

Medium modification of charmed meson masses based on an effective chiral model

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@ Reimei Workshop: New exotic hadron matter
(Inha Univ., Incheon, Korea, October 24, 2016)

Based on

- M. Harada, Y.L. Ma, D. Suenaga, Y. Takeda, in preparation
- Y. Motohiro, Y. Kim, M. Harada, PRC92, 025201 (2015)
- D. Suenga, B.R. He, Y.L. Ma, M. Harada, PRD 91, 036001 (2015)

1. Introduction

Origin of Mass

of Hadrons

?

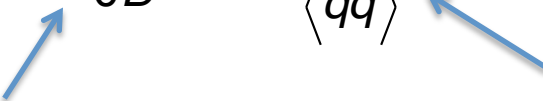
of Us

II

One of the Interesting problems of QCD

Chiral Invariant Mass of Hadrons ?

- Parity doublet model for light baryons
 - In [C.DeTar, T.Kunihiro, PRD39, 2805 (1989)], $N^*(1535)$ is regarded as the chiral partner to the $N(939)$ having the chiral invariant mass.

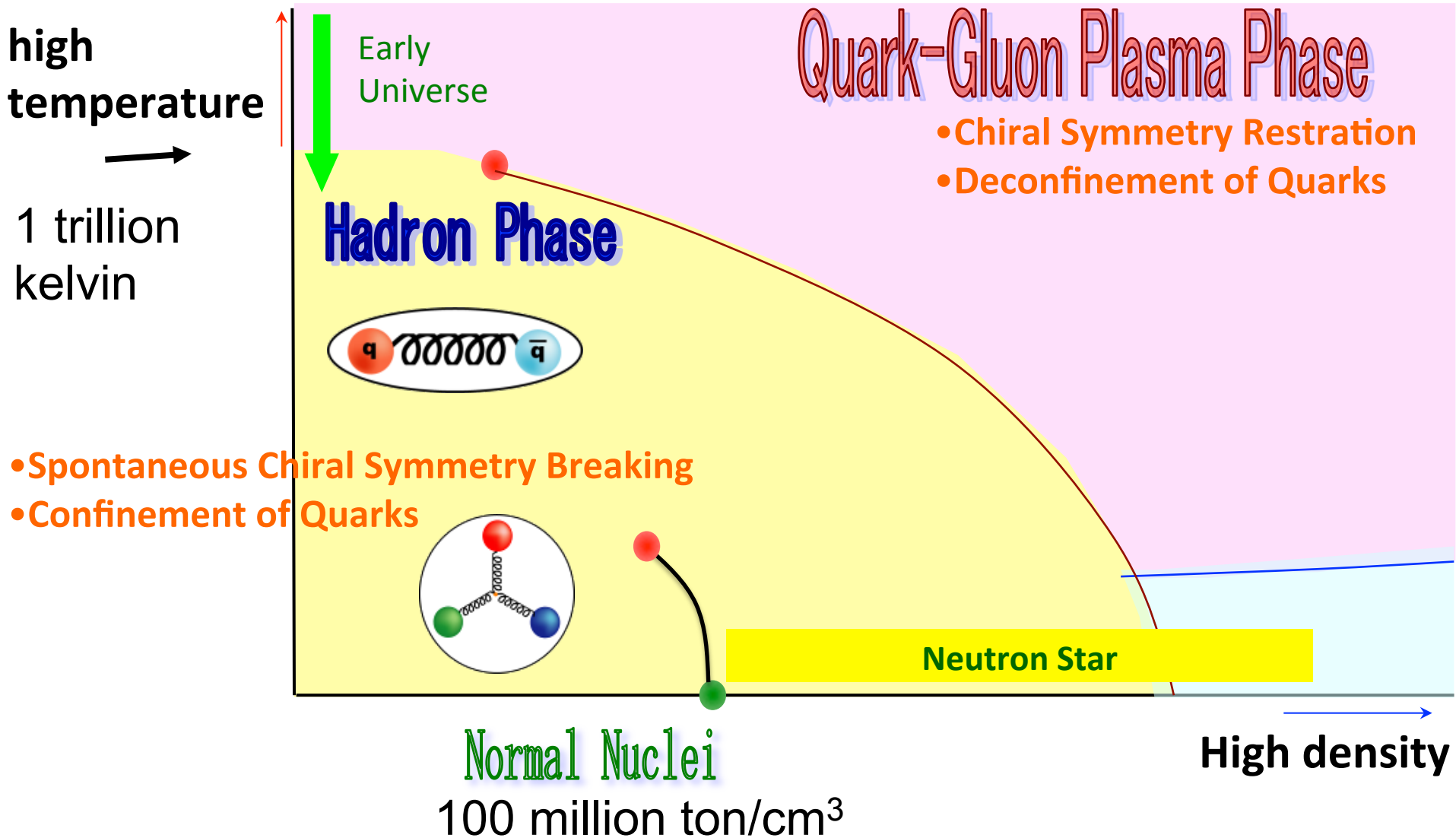
$$m_B = m_{0B} + m_{\langle \bar{q}q \rangle}$$


