

QCD critical point and photons in heavy-ion collisions

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Introduction

■ Beam energy scans: exploration of QCD phase diagram

- RHIC (BNL)

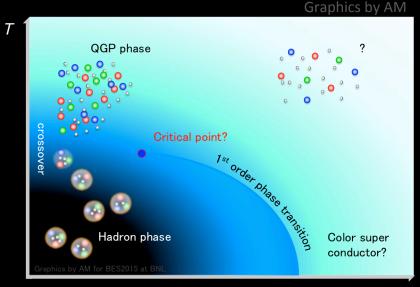
Phase I (2009-11): 7.7-62.4 GeV

Phase II (2017-20?): 3.0 GeV?

- FAIR (GSI), NICA (JINR), SPS (CERN), J-PARC etc.

+ LHC (CERN): 5.5 TeV

We use hydrodynamics to:



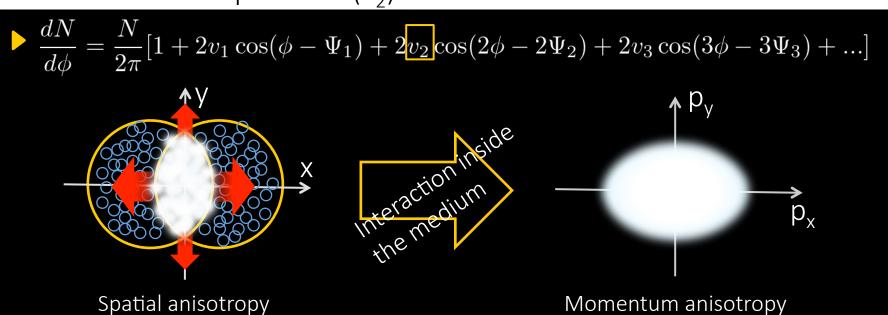
 $\mu_{\rm E}$



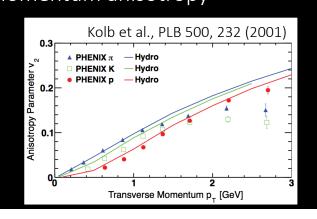
- ▶ Look for signals of a QCD critical point
- \blacktriangleright Determine the QGP properties at finite T, $\mu_{\rm B}$
- Understand the origin of "fluidity"

Introduction

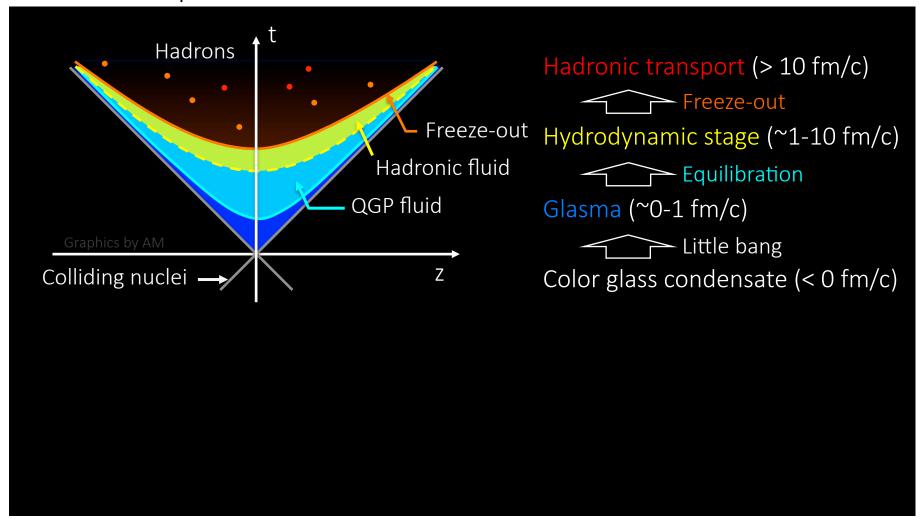
■ Observable: Elliptic flow (v_2)



