

# MACHINE LEARNING FOR B-JET TAGGING

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MICHELA PAGANINI  
ON BEHALF OF THE ATLAS COLLABORATION

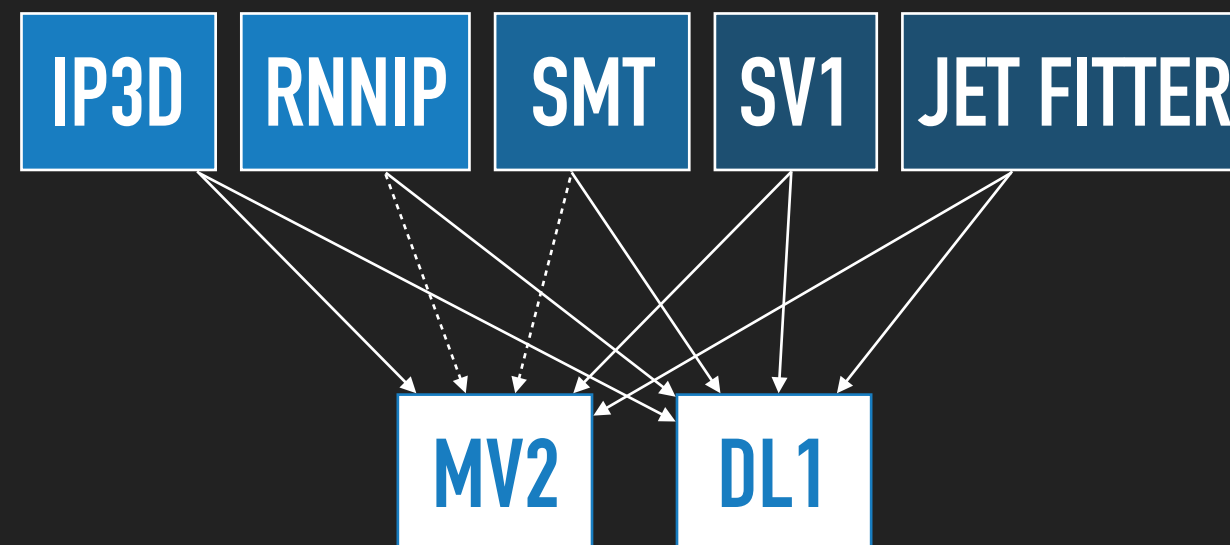
## OPTIMIZATION AND PERFORMANCE STUDIES FOR B-TAGGING IN ATLAS

### IN THIS TALK

ATLAS-PHYS-PUB-2017-003

ATLAS-PHYS-PUB-2017-013

- ▶ Description of flavor tagging ecosystem for the 2017-18 run
- ▶ Focus on Deep Learning-powered improvements

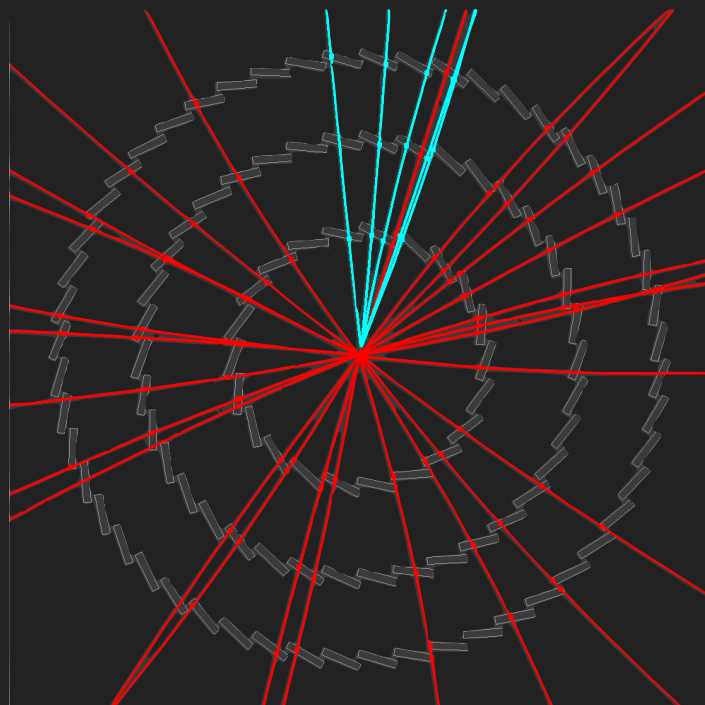
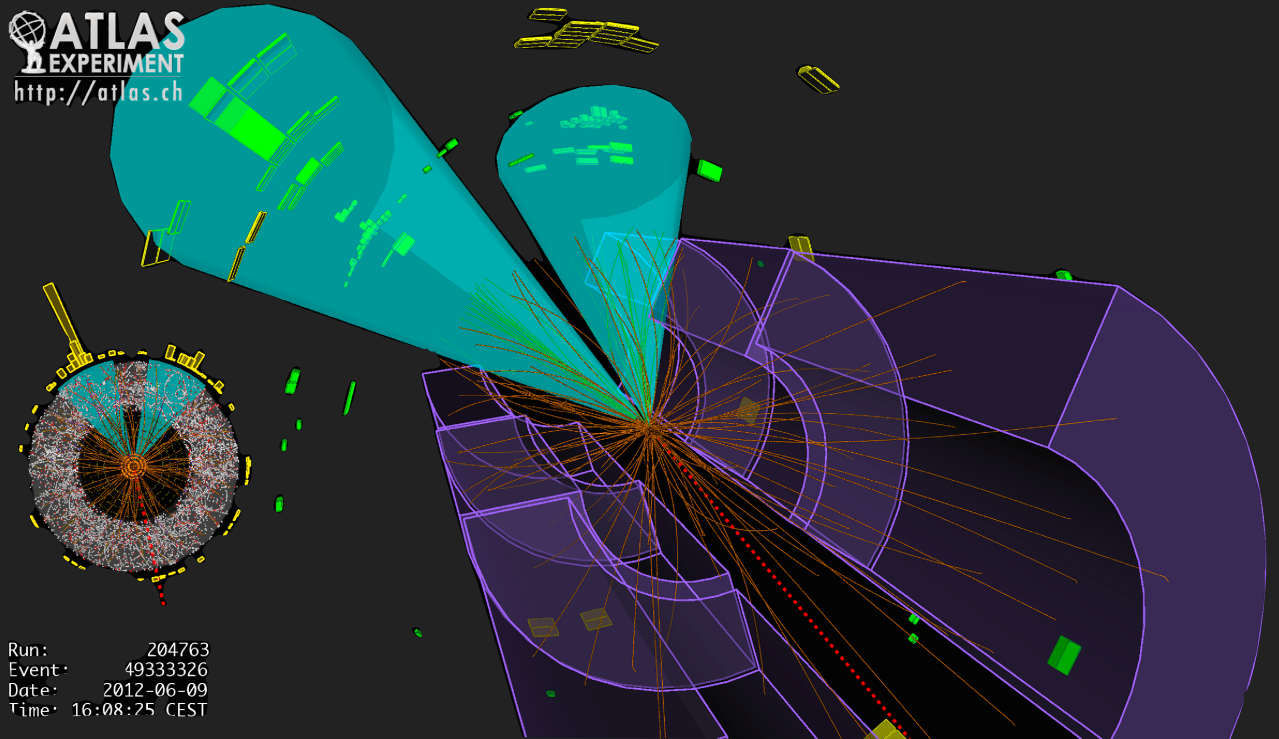


## FLAVOR TAGGING REVIEW

### GOAL OF FLAVOR TAGGING

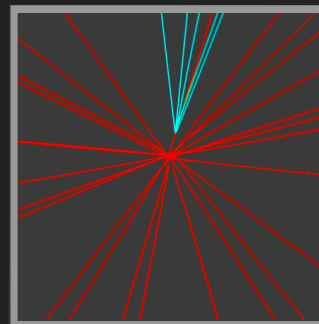
Separate jets that contain ***b*-hadrons** from jets initiated by lighter quark flavors

ATLAS  
EXPERIMENT  
<http://atlas.ch>



ATLAS  
EXPERIMENT  
Run 142195, Event 284154

Decay length = 3.7 mm  
Decay length significance = 22  
Lifetime = 3.1 ps  
Vertex mass = 2.5 GeV  
Number of tracks = 5



- ▶ Average *b*-hadron lifetime  
→ distance travelled before  
decaying (~mm) ideal for  
detection in ATLAS

## FLAVOR TAGGING REVIEW

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### B-HADRON DECAY

- ▶  $b$ -hadron contains  $b$  quark, which decays through a cascade

<b>u</b> up	<b>c</b> charm	<b>t</b> top
<b>d</b> down	<b>s</b> strange	<b>b</b> bottom

Limited by detector resolution, pileup, tracking inefficiency, material interactions, and long-lived decays for light jets

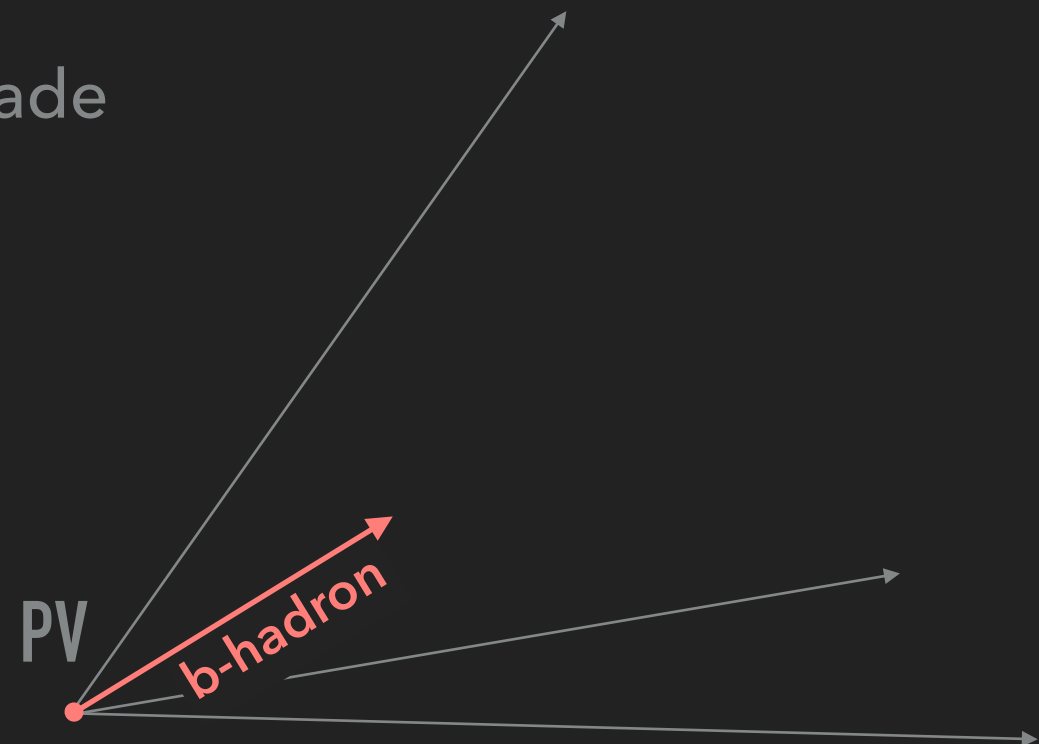
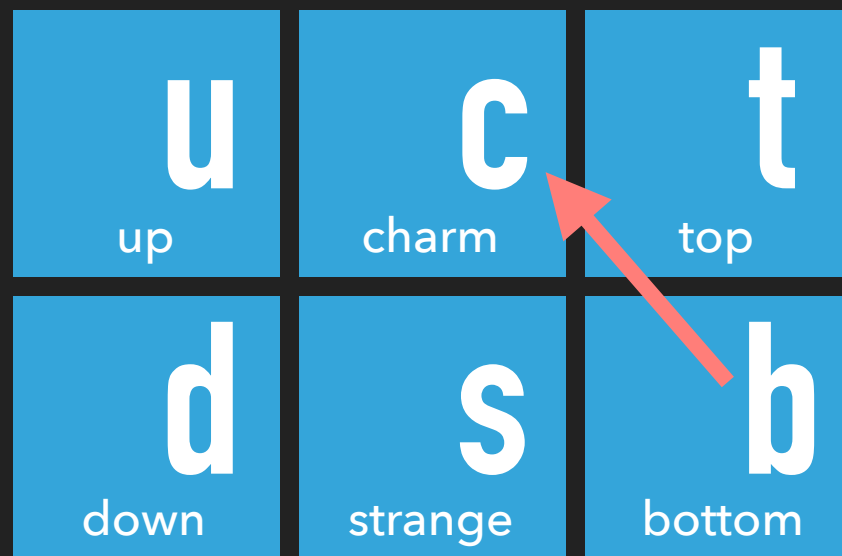


## FLAVOR TAGGING REVIEW

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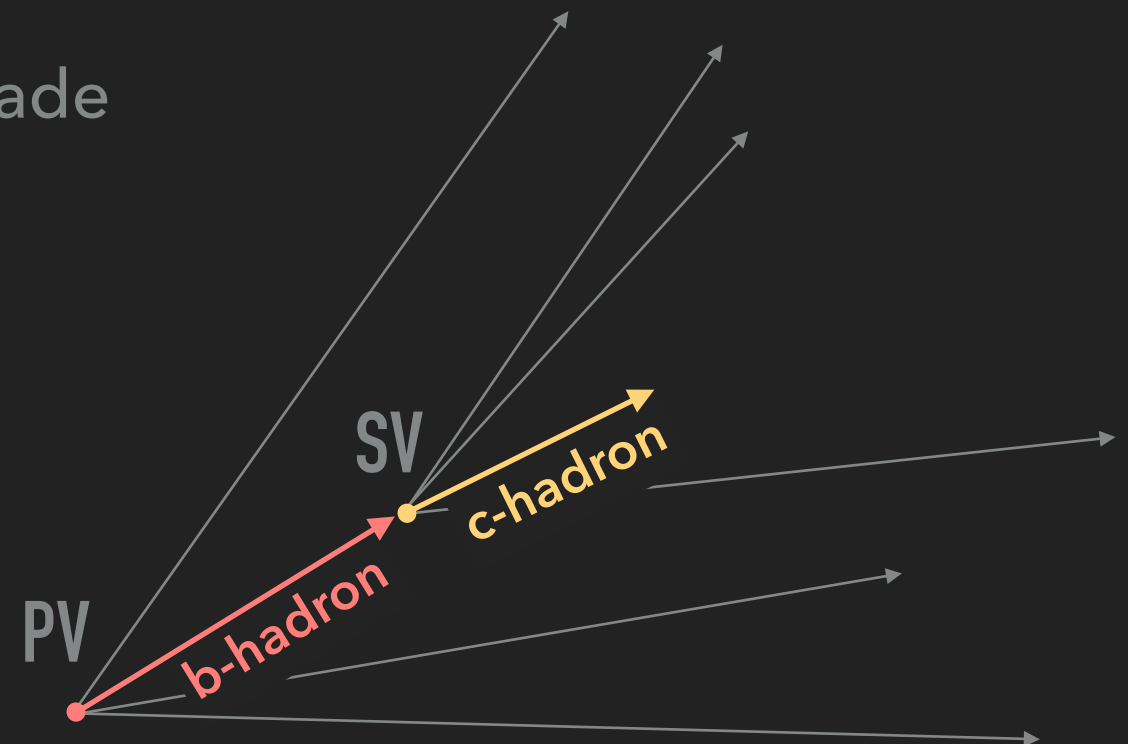
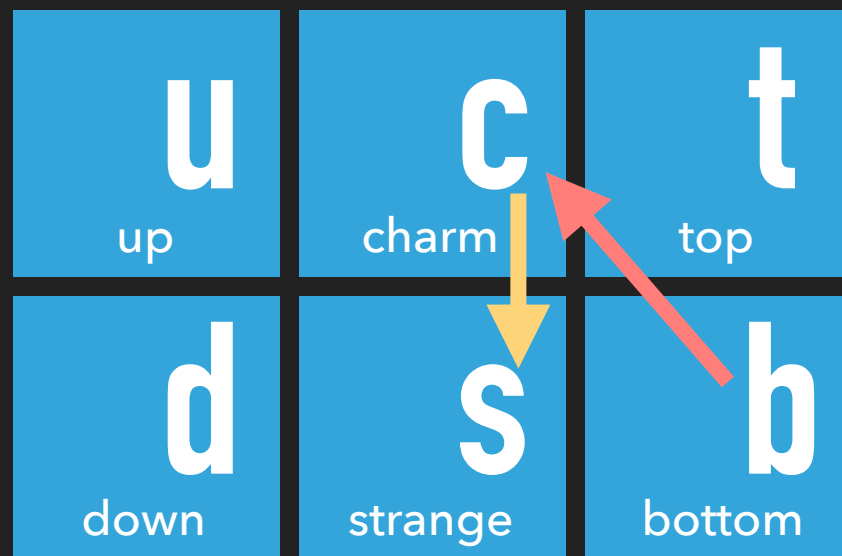