chiral invariant mass

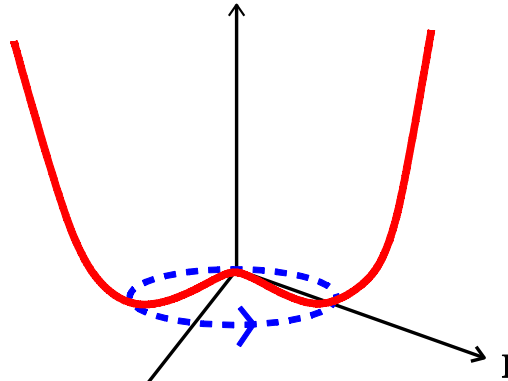
spontaneous chiral symmetry breaking

- How much mass of nucleon is from the spontaneous chiral symmetry breaking ?
- What is the value of the chiral invariant mass ?

Phase diagram of Quark-Gluon system

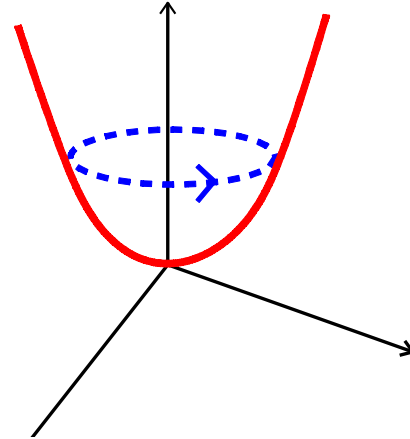


Important for understanding the spontaneous chiral symmetry breaking



chiral symmetry broken phase
at vacuum

$$\langle \bar{q}q \rangle \neq 0 \text{ (chiral condensate)}$$



chiral symmetric phase
at high T and/or density

$$\langle \bar{q}q \rangle = 0$$

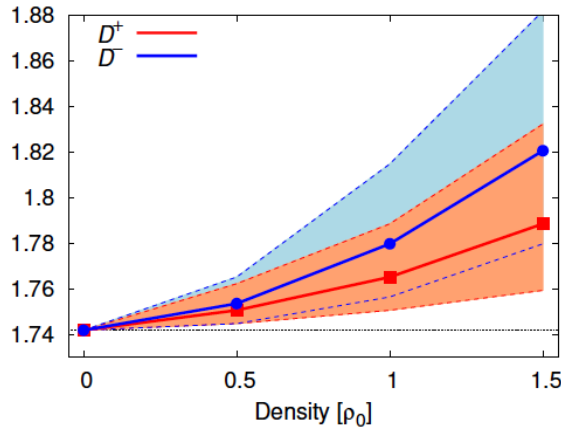
- The spontaneous chiral symmetry breaking is expected to generate a part of hadron masses.
- It causes mass difference between chiral partners.
- Changing T and/or density will cause some change of hadron masses.

In [Y. Motohiro, Y.Kim, M.Harada, Phys. Rev. C 92, 025201 (2015)], we studied nuclear matter using a parity doublet model, and showed some relations between the chiral invariant mass of nucleon and the phase structure. We also presented a density dependence of **the nucleon mass**, which **changes reflecting the partial chiral symmetry restoration**.

**What happens to the masses of charmed
hadrons in nuclear matter ?**

Medium modification of charmed meson masses

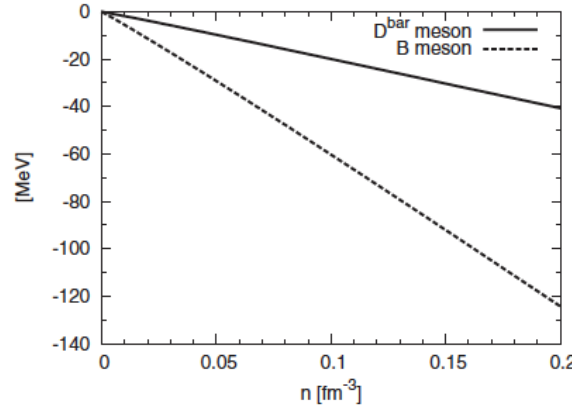
- QCD sum rule



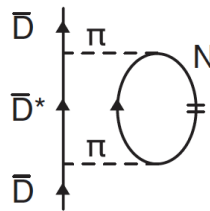
K.Suzuki, P.Gubler, M.Oka, PRC 93, 045209 (2016)

