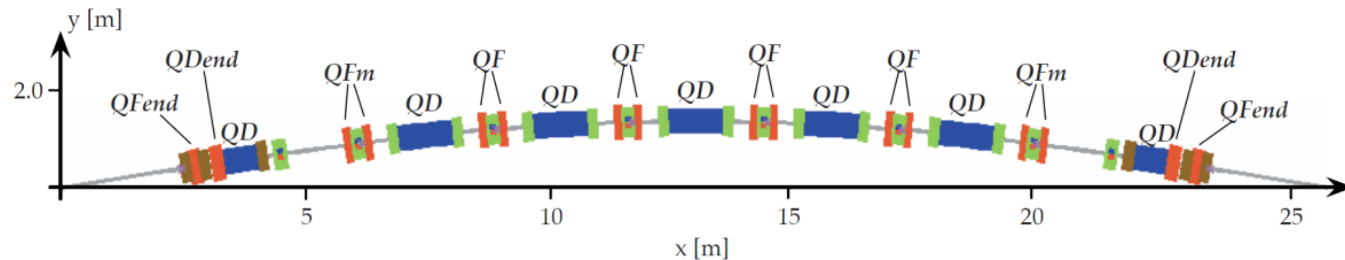
$$mQ_x + nQ_y = p$$

m, n, p integer



Resonance Diagram for
the MAX IV 3 GeV Ring

Twiss Parameters MAX IV 3 GeV Ring

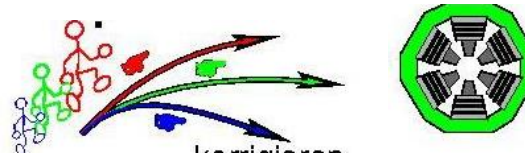


Non-linear perturbations

Chromaticity: quad strength varies with energy.

