

Measuring Gluon Orbital Angular Momentum at the Electron-Ion Collider

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X. Ji, F. Yuan and Y.Z., arXiv:1612.02438

Outline

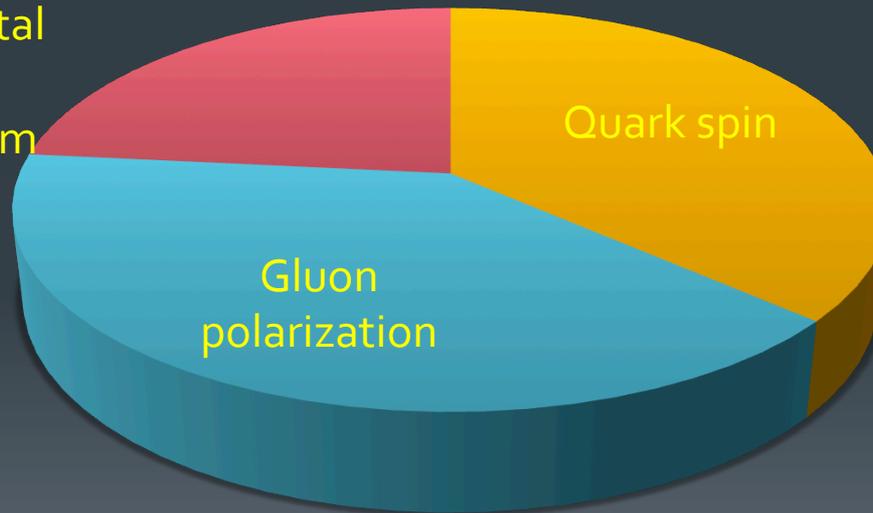
- Gluon OAM and Wigner distribution
- Experimental observable

Outline

- Gluon OAM and Wigner distribution
- Experimental observable

The longitudinal nucleon spin structure

Quark and
gluon orbital
angular
momentum



$$\Delta\Sigma(Q^2=10 \text{ GeV}^2) = 0.366,$$

de Florian et al., 2009

SLAC
HERMES (DESY)
COMPASS (CERN)
JLab
RHIC

Naïve spin sum rule:

$$\frac{1}{2} = \frac{1}{2} \Delta\Sigma + \Delta G + l_q^z + l_g^z$$

$$\Delta G(Q^2=10 \text{ GeV}^2) \sim 0.2,$$

de Florian et al., 2014
Yang, Liu, Y.Z., et al., 2016

Orbital angular momentum

- **OAM in Ji sum rule (Ji, 1997):**
 - Measureable through twist-2 GPD in deeply virtual Compton scattering (DVCS)
 - Parton density interpretation not clear
- **OAM in Jaffe-Manohar sum rule (Jaffe and Manohar, 1989):**
 - Clear partonic interpretation;
 - Related to a TMD (pretzelosity) in model (She, Zhu, and Ma, 2009; H. Avakian et al., 2009, 2010), accessible through SIDIS (Lefky and Prokudin, 2015);
 - Direct measurement not known.

The gluon orbital angular momentum (OAM) and Wigner distribution

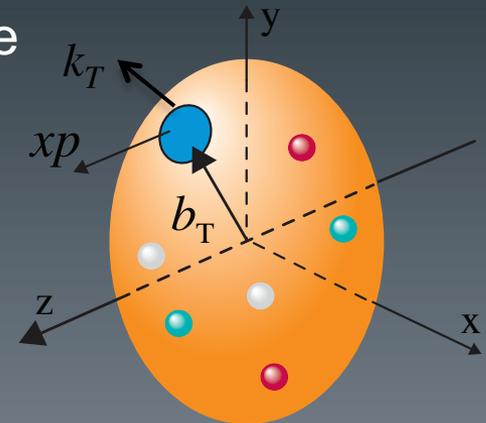
- Moment of a phase space Wigner distribution

$$\begin{aligned}
 l_g &= \int_0^1 dx L_g(x) \\
 &= \int_0^1 dx \int db_{\perp}^2 d^2 k_{\perp} (b_{\perp} \times k_{\perp}) W_{LC}^g(x, 0, k_{\perp}, b_{\perp})
 \end{aligned}$$