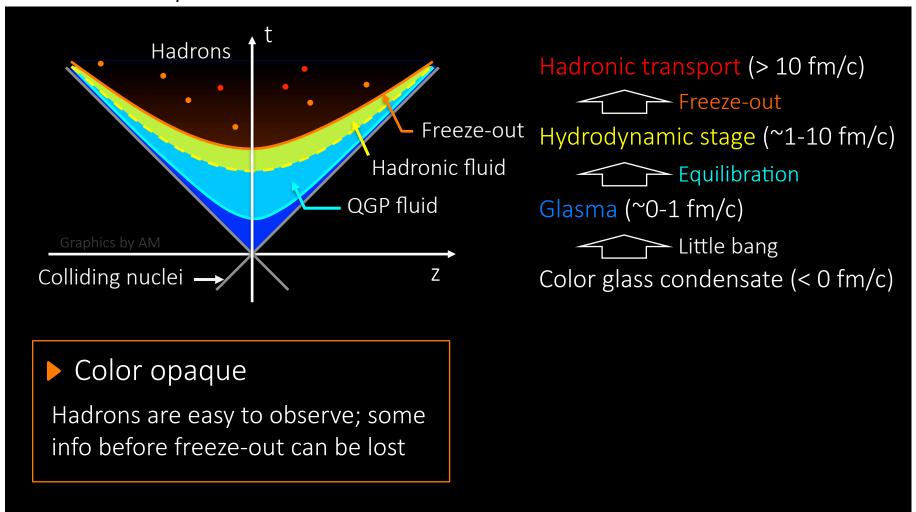
- ▶ Hadron v_2 is found to be large
 - It follows hydrodynamic description
 - An "evidence" for strongly-coupled QGP early equilibration of bulk medium (τ < 1 fm/c)