$$B_z(x) = Sx^2$$

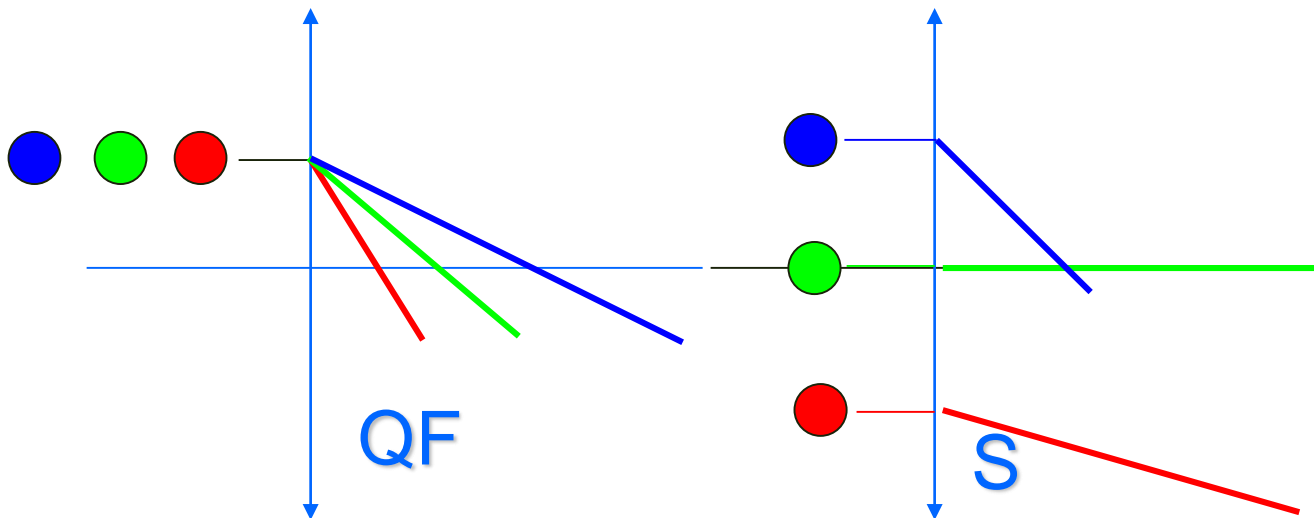
$$G(x) = 2Sx$$



Correction of chromatic aberration with sextupoles



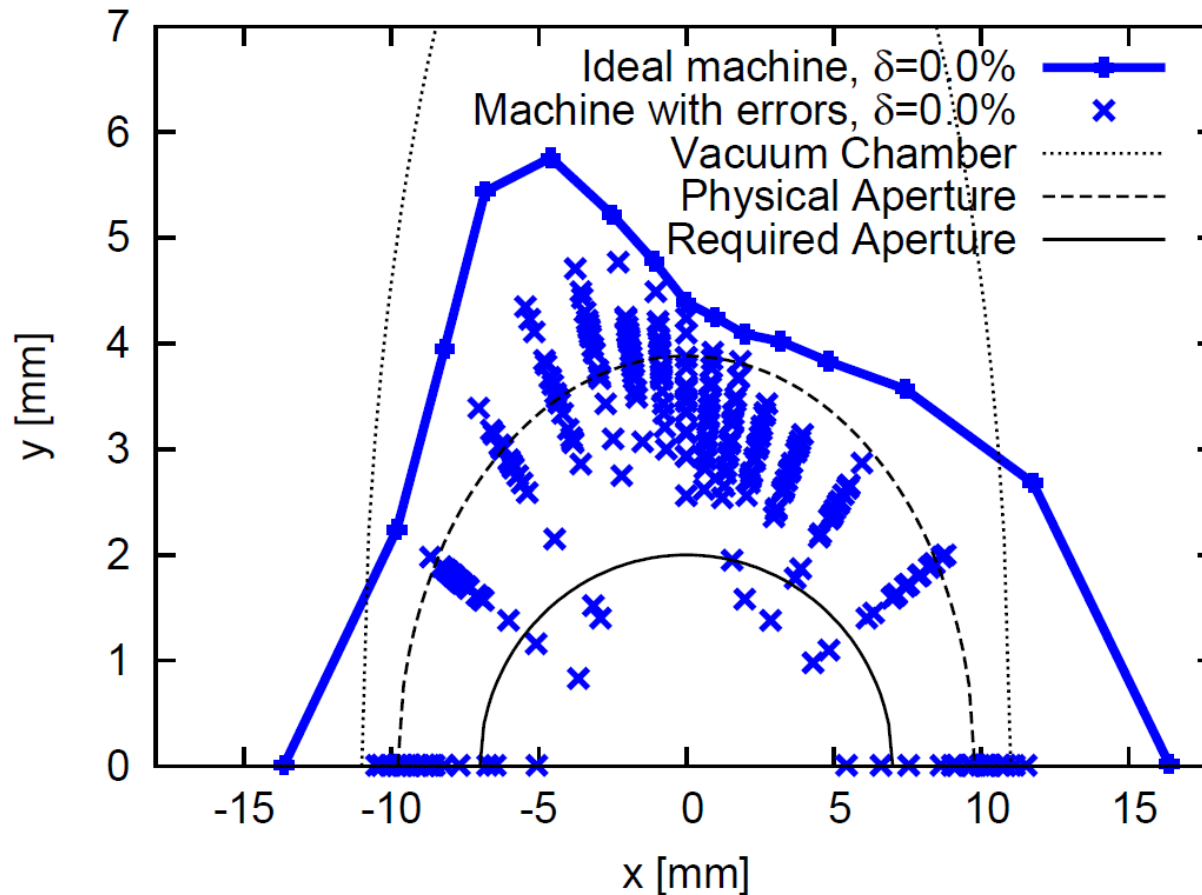
Photo LNL



A sextupole produces a position dependent focussing

Sextupoles are non-linear elements and introduce perturbations

Non-Linear Perturbations and Dynamic Aperture

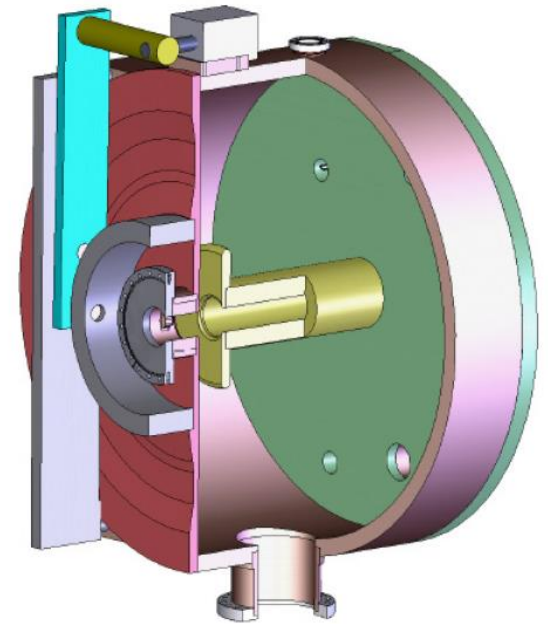
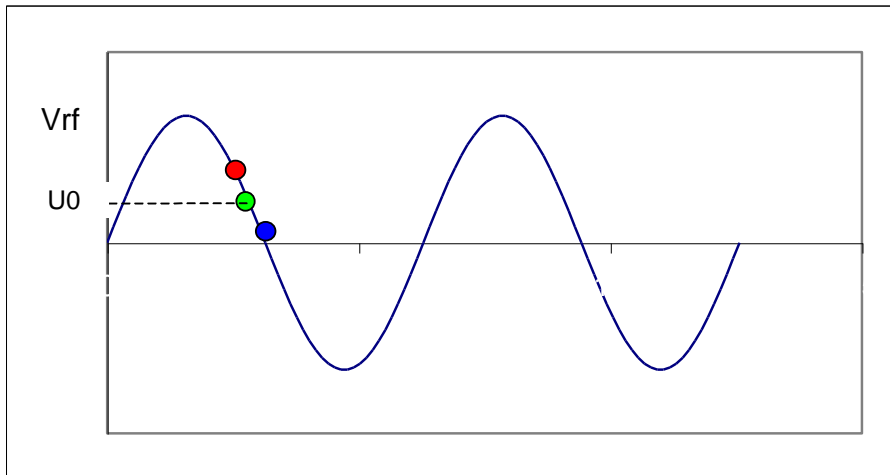


MAX IV DDR, 2010

Longitudinal Dynamics: Phase Stability

Synchrotron Oscillations

Particles with different energies have different revolution periods



MAX IV 100 MHz RF Cavity

For small amplitudes: simple harmonic motion

