

# Lecture 7

## Lattice design with MAD-X

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# Lecture 8 – MADX introduction and examples

- This lecture is based on one by Ted Wilson (CERN) which was in turn based on a lecture by V. Ziemann (Uppsala University)
  - Installing/running MADX (on windows)
  - Input of elements and beamlines
  - Beta functions, tunes, dispersion
  - Matching
  - Examples

All credit to V. Ziemann for example input files  
More examples are on the MAD-X website!

# What is MAD-X?

“A program for accelerator design and simulation with a long history”  
Developed from previous versions (MAD, MAD-8, then finally MAD-X in 2002).  
User guide: <http://mad.web.cern.ch/mad/uguide.html>

- Uses a sequence of elements placed sequentially along a *reference orbit*
- *Reference orbit* is path of a charged particle having the central design momentum of the accelerator through idealised magnets (no fringe fields)
- The reference orbit consists of a series of straight line segments and circular arcs
- local curvilinear right handed coordinate system  $(x, y, s)$

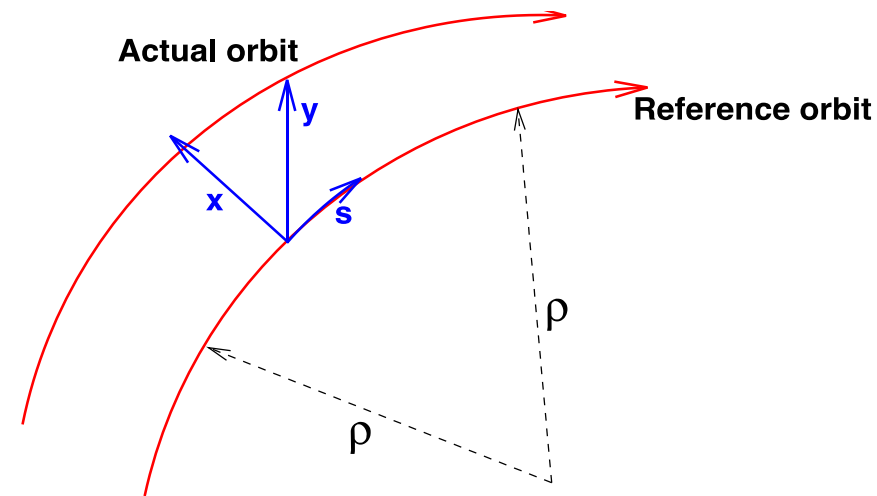


Figure 1: Local coordinate system as used by MAD-X.

# What can it do?

- You can input magnets (& electrostatic elements) according to the manual
  - User guide: <http://madx.web.cern.ch/madx/>
- Calculate beta functions, tune, dispersion, chromaticity, momentum compaction numerically.
- Generates tables and plots (.ps)
- (tip: you might need to install ghostscript to view plots)

# Why choose MAD-X?

- There are any number of tracking and beam optics codes, but MAD-X is *widely used* (especially at CERN), *well maintained* and *well documented*.
  - The more lattice design you do – the more you will appreciate this about MAD-X!
- What it can't do:
  - Acceleration and tracking simultaneously
  - Not so accurate at large excursions from closed orbit (as in an FFAG)
  - Complicated magnet geometries
  - Field maps

# Installing MADX

<http://madx.web.cern.ch/madx/>

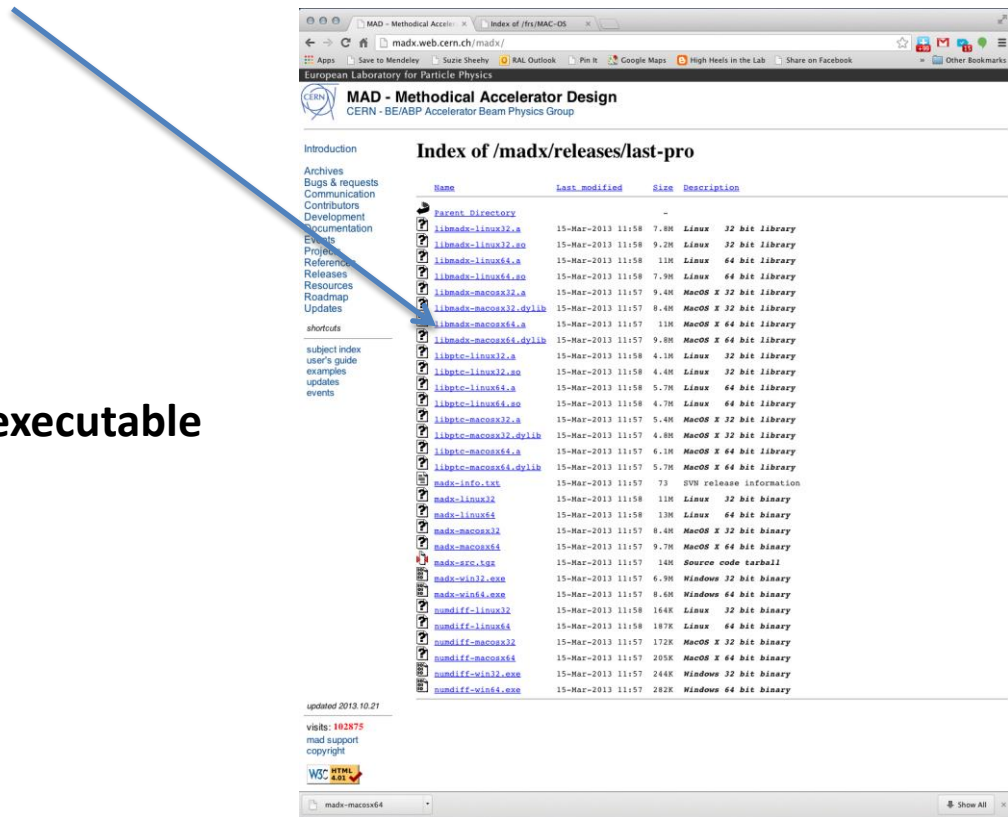
Go to 'Releases'

Get latest production version

Choose your system & download:

**NOTE: You may need to make it executable**

```
mv madx-macosx64 madx
chmod u+x madx
./madx
```



# How to run MADX

- In command prompt:
  - Go to directory (with madx.exe and input files)  
>> `madx.exe < inputfile > outputfile`
- Or on Mac OSX in terminal:
- >> `./madx < inputfile < outputfile`
  - Or you can add the madx.exe location to your path (if you know how...)

