

Charm Physics at BESIII



Xin Shi

IHEP, CAS

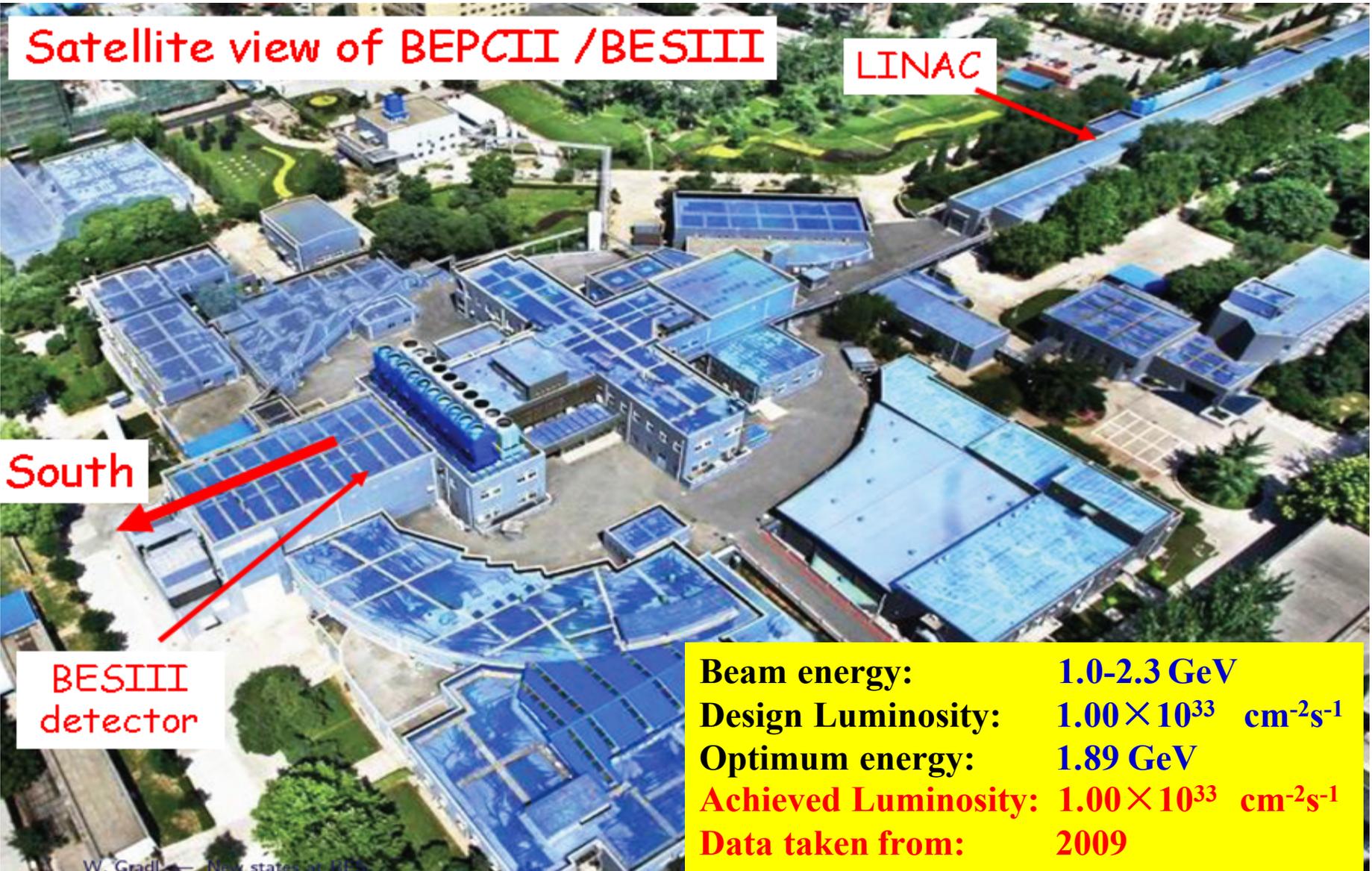
DIS17 @ University of Birmingham

2017.04.04

Outline

- **Overview**
- **D leptonic decays**
- **D hadronic decays**
- **Λ_c^+ decays**
- **Summary**

BEPCII: high luminosity double-ring collider

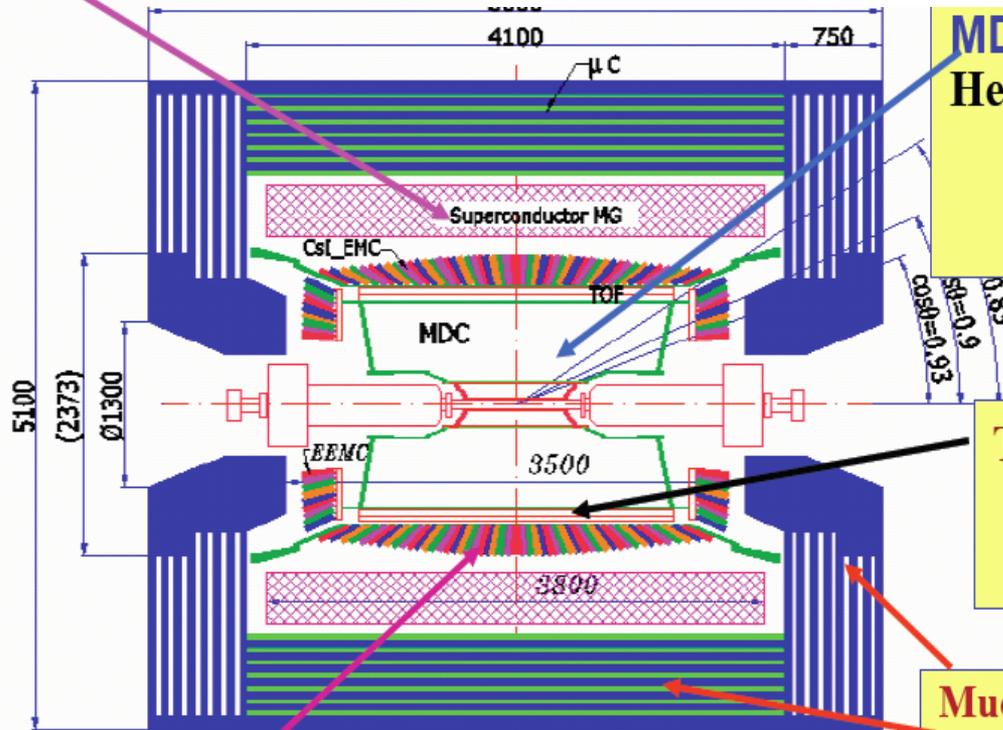


Beam energy:	1.0-2.3 GeV
Design Luminosity:	$1.00 \times 10^{33} \text{ cm}^{-2}\text{s}^{-1}$
Optimum energy:	1.89 GeV
Achieved Luminosity:	$1.00 \times 10^{33} \text{ cm}^{-2}\text{s}^{-1}$
Data taken from:	2009

BESIII detector

Magnet: 1 T Super conducting

Nucl. Instr. Meth. A614, 345 (2010)



MDC: small cell & Gas:
He/C₃H₈ (60/40), 43 layers
 $\sigma_{xy} = 130 \mu\text{m}$
 $\sigma_p/p = 0.5\% @ 1\text{GeV}$
 $dE/dx = 6\%$

TOF:
 $\sigma_T = 100 \text{ ps}$ Barrel
 110 ps Endcap

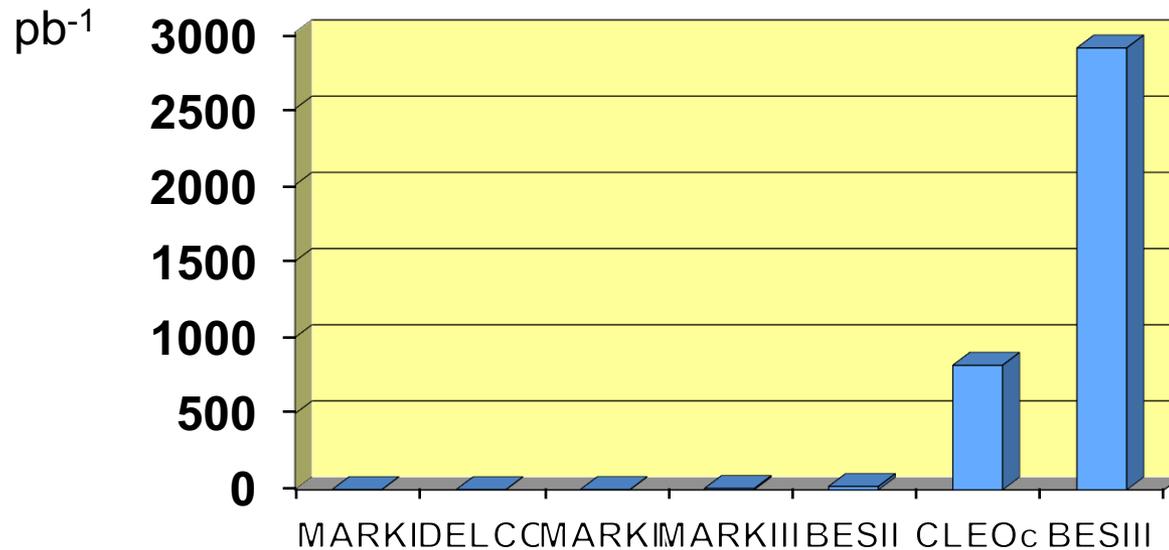
Muon ID: 9 layers RPC
8 layers for endcap

EMC: CsI crystal, 28 cm
 $\Delta E/E = 2.5\% @ 1 \text{ GeV}$
 $\sigma_z = 0.6 \text{ cm}/\sqrt{E}$

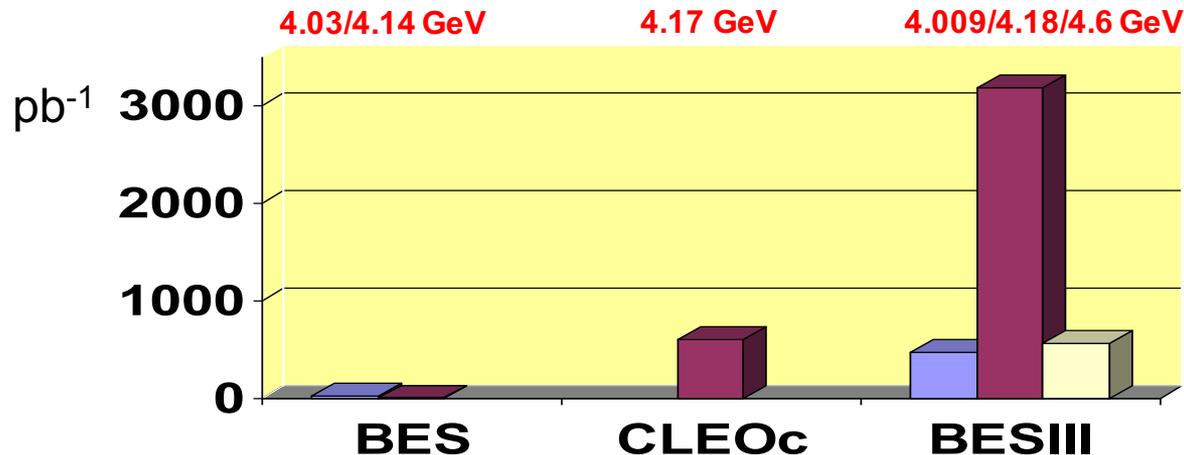
Data Acquisition:
Event rate = 4 kHz
Total data volume $\sim 50 \text{ MB/s}$

$D^{0(+)}, D_s^+, \Lambda_c^+$ samples at BESIII

➤ $D^{0(+)}$ samples at 3.773 GeV



➤ $D_s^+ / D_s^- / \Lambda_c^+$ samples at 4.009/4.18/4.6 GeV



Main goals of charm physics at BESIII

Leptonic and semileptonic decays of charmed mesons (D^0 , D^+ , D_s^+ and Λ_c^+) provide an ideal window to explore weak and strong effects

➤ D leptonic decays

$f_{D(s)^+}$, $f_{K(\pi)^+}^{K(\pi)}$: better calibrate LQCD

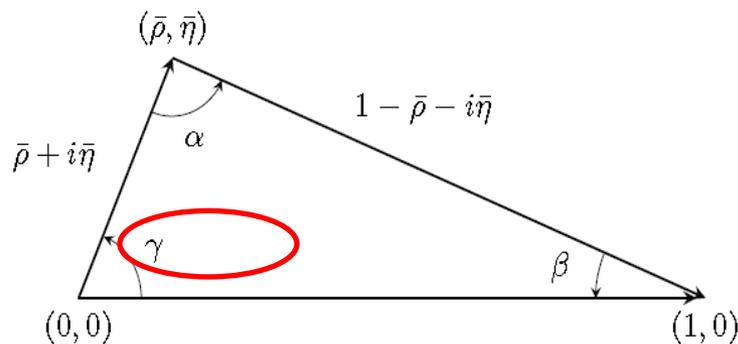
$|V_{cs(d)}|$: better test on CKM unitarity

$$U = \begin{bmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{bmatrix}$$

➤ D hadronic decays

$D^0\bar{D}^0$ mixing parameters and CP violation

Strong phase in D^0 decays: Constraint on γ/ϕ_3 measurement in B decays



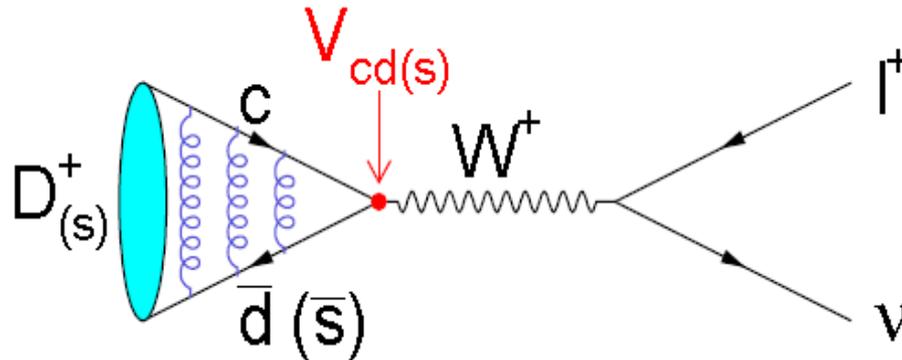
➤ Rare D decays → New physics

➤ Absolute BF's of Λ_c^+

Before BESIII, no absolute BF measurements of Λ_c^+ using near threshold data, in the past 40 years

D leptonic decays

$D_{(s)}^+$ Leptonic Decays



In the SM:

$$\Gamma(D_{(s)}^+ \rightarrow l^+ \nu_l) = \frac{G_F^2 f_{D_{(s)}^+}^2}{8\pi} |V_{cd(s)}|^2 m_l^2 m_{D_{(s)}^+} \left(1 - \frac{m_l^2}{m_{D_{(s)}^+}^2}\right)^2$$

Bridge to precisely measure

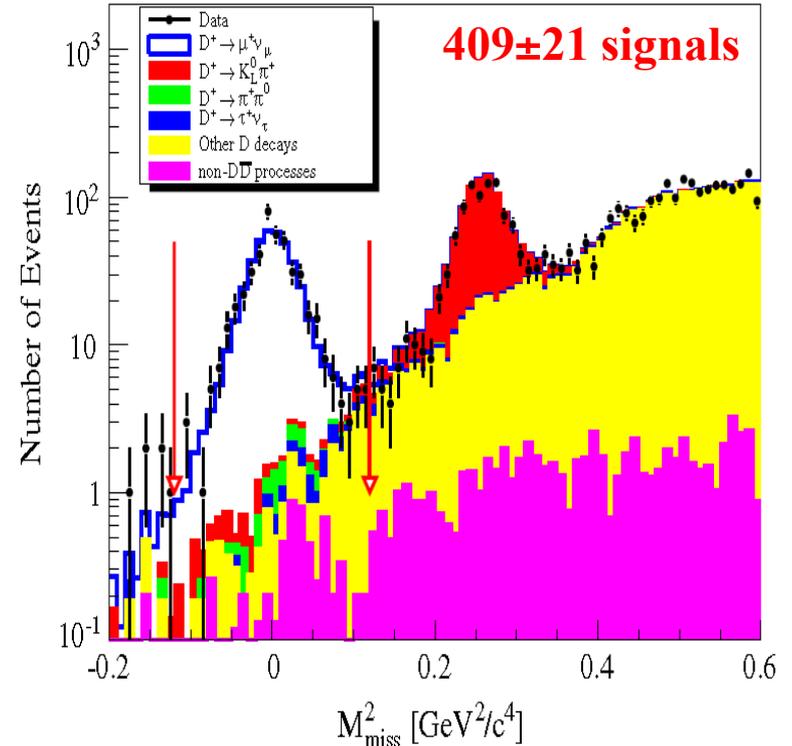
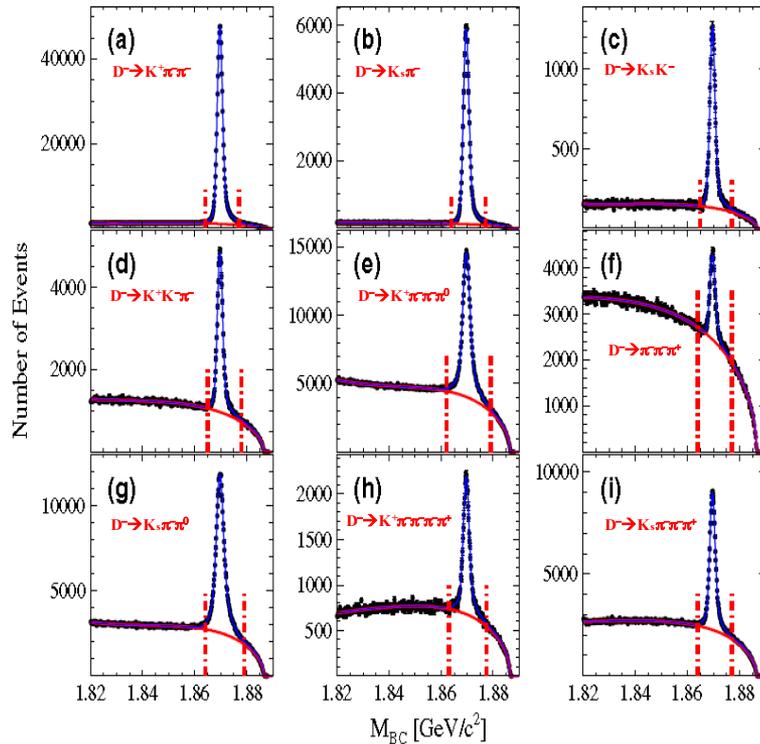
- Decay constant $f_{D_{(s)}^+}$ with input $|V_{cd(s)}|^{\text{CKMfitter}}$
- CKM matrix element $|V_{cd(s)}|$ with input $f_{D_{(s)}^+}^{\text{LQCD}}$

Improved $B[D^+ \rightarrow \mu^+ \nu]$, f_{D^+} and $|V_{cd}|$

$e^+e^- \rightarrow \psi(3770) \rightarrow D^+D^-$

2.93 fb⁻¹ data@ 3.773 GeV

PRD89(2014)051104R



$$N_{D_{\text{tag}}} = (170.31 \pm 0.34) \times 10^4$$

$$B[D^+ \rightarrow \mu^+ \nu] = (3.71 \pm 0.19 \pm 0.06) \times 10^{-4}$$

Input t_{D^+} , m_{D^+} , m_{μ^+} on PDG
and $|V_{cd}|$ of CKM-Fitter

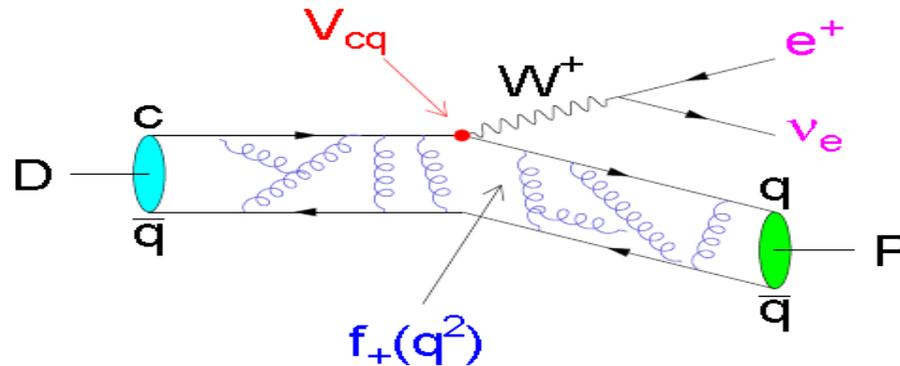
BES III

Input t_{D^+} , m_{D^+} , m_{μ^+} on PDG and
LQCD calculated $f_{D^+} = 207 \pm 4$
MeV [PRL100(2008)062002]

$$f_{D^+} = (203.2 \pm 5.3 \pm 1.8) \text{ MeV}$$

$$|V_{cd}| = 0.2210 \pm 0.0058 \pm 0.0047$$

Semi-leptonic Decay $D^0 \rightarrow K(\pi)^- e^+ \nu$



Differential rates:
$$\frac{d\Gamma}{dq^2} = X \frac{G_F^2 |V_{cd(s)}|^2}{24\pi^3} p^3 |f_+(q^2)|^2$$

Bridge to precisely measure:

■ Form factors $f_+^{D \rightarrow K(\pi)}(0)$ with input $|V_{cd(s)}|^{\text{CKMfitter}}$

– Single pole form

$$f_+(q^2) = \frac{f_+(0)}{1 - \frac{q^2}{M_{\text{pole}}^2}}$$

– Modified pole model

$$f_+(q^2) = \frac{f_+(0)}{\left(1 - \frac{q^2}{M_{\text{pole}}^2}\right) \left(1 - \alpha \frac{q^2}{M_{\text{pole}}^2}\right)}$$