D meson mass is **increased** at finite density

- One-loop in an effective model

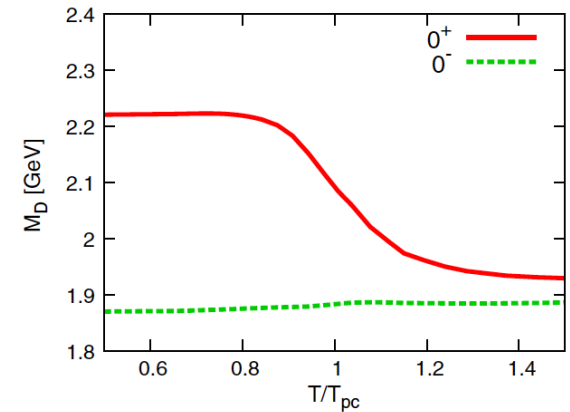


S.Yasui, K.Sudoh, PRC 87, 015202 (2013)

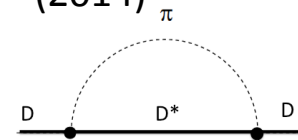


D meson mass is **decreased** at finite density

- One-loop in an effective model at finite temperature



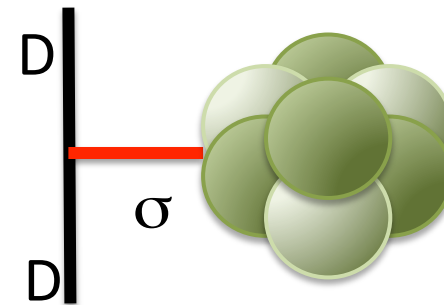
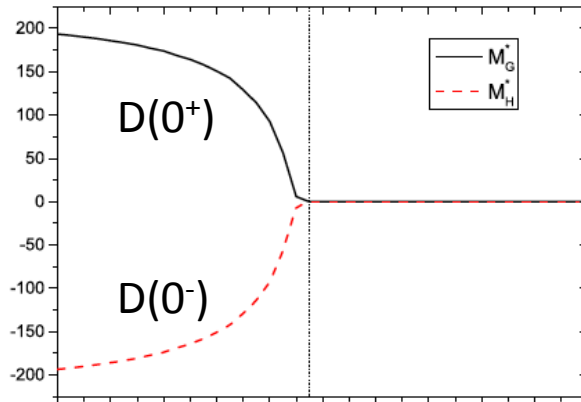
C.Sasaki, PRD 90, 114007 (2014)



D meson mass is **stable** at finite temperature

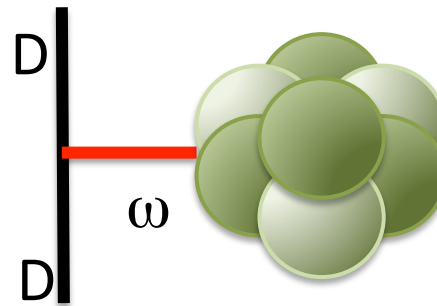
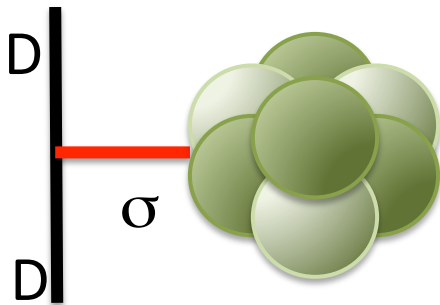
One boson exchange contribution

- Effective **sigma meson exchange contribution**
 - Nuclear matter is created in a Skyrme crystal approach
 - D meson ($J^P=0^-$) is included together with D_0^* ($J^P=0^+$) as the chiral partner
 - D.Suenga, B.R.He, Y.L.Ma. M.Harada, PRD 91, 036001 (2015)



- D meson ($J^P=0^-$) mass is **increased**,
- D_0^* ($J^P=0^+$) mass is **decreased**.
- They are **degenerate** when $\langle \sigma \rangle = 0$.