- Wigner distribution or generalized transeverse momentum distribution (GTMD)

$$\begin{aligned}
 &W_{LC}^g(x, \xi, k_{\perp}, b_{\perp}) \\
 &= \int d^2 \Delta_{\perp} e^{-ib_{\perp} \cdot \Delta_{\perp}} f(x, \xi, k_{\perp}, \Delta_{\perp})
 \end{aligned}$$

Belitsky, Ji, and Yuan, 2004;
 Meissner, Metz and Schlegel, 2009;
 Lorce and Pasquini, 2011;
 Lorce et al., 2012;
 Y. Hatta, 2012;
 Ji, Xiong, and Yuan, 2012.



The gluon orbital angular momentum (OAM) and Wigner distribution

- Parametrization of GTMD

 $F_g^{1,4}$

$$f_g(x, \xi, k_\perp, \Delta_\perp) = F_g(x, \xi, |k_\perp|, |\Delta_\perp|) + i \frac{\vec{k}_\perp \times \vec{\Delta}_\perp}{2M^2} S^+ \underline{F_g^{(l)}(x, \xi, |k_\perp|, |\Delta_\perp|)} + \dots$$

- Gluon OAM density as the moment of GTMD

$$L_g(x, \xi, |\Delta_\perp|) = - \int d^2 k_\perp \frac{k_\perp^2}{2M^2} F_g^{(l)}(x, \xi, |k_\perp|, |\Delta_\perp|)$$

$$L_g(x) = L_g(x, 0, 0)$$

Outline

- Gluon OAM and Wigner distribution
- Experimental observable
- Outlook

Experimental Process

$$f_g(x, \xi, k_{\perp}, \Delta_{\perp})$$

Two independent momenta

Momentum transfer of the proton, exclusive process

Consider $\gamma^* p$ scattering:

2- \rightarrow 2 process, final state momenta not independent;

2- \rightarrow 3 process, one more independent momentum.

Intrinsic transverse momentum k_T , measure dijets!

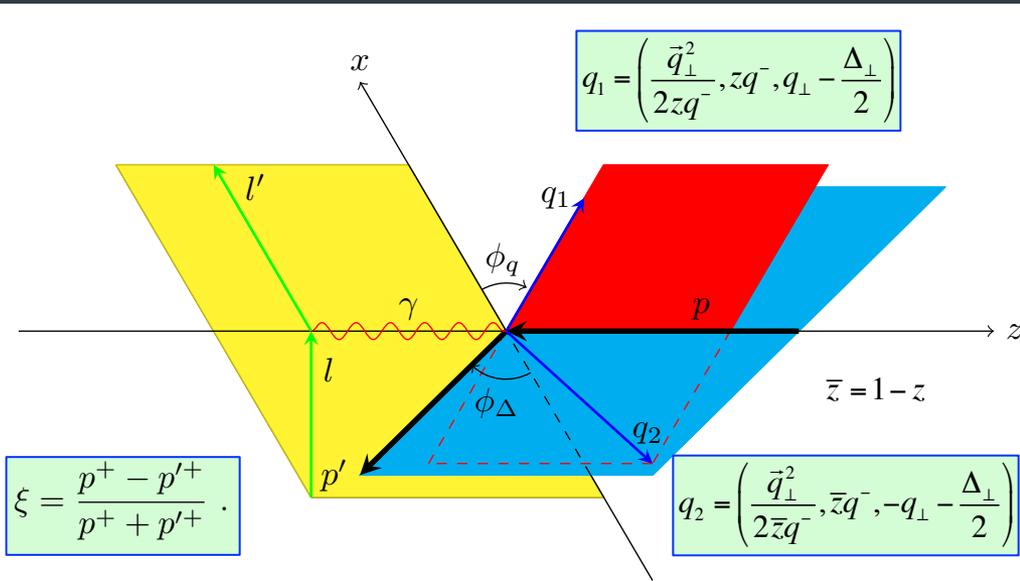
Answer: Exclusive dijet production in $l+p$ scattering ✓

