# Using Tau Polarization to Discriminate different SUSY models and Determine SUSY parameters

D.P.Roy, R.M.Godbole, MG, Phys Lett.2005.

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Monoranjan Guchait TIFR, Mumbai • Polarization of tau plays a very crucial role in collider searches.

D.P.Roy et.al,1995

• Use of it in the case of Higgs searches is helpful; In case of SUSY searches it also acts as a very good tool.

• In the context of ILC, its importance is also under investigation

M.M.Nojiri et.al, 1996, E. Boos et. al. 2003

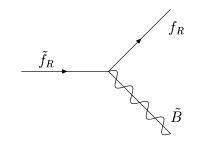
• Our plan

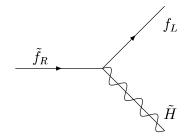
 $\Rightarrow$  Discriminate SUSY models.

 $\Rightarrow$  Determination of SUSY parameters.

# Tau particles are polarized: $\tilde{\tau}_1 \to \tau + \chi_1^0$

$$f = t/\tau$$





$$P_{\tau} = \frac{\Gamma(\tau_R) - \Gamma(\tau_L)}{\Gamma(\tau_R) + \Gamma(\tau_L)}$$
$$= \frac{(a_{11}^R)^2 - (a_{11}^L)^2}{(a_{11}^R)^2 + (a_{11}^L)^2}$$

$$a_{11}^{R} = -\frac{2g}{\sqrt{2}} N_{11} \tan \theta_w \sin \theta_{\tilde{\tau}} - \frac{gm_{\tau}}{\sqrt{2}m_W \cos \beta} N_{13} \cos \theta_{\tilde{\tau}}$$

$$a_{11}^{L} = \frac{g}{\sqrt{2}} [N_{12} + N_{11} \tan \theta_W \cos \theta_{\tilde{\tau}}] - \frac{g m_{\tau}}{\sqrt{2} m_W \cos \beta} \sin \theta_{\tilde{\tau}} N_{13}$$

$$\tilde{\chi}_1^0 = N_{11}\tilde{B} + N_{12}\tilde{W}_3 + N_{13}\tilde{H}_1^0 + N_{14}\tilde{H}_2^0$$

$$\Rightarrow P_{\tau} = P_{\tau}(M_1, \mu, \tan \beta, \theta_{\tilde{\tau}})$$
 (CP conserving SUSY)

### $au ext{-Decays}$

$$\tau^{+} \rightarrow \pi^{+}\nu_{\tau}(12.5\%)$$
 $\rightarrow \rho^{+}\nu_{\tau} \rightarrow \pi^{+}\pi^{0}(24\%)$ 
 $\rightarrow a_{1}\nu_{\tau} \rightarrow \pi^{+}\pi^{0}\pi^{0}\nu_{\tau}(7.5\%)$ 
"1- prong" channel

Angular distributions:

$$\frac{1}{\Gamma_{\pi}} \frac{d\Gamma_{\pi}}{d(\cos \theta)} = \frac{1}{2} (1 + P_{\tau} \cos \theta)$$

$$\frac{1}{\Gamma_{\pi}} \frac{d\Gamma_{v,L}}{d(\cos \theta)} = \frac{m_{\tau}^{2}/2}{m_{\tau}^{2} + 2m_{v}^{2}} (1 + P_{\tau} \cos \theta)$$

$$\frac{1}{\Gamma_{\pi}} \frac{d\Gamma_{v,T}}{d(\cos \theta)} = \frac{m_{v}^{2}}{m_{\tau}^{2} + 2m_{v}^{2}} (1 - P_{\tau} \cos \theta)$$

$$p_{\tau-jet} = xp_{\tau}$$

$$\cos \theta = \frac{2x - 1 - m_{\pi,v}^2 / m_{\tau}^2}{1 - m_{\pi,v}^2} \text{ (E >> } m_{\tau})$$

$$P_{\tau} = +1; \Rightarrow \tau_{jet} \sim \pi, \rho_L, a_{1L}$$

$$P_{\tau} = -1; \Rightarrow \tau_{jet} \sim \rho_T, a_{1T}$$

## Energy sharing among decay products, $\pi^+$ and $\pi^0$ :

$$ho^0 o \pi^+\pi^-$$

$$\frac{1}{\Gamma_{\pi\pi}} \frac{d\Gamma(\rho_L \to \pi^+ \pi^0)}{d(\cos \theta')} \simeq \frac{3}{2} (2x' - 1)^2$$

