EMCal/DCal calibration γ -hadron correlations in pp collisions status and outlook

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In this presentation



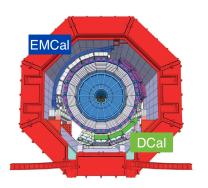
- ► EMCal/DCal 2015 calibration
 - Status
 - Related studies
- ightharpoonup γ -hadron correlations analysis in pp collisions:
 - Physics motivation
 - Results
 - Persepctives

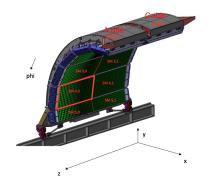


EMCal/DCal detectors



- ► EMCal and DCal composed of Super Modules (SMs)
- ► Each SM is composed of towers which are elementary lecture units



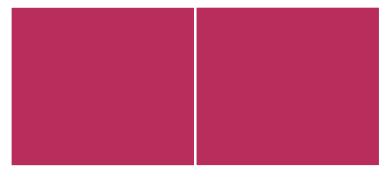




EMCal/DCal calibration status



- In-situ energy calibration tower by tower with π^0 invariant mass:
 - Reconstruct π^0 invariant mass distribution for each tower of EMCal and DCal
 - Apply offline coefficients to put fitted π^0 masses at π^0 PDG mass with iterative process
- Few iterations more needed for analyses





EMCal/DCal calibration related studies



- ▶ In 2015 largest dataset ever for energy calibration: use this opportunity to better understand EMCal and DCal
- Several tasks have been started:
 - Test the accuracy reachable by the current calibration method next slides
 - Statistics
 - Systematics
 - Test the stability of the detector
 - Understand large amount of electronic noise observed in 2015 data

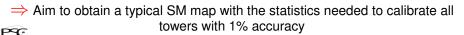




EMCal/DCal calibration accuracy (statistics)



- ▶ Specification: the calibration has to reach 1% accuracy for each tower
- Find how many events are needed to reach n% of statistical uncertainty on the π^0 mass with the calibration
 - Calibrate one sample and apply coefficients on another one
 - Uncertainty on the fitted mass as a function of tower stat = statistical uncertainty



EMCal/DCal calibration accuracy (systematics)



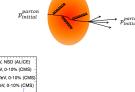
- ▶ Test uncertainty coming from different pieces of the calibration procedure:
 - new trigger configuration: compare fitted means with and without new trigger configuration - no bias
 - alignement: compare invariant mass distributions for 2γ in same SM and 2γ in different SMs bias for DCal
 - combinatorial background shape: compare fitted means after changing bkg shape - no bias

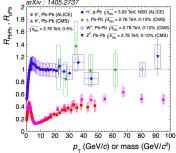


High p_T particles suppression and jet quenching



- ▶ QGP phase induces final state modification compared to pp collisions
- ▶ High p_T particles suppression observed due to parton energy loss in medium
- Parton loses energy by:
 - gluon radiation
 - collisions





⇒ What's the amount of energy lost and where does this energy go?

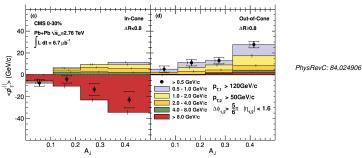


Energy redistribution



- ► From jet analysis (CMS):
 - di-jet momentum imbalance measurement
 - In-cone imbalance corresponds to out-of-cone imbalance

$$p_T^{\parallel} = \sum_i -\rho_T^i \cos(\phi_i - \phi_{\text{leading jet}}) \tag{1}$$



 \Longrightarrow Energy is not recovered in the jet cone and is redistributed preferentially with low p_T particles



Energy loss measurement: observables



- Until now: proof of parton energy loss in medium
- Need more observables to constrain theoretical models
- Several observables:
 - Single particle p_T spectra (R_{AA}) : do not allow precise measurement of energy loss
 - Di-hadron(jet) correlations: bias on initial parton energy
 - γ -jet correlations : exact measurement of fragmentation function
 - γ -hadron correlations : approximation of fragmentation function but possible at lower p_T

 γ -hadron correlations = clean way to measure parton energy redistribution at low p_T



