

First results about elliptic flow with a unified approach at RHIC energies

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Rencontres QGP France - 10-13 October 2016 at Etretat

Overview

- 1 Introduction
- 2 Unified Approach
- 3 Elliptic Flow
- 4 Results
- 5 Conclusion

Introduction

Unified Approach : **EPOS**

- **E**nergy conserving quantum mechanical multiple scattering approach
- based on **P**artons, parton ladders, strings
- **O**ff-shell remnants
- **S**plitting of parton ladder

Introduction

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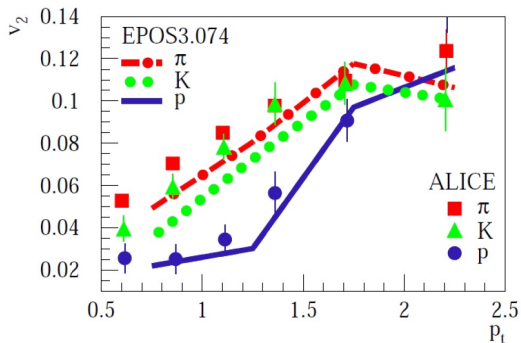
My Work → simplification of EPOS

At the end of Ph D → open-diffusion of EPOS ?

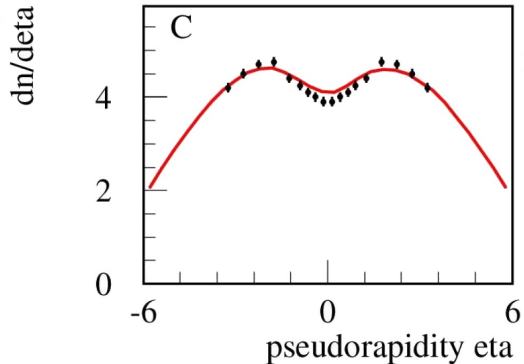
Unified Approach

EPOS reproduce a lot of observables

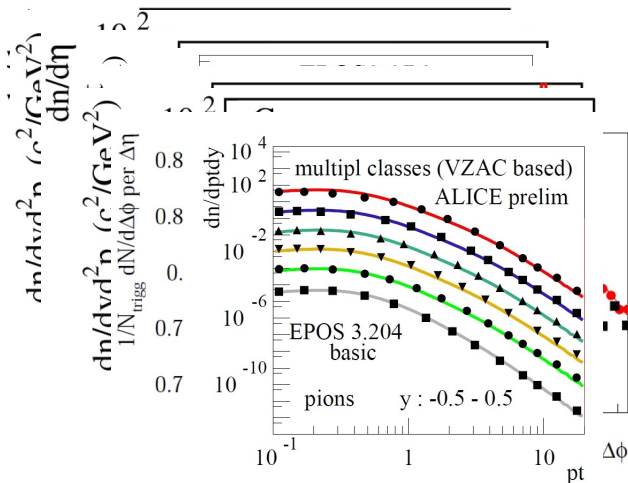
Unified Approach



Unified Approach



Unified Approach

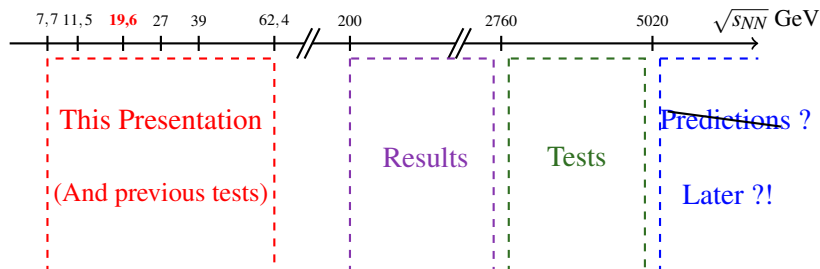


Unified Approach

When do we use EPOS ?

Monte Carlo Method

Model for very high energy.



Unified Approach

How we construct one event ?