$$\frac{1}{\Gamma_{\pi}} \frac{d\Gamma(\rho_T \to \pi^+ \pi^0)}{d(\cos \theta')} \simeq 3x' (1 - x')^2$$

$$x' = \frac{1 + \sqrt{1 - 4m_{\pi}^2/m_{\rho}^2} \cos \theta'}{2} = \frac{p_{\pi}}{p_{\rho}}$$

$$\rho_L \to \pi^+ \pi^0; \text{ asym sharing; } x' \to 0/1$$

$$\rho_T \to \pi^+ \pi^0; \text{ equal sharing; } x' \to 0.5$$

$$\Rightarrow R = \frac{E_{\pi}}{E_{\tau - jet}}$$

Similarly features also hold for  $a_1 \to \pi^+ \pi^0 \pi^0$ 

#### Stau pair production and decays

For a wide class of SUSY models " $\tilde{\tau}_1$  NLSP". (low  $m_0$ , high  $\tan \beta$  scenario)

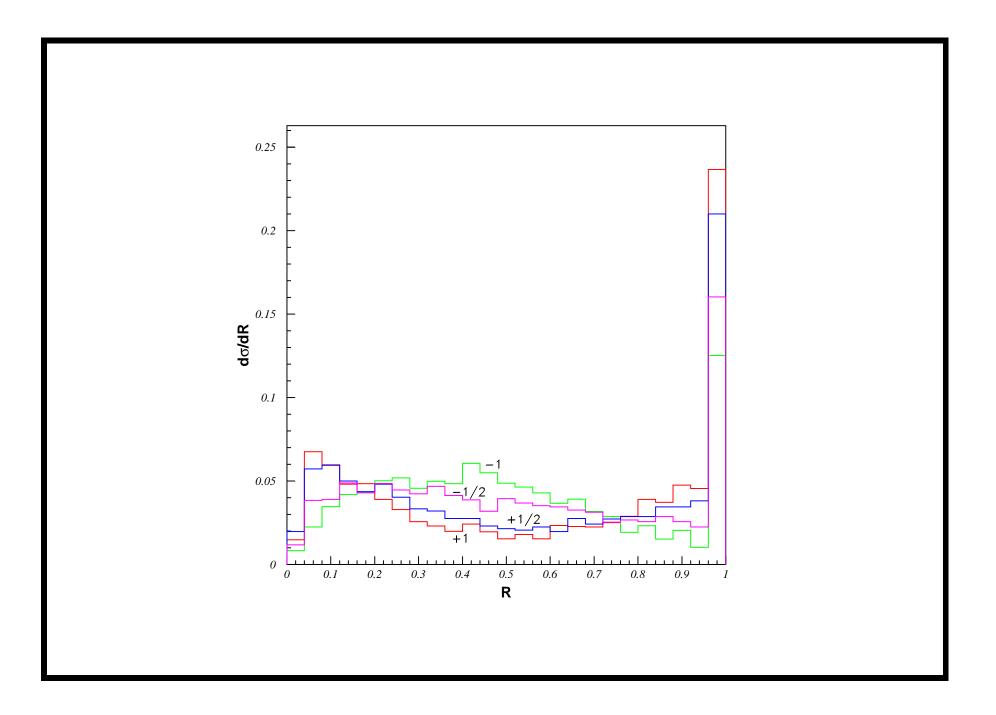
Unambigous SUSY signal from the pair production:

