

# Theoretical challenges in neutrino cross-sections

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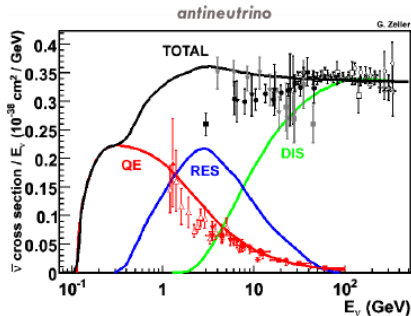
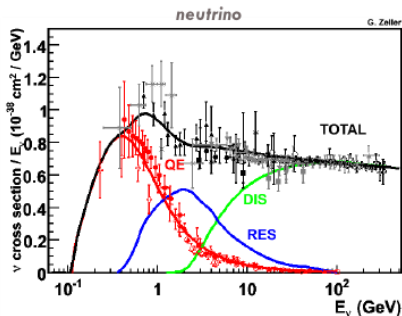
*Workshop on neutrino near detectors based on gas TPCs,*  
CERN, November 8-9, 2016



## Outline:

- Introduction and general remarks.
- Challenge # 1: understanding CCQE peak.
- Challenge # 2: a size and characteristics of 2p-2h contribution.
- Challenge # 3: understanding  $\pi$  production in the  $\Delta$  region on nuclear targets.
- Conclusions.





(from Sam Zeller; based on P. Lipari et al, Phys. Rev. Lett. 74 (1995) 4384)

CCQE is  $\nu_\mu n \rightarrow \mu^- p$ , or  $\bar{\nu}_\mu p \rightarrow \mu^+ n$ .

RES stands for resonance region e.g.  $\nu_\mu p \rightarrow \mu^- \Delta^{++} \rightarrow \mu^- p \pi^+$ ;  
one often speaks about SPP - single pion production

DIS stands for: more inelastic than RES.

In case of nucleus target scattering one must consider also COH (coherent pion production) and MEC (2p-2h).



## General remarks

- Motivation: reconstruction of  $\nu$  energy based on detected final state particles
  - a pattern of  $\nu$  oscillations is energy dependent
- A general picture: impulse approximation
  - interaction is a two step process: scattering on a bound nucleon (CCQE, RES or DIS) followed by final state interactions
  - IA has its own limitations: momentum transfer should be large enough
- Challenges are related both with primary interaction and nuclear effects.
- Typically, challenges have both “theoretical” and “experimental” aspects
  - E.g. for CCQE it would be nice to calculate axial form factor with lattice QCD, but also it would be great to have new measurements in hydrogen/deuterium bubble chamber experiments.



## Challenge # 1. Understanding CCQE/QE peak region.

In a few GeV region **CCQE** is most important to understand properly.

- **CCQE is analogous to  $eN \rightarrow eN$  scattering.**
- **Nuclear effects in electron and neutrino nucleus scattering are similar: mean-free path of virtual photon and W/Z boson are much larger than nucleus size.**
- **We can use information gathered in electron scattering studies.**
- **It is necessary to include MEC contribution.**



## Challenge # 1. (cont.)

In the case of  $\nu$  scattering we know the story:

- MiniBooNE large **CCQE**  $M_A$  measurement.
- Marteau-Martini-Chanfray-Ericson theoretical explanation in terms of a large **MEC** contribution.
- Nieves et al computations implemented in MC generators.
- MiniBooNE **CCQE**  $\bar{\nu}_\mu$  measurement.
- MINERvA **CCQE**  $\nu_\mu$  and  $\bar{\nu}_\mu$  measurements.
- Problems with reproducing all the data with a single model.

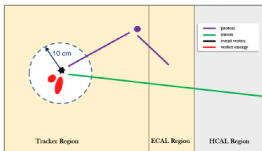


## Challenge # 1. (cont.)

Important question related with the MINERvA measurement: Is Monte Carlo (GENIE) bias fully understood?

### Removing Background Events

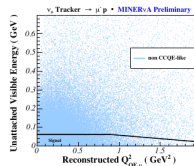
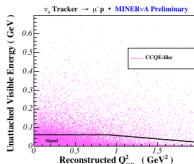
- Large amounts of extra energy, not associated with the muon or proton, usually come from untracked particles
- Define an unattached visible energy, energy outside 10 cm



- Requires the unattached energy versus the 4-momentum transfer QE scattering using the muon kinematics

$$Q_{QE}^2 = 2E_{\nu, QE}(E_{\mu} - p_{\mu}\cos\theta_{\mu}) - m_{\mu}^2$$

Betancourt, NuInt15

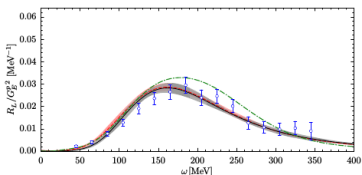


How well MC (here GENIE) reproduces distribution of hadronic energy?



