

Probing GPDs in the photoproduction of a photon and a ρ meson with a large invariant mass

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Transversity of the nucleon using hard processes

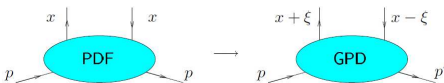
What is transversity?

- Transverse spin content of the proton:

$$\begin{aligned} |\uparrow\rangle(x) &\sim |\rightarrow\rangle + |\leftarrow\rangle \\ |\downarrow\rangle(x) &\sim |\rightarrow\rangle - |\leftarrow\rangle \end{aligned}$$

spin along x helicity states

- Observables which are sensitive to helicity flip thus give access to transversity $\Delta_{Tq}(x)$. Poorly known.
- Transversity GPDs are experimentally very elusive quantities **but recent exciting results**

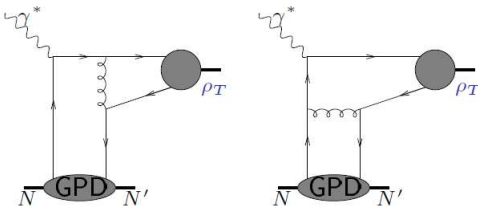


- For massless (anti)particles, chirality = (-)helicity
- **Transversity is thus a chiral-odd quantity**
- Since (in the massless limit) QCD and QED are chiral-even ($\gamma^\mu, \gamma^\mu\gamma^5$), **the chiral-odd quantities ($1, \gamma^5, [\gamma^\mu, \gamma^\nu]$) which one wants to measure should appear in pairs**

Transversity of the nucleon using hard processes: using a two body final state process?

How to get access to transversity GPDs?

- the dominant DA of ρ_T is of twist 2 and chiral-odd ($[\gamma^\mu, \gamma^\nu]$ coupling)
- unfortunately $\gamma^* N^\uparrow \rightarrow \rho_T N' = 0$
 - This cancellation is true at any order : such a process would require a helicity transfer of 2 from a photon.
 - lowest order diagrammatic argument:



$$\gamma^\alpha [\gamma^\mu, \gamma^\nu] \gamma_\alpha \rightarrow 0$$

[Diehl, Gousset, Pire], [Collins, Diehl]

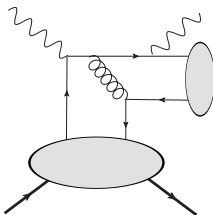
Transversity of the nucleon using hard processes: using a two body final state process?

Can one circumvent this vanishing?

- This vanishing only occurs at **twist 2**
- At twist 3 this process does not vanish [Ahmad, Goldstein, Liuti], [Goloskokov, Kroll]
- However processes involving **twist 3 DAs** may face problems with factorization (end-point singularities)
can be made safe in the high-energy k_T -factorization approach [Anikin, Ivanov, Pire, Szymanowski, Wallon]
- One can also consider a 3-body final state process [Ivanov, Pire, Szymanowski, Teryaev], [Enberg, Pire, Szymanowski], [El Beiyad, Pire, Segond, Szymanowski, Wallon]

Probing **chiral-odd** GPDs using ρ meson + photon production

Processes with **3 body final states** can give access to **chiral-odd GPDs**

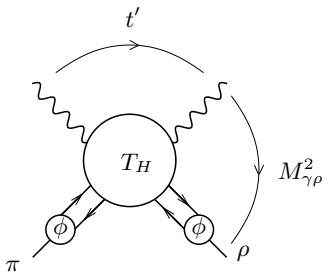


Typical non-zero diagram for a **transverse** ρ meson

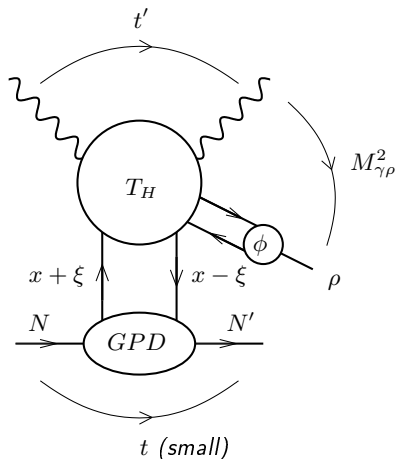
The previous argument does not apply anymore.

