Electroweak physics with inclusive DIS at the LHeC and FCC-eh

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for the LHeC study group

DIS 17

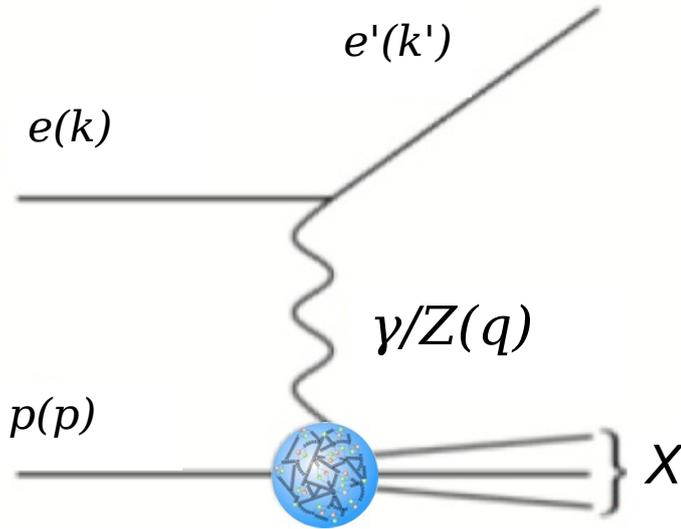25th International Workshop on Deep Inelastic Scattering and Related Topics
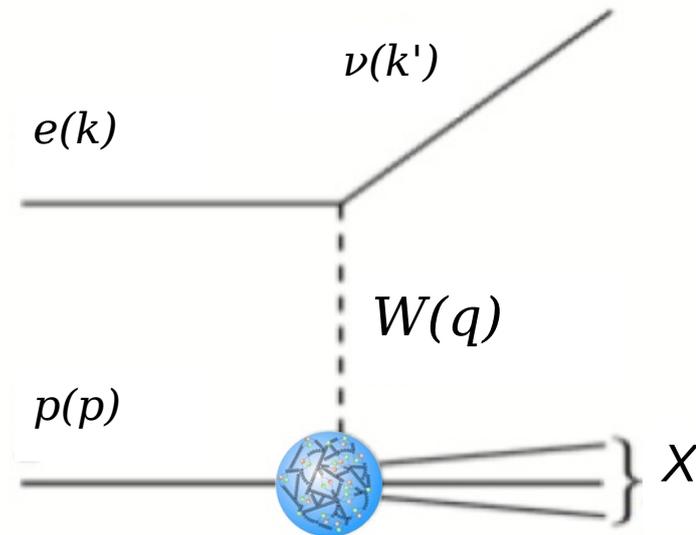Birmingham, UK
05.04.2017

Deep-inelastic electron-proton scattering

Neutral current scattering
$ep \rightarrow e'X$

Charged current scattering
$ep \rightarrow \nu_e X$

R-D. Heuer

"The point-like electron "probes" the interior of the proton via the <u>electroweak force</u>, while acting as a neutral observer with regard to the <u>strong force</u>."

-> Both: Electroweak (EW) and QCD physics are equally important at LHeC (?)

Electroweak effects at HERA

Inclusive DIS as a function of Q²

Lower values of Q²
- NC significantly larger than CC
- CC is mediated only by massive W-boson
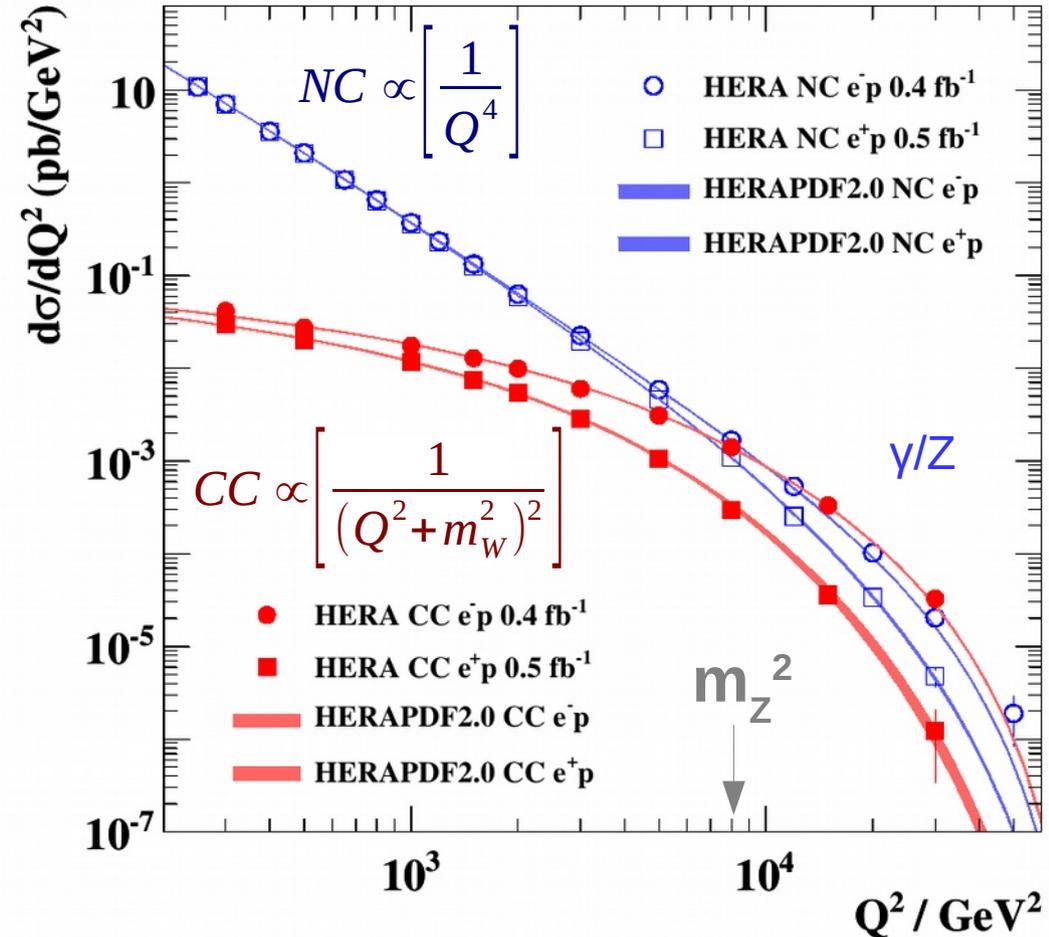- NC: e+p and e-p are identical for photon exchange

Around EW unification scale
- NC and CC of similar size
- $Q^2 \sim m_Z^2 \sim 8000$ GeV²

W and Z-exchange: e+p and e-p differ
- NC: γ/Z-interference differ for e+ and e-
- For CC e+:
  Helicity factor $(1-y)^2$ applies to d-quarks

$$NC \propto \left[\frac{1}{Q^4} \right]$$

$$CC \propto \left[\frac{1}{(Q^2 + m_W^2)^2} \right]$$

HERA NC e⁻p 0.4 fb⁻¹
HERA NC e⁺p 0.5 fb⁻¹
HERAPDF2.0 NC e⁻p
HERAPDF2.0 NC e⁺p
HERA CC e⁻p 0.4 fb⁻¹
HERA CC e⁺p 0.5 fb⁻¹
HERAPDF2.0 CC e⁻p
HERAPDF2.0 CC e⁺p

Electroweak effects in NC DIS

Cross section expressed by generalised structure functions

$$\frac{d\sigma^{\pm}_{NC}}{dQ^2 dx} = \frac{2\pi\alpha^2}{x}\left[\frac{1}{Q^2}\right]^2 (Y_+ F_2 + Y_- x F_3 + y^2 F_L)$$

$$F_2 = F_2^{\gamma} + \kappa_Z(-v_e \mp Pa_e)F_2^{\gamma Z} + \kappa_Z^2(v_e^2 + a_e^2 \pm Pv_e a_e)F_2^Z$$

$$x F_3 = +\kappa_Z(\pm a_e + Pv_e)F_3^{\gamma Z} + \kappa_Z^2\left(\mp 2v_e a_e - P(v_e^2 + a_e^2)\right)x F_3^Z$$