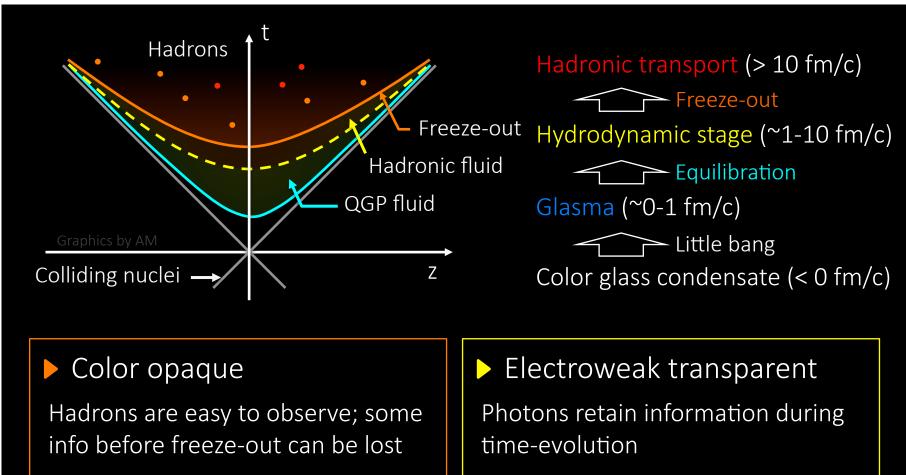
Hadronic point of view



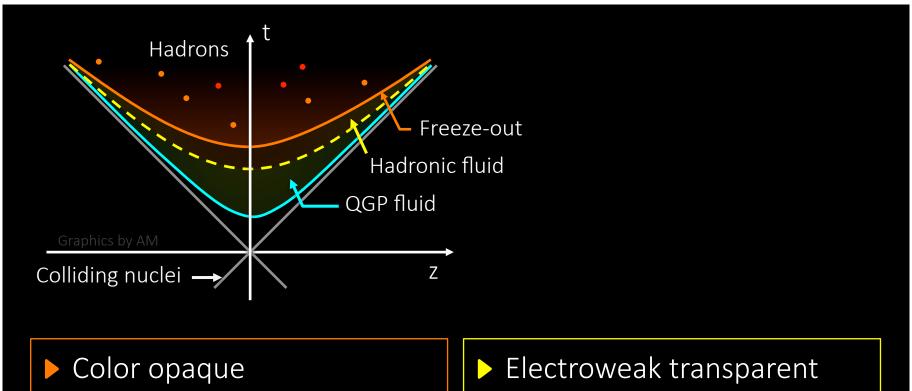
Hadronic point of view



Photonic point of view



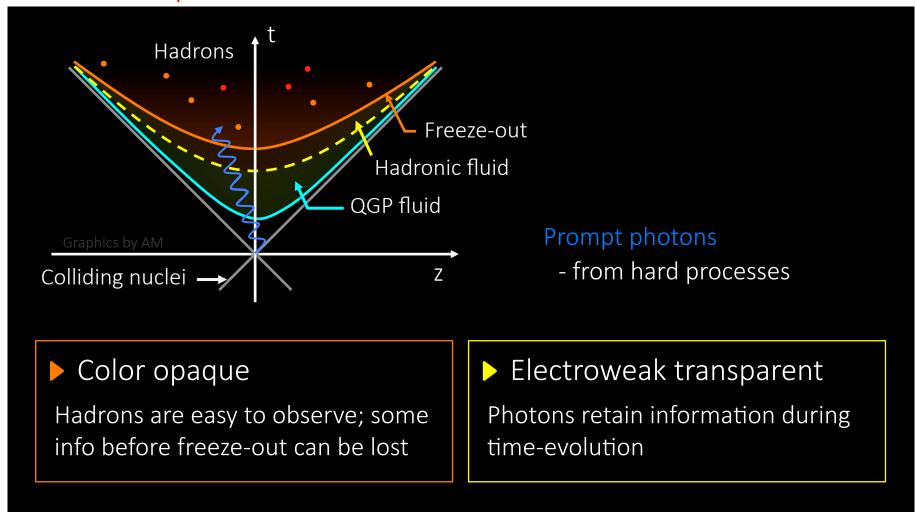
Photonic point of view



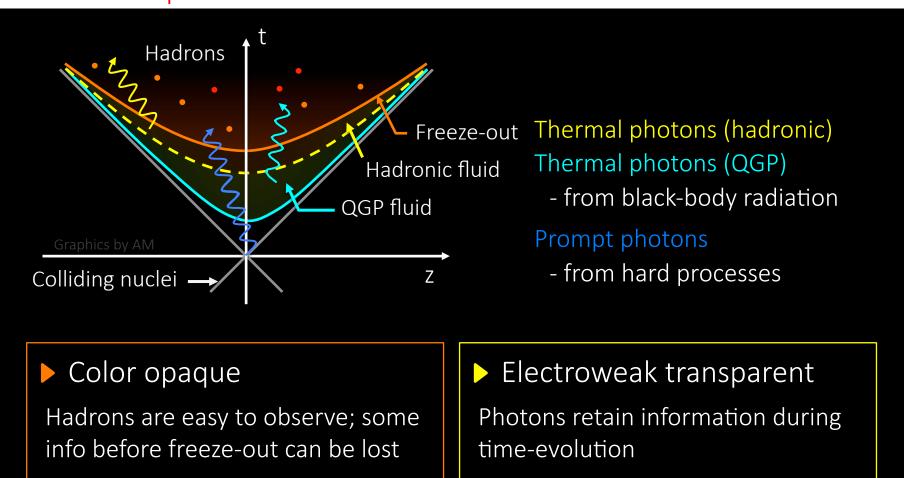
Hadrons are easy to observe; some info before freeze-out can be lost