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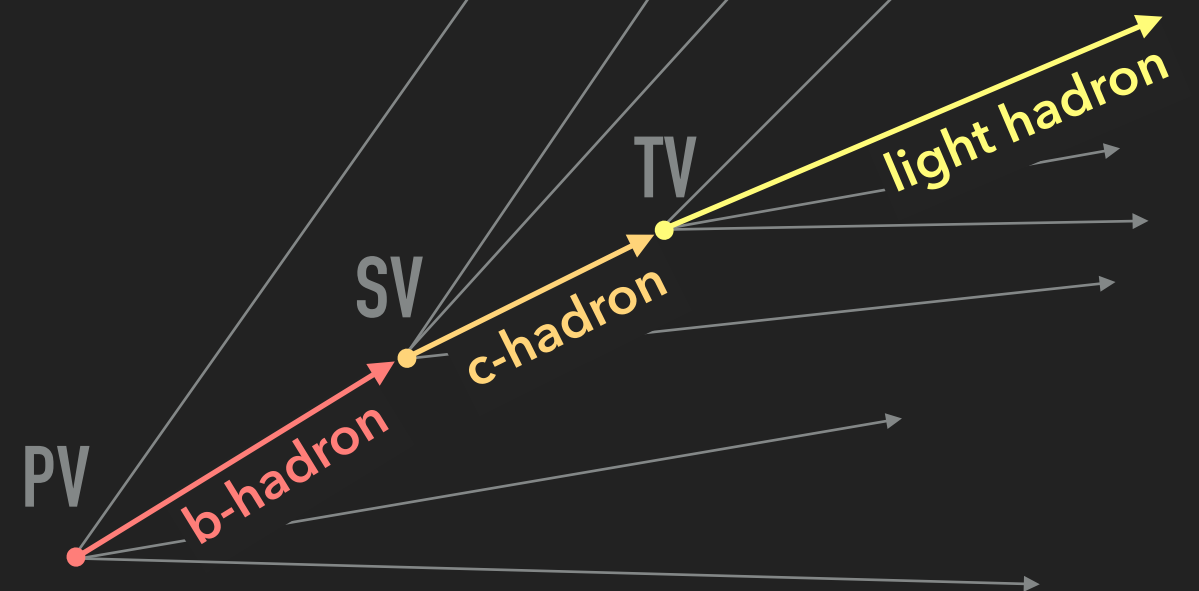
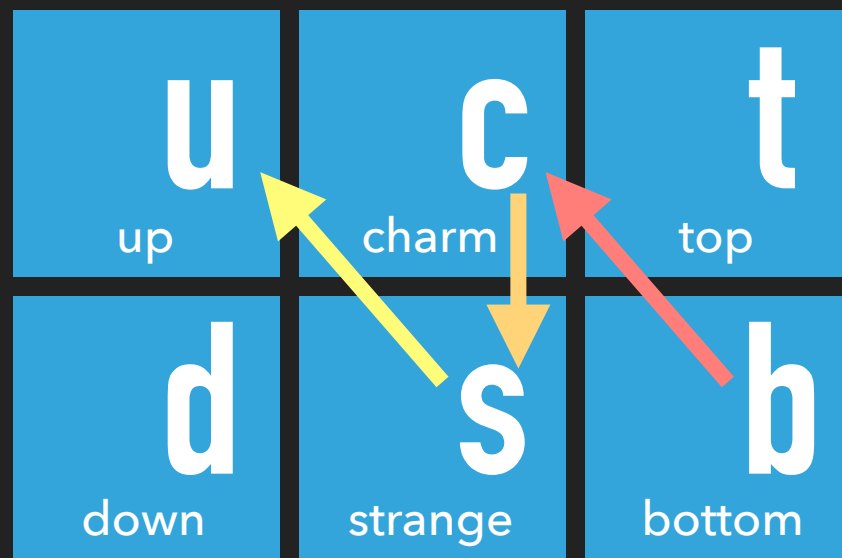


Limited by detector resolution, pileup, tracking inefficiency, material interactions, and long-lived decays for light jets

## FLAVOR TAGGING REVIEW

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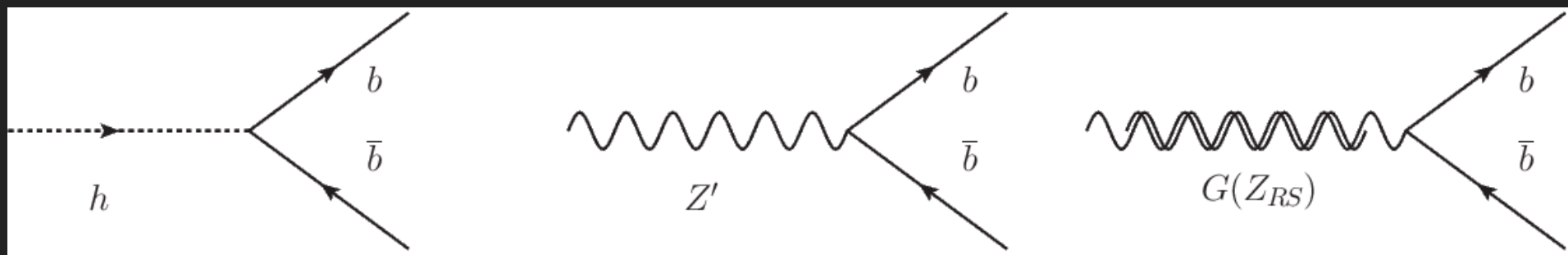


Limited by detector resolution, pileup, tracking inefficiency, material interactions, and long-lived decays for light jets

## FLAVOR TAGGING REVIEW

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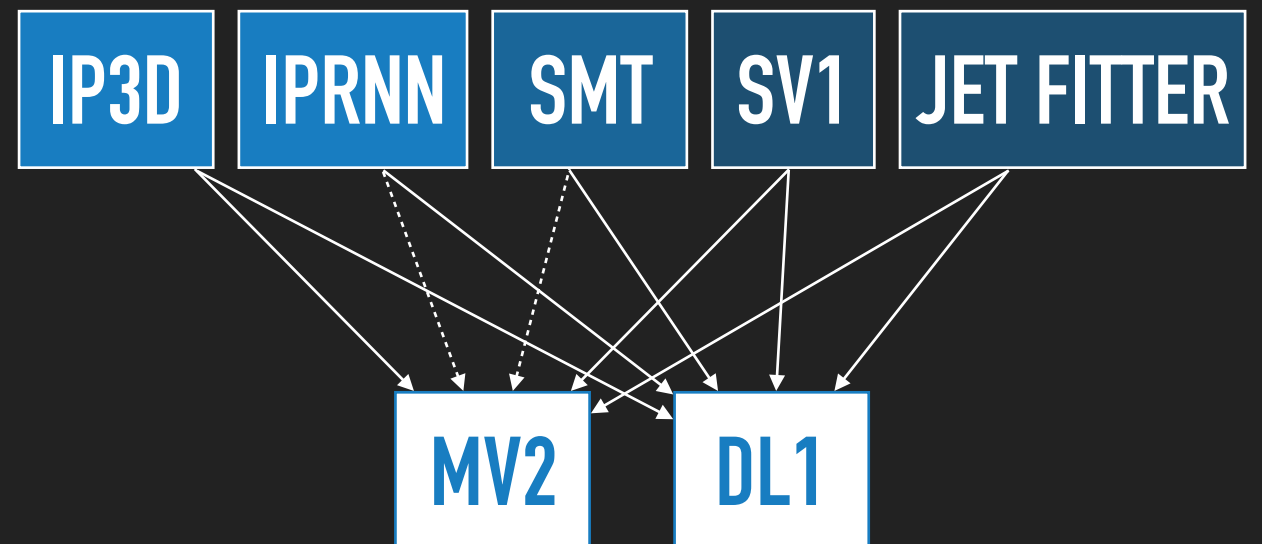
- ▶ Truth labels:
  - ▶  $b$ : if  $b$ -hadron with  $p_T > 5$  GeV within  $\Delta R=0.3$  of jet axis
  - ▶  $c$ : if not  $b$  &  $c$ -hadron with  $p_T > 5$  GeV within  $\Delta R=0.3$  of jet axis
  - ▶  $\tau$ : if not  $b$  or  $c$  &  $\tau$ -lepton with  $p_T > 5$  GeV within  $\Delta R=0.3$  of jet axis
  - ▶ light: otherwise
- ▶ Important for ATLAS Physics program ( $H \rightarrow b\bar{b}$ , SUSY, ...)



## LOW LEVEL TAGGERS

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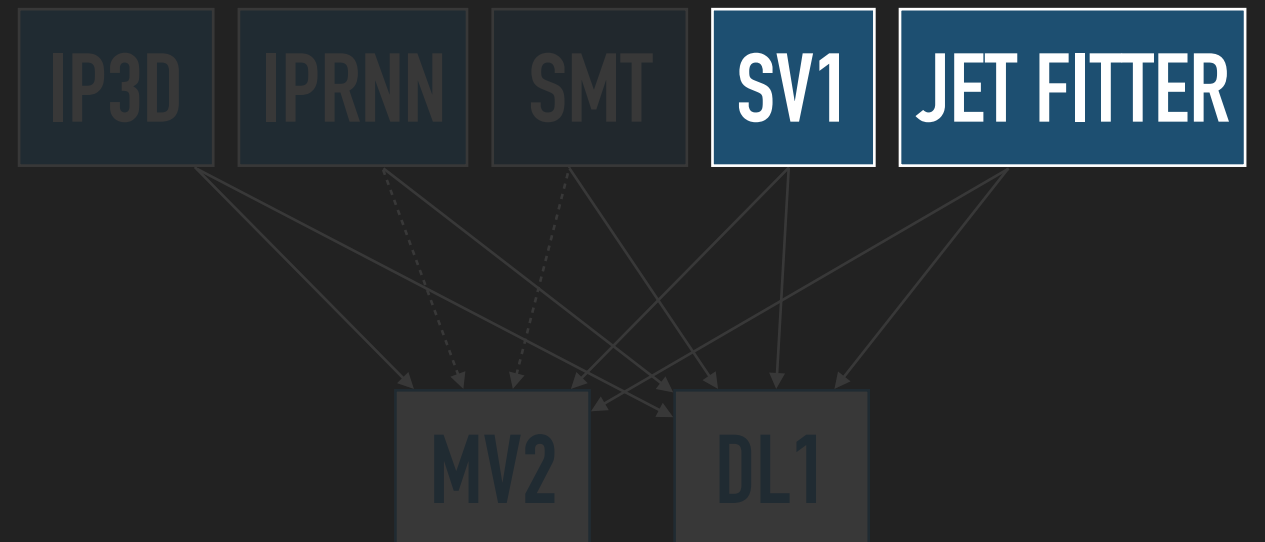
### VERTEX FINDING ALGORITHMS



## LOW LEVEL TAGGERS

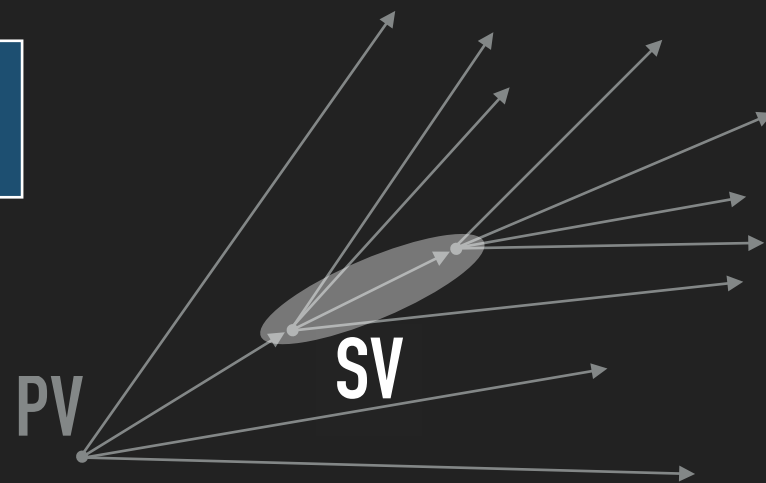
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### VERTEX FINDING ALGORITHMS



## VERTEX FINDING ALGORITHMS

SV1

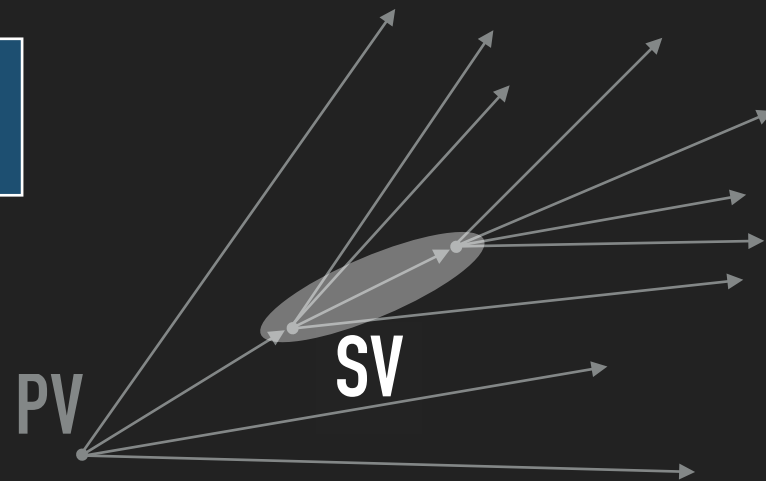


- ▶ reconstructs a single displaced vertex

JET FITTER

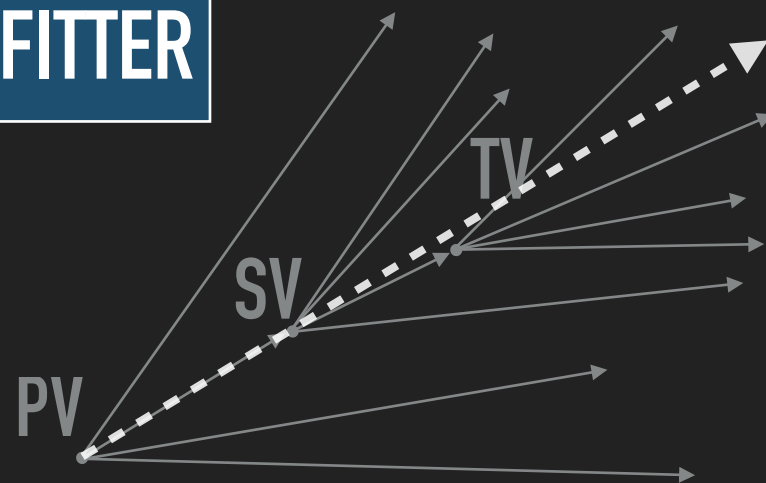
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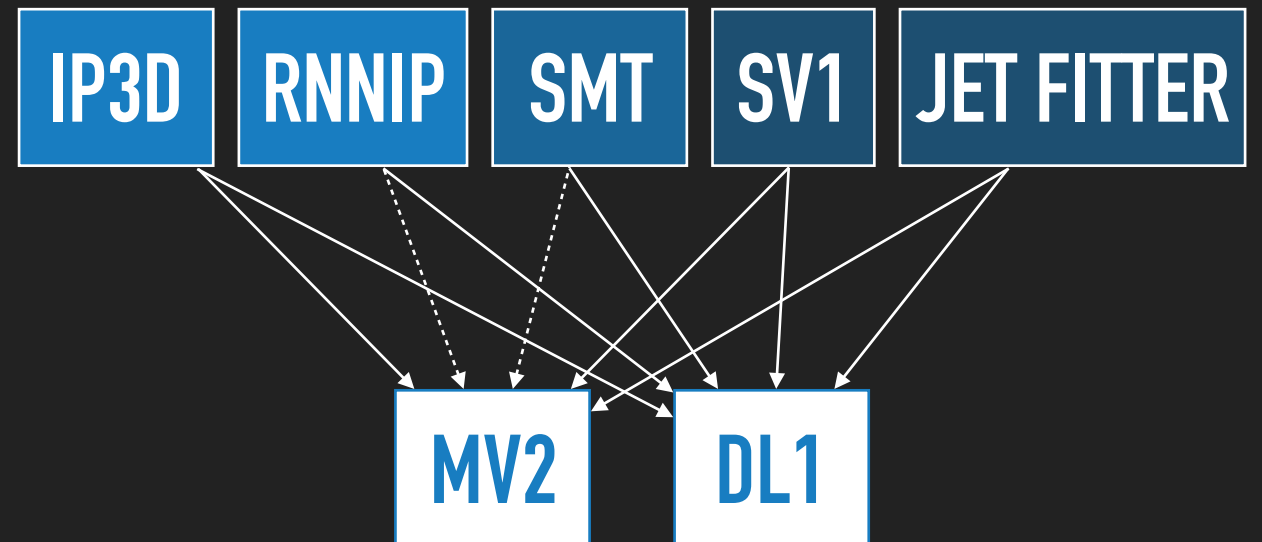
- ▶ performs a topological decay reconstruction along the  $b$ -hadron line of flight