Larger amplitudes: non-linearities (like a pendulum)

$$\ddot{\tau} + \omega_s^2 \tau = 0$$

Brief Recap – Beam Dynamics

Transverse Plane:

$$x''(s) + \left[1/\rho(s)^2 - K(s)\right]x(s) = \frac{1}{\rho} \frac{\Delta p}{p_0}$$

$$z''(s) + K(s)z(s) = 0$$

Longitudinal Plane:

$$\ddot{\tau} + \omega_s^2 \tau = 0$$

- The beam is a collection of many 3D – oscillators.
- If parameters are properly chosen (magnet lattice, RF system), *stable oscillations* are realized in all planes.
- Non-linearities cause distortions that may reduce the available stable area in phase space: reduction of the *dynamic aperture*.

Linear Oscillations – Twiss Parameters

- $Q, \beta(s), \alpha(s), \gamma(s)$
- Are a property of the lattice (the whole accelerator).
- Provide a convenient way to summarize all about the linear behaviour of the accelerator: trajectories, sizes, sensitivity to errors

Outlook

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- How vacuum affects accelerator performance.

How Vacuum Systems affect SR Performance

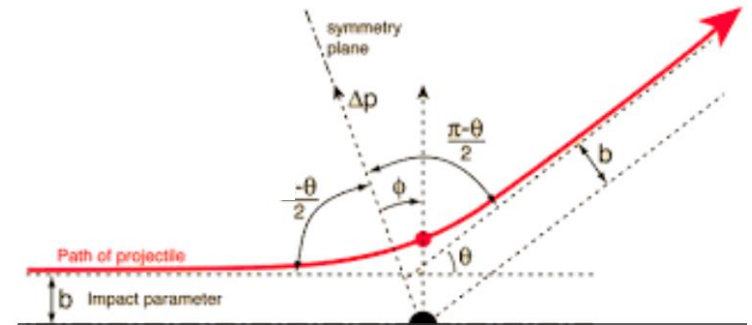
	Quantity	Quality	Examples
Coherent		Wakefields	limits max. current bunch dimensions
Incoherent		Ion Trapping	lifetime tune shifts emittance growth transverse stability
		Scattering Elastic/Inelastic	lifetime : need to top-up more often