## Challenge # 1. (cont.)

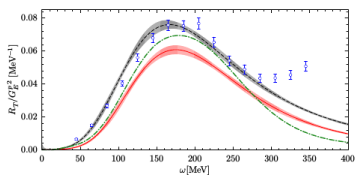
Ab initio Green function Monte Carlo (GFMC) computations (electron scattering) show that there is a significant 2-body current (MEC) contribution in the QE peak region (below results for  $|\vec{q}| = 570$  MeV/c):



Lovato et al, PRL 117 (2016) 082501

- GFMC  $O_{1b}$
- - - GFMC  $O_{1b+2b}$
- PWIA
- World data

$O_{1b+2b}$  is needed to reproduce QE peak in  $R_T$  ( $2b$  is  $2p-2h$ ).



PWIA - plane wave impulse approximation – e.g. Fermi gas model

$O_{1b}$  - one body operator

$O_{1b+2b}$  - one body and two body operator





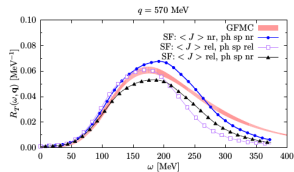
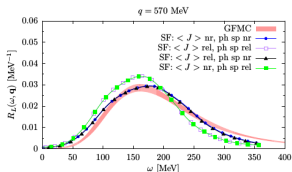
## Challenge # 1. (cont.)

Ab initio computations have important limitations

- light nuclei (numerical complexity and nuclear structure)
- restricted kinematical region (nonrelativistic regime, no pion production)

They may be used to benchmark effective models in kinematical region where both are reliable

- this is challenging because GFMC is most reliable at low  $|\vec{q}|$  when IA cannot be fully trusted.

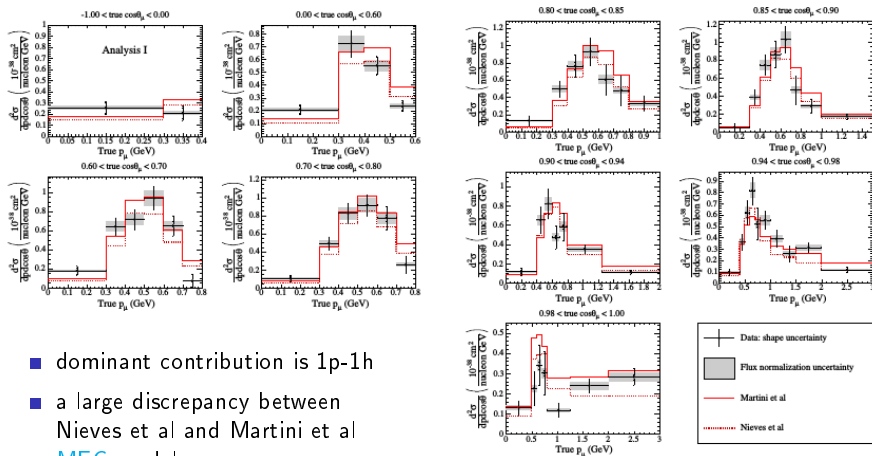


Rocco, Lovato, Benhar, arXiv:1610.06081 [nucl-th]



# Challenge # 2. A size and characteristics of MEC contribution.

T2K results for  $CC0\pi$ : Phys.Rev. D93 (2016) 112012



- dominant contribution is 1p-1h
- a large discrepancy between Nieves et al and Martini et al MEC models.



Challenge # 2. A size and characteristics of MEC contribution.

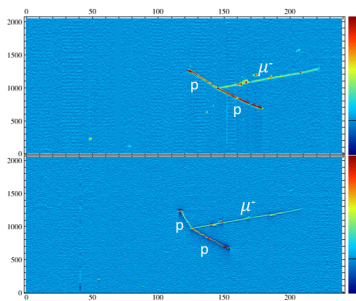
Investigation of more exclusive channels like  $1\mu 0\pi 1p$ ,  $1\mu 0\pi 2p$  can be very useful.