Probing GPDs using ρ meson + photon production

- We consider the process $\gamma N \rightarrow \gamma \rho N'$
- Collinear factorization of the amplitude for $\gamma + N \rightarrow \gamma + \rho + N'$ at large $M_{\gamma\rho}^2$

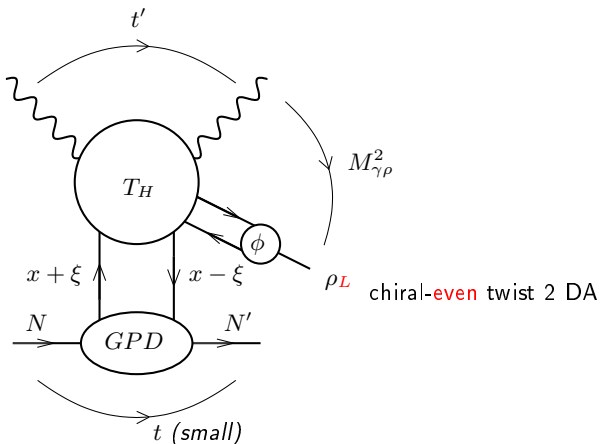


large angle factorization
à la Brodsky Lepage



Probing chiral-even GPDs using ρ meson + photon production

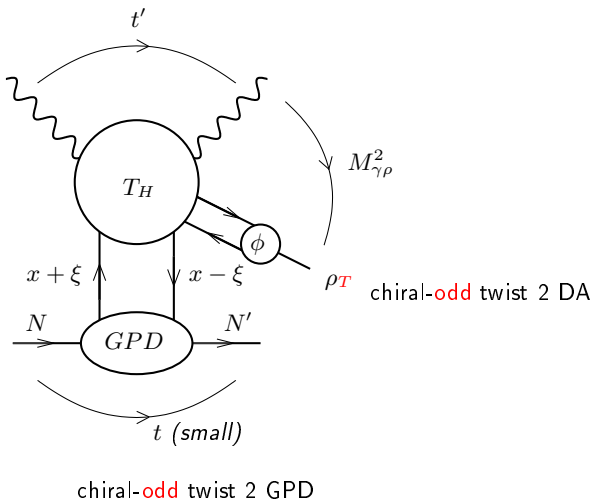
Processes with 3 body final states can give access to chiral-even GPDs



chiral-even twist 2 GPD

Probing chiral-odd GPDs using ρ meson + photon production

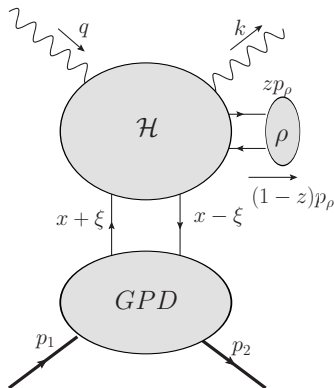
Processes with 3 body final states can give access to chiral-odd GPDs



Master formula based on leading twist 2 factorization

$$\mathcal{A} \propto \int_{-1}^1 dx \int_0^1 dz T(x, \xi, z) \times H(x, \xi, t) \Phi_\rho(z) + \dots$$

- Both the DA and the GPD can be either **chiral-even** or **chiral-odd**.
- At twist 2 the **longitudinal ρ DA** is **chiral-even** and the **transverse ρ DA** is **chiral-odd**.
- Hence we will need both **chiral-even** and **chiral-odd** non-perturbative building blocks and hard parts.



Kinematics

Kinematics to handle GPD in a 3-body final state process

- use a **Sudakov** basis :
light-cone vectors p , n with $2p \cdot n = s$
- assume the following kinematics:
 - $\Delta_{\perp} \ll p_{\perp}$
 - $M^2, m_{\rho}^2 \ll M_{\gamma\rho}^2$

- initial state particle momenta:

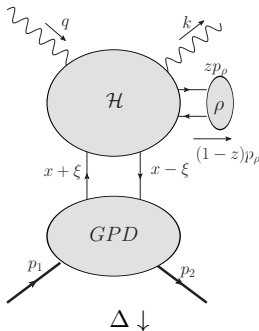
$$q^{\mu} = n^{\mu}, \quad p_1^{\mu} = (1 + \xi) p^{\mu} + \frac{M^2}{s(1+\xi)} n^{\mu}$$

- final state particle momenta:

$$p_2^{\mu} = (1 - \xi) p^{\mu} + \frac{M^2 + \vec{p}_t^2}{s(1 - \xi)} n^{\mu}$$

$$k^{\mu} = \alpha n^{\mu} + \frac{(\vec{p}_t - \vec{\Delta}_t/2)^2}{\alpha s} p^{\mu} + p_{\perp}^{\mu} - \frac{\Delta_{\perp}^{\mu}}{2},$$

$$p_{\rho}^{\mu} = \alpha_{\rho} n^{\mu} + \frac{(\vec{p}_t + \vec{\Delta}_t/2)^2 + m_{\rho}^2}{\alpha_{\rho} s} p^{\mu} - p_{\perp}^{\mu} - \frac{\Delta_{\perp}^{\mu}}{2},$$