Photons retain information during time-evolution

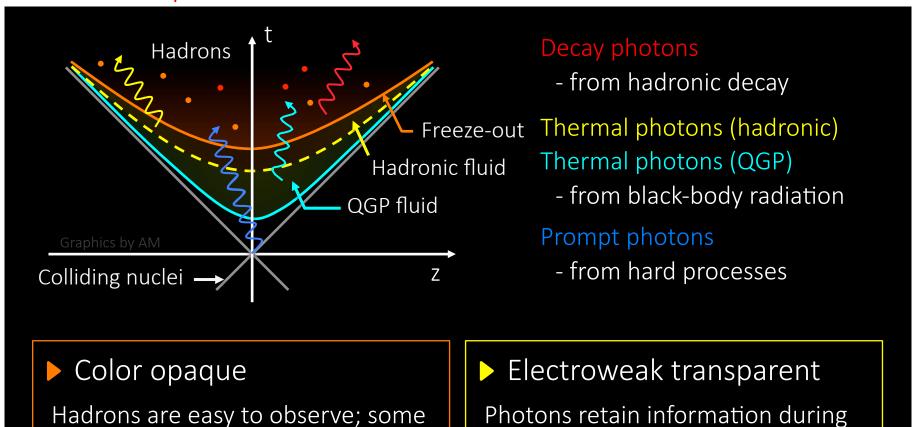
Photonic point of view



Photonic point of view



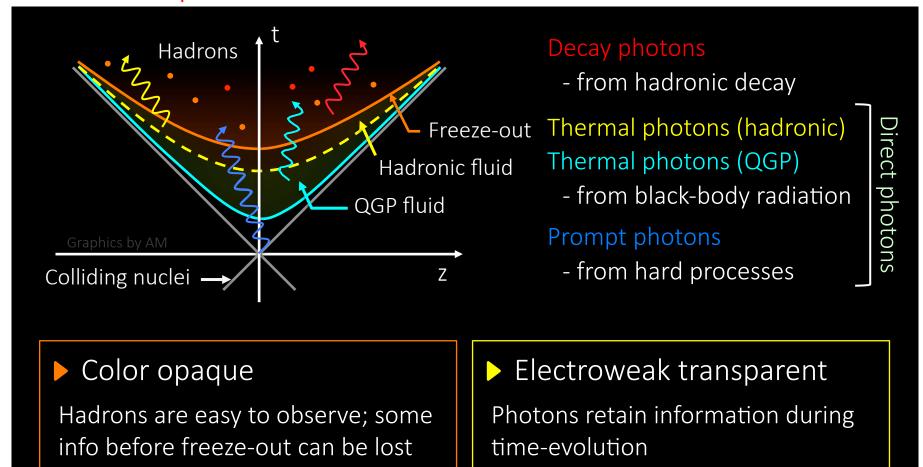
Photonic point of view



time-evolution

info before freeze-out can be lost

Photonic point of view

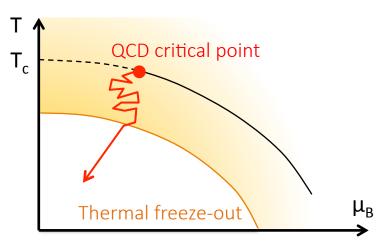


Observable?

AM, Y. Yin and S. Mukherjee, arXiv:1606.00771

QCD critical point (QCP) vs. Thermal freeze-out

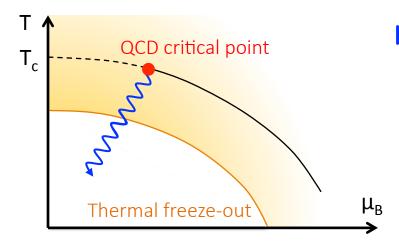
PART 1



QCD medium is thermalized; colored objects (hadrons) are scattered

Signals can be washed away unless

- 1. QCP is near enough to freeze-out
- 2. Its effect on evolution is large enough



▶ Thermal photons penetrate through the medium

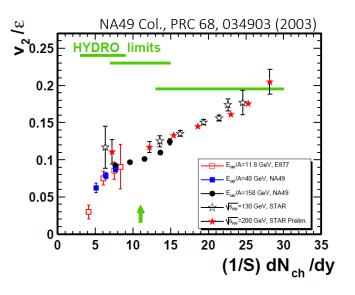
Can the QCP signals be more direct?