Quark-parton model

$$\left[F_2, F_2^{\gamma Z}, F_2^Z\right] = x\sum_q \left[e_q^2, 2e_q v_q, v_q^2 + a_q^2\right]\{q + \bar{q}\}$$

$$\left[xF_3^{\gamma Z}, xF_3^Z\right] = x\sum_q \left[2e_q a_q, 2v_q a_q\right]\{q - \bar{q}\}$$

	e^2	$2ev$
u	4/9	2/9
d	1/9	2/9

EW scheme

$$\kappa_Z(Q^2) \simeq \frac{Q^2}{Q^2 + m_Z^2}\frac{G_F m_Z^2}{2\sqrt{2}\pi\alpha}$$

$$\kappa_Z(Q^2) = \frac{Q^2}{Q^2 + m_Z^2}\frac{1}{4\sin^2\theta_W \cos^2\theta_W}$$

$$(1 + \Delta r)$$

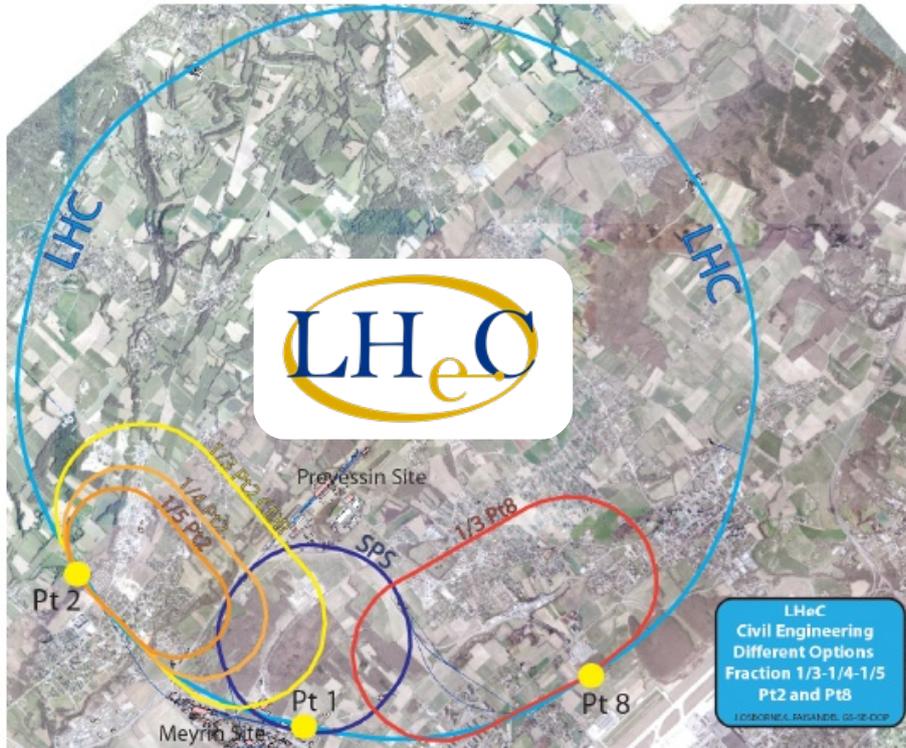**NC DIS cross sections:** *γγ, γZ, ZZ exchange*
- *axial-vector & vector couplings (a,v): parity violation if both are present*

CC DIS: *purely weak cross sections (G_F, m_W)*

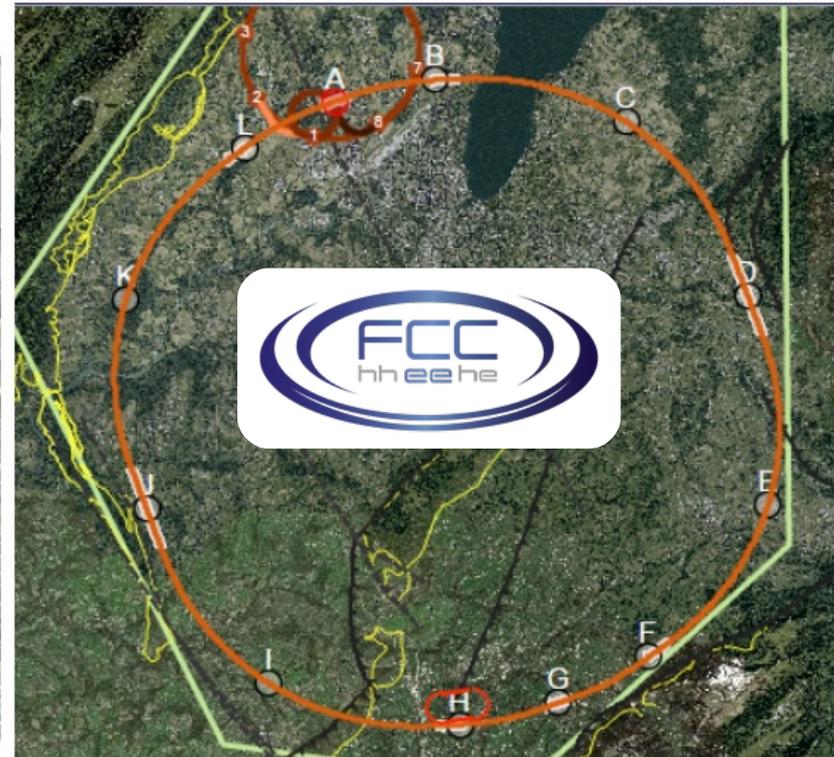*3 independent variables at born-level in DIS, e.g OMS: (α, m_W, m_Z, Δr)*

Future proposed ep-colliders: LHeC & FCC-eh

Electron ring

- Energy recovery linac: $E_e = 60$ GeV
- Polarisation up to $P_e \sim 80\%$
- Similar concept for LHeC & FCC-eh

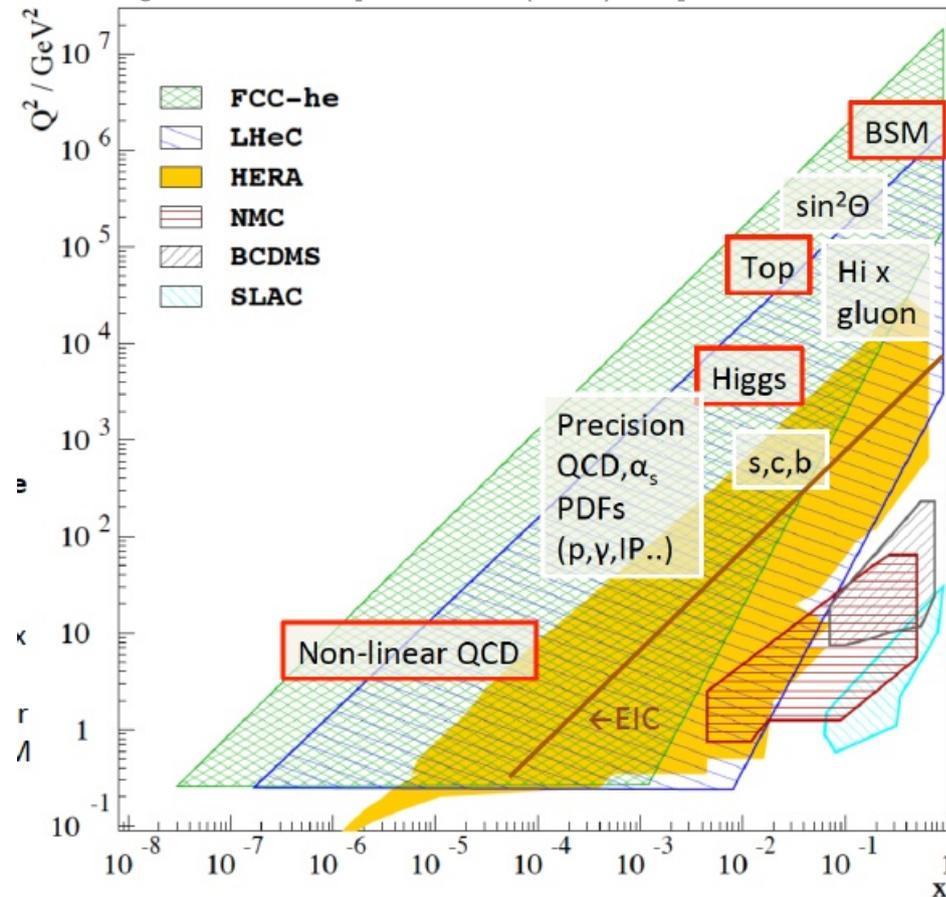**Center-of-mass energies**

- LHeC: $\sqrt{s} \sim 1.3$ TeV
- FCC-eh: $\sqrt{s} \sim 3.5$ TeV
- Up to 1 ab^{-1} integrated luminosity

LHeC & FCC-eh: Large kinematic range

e.g.: P. Newman [NPPS 191 (2009) 307]

Comprehensive physics programme
- Higgs physics
- Top-Quark (properties, top-PDFs)
- Heavy-quarks (s,c,b-quarks)
- low-x physics (non-linear QCD?), also e-Ion
- Precision QCD physics (strong coupling, PDFs)
- Electroweak physics...