Non perturbative **chiral-even** building blocks

- Helicity conserving GPDs at twist 2 :

$$\int \frac{dz^-}{4\pi} e^{ixP^+z^-} \langle p_2, \lambda_2 | \bar{\psi}_q \left(-\frac{1}{2}z^- \right) \gamma^+ \psi \left(\frac{1}{2}z^- \right) | p_1, \lambda_1 \rangle$$

$$= \frac{1}{2P^+} \bar{u}(p_2, \lambda_2) \left[H^q(x, \xi, t) \gamma^+ + E^q(x, \xi, t) \frac{i\sigma^{\alpha+} \Delta_\alpha}{2m} \right] u(p_1, \lambda_1)$$

$$\int \frac{dz^-}{4\pi} e^{ixP^+z^-} \langle p_2, \lambda_2 | \bar{\psi}_q \left(-\frac{1}{2}z^- \right) \gamma^+ \gamma^5 \psi \left(\frac{1}{2}z^- \right) | p_1, \lambda_1 \rangle$$

$$= \frac{1}{2P^+} \bar{u}(p_2, \lambda_2) \left[\tilde{H}^q(x, \xi, t) \gamma^+ \gamma^5 + \tilde{E}^q(x, \xi, t) \frac{\gamma^5 \Delta^+}{2m} \right] u(p_1, \lambda_1)$$

- We will consider the simplest case when $\Delta_\perp = 0$.
- In that case and in the forward limit $\xi \rightarrow 0$ only the H^q and \tilde{H}^q terms survive.

- Helicity conserving (vector) DA at twist 2 :

longitudinal polarization

$$\langle 0 | \bar{u}(0) \gamma^\mu u(x) | \rho^0(p, s) \rangle = \frac{p^\mu}{\sqrt{2}} f_\rho \int_0^1 du e^{-iup \cdot x} \phi_{\parallel}(u)$$

Non perturbative **chiral-odd** building blocks

- Helicity flip GPD at twist 2 :

$$\begin{aligned}
 & \int \frac{dz^-}{4\pi} e^{ixP^+z^-} \langle p_2, \lambda_2 | \bar{\psi}_q \left(-\frac{1}{2}z^- \right) i\sigma^{+i} \psi \left(\frac{1}{2}z^- \right) | p_1, \lambda_1 \rangle \\
 = & \frac{1}{2P^+} \bar{u}(p_2, \lambda_2) \left[H_T^q(x, \xi, t) i\sigma^{+i} + \tilde{H}_T^q(x, \xi, t) \frac{P^+ \Delta^i - \Delta^+ P^i}{M_N^2} \right. \\
 + & \left. E_T^q(x, \xi, t) \frac{\gamma^+ \Delta^i - \Delta^+ \gamma^i}{2M_N} + \tilde{E}_T^q(x, \xi, t) \frac{\gamma^+ P^i - P^+ \gamma^i}{M_N} \right] u(p_1, \lambda_1)
 \end{aligned}$$

- We will consider the simplest case when $\Delta_\perp = 0$.
- In that case and in the forward limit $\xi \rightarrow 0$ **only the H_T^q term survives.**
- Transverse ρ DA at twist 2 :

$$\langle 0 | \bar{u}(0) \sigma^{\mu\nu} u(x) | \rho^0(p, s) \rangle = \frac{i}{\sqrt{2}} (\epsilon_\rho^\mu p^\nu - \epsilon_\rho^\nu p^\mu) f_\rho^\perp \int_0^1 du e^{-iup \cdot x} \phi_\perp(u)$$

Models for DAs

Asymptotic DAs

We take the asymptotic form of the (normalized) DAs:

conformal symmetry, $\mu_F^2 \rightarrow \infty$

$$\phi_{\parallel}(z) = 6z(1-z),$$

$$\phi_{\perp}(z) = 6z(1-z).$$

Model for GPDs: based on the Double Distribution ansatz

DD Parameterization of GPDs

- GPDs can be represented in terms of **Double Distributions** [Radyushkin] based on the **Schwinger** representation of a toy model for GPDs in scalar ϕ^3 theory

$$H^q(x, \xi, t=0) = \int_{-1}^1 d\beta \int_{-1+|\beta|}^{1-|\beta|} d\alpha \delta(\beta + \xi\alpha - x) f^q(\beta, \alpha)$$

- ansatz for these Double Distributions [Radyushkin]:

- chiral-even sector:

$$f^q(\beta, \alpha, t=0) = \Pi(\beta, \alpha) q(\beta) \Theta(\beta) - \Pi(-\beta, \alpha) \bar{q}(-\beta) \Theta(-\beta),$$

$$\tilde{f}^q(\beta, \alpha, t=0) = \Pi(\beta, \alpha) \Delta q(\beta) \Theta(\beta) + \Pi(-\beta, \alpha) \Delta \bar{q}(-\beta) \Theta(-\beta).$$

- chiral-odd sector:

$$f_T^q(\beta, \alpha, t=0) = \Pi(\beta, \alpha) \delta q(\beta) \Theta(\beta) - \Pi(-\beta, \alpha) \delta \bar{q}(-\beta) \Theta(-\beta),$$