Two motivations:

- $\nu_\mu$  energy reconstruction is better.
- Measurement of MEC can hopefully be done.

Transverse kinematics studies:

Lu et al Phys.Rev. C94 (2016) 015503; Lu, Betancourt (for the MINERvA Collaboration), arXiv:1608.04655 [hep-ex]; Dolan, Lu, Pickering, Vladislavjevic, Weber (for the T2K collaboration) arXiv:1610.05077 [hep-ex]



Acciarri et al., PRD90 (2014) 012008

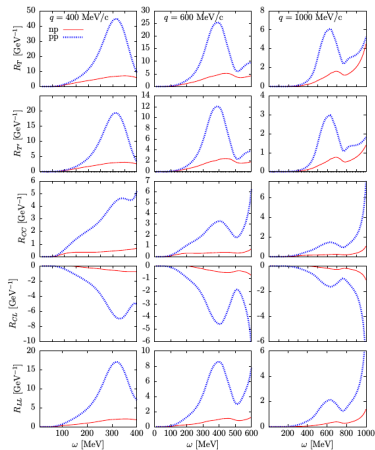
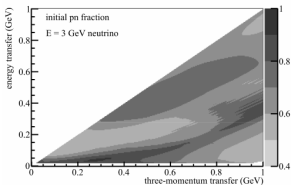
ArgoNeuT hammer events.



## Challenge # 2. A size and characteristics of MEC contribution.

Investigation of more exclusive channels like  $1\mu 1p$ ,  $1\mu 2p$ .

- We need reliable predictions for final state nucleons from of MEC events
  - isospin composition of NN pairs
  - sharing of momentum transfer  $\vec{q}$



## Challenge # 2. A size and characteristics of MEC contribution.

A possible goal is to identify true CCQE in CC0 $\pi$  sample of events. Remaining are MEC and RES with  $\pi$  absorption.

- For  $1\mu 1p0\pi$  events under CCQE hypothesis using energy and momentum conservation one can reconstruct  $\nu$  and neutron momentum vectors.
- $p_T$  is unbalanced transverse momentum (transverse relative to neutrino momentum)

$$p_L = \frac{(M_A + k'_L + p'_L - E' - E_{p'})^2 - p_T^2 - M_{A-1}^{*2}}{2(M_A + k'_L + p'_L - E' - E_{p'})},$$

$$p_{neutron} = \sqrt{\vec{p}_T^2 + p_L^2}.$$

$M_A$  target mass,  $E'$ ,  $k'_L$  muon energy and longitudinal momentum,  $E_{p'}$ ,  $p'_L$  proton energy and longitudinal momentum,  $M_{A-1}^*$  remnant nucleus mass.

$$E_\nu = k'_L + p'_L - p_L.$$

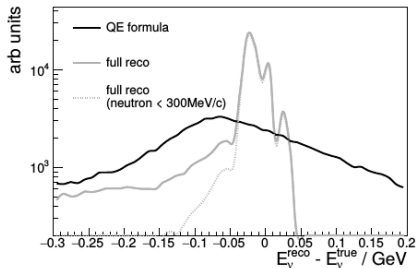
If FSI effects are under control one can arrive at very good separation of CCQE from RES and MEC with an excellent  $E_\nu$  reconstruction of CCQE enhanced sample.

Details: back-up slides.



Challenge # 2. A size and characteristics of MEC contribution.

One gets high purity CCQE sample of events ( $\sim 95\%$ ) with a very good  $\nu_\mu$  energy reconstruction:



Furmanski, JTS, arXiv:1609.03530 [hep-ex].

- Black solid line: traditional CCQE  $E_{rec}$  formula.
- Green solid line: our  $E_\nu$  formula without a cut on neutron momentum.
- Grey dotted line: our  $E_\nu$  formula without a cut on neutron momentum.

Peaks come from argon shell structure!

WARNING: details depend on the quality of MC FSI models.



Challenge # 3. Understanding  $\pi$  production in the  $\Delta$  region on nuclear targets.

There are several ingredients of theoretical computations

- $N \rightarrow \Delta$  transition matrix element (in terms of form factors)
- a model of non-resonant background
- $\Delta$  self-energy in nuclear matter
- $\pi$  final state interactions effects (absorption, charge exchange).