– ISGW2 model

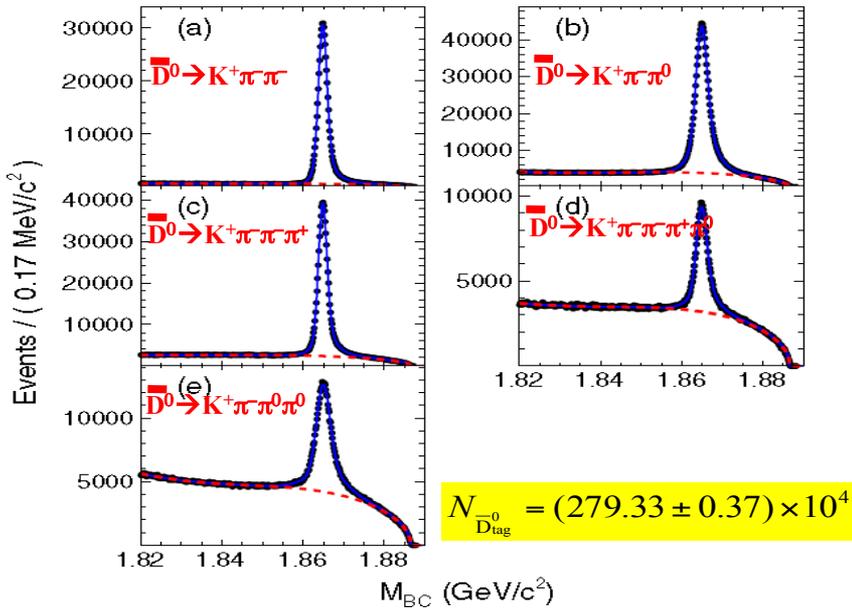
$$f_+(q^2) = f_+(q_{\text{max}}^2) \left(1 + \frac{r_{\text{ISGW2}}^2}{12} (q_{\text{max}}^2 - q^2)\right)^{-2}$$

– Series expansion model

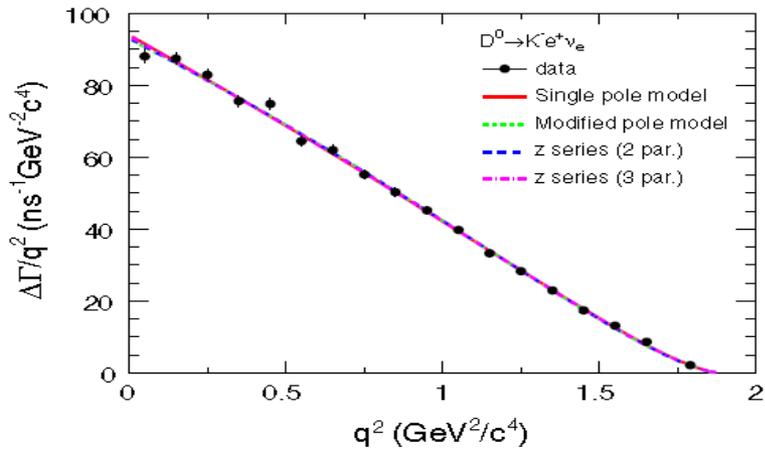
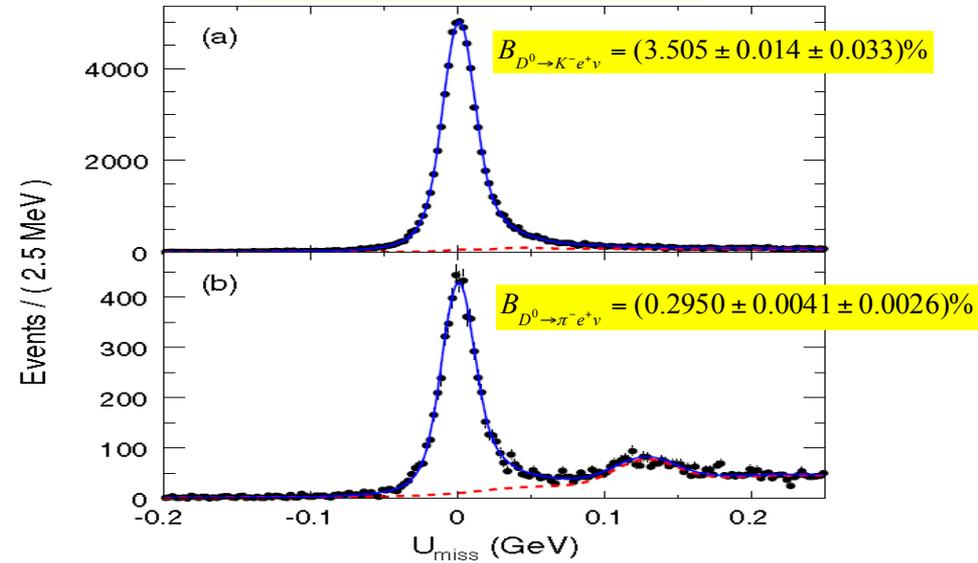
$$f_+(t) = \frac{1}{P(t)\Phi(t, t_0)} a_0(t_0) \left(1 + \sum_{k=1}^{\infty} r_k(t_0) [z(t, t_0)]^k\right)$$

■ CKM matrix element $|V_{cs(d)}|$ with input $f_+^{\text{LQCD}, D \rightarrow K(\pi)}(0)$

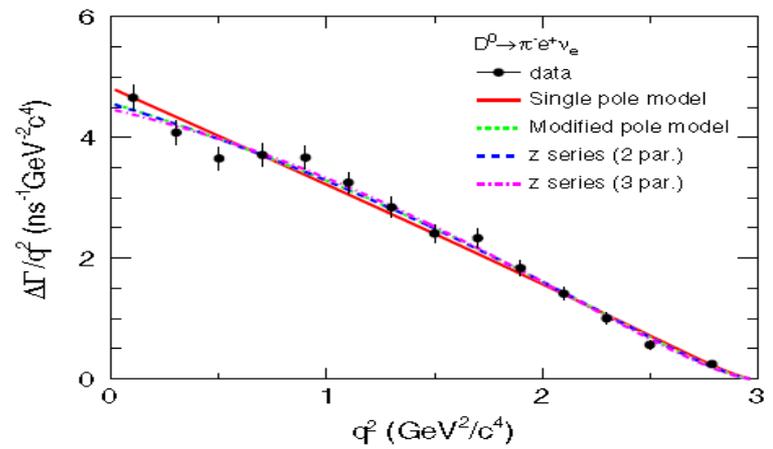
$D^0 \rightarrow K(\pi)^- e^+ \nu \rightarrow f^{D^0 \rightarrow K(\pi)^-} + (q^2) |V_{cs(d)}|$



PRD92(2015)072012



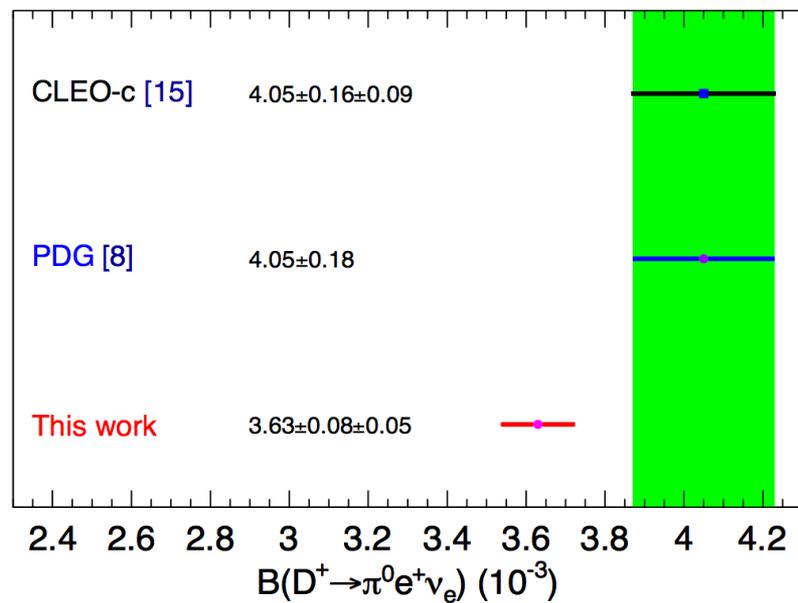
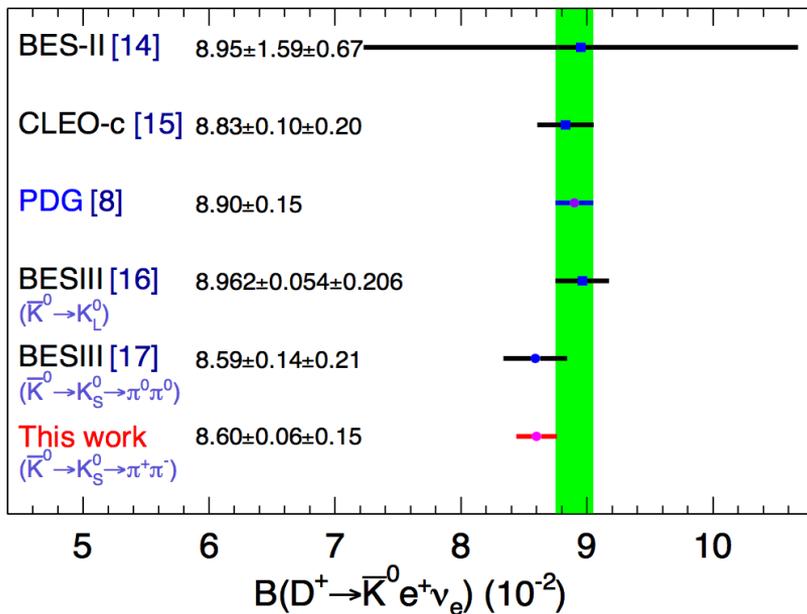
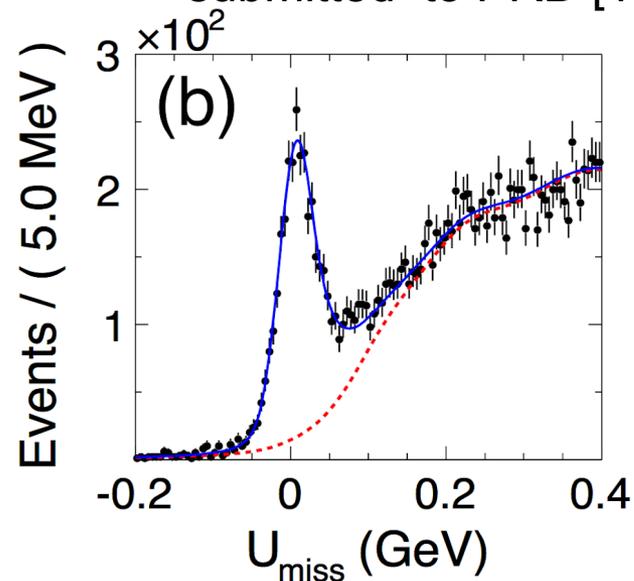
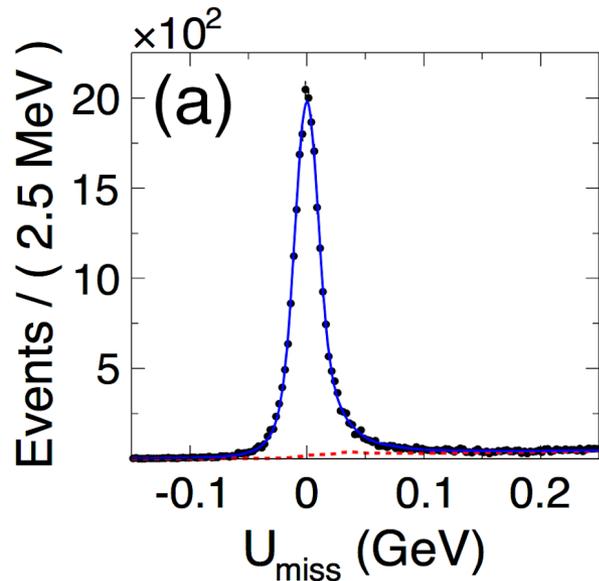
$B[D^0 \rightarrow K^- e^+ \nu]$



$B[D^0 \rightarrow \pi^- e^+ \nu]$

Analysis of $D^+ \rightarrow \bar{K}^0 e^+ \nu$ and $\pi^0 e^+ \nu$

submitted to PRD [1703.09084]



Lepton universality in $D^{0(+)} \rightarrow \pi^{-(0)} l^+ \nu$

Lepton universality (LU)

$$R_{LU}^{0(+)} = \frac{B(D^{0(+)} \rightarrow \pi^{-(0)} \mu^+ \nu)}{B(D^{0(+)} \rightarrow \pi^{-(0)} e^+ \nu)} \sim 0.97$$

Expectations based on ZPC46 (1990)93, PRD69 (2004)074025, PLB633(2006)61 and PDG16

BFs on PDG16:

$$R_{LU}^0 = 0.82 \pm 0.08 \quad (\sim 2.0\sigma)$$

$$B(D^0 \rightarrow \pi^- \mu^+ \nu) = (0.237 \pm 0.024)\%$$

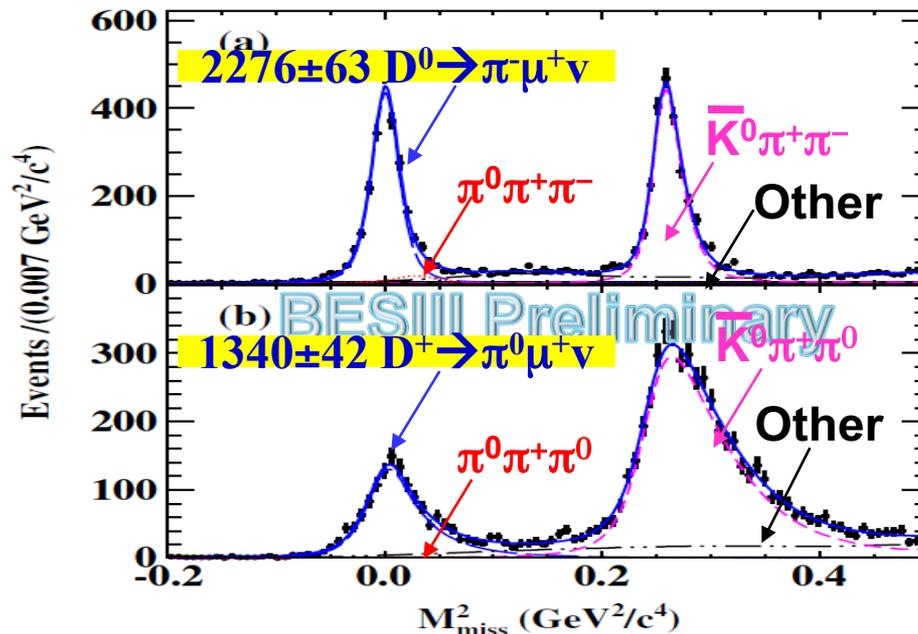
Large error in $B[D^0 \rightarrow \pi^- \mu^+ \nu]$ and no measure of $B[D^+ \rightarrow \pi^0 \mu^+ \nu]$. Precision measurements are desired

Isospin symmetry (IS)

$$R_{IS}^l = \frac{\Gamma(D^0 \rightarrow \pi^- l^+ \nu)}{2\Gamma(D^+ \rightarrow \pi^0 l^+ \nu)} \sim 1$$

PDG16: $R_{IS}^e = 0.911 \pm 0.043 \quad (2.1\sigma)$

BESIII: $R_{IS}^e = 1.03 \pm 0.03 \pm 0.02$



BFs: $B(D^0 \rightarrow \pi^- \mu^+ \nu) = (0.267 \pm 0.007 \pm 0.007)\%$

agrees with PDG and with better precision

$$B(D^+ \rightarrow \pi^0 \mu^+ \nu) = (0.342 \pm 0.011 \pm 0.010)\%$$

measured for the first time

LU: $R_{LU}^0 = 0.918 \pm 0.036 \quad R_{LU}^+ = 0.921 \pm 0.045$

agree with expectation in 1.5(1.1) σ

IS: $R_{IS}^{\mu} = 0.990 \pm 0.054$

agree with IS prediction within uncertainty

Search for $D^+ \rightarrow D^0 e^+ \nu$

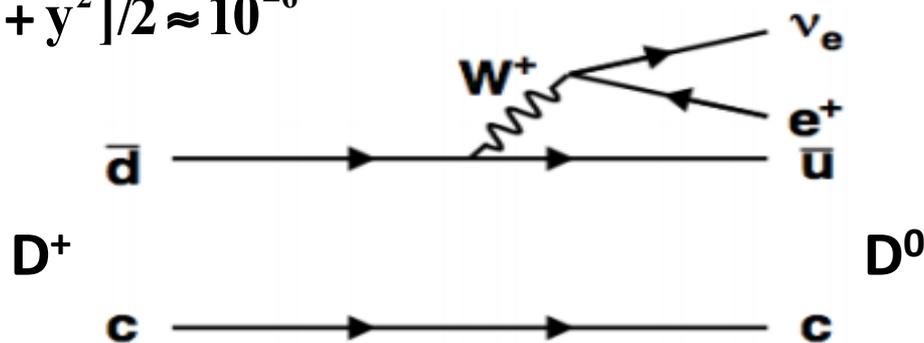
In SM, $D^0 \bar{D}^0$ mixing, CP violation and rare decay of charm are small

$D^0 \bar{D}^0$ mixing $x \approx y \approx 10^{-3} \Rightarrow r_D = [x^2 + y^2]/2 \approx 10^{-6}$

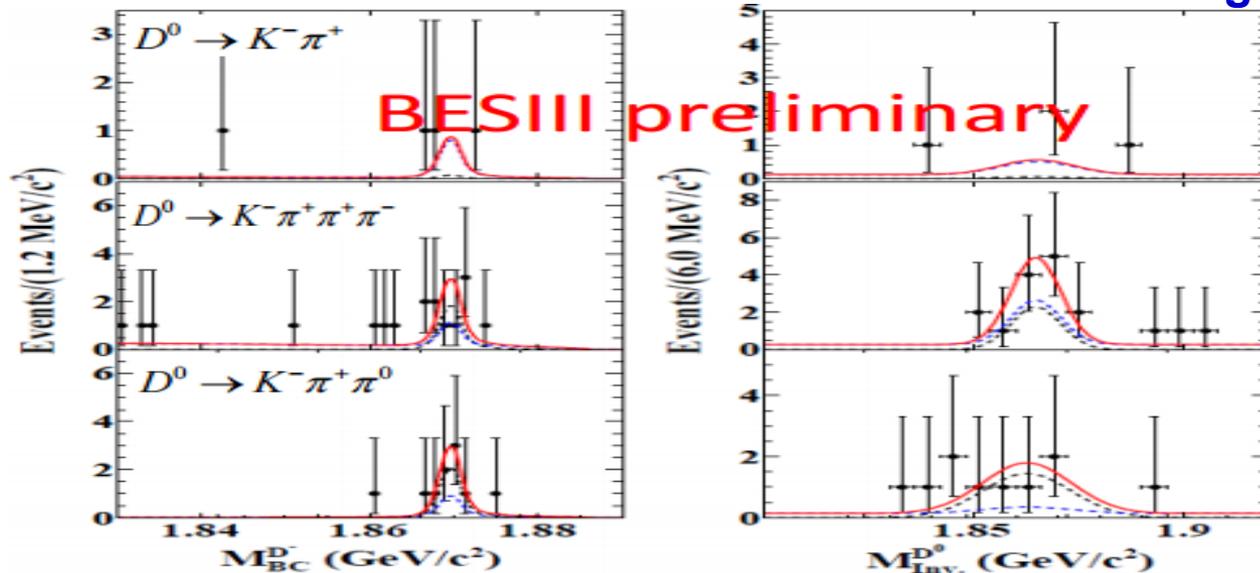
CP violation asymmetries $\sim 10^{-3}$

Rare decays $\leq 10^{-6}$

Applying the SU(3) symmetry for the light quarks, this rare decay branching fraction can be predicted by theoretical calculation and its theoretical value is 2.78×10^{-13} [EPJC, 59:841-845(2009)].



With 6 dominant D^- single tag



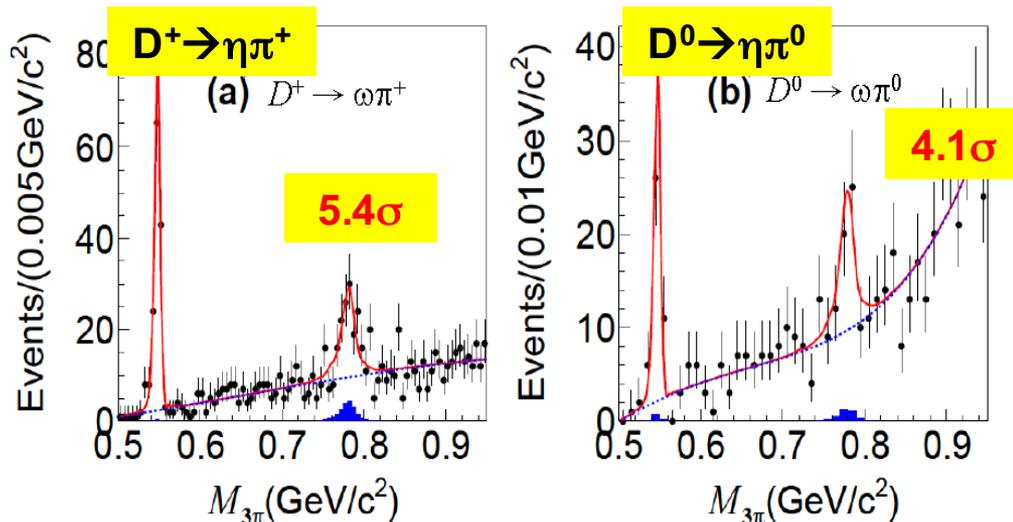
$$B[D^+ \rightarrow D^0 e^+ \nu] < 8.7 \times 10^{-5}$$

D hadronic decays

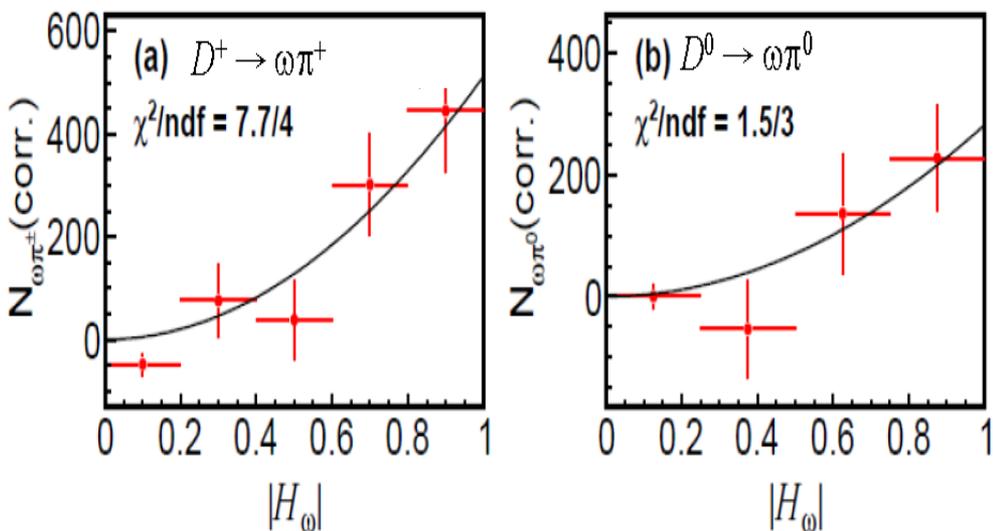
Observation/Evidence of $D \rightarrow \omega\pi$