- $\Pi(\beta, \alpha) = \frac{3}{4} \frac{(1-\beta)^2 - \alpha^2}{(1-\beta)^3}$: profile function

- simplistic factorized ansatz for the t -dependence:

$$H^q(x, \xi, t) = H^q(x, \xi, t=0) \times F_H(t)$$

with $F_H(t) = \frac{C^2}{(t-C)^2}$ a standard **dipole form factor** ($C = .71$ GeV)

Model for GPDs: based on the Double Distribution ansatz

Sets of PDFs

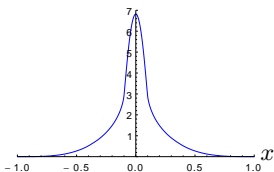
- $q(x)$: unpolarized PDF [GRV-98]
- $\Delta q(x)$ polarized PDF [GRSV-2000]
- $\delta q(x)$: transversity PDF [Anselmino *et al.*]

Model for GPDs: based on the Double Distribution ansatz

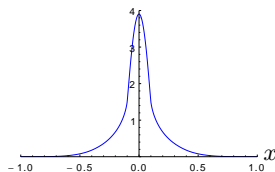
Typical sets of chiral-even GPDs

$$\xi = .1 \leftrightarrow S_{\gamma N} = 20 \text{ GeV}^2 \text{ and } M_{\gamma\rho}^2 = 3.5 \text{ GeV}^2$$

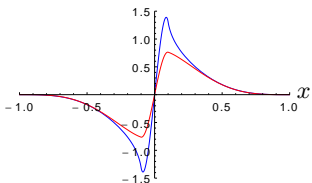
$$\frac{1}{2} H^{u(-)}(x, \xi)$$



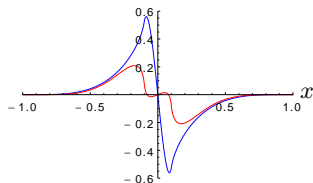
$$\frac{1}{2} H^{d(-)}(x, \xi)$$



$$\frac{1}{2} \tilde{H}^{u(-)}(x, \xi)$$



$$\frac{1}{2} \tilde{H}^{d(-)}(x, \xi)$$

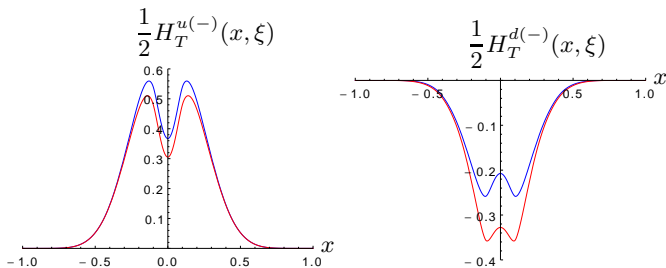


“valence” and “standard”: two GRSV Ansätze for $\Delta q(x)$

Model for GPDs: based on the Double Distribution ansatz

Typical sets of chiral-odd GPDs

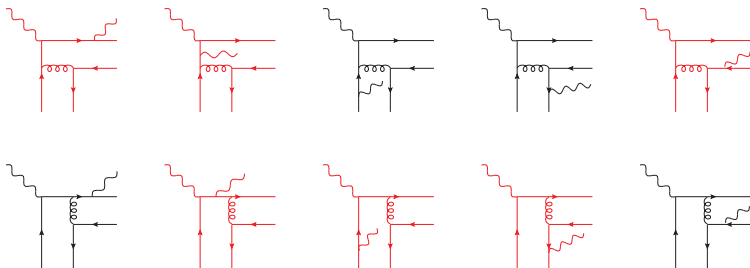
$$\xi = .1 \leftrightarrow S_{\gamma N} = 20 \text{ GeV}^2 \text{ and } M_{\gamma\rho}^2 = 3.5 \text{ GeV}^2$$



“valence” and “standard”: two GRSV Ansätze for $\Delta q(x)$
 \Rightarrow two Ansätze for $\delta q(x)$

Computation of the hard part

20 diagrams to compute



The other half can be deduced by $q \leftrightarrow \bar{q}$ (anti)symmetry
 Red diagrams cancel in the chiral-odd case

Final computation

Final computation

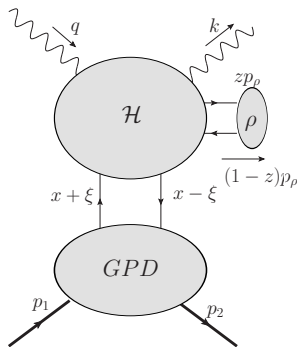
$$\mathcal{A} \propto \int_{-1}^1 dx \int_0^1 dz T(x, \xi, z) H(x, \xi, t) \Phi_\rho(z)$$