## LOW LEVEL TAGGERS

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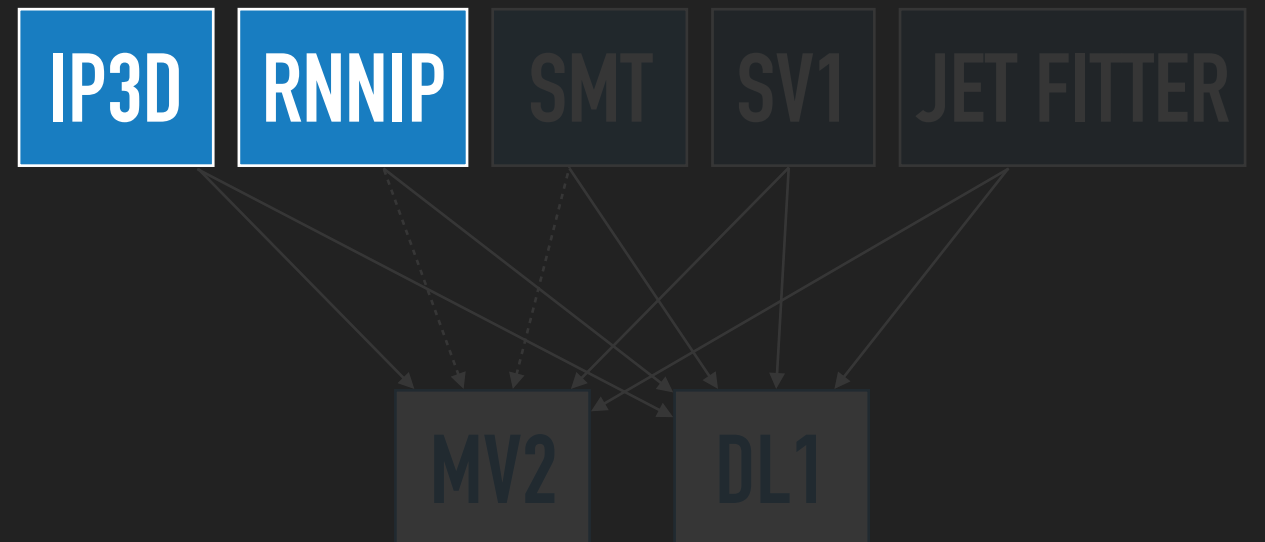
### IMPACT PARAMETER TAGGERS



## LOW LEVEL TAGGERS

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### IMPACT PARAMETER TAGGERS

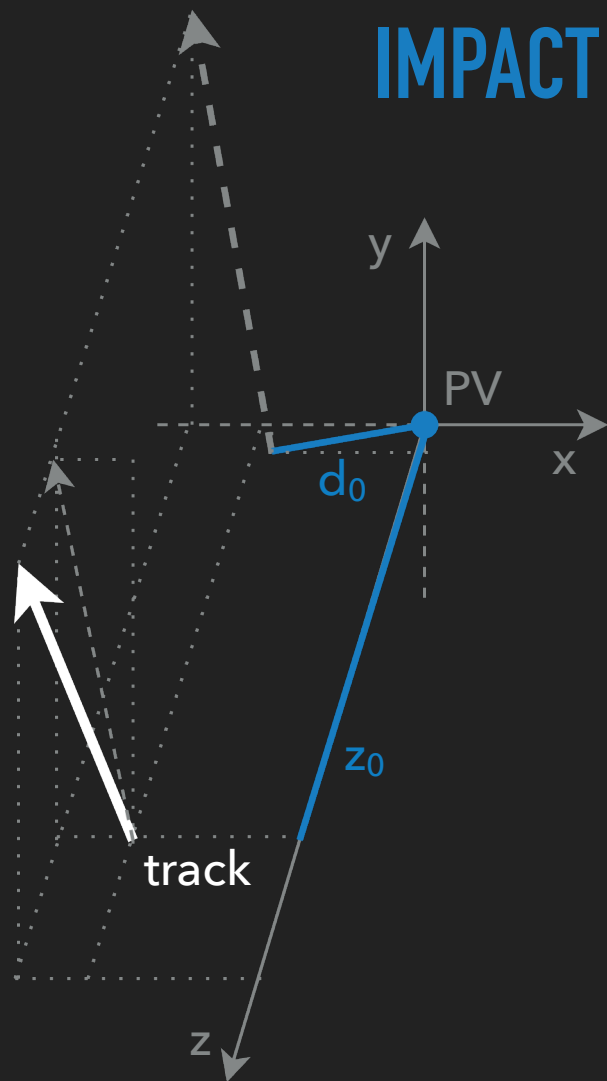


## LOW LEVEL TAGGERS

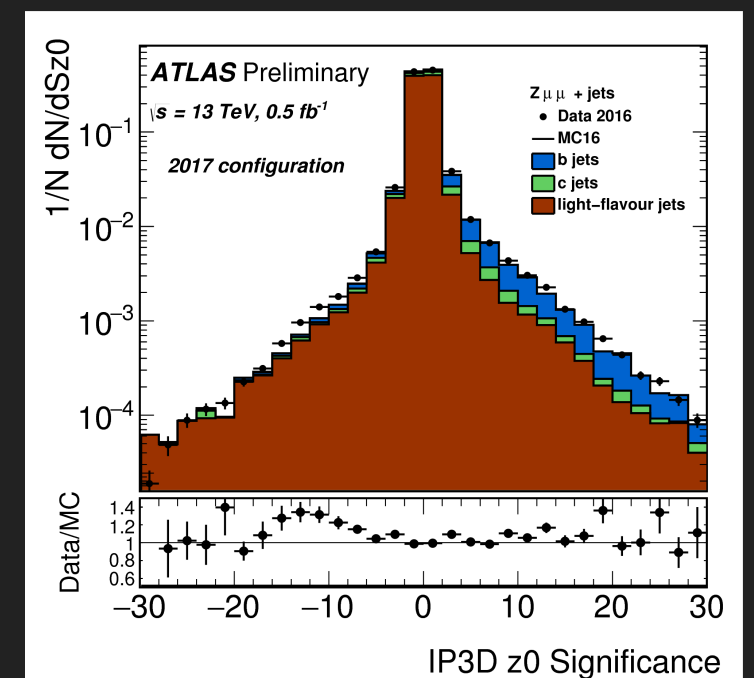
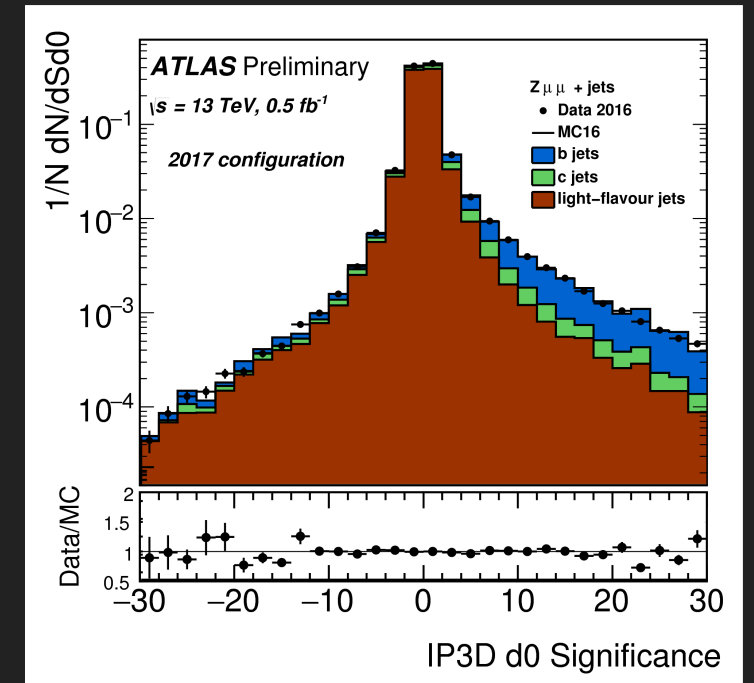
### IMPACT PARAMETER TAGGERS

IP3D

RNNIP



- ▶ measures compatibility of track with primary vertex hypothesis
- ▶ binned 2D likelihood per grade category using each track's transverse ( $S_{d_0} = d_0/\sigma_{d_0}$ ) and longitudinal ( $S_{z_0} = z_0/\sigma_{z_0}$ ) impact parameter significances
- ▶ light: significance consistent with 0

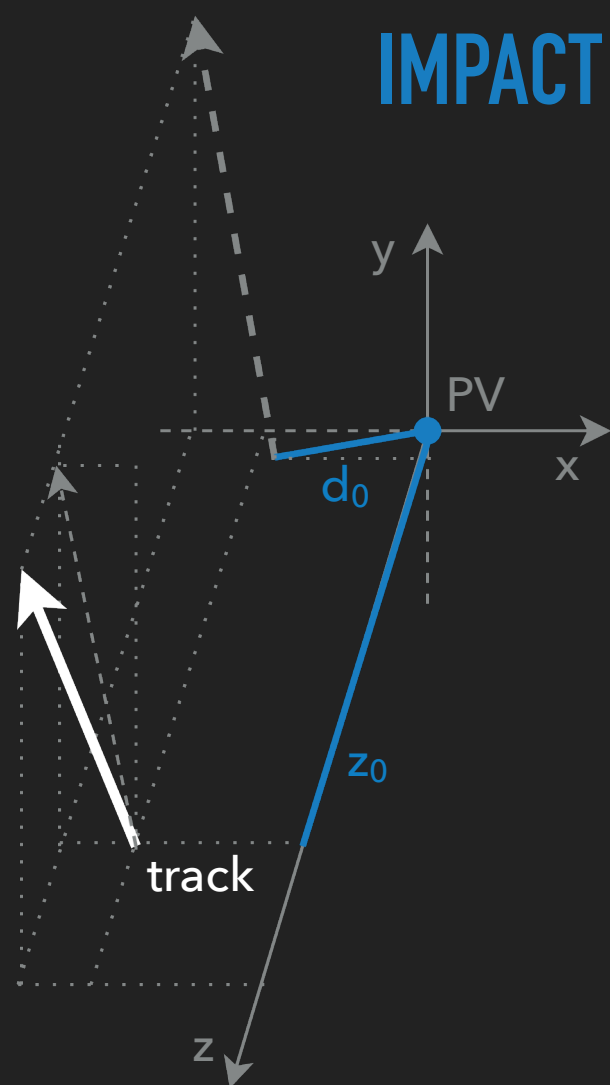


## LOW LEVEL TAGGERS

### IMPACT PARAMETER TAGGERS

IP3D

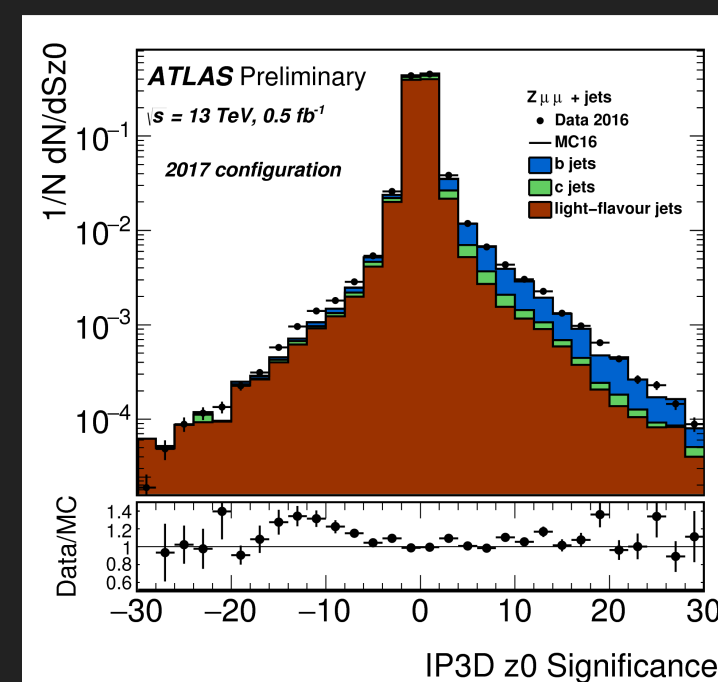
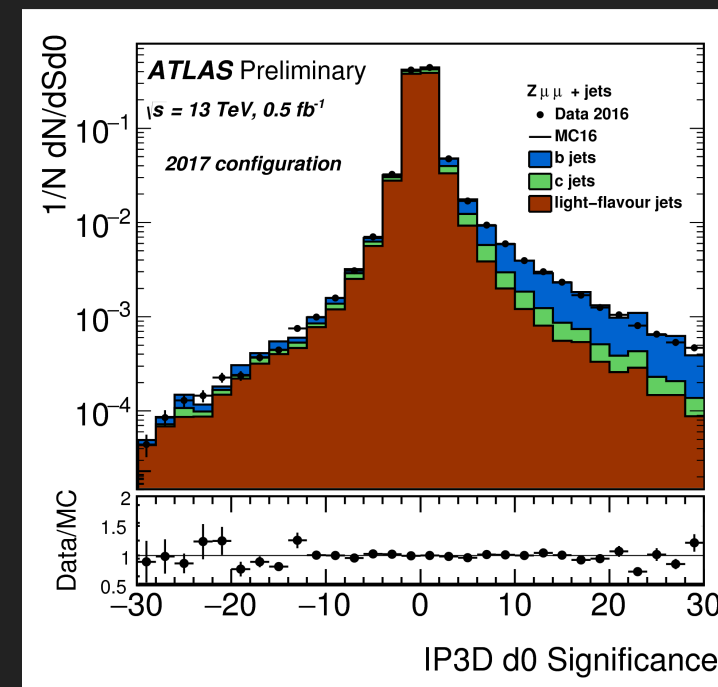
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$$\text{IP3D LLR} = \sum_{i=1}^N \log \frac{p_{b_i}}{p_{u_i}}$$

sum over tracks  
in a jet



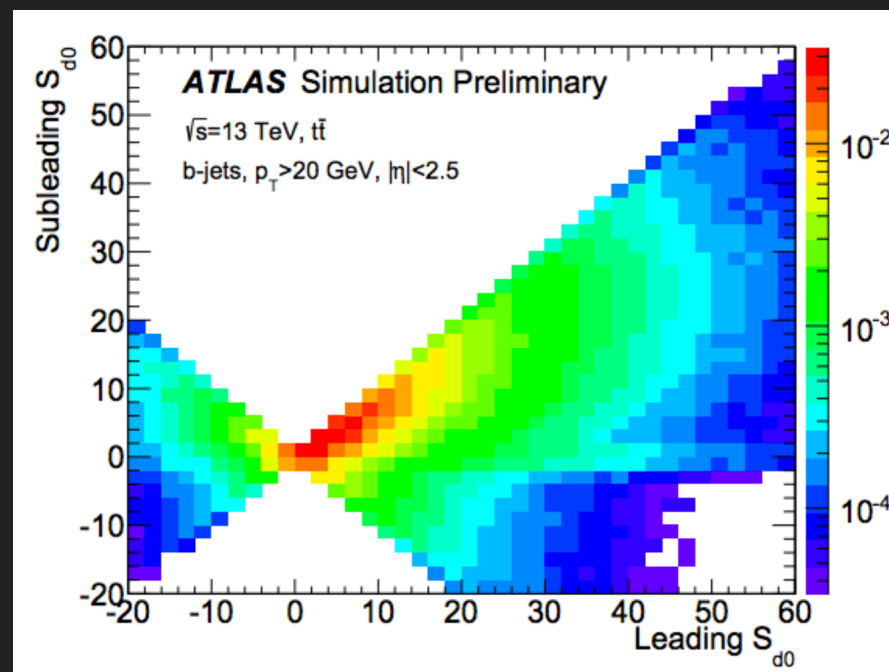
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### IMPACT PARAMETER TAGGERS