PART 2

AM, Y. Yin and S. Mukherjee, In preparation

Hydrodynamic model for BES

A path we have been through

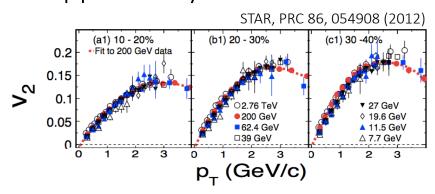


Integrated v₂ becomes small at lower E

"HYDRO limits" estimated with

- + Analytical Glauber model
- + EoS with 1st order PT
- + Ideal hydro Kolb et al., PRC62, 054909 (2000)
- Once thought hydro is only for AA at top energies (which may still be true)

Applicability tests



- Differential v₂ stays large
- We should see if the state-of-art hydrodynamic interpretations work

Equations to solve

■ Relativistic formalism

Energy-momentum conservation $\partial_{\mu}T^{\mu\nu}=0$

Baryon conservation $\partial_{\mu}N_{B}^{\mu}=0$

+ | Equation of state $P = P(e, n_B)$

Ideal hydrodynamics

Equations to solve

■ Relativistic formalism

Energy-momentum conservation $\partial_{\mu}T^{\mu\nu}=0$

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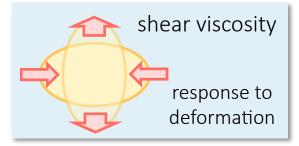
Shear viscosity $\pi^{\mu\nu}=2\eta\nabla^{\langle\mu}u^{\nu\rangle}-\tau_\pi D\pi^{\langle\mu\nu\rangle}+\dots$

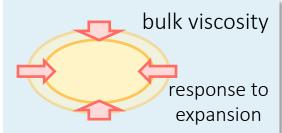
Bulk viscosity $\Pi = -\zeta \nabla_{\mu} u^{\mu} - \tau_{\Pi} D\Pi + \dots$

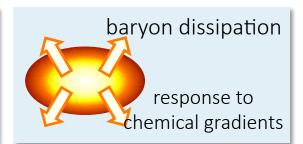
Baryon diffusion $V_B^{\mu} = \kappa_{V_B} \nabla^{\mu} \frac{\mu_B}{T} - \tau_{V_B} \Delta^{\mu\nu} DV_{\nu} + \dots$

Ideal hydrodynamics

Dissipative hydrodynamics







Near the QCD critical point

Bulk viscosity becomes dominant

• Shear viscosity $\eta = \xi^{(4-d)/19}$

 ξ : correlation length

Bulk viscosity: $\zeta = \xi^3$

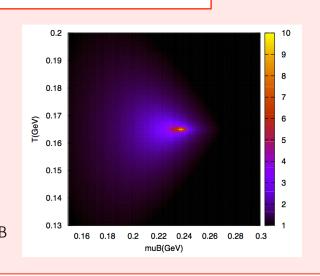
Baryon diffusion: $D_B = \xi^{-1}$



We focus on bulk viscosity and investigate how particle distributions are modified

Parameterization for bulk vicosit

$$\zeta = \zeta_0 \left(\frac{\xi_{\rm eq}}{\xi_0}\right)^3$$
 where $\zeta_0 = 2\left(\frac{1}{3}-c_s^2\right)\frac{e+P}{4\pi T}$ AdS/CFT by A. Buchel, PLB 663, 286 (2008)
$$\xi = \text{that of Ising model mapped on T-}\mu_{\rm B}$$