- In this talk, I introduce our recent work [M.Harada, Y.L.Ma, D.Suenaga, Y.Takeda, in preparation], where we study the charmed meson masses in nuclear matter through the **exchange of sigma and omega mesons**.
- In this talk, I focus on the density dependence in the matter described by **the parity doublet model**.



Outline

1. Introduction
2. Nuclear matter from a parity doublet model
3. Density dependence of effective masses of charmed mesons
4. Summary

2. Nuclear matter from a parity doublet model

Y. Motohiro, Y.Kim, M.Harada, Phys. Rev. C 92, 025201 (2015)

Parity Doublet model

C.DeTar, T.Kunihiro, PRD39, 2805 (1989)

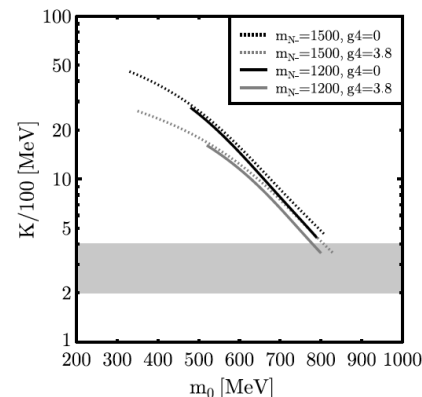
D.Jido, M.Oka, A.Hosaka, PTP106, 873 (2001)

- An excited nucleon with negative parity such as $N^*(1535)$ is regarded as the chiral partner to the $N(939)$ which has the positive parity.
- These nucleons have a chiral invariant mass in addition to the mass generated by the spontaneous chiral symmetry breaking.
- The chiral symmetry is spontaneously broken by the sigma condensate, $\langle \sigma \rangle \neq 0$.

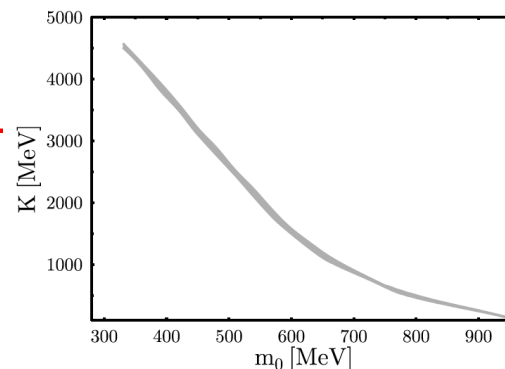
Nuclear matter in parity doublet models

- A parity doublet model including omega meson with 4-point interaction is used in a Walecka-type mean field analysis.
 - Large value of m_0 is needed to reproduce the incompressibility.
- Rho meson is further included with 4-point interaction.
 - $m_0 > 800$ MeV is needed to have $100 < K < 400$ MeV
- In our analysis [Y.Motohiro, Y.Kim, M.Harada, Phys. Rev. C 92, 025201 (2015)], we construct a model with a **6-point interaction of sigma**, but without 4-point interaction for vector mesons.
- Our results show that **$K = 240$ MeV is reproduced for $m_0 > 500$ MeV.**

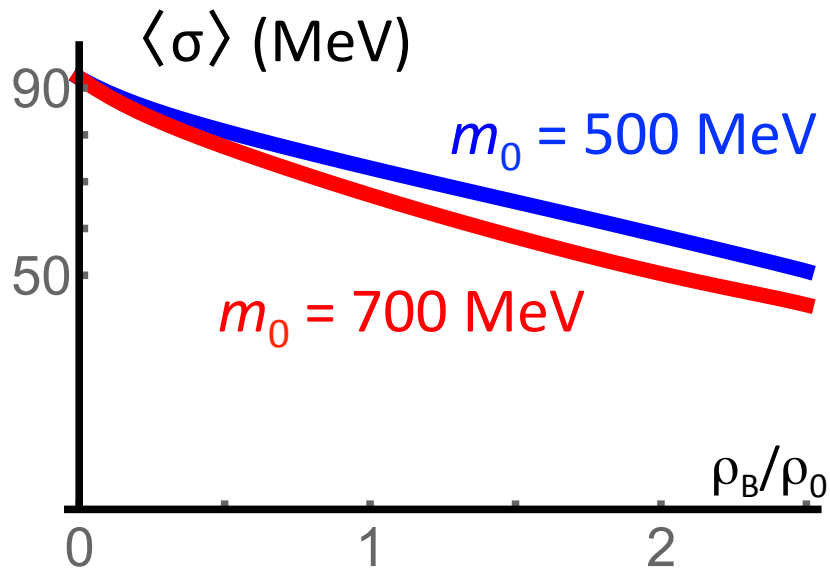
D.Zschesche et al.,
PRC75, 055202 (2007)