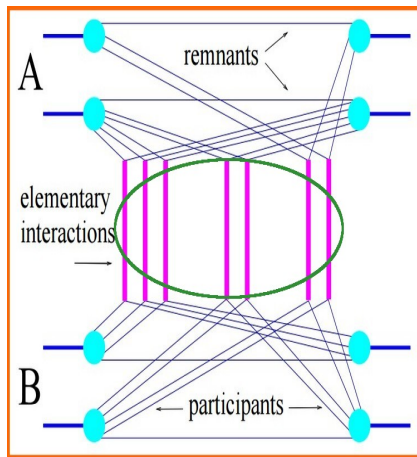
Universal Model for all collisions

Same procedure applies, based on several stages :

- ➊ Initial Conditions
- ➋ Core-Corona Approach
- ➌ Viscous hydrodynamic expansion
- ➍ Statistical hadronization
- ➎ Final state hadronic cascade

Unified Approach

Parton-Based-Gribov-Regge-Theory (PBGRT)



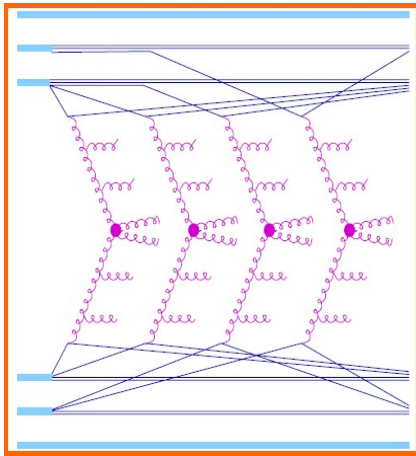
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- Interaction between partons are : **Pomeron** : treated by Quantum Field Theory
- Energy conserved by participants and remnants partons

H. J. Drescher, M. Hladik, S. Ostapchenko, T. Pierog and K. Werner, Phys. Rept. **350**, 93 (2001)

Unified Approach

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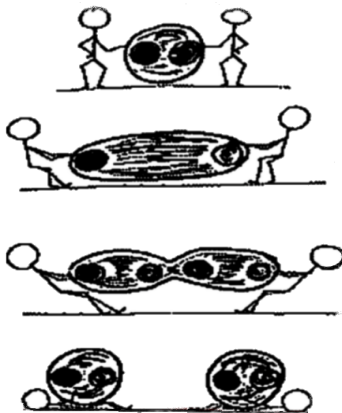
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-
- Interaction between partons are : **Pomeron** : treated by Quantum Field Theory
 - Energy conserved by participants and remnants partons
 - Pomerons become Partons Ladders
 - Partons Ladders become Strings

H. J. Drescher, M. Hladik, S. Ostapchenko, T. Pierog and K. Werner, Phys. Rept. **350**, 93 (2001)

Unified Approach

Lund Model : A phenomenological model of hadronization

- Initial Conditions
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- String without mass and without color between two partons
- **Tension proportional to length**
- When the potential is sufficient
→ one pair of quark-antiquark is created : **Schwinger Mechanism**
- Use at PYTHIA/JETSET

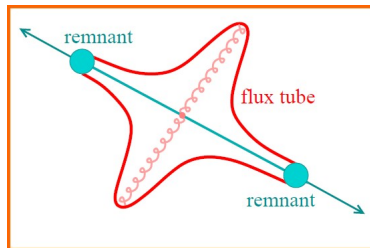
Unified Approach

Core-Corona Approach

Using hydrodynamic \rightarrow the Core become fluid.

Corona become Jet \Rightarrow Later Hadrons !