# An input file – Basic FODO

```
//
// MADX Example 1: FODO cell
// Author: V. Ziemann, Uppsala University
// Date: 060910
// UPDATED SUZIE SHEEHY 04/11/2013 FOR MADX VERSION 5.01.00

TITLE, 'Example 1: FODO.MADX';

BEAM, PARTICLE=ELECTRON, PC=3.0;

D: DRIFT, L=1.0;
QF: QUADRUPOLE, L=0.5, K1=0.2;
QD: QUADRUPOLE, L=0.5, K1=-0.2;

FODO: LINE=(QF, 5*(D), QD, QD, 5*(D), QF);

SETPLOT, POST=2, FONT=-1;

USE, PERIOD=FODO;
TWISS, SAVE, BETX=15.0, BETY=5.0;
PLOT, HAXIS=S, VAXIS=BETX, BETY, NOVERSION=TRUE, TITLE='unmatched beta functions';

// Here MATCH is used as a single command this finds periodic solution
USE, PERIOD=FODO;
MATCH, SEQUENCE=FODO;
TWISS, SAVE;
PLOT, HAXIS=S, VAXIS=BETX, BETY, NOVERSION=TRUE, TITLE='matched beta functions';

Value, TABLE(SUMM, Q1);
Value, TABLE(SUMM, Q2);
WRITE, TABLE=SUMM, FILE=print.dat;
```

← // comments out a line

TITLE at top of output

← Define particle type and momentum (pc) GeV/c  
Or can use ENERGY in GeV.

← Elements are given in the manual including definitions of L, K1 etc...

← Define a 'line' – can be a cell or a whole beamline that you will USE.

← Calculate beta functions from starting values

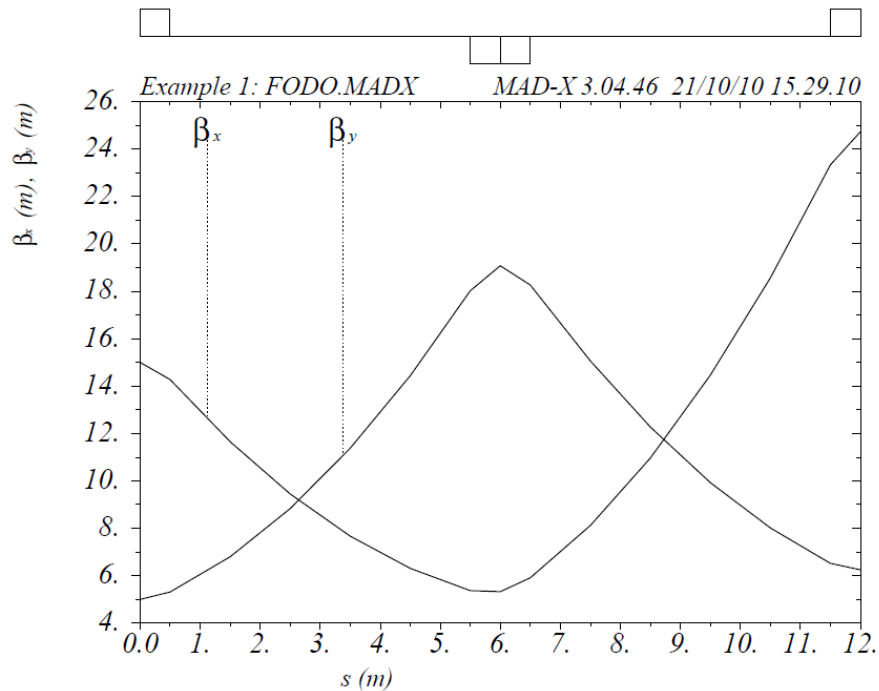
← Plot beta values from TWISS (internal table)

← Match the periodic solution (+Plot that)