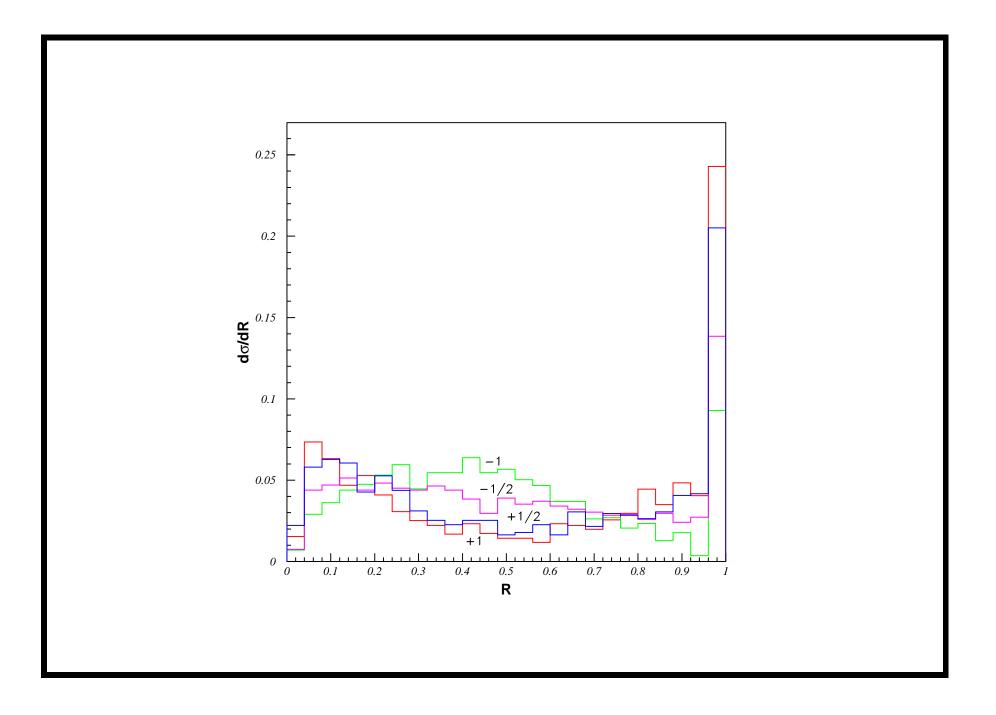
$$e^+e^- \rightarrow \tilde{\tau}_1\tilde{\tau}_1 \rightarrow \tau^+\tau^-\tilde{\chi}_1^0\tilde{\chi}_1^0$$

Cross section depends on  $m_{\tilde{\tau}_1}, m_{\tilde{\chi}_1^0}$  and  $\cos \theta_{\tilde{\tau}_1}$ . Br $(\tilde{\tau}_1 \to \tau \tilde{\chi}_1^0) = 1$ Our Analysis  $\sqrt{s}$ =350 GeV,  $m_{\tilde{\tau}_1}$  =150 GeV,  $m_{\tilde{\chi}_1^0}$ =100 GeV.  $\sigma \sim 200 \text{ fb} \Rightarrow 2 \times 10^4 \text{ signal events for } \mathcal{L}$ =100 fb<sup>-1</sup>.

Tools: PYTHIA interfacing with TAUOLA(including ISR/FSR effects)

$$p_{\tau-\text{jet}}^T > 25 \text{ GeV}, \cos \theta_{\tau-\text{jet}} < 0.75$$





#### **SUSY Models**

• mSUGRA, LSP,  $\tilde{\chi}_1^0$  is dominated by  $\tilde{B}$  component  $(N_{11})$ ;  $\cos \theta_{\tilde{\tau}_1}$  is small for moderate  $\tan \beta$ 

$$P_{\tau} \simeq +1$$

• Non universal SUGRA model, LSP is dominated by Higgsino  $(N_{13})$ ;

$$\Rightarrow P_{\tau} \simeq \cos^2 \theta_{\tilde{\tau}} - \sin^2 \theta_{\tilde{\tau}}$$

• In AMSB model, LSP is domnated by wino component  $N_{12}$ 

$$P_{\tau} \simeq -1$$

• In GMSB model, the LSP is  $\tilde{G}$ ,  $\tilde{\tau}_1 \to \tau \tilde{G}$ 

$$P_{\tau} \simeq \sin^2 \theta_{\tilde{\tau}} - \cos^2 \theta_{\tilde{\tau}}$$

$$\cos \theta_{\tilde{\tau}} = 0.5 \rightarrow P_{\tau} \simeq +1 -1/2, -1 , +1/2$$