$$l + p \rightarrow l' + q_1 + q_2 + p'$$

Braun and Ivanov, 2005

Hatta, Xiao and Yuan, 2016

Kinematics



$$q = l - l', \quad q^2 = -Q^2$$

$$x_{Bj} = \frac{Q^2}{2q \cdot p}, \quad y = \frac{q \cdot p}{l \cdot p},$$

$$\Delta = p' - p, \quad P = \frac{p + p'}{2},$$

$$t = \Delta^2, \quad (q + p)^2 = W^2,$$

$$(q - \Delta)^2 = (q_1 + q_2)^2 = M^2.$$

$$Q^2 \sim W^2 \sim \vec{q}_\perp^2 \gg \Delta_\perp^2$$

$$\mu^2 = z\bar{z}Q^2, \quad \beta = \frac{\mu^2}{\vec{q}_\perp^2 + \mu^2}$$

Scattering Amplitude

Scattering amplitude:

$$M = \frac{e_{em}}{Q^2} \sum_{\lambda=L,\perp} \bar{u}(l') \not{\epsilon}_\lambda(q) u(l) \epsilon_{\lambda,\nu} M_{\gamma^*}^\nu = \frac{e_{em}}{Q^2} \sum_{\lambda=L,\perp} \bar{u}(l') \not{\epsilon}_\lambda(q) u(l) \mathcal{A}_\lambda$$

Leptonic part, averaging
initial spins and summing
over final spins

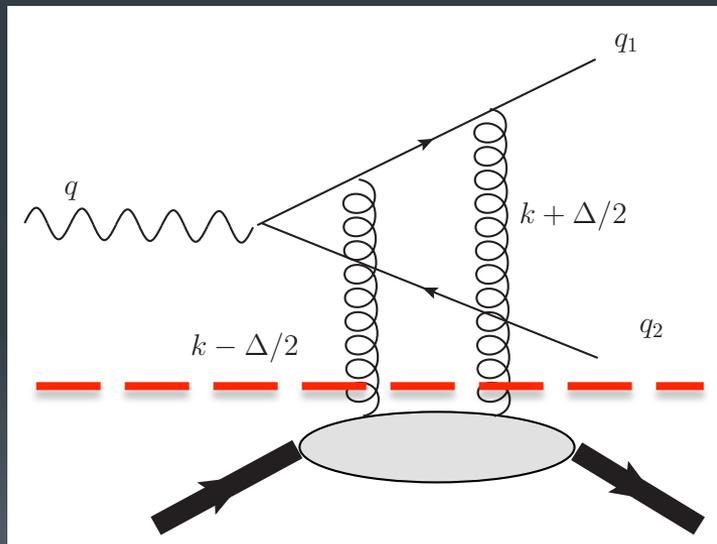
Hadronic part, summing
over final state quark
spins and color

$$\frac{d\sigma}{dydQ^2d\Omega} = \sigma_0 \left[(1-y)|A_L|^2 + \frac{1+(1-y)^2}{2}|A_T|^2 \right]$$

$$\sigma_0 = \frac{\alpha_{em}^2 \alpha_s^2 e_q^2}{16\pi^2 Q^2 y N_c} \frac{4\xi^2 z \bar{z}}{(1-\xi^2)(\vec{q}_\perp^2 + \mu^2)^3}$$

Collinear factorization of hadronic amplitude

- Leading order diagrams (6 in total)
- Collinear Factorization



Hard Part

$$\mathcal{H}(x, \xi, q_{\perp}, k_{\perp}, \Delta_{\perp})$$

Soft Part

$$x f^g(x, \xi, k_{\perp}, \Delta_{\perp})$$

$$i\mathcal{A}_f \propto \int dx d^2k_{\perp} \mathcal{H}(x, \xi, q_{\perp}, k_{\perp}, \Delta_{\perp}) x f^g(x, \xi, k_{\perp}, \Delta_{\perp}),$$

Twist expansion

$$\mathcal{H}(x, \xi, q_{\perp}, k_{\perp}, \Delta_{\perp}) = \mathcal{H}^{(0)}(x, \xi, q_{\perp}, 0, \Delta_{\perp}) + k_{\perp}^{\alpha} \frac{\partial}{\partial k_{\perp}^{\alpha}} \mathcal{H}(x, \xi, q_{\perp}, 0, \Delta_{\perp}) + \dots$$

Twist 2 (Target-spin independent):