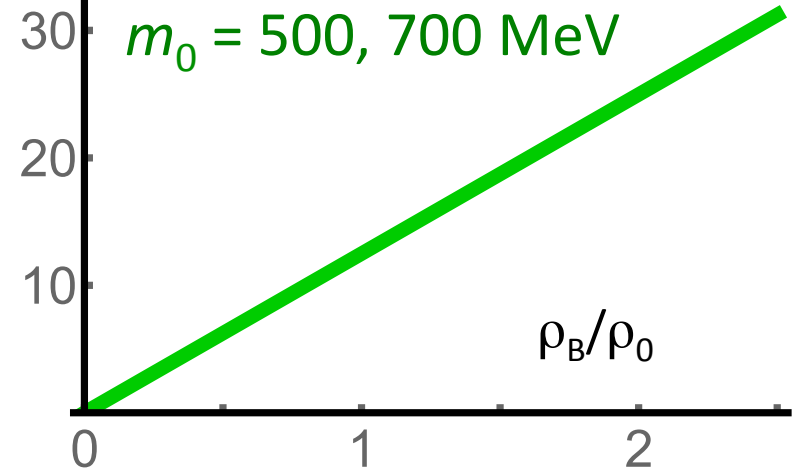
V.Dexheimer et al.,
PRC77, 025803 (2008)



Mean fields



$$\langle \omega \rangle = \frac{g_{\omega NN}}{m_\omega^2} \rho_B \quad (\text{MeV})$$



3. Density dependence of effective masses of charmed mesons

M. Harada, Y.L. Ma, D. Suenaga, Y. Takeda, in preparation

Chiral partner structure for charmed mesons

- M.A.Nowak, M.Rho and I.Zahed, PRD48, 4370 (1993)
- W.A.Bardeen and C.T.Hill, PRD49, 409 (1994)

- 2 heavy quark multiplets with $J_f=1/2$ are regarded as the chiral partner:

$$\left[D(0^-), D^*(1^-) \right] \xleftrightarrow{\text{chiral partner}} \left[D_0^*(0^+), D_1(1^+) \right]$$

- Mass difference is generated by the chiral condensate, and the value is roughly equal to the constituent quark mass.
- Experimental value implies that the chiral partner structure seems to work:

$$m(0^+) - m(0^-) \approx m(1^+) - m(1^-) \approx 0.43 \text{ GeV}$$

An effective Lagrangian

- 2 Heavy meson doublets for $J^P = (0^-, 1^-), (0^+, 1^+)$ mesons

$$H = \frac{1 + v^\mu \gamma_\mu}{2} [D_\mu^* \gamma^\mu + i D \gamma_5] , \quad G = \frac{1 + v^\mu \gamma_\mu}{2} [D_0^* - i \gamma^\mu D'_{1\mu} \gamma_5]$$

- Chiral fields

$$\mathcal{H}_R = \frac{1}{\sqrt{2}} [G + i H \gamma_5] , \quad \mathcal{H}_L = \frac{1}{\sqrt{2}} [G - i H \gamma_5] , \quad \omega_\mu , \quad M = \sigma + i \sum_{a=1}^3 \pi_a \tau_a$$

$$\mathcal{H}_{R,L} \rightarrow \mathcal{H}_{R,L} g_{R,L}^\dagger \quad \omega_\mu \rightarrow \omega_\mu \quad M \rightarrow g_L M g_R^\dagger , \quad (g_{R,L} \in \text{SU}(2)_{R,L})$$

- Spontaneous chiral symmetry breaking : $\langle \sigma \rangle \neq 0$
- An effective Lagrangian invariant under chiral symmetry

$$\begin{aligned} \mathcal{L}/m = & \text{tr} [\mathcal{H}_L (i v \cdot \partial) \bar{\mathcal{H}}_L] + \text{tr} [\mathcal{H}_R (i v \cdot \partial) \bar{\mathcal{H}}_R] \\ & - g_{\omega DD} \text{Tr} [\mathcal{H}_L v^\mu \omega_\mu \bar{\mathcal{H}}_L + \mathcal{H}_R v^\mu \omega_\mu \bar{\mathcal{H}}_R] \\ & + \frac{\Delta_M}{2f_\pi} \text{tr} [\mathcal{H}_L M \bar{\mathcal{H}}_R + \mathcal{H}_R M^\dagger \bar{\mathcal{H}}_L] \\ & - i \frac{g_A}{2f_\pi} \text{tr} [\mathcal{H}_R \gamma_5 \gamma^\mu \partial_\mu M^\dagger \bar{\mathcal{H}}_L - \mathcal{H}_L \gamma_5 \gamma^\mu \partial_\mu M \bar{\mathcal{H}}_R] \end{aligned}$$