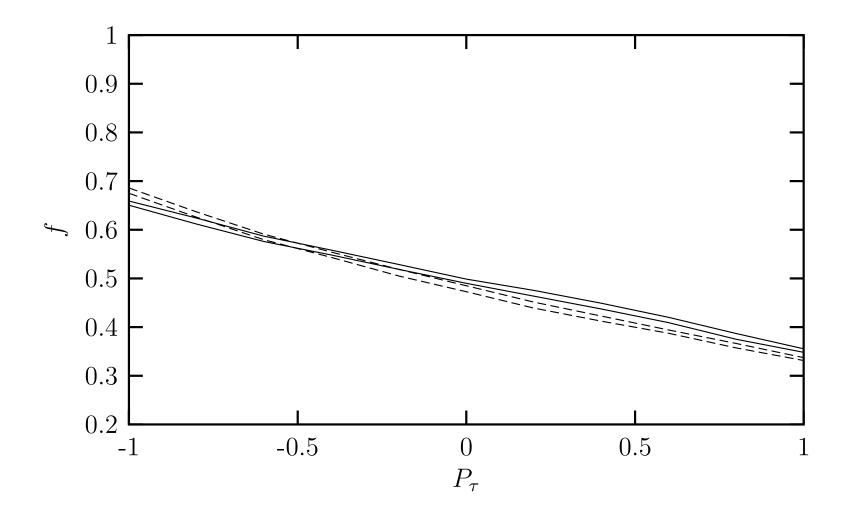
Possible to distinguish different SUSY models by measuring  $P_{\tau}$ .

An observable:

$$f = \frac{\sigma(0.2 < R < 0.8)}{\sigma_{total}}$$

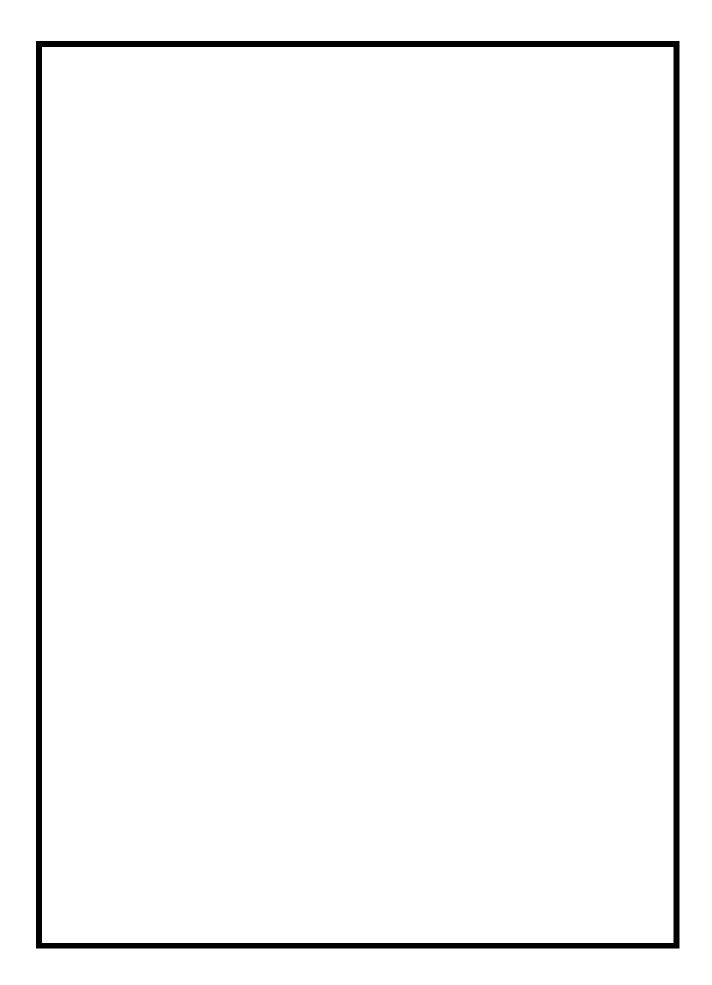
The fractional cross sections in the interval 0.2 < R < 0.8 plotted against  $\tau$  polarization for  $p_{\tau-jet}^T > 25$  GeV (solid lines) and  $p_{\tau-jet}^T > 50$  GeV (dashed lines).