Energy loss measurement: pp reference

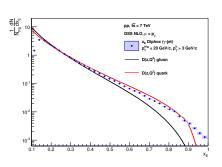


- ▶ Aim: Approximate the Fragmentation Function D(z) using γ -jet events produced with hard processes
 - Compton: $q + g \rightarrow \gamma + q$
 - Annihilation: $q + \bar{q} \rightarrow \gamma + g$
- ▶ Initial parton energy known: $E_{initial}^{parton} \approx E_{\gamma}$
- Good approximation of the FF with the x_E distribution

$$x_E = \frac{p_T^{hadron}}{p_T^{trig}}\cos\Delta\phi \approx z$$
 (2)



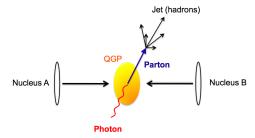




γ -hadron correlation: Method



- ▶ Obtain the x_E distribution for isolated photons: $f(x_E) = \frac{1}{N_{trig}^{\gamma}} \frac{dN_h}{dx_E}$
- ▶ Need to identify:
 - Isolated photons (trigger particles)
 - hadrons coming from the opposite side parton

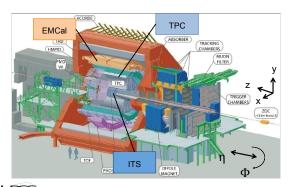


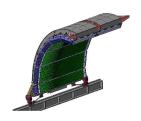


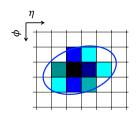
ALICE and EMCal



- ► Charged particles : ITS and TPC
- Neutral particles : EMCal
 - Acceptance: $|\eta| < 0.7$ et $\Delta \Phi = 107^{\circ}$
 - Segmentation in lecture units: towers
 - Showers in EMCal = clusters





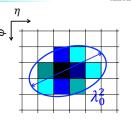


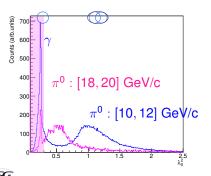


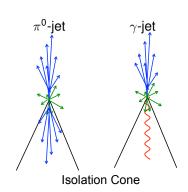
Isolated photons background suppression



- ▶ Main background contribution is $\pi^0 \rightarrow \gamma \gamma$
- Apply cuts on the reconstructed EMCal clusters:
 - Leading particle of the event
 - Charged particles veto
 - Round-shaped cluster ($\lambda_0^2 \in [0.10, 0.27]$)
 - Isolation cut $(\sum p_{\rm T}^{\rm in\ cone} < 1\ {\rm GeV}/c)$







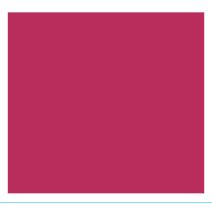
Isolated photons purity



- ▶ After cuts on clusters, background remains → purity estimate
- Purity definition:

$$\mathbb{P} = \frac{\text{direct photons clusters}}{\text{all isolated circular clusters}} \tag{3}$$

Two methods to estimate isolated photons purity both using simulation





Isolated photons purity: Systematics



- All parameters involved in purity estimate have been variated
- Most of them do not lead to a systematic uncertainty
- > Systematic uncertainties come from the discrepancy between data and MC for λ_0^2 (cluster shape) and isolation



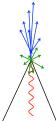


Underlying Event (UE) subtraction



- ▶ UE: Not all the hadrons of the event are coming from the hard process \Rightarrow some hadrons have to be disregarded for x_E calculation
- ▶ In pp collisions: particles production is isotropic in azimuth \Rightarrow UE is the same in different ϕ regions
- ➤ To avoid jet contamination (coming from opposite side parton), UE is estimated in cones orthogonal to trigger particle







Isolated photon x_E distribution



The x_E distribution for isolated photons is defined as:

$$f(x_E)^{\gamma} = \alpha_{corr}^{away} \left(\frac{1}{\mathbb{P}} f(x_E)^{clusters} - \frac{1 - \mathbb{P}}{\mathbb{P}} f(x_E)^{\pi^0} \right) - \alpha_{corr}^{UE} f(x_E)^{UE}$$
 (4)



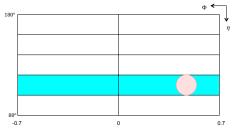


γ -hadron correlations in p-Pb and Pb-Pb (1/2)



Two main issues raise in p-Pb an Pb-Pb collisions :