- One performs the z integration **analytically** using an asymptotic DA $\propto z(1-z)$
- One then plugs our GPD models into the formula and performs the integral w.r.t. x numerically.
- Differential cross section:

$$\left. \frac{d\sigma}{dt du' dM_{\gamma\rho}^2} \right|_{-t=(-t)_{min}} = \frac{|\overline{\mathcal{M}}|^2}{32S_{\gamma N}^2 M_{\gamma\rho}^2 (2\pi)^3}.$$

$|\overline{\mathcal{M}}|^2 =$ averaged amplitude squared

- Kinematical parameters: $S_{\gamma N}^2$, $M_{\gamma\rho}^2$ and $-u'$

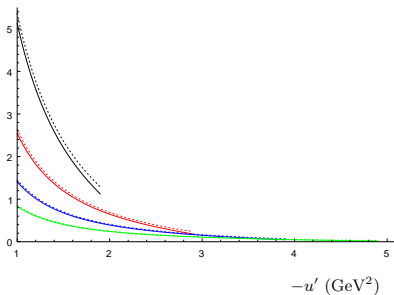


Fully differential cross section

Chiral even cross section

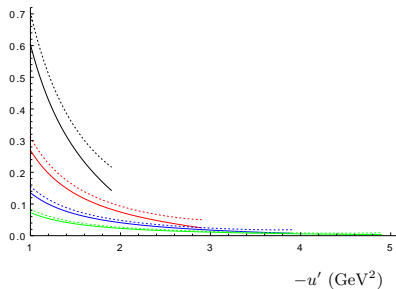
at $-t = (-t)_{\min}$

$$\frac{d\sigma_{\text{even}}}{dM_{\gamma\rho}^2 d(-u') d(-t)} \quad (\text{nb} \cdot \text{GeV}^{-6})$$



proton

$$\frac{d\sigma_{\text{even}}}{dM_{\gamma\rho}^2 d(-u') d(-t)} \quad (\text{nb} \cdot \text{GeV}^{-6})$$



neutron

$$S_{\gamma N} = 20 \text{ GeV}^2$$

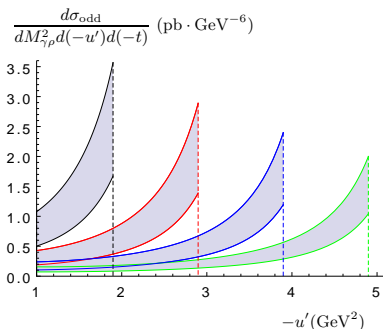
$$M_{\gamma\rho}^2 = 3, 4, 5, 6 \text{ GeV}^2$$

solid: "valence" model

dotted: "standard" model

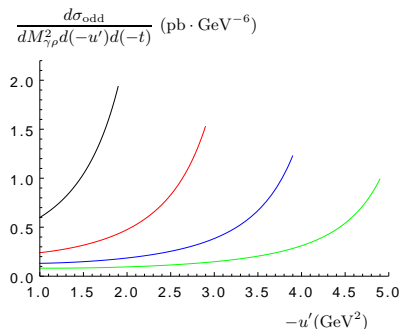
Fully differential cross section

Chiral odd cross section

at $-t = (-t)_{\min}$ 

proton

“valence” and “standard” models,
each of them with $\pm 2\sigma$ [S. Melis]



neutron

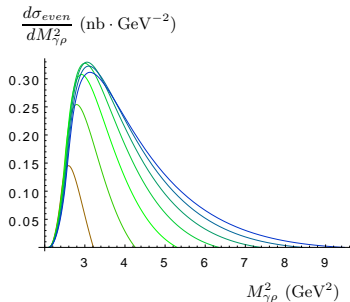
“valence” model only

$$S_{\gamma N} = 20 \text{ GeV}^2$$

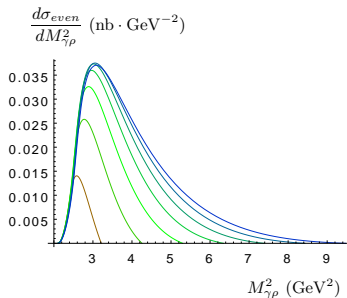
$$M_{\gamma\rho}^2 = 3, 4, 5, 6 \text{ GeV}^2$$

Single differential cross section

Chiral even cross section



proton



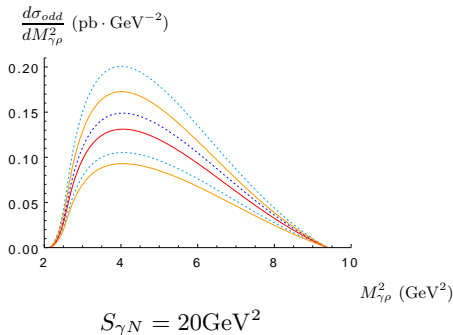
neutron

“valence” scenario

$S_{\gamma N}$ vary in the set 8, 10, 12, 14, 16, 18, 20 GeV² (from left to right)