Double tag method

PRL116(2016)082001



Decay mode	This work	Previous measurements
$D^+ \rightarrow \omega\pi^+$	$(2.74 \pm 0.58 \pm 0.17) \times 10^{-4}$	$< 3.4 \times 10^{-4}$ at 90% C.L.
$D^0 \rightarrow \omega\pi^0$	$(1.05 \pm 0.41 \pm 0.09) \times 10^{-4}$	$< 2.6 \times 10^{-4}$ at 90% C.L.
$D^+ \rightarrow \eta\pi^+$	$(3.13 \pm 0.22 \pm 0.19) \times 10^{-3}$	$(3.53 \pm 0.21) \times 10^{-3}$
$D^0 \rightarrow \eta\pi^0$	$(0.67 \pm 0.10 \pm 0.05) \times 10^{-3}$	$(0.68 \pm 0.07) \times 10^{-3}$



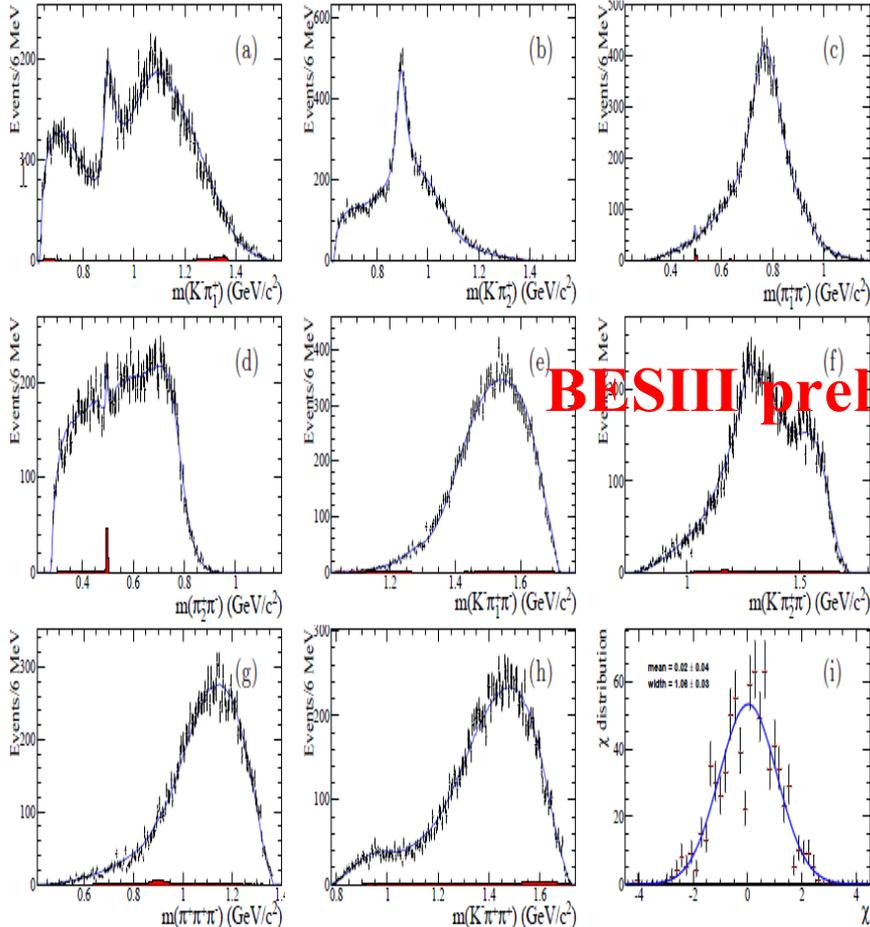
Studies of Singly Cabibbo-suppressed decays is limited by data set and background

Benefit the understanding of SU(3) symmetry breaking and CP violation, improve theory calculation

Amplitude analysis of $D^0 \rightarrow K^- \pi^+ \pi^+ \pi^-$

Help to determine the absolute BF, strong phase, benefit γ/ϕ_3

Previous analyses only from MarkIII and E691

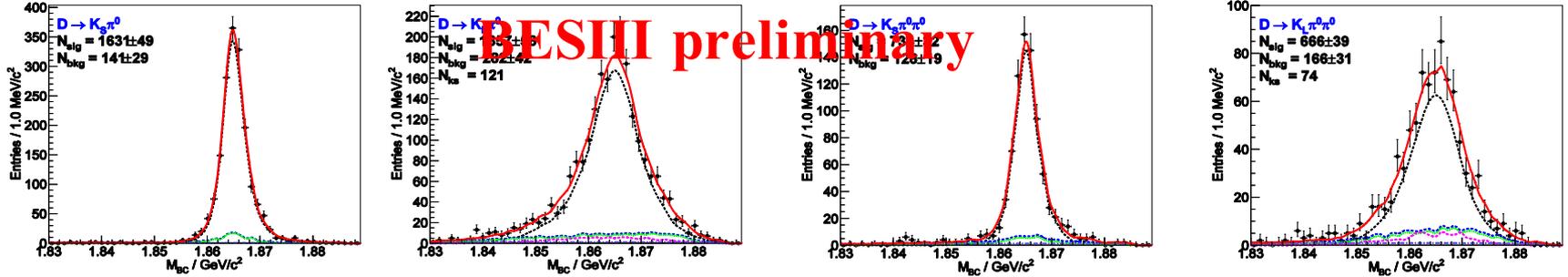


BESIII preliminary

Amplitude	ϕ_i	Fit fraction (%)
$D^0[S] \rightarrow \bar{K}^* \rho^0$	$2.35 \pm 0.06 \pm 0.18$	$6.5 \pm 0.5 \pm 0.8$
$D^0[P] \rightarrow \bar{K}^* \rho^0$	$-2.25 \pm 0.08 \pm 0.15$	$2.3 \pm 0.2 \pm 0.1$
$D^0[D] \rightarrow \bar{K}^* \rho^0$	$2.49 \pm 0.06 \pm 0.11$	$7.9 \pm 0.4 \pm 0.7$
$D^0 \rightarrow K^- a_1^+(1260), a_1^+(1260)[S] \rightarrow \rho^0 \pi^+$	0(fixed)	$53.2 \pm 2.8 \pm 4.0$
$D^0 \rightarrow K^- a_1^+(1260), a_1^+(1260)[D] \rightarrow \rho^0 \pi^+$	$-2.11 \pm 0.15 \pm 0.21$	$0.3 \pm 0.1 \pm 0.1$
$D^0 \rightarrow K_1^-(1270) \pi^+, K_1^-(1270)[S] \rightarrow \bar{K}^{*0} \pi^-$	$1.48 \pm 0.21 \pm 0.24$	$0.1 \pm 0.1 \pm 0.1$
$D^0 \rightarrow K_1^-(1270) \pi^+, K_1^-(1270)[D] \rightarrow \bar{K}^{*0} \pi^-$	$3.00 \pm 0.09 \pm 0.15$	$0.7 \pm 0.2 \pm 0.2$
$D^0 \rightarrow K_1^-(1270) \pi^+, K_1^-(1270) \rightarrow K^- \rho^0$	$-2.46 \pm 0.06 \pm 0.21$	$3.4 \pm 0.3 \pm 0.5$
$D^0 \rightarrow (\rho^0 K^-)_A \pi^+, (\rho^0 K^-)_A [D] \rightarrow K^- \rho^0$	$-0.43 \pm 0.09 \pm 0.12$	$1.1 \pm 0.2 \pm 0.3$
$D^0 \rightarrow (\rho^0 K^-)_S \pi^+$	$-0.14 \pm 0.11 \pm 0.10$	$7.4 \pm 1.6 \pm 5.7$
$D^0 \rightarrow (K^- \pi^+)_S \rho^0$	$-2.45 \pm 0.19 \pm 0.47$	$2.0 \pm 0.7 \pm 1.9$
$D^0 \rightarrow (K^- \rho^0)_V \pi^+$	$-1.34 \pm 0.12 \pm 0.09$	$0.4 \pm 0.1 \pm 0.1$
$D^0 \rightarrow (\bar{K}^{*0} \pi^-)_P \pi^+$	$-2.09 \pm 0.12 \pm 0.22$	$2.4 \pm 0.5 \pm 0.5$
$D^0 \rightarrow \bar{K}^{*0} (\pi^+ \pi^-)_S$	$-0.17 \pm 0.11 \pm 0.12$	$2.6 \pm 0.6 \pm 0.6$
$D^0 \rightarrow (\bar{K}^{*0} \pi^-)_V \pi^+$	$-2.13 \pm 0.10 \pm 0.11$	$0.8 \pm 0.1 \pm 0.1$
$D^0 \rightarrow ((K^- \pi^+)_S \pi^-)_A \pi^+$	$-1.36 \pm 0.08 \pm 0.37$	$5.6 \pm 0.9 \pm 2.7$
$D^0 \rightarrow K^- ((\pi^+ \pi^-)_S \pi^-)_A$	$-2.23 \pm 0.08 \pm 0.22$	$13.1 \pm 1.9 \pm 2.2$
$D^0 \rightarrow (K^- \pi^+)_S (\pi^+ \pi^-)_S$	$-1.40 \pm 0.04 \pm 0.22$	$16.3 \pm 0.5 \pm 0.6$
$D^0[S] \rightarrow (K^- \pi^+)_V (\pi^+ \pi^-)_V$	$1.59 \pm 0.13 \pm 0.41$	$5.4 \pm 1.2 \pm 1.9$
$D^0 \rightarrow (K^- \pi^+)_S (\pi^+ \pi^-)_V$	$-0.16 \pm 0.17 \pm 0.43$	$1.9 \pm 0.6 \pm 1.2$
$D^0 \rightarrow (K^- \pi^+)_V (\pi^+ \pi^-)_S$	$2.58 \pm 0.08 \pm 0.25$	$2.9 \pm 0.5 \pm 1.7$
$D^0 \rightarrow (K^- \pi^+)_T (\pi^+ \pi^-)_S$	$-2.92 \pm 0.14 \pm 0.12$	$0.3 \pm 0.1 \pm 0.1$
$D^0 \rightarrow (K^- \pi^+)_S (\pi^+ \pi^-)_T$	$2.45 \pm 0.12 \pm 0.37$	$0.5 \pm 0.1 \pm 0.1$

Absolute BFs and y_{CP} of $D^0 \rightarrow K_{S/L} \pi^0 (\pi^0)$

- Two dimensional fits to $M_{BC}(\text{tag})$ versus $M_{BC}(\text{signal})$
- Projections of DT events on the $M_{BC}(\text{sig})$ vs. $K\pi$ (for example)



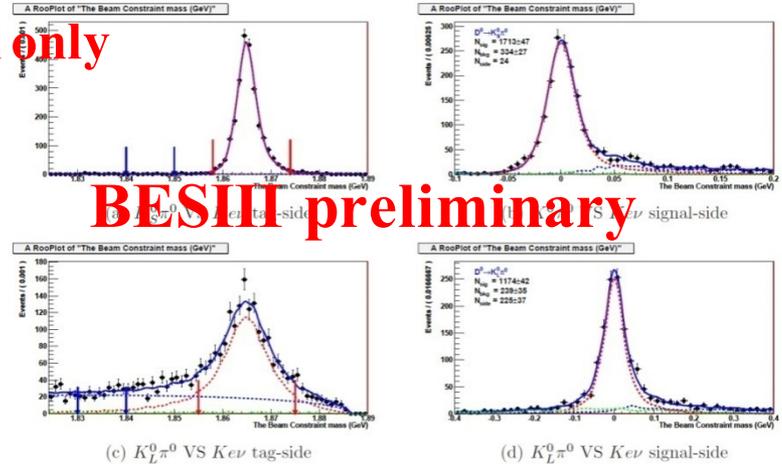
Branching fractions and asymmetries

Statistical only

$$R(D \rightarrow K_{S,L} + \pi's) = \frac{Br(D \rightarrow K_S \pi's) - Br(D \rightarrow K_L \pi's)}{Br(D \rightarrow K_S \pi's) + Br(D \rightarrow K_L \pi's)}$$

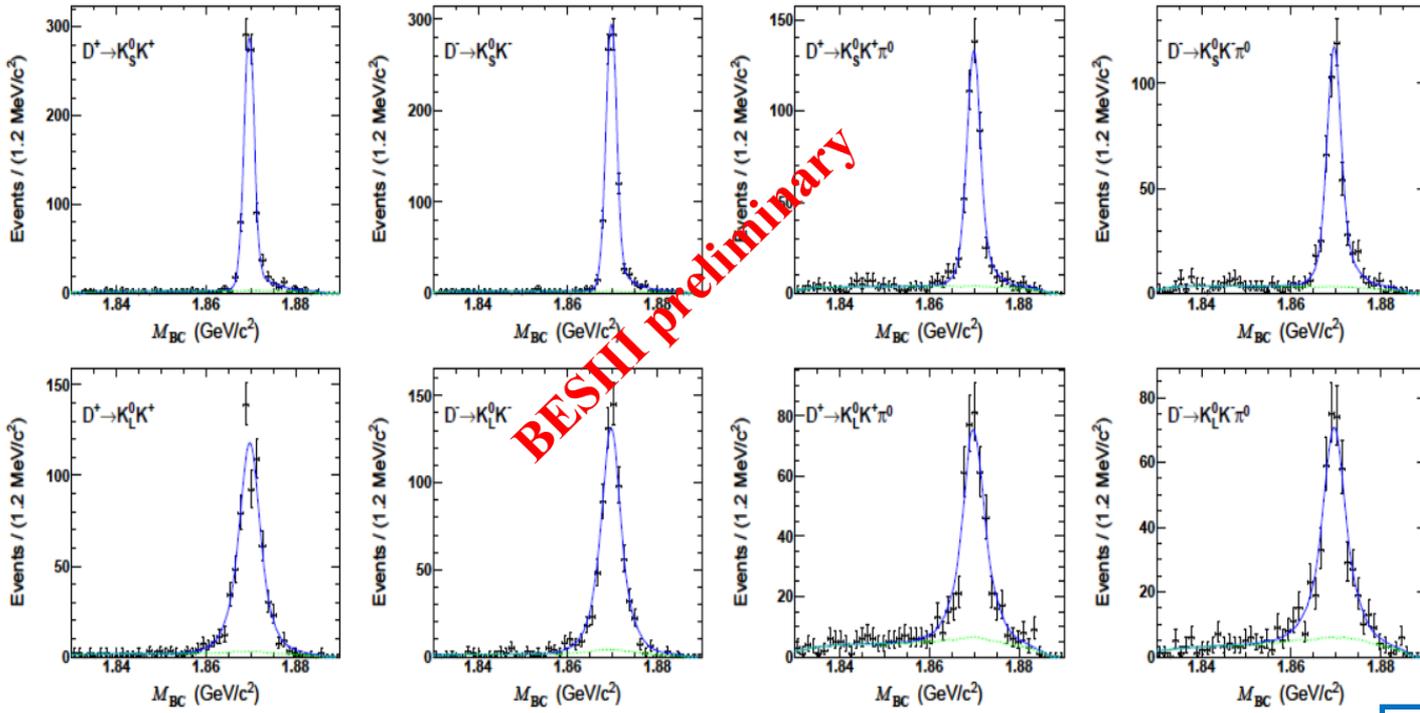
Table 10: Decay rates and the asymmetries of $D \rightarrow K_{S,L}^0 \pi^0$ and $D \rightarrow K_{S,L}^0 \pi^0 \pi^0$.

$D \rightarrow K_{S,L}^0 \pi^0$			
	$Br_{K_S \pi^0}(\%)$	$Br_{K_L \pi^0}(\%)$	$R(D \rightarrow K_{S,L} \pi^0)$
$K\pi$	1.208 ± 0.041	1.061 ± 0.038	0.0646 ± 0.0245
$K3\pi$	1.212 ± 0.037	0.985 ± 0.036	0.1035 ± 0.0237
$K\pi\pi^0$	1.251 ± 0.028	0.953 ± 0.029	0.1351 ± 0.0186
All	1.230 ± 0.020	0.991 ± 0.019	0.1077 ± 0.0125
$D \rightarrow K_{S,L}^0 \pi^0 \pi^0$			
	$Br_{K_S 2\pi^0}(\%)$	$Br_{K_L 2\pi^0}(\%)$	$R(D \rightarrow K_{S,L} 2\pi^0)$
$K\pi$	1.024 ± 0.049	1.299 ± 0.080	-0.1183 ± 0.0385
$K3\pi$	0.887 ± 0.043	1.097 ± 0.073	-0.1060 ± 0.0409
$K\pi\pi^0$	1.010 ± 0.036	1.158 ± 0.060	-0.0681 ± 0.0313
All	0.975 ± 0.024	1.175 ± 0.040	-0.0929 ± 0.0209



- $y_{CP} ((K_S \pi^0, K_L \pi^0) \text{ vs. } Kev) = (0.98 \pm 2.43)\%$

Absolute BFs and A_{CP} of $D^+ \rightarrow K_{S/L} K^+(\pi^0)$

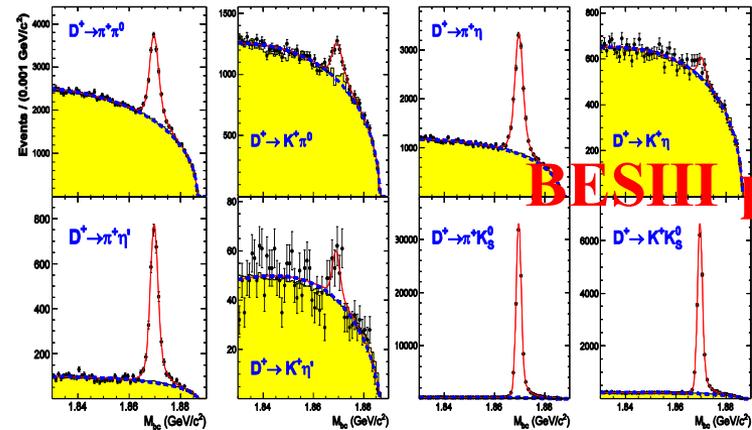
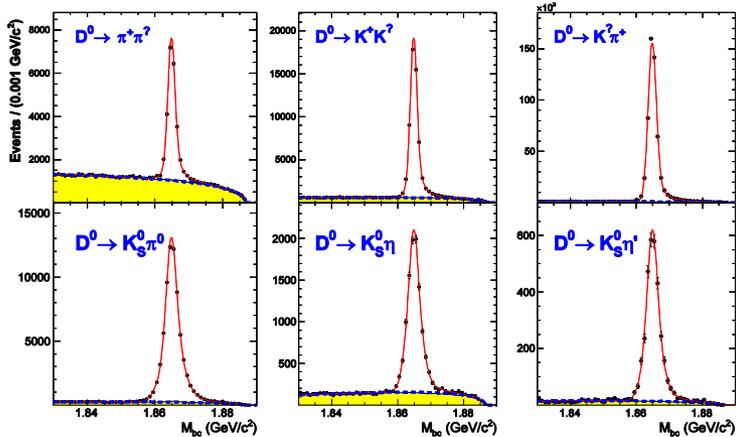


The first and second uncertainties are statistical and systematic

$$A_{CP} = \frac{\mathcal{B}(D^+) - \mathcal{B}(D^-)}{\mathcal{B}(D^+) + \mathcal{B}(D^-)}$$

Mode	$\mathcal{B}(D^+) (\times 10^{-3})$	$\mathcal{B}(D^-) (\times 10^{-3})$	$\bar{\mathcal{B}} (\times 10^{-3})$	$A_{CP} (\%)$
$K_S^0 K^\pm$	$3.01 \pm 0.12 \pm 0.10$	$3.10 \pm 0.12 \pm 0.10$	$3.06 \pm 0.09 \pm 0.10$	$-1.5 \pm 2.8 \pm 1.6$
$K_S^0 K^\pm \pi^0$	$5.23 \pm 0.28 \pm 0.24$	$5.09 \pm 0.29 \pm 0.22$	$5.16 \pm 0.21 \pm 0.23$	$1.4 \pm 4.0 \pm 2.4$
$K_L^0 K^\pm$	$3.13 \pm 0.14 \pm 0.13$	$3.32 \pm 0.15 \pm 0.13$	$3.23 \pm 0.11 \pm 0.13$	$-3.0 \pm 3.2 \pm 1.2$
$K_L^0 K^\pm \pi^0$	$5.17 \pm 0.30 \pm 0.21$	$5.26 \pm 0.30 \pm 0.20$	$5.22 \pm 0.22 \pm 0.21$	$-0.9 \pm 4.1 \pm 1.6$

BF measurements of some $D^{0(+)} \rightarrow PP$



BESIII preliminary

- ◆ The study of the hadronic decays of charmed D mesons is of great significance in the study of the strong and weak interactions in D decays.
- ◆ The analysis on $D \rightarrow PP$ modes will provide materials for the study of SU(3) breaking effect¹. And the observation of CP violation in D decay is commonly believed to be indications of new physics.
- ◆ $D^0 \rightarrow K^- \pi^+$ is an important normalization mode.
- ◆ Most of the D decays have been studied by CLEO in 2010², other measurements come from Belle³, BaBar⁴ and CDF⁵, etc.
- ◆ Some of the branching fractions (BFs) are not well established. With the 2.93 fb⁻¹ data taken at 3.773 GeV within BESIII, the results will help to improve these measurements.