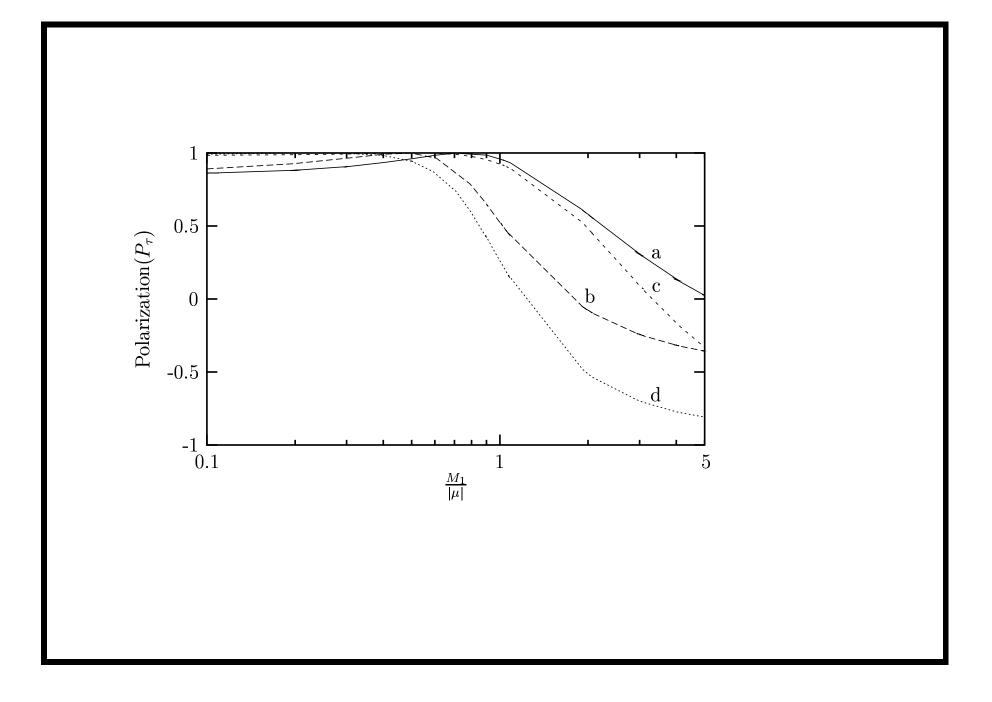
$$\Delta P_{\tau} = \pm 0.03 \ (\pm 0.05) \text{ near } P_{\tau} = -1(+1)$$



#### Partial determination of SUSY parameters

- $\tan \beta$  and  $\cos \theta_{\tilde{\tau}}$  is known from some other measurements
- Assume also  $M_1 \simeq 0.5 M_2$  which is true for most of the model.
- Assume that the absolute scale of one of the SUSY masses, in terms some combinantion of  $M_1, M_2$  and  $\mu$ , can be measured.
- Polarization of  $\tau$  is shown against  $M_1/|\mu|$  for a fixed value of  $m_{\tilde{Z}_1} = 100$  GeV and  $M_1/M_2 = 0.5$  and different sets of parameters:(a)  $\tan \beta = 10, \cos \theta_{\tau} = 0.5$ ; (b)  $\tan \beta = 40, \cos \theta_{\tilde{\tau}} = 0.5$ ; (c)  $\tan \beta = 10, \cos \theta_{\tilde{\tau}} = 0.2$ ; (d)  $\tan \beta = 40, \cos \theta_{\tilde{\tau}} = 0.2$ .