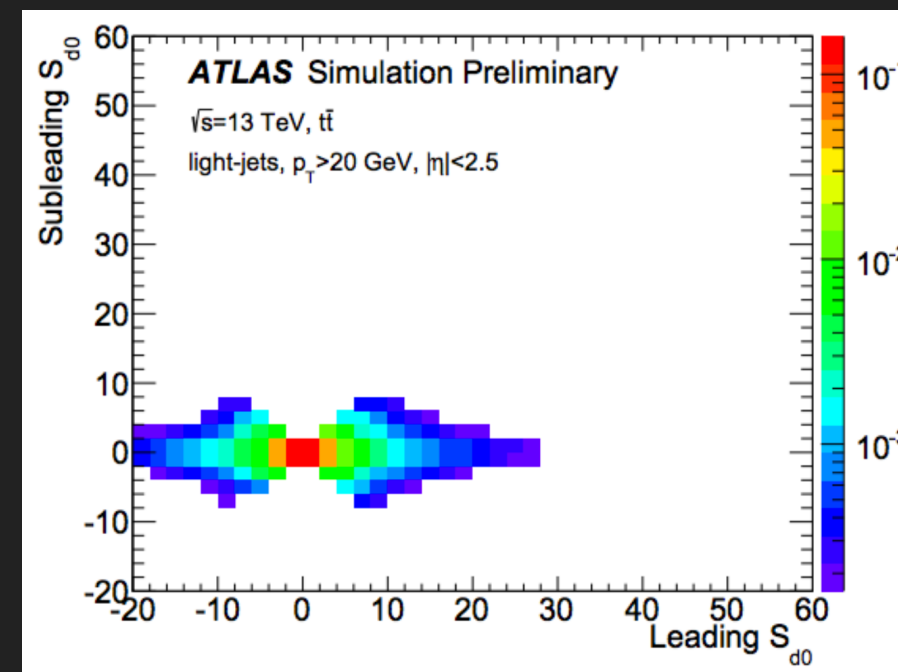
IP3D

RNNIP

- ▶ Based on Recurrent Neural Networks
- ▶ Exploits correlation among tracks, neglected by IP3D



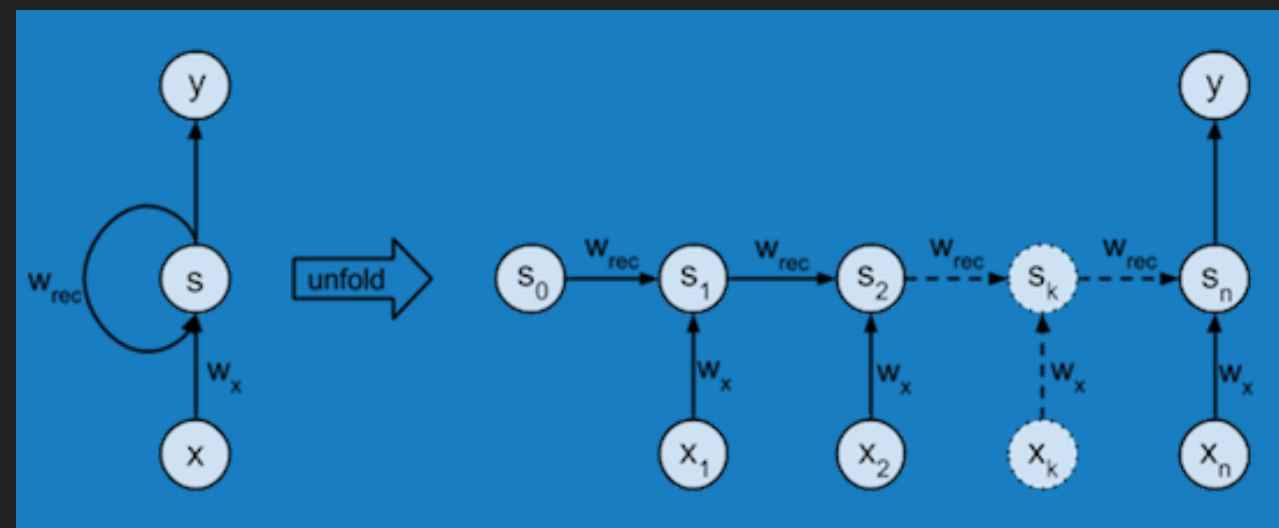
*b-jets*



*light jets*

# RECURRENT NEURAL NETWORKS

- ▶ Neural network unit to learn **sequence-based dependencies** for arbitrary-length input sequences

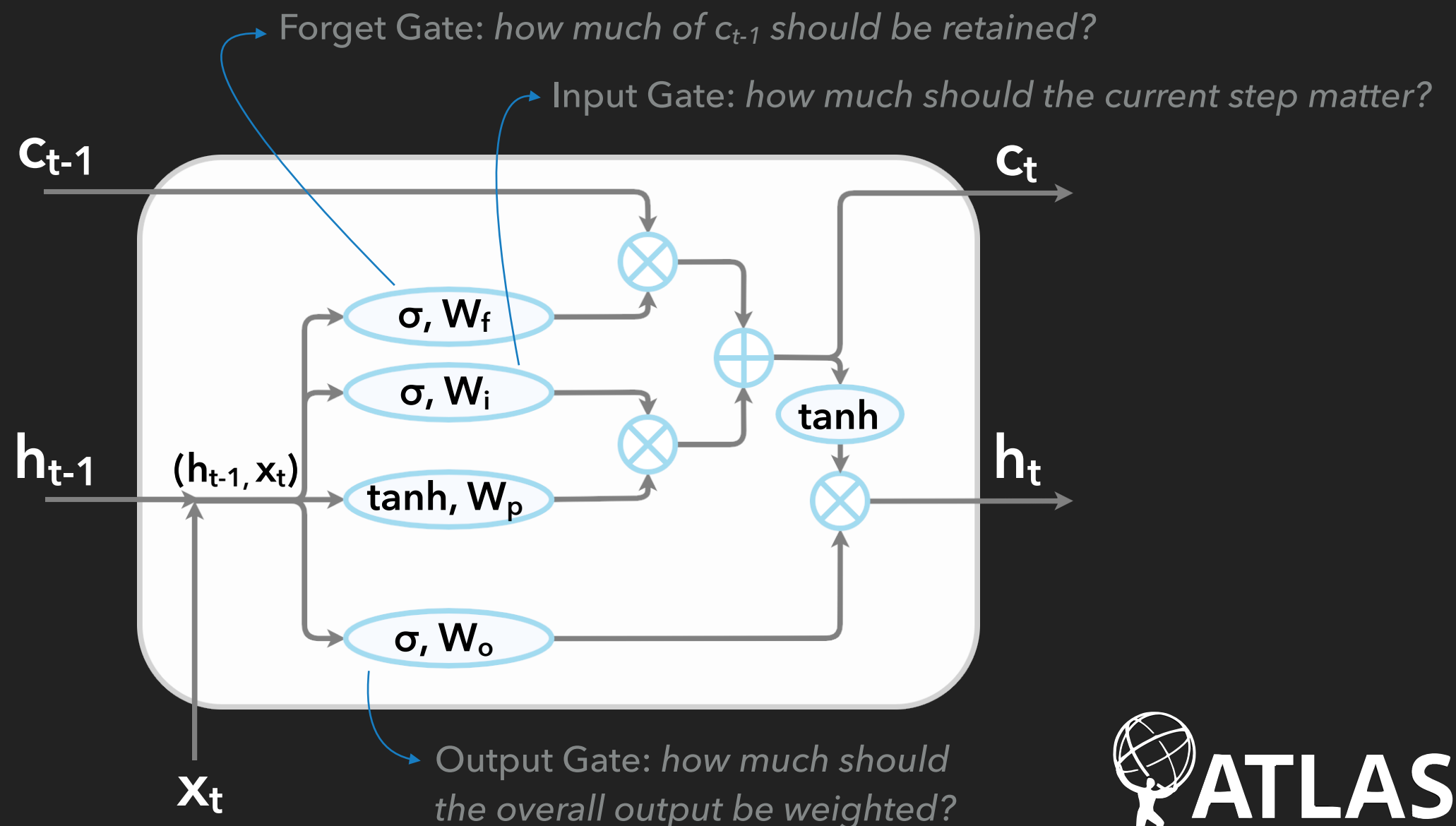


from Peter Roelants

- ▶ Cell holds internal state vector
- ▶ Identically applied to every entry in sequence
- ▶ Recurrent loop feeds back into cell

## LSTM

### ► Long-Short Term Memory units

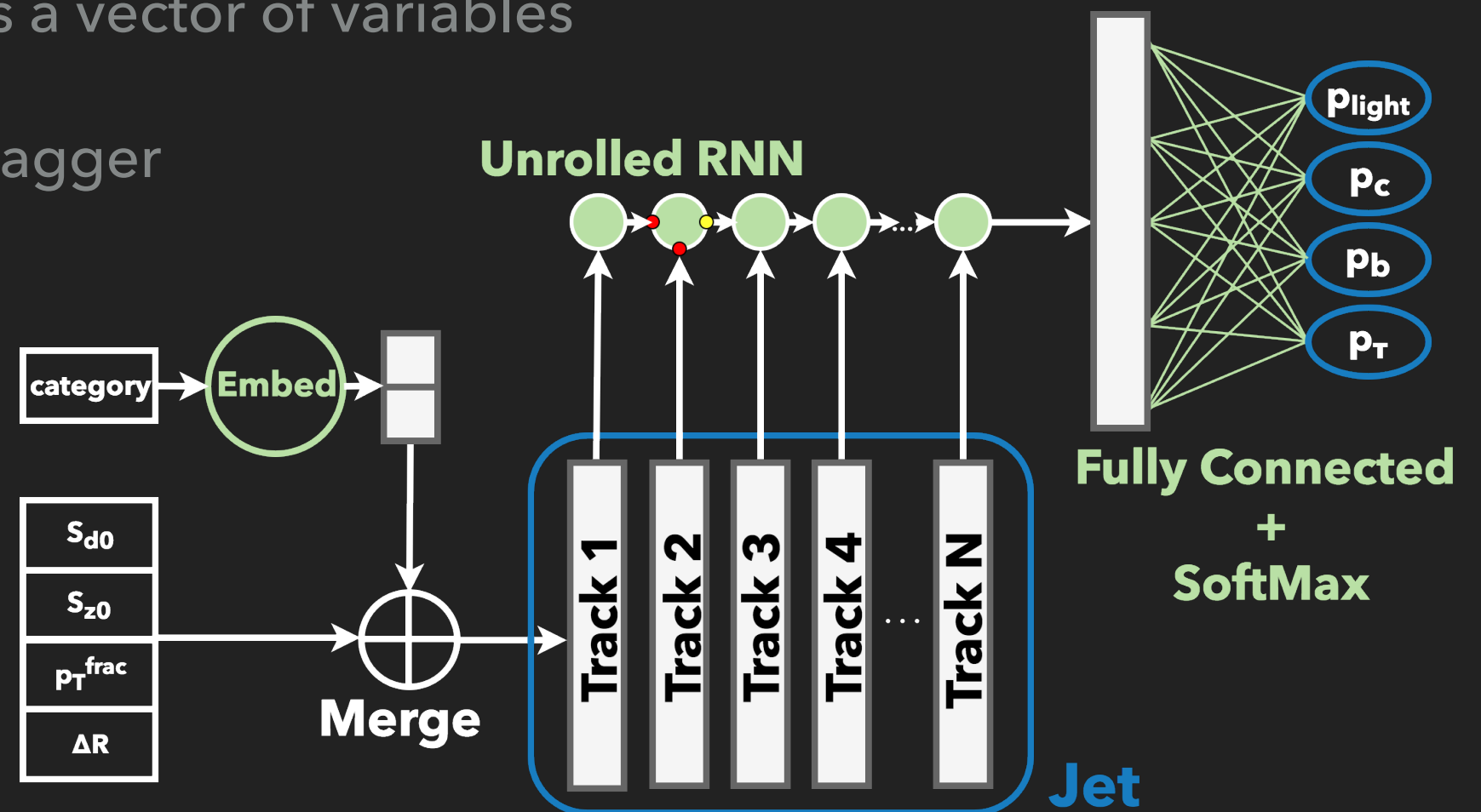


## LOW LEVEL TAGGERS

### IMPACT PARAMETER TAGGERS

#### RNNIP

- ▶ Represent jets as a sequence of tracks ordered by  $|S_{d0}|$
- ▶ Each track is a vector of variables
- ▶ Multi-class tagger