Mode	$N_{\text{signal}}^{\text{net}}$	ϵ (%)	$\mathcal{B} \pm (\text{stat}) \pm (\text{sys})$	\mathcal{B}_{PDG}
$\pi^+ \pi^-$	21105 ± 249	66.03 ± 0.25	$(1.505 \pm 0.018 \pm 0.031) \times 10^{-3}$	$(1.421 \pm 0.025) \times 10^{-3}$
η	5438 ± 273	62.82 ± 0.32	$(4.229 \pm 0.020 \pm 0.087) \times 10^{-3}$	$(4.01 \pm 0.07) \times 10^{-3}$
$K^- \pi^+$	537745 ± 767	64.98 ± 0.09	$(3.896 \pm 0.006 \pm 0.073) \%$	$(3.93 \pm 0.04) \%$
$K_S^0 \pi^0$	66539 ± 302	38.06 ± 0.17	$(1.236 \pm 0.006 \pm 0.032) \%$	$(1.20 \pm 0.04) \%$
$K_S^0 \eta$	9532 ± 126	31.96 ± 0.14	$(5.149 \pm 0.068 \pm 0.134) \times 10^{-3}$	$(4.85 \pm 0.30) \times 10^{-3}$
$K_S^0 \eta'$	3007 ± 61	12.66 ± 0.08	$(9.562 \pm 0.197 \pm 0.379) \times 10^{-3}$	$(9.5 \pm 0.5) \times 10^{-3}$
$\pi^0 \pi^+$	10108 ± 267	48.98 ± 0.34	$(1.259 \pm 0.033 \pm 0.025) \times 10^{-3}$	$(1.24 \pm 0.06) \times 10^{-3}$
$\pi^0 K^+$	1834 ± 168	51.52 ± 0.42	$(2.171 \pm 0.198 \pm 0.060) \times 10^{-4}$	$(1.89 \pm 0.25) \times 10^{-4}$
$\eta \pi^+$	11636 ± 215	46.96 ± 0.25	$(3.790 \pm 0.070 \pm 0.075) \times 10^{-3}$	$(3.66 \pm 0.22) \times 10^{-3}$
ηK^+	439 ± 72	48.21 ± 0.31	$(1.393 \pm 0.228 \pm 0.124) \times 10^{-4}$	$(1.12 \pm 0.18) \times 10^{-4}$
$\eta' \pi^+$	3088 ± 83	21.49 ± 0.18	$(5.122 \pm 0.140 \pm 0.210) \times 10^{-3}$	$(4.84 \pm 0.31) \times 10^{-3}$
$\eta' K^+$	87 ± 25	22.39 ± 0.22	$(1.377 \pm 0.428 \pm 0.202) \times 10^{-4}$	$(1.83 \pm 0.23) \times 10^{-4}$
$K_S^0 \pi^+$	93884 ± 352	51.38 ± 0.18	$(1.591 \pm 0.006 \pm 0.033) \times 10^{-2}$	$(1.53 \pm 0.06) \times 10^{-2}$
$K_S^0 K^+$	17704 ± 151	48.45 ± 0.14	$(3.183 \pm 0.028 \pm 0.065) \times 10^{-3}$	$(2.95 \pm 0.15) \times 10^{-3}$

$$\mathcal{B} = \frac{N_{\text{net}}^{\text{signal}}}{2 \cdot N_{D^0 \bar{D}^0} (D^+ D^-) \cdot \epsilon}, N_{D^0 \bar{D}^0} = (10,621 \pm 29_{\text{stat}}) \times 10^3, N_{D^+ D^-} = (8,296 \pm 31_{\text{stat}}) \times 10^3$$

quoted from Derrick's talk given at APS2014

The $\mathcal{B}(D^0 \rightarrow K^- \pi^+)$ has been corrected by the PDG value of $\mathcal{B}(D^0 \rightarrow K^+ \pi^-)$.

For $D^0 \rightarrow K_S^0 \eta$, $D^+ \rightarrow \pi^0 \pi^+$, $D^+ \rightarrow \eta \pi^+$, $D^+ \rightarrow \eta' \pi^+$, $D^+ \rightarrow K_S^0 \pi^+$ and $D^+ \rightarrow K_S^0 K^+$, it shows better precision than the present values.

Λ_c^+ decays

Absolute BFs of Λ_c^+ decays

- Λ_c^+ was observed in 1979
- Before 2014, all decays of Λ_c^+ are measured relative to $\Lambda_c^+ \rightarrow pK^-\pi^+$, which suffer large error of 25%, with high energy data. No absolute measurement using data produced at Λ_c^+ pair threshold
- Sum of BF of known decays Λ_c^+ is only about 60%
- In 2014, Belle reported improved measurement of $B[\Lambda_c^+ \rightarrow pK^-\pi^+]$, with a precision of ~5%

Λ_c^+ DECAY MODES	Fraction (Γ_i/Γ)	Scale factor/ Confidence level	P (MeV/c)
Hadronic modes with a ρ: $S = -1$ final states			
$\rho\bar{K}^0$	(2.3 \pm 0.6) %		873
$\rho K^-\pi^+$	[a] (5.0 \pm 1.3) %		823
$\rho\bar{K}^*(892)^0$	[b] (1.6 \pm 0.5) %		685
$\Delta(1232)^{++}K^-$	(8.6 \pm 3.0) $\times 10^{-3}$		710
$\Lambda(1520)\pi^+$	[b] (1.8 \pm 0.6) %		627
$\rho K^-\pi^+$ nonresonant	(2.8 \pm 0.8) %		823
$\rho\bar{K}^0\pi^0$	(3.3 \pm 1.0) %		823
$\rho\bar{K}^0\eta$	(1.2 \pm 0.4) %		568
Hadronic modes with a hyperon: $S = -1$ final states			
$\Lambda\pi^+$	(1.07 \pm 0.28) %		864
$\Lambda\pi^+\pi^0$	(3.6 \pm 1.3) %		844
$\Lambda\rho^+$	< 5 %	CL=95%	636
$\Lambda\pi^+\pi^+\pi^-$	(2.6 \pm 0.7) %		807
$\Sigma(1385)^+\pi^+\pi^-, \Sigma^{*+} \rightarrow$	(7 \pm 4) $\times 10^{-3}$		688
$\Lambda\pi^+$			
$\Sigma(1385)^-\pi^+\pi^+, \Sigma^{*-} \rightarrow$	(5.5 \pm 1.7) $\times 10^{-3}$		688
$\Lambda\pi^-\rho^0$			
$\Lambda\pi^+\rho^0$	(1.1 \pm 0.5) %		524
$\Sigma(1385)^+\rho^0, \Sigma^{*+} \rightarrow \Lambda\pi^+$	(3.7 \pm 3.1) $\times 10^{-3}$		363
$\Lambda\pi^+\pi^+\pi^-\pi^0$ nonresonant	< 8 $\times 10^{-3}$	CL=90%	807
$\Lambda\pi^+\pi^+\pi^-\pi^0$ total	(1.8 \pm 0.8) %		757
$\Lambda\pi^+\eta$	[b] (1.8 \pm 0.6) %		691
$\Sigma(1385)^+\eta$	[b] (8.5 \pm 3.3) $\times 10^{-3}$		570
$\Lambda\pi^+\omega$	[b] (1.2 \pm 0.5) %		517
$\Lambda\pi^+\pi^+\pi^-\pi^0$, no η or ω	< 7 $\times 10^{-3}$	CL=90%	757
$\Lambda K^+\bar{K}^0$	(4.7 \pm 1.5) $\times 10^{-3}$	S=1.2	443
$\Xi(1690)^0 K^+, \Xi^{*0} \rightarrow \Lambda\bar{K}^0$	(1.3 \pm 0.5) $\times 10^{-3}$		286
$\Sigma^0\pi^+$	(1.05 \pm 0.28) %		825
$\Sigma^+\pi^0$	(1.00 \pm 0.34) %		827
$\Sigma^+\eta$	(5.5 \pm 2.3) $\times 10^{-3}$		713
$\Sigma^+\pi^+\pi^-$	(3.6 \pm 1.0) %		804
$\Sigma^+\rho^0$	< 1.4 %	CL=95%	575
$\Sigma^-\pi^+\pi^+$	(1.7 \pm 0.5) %		799
$\Sigma^0\pi^+\pi^0$	(1.8 \pm 0.8) %		803
$\Sigma^0\pi^+\pi^+\pi^-$	(8.3 \pm 3.1) $\times 10^{-3}$		763
$\Sigma^+\pi^+\pi^-\pi^0$	—		767
$\Sigma^+\omega$	[b] (2.7 \pm 1.0) %		569
Semileptonic modes			
$\Lambda\ell^+\nu_\ell$	[c] (2.0 \pm 0.6) %		871
$\Lambda e^+\nu_e$	(2.1 \pm 0.6) %		871
$\Lambda\mu^+\nu_\mu$	(2.0 \pm 0.7) %		867
Inclusive modes			
e^+ anything	(4.5 \pm 1.7) %		—
$p e^+$ anything	(1.8 \pm 0.9) %		—
p anything	(50 \pm 16) %		—

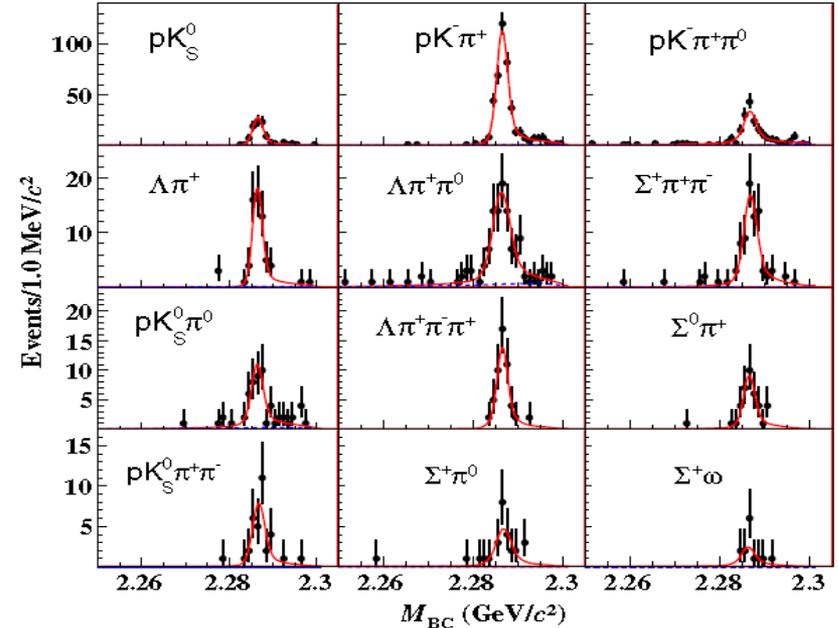
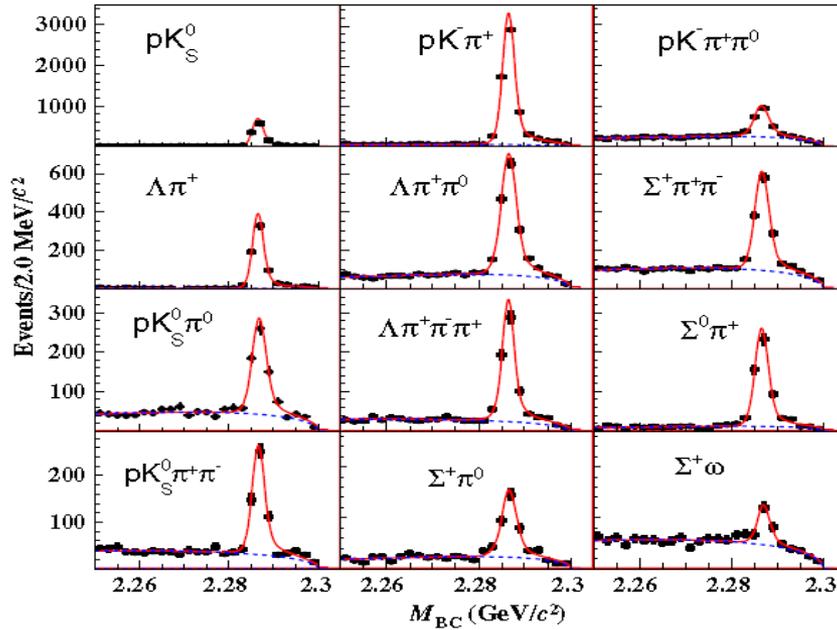
Systematic studies of Λ_c^+ , search for new decays, absolute BF measurements are important to fully explore the Λ_c^+ decay mechanisms

Significantly improved BFs of $\Lambda_c^+ \rightarrow$ decays

PRL116(2016)052001

ST: ~15000

DT: ~1000



$$N_j^{ST} = N_{\Lambda_c^+ \bar{\Lambda}_c^-} \mathcal{B}_j \epsilon_j$$

$$N_{ij}^{DT} = N_{\Lambda_c^+ \bar{\Lambda}_c^-} \mathcal{B}_i \mathcal{B}_j \epsilon_{ij}$$

$$\mathcal{B}_i = \frac{N_{ij}^{DT} \epsilon_j}{N_j^{ST} \epsilon_{ij}}$$

$$N_{i-}^{DT} = N_{\Lambda_c^+ \bar{\Lambda}_c^-} \sum_j \mathcal{B}_i \mathcal{B}_j \epsilon_{i-}^{DT}$$

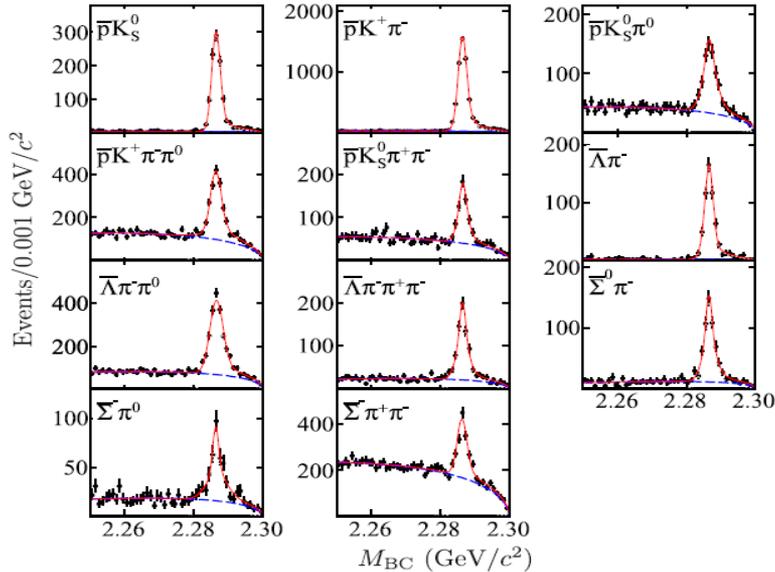
$$\epsilon_{i-}^{DT} \equiv [\sum_j (\mathcal{B}_j \epsilon_{ij}) / \sum_j \mathcal{B}_j]$$

Mode	This work (%)	PDG (%)
pK_S^0	$1.52 \pm 0.08 \pm 0.03$	1.15 ± 0.30
$pK^- \pi^+$	$5.84 \pm 0.27 \pm 0.23$	5.0 ± 1.3
$pK_S^0 \pi^0$	$1.87 \pm 0.13 \pm 0.05$	1.65 ± 0.50
$pK_S^0 \pi^+ \pi^-$	$1.53 \pm 0.11 \pm 0.09$	1.30 ± 0.35
$pK^- \pi^+ \pi^0$	$4.53 \pm 0.23 \pm 0.30$	3.4 ± 1.0
$\Lambda \pi^+$	$1.24 \pm 0.07 \pm 0.03$	1.07 ± 0.28
$\Lambda \pi^+ \pi^0$	$7.01 \pm 0.37 \pm 0.19$	3.6 ± 1.3
$\Lambda \pi^+ \pi^- \pi^+$	$3.81 \pm 0.24 \pm 0.18$	2.6 ± 0.7
$\Sigma^0 \pi^+$	$1.27 \pm 0.08 \pm 0.03$	1.05 ± 0.28
$\Sigma^+ \pi^0$	$1.18 \pm 0.10 \pm 0.03$	1.00 ± 0.34
$\Sigma^+ \pi^+ \pi^-$	$4.25 \pm 0.24 \pm 0.20$	3.6 ± 1.0
$\Sigma^+ \omega$	$1.56 \pm 0.20 \pm 0.07$	2.7 ± 1.0

**Better
precision for
most channels**

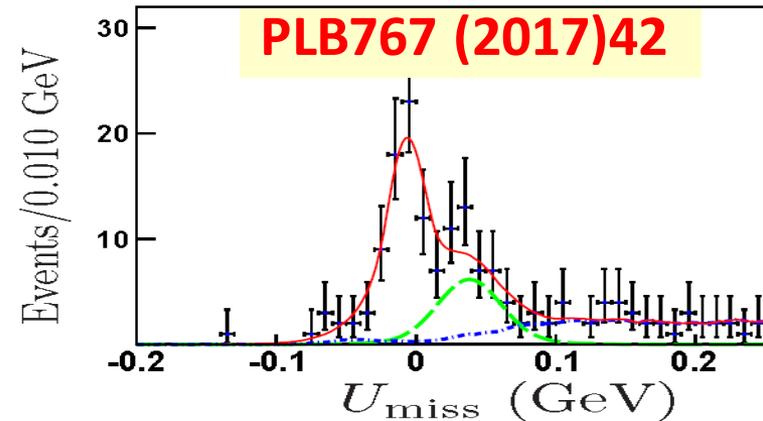
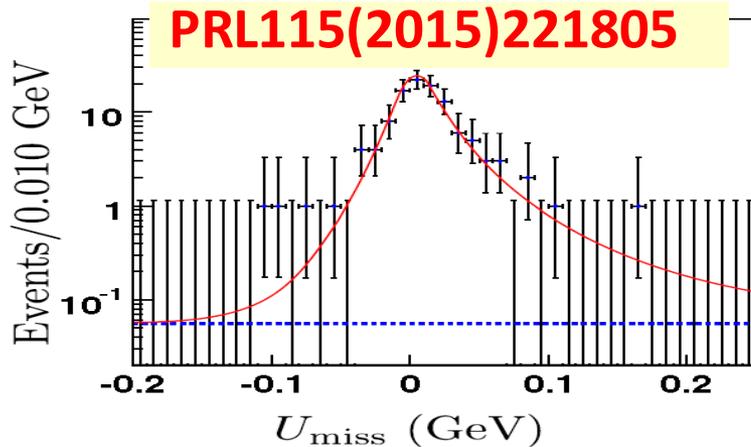
First absolute BF's of $\Lambda_c^+ \rightarrow \Lambda l^+ \nu$

Theory: (1.4-9.2)%



Theoretical Models	predicated branching fraction for $\Lambda_c^+ \rightarrow \Lambda e^+ \nu_e$
MBM [1]	1.9%
NRQM [1]	2.6%
SU(4)-symmetry limit [2]	9.2%
RSQM [3]	4.4%
QCM [4]	5.62%
SQM [5]	1.96%
NRQM2 [6]	2.15%
NRQM3 [7]	1.42%
QCD SR1 [8]	$(3.0 \pm 0.9)\%$
QCD SR2 [9]	$(2.6 \pm 0.4)\%$
QCD SR3 [9]	$(5.8 \pm 1.5)\%$
STSR [10]	2.22% for $\Lambda_c^+ \rightarrow \Lambda l^+ \nu_l$
BTNR [10]	1.58% for $\Lambda_c^+ \rightarrow \Lambda l^+ \nu_l$
HO SR [10]	4.72% for $\Lambda_c^+ \rightarrow \Lambda l^+ \nu_l$
HONR [10]	4.2% for $\Lambda_c^+ \rightarrow \Lambda l^+ \nu_l$
LCSR _s [11]	$(3.0 \pm 0.3)\%$ for $\Lambda_c^+ \rightarrow \Lambda l^+ \nu_l$ (CZ-type)
PDG 2014 [14]	$(2.1 \pm 0.6)\%$
BESIII	$(3.63 \pm 0.38 \pm 0.20)\%$

3 fb⁻¹ help to explore FF studies



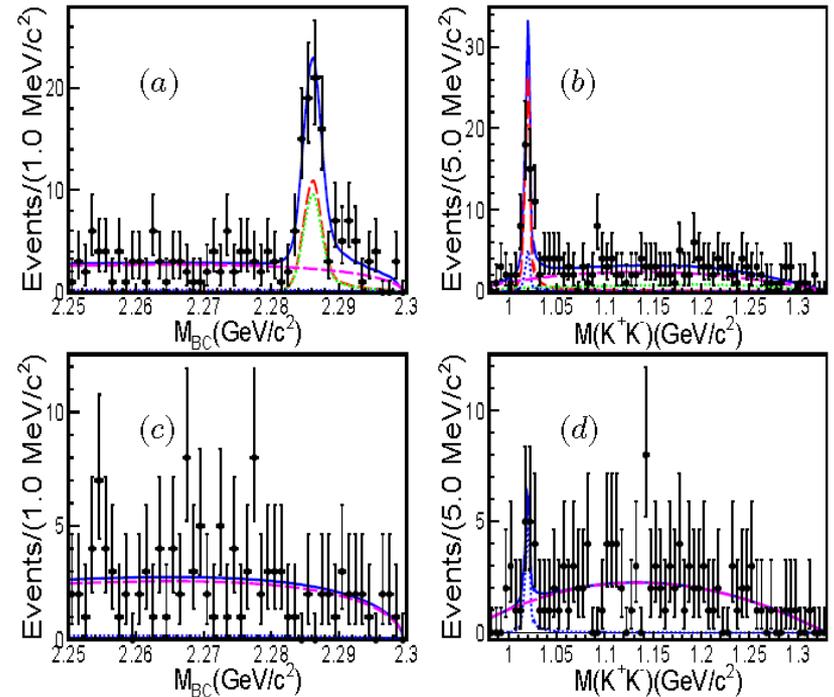
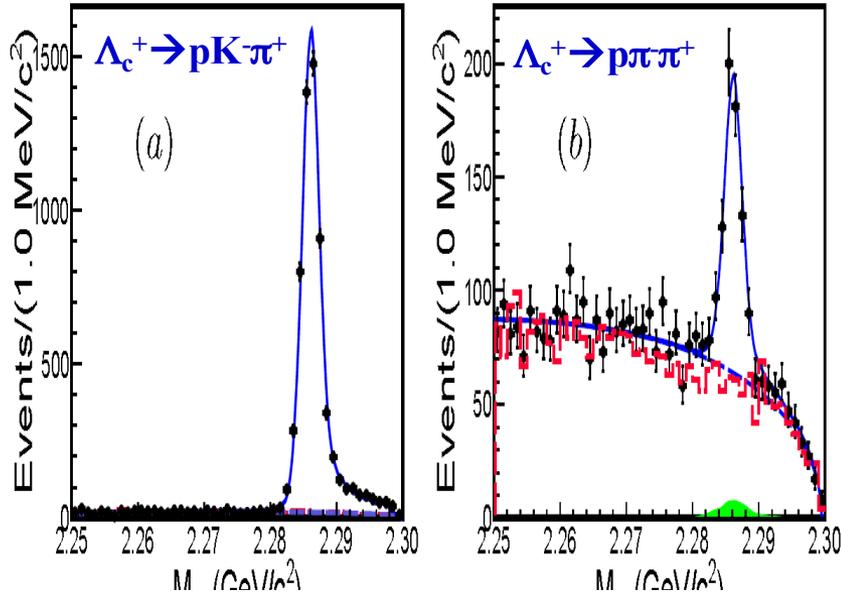
$$B[\Lambda_c^+ \rightarrow \Lambda e^+ \nu_e] = (3.63 \pm 0.38 \pm 0.20)\%$$

$$B[\Lambda_c^+ \rightarrow \Lambda \mu^+ \nu_\mu] = (3.49 \pm 0.46 \pm 0.26)\%$$

$$\Gamma[\Lambda_c^+ \rightarrow \Lambda \mu^+ \nu_\mu] / \Gamma[\Lambda_c^+ \rightarrow \Lambda e^+ \nu_e] = 0.96 \pm 0.16 \pm 0.04$$