- Initial Conditions
- **Core-Corona Approach**
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GDRE2012, Nantes, Jul 2012, Klaus WERNER, Subatech, Nantes

More Scattering \Rightarrow

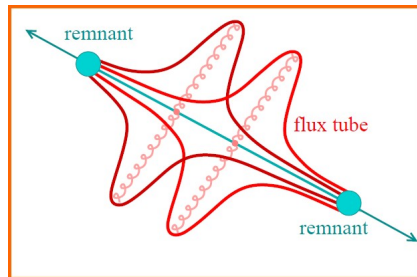
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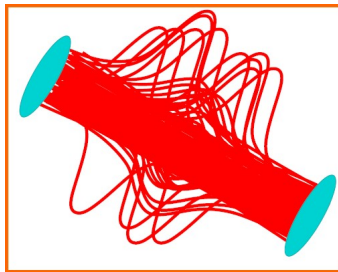
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B. Guiot and K. Werner, J. Phys. Conf. Ser. **589** (2015) no.1

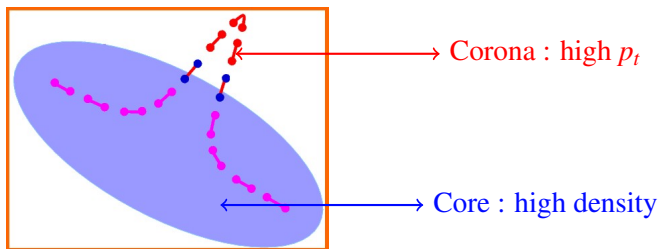
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Core-Corona Approach

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Hydrodynamical expansion

Core evolves with respect to the equation of relativistic viscous hydrodynamics

Local energy momentum :

$$\partial_\mu T^{\mu\nu} = 0 \quad \nu = 0, \dots, 3$$

and the conservation of net charges,

$$\partial N_k^\mu = 0, \quad k = B, S, Q$$

with B, S and Q referring to
baryon number, strangeness and electric charge

Unified Approach

- Initial Conditions
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- **Statistical hadronization**
- **Final state hadronic cascade**

Statistical Hadronization

Core-Matter make hadronization

Defined by a constant temperature T_H

Procedure of Cooper-Frye

K. Werner, Iu. Karpenko, T. Pierog, M. Bleicher, K. Mikhailov, arXiv:1010.0400, Phys. Rev. C 83, 044915 (2011)

Hadronic Cascade

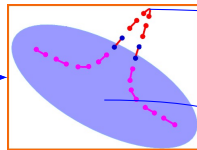
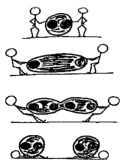
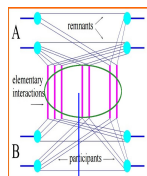
Hadron density still big \rightarrow hadron-hadron rescatterings