## LOW LEVEL TAGGERS

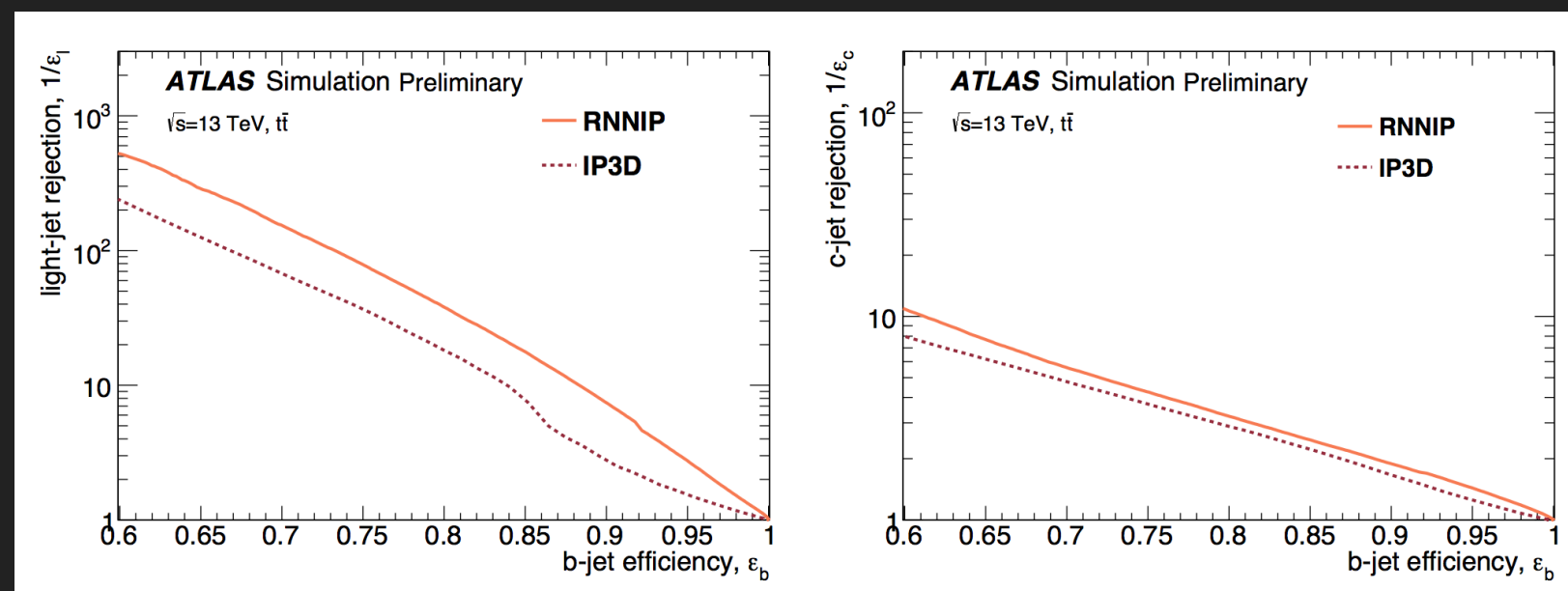
### IMPACT PARAMETER TAGGERS

RNNIP

- Combine output in discriminant:

$$D_{\text{RNN}}(b) = \ln \frac{p_b}{f_c p_c + f_\tau p_\tau + (1 - f_c - f_\tau) p_{\text{light}}}$$

- Can be tuned after training



- IP3D and RNNIP tagged jets are partly complementary  
→ increased performance when both are inputs to subsequent tagger

## LOW LEVEL TAGGERS

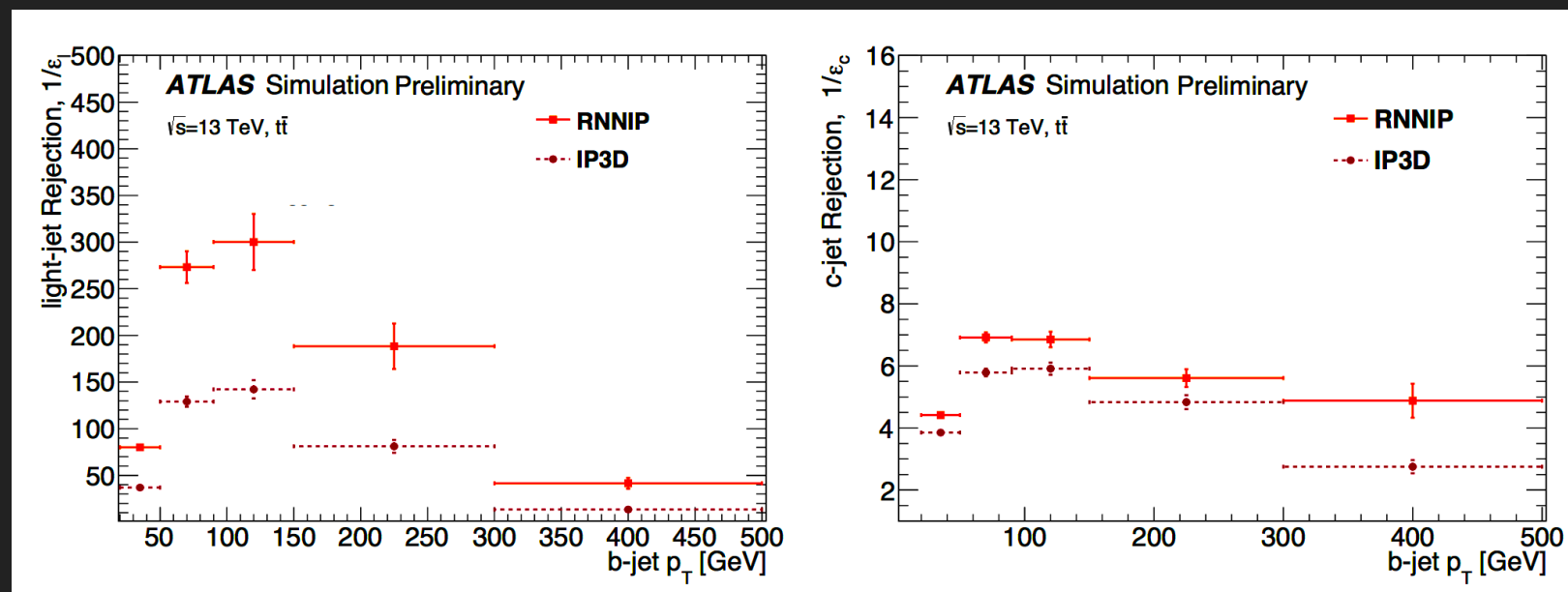
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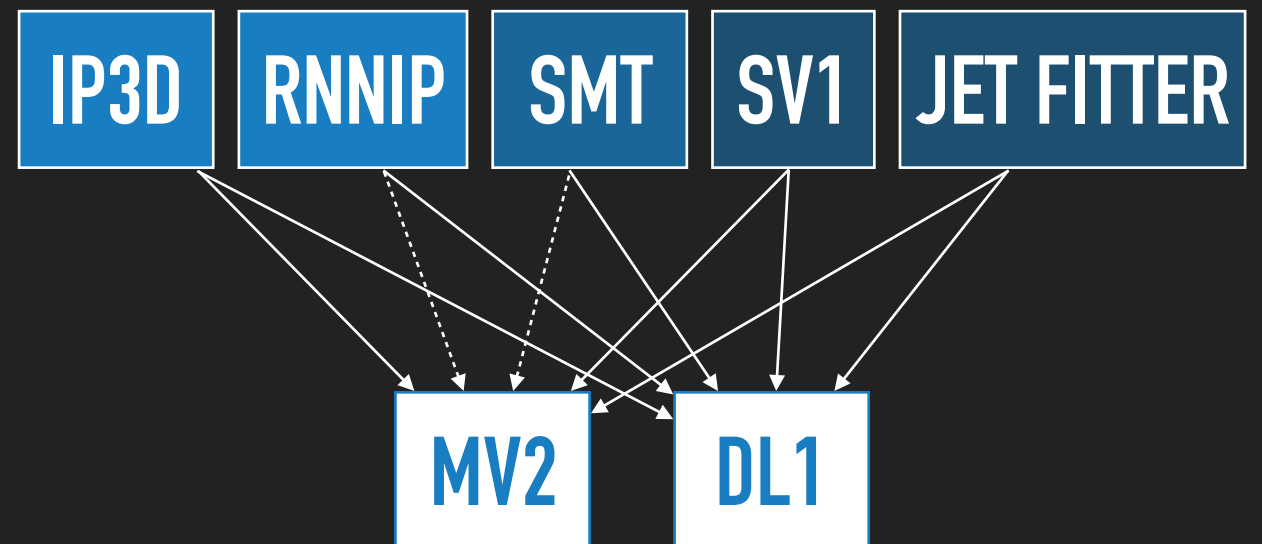


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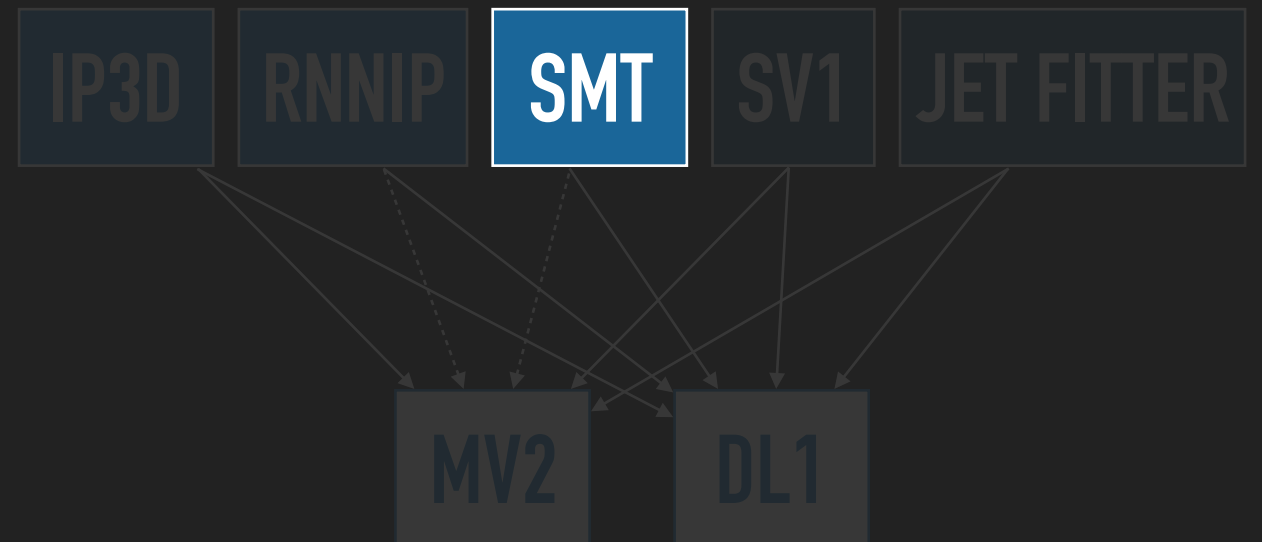
### SOFT MUON TAGGER



## LOW LEVEL TAGGERS

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### SOFT MUON TAGGER



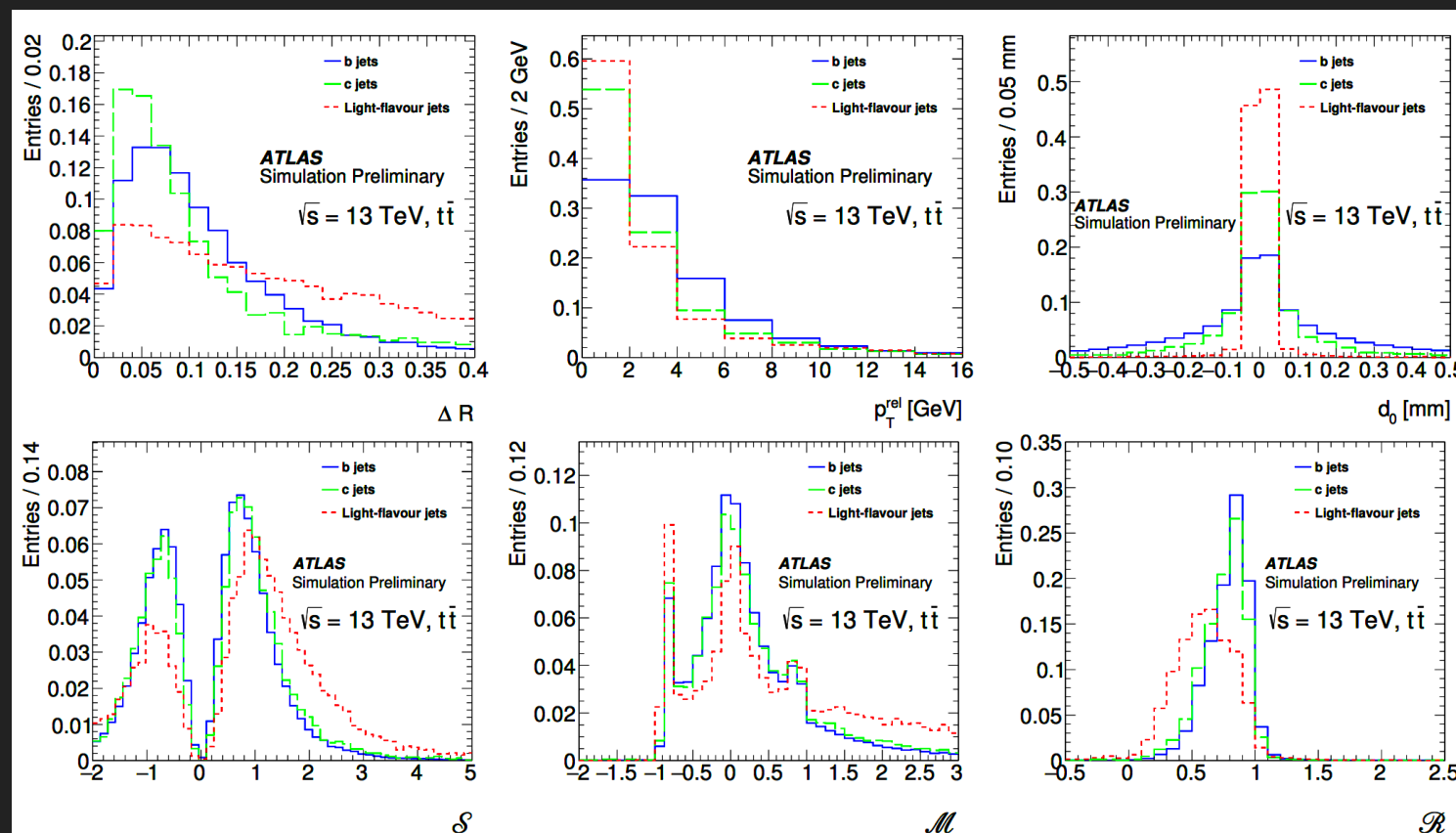
## LOW LEVEL TAGGERS

### SOFT MUON TAGGER

SMT

- Reconstructs muons from semi-leptonic decays
- Limited by the semi-leptonic branching ratio  
 $\text{BR}(b \rightarrow \mu \nu X) + \text{BR}(b \rightarrow c \rightarrow \mu \nu X) \approx 21\%$
- Complementary to other low level taggers that are based on lifetime information