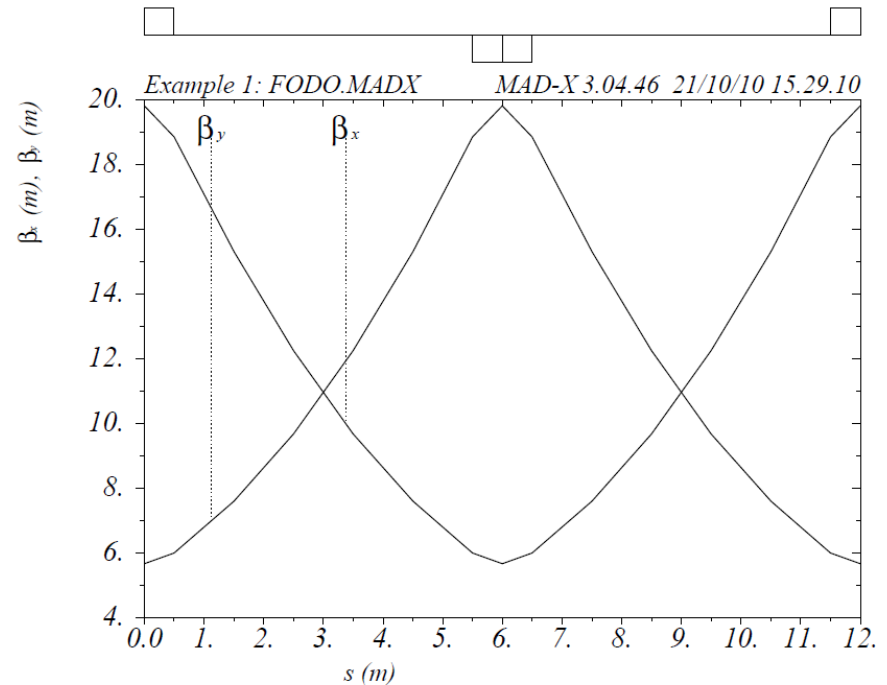
← Output to tables



# Result of a MADX run



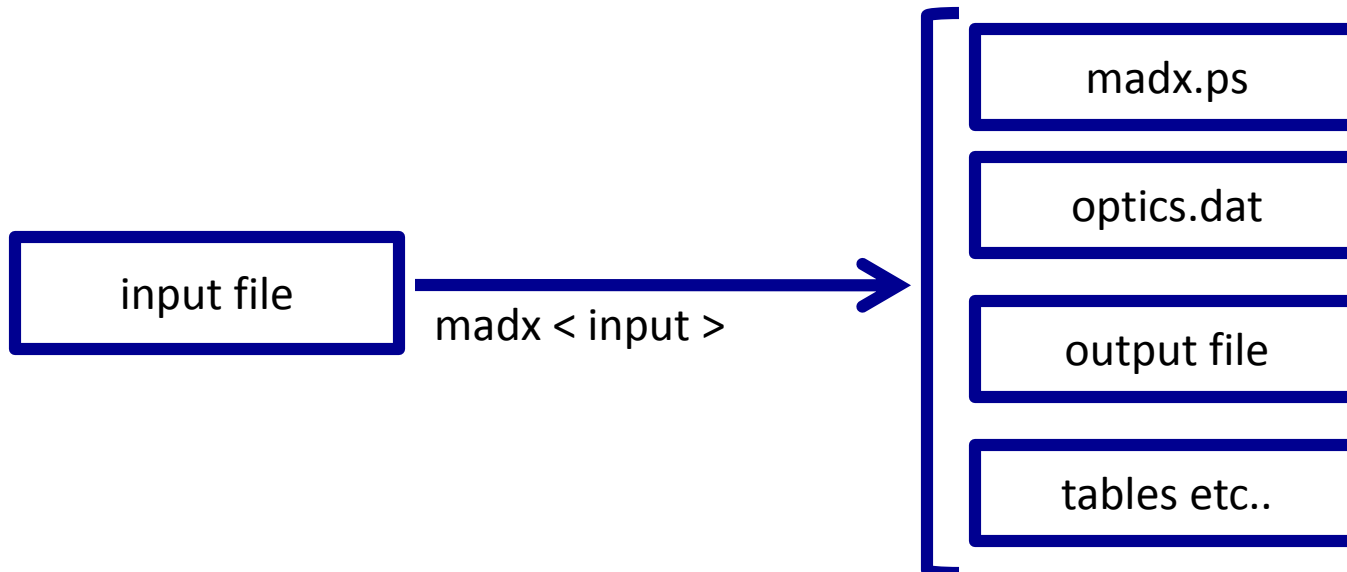
With  $\beta_x$  starting at 15m ( $\beta_y$  at 5m)



If the line is matched (periodic)  
 $\beta_{\text{start}} = \beta_{\text{end}}$

# Output files

- Optics.dat
- Your specified output file `madx< input > output`
- Can specify tables



# Add bending magnets

- Can introduce your own parameters (watch the :=)
- Can use alternative 'sequence' format
- Let's add dipoles
- Look at dispersion

```

TITLE,'Example 2: FODO2.MADX';
BEAM, PARTICLE=ELECTRON,PC=3.0;
DEGREE:=PI/180.0;           // for readability

QF: QUADRUPOLE,L=0.5,K1=0.2;  // still half-length
QD: QUADRUPOLE,L=1.0,K1=-0.2; // changed to full length
B: SBEND,L=1.0,ANGLE=15.0*DEGREE; // added dipole

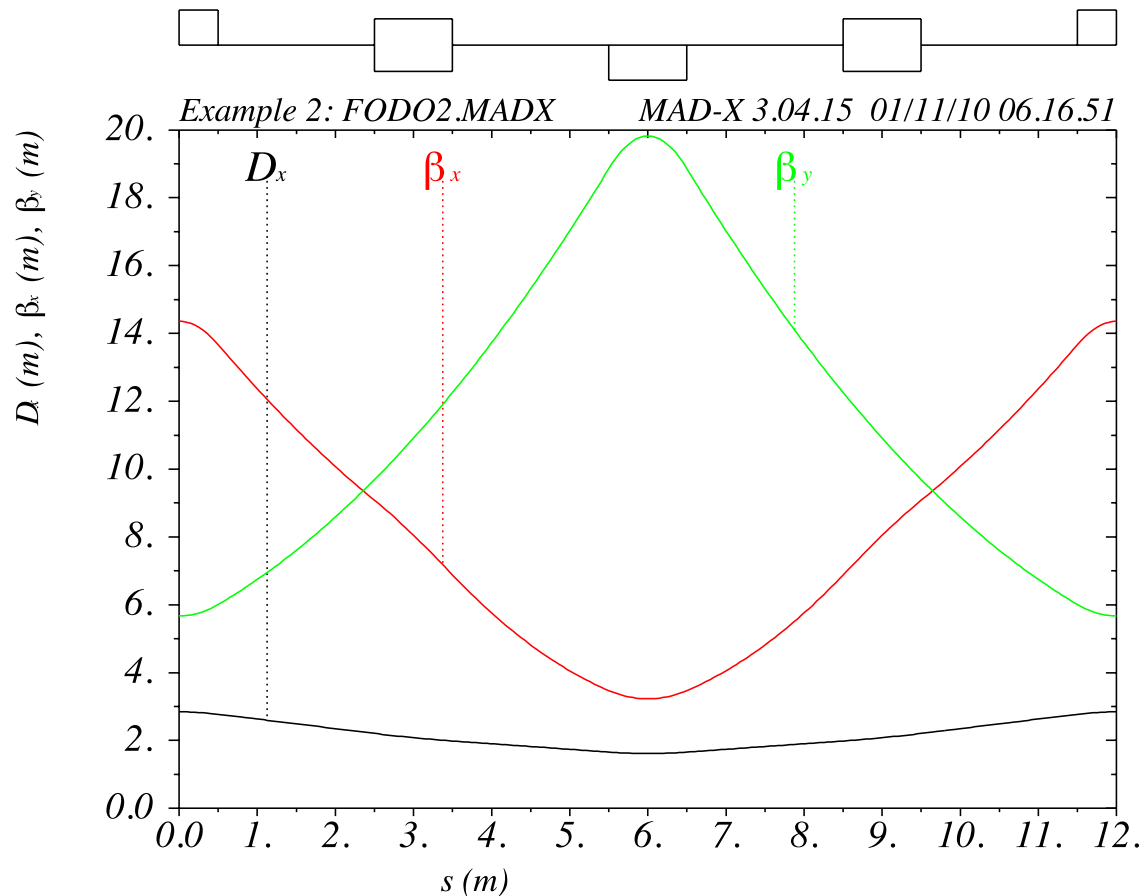
FODO: SEQUENCE,REFER=ENTRY,L=12.0;
  QF1: QF,  AT=0.0;
  B1:  B,   AT=2.5;
  QD1: QD,  AT=5.5;
  B2:  B,   AT=8.5;
  QF2: QF,  AT=11.5;
ENDSEQUENCE;

USE, PERIOD=FODO;
//MATCH, SEQUENCE=FODO; //Uncomment to match
SELECT,FLAG=SECTORMAP,clear;
SELECT,FLAG=TWISS,column=name,s,betx,bety;
TWISS, file=optics.dat,sectormap;

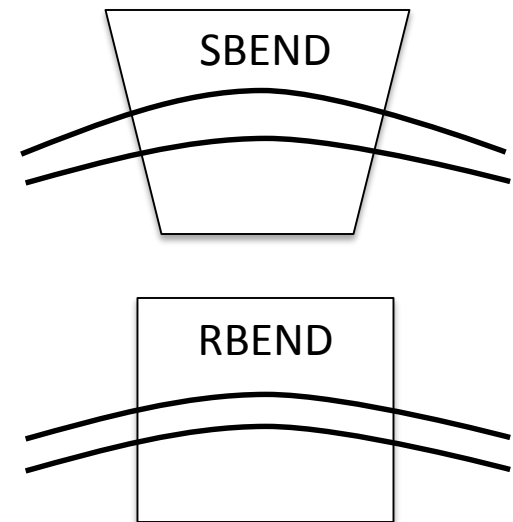
PLOT,HAXIS=S, COLOUR=100, VAXIS=DX, BETX, BETY,
INTERPOLATE=TRUE;

Value, TABLE(SUMM,Q1);
Value, TABLE(SUMM,Q2);
  