- ► The isolation of the trigger particle in high multiplicity environment
 - $\sum p_{\mathrm{T}}^{\mathrm{in\;cone}} pprox 2\;\mathrm{GeV}/c\;\mathrm{in\;p ext{-}Pb\;collisions}$
 - $\sum p_{
 m T}^{
 m in\ cone}$ up to 40 GeV/c in Pb-Pb collisions
 - \bullet Estimate in η band around the isolation cone allows to get rid of collective effects



- ► The subtraction of the UE in the away side

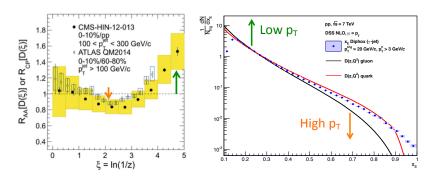




γ -hadron correlations in p-Pb and Pb-Pb (2/2)



- What we expect to see
 - No change in p-Pb collisions
 - Modification of the x_E distribution depending on the medium properties in Pb-Pb collisions



⇒ The first bins are the most important



γ -hadron correlations analysis improvement



- ▶ With run II data: systematics will be the dominant uncertainties
- ightharpoonup Dominant systematic at low x_E comes from purity
- Need to improved purity estimate method:
 - Reach a better agreement between data and Monte-Carlo for λ_0^2 and $\sum p_{\rm T}^{\rm in\;cone}$ distributions
 - Improve isolation method





pratoire de Physique

What future after γ -hadron correlations?



- ▶ Numerous measurements will be needed to constrain theoretical models
- $ightharpoonup \gamma$ -hadron correlations is just the beginning: allows to understand UE and isolated photons purity and access plenty of different variables
- Access parton energy loss and energy redistribution with differential studies:
 - Parton energy loss vs energy

run II

Parton energy redistribution

run II

 \star γ -jet allows to access to other informations than di-jet

run II

Medium length dependency
 Study for different centrality classes

Mass and color charge dependency

run III

- \star quark vs gluon = γ -jet vs π^0 -jet
- Will need heavy quark jet tagging

Conclusions



- ▶ Better understanding of EMCal and DCal with the estimate of the statistical and systematic uncertainties
- Fragmentation function and parton medium induced energy loss can be approach with γ -hadron correlations
- $ightharpoonup \gamma$ -hadron correlations analysis in pp collisions is close to final
- The two main difficulties of the analysis (purity and UE) are now better understood
- ▶ For the future:
 - First step with p-Pb collisions then Pb-Pb collisions
 - Second step: move to all the other observables accessible to probe the QGP

⇒ Still lots of exiting work to measure parton energy loss and to understand quantitatively the medium induced modification of the fragmentation process

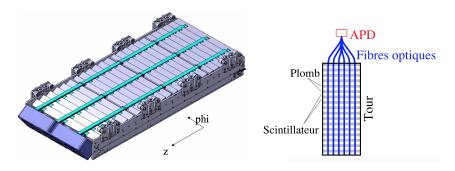


BACK UP

EMCal/DCal segmentation



- ► EMCal (DCal) = 10 + 2/3 SMs (6 + 2/3)
- ▶ 1 SM = 24 stripmodules
- ▶ 1 stripmodules = $12 \times (2 \times 2)$ towers





EMCal/DCal energy calibration procedure



Reconstruct π^0 invariant mass for each tower with

$$m_{\pi^0} = \sqrt{2E_1E_2 \times (1 - \cos\theta_{12})} \tag{5}$$

- Combined all clusters from 1 tower with all clusters from the event in the same SM → signal + combinatorial background
- Fit the distribution obtained with gauss (signal) + pol2 (bkg)
- Peak position = tower decalibration
- Offline coefficient to correct
- Iterative procedure because of the two photons (i.e. two clusters, towers) involved in m_{π^0}
- Coefficients can be used to recalculate HVs



EMCal/DCal tower gain and HVs



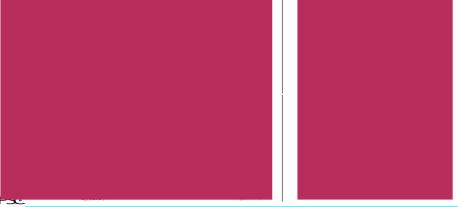
- APD change light from optic fibers to electric signal
- ► Each APD has a gain which depends on the HVs applied: $G(U) = A + Be^{kU}$
- ► Changing HVs change APD gain → change number of ADC (i.e energy) collected for a same generated light