Defined new variables to separate muons from  $b$ -decays, and bkg muons from decays in flight of pions and kaons:



$$S = q \sum_i \frac{\Delta\phi_{\text{scat}}^i}{\sigma_{\Delta\phi_{\text{scat}}^i}}$$

$$\mathcal{M} = \frac{p_{\text{ID}} - p_{\text{MS}}^{\text{extr}}}{\sigma_{E_{\text{loss}}}}$$

$$\mathcal{R} = \frac{(q/p)_{\text{ID}}}{(q/p)_{\text{MS}}}$$

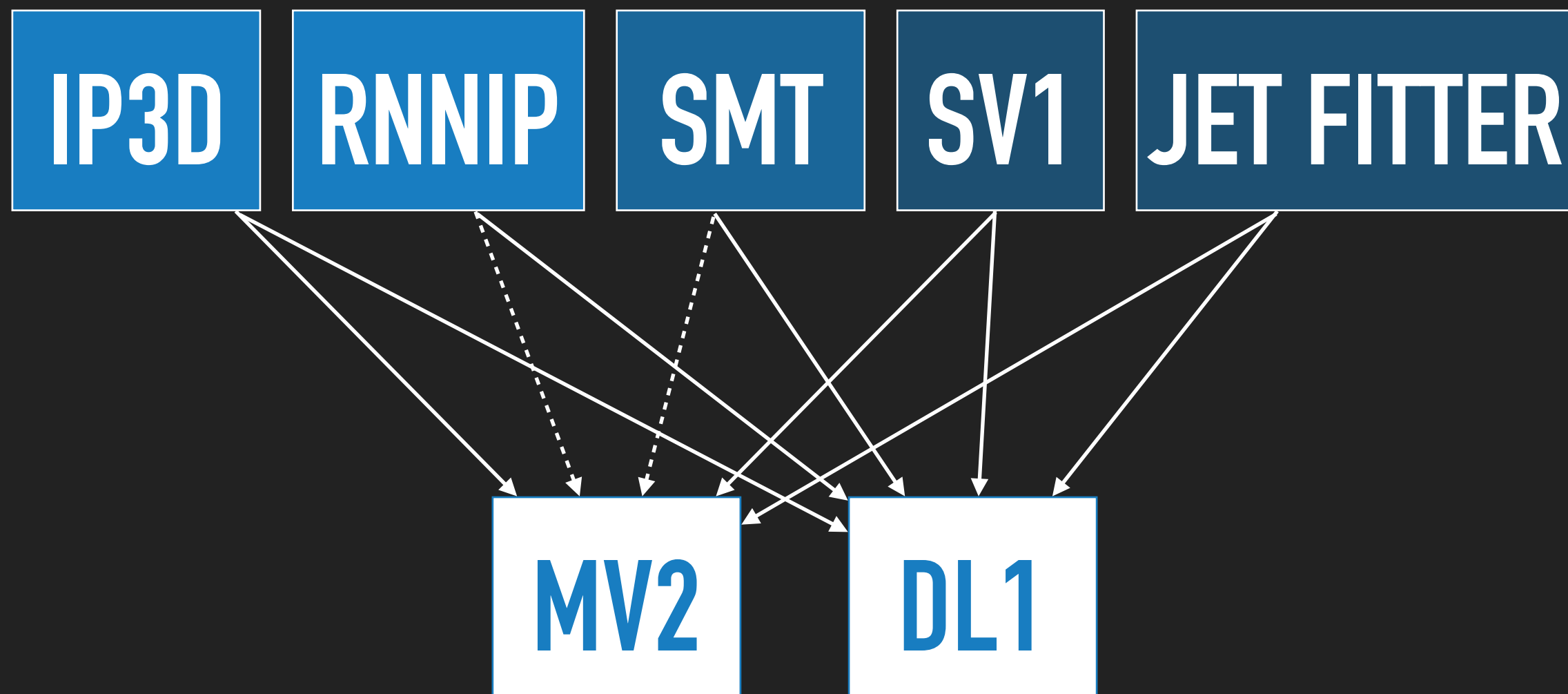
**IP3D**

**RNNIP**

**SMT**

**SV1**

**JET FITTER**



## HIGH LEVEL TAGGERS

### MV2

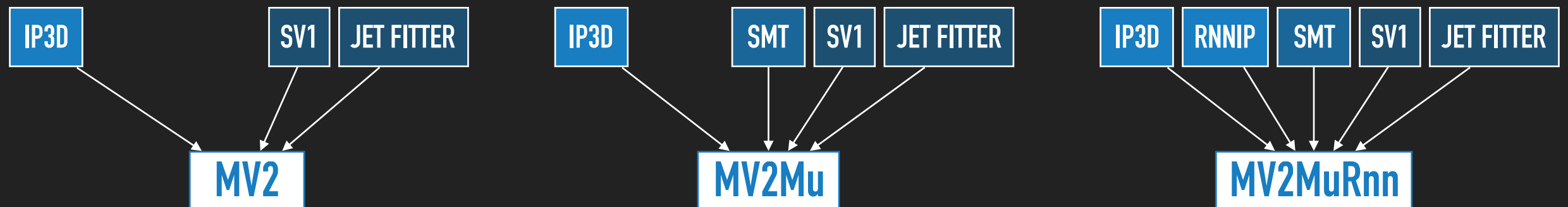
## GRADIENT BOOSTED DECISION TREE

- ▶ Trained with ROOT TMVA

- ▶  $b$  vs non- $b$

Default non- $b$  background: 7% charm and 93% light

- ▶ Various versions:



- ▶ For c-tagging:

- ▶ MV2c100 trained on 100%  $c$  background
- ▶ MV2cl100 for  $c$  vs light, no  $b$



## HIGH LEVEL TAGGERS

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**DL1**

### DEEP NEURAL NETWORK

- ▶ Trained with Keras (Theano backend)
- ▶ In ATLAS codebase using [LWTNN](#)
- ▶ Multi-class ( $b$ ,  $c$ , light)
- ▶ Architecture: fully connected + maxout + ReLU + batch norm layers

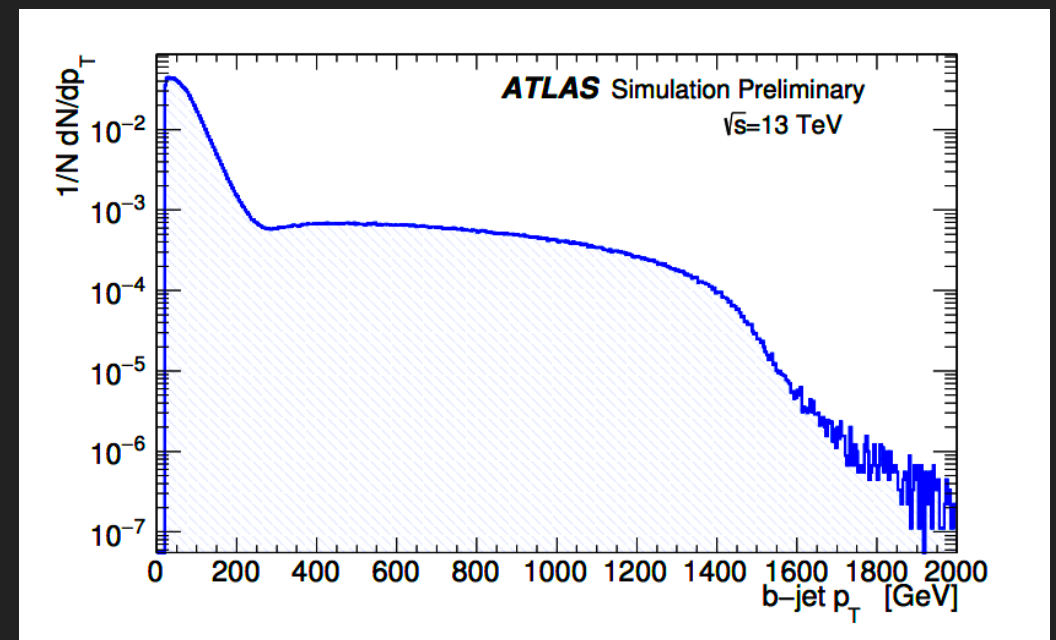
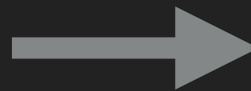
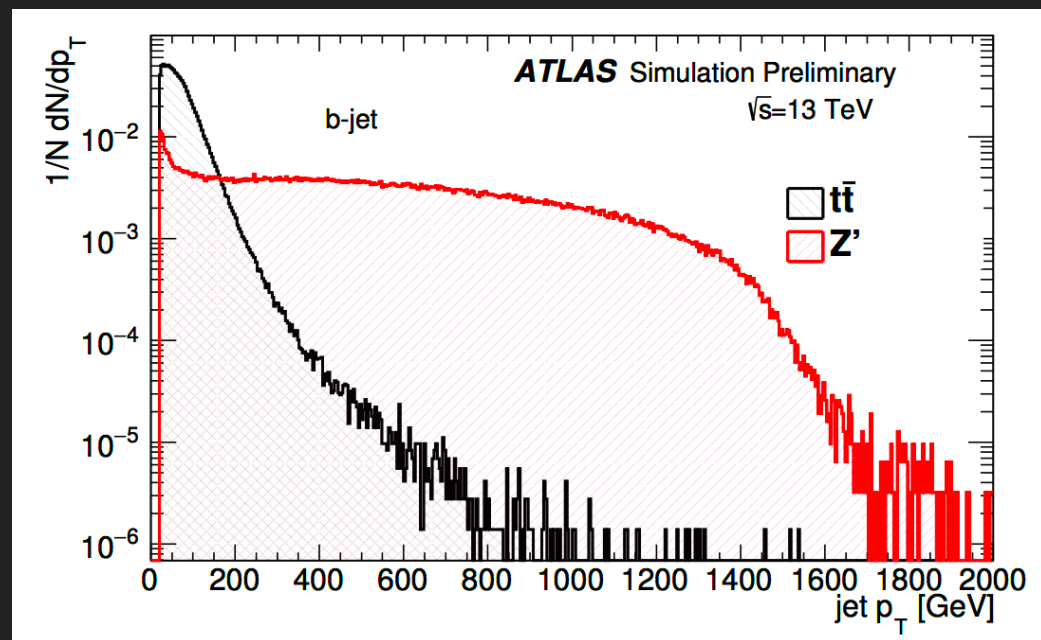
### ADVANTAGES

- |                             |   |
|-----------------------------|---|
| ▶ flexibility in future R&D | ▶ easy to extend to new input variables |
| ▶ easy to train             | ▶ can be trained adversarially          |
| ▶ min standalone code       | ▶ can be trained end-to-end with RNNIP  |
| ▶ GPU enabled               |   |
| ▶ modular                   |   |

## TRAINING IMPROVEMENTS

### HYBRID SAMPLE

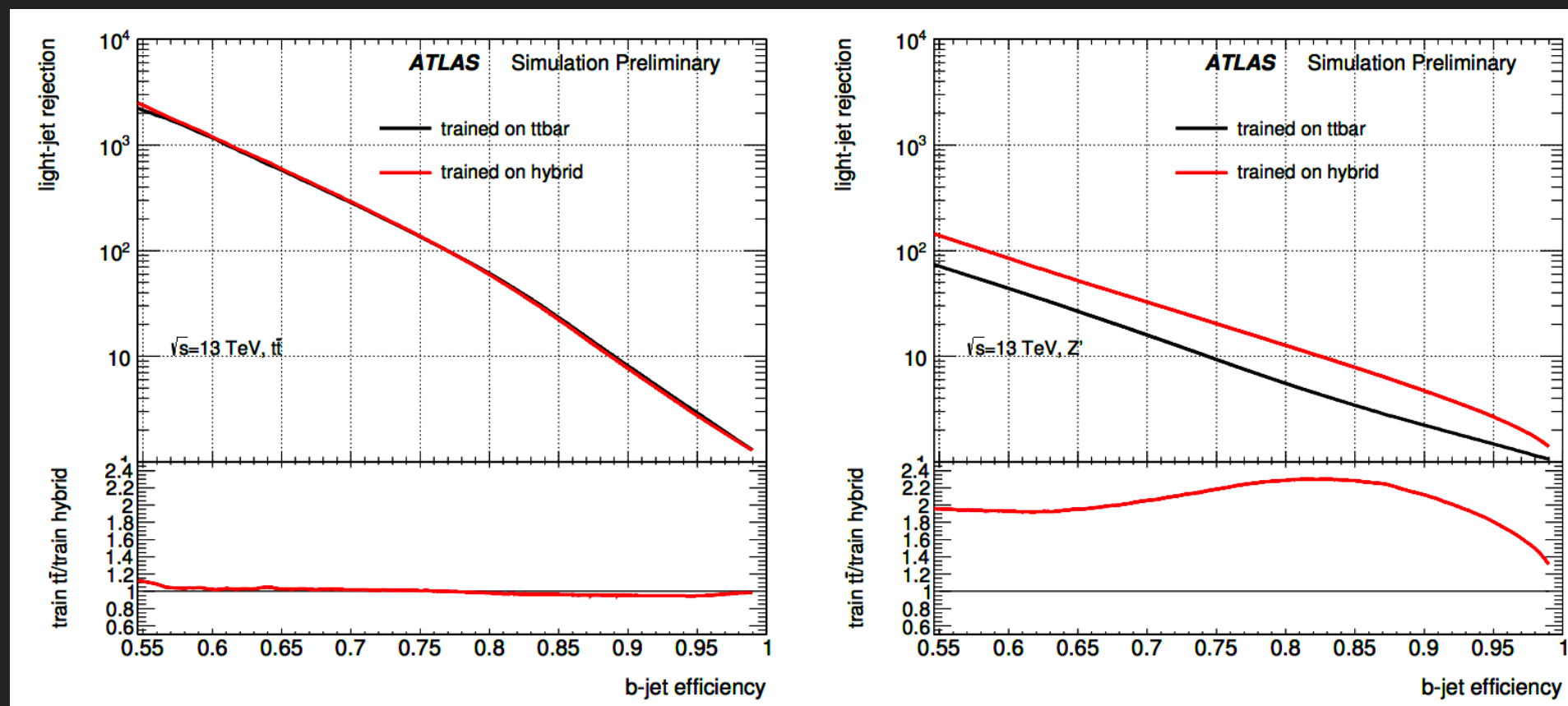
- ▶ Join  $t\bar{t}$  and  $Z'$  samples  $\sim 250$  GeV to extend kinematic range



## TRAINING IMPROVEMENTS

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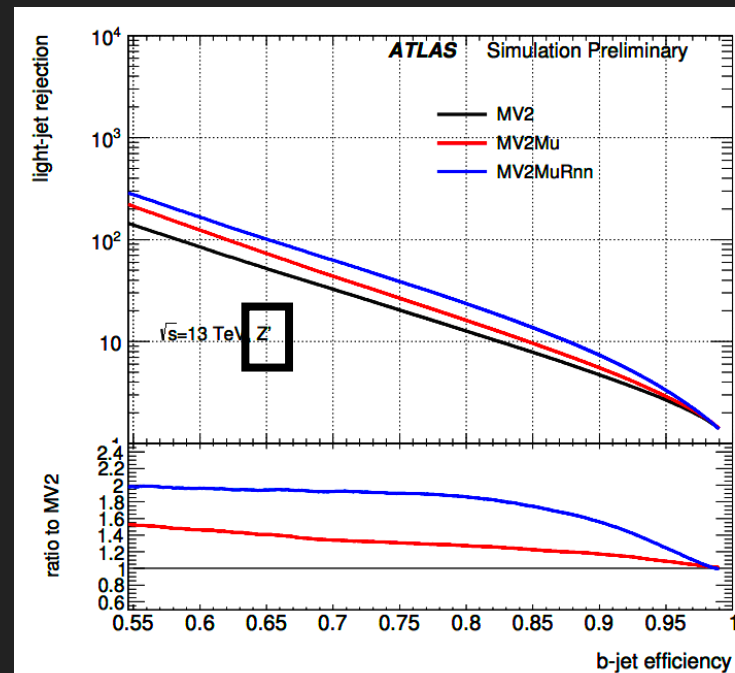
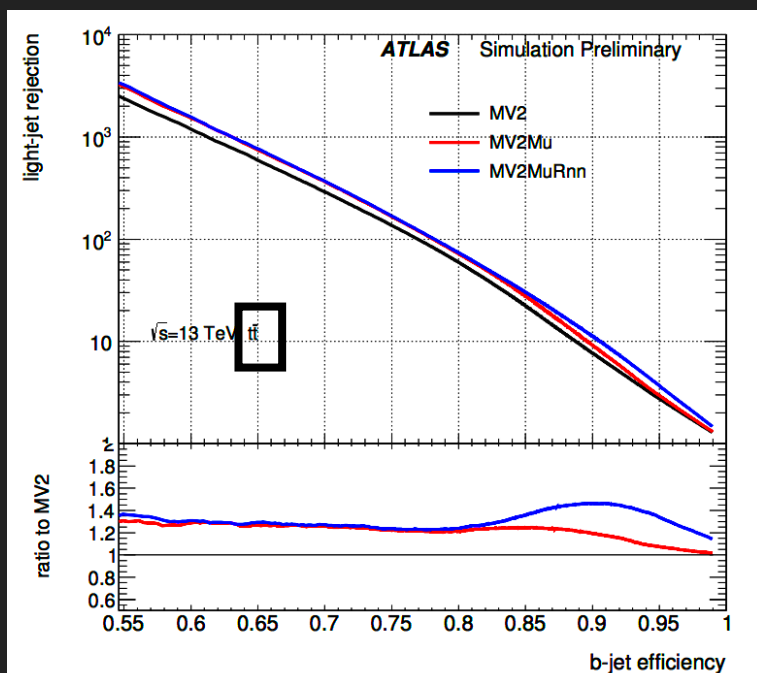
- Improves MV2 performance at high  $p_T$  with no performance degradation for  $t\bar{t}$