Single differential cross section

Chiral odd cross section

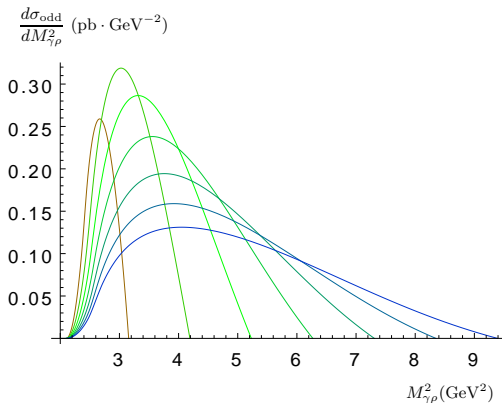


Various ansätze for the PDFs Δq used to build the GPD H_T :

- *dotted curves*: “standard” scenario
- *solid curves*: “valence” scenario
- *deep-blue* and *red* curves: central values
- *light-blue* and *orange*: results with $\pm 2\sigma$.

Single differential cross section

Chiral odd cross section

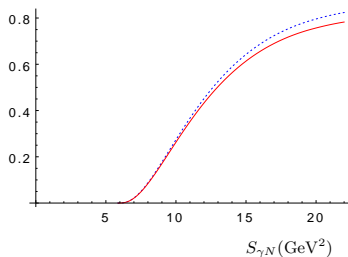


proton, "valence" scenario

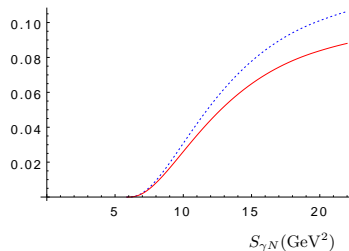
$S_{\gamma N}$ vary in the set 8, 10, 12, 14, 16, 18, 20 GeV² (from left to right)

Integrated cross-section

Chiral even cross section

 σ_{even} (nb)

proton

 σ_{even} (nb)

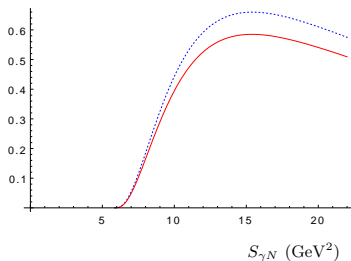
neutron

solid red: "valence" scenario

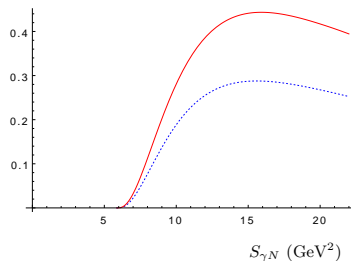
dashed blue: "standard" one

Integrated cross-section

Chiral odd cross section

 σ_{odd} (pb)


proton

 σ_{odd} (pb)


neutron

solid red: “valence” scenario

dashed blue: “standard” one

Counting rates for 100 days

example: JLab Hall B

- untagged incoming $\gamma \Rightarrow$ Weizsäcker-Williams distribution
- With an expected luminosity of $\mathcal{L} = 100 \text{ nb}^{-1} \text{ s}^{-1}$, for 100 days of run:
 - Chiral even case : $\simeq 6.8 \cdot 10^6 \rho_L$.
 - Chiral odd case : $\simeq 7.5 \cdot 10^3 \rho_T$

Conclusion

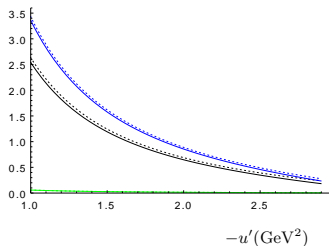
- High statistics for the chiral-even component: enough to extract H (\tilde{H} ?) and **test the universality of GPDs**
- In this chiral-even sector: analogy with **Timelike Compton Scattering**, the $\gamma\rho$ pair playing the role of the γ^* .
- Strong dominance of the chiral-even component w.r.t. the chiral-odd one:
 - In principle the separation ρ_L/ρ_T can be performed by an angular analysis of its decay products, but this could be very challenging. Cuts in θ_γ might help
 - Future: **study of polarization observables** \Rightarrow sensitive to the interference of these two amplitudes
- The **Bethe Heitler** component (outgoing γ emitted from the incoming lepton) is:
 - zero for the chiral-odd case
 - suppressed for the chiral-even case
- Our result can also be applied to **electroproduction** ($Q^2 \neq 0$) after adding **Bethe-Heitler** contributions and interferences.
- Possible measurement at **JLAB** (Hall B, C, D)
- A similar study could be performed at **COMPASS**. **EIC**, **LHC** in UPC?