Huge increase of kinematical reach over previous DIS experiments

Simulated data sets

Simulated <u>neutral and charged current</u> cross sections

- Pseudo-data applicable for both: EW and QCD studies

Correlated and uncorrelated syst. and stat. errors

- Numerical treatment of errors [PHE-1990-02, J. Blümlein, M. Klein]

source of uncertainty	error on the source or cross section
scattered electron energy scale $\Delta E'_e / E'_e$	0.1 %
scattered electron polar angle	0.1 mrad
hadronic energy scale $\Delta E_h / E_h$	0.5 %
calorimeter noise (only $y < 0.01$)	1-3 %
radiative corrections	0.5%
photoproduction background (only $y > 0.5$)	1 %
global efficiency error	0.7 %

- Assumptions gauged with H1 (best achieved values)
- Total cross section errors typically: 0.8% at low-x, and 2% at high-x
- Simulated data have full systematic error
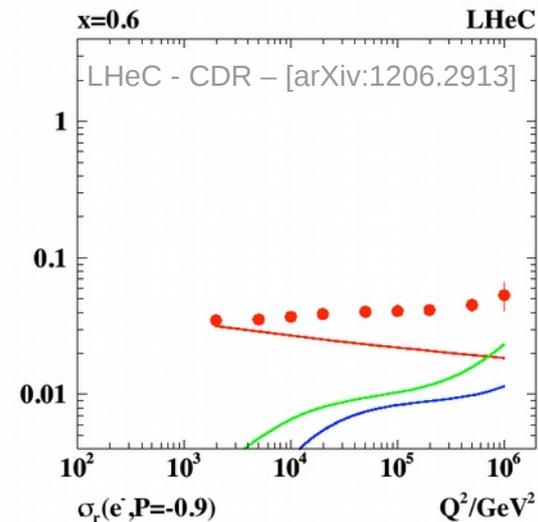- Luminosity measurement ~1% (0.5% may be reachable)

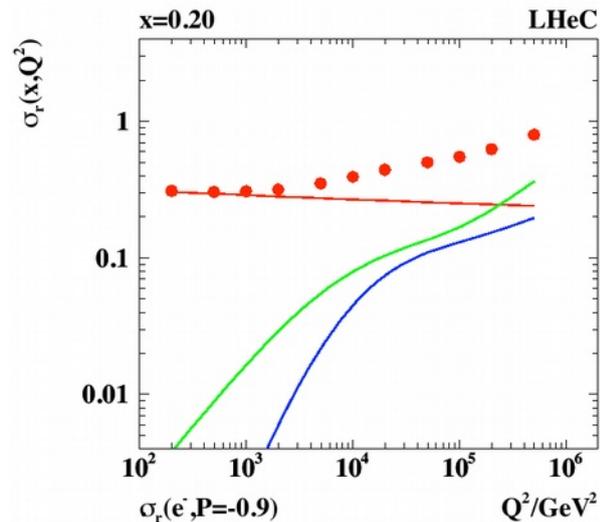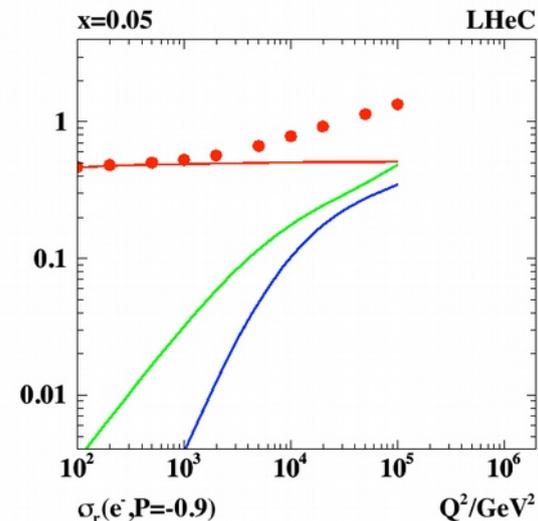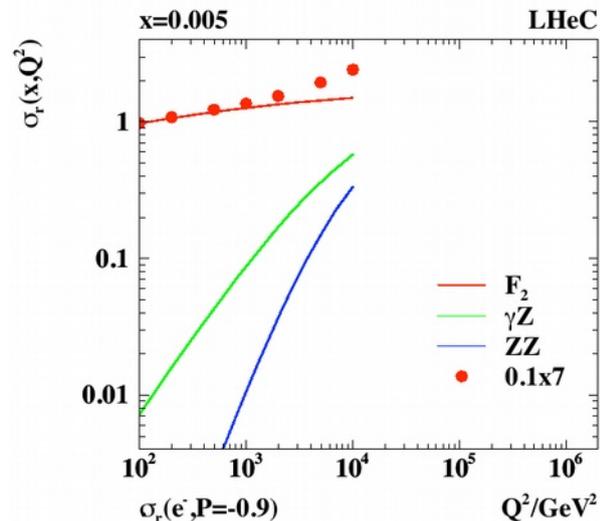# Reduced NC e⁻p scattering cross sections

Reduced cross sections

$$\frac{d^2\sigma_{NC}}{dxdQ^2} = \frac{2\pi\alpha^2 Y_+}{Q^4 x} \cdot \sigma_{r,NC}$$

Huge Z exchange effects

- starting around EW scale
- $Q^2 > 1000$ GeV^2

- Interference effects
- Z-exchange

Cross section raises for high-x due to EW effects

- Contrary to HERA:
  x ~ 0.2 'scaling'
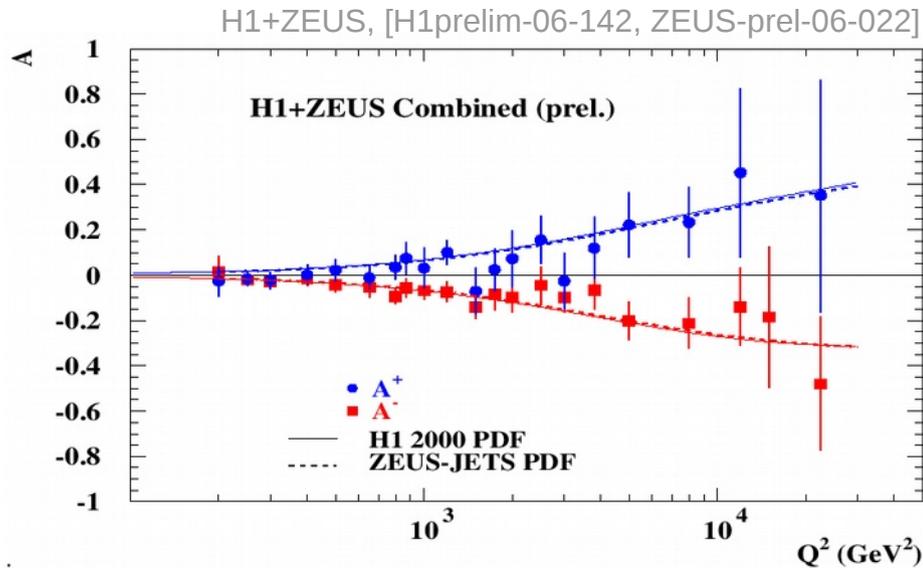 x > 0.2 gluon bremsstrahlung