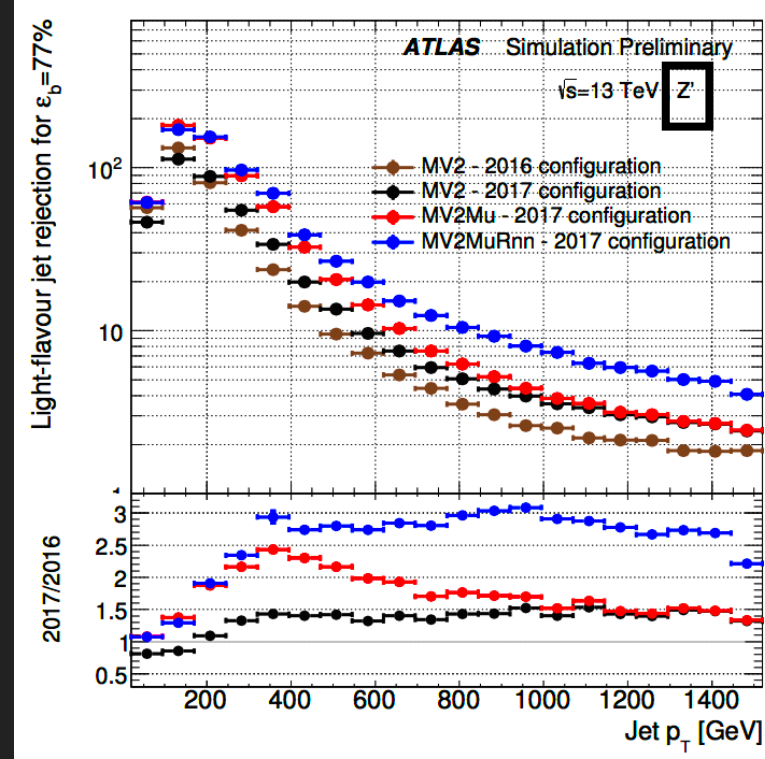
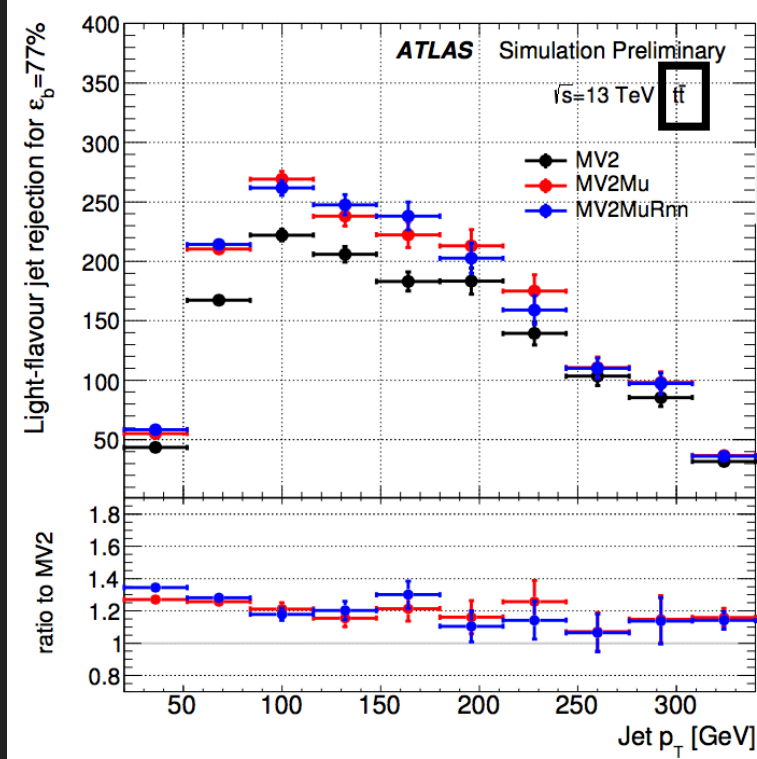
# PERFORMANCE

## MV2 VARIANTS EVALUATION – B VS LIGHT

ROC  
Curves



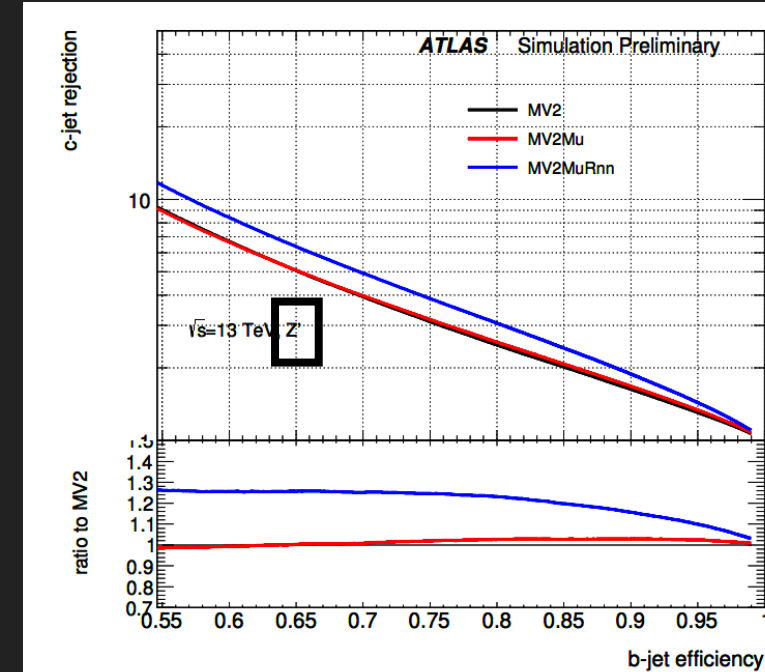
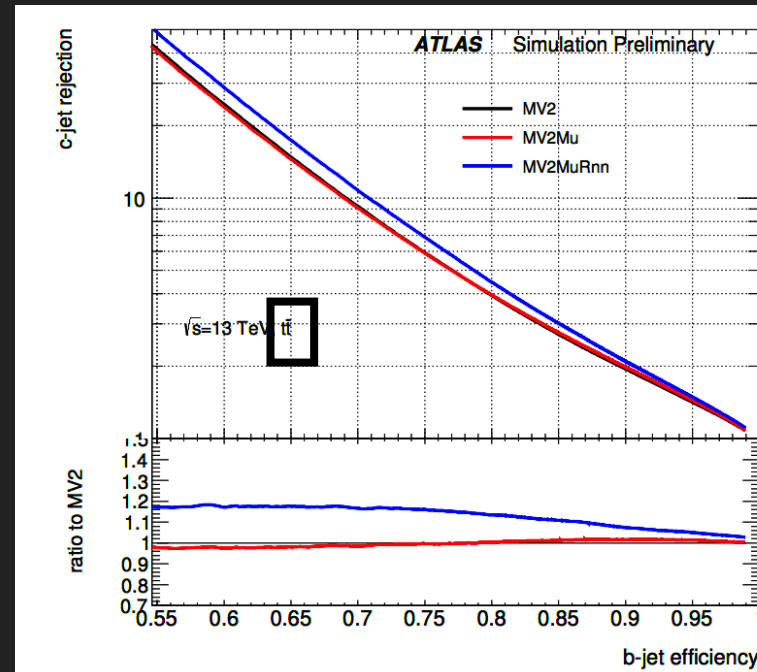
Performance  
in bins of  
 $p_T$



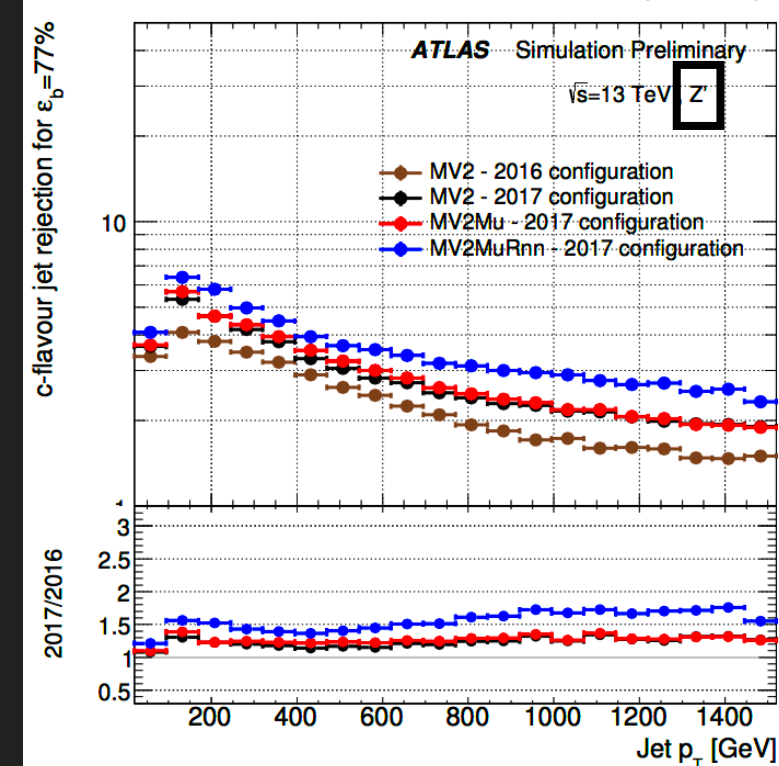
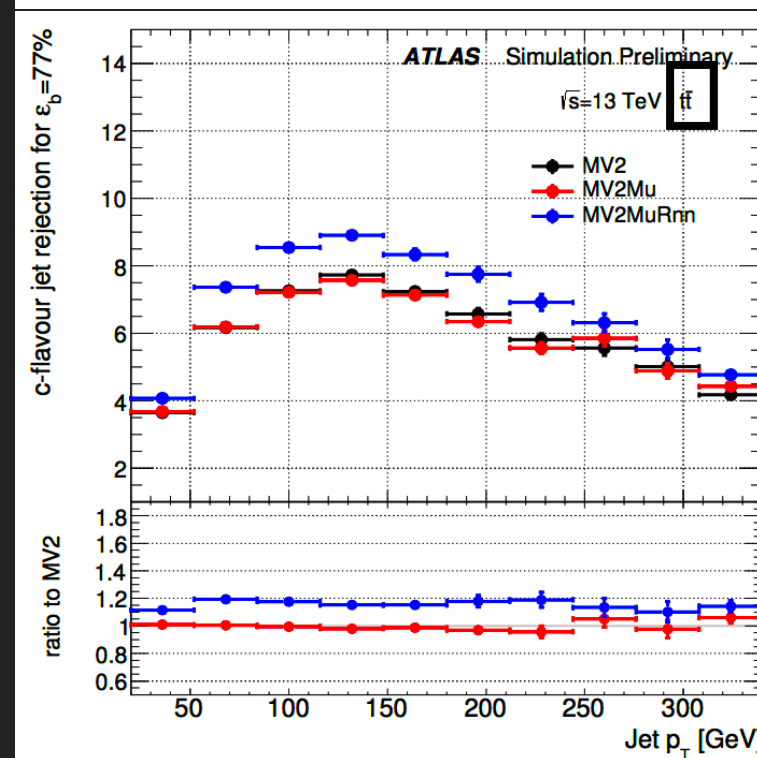
# PERFORMANCE

## MV2 VARIANTS EVALUATION – B VS C

ROC  
Curves



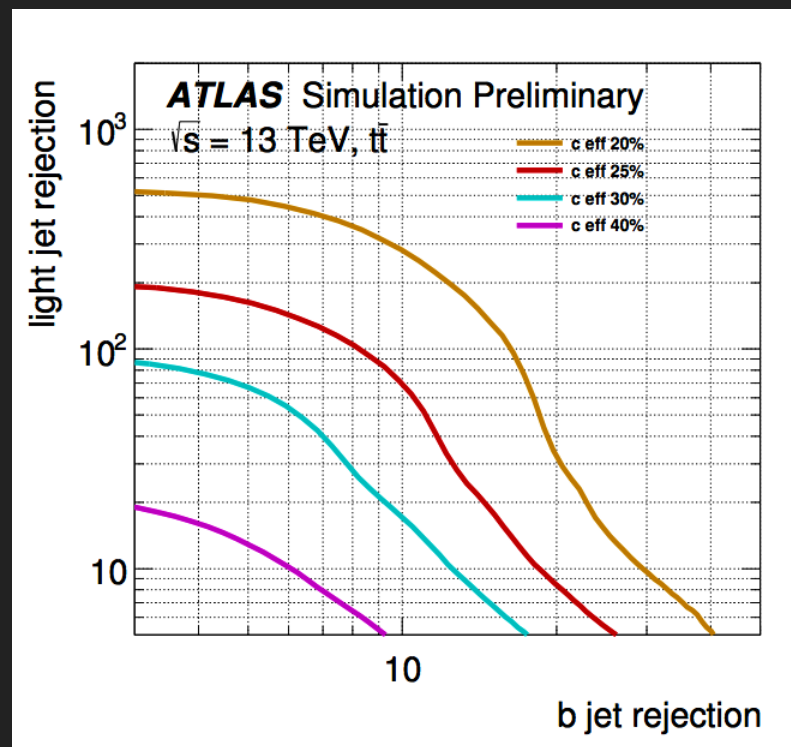
Performance  
in bins of  
 $p_T$



## PERFORMANCE

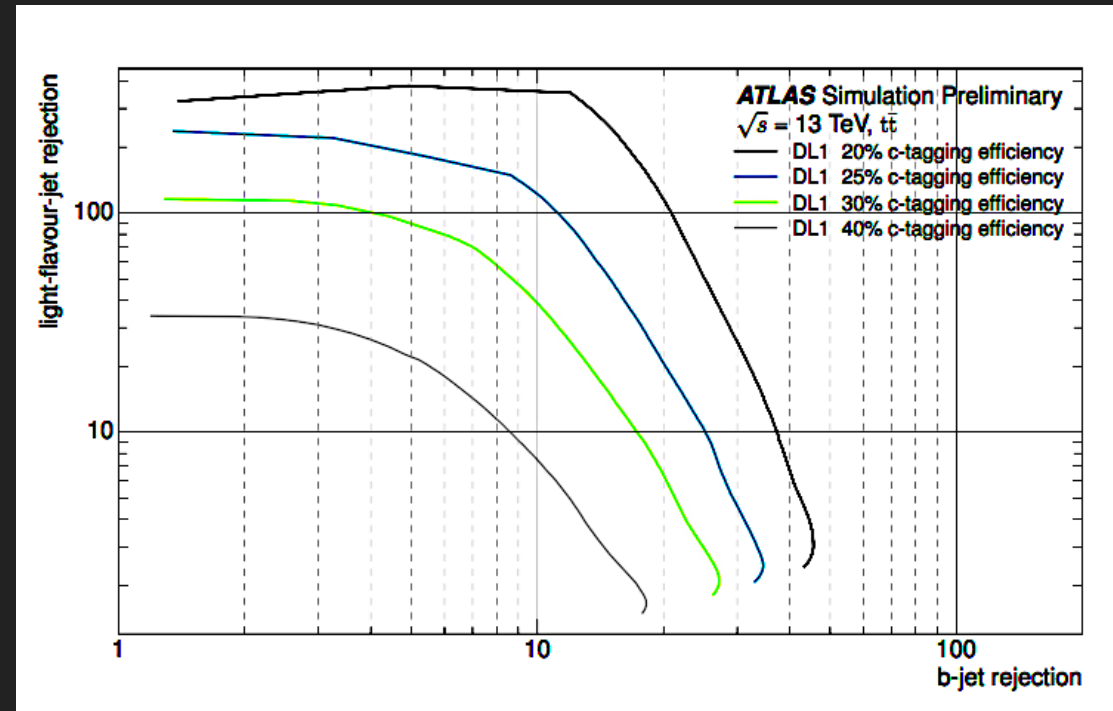
### c-EFFICIENCY ISO-CURVES

- ▶ When multi-label tagging is enabled, can look at tagging rejections trade-off at constant c-efficiency