Braun and Ivanov, 2005

$$i\mathcal{A}_f^{(0)} \propto \int dx \mathcal{H}^{(0)}(x, \xi, q_{\perp}, 0, 0) x F_g(x, \xi, \Delta_{\perp})$$

Gluon GPD

Twist 3 (Target-spin dependent):

$$\int d^2 k_{\perp} (\vec{q}_{\perp} \cdot \vec{k}_{\perp}) x f^g(x, \xi, k_{\perp}, \Delta_{\perp}) = -i S^+ (\vec{q}_{\perp} \times \vec{\Delta}_{\perp}) x L_g(x, \xi, \Delta_{\perp}) + \dots,$$

Differential cross section

- Result:

$$\Delta\sigma = (\sigma(S^+) - \sigma(-S^+))/2$$

$$\frac{d\Delta\sigma}{dydQ^2d\Omega} = \sigma_0\lambda_p \frac{2(\bar{z} - z)(\vec{q}_\perp \times \vec{\Delta}_\perp)}{\vec{q}_\perp^2 + \mu^2} \left[(1-y)A_{fL} + \frac{1 + (1-y)^2}{2} A_{fT} \right]$$

λ_p Nucleon Polarization

$$A_{fL} = 16\beta \operatorname{Im} \left([\mathcal{F}_g^* + 4\xi^2\bar{\beta}\mathcal{F}_g'^*] [\mathcal{L}_g + 8\xi^2\bar{\beta}\mathcal{L}_g'] \right) ,$$

$$A_{fT} = 2 \operatorname{Im} \left([\mathcal{F}_g^* + 2\xi^2(1-2\beta)\mathcal{F}_g'^*] \left[\mathcal{L}_g + 2\bar{\beta} \left(\frac{1}{z\bar{z}} - 2 \right) (\mathcal{L}_g + 4\xi^2(1-2\beta)\mathcal{L}_g') \right] \right)$$

Generalized Compton Form Factors

- Definition:

$$\mathcal{F}_g(\xi, t) = \int dx \frac{1}{(x + \xi - i\varepsilon)(x - \xi + i\varepsilon)} F_g(x, \xi, t) ,$$

$$\mathcal{F}'_g(\xi, t) = \int dx \frac{1}{(x + \xi - i\varepsilon)^2(x - \xi + i\varepsilon)^2} F_g(x, \xi, t) .$$

$$\mathcal{L}_g(\xi, t) = \int dx \frac{x\xi}{(x + \xi - i\varepsilon)^2(x - \xi + i\varepsilon)^2} xL_g(x, \xi, t) ,$$

$$\mathcal{L}'_g(\xi, t) = \int dx \frac{x\xi}{(x + \xi - i\varepsilon)^3(x - \xi + i\varepsilon)^3} xL_g(x, \xi, t) .$$

- x -dependence cannot be measured:

Needs modelling of the GPD and GTMD;

Real part: principle value integration. Imaginary part: $F(\xi, \pm\xi, t), L(\xi, \pm\xi, t)$.

Single longitudinal target-spin asymmetry

- Definition:

$$A_{\sin(\phi_q - \phi_\Delta)} = \int d\phi_q d\phi_\Delta \frac{d\sigma_\uparrow - d\sigma_\downarrow}{d\phi_q d\phi_\Delta} \sin(\phi_q - \phi_\Delta) \bigg/ \int d\phi_q d\phi_\Delta \frac{d\sigma_\uparrow + d\sigma_\downarrow}{d\phi_q d\phi_\Delta}$$

$$A_{\sin(\phi_q - \phi_\Delta)} \propto \frac{(\bar{z} - z) |\vec{q}_\perp| |\vec{\Delta}_\perp|}{\vec{q}_\perp^2 + \mu^2}$$

- Feature:

Asymmetric jets

Suppressed effect $O(\Delta_T/Q)$

Similar observable in the same process at small x :