```

# Output from FODO with dipole



Note the colours!  
We now have dispersion  
(from bending magnet)  
Focusing changed as we  
used SBEND



- If you add  
SELECT, FLAG=SECTOR  
SELECT, FLAG=TWISS,  
TWISS, file=optics
- You will get  
matrices
- and an out

You can customise  
select, flag=my\_sec  
Or even select by comp  
select, flag=my\_sec

```

optics.dat
@ NAME           %05s "TWISS"
@ TYPE           %05s "TWISS"
@ SEQUENCE       %04s "FODO"
@ PARTICLE       %08s "ELECTRON"
@ MASS           %le      0.000510998902
@ CHARGE         %le      -1
@ ENERGY        %le      3.000000044
@ PC             %le      3
@ GAMMA          %le      5870.854187
@ KBUNCH         %le      1
@ BCURRENT       %le      0
@ SIGE           %le      0
@ SIGT           %le      0
@ NPART          %le      0
@ EX             %le      1
@ EY             %le      1
@ ET             %le      1
@ LENGTH         %le      12
@ ALFA           %le      0.0910331259
@ ORBIT5         %le      -0
@ GAMMATR        %le      3.314364527
@ Q1             %le      0.2909501025
@ Q2             %le      0.1913459932
@ DQ1            %le      -0.2152485772
@ DQ2            %le      -0.2276020063
@ DXMAX          %le      2.84272104
@ DYNAMX         %le      0
@ XCOMAX         %le      0
@ YCOMAX         %le      0
@ BETXMAX        %le      14.36014477
@ BETYMAX        %le      18.85637615
@ XCORMS         %le      0
@ YCORMS         %le      0
@ DXRMS          %le      2.388159047
@ DYRMS          %le      0
@ DELTAP         %le      0
@ SYNCH_1        %le      0
@ SYNCH_2        %le      0
@ SYNCH_3        %le      0
@ SYNCH_4        %le      0
@ SYNCH_5        %le      0
@ TITLE          %21s "Example 2: FODO2.MADX"
@ ORIGIN         %20s "MAD-X 3.04.15 Darwin"
@ DATE           %08s "01/11/10"
@ TIME           %08s "08.52.11"
* NAME           S           BETX           BETY
$ %s             %le      %le      %le
"FODO$START"    0           14.36014477    5.674619595
"QF1"           0.5         13.67114589    6.007906055
"DRIFT_0"       2.5         9.081076899    9.690010744
"B1"            3.5         6.880079877    12.25970476
"DRIFT_0"       5.5         3.471640314    18.85637615
"QD1"           6.5         3.471640314    18.85637615
"DRIFT_0"       8.5         6.880079877    12.25970476
"B2"            9.5         9.081076899    9.690010744
    
```

# Matching

- Matching lets MAD-X do the tedious work for you!
- Before MATCH select at least one sequence (USE)
- Initiated by the MATCH command
- Initiating:
  - MATCH, SEQUENCE='name1', 'name2',..., 'nameX';
- Can define constraints & variables (magnets) to achieve aim

```
MATCH, SEQUENCE = FODO;
```

```
CONSTRAINT,SEQUENCE=FODO, RANGE=#E, MUX=0.1666666, MUY=0.25;
```

```
VARY, NAME=QF->K1, STEP=1E-6;
```

```
VARY, NAME=QD->K1, STEP=1E-6;
```

```
LMDIF,CALLS=500,TOLERANCE=1E-20;
```

```
ENDMATCH;
```