Elastic Scattering

Illustration from <http://hyperphysics.phy-astr.gsu.edu>

Rutherford Scattering cross-section

$$\frac{d\sigma_{el}}{d\Omega} = \left(\frac{1}{4\pi\epsilon_0} \frac{Ze_0^2}{2p_0c} \right)^2 \frac{1}{\sin^4\left(\frac{\theta}{2}\right)}$$



Particles are lost if scattered by angles larger than:

$$\theta_{max}^2 = \frac{\left(A^2 / \beta \right)_{min}}{\beta_0}$$

Aperture limitation around the whole ring

Beta function where the collision occurred

$$\frac{1}{\tau_{el}} = -\frac{1}{N} \frac{dN}{dt} = 2\pi c n \int_{\theta_{max}}^{\pi} \frac{d\sigma_{el}}{d\Omega} \sin \theta d\theta$$

electrons

Gas density

Watch out for:

- **low energy**
- **small apertures**
- **high pressure at high beta locations**
- **High Z**

Assuming Nitrogen

$$\tau_{el}[hr] = \frac{10.25 E[GeV]^2 \epsilon_A[mmrad]}{\langle \beta \rangle (m) P[ntorr]}$$

Inelastic Scattering (bremsstrahlung)

- Particle lose energy through radiation emission in collision with nuclei and electrons.
- If energy loss is larger than acceptance, particle is lost

$$\frac{d\sigma_{BS}}{d\delta} = \frac{\alpha_f 4Z^2 r_e^2}{\delta} \left\{ \left[\frac{4}{3} \left(1 - \frac{\delta}{E} \right) + \left(\frac{\delta}{E} \right)^2 \right] \ln \left(\frac{183}{Z^{\frac{1}{3}}} \right) + \frac{1}{9} \left(1 - \frac{\delta}{E} \right) \right\}$$

Particles are lost if they lose energy larger than the acceptance: δ_{acc}

$$\begin{aligned} \frac{1}{\tau_{BS}} &= - \frac{1}{N} \frac{dN}{dt} \\ &= cn \int_{\delta_{acc}}^E \frac{d\sigma_{BS}}{d\delta} d\delta = cn 4\alpha_f Z^2 r_e^2 \left\{ \frac{4}{3} \left(\ln \left(\frac{E}{\delta_{acc}} \right) - \frac{5}{8} \right) \ln \left(\frac{183}{Z^{\frac{1}{3}}} \right) + \frac{1}{9} \left(\ln \left(\frac{E}{\delta_{acc}} \right) - 1 \right) \right\} \end{aligned}$$

α_f Fine structure constant

r_e Classical electron radius

Watch out for high Z

Weak dependence on energy and energy acceptance

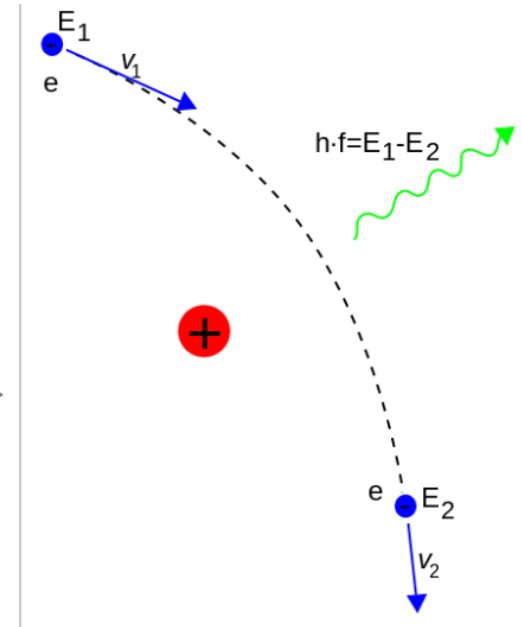


Illustration <https://de.wikipedia.org>

Ion Trapping

- circulating electrons collide with residual gas molecules producing positive ions that can be captured (trapped) by the beam