Masses of charmed mesons in nuclear matter

- Relevant interactions for $D(J^P=0^-)$, $D(J^P=0^+)$

$$\begin{aligned}\mathcal{L}/m = & -2D \left[v^\mu (i\partial_\mu + g_{\omega DD} \omega_\mu) - \frac{1}{2} \Delta_M \frac{\sigma}{f_\pi} \right] D^\dagger \\ & + 2D_0^* \left[v^\mu (i\partial_\mu + g_{\omega DD} \omega_\mu) + \frac{1}{2} \Delta_M \frac{\sigma}{f_\pi} \right] (D_0^*)^\dagger\end{aligned}$$

- Effective masses for $D(J^P=0^-)$, $D(J^P=0^+)$ in nuclear matter

$$m_{D(-)}^{(\text{eff})} = m - \frac{1}{2} \Delta_M \frac{\langle \sigma \rangle}{f_\pi} + g_{\omega DD} \langle \omega_0 \rangle$$

$$m_{D(+)}^{(\text{eff})} = m + \frac{1}{2} \Delta_M \frac{\langle \sigma \rangle}{f_\pi} + g_{\omega DD} \langle \omega_0 \rangle$$

- Effective masses for anti-charmed mesons

$$m_{\bar{D}(-)}^{(\text{eff})} = m - \frac{1}{2} \Delta_M \frac{\langle \sigma \rangle}{f_\pi} - g_{\omega DD} \langle \omega_0 \rangle$$

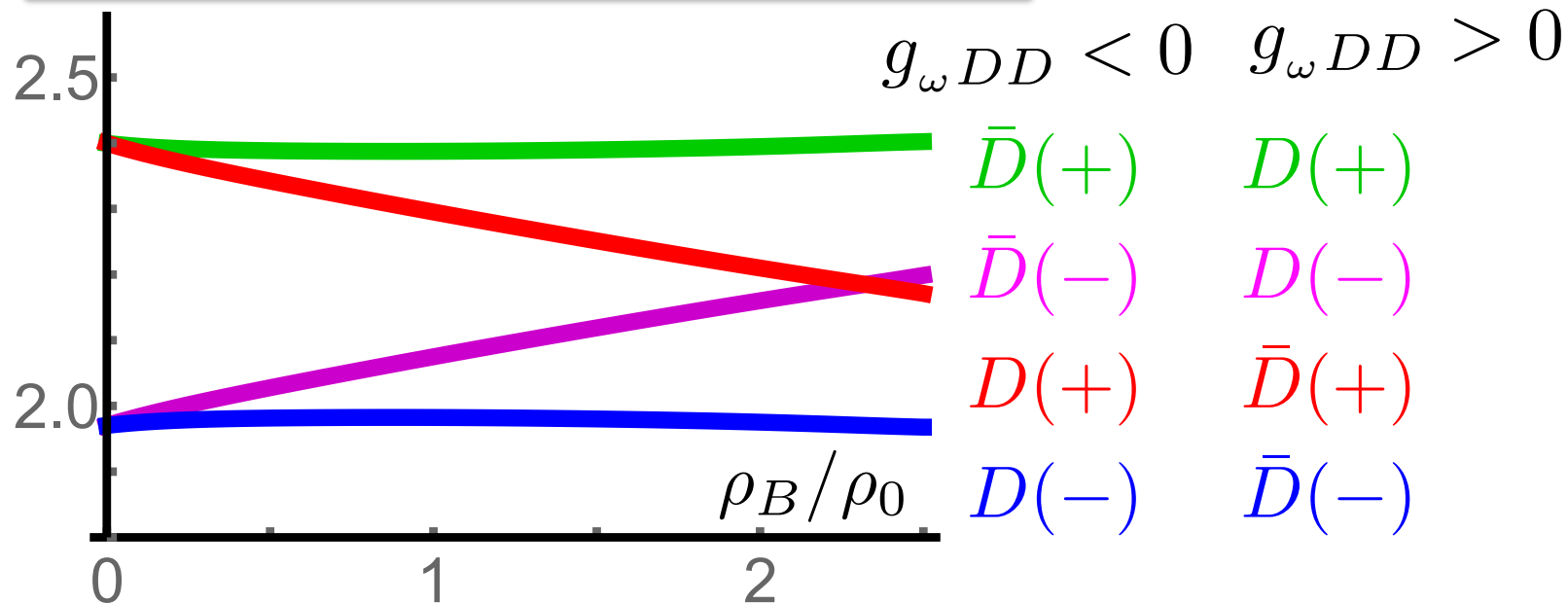
$$m_{\bar{D}(+)}^{(\text{eff})} = m + \frac{1}{2} \Delta_M \frac{\langle \sigma \rangle}{f_\pi} - g_{\omega DD} \langle \omega_0 \rangle$$