NC DIS Polarisation asymmetry

Polarisation asymmetry

- Z-exchange as a function of Q^2

$$A^{\pm} = \frac{2}{P_L^{\pm} - P_R^{\pm}} \cdot \frac{\sigma^{\pm}(P_L^{\pm}) - \sigma^{\pm}(P_R^{\pm})}{\sigma^{\pm}(P_L^{\pm}) + \sigma^{\pm}(P_R^{\pm})}$$
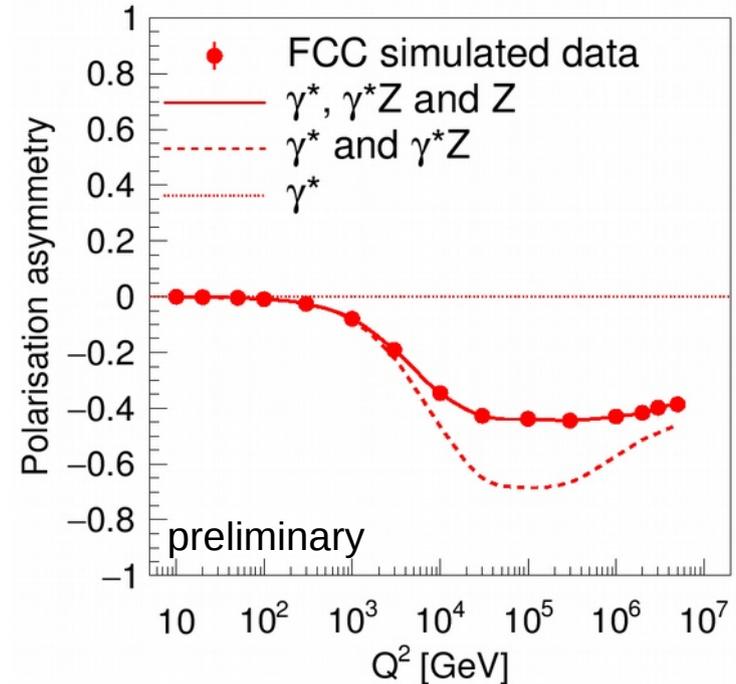
- Parity violation effects in NC EW interactions

H1+ZEUS, [H1prelim-06-142, ZEUS-prel-06-022]

Cross section asymmetry as a function of Q^2

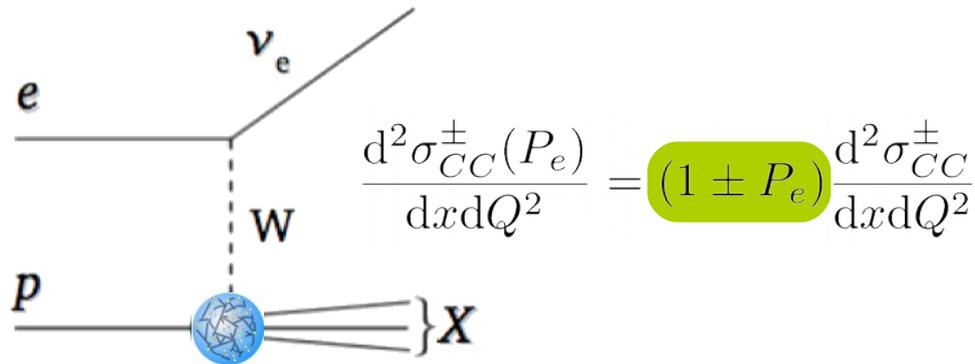## *Polarisation asymmetry at LHeC & FCC*

- At large *x*:
  $A^{\pm}$ measures d_v/u_v ratio of valence quarks

Differences btw. left- and right-handed NC DIS are expressed by $F_2^{\gamma Z}$ and $F_3^{\gamma Z}$
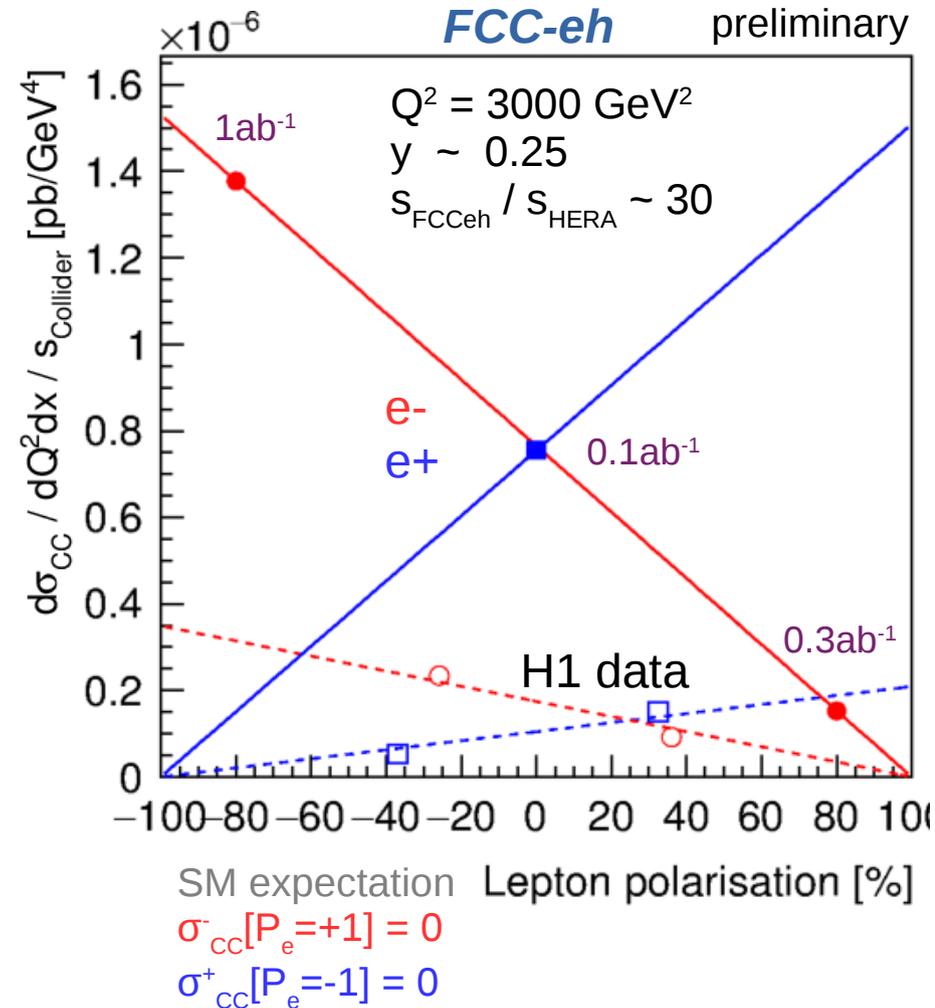
Polarised Charged Current DIS

$$\frac{\mathrm{d}^2\sigma^{\pm}_{CC}(P_e)}{\mathrm{d}x\,\mathrm{d}Q^2} = (1 \pm P_e)\frac{\mathrm{d}^2\sigma^{\pm}_{CC}}{\mathrm{d}x\,\mathrm{d}Q^2}$$

CC depends on *longitudinal polarisation*
- W-boson couples only to left-handed particles

LHeC and FCC
- Huge cross section due to √s
- For fixed (Q2,y), increase due lower x values
  - -> Gluon induced processes
  - -> Helicity effects important at high-x (only)

Most data: electrons with P~-80%

FCC-eh preliminary

$Q^2 = 3000$ GeV^2
$y \sim 0.25$
$s_{FCCeh} / s_{HERA} \sim 30$

1ab^{-1}

e-
e+

0.1ab^{-1}

0.3ab^{-1}

H1 data

dσ_{CC} / dQ^{2}dx / s$_{Collider}$ [pb/GeV^4]

Lepton polarisation [%]

SM expectation
$\sigma^{-}_{CC}[P_e=+1] = 0$
$\sigma^{+}_{CC}[P_e=-1] = 0$

Study of EW parameters - methodology

Determination of EW parameters from '<u>combined fit: EW+PDF</u>'
- account for correlations to PDF uncertainties,
  since these are also determined from DIS data

For this study
- Employ only <u>inclusive NC and CC DIS</u> data
- <u>No direct measurements</u> of real Z/W-bosons (or t, H)
- -> significant improvements expected if direct measurements are further considered

HERA or published results as reference
- H1+ZEUS combined data (unpolarized) (EPJ C75 (2015) 2)