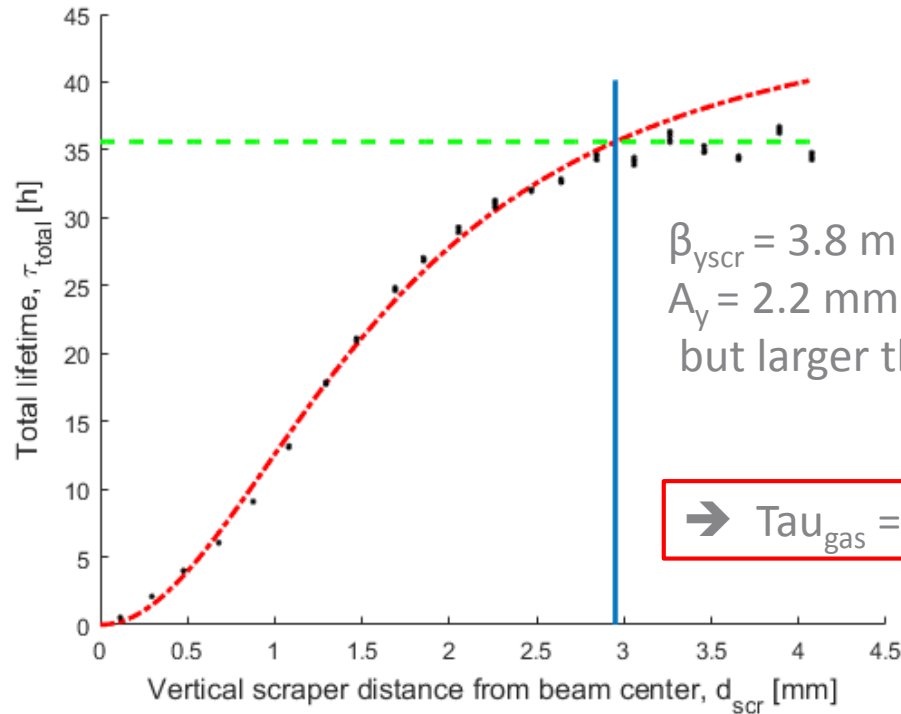
- Reduces beam lifetime : increased local pressure.
- Tune –shifts, Tune spreads
- Emittance Growth
- Coherent Collective instabilities (multi-bunch)

This had some nearly catastrophic effects on some early low energy injection machines

Lifetime contributions at the MAX IV 3 GeV Ring

$$\tau_{\text{tot}} = 36 \text{ h} \quad \text{or} \quad I \cdot \tau_{\text{tot}} = 2.5 \text{ Ah}$$

Slide courtesy Åke Andersson



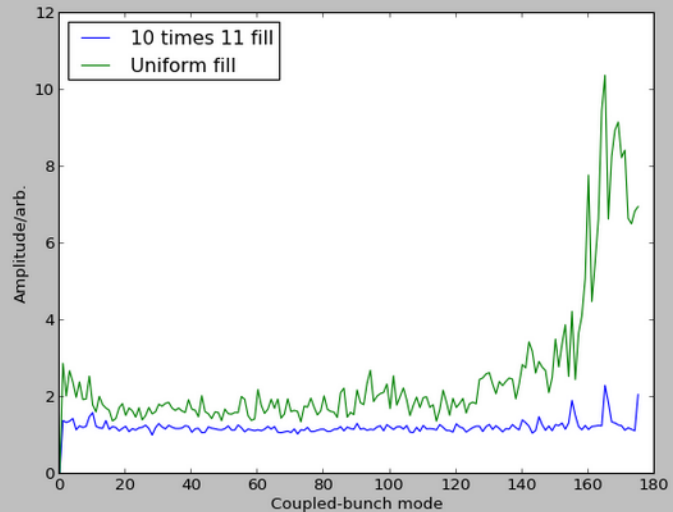
$$\rightarrow \tau_{\text{gas}} = 60 \text{ h} \quad \text{or} \quad I \cdot \tau_{\text{gas}} = 4.2 \text{ Ah}$$