SCS decays $\Lambda_c^+ \rightarrow pK^+K^-$ and $p\pi^+\pi^-$

PRL117(2016)232002

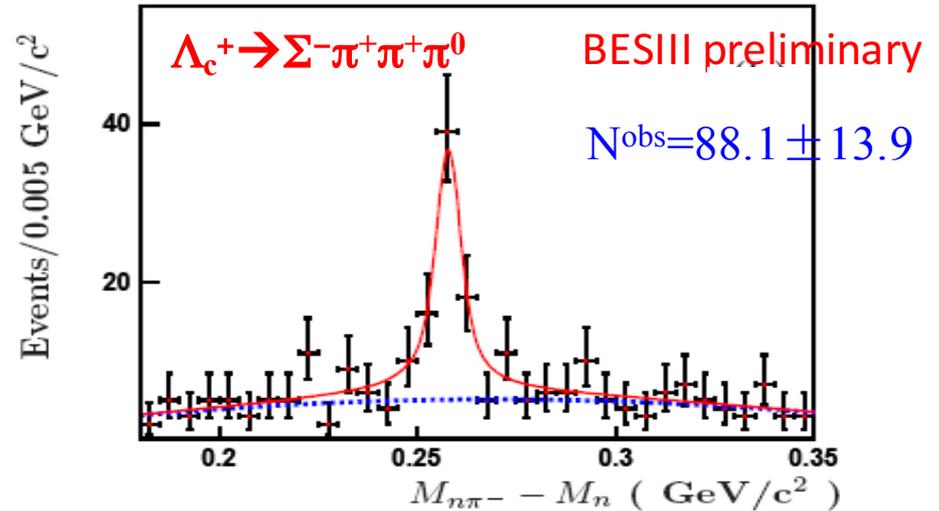
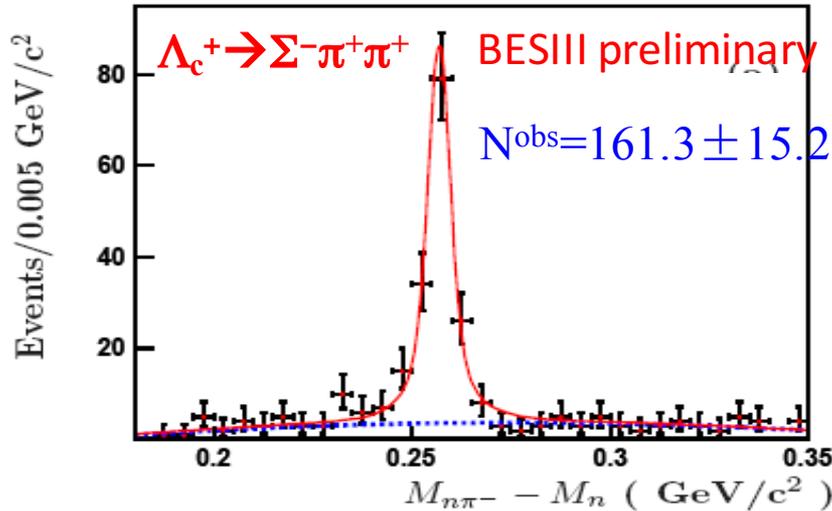


These help to distinguish predictions from different theoretical models and understand contributions from factorizable effects

Decay modes	$\mathcal{B}_{\text{mode}}/\mathcal{B}_{\text{ref.}}$	$\mathcal{B}_{\text{mode}}$	$\mathcal{B}(\text{PDG})$
$\Lambda_c^+ \rightarrow p\pi^+\pi^-$	$(6.70 \pm 0.48 \pm 0.25) \times 10^{-2}$	$(3.91 \pm 0.28 \pm 0.15 \pm 0.24) \times 10^{-3}$	$(3.5 \pm 2.0) \times 10^{-3}$
$\Lambda_c^+ \rightarrow p\phi$	$(1.81 \pm 0.33 \pm 0.13) \times 10^{-2}$	$(1.06 \pm 0.19 \pm 0.08 \pm 0.06) \times 10^{-3}$	$(8.2 \pm 2.7) \times 10^{-4}$
$\Lambda_c^+ \rightarrow pK^+K^-$ (non- ϕ)	$(9.36 \pm 2.22 \pm 0.71) \times 10^{-3}$	$(5.47 \pm 1.30 \pm 0.41 \pm 0.33) \times 10^{-4}$	$(3.5 \pm 1.7) \times 10^{-4}$

Observation of $\Lambda_c^+ \rightarrow \Sigma^- \pi^+ \pi^+ \pi^0$

More studies of decays containing neutron



Preliminary results :

$$B[\Lambda_c^+ \rightarrow \Sigma^- \pi^+ \pi^+] = (1.81 \pm 0.17)\%$$

$$B[\Lambda_c^+ \rightarrow \Sigma^- \pi^+ \pi^+ \pi^0] = (2.11 \pm 0.33)\% \quad \text{[First observation]}$$

where the errors are statistical only. The sources of the systematic errors arise mainly from the systematic uncertainties in PID, tracking, π^0 efficiency, fitting, MC statistics and number of $\bar{\Lambda}_c^-$ tags. The total systematic errors are estimated to be about 5%.

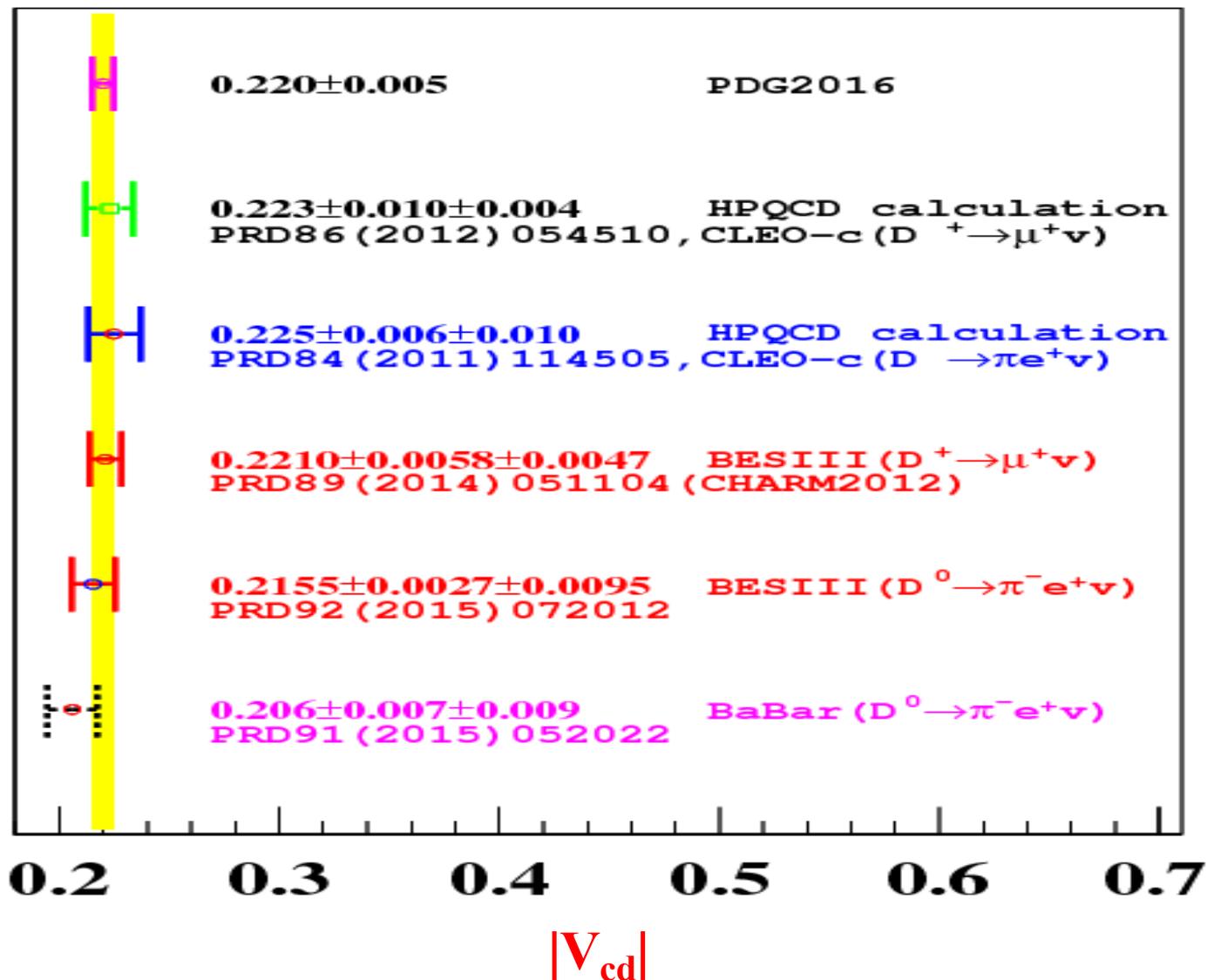
The measured branching fraction for $\Lambda_c^+ \rightarrow \Sigma^- \pi^+ \pi^+$ is consistent with and more precise than $B[\Lambda_c^+ \rightarrow \Sigma^- \pi^+ \pi^+] = (2.3 \pm 0.4)\%$ in PDG2015.

Summary

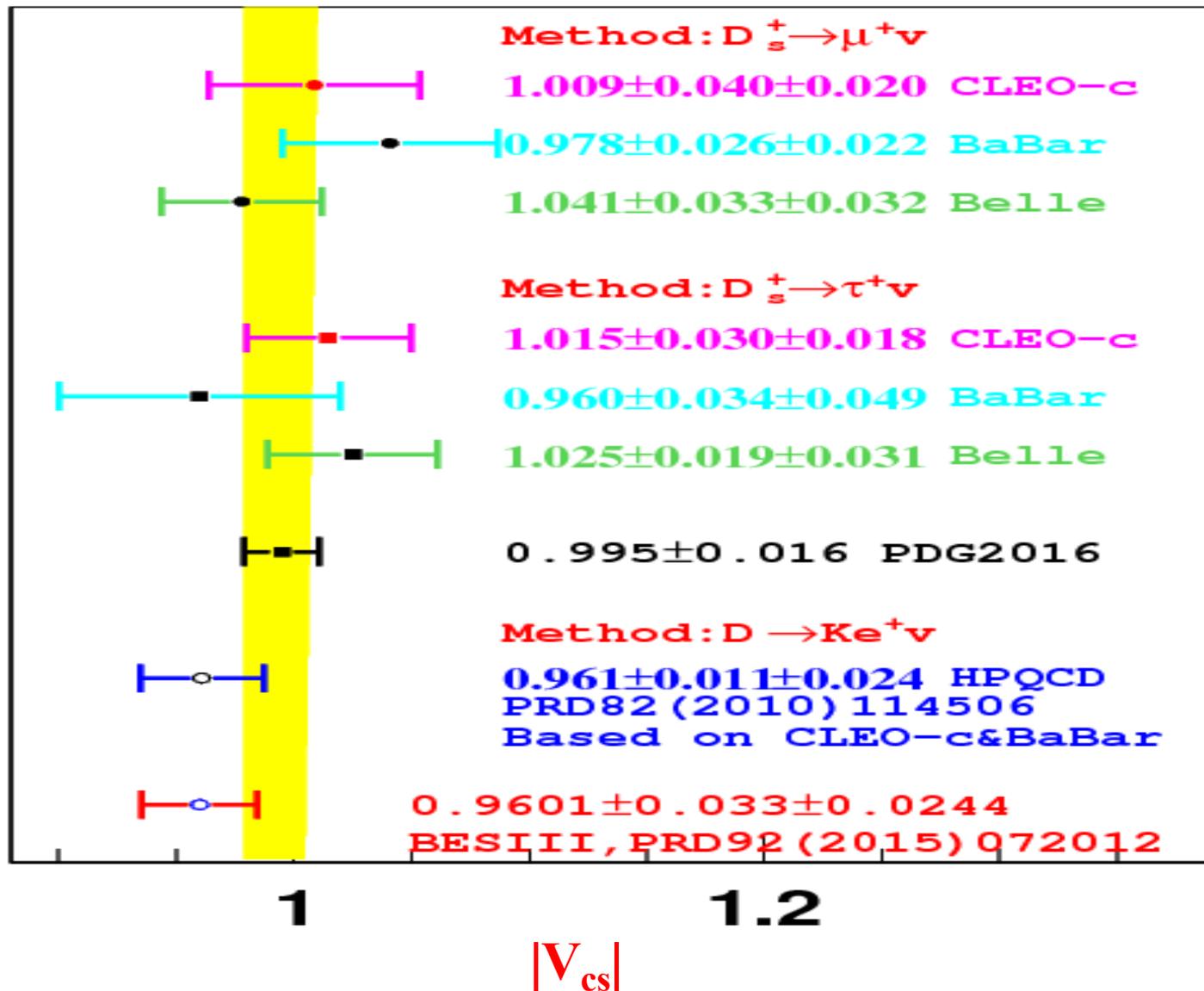
- With 2.93, 0.482, 0.567 fb⁻¹ data taken at 3.773, 4.009 and 4.6 GeV, BESIII have studied leptonic related and hadronic decays of D, first measurement of the absolute BFs of Λ_c^+
- Improved measurements of decay constant f_{D^+} and form factor $f_+^{D \rightarrow K(\pi)}(q^2)$, which are important to test and calibrate LQCD calculations
- Improved measurements of CKM matrix element $|V_{cs(d)}|$, which are important to test the CKM matrix unitarity
- Preliminary of strong phase in $D^0 \rightarrow K_S \pi^+ \pi^-$
- More results with better precision are expected with more data
- About 3 fb⁻¹ data at 4.18 GeV has been taken in 2016, measurement of $f_{D_{S^+}}$ and $|V_{cs}|$ by $D_S^+ \rightarrow l^+ \nu$, FF studies of $D_S^+ \rightarrow \eta^{(\prime)} e^+ \nu$ are expected in the near future

Backup

Comparison of $|V_{cd}|$

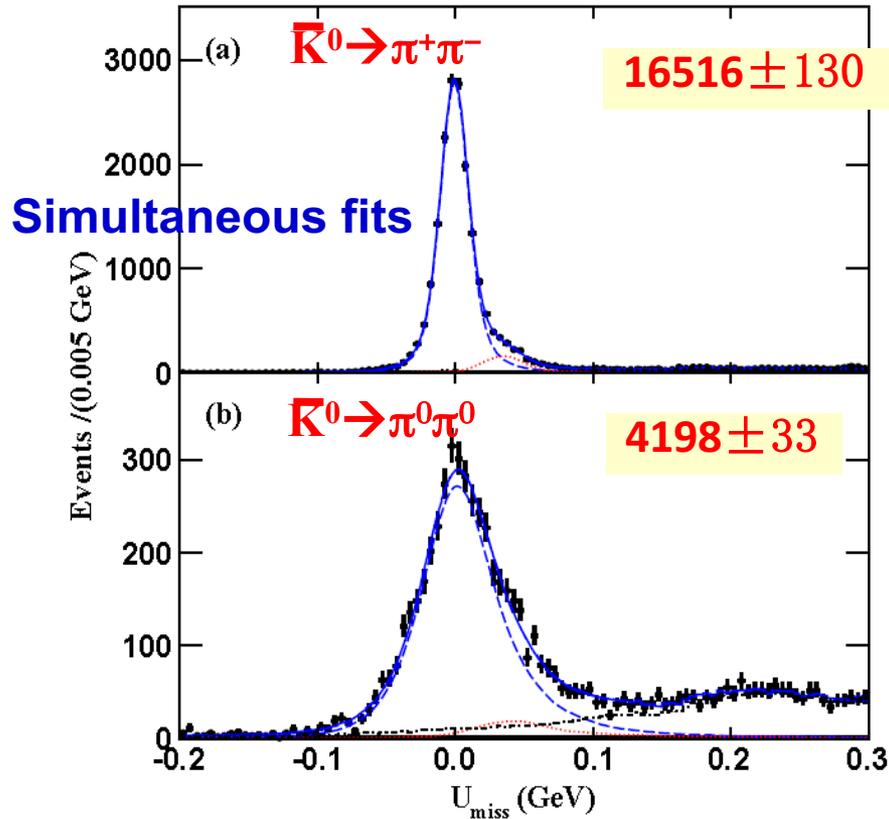


Comparison of $|V_{cs}|$

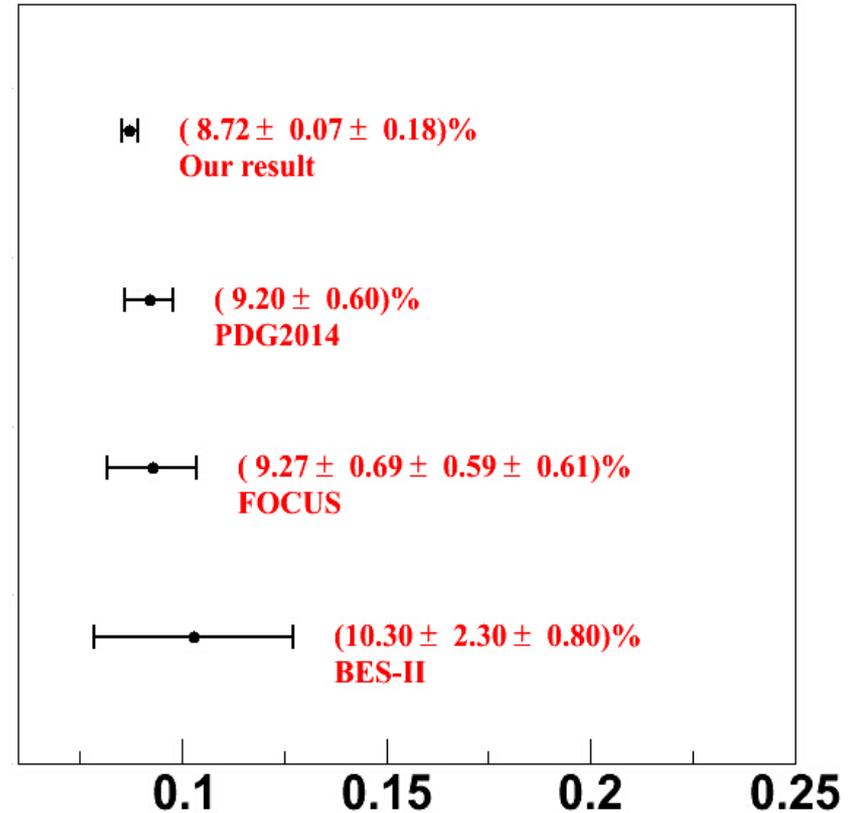


Improved BF for $D^+ \rightarrow \bar{K}^0 \mu^+ \nu$

With 6 dominant D^- single tag



EPJC76(2016)369



Taking $B[D^0 \rightarrow K^- \mu^+ \nu]$
and $B[D^+ \rightarrow \bar{K}^0 e^+ \nu]$
from the PDG as input

$$\frac{\Gamma[D^0 \rightarrow K^- \mu^+ \nu]}{\Gamma[D^+ \rightarrow \bar{K}^0 \mu^+ \nu]} = 0.963 \pm 0.044$$

$$\frac{\Gamma[D^+ \rightarrow \bar{K}^0 \mu^+ \nu]}{\Gamma[D^+ \rightarrow \bar{K}^0 e^+ \nu]} = 0.988 \pm 0.033$$

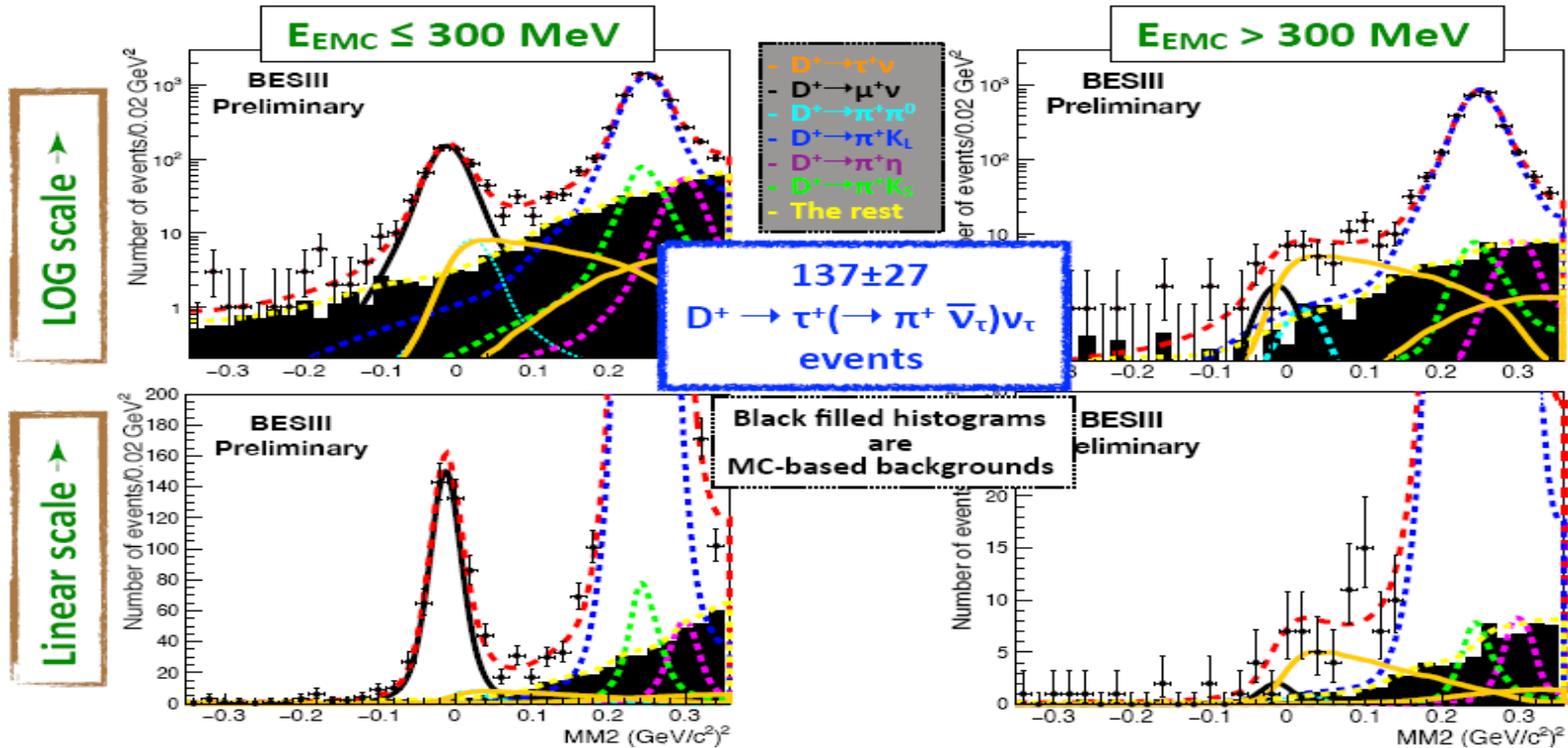
Support isospin conservation in
these two decays within errors