Backup

Chiral-even cross section

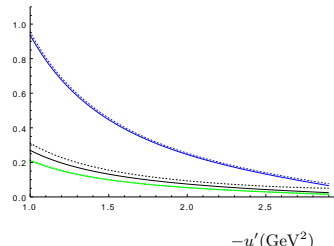
Contribution of u versus d

$$\frac{d\sigma_{\text{even}}}{dM_{\gamma\rho}^2 d(-u')d(-t)} \quad (\text{nb} \cdot \text{GeV}^{-6})$$



proton

$$\frac{d\sigma_{\text{even}}}{dM_{\gamma\rho}^2 d(-u')d(-t)} \quad (\text{nb} \cdot \text{GeV}^{-6})$$



neutron

$M_{\gamma\rho}^2 = 4 \text{ GeV}^2$. Both vector and axial GPDs are included.

$u + d$ quarks u quark d quark

Solid: "valence" model

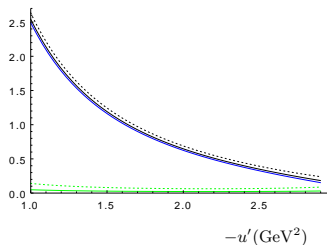
dotted: "standard" model

- u -quark contribution dominates due to the charge effect
- the interference between u and d contributions is important and negative.

Chiral-even cross section

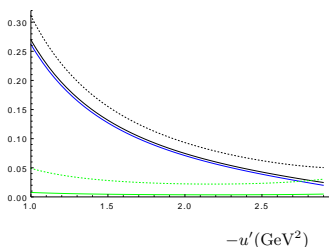
Contribution of vector versus axial amplitudes

$$\frac{d\sigma_{\text{even}}}{dM_{\gamma\rho}^2 d(-u') d(-t)} \quad (\text{nb} \cdot \text{GeV}^{-6})$$



proton

$$\frac{d\sigma_{\text{even}}}{dM_{\gamma\rho}^2 d(-u') d(-t)} \quad (\text{nb} \cdot \text{GeV}^{-6})$$



neutron

$M_{\gamma\rho}^2 = 4 \text{ GeV}^2$. Both u and d quark contributions are included.

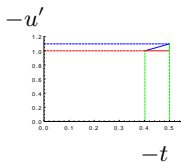
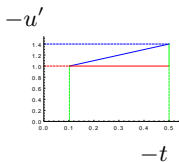
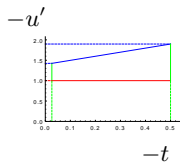
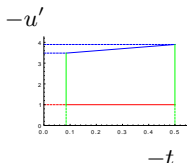
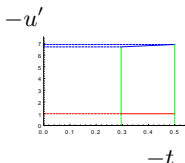
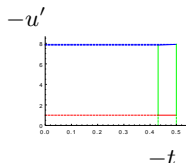
vector + axial amplitudes / vector amplitude / axial amplitude

solid: "valence" model

dotted: "standard" model

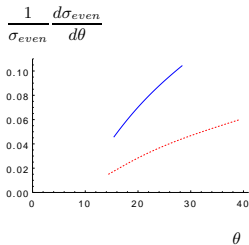
- dominance of the vector GPD contributions
- no interference between the vector and axial amplitudes

Phase space integration

Evolution of the phase space in $(-t, -u')$ planelarge angle scattering: $M_{\gamma\rho}^2 \sim -u' \sim -t'$ in practice: $-u' > 1 \text{ GeV}^2$ and $-t' > 1 \text{ GeV}^2$ and $(-t)_{\min} \leq -t \leq .5 \text{ GeV}^2$
this ensures large $M_{\gamma\rho}^2$ example: $S_{\gamma N} = 20 \text{ GeV}^2$  $M_{\gamma\rho} = 2.2 \text{ GeV}^2$  $M_{\gamma\rho} = 2.5 \text{ GeV}^2$  $M_{\gamma\rho} = 3 \text{ GeV}^2$  $M_{\gamma\rho} = 5 \text{ GeV}^2$  $M_{\gamma\rho} = 8 \text{ GeV}^2$  $M_{\gamma\rho} = 9 \text{ GeV}^2$

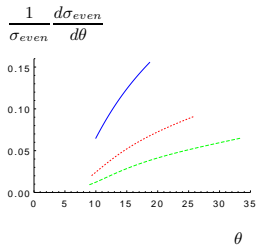
Effects of an experimental angular restriction for the produced γ ?Angular distribution of the produced γ (chiral-even cross section)

after boosting to the lab frame



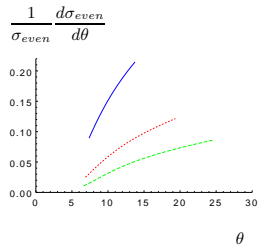
$$S_{\gamma N} = 10 \text{ GeV}^2$$

$$M_{\gamma\rho}^2 = 3, 4 \text{ GeV}^2$$



$$S_{\gamma N} = 15 \text{ GeV}^2$$

$$M_{\gamma\rho}^2 = 3, 4, 5 \text{ GeV}^2$$



$$S_{\gamma N} = 20 \text{ GeV}^2$$

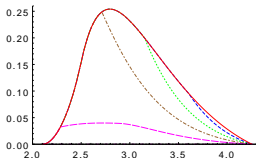
$$M_{\gamma\rho}^2 = 3, 4, 5 \text{ GeV}^2$$