## Challenge # 3 (cont.)

$N \rightarrow \Delta$  transition matrix elements, a lot of hard work to extract information from old ANL and BNL deuterium bubble target experiments:

- an apparent cross section normalization tension understood in terms of flux errors  
Graczyk, JTS, et al, PRD80 (2009) 093001; Rodrigues et al, Eur.Phys.J. C76 (2016) 474
- inclusion of non-resonant background has impact on extracted values of  $M_A^{res}$  and  $C_A^5(0)$   
Hernandez, Nieves, Valverde, PRD76 (2007) 033005
- most of studies focus on  $\nu_\mu p \rightarrow \mu^- p \pi^+$  channel but there seem to be a tension with other two channels  
Graczyk, Żmuda, JTS, PRD90 (2014) 093001
- deuteron effects are surprisingly large  
Wu, Sato, Lee, PRC91 (2015) 035203





## Challenge # 3. (cont.)

## MiniBooNE

- target is  $CH_2$
- flux peaks at 600 MeV, without high energy tail  $\Rightarrow$  the relevant dynamics is in the  $\Delta$  region
- coherent  $\pi^+$  production is a part of the signal
- signal is defined as  $1\pi^+$  and no other pions in the final state.

Aguilar-Arevalo et al. [MiniBooNE Collaboration], PRD83 052007 (2011).

## MINERvA

- target is CH
- NuMi flux (1.5 – 10) GeV with  $\langle E_\nu \rangle \sim 4$  GeV
- a cut  $W < 1.4$  GeV
- as a result, the  $\Delta$  region is investigated, like in the MiniBooNE experiment
- coherent  $\pi^+$  production is a part of the signal
- signal is defined as  $1\pi^+$  and no other  $\pi^\pm$  in the final state
  - contrary to MiniBooNE there can be arbitrary number of  $\pi^0$ 's in the final state
  - due to  $W$  cut there is no phase space for many  $\pi^0$ 's though

Eberly et al, [MINERvA Collaboration], PRD92 (2015) 092008



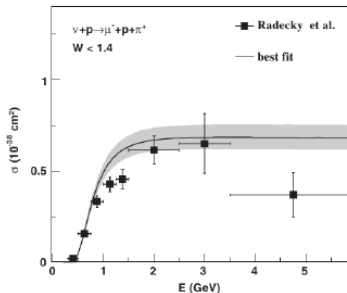
## Challenge # 3. (cont.)

Does it make sense to compare MiniBooNE and MINERvA results?

- very different energies

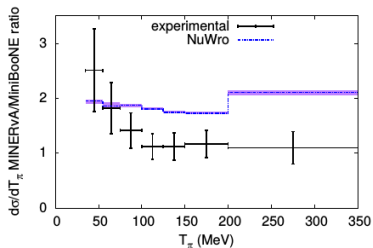
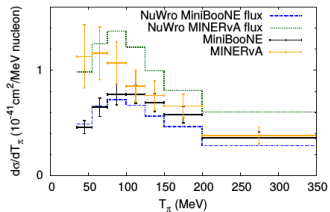
But...

- the same  $\Delta$  mechanism



- the only major difference is coming from  $\nu$  energy is normalization
- $\pi^+$  production cross section at 4 GeV is  $\sim$  twice that at 700 MeV
- less important: slightly different definitions of the signal.

## Challenge # 3. (cont.)



- the ratio is expected to be quite flat
- there is a worrying data/MC normalization discrepancy, more than 40%

The actual normalization discrepancy is smaller because MINERvA made better estimate of the flux and all the older cross section must be increased by 10-15% (no official data available yet).

NuWro is not perfect but the ratio result seems to be mostly independent on the model details. The only really important input is  $\Delta$  excitation cross section.



## Conclusions

- There is a lot of experimental and theoretical activities focused on  $\nu$  cross sections.
- There is a lot of progress,

but ... much is left to be done.

My feeling is that further progress depend on precise cross section measurements (**experimental challenges**)

- $\pi$  production – to resolve MiniBooNE/MINERvA tension.
- **CCQE** peak – to estimate a size of **MEC** contribution.

and on (**theoretical challenges**)

- ability to explore information contained in hadronic final state (FSI effects for  $\pi$  and nucleons, reliable models of hadronic final state from **MEC** events).



Back-up slides



Challenge # 2. A size and characteristics of MEC contribution.