Consistent with theory
prediction 0.97 within error

Evidence for $D^+ \rightarrow \tau^+(\pi^+ \nu) \nu$ (4σ)

11

Fitting to DATA



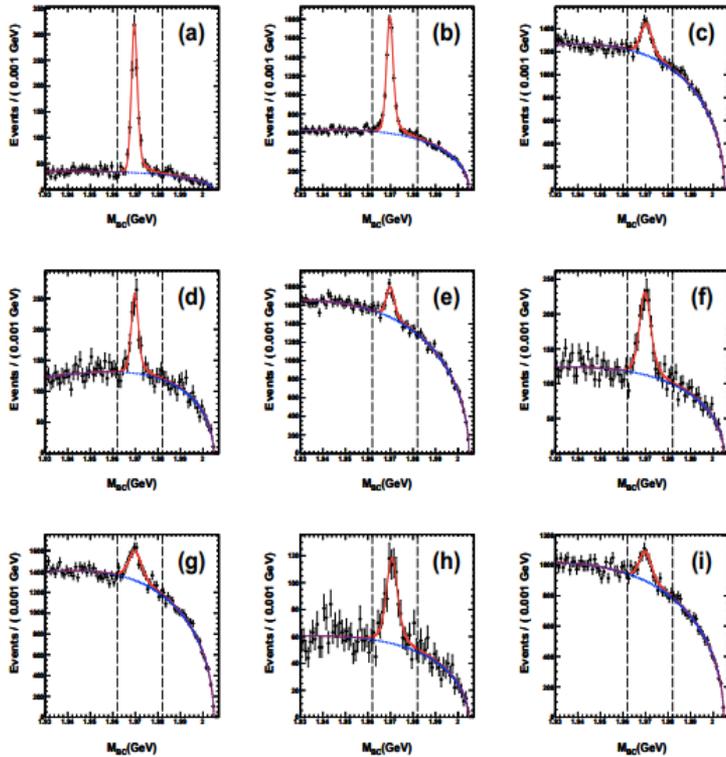
$$B[D^+ \rightarrow \tau^+ \nu] = (1.20 \pm 0.24_{\text{stat.}}) \times 10^{-3}$$

$$R \equiv \frac{\Gamma(D^+ \rightarrow \tau^+ \nu)}{\Gamma(D^+ \rightarrow \mu^+ \nu)} = \frac{m_{\tau^+}^2 \left(1 - \frac{m_{\tau^+}^2}{M_{D^+}^2}\right)^2}{m_{\mu^+}^2 \left(1 - \frac{m_{\mu^+}^2}{M_{D^+}^2}\right)^2}$$

SM prediction: 2.66 ± 0.01

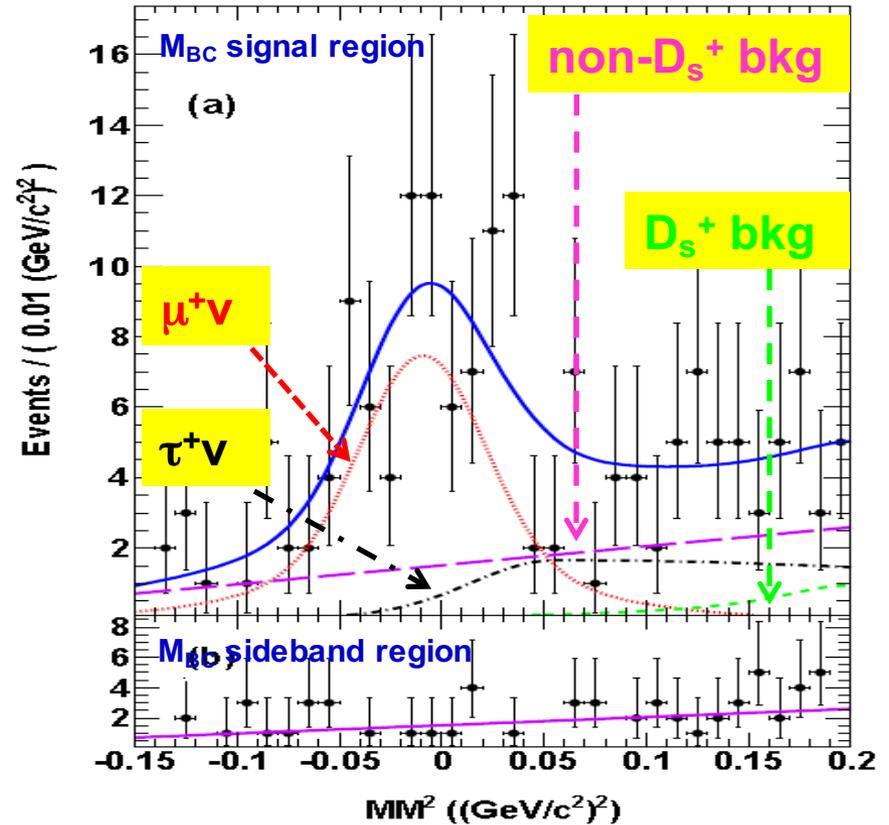
BESIII: 3.21 ± 0.64

$f_{D_{S^+}}$ at 4.009 GeV



$$N_{D_{S^+}^{tag}} = 15127 \pm 312$$

PRD94(2016)072004



$$B[D_{S^+} \rightarrow \mu^+ \nu] = (0.495 \pm 0.067 \pm 0.026)\%$$

$$B[D_{S^+} \rightarrow \tau^+ \nu] = (4.83 \pm 0.65 \pm 0.26)\%$$

$$f_{D_{S^+}} = (241.0 \pm 16.3 \pm 6.6) \text{ MeV}$$

Search for $D^{0(+)} \rightarrow a_0(980)^{-(-)} e^+ \nu$

- Explore the nontrivial internal structure of light hadron mesons, traditional qqbar states, tetra quark system.
- With chiral unitarity approach in the coupled channels, BF is predicted to be order of $5(6) \times 10^{-5}$ for $D^{0(+)}$ decays
- Improve understanding of classification of light scalar mesons

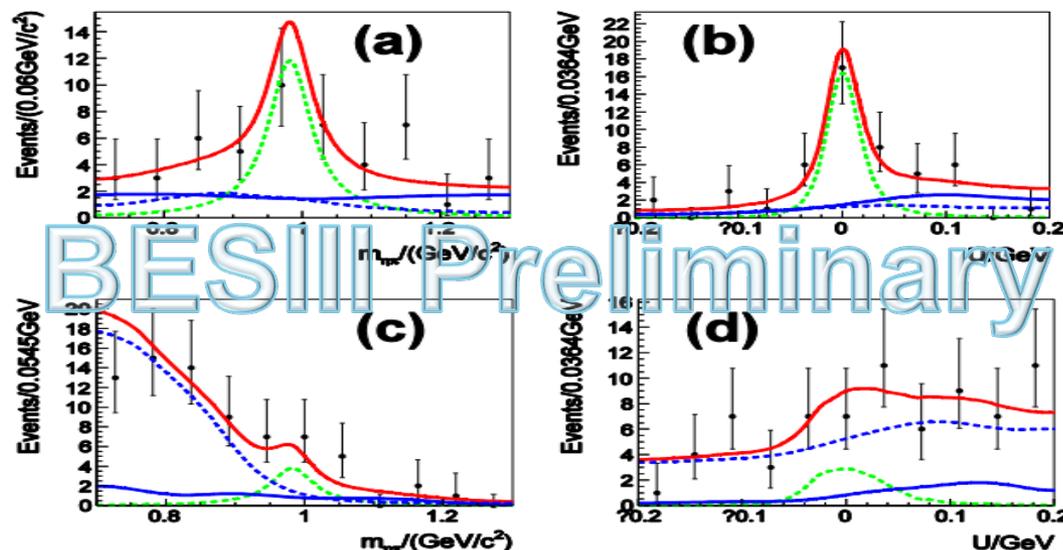
$$R \equiv \frac{B(D^+ \rightarrow f_0 l^+ \nu) + B(D^+ \rightarrow \sigma l^+ \nu)}{B(D^+ \rightarrow a_0 l^+ \nu)}$$

R=1(3) if traditional qqbar (tetra quark) system

$$\begin{aligned} \odot B(D^0 \rightarrow a_0(980)^- e^+ \nu_e) \times B(a_0(980)^- \rightarrow \eta \pi^-) \\ = (1.12_{-0.28}^{+0.31}(\text{stat}) \pm 0.10(\text{syst})) \times 10^{-4} \end{aligned}$$

$$\begin{aligned} \odot B(D^+ \rightarrow a_0(980)^0 e^+ \nu_e) \times B(a_0(980)^0 \rightarrow \eta \pi^0) \\ = (1.47_{-0.59}^{+0.73}(\text{stat}) \pm 0.14(\text{syst})) \times 10^{-4} \end{aligned}$$

With 3(6) dominant $D^{0(-)}$ single tag



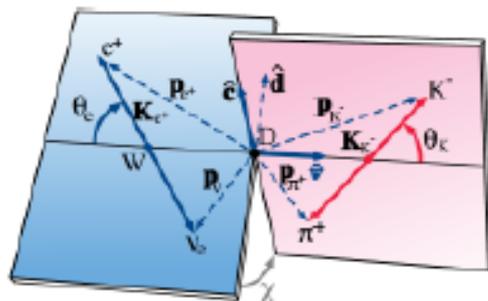
5.9 σ

$$\odot B(D^+ \rightarrow a_0(980)^0 e^+ \nu_e) \times B(a_0(980)^0 \rightarrow \eta \pi^0)$$

$< 2.7 \times 10^{-4}$ @ 90% C.L.

3.0 σ

Study of $D \rightarrow Ve^+\nu$



- $m^2 = (p_{\pi^+} + p_{K^-})^2$

- $\cos(\theta_K) = \frac{\hat{v} \cdot \mathbf{K}_{K^-}}{|\mathbf{K}_{K^-}|}$

- $\cos(\chi) = \hat{c} \cdot \hat{d}$

- $q^2 = (p_{e^+} + p_{\nu_e})^2$

- $\cos(\theta_e) = -\frac{\hat{v} \cdot \mathbf{K}_{e^+}}{|\mathbf{K}_{e^+}|}$

- $\sin(\chi) = (\hat{c} \times \hat{v}) \cdot \hat{d}$

Decay rate depend on **5 variables** and **3 form factors**

$$d^5\Gamma = \frac{G_F^2 |V_{cs}|^2}{(4\pi)^6 m_D^2} X \beta \mathcal{I}(m^2, q^2, \theta_K, \theta_e, \chi) dm^2 dq^2 d\cos(\theta_K) d\cos(\theta_e) d\chi$$

- $X = p_{K\pi} m_D$, $p_{K\pi}$ is the momentum of the $K\pi$ system in the D rest frame
- $\beta = 2p^*/m$, p^* is the breakup momentum of the $K\pi$ system in its rest frame
- \mathcal{I} can be expressed in terms of helicity amplitudes $H_{0,\pm}$:

$$H_0(q^2) = \frac{1}{2m_q} \left[(m_D^2 - m^2 - q^2)(m_D + m)A_1(q^2) - 4 \frac{m_D^2 p_{K\pi}^2}{m_D + m} A_2(q^2) \right]$$

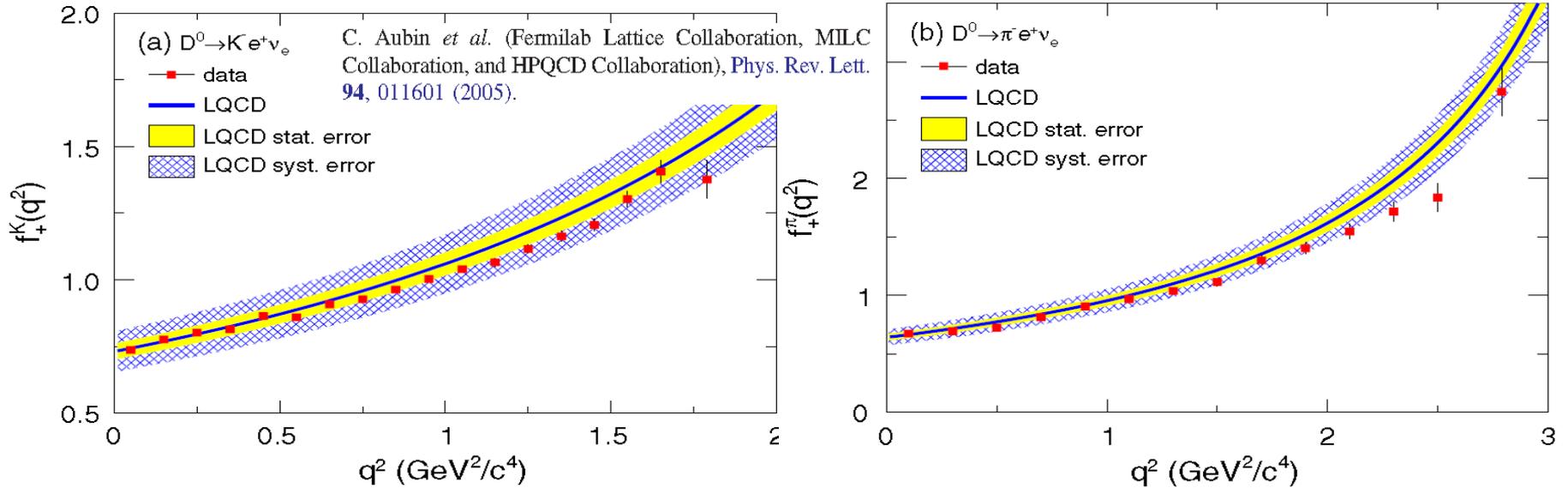
$$H_{\pm}(q^2) = (m_D + m)A_1(q^2) \mp \frac{2m_D p_{K\pi}}{m_D + m} V(q^2)$$

- Vector form factor: $V(q^2) = \frac{V(0)}{1 - q^2/m_V^2}$; or: FF ratio $r_V = V(0)/A_1(0)$

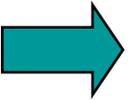
- Axial-vector form factor: $A_1(q^2) = \frac{A_1(0)}{1 - q^2/m_A^2}$, $A_2(q^2) = \frac{A_2(0)}{1 - q^2/m_A^2}$; or: FF ratio $r_2 = A_2(0)/A_1(0)$

Calibration of LQCD

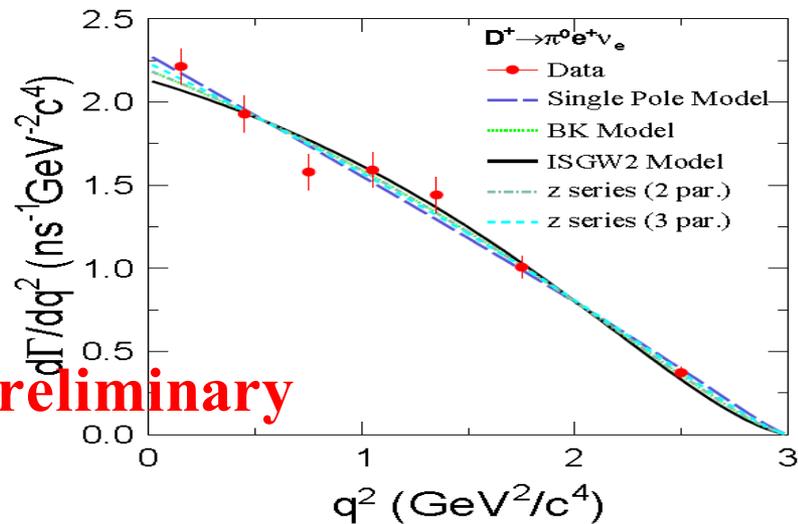
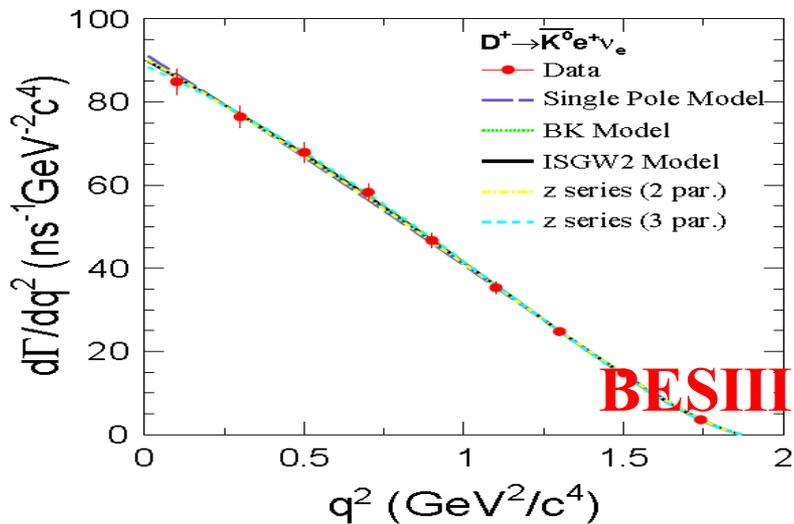
PRD92(2015)072012



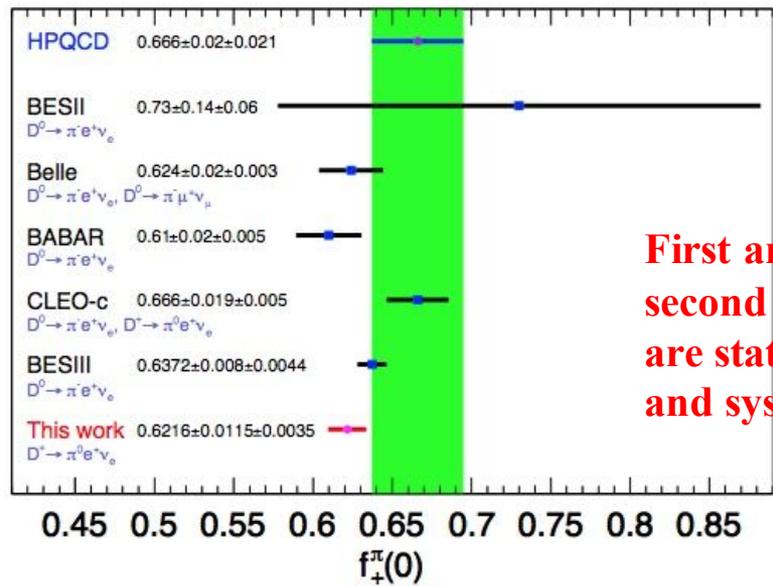
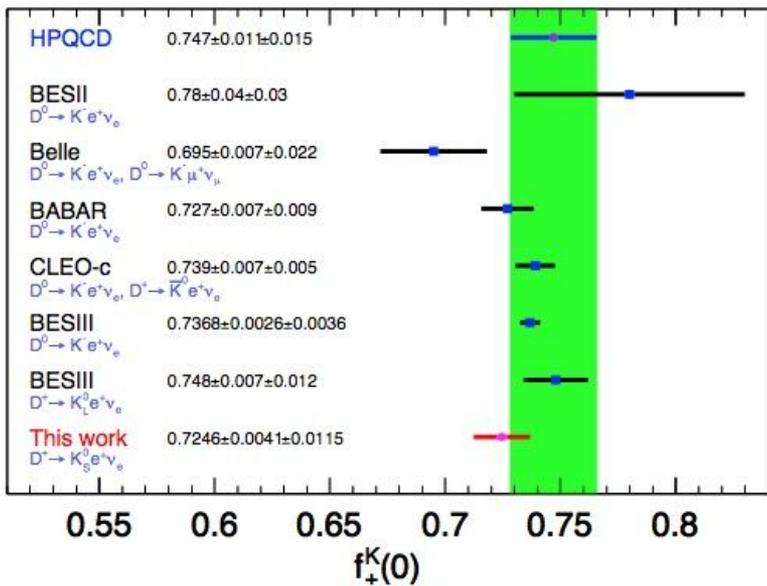
		$D^0 \rightarrow K e^+ \nu$		$D^0 \rightarrow \pi e^+ \nu$
Simple Pole	$f_K^+(0) V_{cs} $	$0.7209 \pm 0.0022 \pm 0.0033$	$f_\pi^+(0) V_{cd} $	$0.1475 \pm 0.0014 \pm 0.0005$
	M_{pole}	$1.9207 \pm 0.0103 \pm 0.0069$	M_{pole}	$1.9114 \pm 0.0118 \pm 0.0038$
Mod. Pole	$f_K^+(0) V_{cs} $	$0.7163 \pm 0.0024 \pm 0.0034$	$f_\pi^+(0) V_{cd} $	$0.1437 \pm 0.0017 \pm 0.0008$
	α	$0.3088 \pm 0.0195 \pm 0.0129$	α	$0.2794 \pm 0.0345 \pm 0.0113$
Series.2.Par	$f_K^+(0) V_{cs} $	$0.7172 \pm 0.0025 \pm 0.0035$	$f_\pi^+(0) V_{cd} $	$0.1435 \pm 0.0018 \pm 0.0009$
	r_1	$-2.2278 \pm 0.0864 \pm 0.0575$	r_1	$-2.0365 \pm 0.0807 \pm 0.0260$
Series.3.Par	$f_K^+(0) V_{cs} $	$0.7196 \pm 0.0035 \pm 0.0041$	$f_\pi^+(0) V_{cd} $	$0.1420 \pm 0.0024 \pm 0.0010$
	r_1	$-2.3331 \pm 0.1587 \pm 0.0804$	r_1	$-1.8434 \pm 0.2212 \pm 0.0690$
	r_2	$3.4223 \pm 3.9090 \pm 2.4092$	r_2	$-1.3871 \pm 1.4615 \pm 0.4677$