EMCal/DCal electronic noise



- In 2015 data electronic noise is observed
- ▶ Discriminate noise and true π^0 with absolute time cut
- No change with pair difference time cut → the electronic noise is correlated
- Energy spectra can help to detect which tower of a duo is the bad one



EMCal/DCal gain variation



- Several peaks observed for the same tower
- Is it due to gain change with time?
- Study on detector stability should answer



EMCal/DCal calibration statistical uncertainty



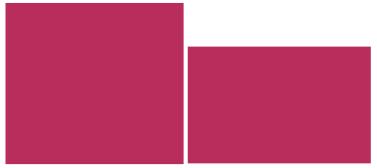
- Aim: determine fitted mass uncertainty as a function of the number of π^0 for each tower
- ▶ Theory: $\sigma_{\mu} = 1/\sqrt{N_{\pi^0}}$
- ▶ But there is combinatorial background
- Method used:
 - Calibrate 1 data sample with few iteration automatically
 - Apply coefficients found on another data sample
 - Extract the fitted mean relative difference between the two samples for tagged good towers
 - Discretize as a function of the average number of π^0

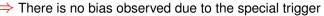


EMCal/DCal new trigger configuration



- ▶ New trigger configuration was tested during 2015 calibration data taking
- New configuration allows to populate more at the edges than the center of the SMs
- Aim: be able to calibrate towers that are at the edges of SMs
- Compare fitted mass obtain for flagged good towers with and without the special trigger configuration







EMCal/DCal background shape bias



- lacktriangle The background is part of the fit used to obtain π^0 mass
- ▶ Structure is observed as per the χ^2 of the fit
- ▶ Does the mis-reproduction of the background shape by the fit induce a bias in the π^0 mass estimate ?
- Use typical difference between the fit and the real background shape to deteriorate good towers
- Compare the fitted mass between good towers and deteriorated background towers





 \Rightarrow Bias smaller than statistical uncertainty observed

EMCal/DCal alignement



- ▶ To avoid any bias from bad SMs alignement the two photons used to build π^0 mass have to be in the same SM
- To collect more statistics at the edges we would like to open up this cut
- Alignement is better for EMCal than DCal
- Compare fitted mass for 2 photons in the same SM and two photons in different SMs

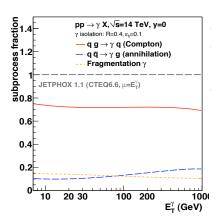
⇒ Bias observed for DCal



Production fraction of hard processes



Dominant processus : Compton diffusion $\Rightarrow x_E$ distribution slope approximate the quark FF

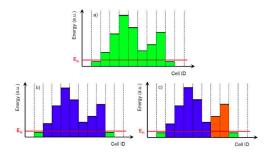




EMCal: clusterization



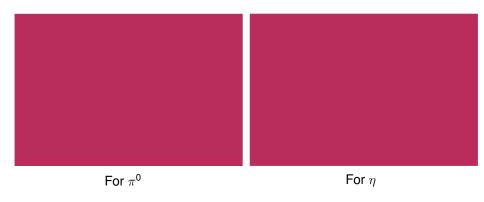
Several types of clusterization to reconstruct particles in EMCal : V1, V2, NxM, V1+Unfolding





Neutral mesons kinematics





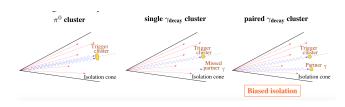
 $\Rightarrow \pi^0$ are asymmetric decays and η are more symmetric



Bias assumption



- ▶ Paired gamma decays : present only at low λ_0^2
- ▶ MCC : at high λ_0^2



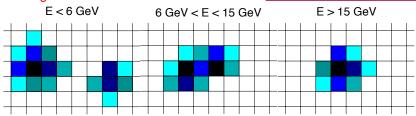


Cluster shape



- ▶ Cluster shape described by λ_0^2 parameter
- Photons: 1 circular cluster $0.1 < \lambda_0^2 < 0.27$
- lacktriangledown $\pi^0 o \gamma \gamma$ (background for direct photons):
 - E < 6 GeV: 2 circular clusters
 - 6 GeV < E < 15 GeV: 1 elongated cluster
 - E > 15 GeV: 1 almost circular cluster