LHeC and FCC-eh: Simulated NC&CC DIS data
- e-   +80%, -80%
- e+   unpolarised
- FCC: low-$\sqrt{s}$ unpolarised electron-data

Electroweak parameters in inclusive DIS

Fitting methodology

- QCD (PDF) fit in NLO precision using ZM-VFNS using QCDNUM
  - 13 free PDF parameters
  - details of PDF fit are only of minor importance,
    because PDF fit is used only used to determine PDF uncertainties
    on EW parameters

EW calculations

- Calculations are performed in on-mass shell scheme:
  $(\alpha_{em}, m_Z, m_W, \Delta r)$ with $\Delta r = \Delta r(\alpha_{em}, m_W, m_Z, m_t, m_H, ...)$
- More general, also <u>vector</u> and <u>axial-vector couplings</u> are 'free'
  parameters
- Dependence on m_t and m_H through loop-corrections (Δr)
- $\sin^2\theta_W$ and g_f are calculated quantities and thus no free parameters

Weak-boson masses

Z-boson mass from EW+PDF fit to inclusive NC&CC DIS data

- on-shell definition
- all other masses expected to be known
- PDFs are determined as well

Z-boson mass

- HERA $(56)_{exp}(25)_{PDF}$
- LHeC $(16)_{exp}(10)_{PDF}$
- FCC $(11)_{exp}(3)_{PDF}$
- PDF uncertainties beome negligibly small (outer errors)

-> Measurement of Z-boson mass not limited by PDFs
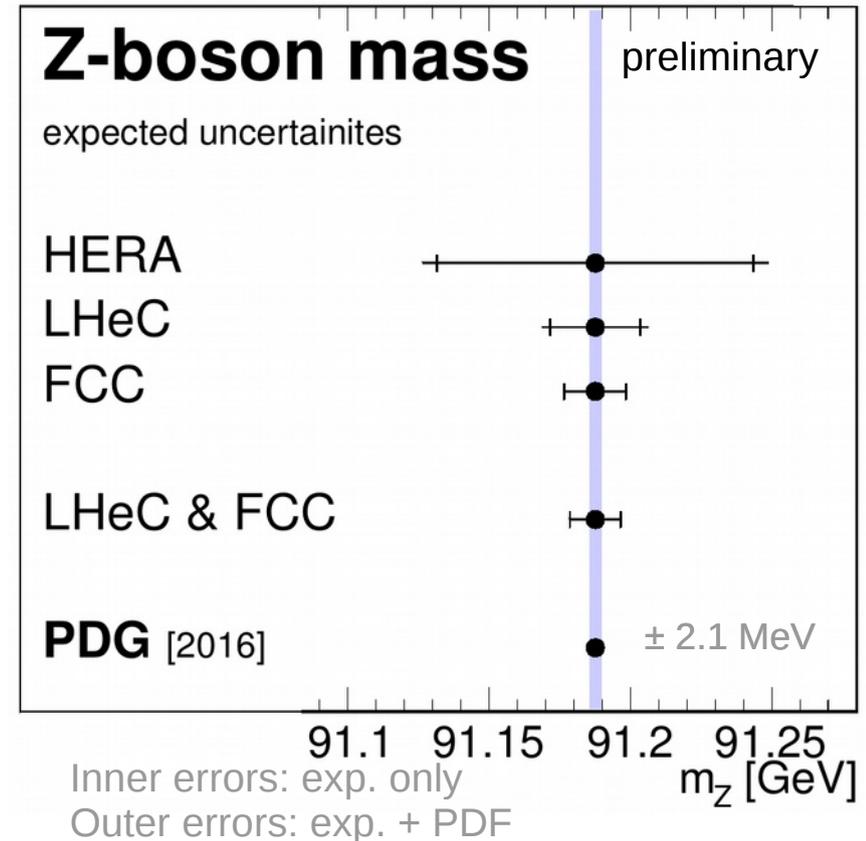
Weak-boson masses

W-boson mass from NC&CC DIS data

- All other masses expected to be known
- HERA $\pm 63_{(exp)} 29_{(PDF)}$
- LHeC $\pm 14_{(exp)} 10_{(PDF)}$
- FCC $\pm 9_{(exp)} 4_{(PDF)}$
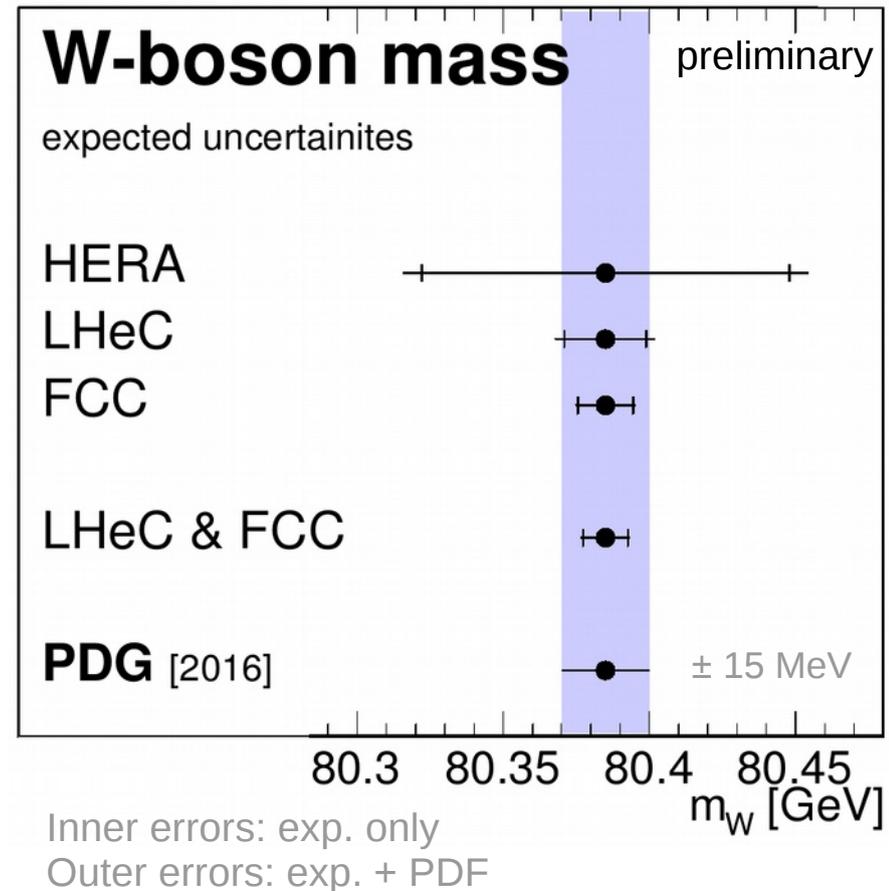
> HERA prospects (1987)
> $m_W \sim \pm$ 80-100 MeV
> Our HERA value
> $m_W \sim \pm 63_{(exp)} 29_{(PDF)}$

Competitive W-boson mass

- CC kinematics constraint by IS + FS measurements
  -> no missing E_T needed !!
- PDF uncertainties are small

W-boson masss at high precision

W-boson mass preliminary

expected uncertainites

HERA
LHeC
FCC

LHeC & FCC

PDG [2016] ± 15 MeV

80.3 80.35 80.4 80.45
m_W [GeV]