Charmed meson masses

$$m_{D(-)}^{(\text{eff})} = m - \frac{1}{2}\Delta_M \frac{\langle\sigma\rangle}{f_\pi} + g_{\omega DD} \langle\omega_0\rangle \quad m_{\bar{D}(-)}^{(\text{eff})} = m - \frac{1}{2}\Delta_M \frac{\langle\sigma\rangle}{f_\pi} - g_{\omega DD} \langle\omega_0\rangle$$

$$m_{D(+)}^{(\text{eff})} = m + \frac{1}{2}\Delta_M \frac{\langle\sigma\rangle}{f_\pi} + g_{\omega DD} \langle\omega_0\rangle \quad m_{\bar{D}(+)}^{(\text{eff})} = m + \frac{1}{2}\Delta_M \frac{\langle\sigma\rangle}{f_\pi} - g_{\omega DD} \langle\omega_0\rangle$$

An example $|g_{\omega DD}| = 3.4$



Increasing or decreasing of pseudo-scalar D(-) meson mass only is not enough for measuring the partial chiral symmetry restoration.

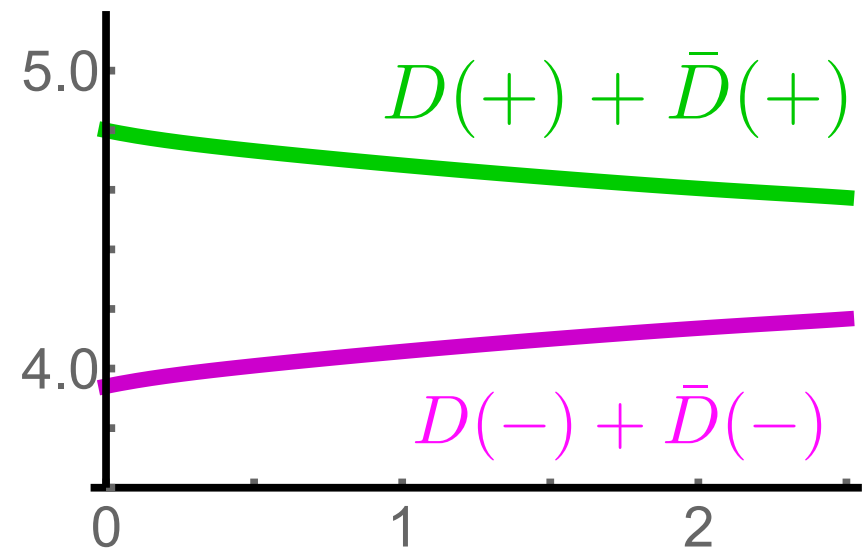
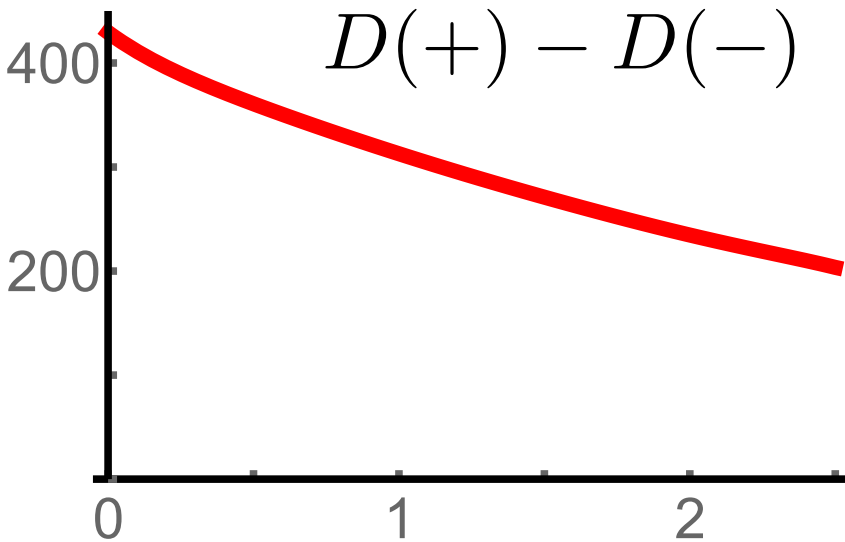
Partial chiral symmetry restoration