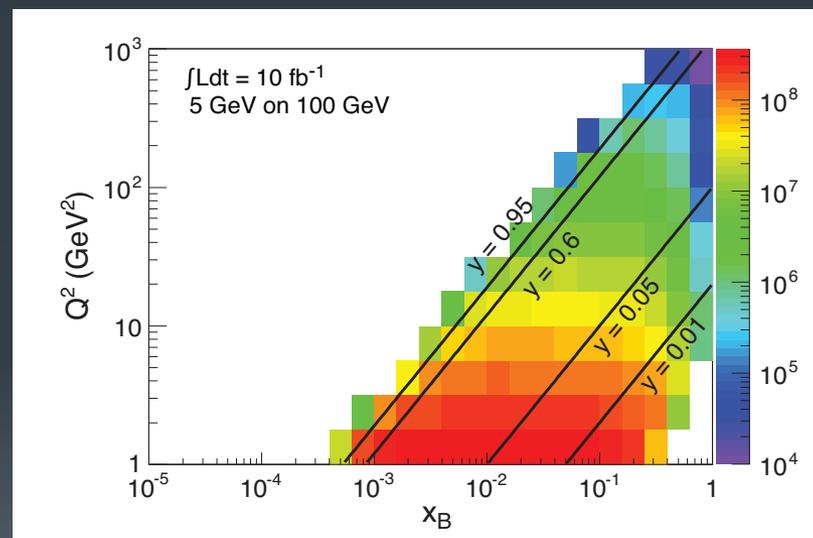
Hatta, Nakagawa, Yuan and Y.Z., 2016
double exclusive Drell-Yan:

Bhattacharya, Metz, and Zhou, 2017

Hatta, Bhattacharya's talks

Measurement at EIC

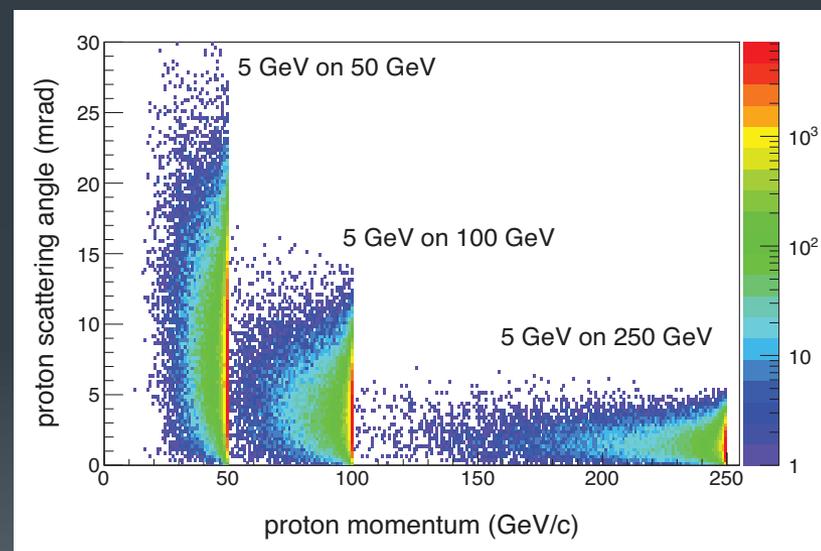
- Key measurements:
 - Dijet momenta
 - Final state nucleon momentum
- Kinematics:
 - Large Bjorken x , high Q^2 ;
 - Nucleon deflection angle (determines t and ξ).



A. Accardi et al., arXiv: 1212.1701

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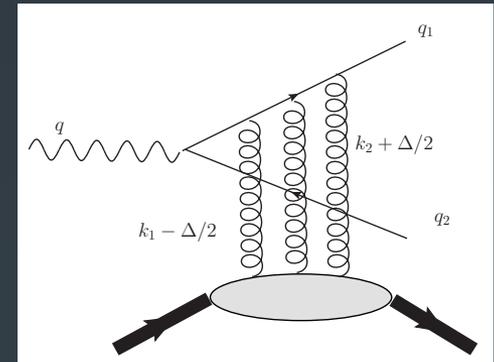


A. Accardi et al., arXiv: 1212.1701

Outlook

Remaining issues:

- Include genuinely twist-three diagrams;
- One-loop radiative corrections, test validity of collinear factorization



After all, the leading contribution to the single target-spin asymmetry is strongly sensitive to the gluon OAM!

Summary

- Gluon OAM in the Jaffe-Manohar sum rule can be measured through the Wigner distribution;
- The leading contribution to the single longitudinal target-spin asymmetry in exclusive dijet production from ep scattering is strongly sensitive to the gluon OAM.
- Differential cross section formula has been derived for the experimental observable.