Energy dependence for λ_0^2 cuts applied for selecting π^0





Isolation



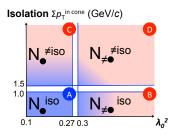
- Measure hadronic activity in isolation cone, with R = 0.4, around the cluster candidate
- ▶ Direct photons from γ -jet events have to be isolated
- ▶ Isolation criteria: $\sum p_T < 1 \text{ GeV/}c$
- Anti-isolation criteria: $\sum p_T > 1.5 \text{ GeV/}c$ (used for bkg study)



Isolation and λ_0^2 space phase



- lsolation and λ_0^2 cuts divide space phase into 4 areas:
 - A: mainly signal region (isolated photons) + background
 - B, C and D: mainly background regions (π^0) + signal
- Estimate the purity of direct photons in A zone



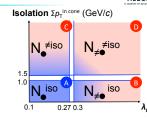


Notations and definitions



- ► Amount of particles:
 - S: direct photons
 - B: background $(\pi^0, \eta, \text{gamma decays } (\pi^0, \eta), ...)$
 - N = S + B
- Isolation criteria:
 - isol: isolation cone activity $\sum p_T < 1$ GeV/c (A, B)
 - \neq isol: isolation cone acitivity $\sum p_T > p_T^{thres}$ (C, D)
- Circularity of the clusters:
 - •: round shape cluster $\lambda_0^2 < 0.27$ (A, C)
 - \neq •: elliptic cluster $\lambda_0^2 > f^{thres}(p_T^{trig})$ (B, D)
- Purity = number of clusters coming from isolated photons in our isolated and round shape clusters sample

$$\mathbb{P} = \frac{S_{\bullet}^{isol}}{N^{isol}} = 1 - \frac{B_{\bullet}^{isol}}{N^{isol}} \tag{6}$$



Purity estimate: data method

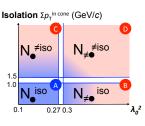


Assume background isolation fractions are the same at low and high λ_0^2

$$\frac{B_{\bullet}^{\text{isol}}/B_{\bullet}^{\neq \text{isol}}}{B_{\neq \bullet}^{\text{isol}}/B_{\neq \bullet}^{\neq \text{isol}}} = 1 \tag{7}$$

$$\mathbb{P}_{1} = 1 - \frac{B_{\bullet}^{\neq \text{isol}} / N_{\bullet}^{\text{isol}}}{B_{\neq \bullet}^{\neq \text{isol}} / B_{\neq \bullet}^{\text{isol}}}$$
(8)

▶ The isolation fractions ratio between low and high λ_0^2 deviates significantly from 1 due to the presence of gamma decays and MultiContribution Clusters



⇒ Try now to correct this purity estimate using simulation



Purity estimate: Corrections 1/2

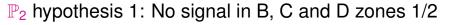


- P₂ using JJ simulation:
 - Assume no signal in background zones
 - Correct only bias from gamma decays and MultiContribution Clusters

$$\left(\frac{B_{\bullet}^{isol}/B_{\bullet}^{\neq isol}}{B_{\neq \bullet}^{isol}/B_{\neq \bullet}^{\neq isol}}\right)_{data} = \left(\frac{B_{\bullet}^{isol}/B_{\bullet}^{\neq isol}}{B_{\neq \bullet}^{isol}/B_{\neq \bullet}^{\neq isol}}\right)_{MC(\mathcal{J})}$$
(9)

Replacing B^{isol}_{\bullet} in \mathbb{P} :

$$\mathbb{P}_{2} = 1 - \left(\frac{B_{\bullet}^{\neq \text{isol}}/N_{\bullet}^{\text{isol}}}{B_{\neq \bullet}^{\neq \text{isol}}/B_{\neq \bullet}^{\text{isol}}}\right)_{data} \times \left(\frac{B_{\bullet}^{\text{isol}}/B_{\bullet}^{\neq \text{isol}}}{B_{\neq \bullet}^{\text{isol}}/B_{\neq \bullet}^{\neq \text{isol}}}\right)_{MC(JJ)}$$
(10)