$$m_{D(-)}^{(\text{eff})} = m - \frac{1}{2}\Delta_M \frac{\langle\sigma\rangle}{f_\pi} + g_{\omega DD} \langle\omega_0\rangle$$

$$m_{D(+)}^{(\text{eff})} = m + \frac{1}{2}\Delta_M \frac{\langle\sigma\rangle}{f_\pi} + g_{\omega DD} \langle\omega_0\rangle$$

$$m_{\bar{D}(-)}^{(\text{eff})} = m - \frac{1}{2}\Delta_M \frac{\langle\sigma\rangle}{f_\pi} - g_{\omega DD} \langle\omega_0\rangle$$

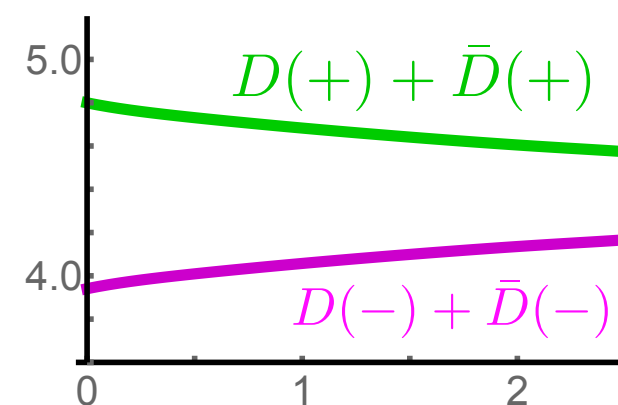
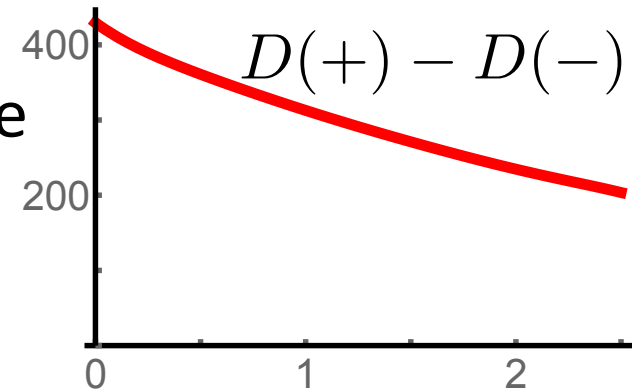
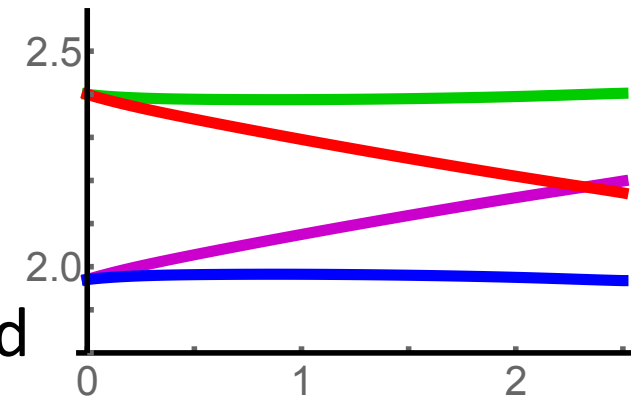
$$m_{\bar{D}(+)}^{(\text{eff})} = m + \frac{1}{2}\Delta_M \frac{\langle\sigma\rangle}{f_\pi} - g_{\omega DD} \langle\omega_0\rangle$$



- In addition to study the mass difference of chiral partners, taking average of particle and anti-particle will give a clue for partial chiral symmetry restoration.
- Threshold energy for production of D and anti-D meson pair in medium is larger than vacuum reflecting the partial chiral symmetry restoration.

4. Summary

- We studied density dependence of charmed meson masses from the **mean field** contributions of **sigma** and **omega** mesons in the nuclear medium described in the **parity doublet model**.
- Increasing or decreasing of $D(-)$ meson mass only is not enough for measure the chiral symmetry restoration.
- In addition to study the **mass difference of chiral partners**, taking **average of particle and anti-particle** will give a clue for partial chiral symmetry restoration.
- Threshold energy for **production of D and anti- D meson pair** in medium is **larger** than vacuum reflecting the partial chiral symmetry restoration.



The End