Comparisons of FFs by $D^+ \rightarrow \bar{K}^0(\pi^0)e^+\nu$



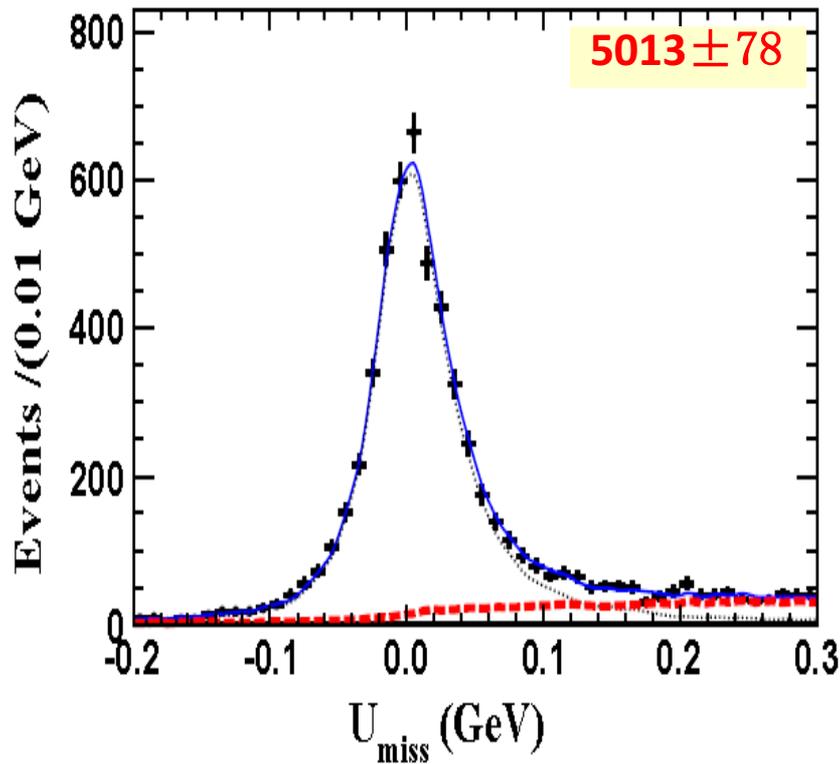
BESIII preliminary



First and second errors are statistical and systematic

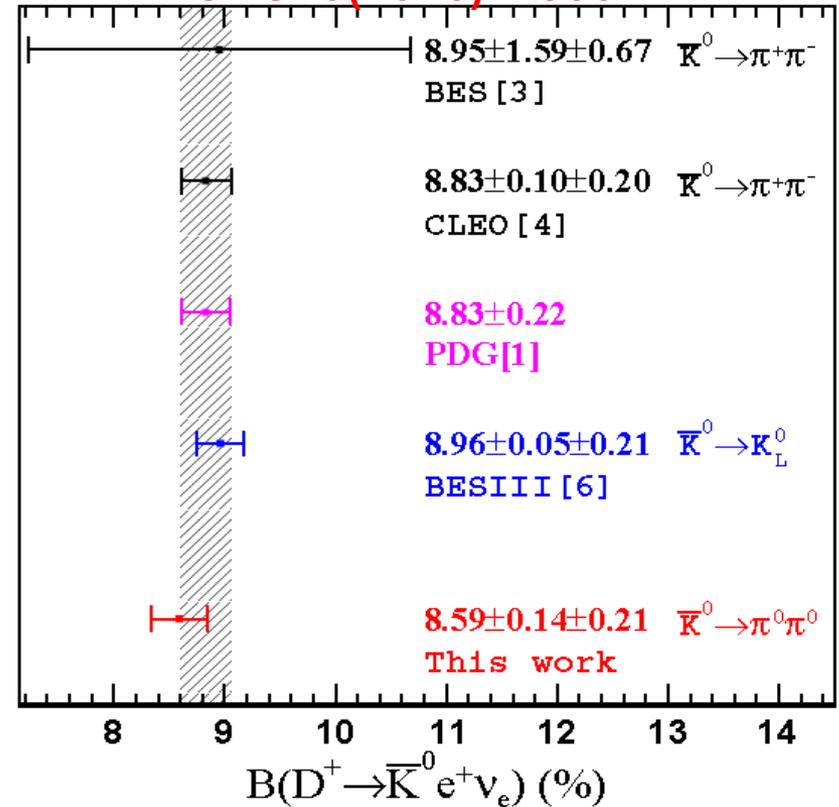
Absolute BF for $D^+ \rightarrow \bar{K}^0 e^+ \nu$ via $\bar{K}^0 \rightarrow \pi^0 \pi^0$

With 6 dominant D⁻ single tag



Taking τ_{D^+} , τ_{D^0} , $B[D^0 \rightarrow K^- e^+ \nu]$ and $B[D^+ \rightarrow \bar{K}^0 e^+ \nu]$ from the PDG as input

CPC40(2016)113001

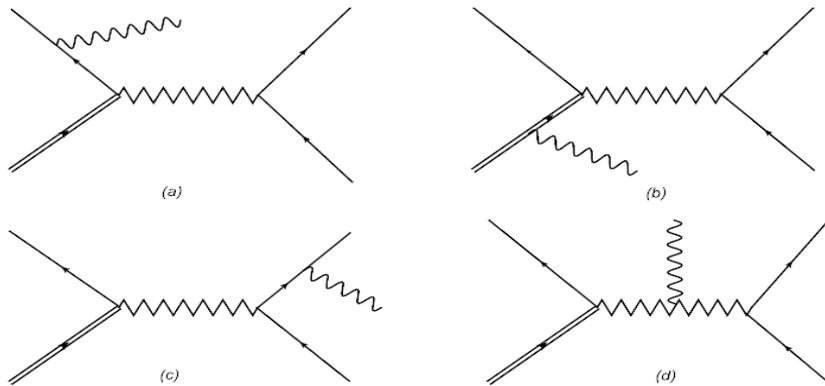


$$\frac{\Gamma[D^0 \rightarrow K^- e^+ \nu]}{\Gamma[D^+ \rightarrow \bar{K}^0 e^+ \nu]} = 0.969 \pm 0.025$$

Supporting isospin conservation in these two decays within 1.2σ

Search for $D^+ \rightarrow \gamma e^+ \nu$

J.C. Yang and M.Z. Yang, NPB889,778(2014)



Tree level amplitudes

With 6 dominant D- single tag

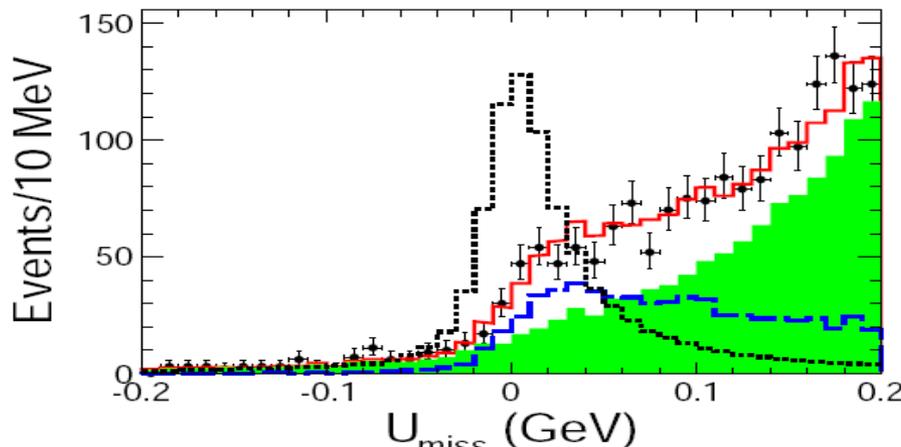
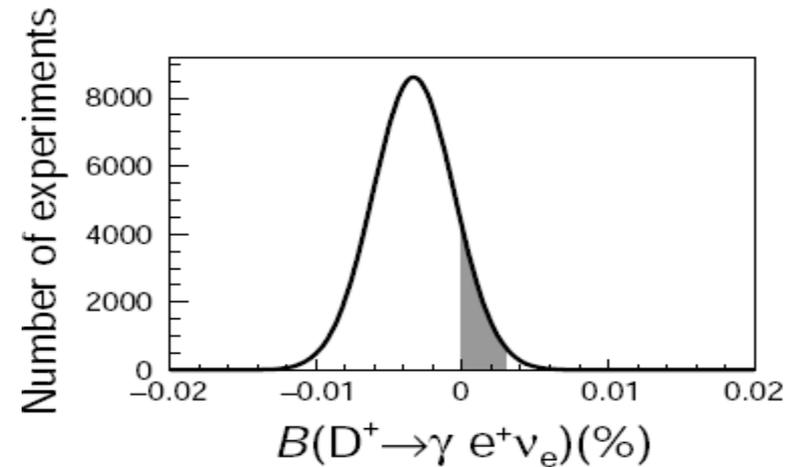


FIG. 2. (color online) The U_{miss} distribution. Dots with error bars are data, the red solid-line histogram shows the overall fit curve, the blue dash-line histogram shows the background $D^+ \rightarrow \pi^0 e^+ \nu_e$, and the green shaded histogram includes all other background. The black dotted line shows the signal MC simulation normalized to the branching fraction $\mathcal{B}(D^+ \rightarrow \gamma e^+ \nu_e) = 100 \times 10^{-5}$.

Various theory models predict BFs in 10^{-6} – 10^{-4}

Figure 1: Feynman diagrams of short-distance contribution at tree level (taken from Ref. [1]). The double line represents the heavy quark propagator. Fig.(a) and (b) are structure-dependent radiative decays, Fig.(c) is the Bremsstrahlung radiative decay. Fig.(d) is suppressed by a factor of $1/m_W^2$.

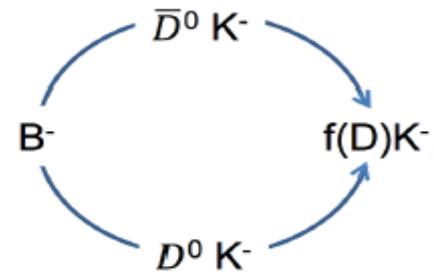
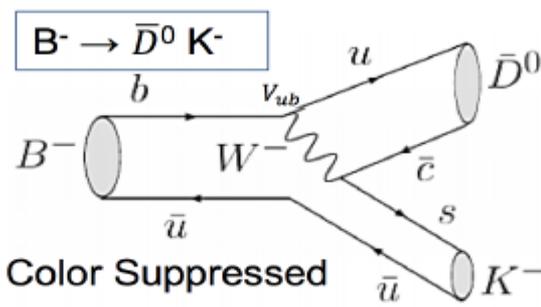
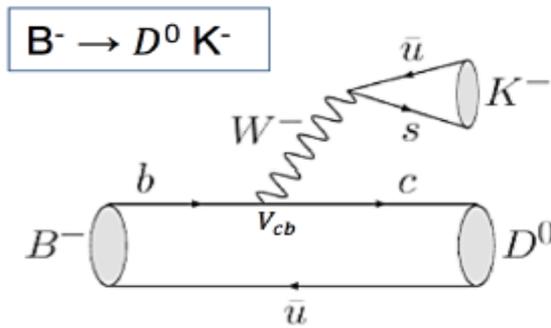
arXiv: 1702.05837[hep-ex], accepted by PRD



Upper limit is set at 90% CL

$$\mathcal{B}[D^+ \rightarrow \gamma e^+ \nu] |_{E_\gamma > 10 \text{ MeV}} < 3.0 \times 10^{-4}$$

γ/ϕ_3 at BELLE



$$\frac{\langle B^- \rightarrow \bar{D}^0 K^- \rangle}{\langle B^- \rightarrow D^0 K^- \rangle} = r_B e^{i(\delta_B - \phi_3)}$$

测量 $b \rightarrow c$ 和 $b \rightarrow u$ 的干涉

$$\Gamma(B^- \rightarrow f(D^0)K^-) = A_B^2 A_f^2 (r_D^2 + r_B^2 + 2r_D r_B \cos(\delta_B + \delta_D - \phi_3))$$

Belle Model-Dependent Dalitz [Phys. Rev. D 81, 112002 (2010)]
 $78.4^{+10.8}_{-11.6} (stat) \pm 3.6 (syst) \pm 8.9 (Model)$

Belle Model-Independent Dalitz [Phys. Rev. D 85, 112014 (2012)]
 $77.3^{+15.1}_{-14.9} (stat) \pm 4.2 (syst) \pm 4.3 (c_i/s_i)$

CLEO $\bar{K}^0 \pi^+ \pi^-$

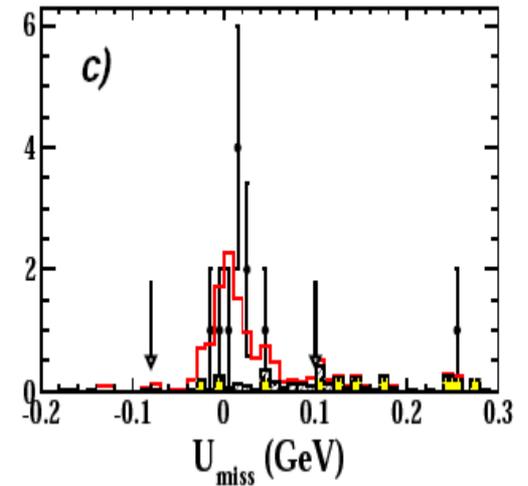
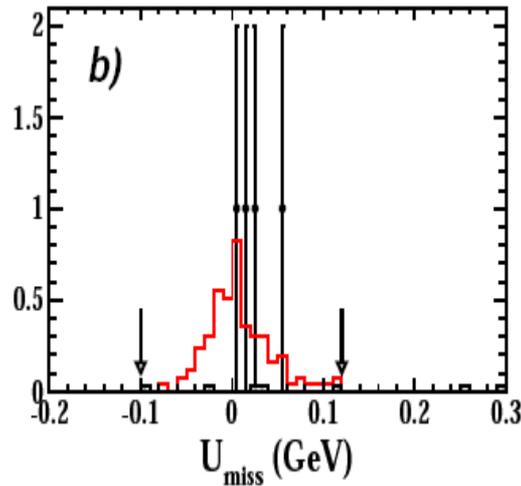
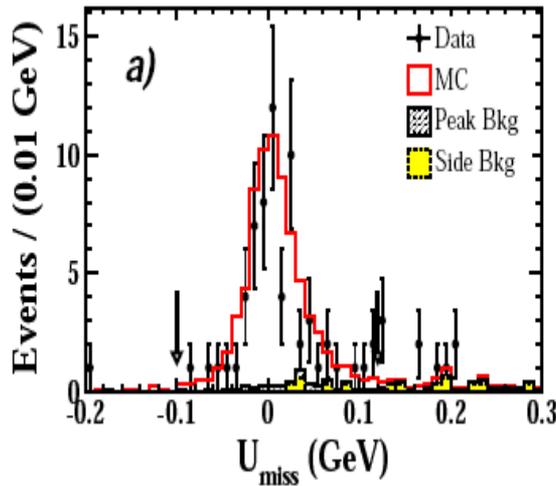
BelleII 和 LHCb 最终统计误差可以达到 1.5 度左右，要求 D Dalitz 衰变的不确定性为 1.0 度。

期待 BESIII 进一步改进 (c_i, s_i) ，以改进 γ/ϕ_3 精度

Measurements of BFs of $D_s^+ \rightarrow \eta^{(\prime)} e^+ \nu$

- Benefit the understanding of the source of difference of inclusive decay rates of $D^{0(+)}$ and D_s^+
- Complementary information to understand η - η' mixing

PRD94(2016)112003

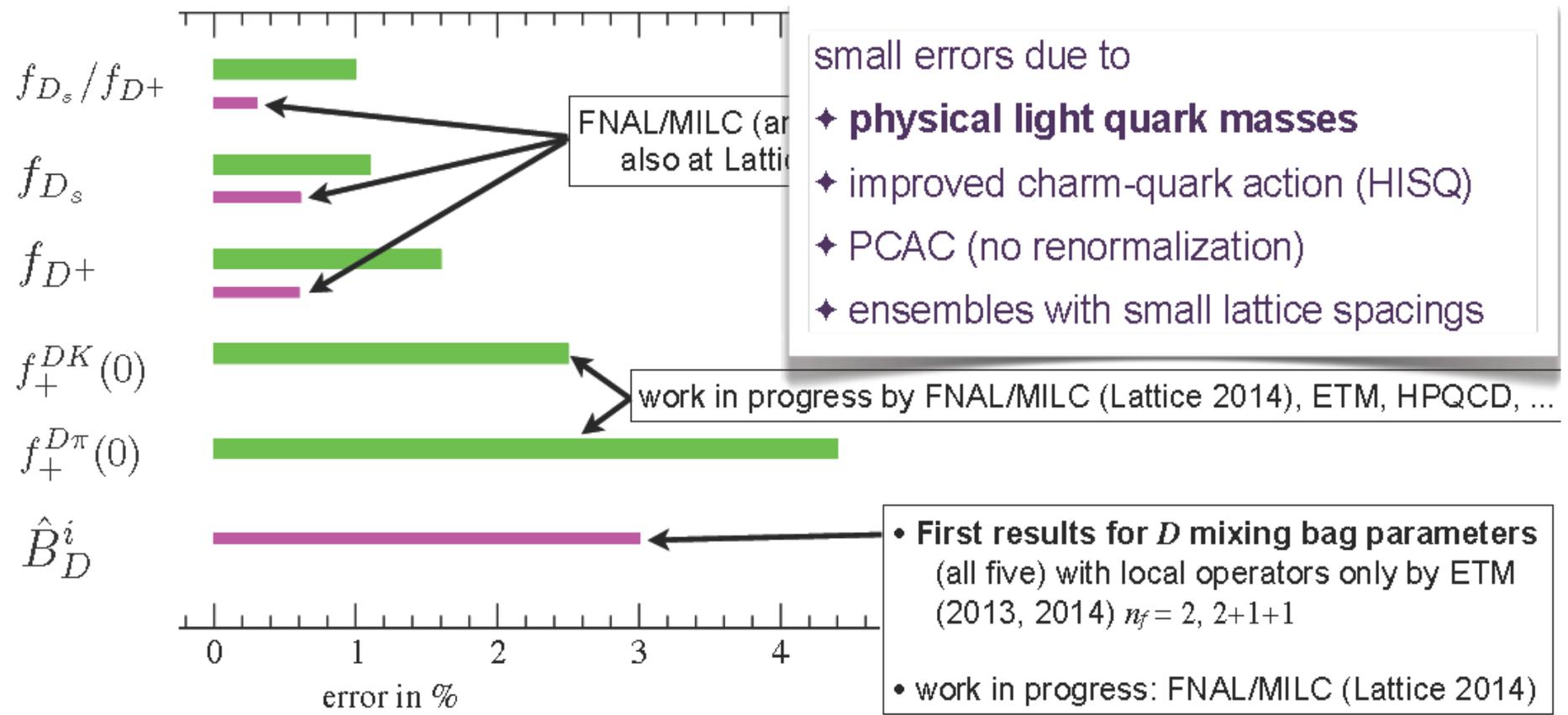


	BESIII	CLEOII 95	CLEOc09	CLEOc15	PDG [4]
$B(D_s^+ \rightarrow \eta e^+ \nu_e)$ [%]	$2.30 \pm 0.31 \pm 0.08$	—	$2.48 \pm 0.29 \pm 0.13$	$2.28 \pm 0.14 \pm 0.20$	2.67 ± 0.29
$B(D_s^+ \rightarrow \eta' e^+ \nu_e)$ [%]	$0.93 \pm 0.30 \pm 0.05$	—	$0.91 \pm 0.33 \pm 0.05$	$0.68 \pm 0.15 \pm 0.06$	0.99 ± 0.23
$\frac{B(D_s^+ \rightarrow \eta' e^+ \nu_e)}{B(D_s^+ \rightarrow \eta e^+ \nu_e)}$	$0.40 \pm 0.14 \pm 0.02$	$0.35 \pm 0.09 \pm 0.07$	—	—	—

Better input f_{D^+} from LQCD

Taking from Aida X. El-Khadra's talk at Beauty2014

errors (in %) comparison: **FLAG-2 averages** vs. **new results**

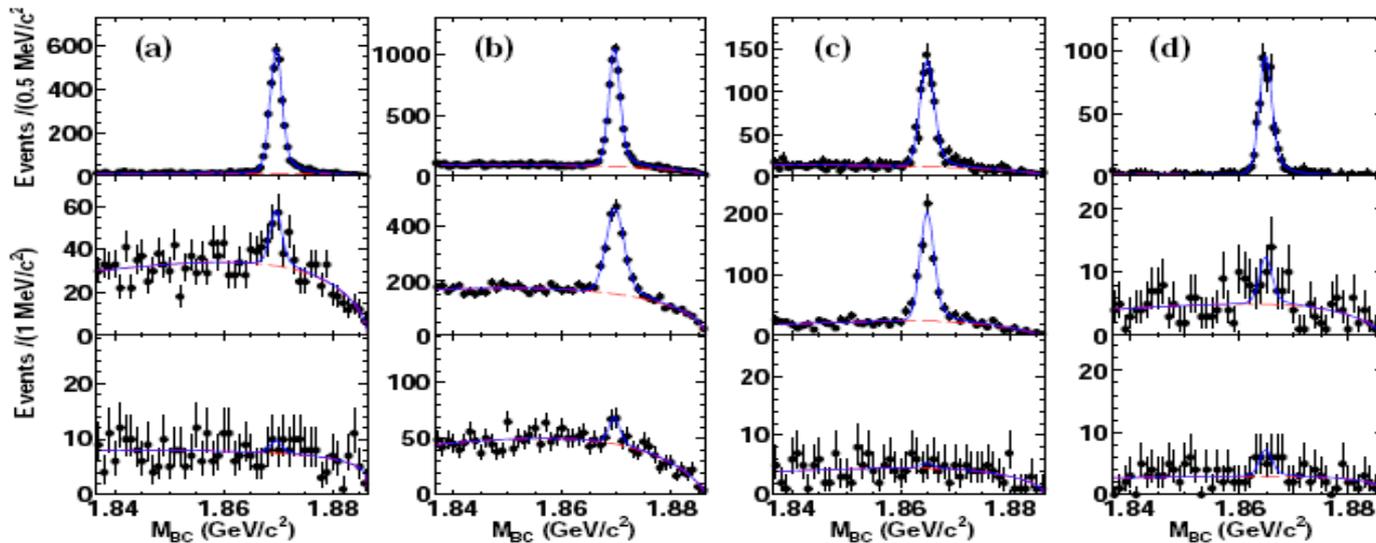


review by C. Bouchard @ Lattice 2014

BFs of $D^+ \rightarrow 2K_S K(\pi)^+$ and $D^0 \rightarrow 2(3)K_S$

Comprehensive or improved measurements of 3-body decays benefit the understanding of the interplay between weak and strong interactions in multibody decays, where theory is poor than 2-body decays

BF of $D^0 \rightarrow K_S K_S$ will be helpful to explore the SU(3) symmetry breaking in D decays



Comparisons of the branching fractions (in 10^{-4}) measured in this work with the PDG values