Vertical Scraper Measurements
by Jens Sundberg

$$\rightarrow \tau_{\text{Tou}} = 90 \text{ h} \quad \text{or} \quad I \cdot \tau_{\text{Tou}} = 6.2 \text{ Ah}$$

Transverse collective instabilities driven by ions

Increased stability by adding a gap to the bunch train



2016/07/06: MAX IV 3 GeV Ring
Early commissioning

Transverse beam blow up due to ion trapping

Ion Clearing ON



Ion Clearing OFF



LNLS 1.37 GeV electron storage rig

R.H.A.Farias et al: *Optical Beam Diagnostics for the LNLS Synchrotron Light Source*, EPAC98, p.2238.

Thank you for your attention

■ References

- H. Wiedemann, *Particle Accelerator Physics I and II*, Springer Verlag.
- M.Sands, *The Physics of Electron Storage Rings*
- D.A.Edwards and M.J.Syphers, *An Introduction to the Physics of High Energy Accelerators*, Wiley
- CAS – CERN Accelerator Schools (Basic and Advanced)

Back up slides

Why Synchrotron Light ?

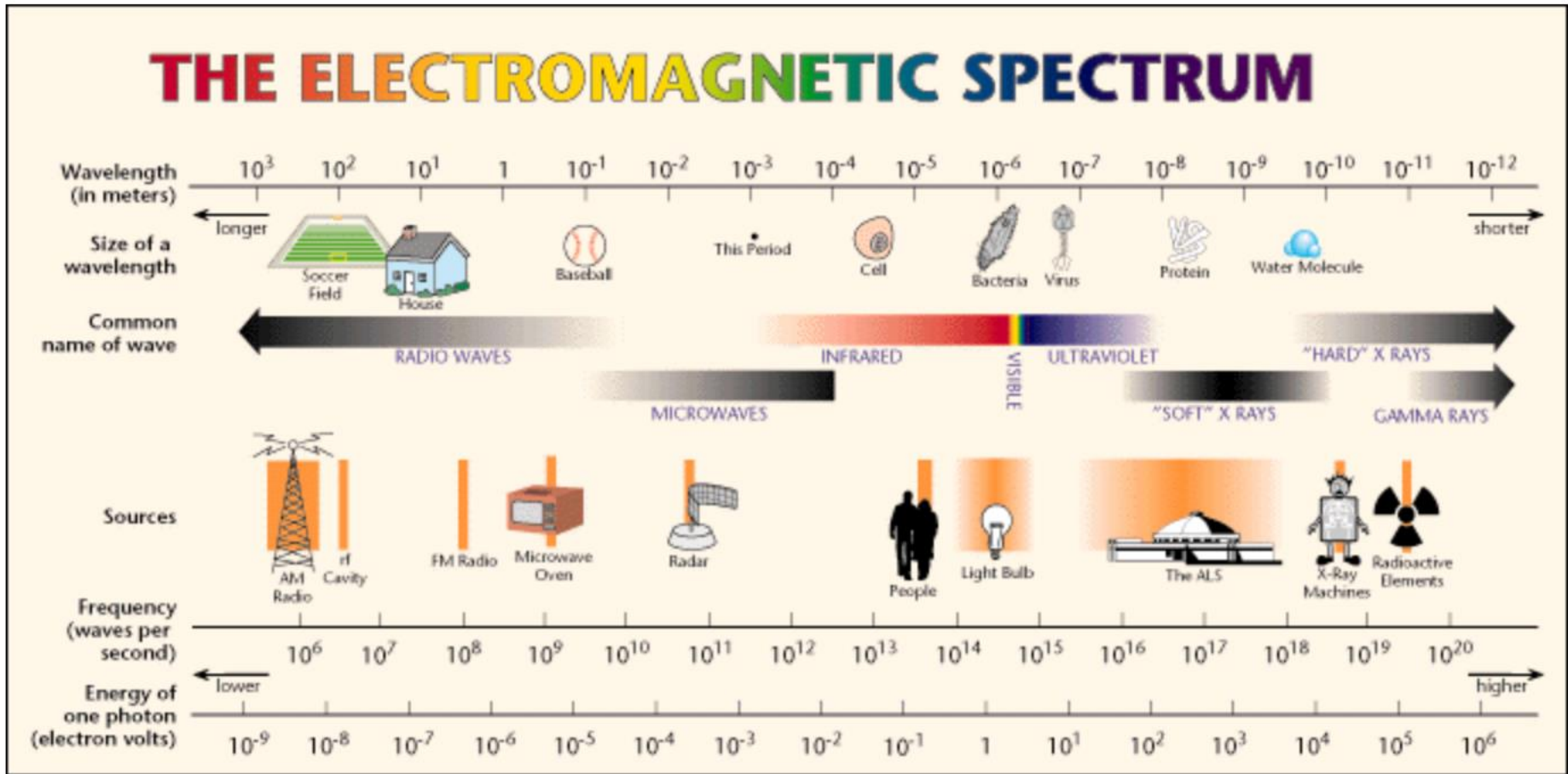


Image: Lawrence Berkely Lab

Lattice Design for *Low Emittance* Rings

General Problem Statement – Scaling Laws

$$\varepsilon_0 = C_q \frac{\gamma^2 \left\langle \frac{H}{\rho^3} \right\rangle}{J_x \left\langle \frac{1}{\rho^2} \right\rangle} \quad H(s) = \beta(s)\eta'^2(s) + 2\alpha(s)\beta(s) + \gamma(s)\eta^2(s)$$

$$J_x = 1 - \mathcal{D} \quad \mathcal{D} = \frac{\oint \frac{\eta(s)}{\rho^3(s)} (1 + 2\rho^2(s)k(s))}{\oint \frac{ds}{\rho^2(s)}}$$

$$\varepsilon_0 = C_q \frac{\gamma^2}{J_x} \frac{\langle H \rangle_{dip}}{\rho} \quad \text{isomagnetic}$$

Defining the Basic Parameters of a SR based Light Source

Energy

$$E_1 = \frac{hc}{\lambda_p} \frac{2\gamma^2}{\left(1 + \frac{1}{2} K_u^2\right)}$$

Photon energy range +
Insertion device Technology +
Top-up Injection

$$B_0[\text{Tesla}] = 3.694 \exp \left(-5.068 \frac{g}{\lambda_p} + 1.52 \left(\frac{g}{\lambda_p} \right)^2 \right)$$

Diameter

Emittance (brightness) requirements

$$\varepsilon_0 = C_q \frac{\gamma^2 \theta^3}{12 \sqrt{15} J_x} F$$

Electrostatic SR

Stores 25 keV ions.