Use **UrQMD Model**

M. Bleicher et al., J. Phys. G25 (1999) 1859

H. Petersen, J. Steinheimer, G. Burau, M. Bleicher and H. Stöcker, Phys. Rev. C78 (2008) 044901

Unified Approach



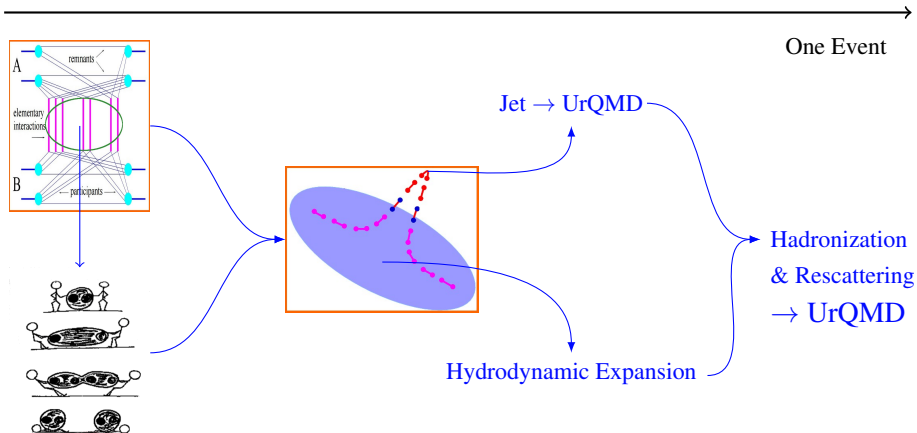
Jet → UrQMD

Hydrodynamic Expansion

One Event

Hadronization
& Rescattering
→ UrQMD

Unified Approach



Let's stop talking about EPOS now

Data Comparison

RHIC at few energies

Elliptic flow of identified hadrons in Au+Au collisions at

$$\sqrt{s_{NN}} = 7.7 - 62.4 \text{ GeV}$$

L. Adamczyk *et al.* [STAR Collaboration], Phys. Rev. C **88** (2013) 014902

Measurements of the elliptic flow, v_2 , of identified hadrons ($\pi^\pm, K^\pm, K_s^0, p, \bar{p}, \phi, \Lambda, \bar{\Lambda}, \Xi^-, \bar{\Xi}^+, \Omega^-, \bar{\Omega}^+$) in Au+Au collisions at $\sqrt{s_{NN}} = 7.7, 11.5, \mathbf{19.6}, 27, 39$ and 62.4 GeV are presented.

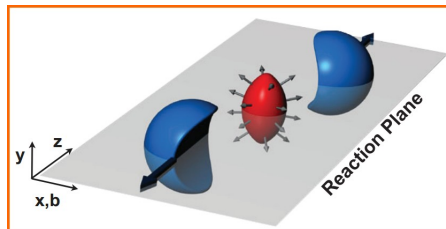
Here, we compare at 19.6 GeV

We use the same method of STAR to compare Data and Results

Elliptic Flow

Anisotropic Flow

Direct evidence of flow : anisotropy in particle momentum distributions correlated with the reaction plane.



R. Snellings, New J. Phys. **13** (2011) 055008

Elliptic Flow

Anisotropic Flow

A way of characterizing the various patterns of anisotropic flow is to use a Fourier expansion :

$$E \frac{d^3N}{d^3\mathbf{p}} = \frac{1}{2\pi} \frac{d^2}{p_t dp_t dy} \left(1 + 2 \sum_{n=1}^{\infty} v_n \cos [n(\phi - \psi_{RP})] \right)$$

E : energy of the particle ; p : momentum ; p_t : transverse momentum ; ϕ : azimuthal angle ; y : rapidity ; ψ_{RP} : reaction plane angle.

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Anisotropic Flow : ($n=1$: Directed Flow , $n=2$: Elliptic Flow)

$$v_n(pt, y) = \langle \cos [n(\phi(pt, y) - \Psi_{RP})] \rangle$$

Elliptic Flow

Eta-Sub : Event Plane Method

Event Flow vector (projection of azimuthal angle) :

$$Q_{n,x} = \sum_i w_i \cos(n\phi_i) = Q_n \cos(n\Psi_n)$$

$$Q_{n,y} = \sum_i w_i \sin(n\phi_i) = Q_n \sin(n\Psi_n)$$

The sum goes over all particles i used in *the event plane calculation*.
 ϕ_i and w_i are the lab azimuthal angle and weight for particle

Where Ψ_n **the event plane angle** :

$$\Psi_n = \tan^{-1} \left(\frac{\sum_i w_i \sin(n\phi_i)}{\sum_i w_i \cos(n\phi_i)} \right) / n$$

Elliptic Flow

Eta-Sub : Event Plane Method

$$v_n^{\text{obs}}(p_T, y) = \langle \cos[n(\phi_i - \Psi_n)] \rangle$$

Average over all particles in all events with their azimuthal angle ϕ_i in a given rapidity and p_T momentum space.

Elliptic Flow

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Average over all particles in all events with their azimuthal angle ϕ_i in a given rapidity and p_T momentum space.

$$\mathcal{R} = \langle \cos[n(\Psi_n - \Psi_{RP})] \rangle$$

average over all events

Elliptic Flow

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Average over all particles in all events with their azimuthal angle ϕ_i in a given rapidity and p_T momentum space.