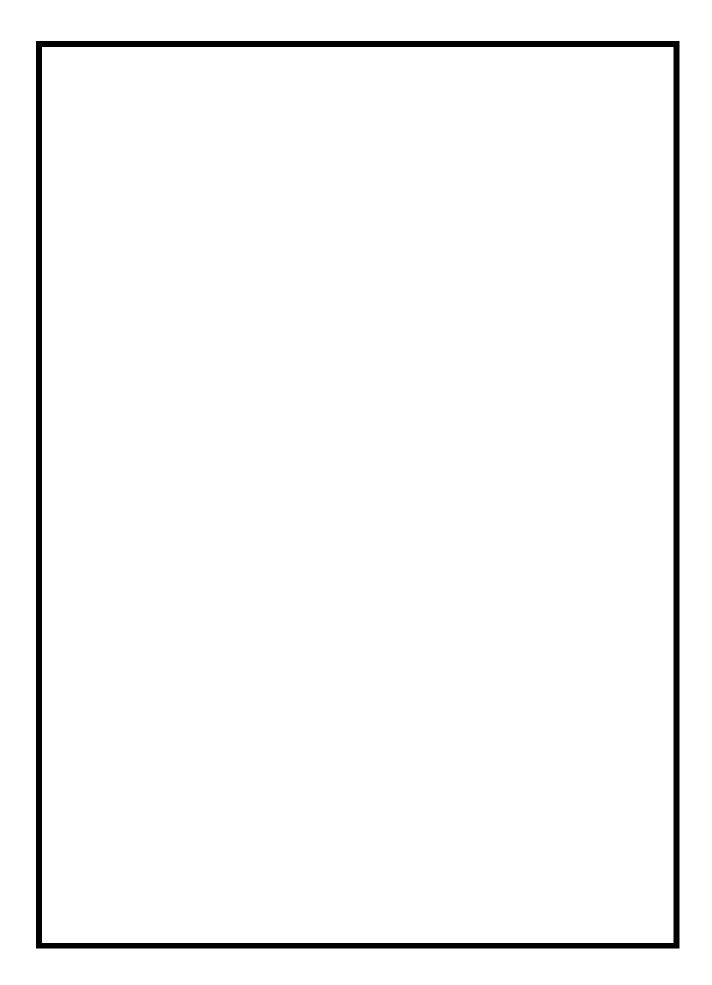


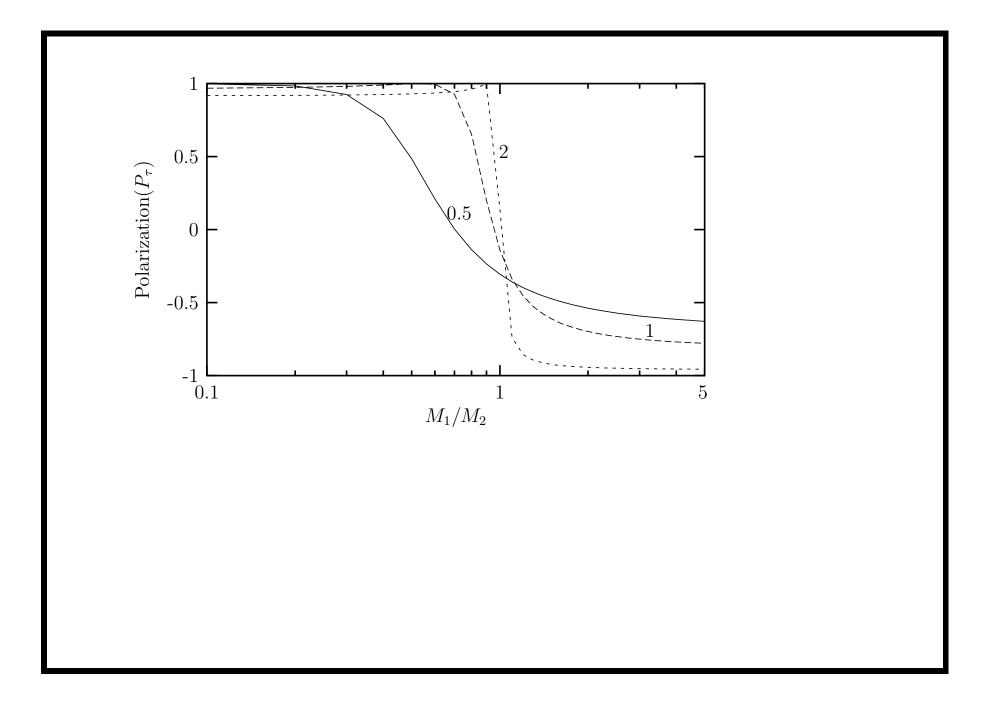


#### Parameter determination

Parameters:  $M_2, M_1, \mu, \tan \beta$ 

- Chargino sector:  $M_2, \mu, \tan \beta$
- Measurements:  $m_{\tilde{\chi}_1^{\pm}}, \sigma_L, \sigma_R, \sigma_T \Rightarrow M_2, \mu, \tan \beta$  and  $m_{\tilde{\nu}}$
- Combining these measurements and measuring  $P_{\tau}$  and  $\theta_{\tilde{\tau}} \Rightarrow M_1$ .
- In a global fit  $P_{\tau}$  will be one of the important variable in a model independent determination of  $\theta_{\tilde{\tau}}, M_2, \mu$  and  $\tan \beta$





#### Conclusion

- Polarization of  $\tau$  depends on the composition of  $\tilde{\chi}_1^0$ .
- Polarisation of  $\tau$  is different for different SUSY models.
- It is possible to discriminate different SUSY models by measuring  $P_{\tau}$ . Resolution error, basically statistical error in measurements of  $P_{\tau}$ .
- Partial determination of SUSY parameter  $(M_1)$  is possible.
- Full determination of SUSY EW paramters are possible in association with the measurements of Chargino sector, may also offer for consistency checks