# Matching input file

```
TITLE, 'Example 3: MATCH1.MADX';  
BEAM, PARTICLE=ELECTRON, PC=3.0;
```

```
D: DRIFT, L=1.0;  
QF: QUADRUPOLE, L=0.5, K1:=0.2;  
QD: QUADRUPOLE, L=0.5, K1:=-0.2;
```

```
FODO: LINE=(QF, 5*(D), QD, QD, 5*(D), QF);  
USE, PERIOD=FODO;
```

```
//...match phase advance at end of cell to 60 and 90 degrees  
MATCH, SEQUENCE=FODO;  
CONSTRAINT, SEQUENCE=FODO, RANGE=#E, MUX=0.16666666, MUY=0.25;  
VARY, NAME=QF->K1, STEP=1E-6;  
VARY, NAME=QD->K1, STEP=1E-6;  
LMDIF, CALLS=500, TOLERANCE=1E-20;  
ENDMATCH;
```

```
SELECT, FLAG=SECTORMAP, clear;  
SELECT, FLAG=TWISS, column=name, s, betx, alfx, bety, alfy;  
TWISS, file=optics.dat, sectormap;
```

```
PLOT, HAXIS=S, VAXIS=BETX, BETY;  
Value, TABLE(SUMM, Q1); // verify result  
Value, TABLE(SUMM, Q2);
```

Matching commands

Print out final values of matching

# Matching example

- Demonstration MATCH1.MADX



# Fitting beta functions

- Use MATCH2.MADX

```

Initial Penalty Function = 0.87329908E+02

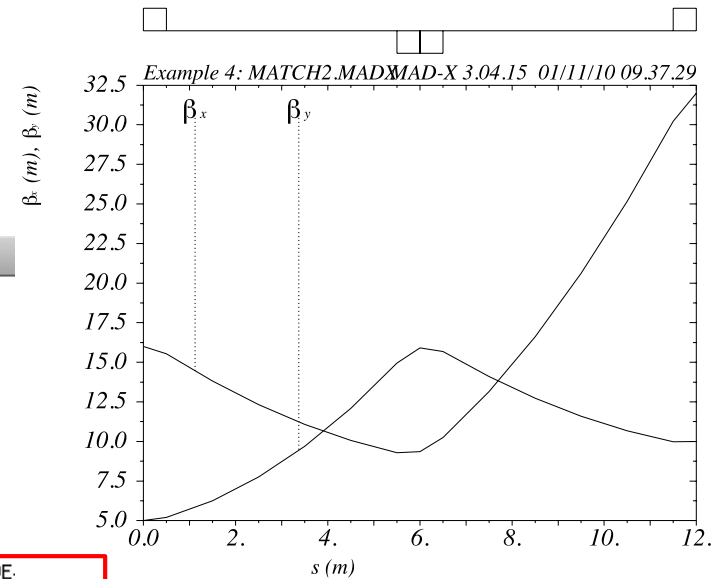
call:      5  Penalty function = 0.14687632E+02
call:      8  Penalty function = 0.52122712E+00
call:     11  Penalty function = 0.14867643E-03
call:     14  Penalty function = 0.17048760E-10
call:     17  Penalty function = 0.86820304E-19
call:     20  Penalty function = 0.66895405E-27
+++++++ LMDIF ended: converged successfully
call:     20  Penalty function = 0.66895405E-27
fodo$end:1      betx      4      3.20000000E+01      3.20000000E+01      5.04870979E-
fodo$end:1      bety      4      1.00000000E+01      1.00000000E+01      6.18466950E-20
qf->k1          1.21494427E-01      -1.00000000E+20      1.00000000E+20
qd->k1          -1.58047975E-01      -1.00000000E+20      1.00000000E+20

GXPLOTT-X11 1.50 initialized

plot number = 1

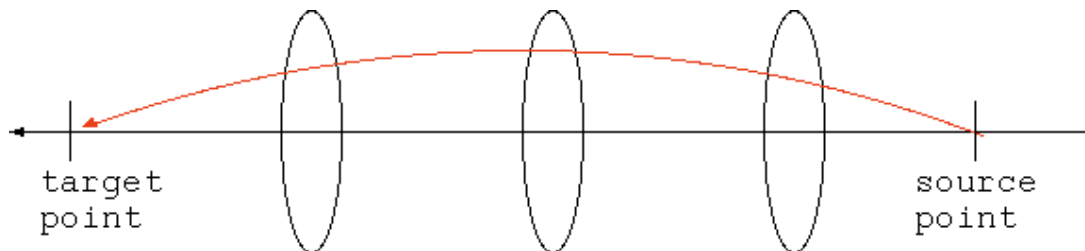
+++++++
+          MAD-X 3.04.15          +
+ Code Modification Date: 15.01.2008      +
+ Execution Time Stamp: 01.11.10 09.39.37 +
+++++++
//
// MADX Example 1: FODO matching final beta function

```



# Transfer matrix matching

- Sometimes want to constrain transfer matrix elements to some value.
- For example  $R_{16}=0$  and  $R_{26}=0$  will make the horizontal position and angle independent of the momentum after a beamline.
- This is called an 'Achromat'.
- Other versions are imaginable
- point-to-point imaging  $\rightarrow R_{12} = 0$ .
  - This means  $\sin(\mu)=0$  or a phase advance of a multiple of  $\pi$ .



# Examples in MAD-X

- FODO arcs
- Dispersion suppressor
- ‘Telescopes’ for low- $\beta$
- Synchrotron radiation lattices + achromats

# Is that it?

- ‘the not-so-ideal world’
- What happens to  $\alpha, \beta, \gamma$  if we stop focusing for a distance?