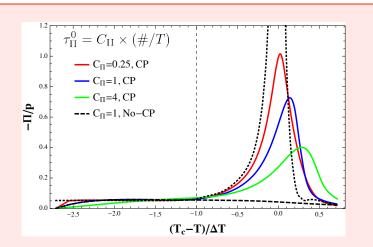


Near the QCD critical point

- Bulk viscosity becomes dominant
 - ▶ Relaxation time

$$au_\Pi = au_{\Pi,0} igg(rac{\xi_{
m eq}}{\xi_0}igg)^3$$
 as causality suggests

$$\lim_{k \to \infty} \frac{d\omega}{dk} = \sqrt{c_s^2 + \frac{\zeta}{\tau_{\Pi}(\epsilon + P)}} < 1$$



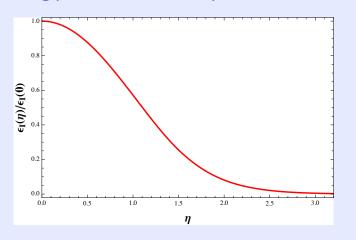
- Causal hydrodynamics is applicable because Π is "frozen" for large τ_Π
- Bulk viscous relaxation time from AdS/CFT approach

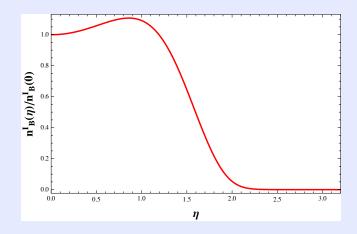
$$au_{\Pi,0} = C_{\Pi} rac{18 - (9 \ln 3 - \sqrt{3}\pi)}{24\pi T}$$
 (C_{\Pi} = 1)

avoids the issue of cavitation $(\Pi > P)$

Initial conditions

- Longitudinal distribution
- H. J. Drescher and Y. Nara, PRC 75, 034905; 76, 041903Y. Mehtar-Tani and G. Wolschin, PRL 102, 182301; PRC 80, 054905
- Color glass models extrapolated to lower energies for the shapes of energy and net baryon distribution





Energy density peaks at $\eta=0$, while net baryon density at finite η

Chemical potential is larger at forward rapidity η

* $\eta_s = \frac{1}{2} \ln \frac{t+z}{t-z}$ is the "angle" of hyperbolic coordinate

Equation of state

■ Hadron resonance gas + lattice QCD AM and B. Schenke, Phys. Lett. B 752, 317 (2016)

Lattice QCD has a sign problem at finite density

Taylor expansion up to the 4th order is used for QGP phase

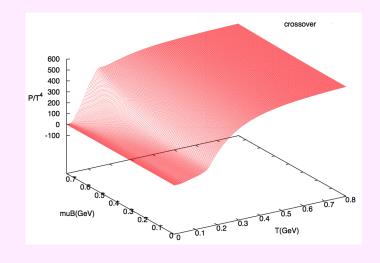
$$rac{P}{T^4} = rac{P_0}{T^4} + rac{1}{2}\chi_B^{(2)} igg(rac{\mu_B}{T}igg)^2 + rac{1}{4!}\chi_B^{(4)} igg(rac{\mu_B}{T}igg)^4 + \mathcal{O}igg(rac{\mu_B}{T}igg)^6$$

HotQCD, PRD 90, 094503 (2014), PRD 86, 034509 (2012), PRD 92, 074043 (2015)

$$\frac{P}{T^4} = \frac{1}{2} \left[1 - \tanh \frac{T - T_c(\mu_B)}{\Delta T_c} \right] \frac{P_{\text{HRS}}(T)}{T^4}$$
$$+ \frac{1}{2} \left[1 + \tanh \frac{T - T_c(\mu_B)}{\Delta T_c} \right] \frac{P_{\text{lat}}(T_s)}{T_s^4}$$

where

$$T_c = 0.166 - c(0.139\mu_B^2 + 0.053\mu_B^4)$$
$$T_s = T + d[T_c(0) - T_c(\mu_B)]$$