Eta-sub method : two planes defined by negative (A) and positive (B) pseudorapidity with \approx equal multiplicity :

$$\mathcal{R}_{n,sub} = \sqrt{\langle \cos[n(\Psi_n^A - \Psi_n^B)] \rangle}$$

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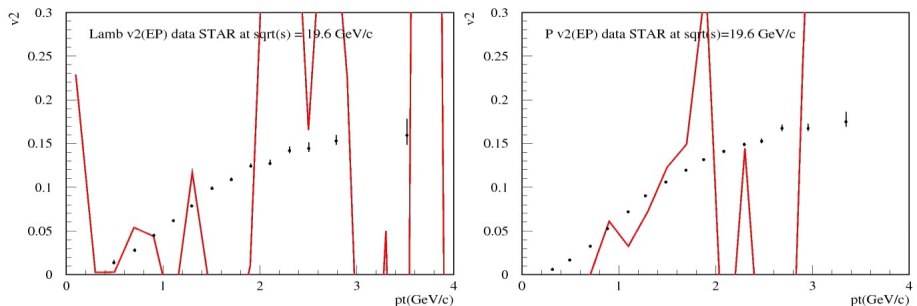
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The final flow coefficients are :

$$v_n = \frac{v_n^{\text{obs}}}{\mathcal{R}_{n,sub}}$$

Results : v_2 vs p_t



Bad Results !

Results

What have we forgotten ?

First :

Take in account the weight of particle : w_i

$$Q_{n,x} = \sum_i w_i \cos(n\phi_i) = Q_n \cos(n\Psi_n)$$

weight w_i is linear to p_t up to 2 GeV/c, after equal to 2 GeV/c

Results

What have we forgotten ?

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Second :

Take all triggers and all experimental conditions

Results

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First :

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Second :

Take all triggers and all experimental conditions

- acceptance of pseudorapidity between -1 and 1 with a gap of 0.05 in the middle (two ranges of η)
- acceptance of rapidity between -1 and 1
- acceptance of momentum between 0.15 and 5 GeV/c
- acceptance centrality between 0 and 80 %

Results

What have we forgotten ?

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Take in account the weight of particle : w_i

Second :

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Third :

First approach of eta-sub method with EPOS

Results

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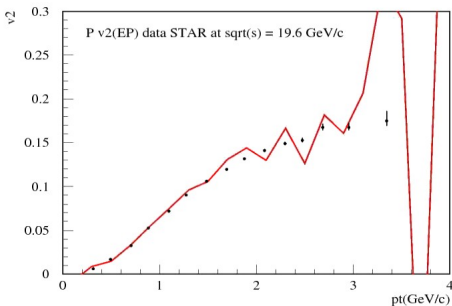
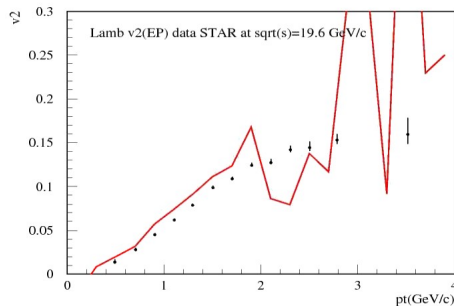
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Results : v_2 vs p_t



First good results but work in progress !

Conclusion

EPOS was created for **very high energy** with an application for multiple scattering

EPOS has good results at number of observables → **very high energy**

Conclusion

EPOS was created for **very high energy** with an application for multiple scattering

EPOS has good results at number of observables \rightarrow **very high energy**

But : **First Study at "low" energies** ($\sqrt{s} = 7.7$ GeV at $\sqrt{s} = 62.4$ GeV) for v_2

We obtain good results !

Maybe EPOS can also reproduce observables at less high energy

Thanks you !!!