$$b(s) = b_0 - 2a_0s + g_0s^2$$

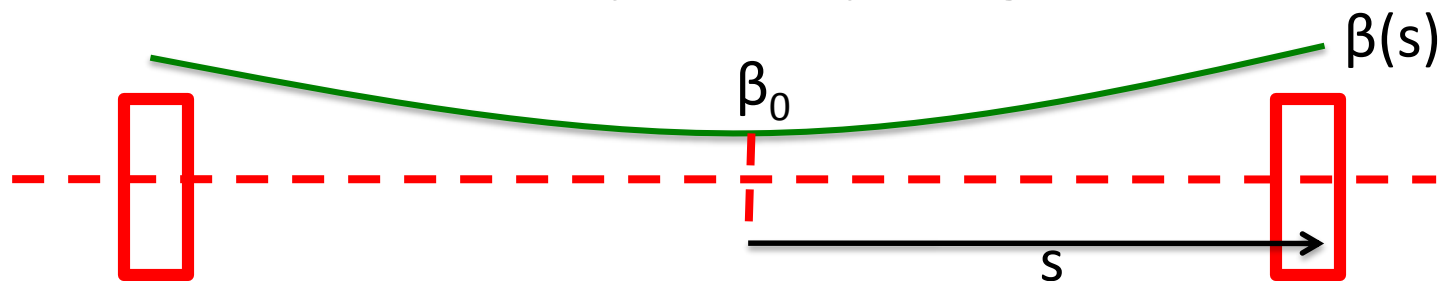
$$a(s) = a_0 - g_0s$$

$$g(s) = g_0$$

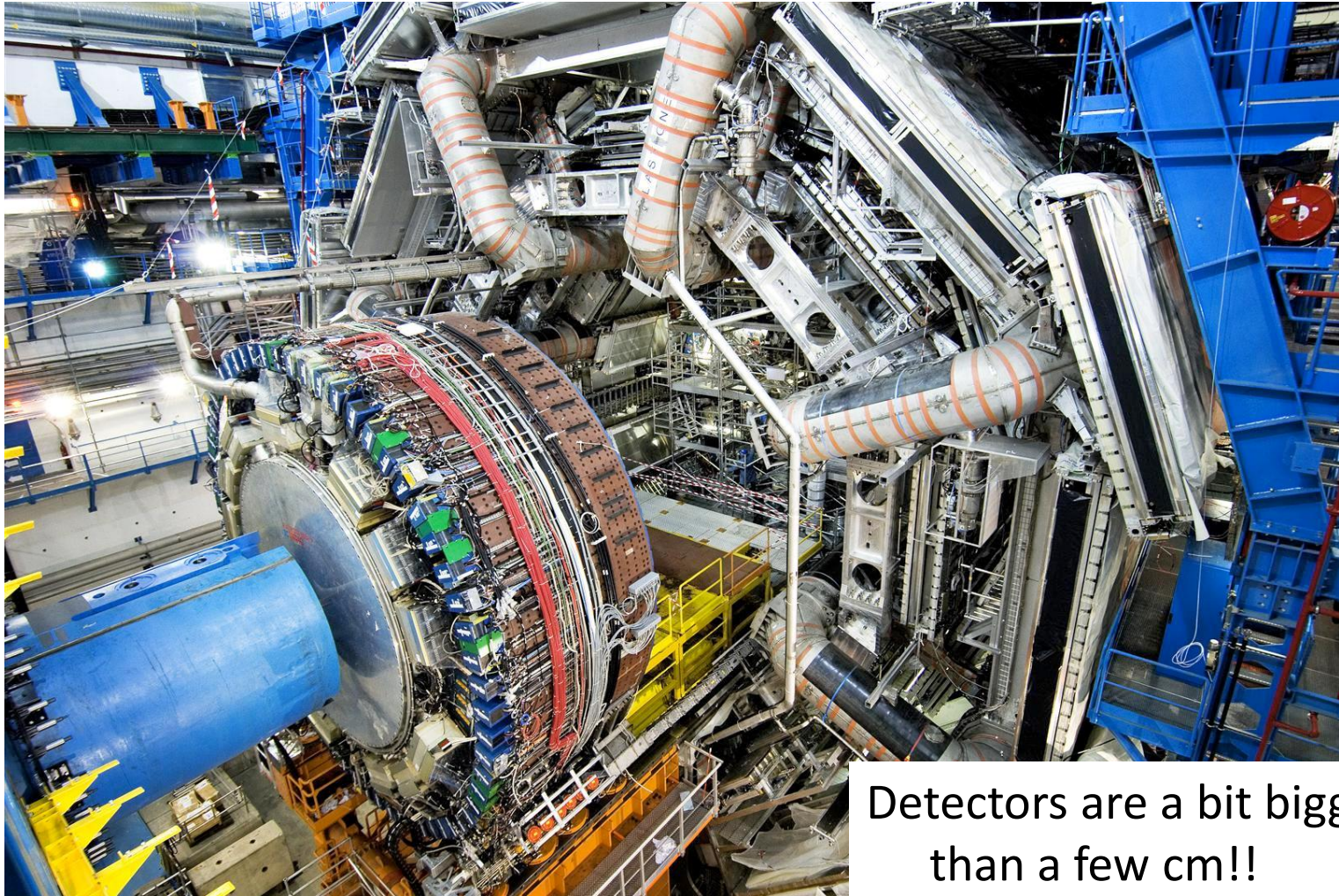
The drift length:

$$M = \begin{pmatrix} \hat{e}1 & s\hat{u} \\ \hat{e}0 & 1\hat{u} \end{pmatrix}$$

- If we take the center of a drift ( $\alpha_0=0$ ), we find  $b(s) = b_0 + \frac{s^2}{b_0}$
- It doesn't matter what you do –  $\beta$  will grow!



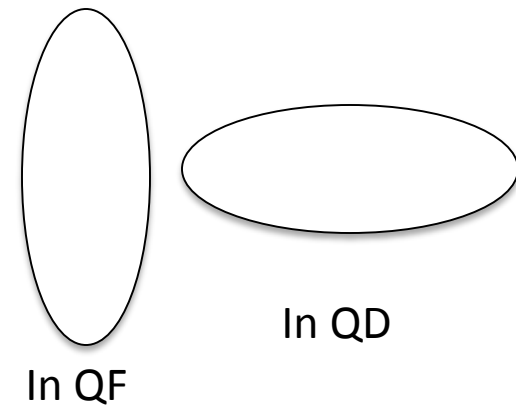
# Seems fine, until...



Detectors are a bit bigger  
than a few cm!!