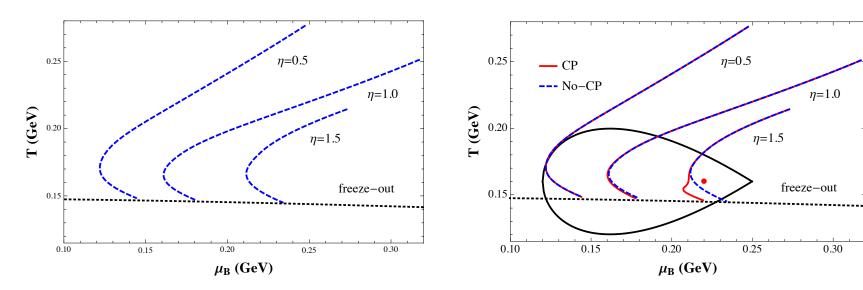


*Currently no QCP; effects of 1st order phase transition may not be dramatic

Trajectories on μ_B -T plane

■ 1+1 dimensional hydrodynamic demonstration

AM, Y. Yin and S. Mukherjee, arXiv:1606.00771

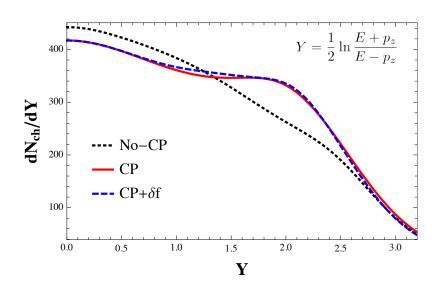


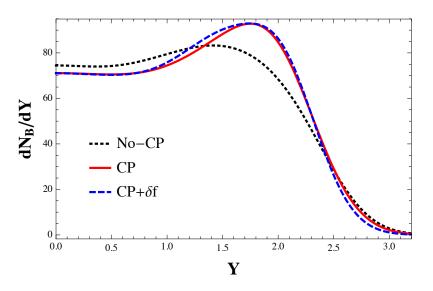
- Critical point is placed by hand at $(\mu_B, T) = (0.22 \text{ GeV}, 0.16 \text{ GeV})$ by mapping the critical region of Ising model onto the μ_B -T plane
- If the QCP exists, the trajectory is pushed away from it on the lower μ_B side because of bulk viscous entropy production

Rapidity distributions

■ 1+1 dimensional hydrodynamic demonstration

AM, Y. Yin and S. Mukherjee, arXiv:1606.00771



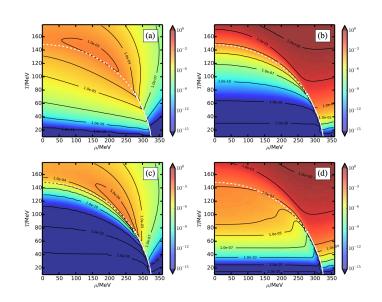


- Charged particle and net baryon distributions are deformed if the critical point is contacted
- dN_{ch}/dy deformation is caused by entropy production and enhanced flow convection due to the reduction in effective pressure P - Π
- dN_B/dy deformation is by convection only

Thermal photons

Does emission rate contains a signal of QCP?

Few studies on the emission rate at finite density in the vicinity



Linear sigma model suggests no dramatic enhancement at QCP

F. Wunderlich and B. Kämper., PoS CPOD 2014, 027 (2015)



Bulk viscosity can change the emission rate via the distortion of the phase-space distribution

$$E\frac{dR_i}{d^3p} = \int \frac{d^3p_1}{2E_1(2\pi)^3} \frac{d^3p_2}{2E_2(2\pi)^3} \frac{d^3p_3}{2E_3(2\pi)^3} (2\pi)^4 \delta(p_1^{\mu} + p_2^{\mu} - p_3^{\mu} - p^{\mu}) |\mathcal{M}_i|^2 f_1(E_1) f_2(E_2) [1 \pm f_3(E_3)]$$

Bulk viscous corrections

- How to determine δf_{bulk}
 - Step 1: Expand the exponent y^i in $f^i = \frac{1}{\exp{(y^i)} \mp 1}$ around equilibrium in terms of Π