JLab Hall B detector equipped between 5° and 35°

Effects of an experimental angular restriction for the produced γ ?Angular distribution of the produced γ (chiral-even cross section)

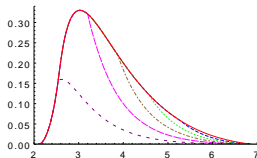
after boosting to the lab frame

$$\frac{d\sigma_{\text{even}}}{dM_{\gamma\rho^2}} (\text{nb} \cdot \text{GeV}^{-2})$$

 $M_{\gamma\rho}^2$

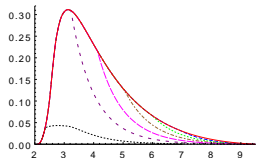
$$S_{\gamma N} = 10 \text{ GeV}^2$$

$$\frac{d\sigma_{\text{even}}}{dM_{\gamma\rho^2}} (\text{nb} \cdot \text{GeV}^{-2})$$

 $M_{\gamma\rho}^2$

$$S_{\gamma N} = 15 \text{ GeV}^2$$

$$\frac{d\sigma_{\text{even}}}{dM_{\gamma\rho^2}} (\text{nb} \cdot \text{GeV}^{-2})$$

 $M_{\gamma\rho}^2$

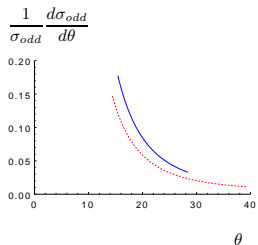
$$S_{\gamma N} = 20 \text{ GeV}^2$$

$$\theta_{\text{max}} = 35^\circ, 30^\circ, 25^\circ, 20^\circ, 15^\circ, 10^\circ$$

JLab Hall B detector equipped between 5° and 35° \Rightarrow this is safe!

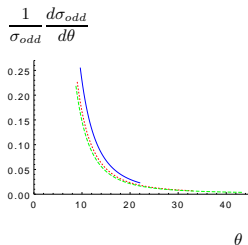
Effects of an experimental angular restriction for the produced γ ?Angular distribution of the produced γ (chiral-odd cross section)

after boosting to the lab frame



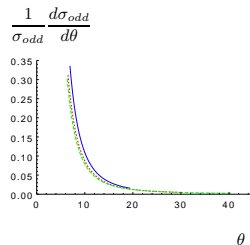
$$S_{\gamma N} = 10 \text{ GeV}^2$$

$$M_{\gamma\rho}^2 = 3, 4 \text{ GeV}^2$$



$$S_{\gamma N} = 15 \text{ GeV}^2$$

$$M_{\gamma\rho}^2 = 3.5, 5, 6.5 \text{ GeV}^2$$



$$S_{\gamma N} = 20 \text{ GeV}^2$$

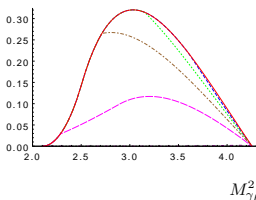
$$M_{\gamma\rho}^2 = 4, 6, 8 \text{ GeV}^2$$

JLab Hall B detector equipped between 5° and 35°

Effects of an experimental angular restriction for the produced γ ?Angular distribution of the produced γ (chiral-odd cross section)

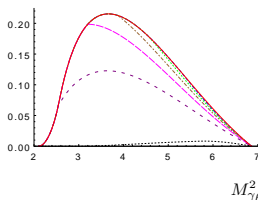
after boosting to the lab frame

$$\frac{d\sigma_{odd}}{dM_{\gamma\rho^2}} \text{ (pb.GeV}^{-2}\text{)}$$



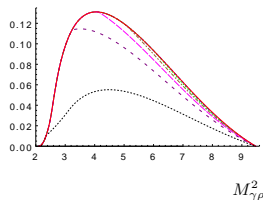
$$S_{\gamma N} = 10 \text{ GeV}^2$$

$$\frac{d\sigma_{odd}}{dM_{\gamma\rho^2}} \text{ (pb.GeV}^{-2}\text{)}$$



$$S_{\gamma N} = 15 \text{ GeV}^2$$

$$\frac{d\sigma_{odd}}{dM_{\gamma\rho^2}} \text{ (pb.GeV}^{-2}\text{)}$$



$$S_{\gamma N} = 20 \text{ GeV}^2$$

$$\theta_{max} = 35^\circ, 30^\circ, 25^\circ, 20^\circ, 15^\circ, 10^\circ$$

JLab Hall B detector equipped between 5° and 35° \Rightarrow this is safe!