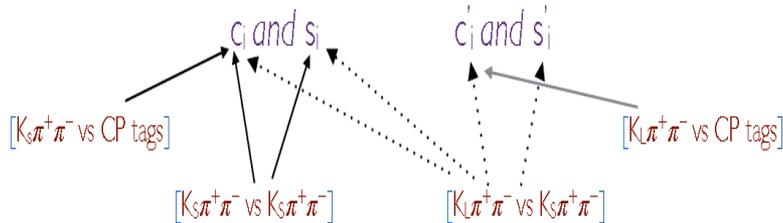
Decay modes	This work	PDG
$D^+ \rightarrow K_S^0 K_S^0 K^+$	$25.4 \pm 0.5 \pm 1.2$	45 ± 20
$D^+ \rightarrow K_S^0 K_S^0 \pi^+$	$27.0 \pm 0.5 \pm 1.2$	-
$D^0 \rightarrow K_S^0 K_S^0$	$1.67 \pm 0.11 \pm 0.11$	1.7 ± 0.4
$D^0 \rightarrow K_S^0 K_S^0 K_S^0$	$7.21 \pm 0.33 \pm 0.44$	9.1 ± 1.3

PLB765(2017)231

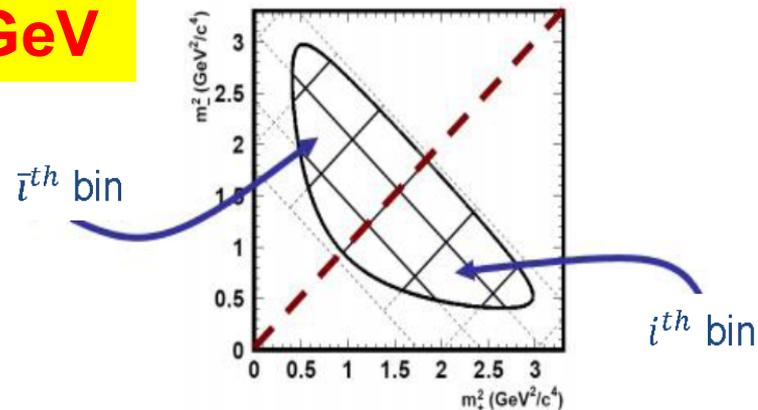
$D^0 \rightarrow \bar{K}^0 \pi^+ \pi^-$ DPA $\rightarrow (c_i, s_i)$

at 3.773 GeV

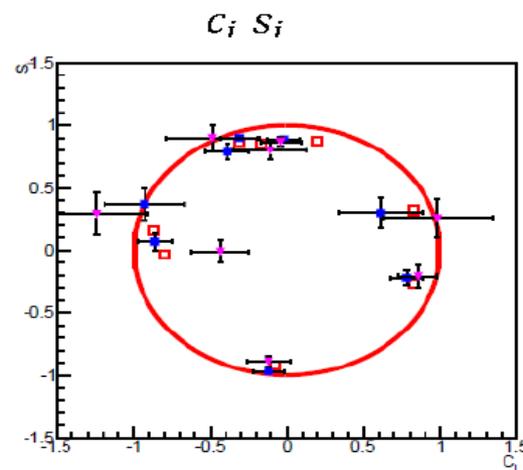
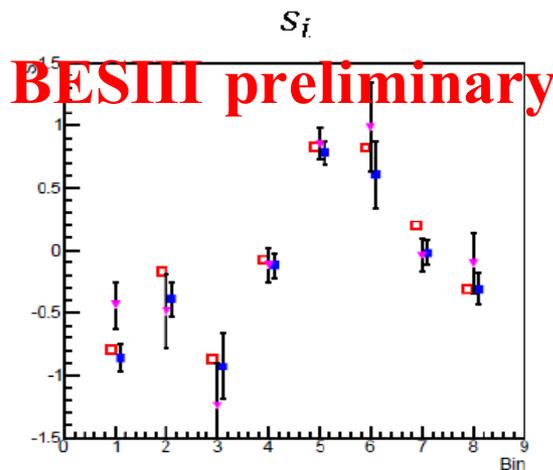
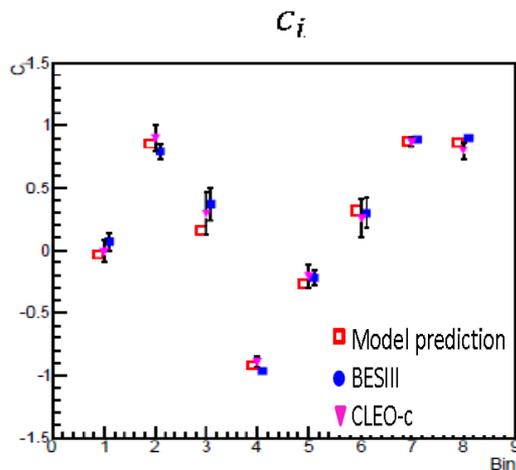
c_i, s_i can be measured using the Double Tags:
 $D^0 \rightarrow K_S \pi^+ \pi^-$ vs ($K_{S/L} \pi^+ \pi^-$ or CP tags)



Use both (c_i, s_i) and (\bar{c}_i, \bar{s}_i) to further constrain the results (c_i, s_i)



Mirrored binning over $x=y$ makes it so $c_i = c_{\bar{i}}$ and $s_i = -s_{\bar{i}}$



此BESIII输入对 γ/ϕ_3 的影响: $3\text{fb}^{-1} \rightarrow 2.1^0$

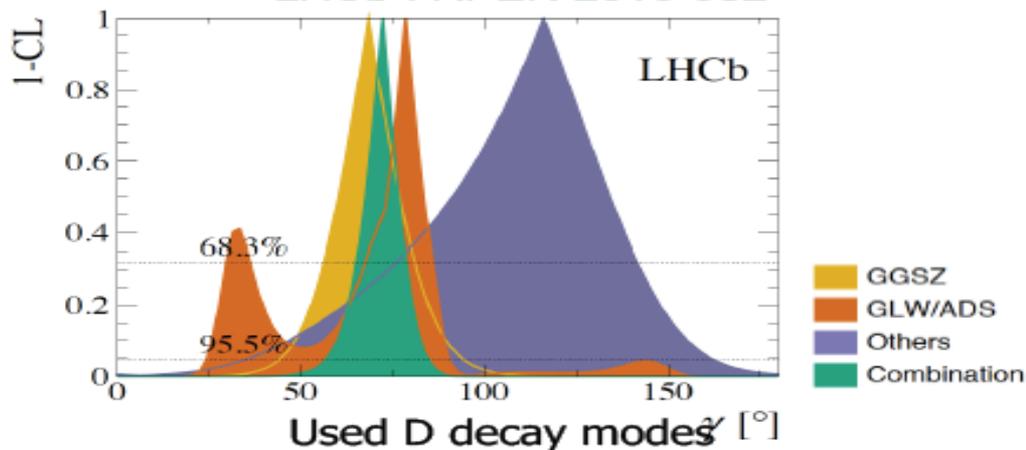
Constrain on γ/ϕ_3 measurement

Blow slides is taken from Liming Zhang's talk at FPCPV2016

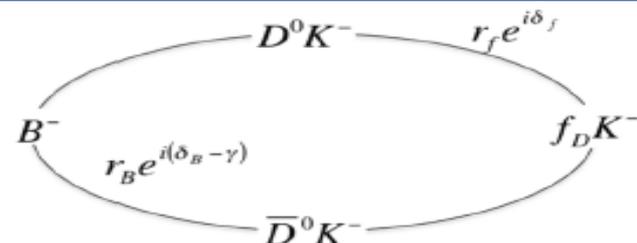


γ combination at LHCb

Determine γ from CPV measurements
LHCb-PAPER-2016-032



GLW: $D \rightarrow K^+ K^-$ $\pi^+ \pi^-$ $K_S^0 \pi^0$	ADS: $D \rightarrow \pi^+ K^-$	quasi-ADS $D \rightarrow \pi^+ K^- \pi^+ \pi^-$ $\pi^+ K^- \pi^0$
GGSZ $D \rightarrow K_S^0 \pi^+ \pi^-$ $K_S^0 K^+ K^-$	quasi-GLW $D \rightarrow \pi^+ \pi^- \pi^+ \pi^-$ $K^+ K^- \pi^0$ $\pi^+ \pi^- \pi^0$	GLS $D \rightarrow K_S^0 K^+ \pi^+$ $K_S^0 \pi^+ K^+$



$$\gamma = (72.2^{+6.8}_{-7.3})^\circ \text{ syst. included}$$

BaBar: $\gamma = (70 \pm 18)^\circ$

Belle: $\gamma = (73^{+13}_{-15})^\circ$

Prospects

Sample	$\sigma_{\text{stat}}(\gamma)^\circ$
Run 1	8
Run 2	4
Upgrade	~ 1
Future upgrade	< 0.5

- Current one syst. $\sim 2^\circ$ from CLEO strong phase measurements
- 15-20 fb^{-1} $\psi(3370)$ data from BESIII are desired to avoid syst. limitation for upgrade scenario

More $\psi(3770)$ data at BESIII will better constrain on γ/ϕ_3 45

PWA analysis of $D^+ \rightarrow K^- \pi^+ e^+ \nu$

PRD94(2016)032001

Fractions with $>5\sigma$ significance

$$f(D^+ \rightarrow (K^- \pi^+)_{K^{*0}(892)} e^+ \nu_e) = (93.93 \pm 0.22 \pm 0.18)\%$$

$$f(D^+ \rightarrow (K^- \pi^+)_{S\text{-wave}} e^+ \nu_e) = (6.05 \pm 0.22 \pm 0.18)\%$$

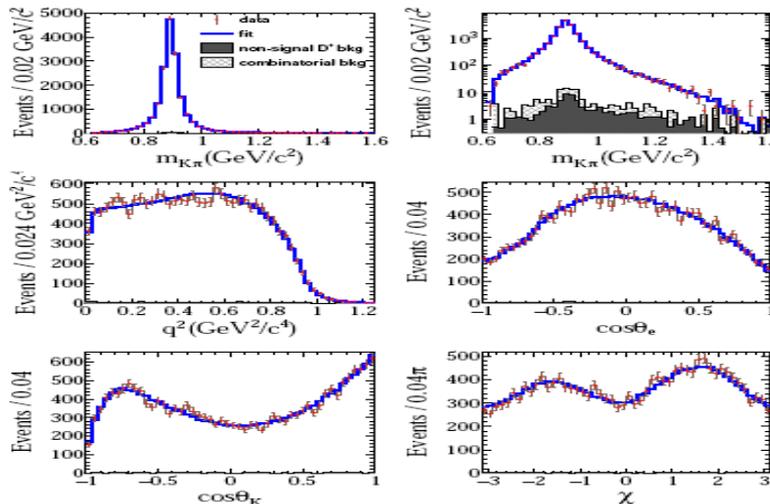
Properties of different $K\pi$ (non-) resonant amplitudes

$$m_{K^{*0}(892)} = (894.60 \pm 0.25 \pm 0.08) \text{ MeV}/c^2$$

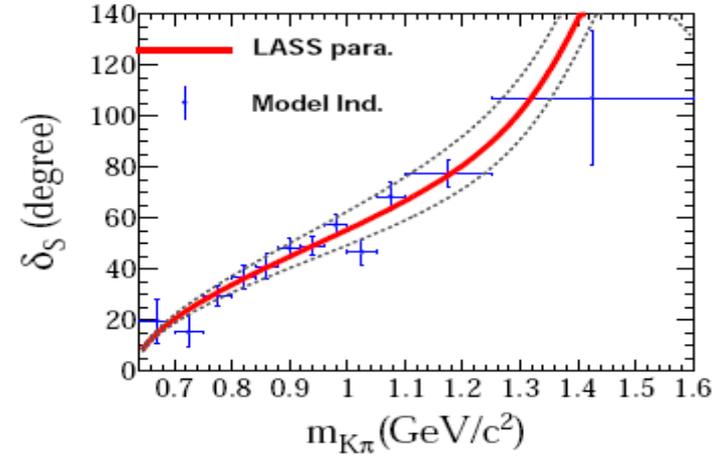
$$\Gamma_{K^{*0}(892)} = (46.42 \pm 0.56 \pm 0.15) \text{ MeV}/c^2$$

$$r_{BW} = (3.07 \pm 0.26 \pm 0.11) (\text{GeV}/c)^{-1}$$

q^2 dependent form factors in $D^+ \rightarrow \bar{K}^{*0}(892)e^+ \nu$



Model independent S-wave phase measurement



$$V(q^2) = \frac{V(0)}{1 - q^2/m_V^2}, \quad A_{1,2}(q^2) = \frac{A_{1,2}(0)}{1 - q^2/m_A^2}$$

$M_{V/A}$ is expected to $M_{D^{*(1/+)}}$

$$m_V = (1.81^{+0.25}_{-0.17} \pm 0.02) \text{ GeV}/c^2$$

$$m_A = (2.61^{+0.22}_{-0.17} \pm 0.03) \text{ GeV}/c^2$$

$$A_1(0) = 0.573 \pm 0.011 \pm 0.020$$

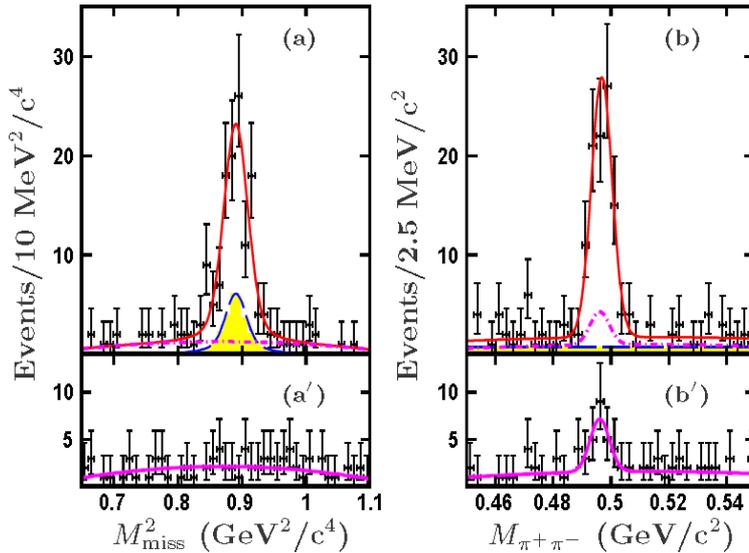
$$r_V = V(0)/A_1(0) = 1.411 \pm 0.058 \pm 0.007$$

$$r_2 = A_2(0)/A_1(0) = 0.788 \pm 0.042 \pm 0.008$$

Model independent form factors

Observation of $\Lambda_c^+ \rightarrow nK_S\pi^+$

PRL118(2017)112001



$$\mathcal{B}[\Lambda_c^+ \rightarrow nK_S\pi^+] = (1.82 \pm 0.23 \pm 0.11)\%$$

$$\Gamma[\Lambda_c^+ \rightarrow n\bar{K}^0\pi^+] / \Gamma[\Lambda_c^+ \rightarrow pK^-\pi^+] = 0.62 \pm 0.09$$

$$\Gamma[\Lambda_c^+ \rightarrow n\bar{K}^0\pi^+] / \Gamma[\Lambda_c^+ \rightarrow p\bar{K}^0\pi^+] = 0.97 \pm 0.16$$

First measurement of BF of Λ_c^+ decay containing neutron

$$\cos \delta = -0.24 \pm 0.08$$

$$|I^{(1)}| / |I^{(0)}| = 1.14 \pm 0.11$$

Help to understand SU(3) and isospin symmetry and determine strong phase

Cai-Dian Lv et al, PRD93(2016)056008

$\cos \delta$

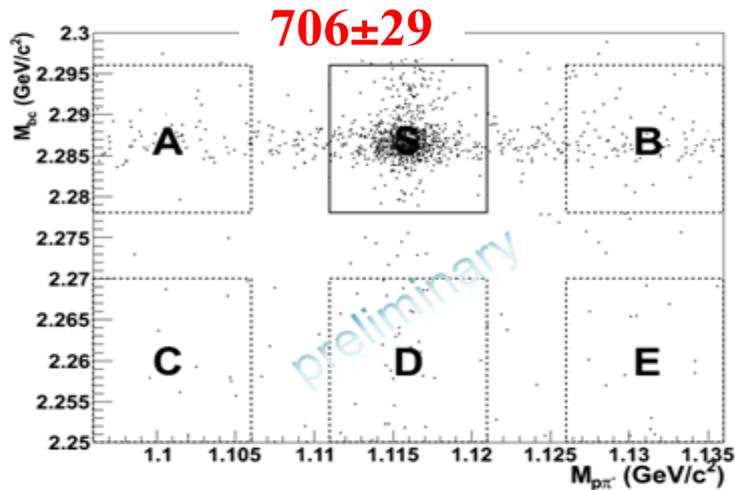
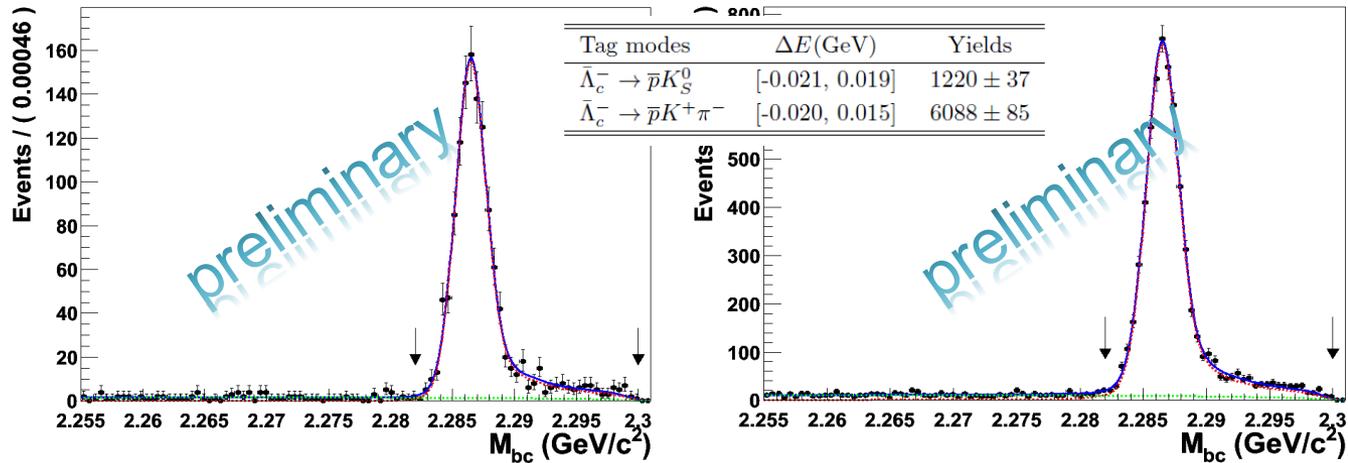
$$= \frac{\mathcal{B}(n\bar{K}^0\pi^+) - \mathcal{B}(pK^-\pi^+)}{2\sqrt{\mathcal{B}(p\bar{K}^0\pi^0)(\mathcal{B}(pK^-\pi^+) + \mathcal{B}(n\bar{K}^0\pi^+) - \mathcal{B}(p\bar{K}^0\pi^0))}}$$

$$R_p = \frac{\mathcal{B}(\Lambda_c \rightarrow p\bar{K}^0\pi^0)}{\mathcal{B}(\Lambda_c \rightarrow pK^-\pi^+)}, \quad R_n = \frac{\mathcal{B}(\Lambda_c \rightarrow n\bar{K}^0\pi^+)}{\mathcal{B}(\Lambda_c \rightarrow pK^-\pi^+)}$$

involving a neutron. Under the isospin symmetry, its amplitude is related to those of the most favored proton modes $\Lambda_c^+ \rightarrow pK^-\pi^+$ and $\Lambda_c^+ \rightarrow p\bar{K}^0\pi^0$ as $\mathcal{A}(n\bar{K}^0\pi^+) + \mathcal{A}(pK^-\pi^+) + \sqrt{2}\mathcal{A}(p\bar{K}^0\pi^0) = 0$. Hence, precise measure-

[2,3]. In the three-body Λ_c^+ decay to $N\bar{K}\pi$, the total decay amplitudes can be decomposed into two isospin amplitudes of the $N\bar{K}$ system as isosinglet ($I^{(0)}$) and isospin-one ($I^{(1)}$). In the factorization limit, the color-allowed tree diagram, in which the π^+ is emitted and the $N\bar{K}$ is an isosinglet, dominates $I^{(0)}$, and $I^{(1)}$ is expected to be small compared to $I^{(0)}$ as it can only proceed through the color-suppressed tree diagrams. Though the factorization scheme is spoiled in

Inclusive decay $\Lambda_c^+ \rightarrow \Lambda X$



Help to explore the source of missing decays and search for new decay. Better input for charm baryon and B physics

$$N_{sig} = N_S - (N_A + N_B)/2 - r \cdot N_D + r \cdot (N_C + N_E)/2$$

$$\mathcal{B}(\Lambda_c^+ \rightarrow \Lambda + X) = (36.98 \pm 2.18)\% \quad \text{stat. only}$$

Agrees with PDG2015 value (35 ± 11)%, which has no update after 1992

$$\mathcal{A}_{CP} = \frac{\mathcal{B}(\Lambda_c^+ \rightarrow \Lambda + X) - \mathcal{B}(\bar{\Lambda}_c^- \rightarrow \bar{\Lambda} + X)}{\mathcal{B}(\Lambda_c^+ \rightarrow \Lambda + X) + \mathcal{B}(\bar{\Lambda}_c^- \rightarrow \bar{\Lambda} + X)}$$

Decay mode	Branching fraction(%)	\mathcal{A}_{CP}
$\Lambda_c^+ \rightarrow \Lambda + X$	38.02 ± 3.24	
$\bar{\Lambda}_c^- \rightarrow \bar{\Lambda} + X$	36.70 ± 3.04	0.02 ± 0.06

Prospects on $f_{D(s)^+}$, $f^{K(\pi)^+}(0)$, $|V_{cs(d)}|$ and Λ_c^+

- Precision of the LQCD calculations of f_{D^+} , $f_{D_s^+}$, $f_{D^+}:f_{D_s}$ is 0.5%, 0.5% and 0.3%. Measurements of $f_{D(s)^+}$ and $|V_{cs(d)}|$ by $D_{(s)}^+ \rightarrow l^+ \nu$ are still statistically limited. More 10 fb^{-1} data near 3.773/4.18 GeV will help to improve precision to 1% level
- Measurements of $|V_{cs(d)}|$ by $D \rightarrow K(\pi) e^+ \nu$ is restricted by precision of LQCD calculation 2.4(4.4)%. Improved theoretical calculation will be very helpful
- Measurements of $f_{\pi^+}(0)$ by $D \rightarrow \pi e^+ \nu$ is still statistics limited. More 10 fb^{-1} data at 3.773 GeV can improve precision to 1% level
- In addition, with more 3 fb^{-1} data in 4.6-4.65 GeV will help to improve $B[\Lambda_c^+ \rightarrow p K^- \pi^+]$ to 2% level and explore FF in $\Lambda_c^+ \rightarrow \Lambda l^+ \nu$ decays