S.Moller, EPAC98

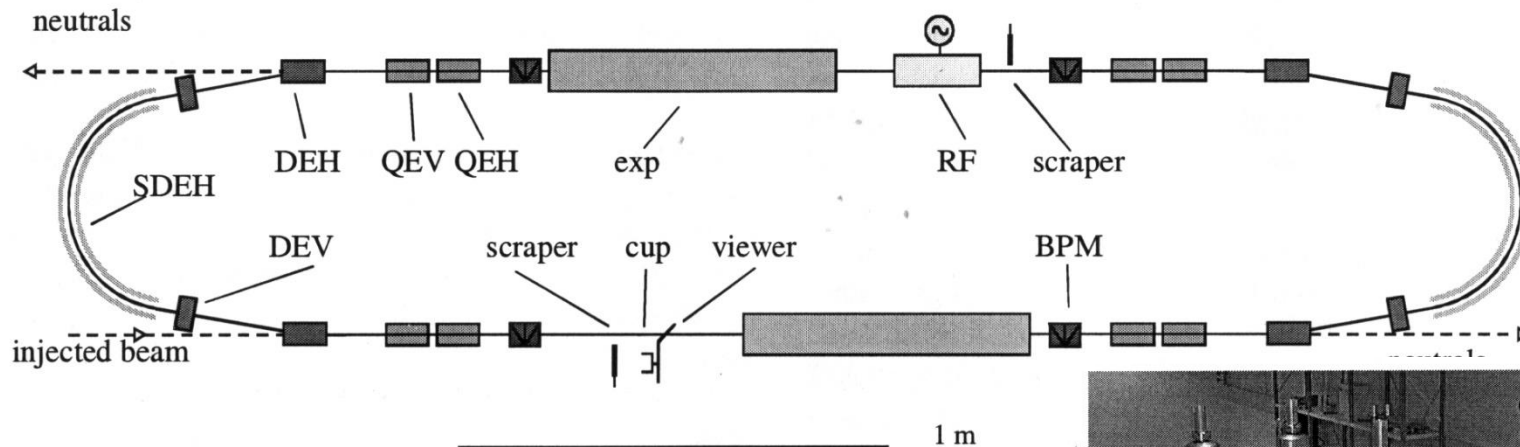


Figure 1: Layout of the ELISA storage ring. The abbreviations are explained i

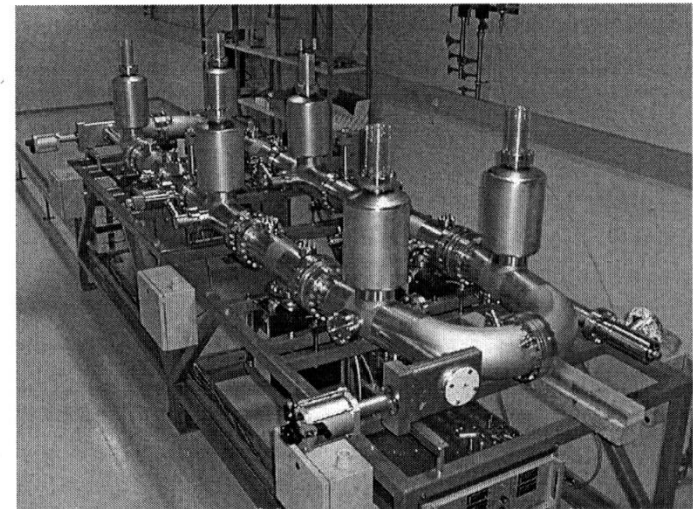


Figure 3: Picture of the ELISA storage ring.

Beam Guiding

Why magnetic fields ?

Lorentz Force $\vec{F} = -e_0(\vec{E} + \vec{v} \times \vec{B})$

at 3.0 GeV,

B= 1.0 T

E = 500 MV/m !!

Transverse Beam Dynamics

- Zeroth order: guide fields (dipoles)
- First order : Focusing – linear oscillations (quadrupoles). *Alternating Gradient.*
- Second order: Chromatic Aberrations and corrections (sextupoles)
- Effects of perturbations, non-linearities
Dynamic Aperture.

Damping/Excitation of Longitudinal Oscillations

- Photon emission depends on particle energy (larger energy, more emission). This adds a **dissipative** term to the eqs. of motion.
- However, emission happens in the form of **discrete** events (photons). At each emission, there is a **sudden** change in particle energy (but no sudden change in particle position).
- Both effects together lead to an **equilibrium** state that defines the bunch dimensions in longitudinal phase space

Energy spread

Bunch length

$$\sigma_p^2 = C_q \frac{\gamma^2}{J_s} \frac{\left\langle \frac{1}{\rho^3} \right\rangle_s}{\left\langle \frac{1}{\rho^2} \right\rangle_s}$$

$$\sigma_l = \frac{c\alpha}{\Omega_s} \sigma_p$$

Depends on lattice

Damping/Excitation of Transverse Oscillations

- Discrete photon emission changes momentum along the direction of propagation. If this happens in a **dispersive** region of the magnet lattice, a transverse (betatron) oscillation will be **excited**.
- Momentum is regained at the RF cavity only along the longitudinal direction. This causes a reduction of the particle angles (**damping**).
- Both effects together lead to an **equilibrium** state that defines the transverse beam dimension and angular spread, i.e., the **emittance**.

$$\varepsilon_0 = C_q \frac{\gamma^2}{J_x} \left\langle \frac{1}{\rho^3} \right\rangle$$

Isomagnetic

$$\varepsilon_0 = C_q \frac{\gamma^2 \theta^3}{12 \sqrt{15} J_x} F$$

$H(s) = \beta(s) \left(\frac{1}{2} \frac{d\theta}{ds} \right)^2 + \gamma(s) \eta(s)^2$

Number of dipoles

Lattice

The Challenge of High Brightness Source Source Design: a beam dynamics perspective