$M_{A-1}^*$  can be estimated using information about argon shell model structure:

Subshell	$E_\alpha$ [MeV]	$\sigma_\alpha$ [MeV]	# neutrons $n_\alpha$
$1s_{1/2}$	62	6.25	2
$1p_{3/2}$	40	3.75	4
$1p_{1/2}$	35	3.75	2
$1d_{5/2}$	18	1.25	6
$2s_{1/2}$	13.15	1	2
$1d_{3/2}$	11.45	0.75	4
$1f_{7/2}$	5.56	0.75	2

Ankowski, JTS, Phys.Rev. C77 (2008) 044311

where  $E_\alpha$  is energy level and  $\sigma_\alpha$  is its width.

One gets probability distribution for separation energy:

$$P(E) = \frac{1}{N} \sum_{\alpha} n_{\alpha} G(E - E_{\alpha}, \sigma_{\alpha})$$

( $G$  is Gaussian distribution,  $N$  number of neutrons) and

$$M_A = 22M_n + 18M_p - 343.81 \text{ MeV},$$

$$M_{A-1}^* = M_A - M_n + E.$$



Challenge # 2. A size and characteristics of MEC contribution.

Selection:  $1\mu 1p0\pi$  with some proton reconstruction threshold  $p_{thr}$ ?

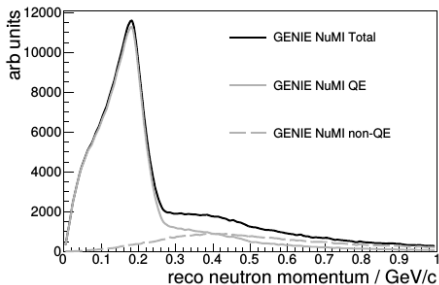
When reconstructed neutron momentum has very large value (wrt Fermi momentum)?

- Event was MEC. Second proton momentum is below threshold.
- Event was RES with  $\pi$  being absorbed.
- Event was CCQE with proton suffering from severe FSI effects.



## Challenge # 2. A size and characteristics of MEC contribution.

Typical distribution of reconstructed neutron momentum:

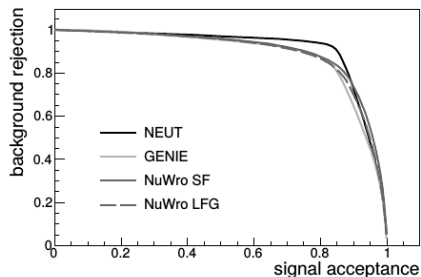


Furmanski, JTS, arXiv:1609.03530 [hep-ex].

Optimal cut is  $p_{cut} \approx 300$  MeV/c.

A sample that are rejected contains many MEC events!.

One can try to optimize reconstructed neutron momentum cut:





## Challenge # 3. (cont.)

Composition of signal in two experiments according to NuWro  
MiniBooNE

- RES: 87.1%
- COH: 6.7%
- DIS: 3.6%
- CCQE and MEC: 2.7%

MINERvA

- RES: 84.7%
- COH: 10.7%
- CCQE and MEC: 4.6%



## Challenge # 3. (cont.)

The only relevant difference is in normalization: at MINERvA energies cross section is larger by a factor of  $\sim 2$ !

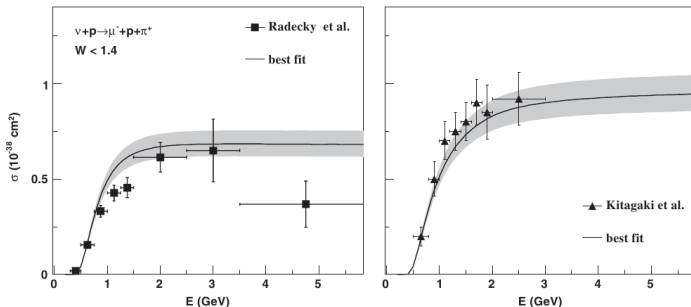


FIG. 5. Total cross section for  $\nu + p \rightarrow \mu^- + p + \pi^+$ . In the left panel the ANL data [5] with the cut  $W = 1.4$  are shown (black squares), while the right panel presents the BNL data [42] (without cuts in  $W$ )—black triangles. The overall normalization error is not plotted. The best fit curves were obtained with a corresponding cut in  $W$ . The theoretical curves were obtained with dipole parametrization Eq. (32) with  $M_A = 0.94$  GeV and  $C_2^2(0) = 1.19$ . The shaded areas denote the  $1\sigma$  uncertainties of the best fit. The theoretical curves are not modified by the deuteron correction effect.

Graczyk, Kiełczewska, Przewłocki, JTS, PRD80 093001 (2009).