Inner errors: exp. only
Outer errors: exp. + PDF

(Indirect) determination of boson masses

W- and Z-boson masses: Most important input parameters to EW calculation

FCC/LHeC
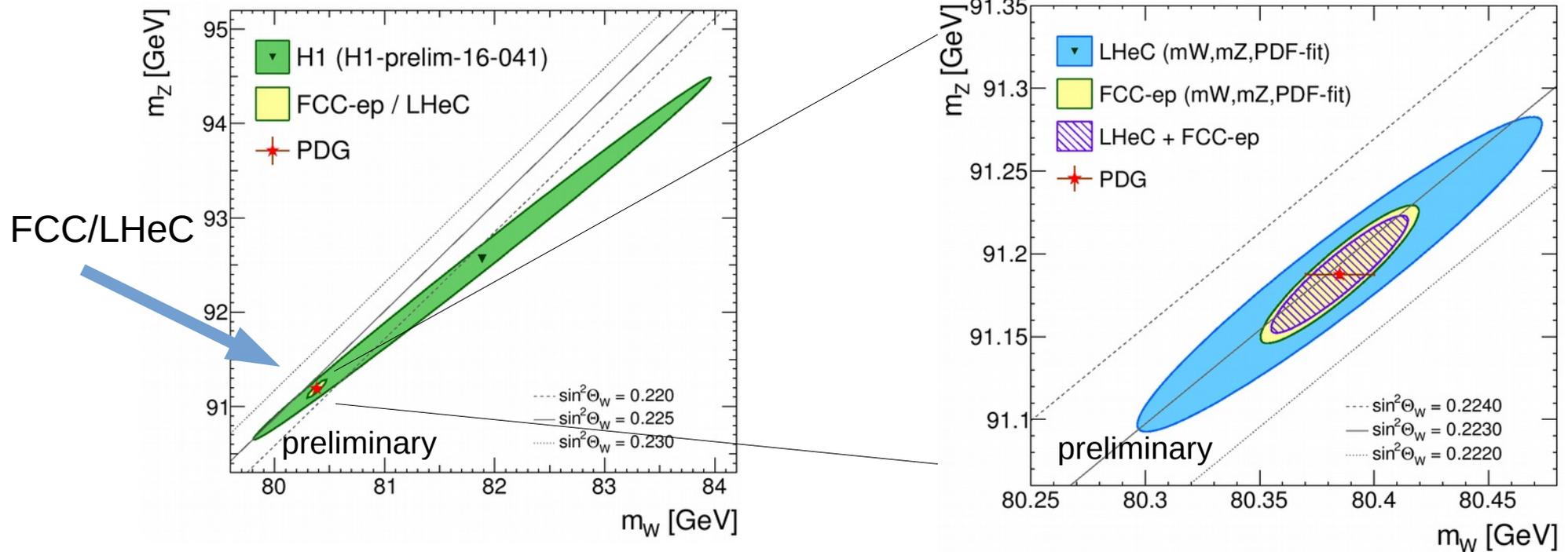
- LHeC & FCC: Greatly improved precision as compared to HERA
  - Benefit from increadibly higher cross sections than HERA
  - Correlation between m_W and m_Z will be reduced with increasing scale (FCC) -> higher precision
- HERA with large uncertainty due to m_W-m_Z correlation (H1-prelim-16-041)
- PDFs will not be the limiting factor for EW physics !

W-boson and top-mass

Top mass and W-boson mass
- Highly correlated
- Very sensitive to BSM physics 'holy grail' of EW physics

m_W-m_t determinations
- large correlation (as expected)
- significant improvement over LEP+SLD results expected
- PDF uncertainties will not be limiting factors
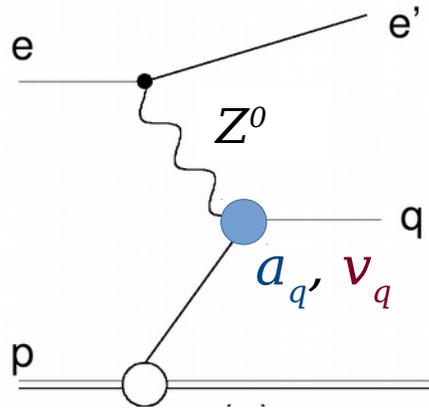
This is only from inclusive DIS !
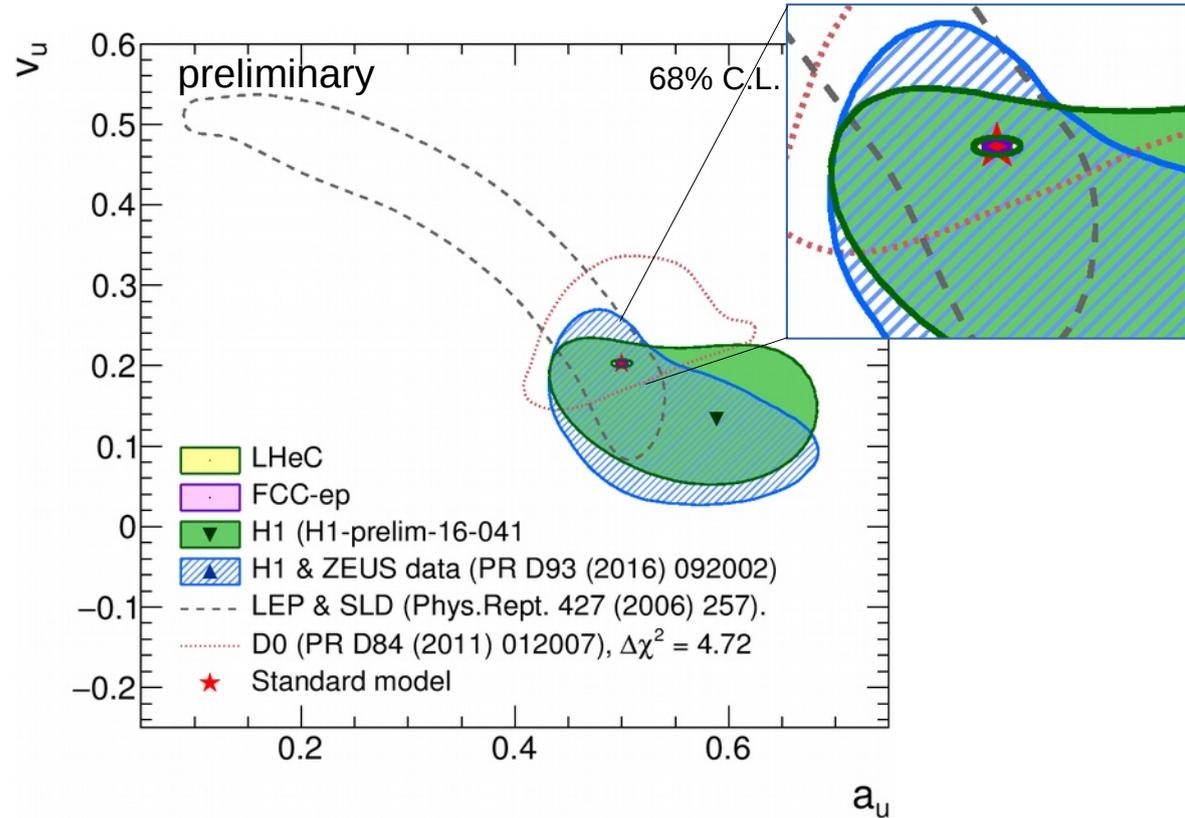- -> additional measurements of top or W-boson production will be allow for significant improvements
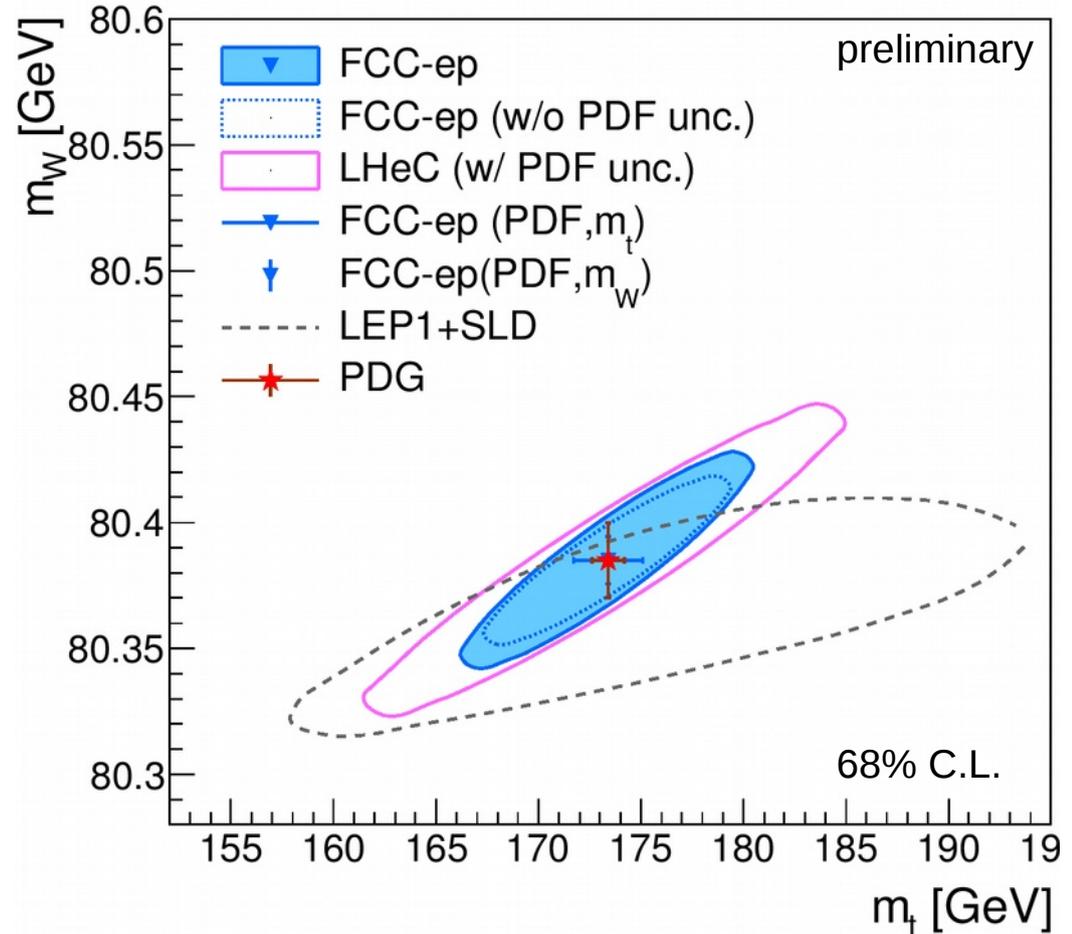
Light quark couplings at LHeC and FCC-eh