- ▶ Closure test: check difference between \mathbb{P}_{MC}^{truth} and \mathbb{P}_{reco}
- $ightharpoonup \mathbb{P}_{reco}$: found by replacing data term in \mathbb{P}_2 with a GJ + JJ simulation
- ▶ If no signal in B, C and D zones: $p_{reco} = p_{MC}^{truth}$

$$\mathbb{P}_{2,reco} = 1 - \left(\frac{B_{\bullet}^{\neq \text{isol}}/B_{\bullet}^{\text{isol}}}{B_{\neq \bullet}^{\neq \text{isol}}/B_{\neq \bullet}^{\text{isol}}}\right)_{GJ+JJ} \times \left(\frac{B_{\bullet}^{\text{isol}}/B_{\bullet}^{\neq \text{isol}}}{B_{\neq \bullet}^{\text{isol}}/B_{\neq \bullet}^{\neq \text{isol}}}\right)_{MC(JJ)}$$
(11)



Purity estimate: Corrections 2/2



- ▶ P₃ using GJ+JJ simulation:
 - Correction of P2: take into account signal in background region
 - $B_i^J = \mathscr{C}_i^J \times N_i^J$

$$\begin{pmatrix} B_{\bullet}^{isol}/B_{\bullet}^{\neq isol} \\ B_{\bullet}^{isol}/B_{\neq}^{\neq isol} \end{pmatrix}_{data} = \begin{pmatrix} B_{\bullet}^{isol}/B_{\bullet}^{\neq isol} \\ B_{\bullet}^{isol}/B_{\neq}^{\neq isol} \end{pmatrix}_{data} \text{ and } \begin{pmatrix} \mathcal{C}_{\bullet}^{\neq isol} \\ \mathcal{C}_{\bullet}^{\neq isol} \\ \mathcal{C}_{\bullet}^{\neq isol} \\ \mathcal{C}_{\bullet}^{\neq isol} \end{pmatrix}_{data} = \begin{pmatrix} \mathcal{C}_{\bullet}^{\neq isol} \\ \mathcal{$$

$$\Leftrightarrow \left(\frac{B_{\bullet}^{isol}/N_{\bullet}^{\neq isol}}{N_{\neq \bullet}^{isol}/N_{\neq \bullet}^{\neq isol}}\right)_{data} = \left(\frac{B_{\bullet}^{isol}/N_{\bullet}^{\neq isol}}{N_{\neq \bullet}^{isol}/N_{\neq \bullet}^{\neq isol}}\right)_{MC(GJ+JJ)} \tag{13}$$

Replacing B^{isol}_{\bullet} in \mathbb{P} :

$$\mathbb{P}_{3} = 1 - \left(\frac{N_{\bullet}^{\neq \text{isol}}/N_{\bullet}^{\text{isol}}}{N_{\neq \bullet}^{\neq \text{isol}}/N_{\neq \bullet}^{\text{isol}}}\right)_{data} \times \left(\frac{B_{\bullet}^{|sol}/N_{\bullet}^{\neq \text{isol}}}{N_{\neq \bullet}^{|sol}/N_{\neq \bullet}^{\neq \text{isol}}}\right)_{MC(GJ+JJ)}$$
(14)

▶ P₃ will be used for final purity estimate while signal contamination reproduction will be tested with P₂



Closure test



Try to get back to MC truth by replacing data with gamma-jet + jet-jet cocktail

$$\begin{array}{l} \blacktriangleright \quad p_{2} \colon \left(\frac{N_{<}^{\neq \text{ isol}}/N_{>}^{\text{isol}}}{N_{>}^{\neq \text{ isol}}/N_{>}^{\text{isol}}}\right)_{data} \rightarrow \left(\frac{N_{<}^{\neq \text{ isol}}/N_{>}^{\text{isol}}}{N_{>}^{\neq \text{ isol}}/N_{>}^{\text{isol}}}\right)_{MC_{GJ+JJ}} \\ p_{2} = 1 - \frac{S_{<}^{\text{isol}}}{N_{>}^{\text{isol}}} = p_{MC}^{truth} \\ \blacktriangleright \quad p_{3} \colon \left(\frac{N_{<}^{\neq \text{ isol}}/N_{>}^{\text{isol}}}{N_{>}^{\neq \text{ isol}}/N_{>}^{\text{isol}}}\right)_{data} \rightarrow \left(\frac{N_{<}^{\neq \text{ isol}}/N_{>}^{\text{isol}}}{N_{>}^{\neq \text{ isol}}/N_{>}^{\text{isol}}}\right)_{MC_{GJ+JJ}} \\ p_{3} = p_{MC}^{truth} \text{ by construction} \end{array}$$