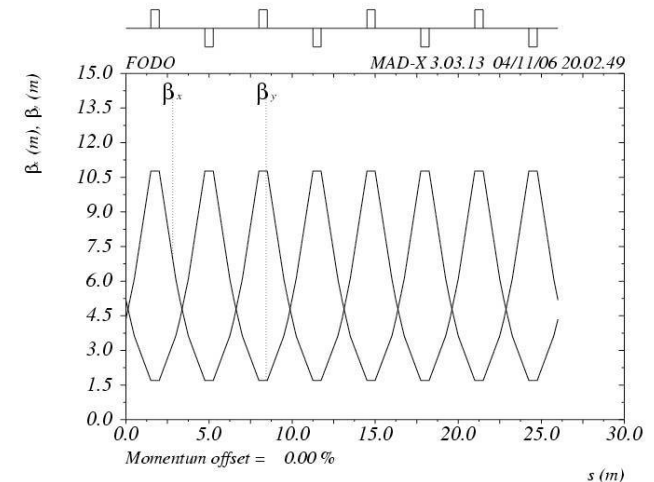
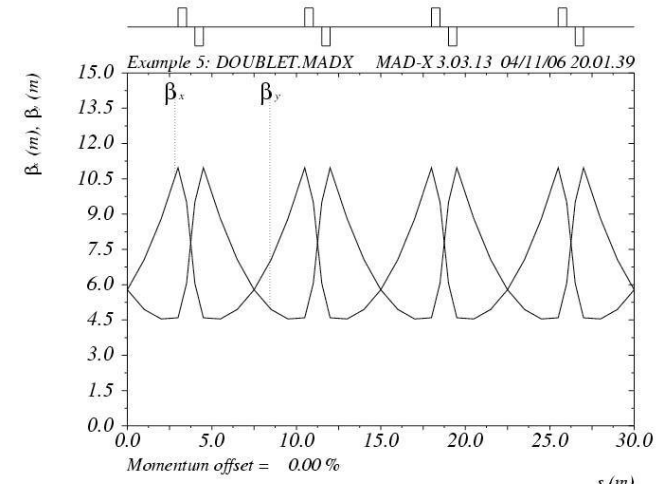
# FODO Arcs

- Usually in colliders – take beam between interaction regions
- Simple and tunable ( $\beta_x$  large in QF,  $\beta_y$  at QD)
- Moderate quad strengths
- The beam is not round
- In arcs dipoles generate dispersion



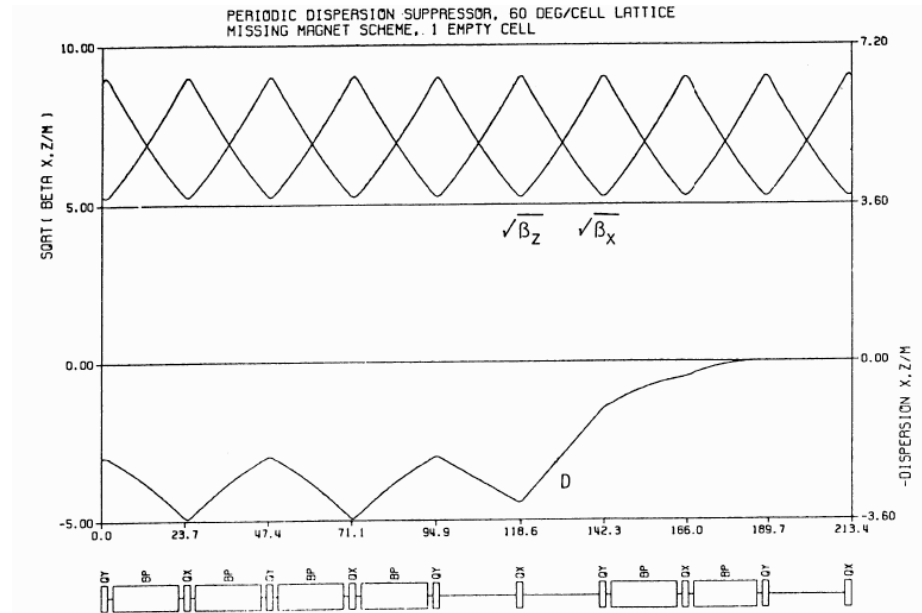
# FD Doublet Lattice

- More space between quads
- Stronger quad strengths
- Round beams
- Used in CTF3 linac



# Dispersion suppressor

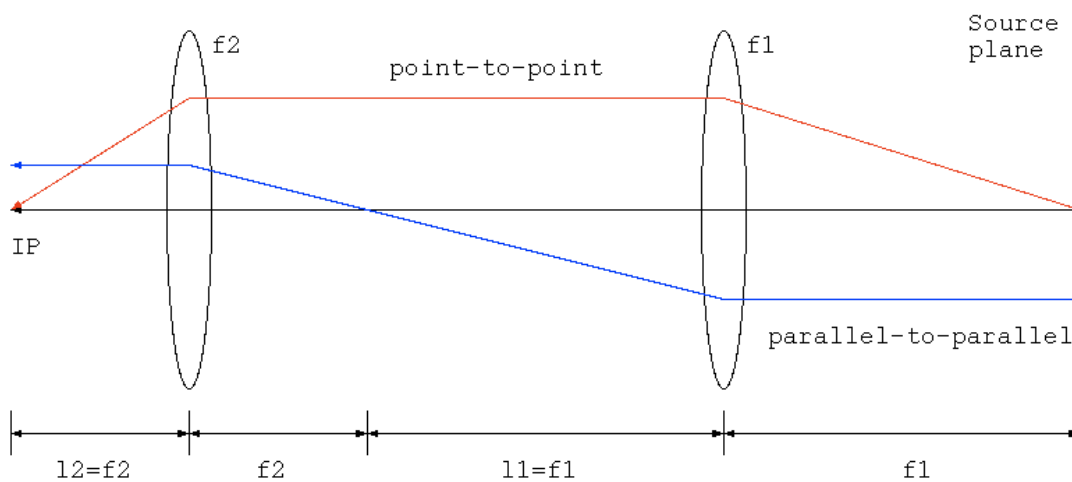
- Want small spot size at interaction point
- Spot size:  $\sqrt{\epsilon\beta + (D\Delta p/p)^2}$
- Missing magnet dispersion suppression scheme
- Works with proper phase advance between elements



Bring D from FODO cell value to zero by a forced oscillation around  $\sim\frac{1}{2}$  of that in the FODO cells



# Telescope and low $\beta$



- Used in colliders to achieve small beam size at IP
- Doublet or Triplet
- Want:
  - Point-to-point  $R_{12}=0$
  - Parallel to parallel  $R_{21}=0$
  - $R_{11}$ =demagnification
- Ratio of focal lengths
- Needs to work in both planes with doublets/triplets

$$\begin{pmatrix} x \\ C \\ e \end{pmatrix}_1 = \begin{pmatrix} l_1 & 0 \\ 0 & 1 \\ 0 & -1/f_1 \end{pmatrix} \begin{pmatrix} x \\ C \\ e \end{pmatrix}_2$$