**Axial *and* vector-axial *couplings of quarks*
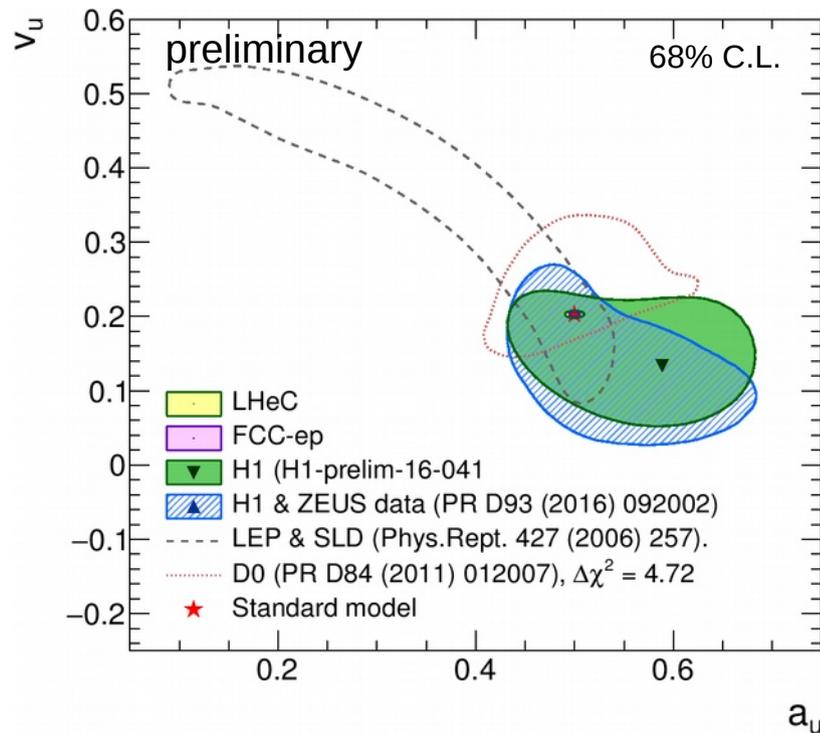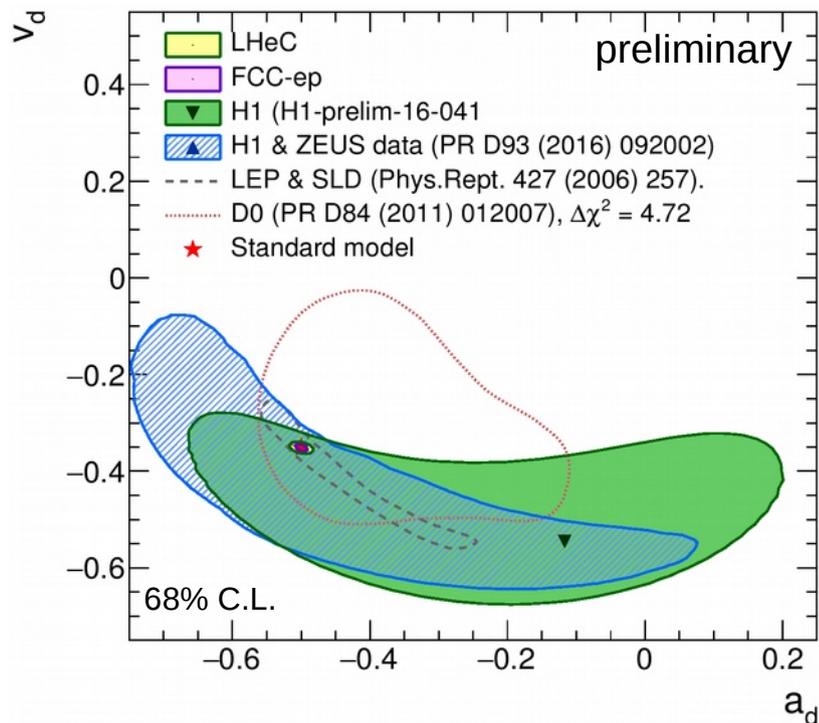
- Couplings of quarks to Z-boson

$$a_q = I^{(3)}_{q,L} \qquad v_q = I^{(3)}_{q,L} - 2 Q_q \sin^2 \theta_W$$

LHeC and FCC-ep
- Polarisation of lepton beam ($P_e \sim \pm 80\%$) improves precision
- Very precise measurements of weak light-quark couplings feasible

Light quark couplings at LHeC and FCC-eh

LHeC and FCC-ep

- Up-quark and down-quark couplings determined simultaneously
- Very precise measurements of weak light-quark couplings feasible

$$a_u = 0.5 +/- 0.003$$
$$a_d = -0.5 +/- 0.005$$
$$v_u = 0.20 +/- 0.002$$
$$v_d = -0.35 +/- 0.005$$

High precision test of electroweak sector of Standard Model

Weak mixing angle

Weak mixing angle

- on-shell scheme:
  No scale dependence
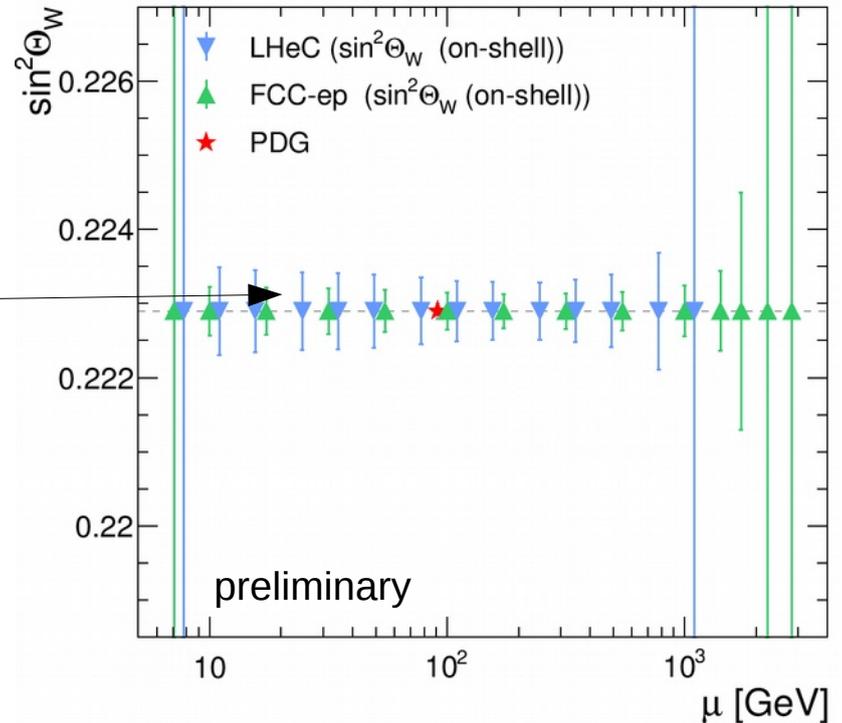
$$\sin^2\theta_W = 1 - \frac{m_W^2}{m_Z^2}$$