The tensor structure allowed in Israel-Stewart theory is

$$\delta y^{i} = [b_{i}D_{\Pi}u_{\mu}p_{i}^{\mu} + B_{\Pi}g_{\mu\nu}p_{i}^{\mu}p_{i}^{\nu} + (\tilde{B}_{\Pi} - B_{\Pi})p_{i}^{\mu}p_{i}^{\nu}]\Pi$$

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Step 2: Have it satisfy the self-consistency conditions

$$\delta T^{\mu\nu} = \sum_{i} \int \frac{g_{i} d^{3} p}{(2\pi)^{3} E_{i}} p_{i}^{\mu} p_{i}^{\nu} \delta f^{i} \qquad \delta N_{J}^{\mu} = \sum_{i} \int \frac{q_{i}^{J} g_{i} d^{3} p}{(2\pi)^{3} E_{i}} p_{i}^{\mu} \delta f^{i}$$

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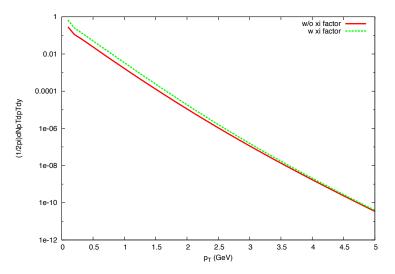
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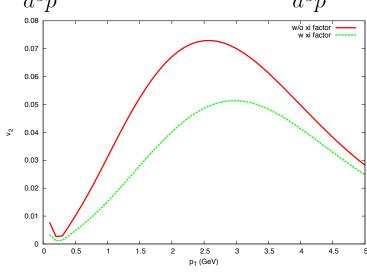
We have the coefficients

$$\begin{split} D_{\Pi} &= 3(J_{40}J_{31}^B - J_{41}J_{30}^B)\mathcal{J}_3^{-1} & \mathcal{J}_3 = 5J_{42}J_{30}^BJ_{30}^B + 3J_{31}^BJ_{40}J_{31}^B + 3J_{41}J_{41}J_{20}^{BB} \\ B_{\Pi} &= (J_{30}^BJ_{30}^B - J_{40}J_{20}^{BB})\mathcal{J}_3^{-1} & -3J_{31}^BJ_{41}J_{30}^B - 3J_{41}J_{30}^BJ_{31}^B - 5J_{42}J_{40}J_{20}^{BB} \\ \tilde{B}_{\Pi} &= 3(J_{41}J_{20}^{BB} - J_{30}^BJ_{31}^B)\mathcal{J}_3^{-1} & J_{mn} : \text{momentum integrals of } f_0^i \end{split}$$

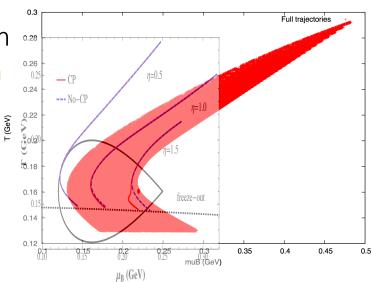
Critical enhancement

■ (2+1)-D hydrodynamic tests with $E\frac{dR}{d^3p} = [1 + 0.1(\xi/\xi_0)^3] \times E\frac{dR_0}{d^3p}$





- The magnitude and sign of correction is sensitive to the shape and location of the critical region
- Early emission leads to small momentum anisotropy v₂
- Work in progress stay tuned



Summary and outlook

- QCD critical point is a hot topic in heavy-ion collisions
- Bulk viscosity can become dominant near QCP
- Medium evolution itself can be affected if the system came across QCP
 - Trajectories and rapidity distributions are warped by entropy production and enhanced convection
- Thermal photons can be a good signal of QCP
 - Bulk viscous enhancement is a key
- Full estimation of off-equilibrium and finite-density photon emission rate is important (work in progress)
- Will be interesting to have the photon data from BES-RHIC, SPS, FAIR, NICA etc.

Fin

Merci!