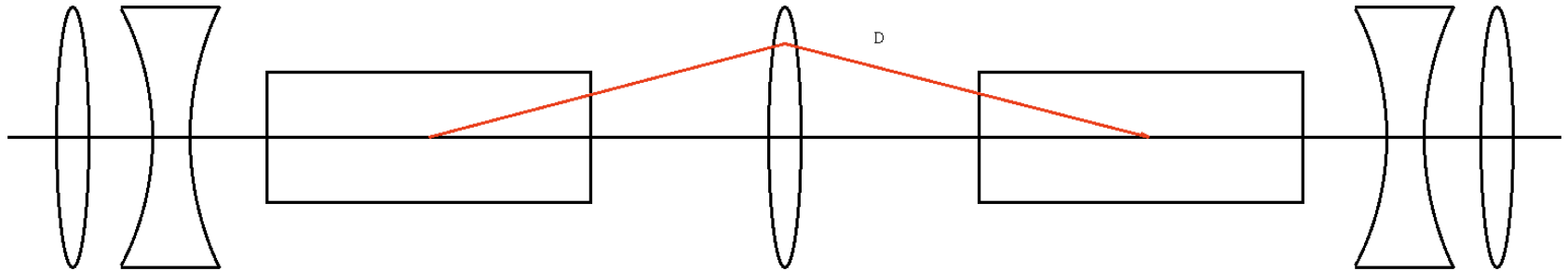
For one module with  $l_1=f_1$

$$\begin{pmatrix} x \\ C \\ e \end{pmatrix}_1 = \begin{pmatrix} 0 & f_1 \\ -1/f_1 & 0 \end{pmatrix} \begin{pmatrix} x \\ C \\ e \end{pmatrix}_2$$

For both modules:

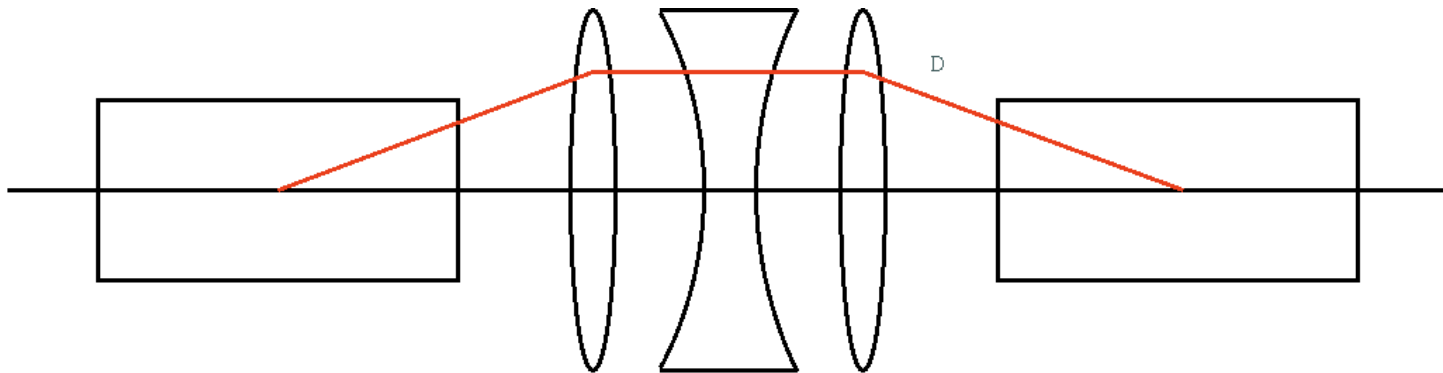
$$R = \begin{pmatrix} -f_2/f_1 & 0 \\ 0 & -f_1/f_2 \end{pmatrix}$$

# Double bend achromat



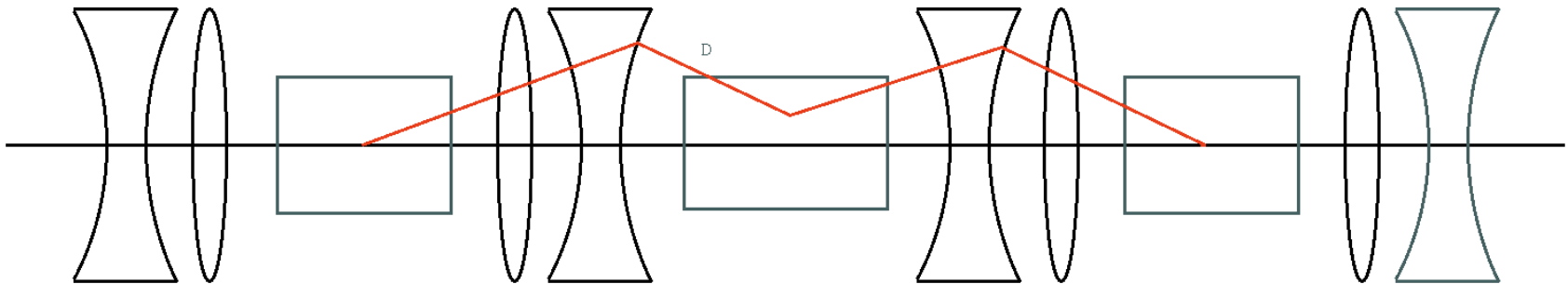
- One dipole generates dispersion and the next, which is 180 degrees apart will take it out again
- Remember: the dispersion is the orbit of a particle with slightly too high momentum w.r.t the reference particle
- Quadrupoles are used to make  $\beta_x$  in dipoles small

# Triplet achromat



- Do the 180 degrees in the horizontal plane and the beta matching by quads between dipoles
- very compact, few magnets, but not flexible

# Triple bend achromat



- Small emittance.
- Very flexible due to large number of quadrupoles.
- Adjacent drift space can be made long to accommodate undulators/wigglers.

# Resources

- Many examples available at the MAD-X website
  - A helpful ‘primer’ by W. Herr:  
[http://madx.web.cern.ch/madx/doc/madx\\_primer.pdf](http://madx.web.cern.ch/madx/doc/madx_primer.pdf)

You can always ask me or another lecturer – though we can’t promise to know the answer!