Weak mixing angle

- Expected precision:

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LHeC   ±0.0003(exp) 0.0002(PDF)
FCC    ±0.0002(exp) 0.00008(PDF)
PDG    ±0.00010
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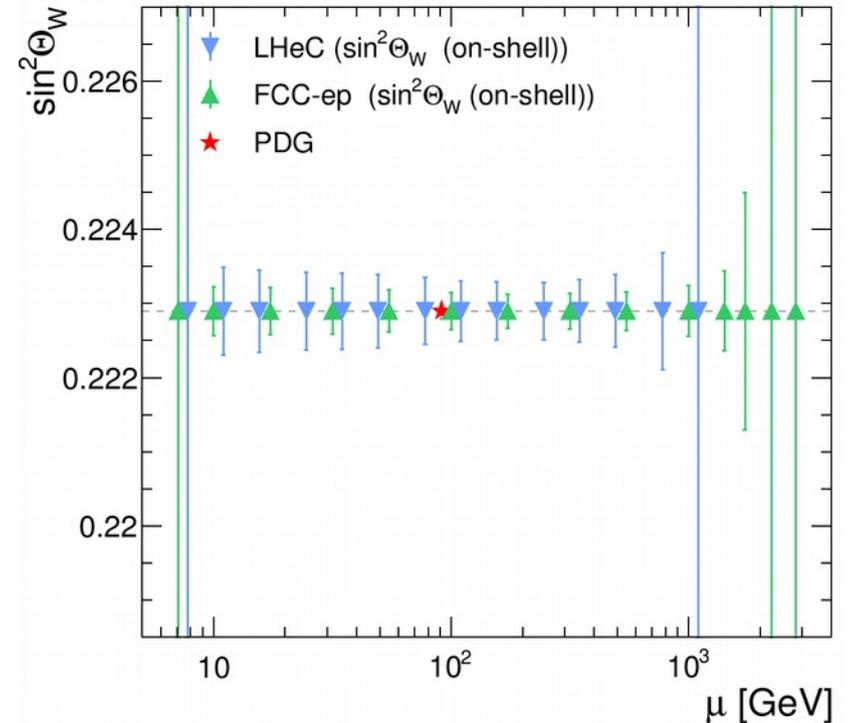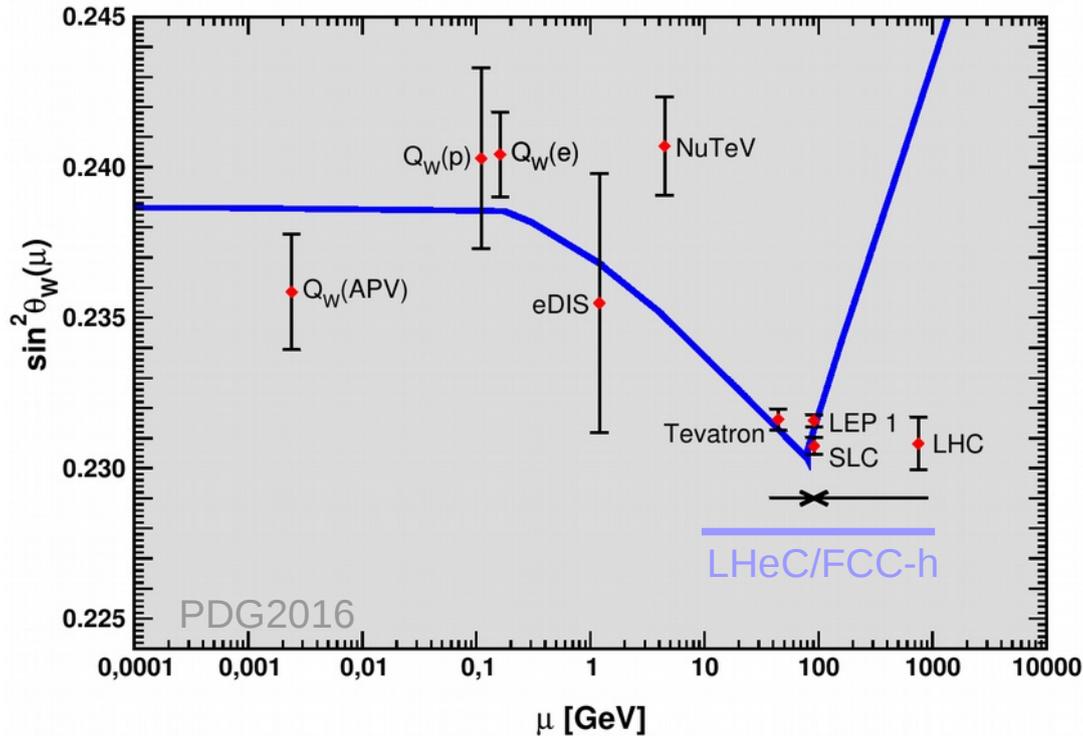
- Inclusive data will be competitive to direct measurements at the Z-pole

Δm_W ~10-15 MeV over a wide range

Inclusive DIS data from LHeC and FCC-ep probes scale dependence of EW theory in impressive range from 10 GeV up to TeV scale
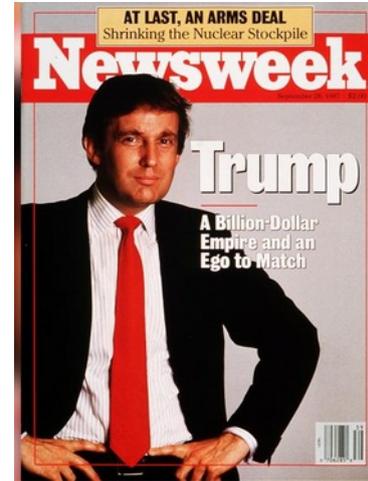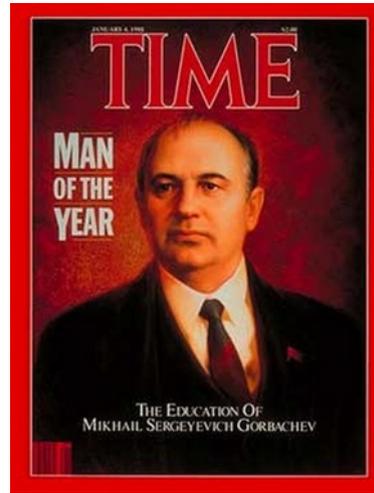
Weak mixing angle

PDG2016

on-shell translated to

- MS-bar definition or 'effective' weak mixing angle

Precise tests of weak mixing angle over a large scale range
At EW-scale: complementary to s-channel extractions

30 years ago: 1987

LHeC and **FCC**

Summarizing, ~~HERA~~ should allow for meaningful tests of the electroweak theory, complementary to e^+e^--colliders and more accurate than presently operating fixed target or $\bar{p}p$-experiments.

J. Blümlein, M. Klein, T. Riemann, Conference: C87-05-25 (Warsaw Sympos (1987) 39 & DESY HERA Workshop (1987) 687

Conclusions

Studies of EW parameters using simulated LHeC and FCC-eh data
- *Complementary regime to LEP and LHC (space-like momentum transfer)*

LHeC and FCC-eh inclusive DIS data
- *Precision of EW parameters will greatly improve HERA results*
- *Competitive with LEP+SLD results in case of indirect determinations*
- *'ultimate' measurement of weak couplings of light-quarks*
- *Competitive measurements of the W-boson mass*

```
DESY    -> CERN
EUR     -> CHF
PETRA   -> LEP
HERA    -> LHeC
```

EW physics
- *High accuracy over impressive range from 10 GeV up to the TeV regime*

Expected precision
- *PDFs will not be the limiting factor for EW studies*
- *Additional direct measurements (e.g. Z, W, top, H production) will support the indirect determinations (not studied here)*

New physics beyond the SM may show up at large momentum transfers or in precision Standard Model measurements