P₃ results in data



- Two JJ simulations are available:
 - γ_{decay} $p_T > 3.5$ GeV/c in EMCal: valid in all analysis p_T range
 - γ_{decay} $p_T > 7$ GeV/c in EMCal: unbiased only after 16 GeV/c
- ▶ Apply the GJ+JJ correction anti-isolation cut at 1.5 GeV/c and high λ_0^2 cut at 0.3 on data and simulation







Cross check with p2



- $ightharpoonup \mathbb{P}_3$ should be compatible with \mathbb{P}_2 if the signal contamination is properly reproduce
- ▶ Compare \mathbb{P}_3 with \mathbb{P}_2 with no signal in background region (see backup and presentation *here*)
- P₂ [1 GeV/c,0.3]: bias due to signal contamination in bkg regions
- $ightharpoonup \mathbb{P}_3$ [1 GeV/c, 0.3]: little bias
- ▶ P₃ [1.5 GeV/c,0.3]: compatible with P₂ tight cuts

 \Rightarrow No signal contamination bias for \mathbb{P}_3 with our set of cuts



Systematics sources



The systematic uncertainties come from hypotheses made for \mathbb{P}_3 :

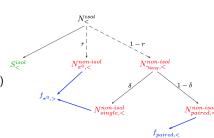
$$\begin{pmatrix}
B_{\bullet}^{isol} / B_{\bullet}^{\neq isol} \\
B_{\bullet}^{isol} / B_{\bullet}^{\neq isol}
\end{pmatrix}_{data} = \begin{pmatrix}
B_{\bullet}^{isol} / B_{\bullet}^{\neq isol} \\
B_{\bullet}^{isol} / B_{\bullet}^{\neq isol}
\end{pmatrix}_{MC(GJ+JJ)} \text{ and } \begin{pmatrix}
C_{\bullet}^{\neq isol} \\
C_{\bullet}^{\neq isol} \\
C_{\bullet}^{\neq isol}
\end{pmatrix}_{data} = \begin{pmatrix}
C_{\bullet}^{\neq isol} \\
C_{\bullet}^{\neq isol}
\\
C_{\bullet}^{\neq isol}
\end{pmatrix}_{MC(GJ+JJ)}$$
(15)

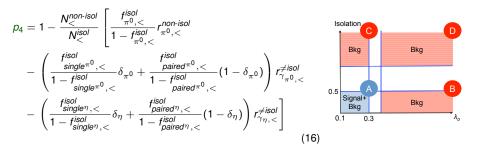
- Signal proportion in GJ+JJ simulation: 0.5 to 1 %
- ► Smearing (see backup and presentation *here*) of λ_0^2 in simulation ($\mathscr{C}_{\neq \bullet}^{isol}$): 1 to 1.5 %
- ▶ Sensibility to $\mathscr{C}_{\bullet}^{\neq isol}$: $\leq 0.5 \%$
- ▶ Uncertainties on background isolation fractions ratio: ≤ 8%

Splitting method: formula



- ► Split the background contributions
- Proportion of species $r_{i,<}^{iso} = N_{i,<}^{iso}/N_{tot,<}^{iso}$ (MC)
- Isolation fraction $f_{i,<} = N_{i,<}^{iso}/N_{i,<}^{iso+\neq iso}$ (data)
- Fraction of single gamma decays $\delta_i = N_i^{\text{single}}/N_i^{\text{single}+\text{paired}}$ (MC)











Propagate analytically uncertainties on $\alpha_{\it corr}^i$ to $\it x_E$ distribution

Parton energy loss



(17)

$$\Delta E \approx \alpha_s C_R \hat{q} L^2$$

where

- $ightharpoonup C_R$ is the Casimir factor (3/4 for q, 3 for g)
- \hat{q} is the medium transport coefficient
- L is the le