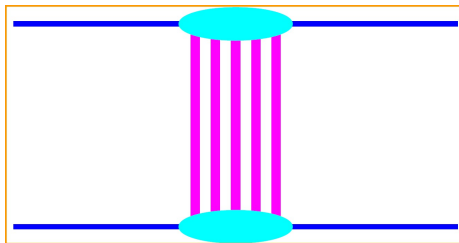
Gribov-Regge Theory and Pomeron

Effective Field Theory

Elementary interaction \rightarrow Pomeron exchange

Pomeron : Quantum numbers of vacuum

Vladimir Gribov in ≈ 1960



Elastic Amplitude : $T(s, t) \approx i s^{\alpha_0 + \alpha' t}$

Hydrodynamic equations

Based on the four-momenta of string segments, we compute the energy momentum tensor and the flavor flow vector at some position x (at $\tau = \tau_0$) as :

$$T^{\mu\nu} = \sum_i \frac{\delta p_i^\mu \delta p_i^\nu}{\delta p_i^0} g(x - x_i)$$

$$N_q^\mu(x) = \sum_i \frac{\delta p_i^\mu}{\delta p_i^0} q_i g(x - x_i)$$

where $q = u, d, s$

arXiv:1312.1233v1 [nucl-th] 4 Dec 2013

Unified Approach

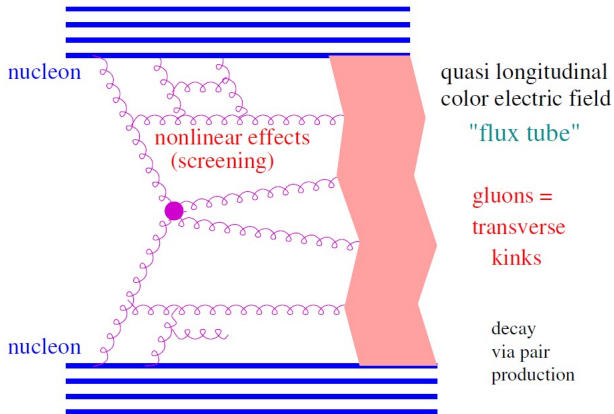
Initial Conditions : PBGRT to initialize collisions, Pomerons treated by partons ladders after by Lund string

Core-Corona Approach Determine Jet and Quark Gluon Plasma

Viscous hydrodynamic expansion for the "core-matter"

Statistical Hadronization Procedure of Cooper-Frye

Final state hadronic Cascade Rescattering of products particle for the transport : UrQMD Model



Initial conditions. A Gribov-Regge multiple scattering approach is employed, where the elementary object (by definition called Pomeron) is a DGLAP parton ladder, using in addition a CGC motivated saturation scale for each Pomeron. The parton ladders are treated as classical relativistic (kinky) strings.

Core-corona approach. At some early proper time τ_0 , one separates fluid (core) and escaping hadrons, including jet hadrons (corona), based on the momenta and the density of string segments. The corresponding energy-momentum tensor of the core part is transformed into an equilibrium one, needed to start the hydrodynamical evolution. This is based on the hypothesis that equilibration happens rapidly and affects essentially the space components of the energy-momentum tensor.

Viscous hydrodynamic expansion. Starting from the initial proper time τ_0 , the core part of the system evolves according to the equations of relativistic viscous hydrodynamics. A cross-over equation-of-state is used, compatible with lattice QCD.

Statistical hadronization. The “core-matter” hadronizes on some hypersurface defined by a constant temperature T_H , where a so-called Cooper-Frye procedure is employed, using equilibrium hadron distributions.

Final state hadronic cascade. After hadronization, the hadron density is still big enough to allow hadron-hadron rescatterings. For this purpose, we use the UrQMD model.

We will present a “realistic” treatment of the hydrodynamic evolution of ultrarelativistic heavy ion collisions, based on the following features:

- ▷ initial conditions obtained from a flux tube approach (EPOS),
 - compatible with the string model used since many years for elementary collisions (electron-positron, proton proton),
 - and the color glass condensate picture;
- ▷ consideration of the possibility to have a (moderate) initial collective transverse flow;
- ▷ event-by-event procedure,
 - taking into the account the highly irregular space structure of single events,
 - leading to so-called ridge structures in two-particle correlations;
- ▷ core-corona separation, considering the fact that only a part of the matter thermalizes;