MV2c100 & MV2c1100

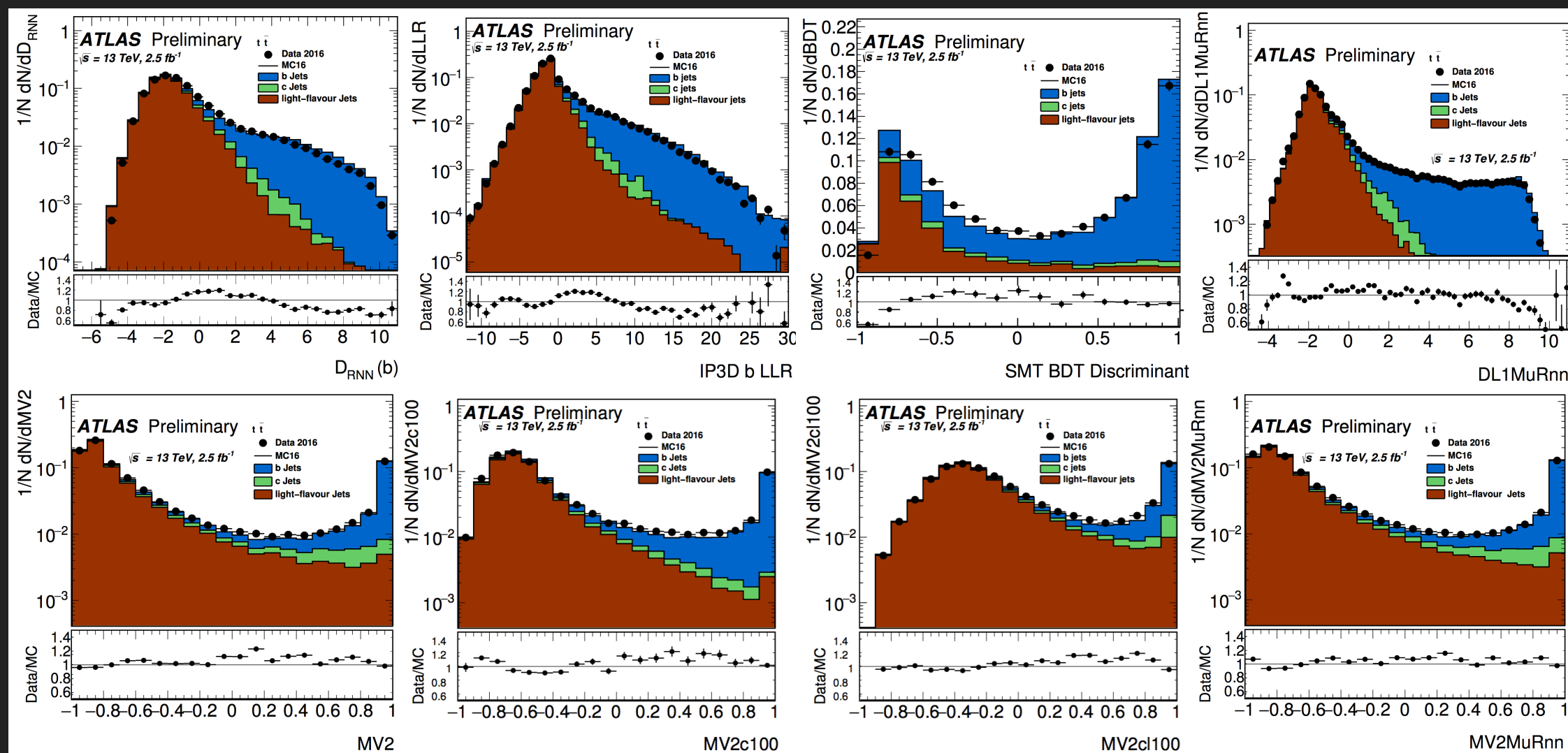
DL1





# MODELLING

## IMPROVED DATA-MC AGREEMENT



- ▶ Due to improvement in tracking simulation
- ▶ Minor local discrepancies

## SUMMARY

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### WHAT TO EXPECT

- ▶ Better data - Monte Carlo agreement
- ▶ More performant flavor tagging, due to:
  - ▶ availability of new hybrid training sample to extend  $p_T$  range
  - ▶ improvements and innovations in low level taggers, such as **RNNIP<sup>■</sup>** and SMT
  - ▶ improvements and innovations in high level taggers, such as **DL1<sup>■</sup>**

■ = deep learning taggers



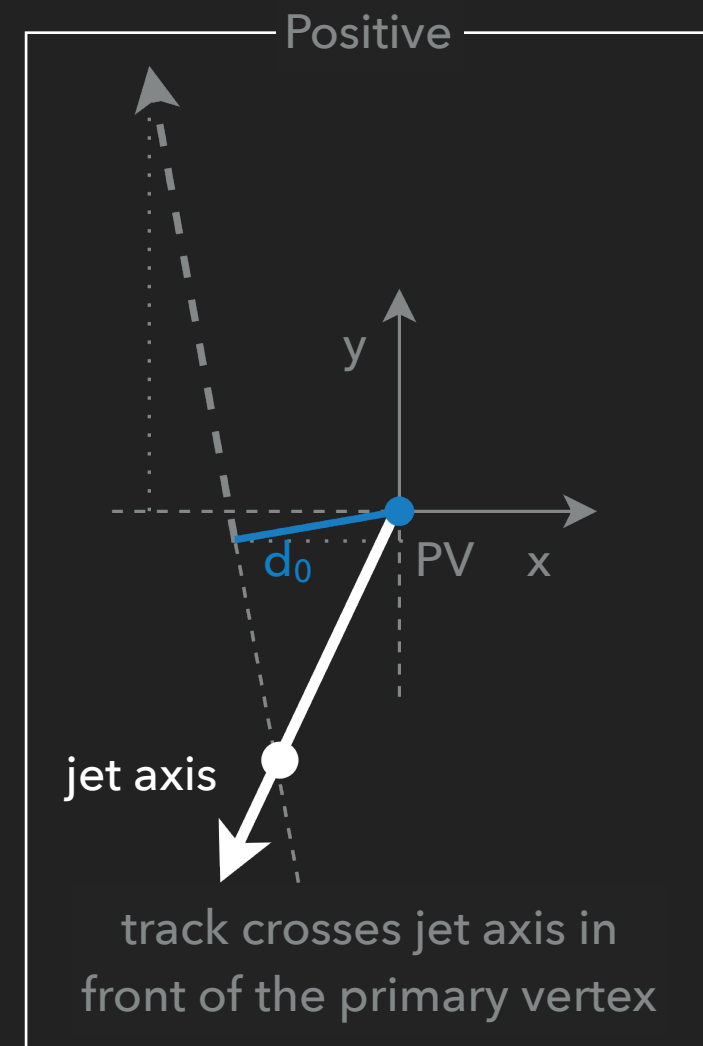
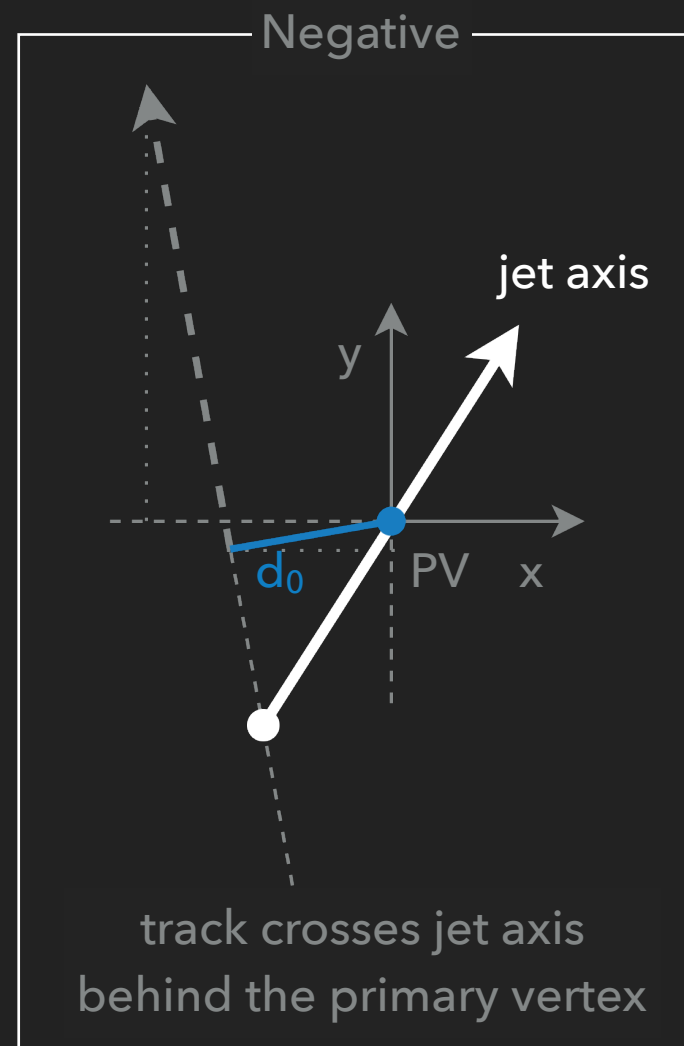
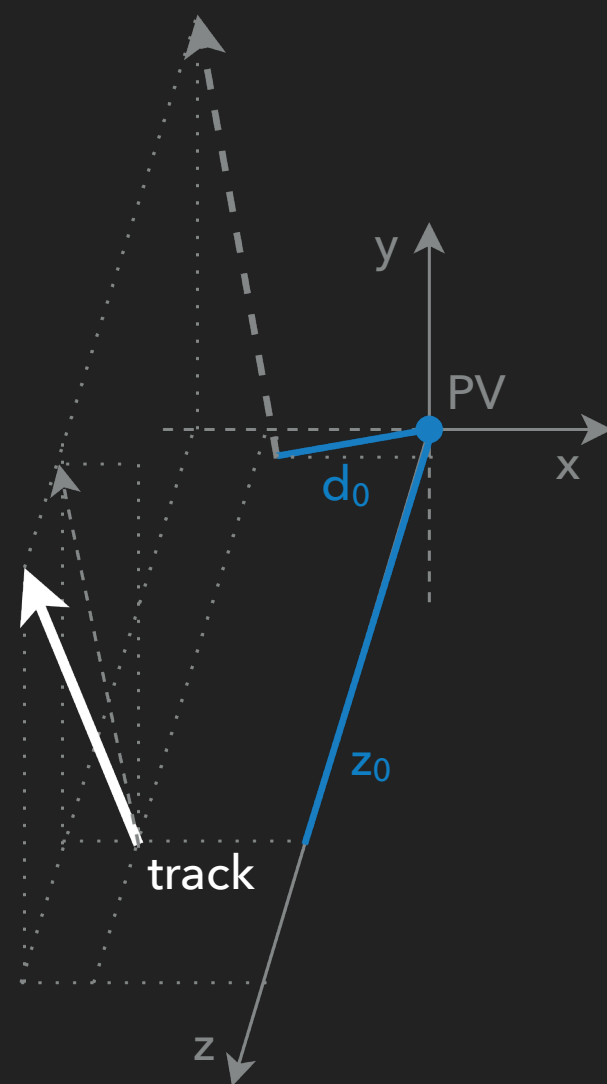


**BACKUP**

## LOW LEVEL TAGGERS

# IMPACT PARAMETER DEFINITION

► Sign:



### LSTM & GRU

- ▶ Mitigate issues with **exploding and vanishing gradients**
- ▶ Improve knowledge persistence of long-term dependencies
- ▶ Internal gating mechanisms to read, write, reset memory
- ▶ Classical RNN:

$$\begin{cases} \mathbf{s}_t = \mathbf{W}_{\text{rec}} \phi(\mathbf{s}_{t-1}) + \mathbf{W}_x \mathbf{x}_t \\ \mathbf{y}_t = \mathbf{W}_y \mathbf{s}_t \end{cases}$$

- ▶ Train by optimizing objective function:  $\mathcal{L}$

## EXPLODING & VANISHING GRADIENTS

$$\frac{\partial \mathcal{L}_t}{\partial \mathbf{W}_{\text{rec}}} = \sum_{k=1}^t \frac{\partial \mathcal{L}_t}{\partial \mathbf{y}_t} \frac{\partial \mathbf{y}_t}{\partial \mathbf{s}_t} \boxed{\frac{\partial \mathbf{s}_t}{\partial \mathbf{s}_k}} \frac{\partial \mathbf{s}_k}{\partial \mathbf{W}_{\text{rec}}}$$

## EXPLODING & VANISHING GRADIENTS

$$\frac{\partial \mathcal{L}_t}{\partial \mathbf{W}_{\text{rec}}} = \sum_{k=1}^t \frac{\partial \mathcal{L}_t}{\partial \mathbf{y}_t} \frac{\partial \mathbf{y}_t}{\partial \mathbf{s}_t} \boxed{\frac{\partial \mathbf{s}_t}{\partial \mathbf{s}_k}} \frac{\partial \mathbf{s}_k}{\partial \mathbf{W}_{\text{rec}}}$$

product of Jacobians

$$\prod_{i=k+1}^t \frac{\partial \mathbf{s}_i}{\partial \mathbf{s}_{i-1}} = \prod_{i=k+1}^t \mathbf{W}_{\text{rec}}^T \text{diag}[\phi'(\mathbf{s}_{i-1})]$$

## EXPLODING & VANISHING GRADIENTS

$$\frac{\partial \mathcal{L}_t}{\partial \mathbf{W}_{\text{rec}}} = \sum_{k=1}^t \frac{\partial \mathcal{L}_t}{\partial \mathbf{y}_t} \frac{\partial \mathbf{y}_t}{\partial \mathbf{s}_t} \boxed{\frac{\partial \mathbf{s}_t}{\partial \mathbf{s}_k}} \frac{\partial \mathbf{s}_k}{\partial \mathbf{W}_{\text{rec}}}$$

product of Jacobians

$$\prod_{i=k+1}^t \boxed{\frac{\partial \mathbf{s}_i}{\partial \mathbf{s}_{i-1}}} = \prod_{i=k+1}^t \mathbf{W}_{\text{rec}}^T \text{diag}[\phi'(\mathbf{s}_{i-1})]$$

norm is bounded above

$$\left\| \frac{\partial \mathbf{s}_i}{\partial \mathbf{s}_{i-1}} \right\| \leq \|\mathbf{W}_{\text{rec}}^T\| \|\text{diag}[\phi'(\mathbf{s}_{i-1})]\| \leq \gamma_w \gamma_\phi$$

## EXPLODING & VANISHING GRADIENTS

$$\frac{\partial \mathcal{L}_t}{\partial \mathbf{W}_{\text{rec}}} = \sum_{k=1}^t \frac{\partial \mathcal{L}_t}{\partial \mathbf{y}_t} \frac{\partial \mathbf{y}_t}{\partial \mathbf{s}_t} \boxed{\frac{\partial \mathbf{s}_t}{\partial \mathbf{s}_k}} \frac{\partial \mathbf{s}_k}{\partial \mathbf{W}_{\text{rec}}}$$

product of Jacobians

$$\prod_{i=k+1}^t \boxed{\frac{\partial \mathbf{s}_i}{\partial \mathbf{s}_{i-1}}} = \prod_{i=k+1}^t \mathbf{W}_{\text{rec}}^T \text{diag}[\phi'(\mathbf{s}_{i-1})]$$

norm is bounded above

$$\left\| \frac{\partial \mathbf{s}_i}{\partial \mathbf{s}_{i-1}} \right\| \leq \|\mathbf{W}_{\text{rec}}^T\| \|\text{diag}[\phi'(\mathbf{s}_{i-1})]\| \leq \gamma_w \gamma_\phi$$

$$\left\| \frac{\partial \mathbf{s}_t}{\partial \mathbf{s}_k} \right\| \leq (\gamma_w \gamma_\phi)^{t-k}$$

for long sequences:

- goes to 0 if  $\arg < 1$
- diverges for  $\arg > 1$