

Implications of low-scale strings to LHC and the early Universe

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and

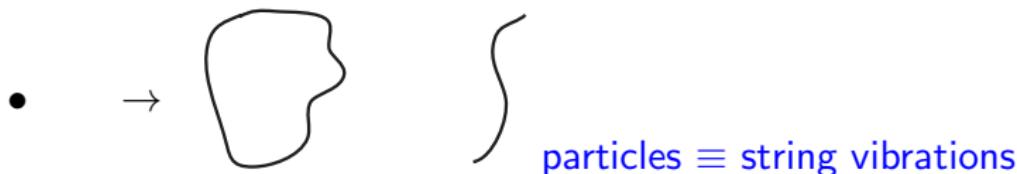
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Physics in LHC and the Early Universe

University of Tokyo, Japan, 9-11 January 2017

String theory: Quantum Mechanics + General Relativity

point particle → extended objects



- quantum gravity
- framework of unification of all interactions
- “ultimate” theory:
 - ultraviolet finite
 - no free parameters

mass scale (tension): $M_{\text{string}} \leftrightarrow$ size: l_{string}

rigid string : known particles (massless)

vibrations : infinity of massive particles

Main predictions of String Theory

→ inspirations for BSM physics

Consistency of the Theory ⇒

- Spacetime supersymmetry but arbitrary breaking scale
- Extra dimensions of space six or seven in M-theory
- Brane-world description of our Universe
 - matter and gauge interactions may be localised in less dimensions
 - p -brane: extended in p spatial dimensions

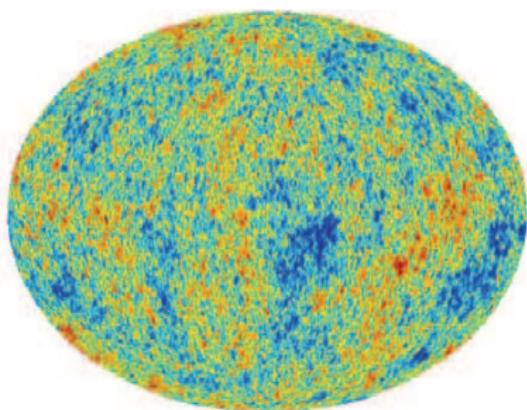
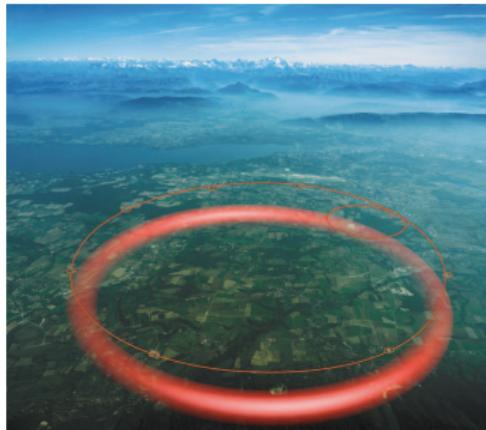
$p = 0$: particle, $p = 1$: string, ...

⇒ Two types of new dimensions:

- ① longitudinal: along the brane-world \Rightarrow $R_{\parallel} \lesssim 10^{-16}$ cm
- ② transverse: only gravitational signal \Rightarrow $R_{\perp} \lesssim 0.1$ mm
- Landscape of vacua

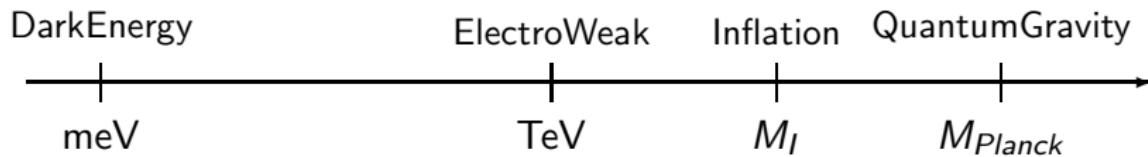
Connect string theory to the real world

- Is string theory a tool for strong coupling dynamics
or a theory of fundamental forces?
- If theory of Nature can string theory describe
both particle physics and cosmology?



Problem of scales

- describe high energy (**SUSY?**) extension of the Standard Model
unification of all fundamental interactions
 - incorporate Dark Energy
simplest case: infinitesimal (tunable) +ve cosmological constant
 - describe possible accelerated expanding phase of our universe
models of inflation (approximate de Sitter)
- ⇒ 3 very different scales besides M_{Planck} :



At what energies strings may be observed?

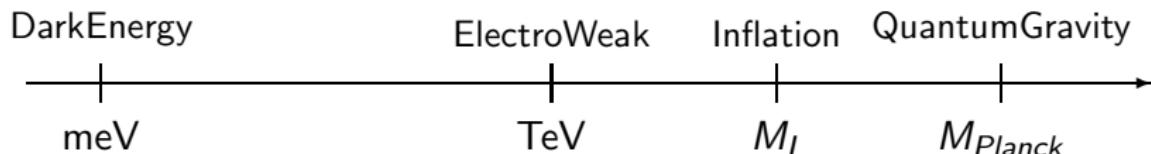
Very different answers depending mainly on the value of the string scale M_s

Before 1994: $M_s \simeq M_{\text{Planck}} \sim 10^{18} \text{ GeV}$ $l_s \simeq 10^{-32} \text{ cm}$ After 1994:

- arbitrary parameter : Planck mass $M_P \longrightarrow \text{TeV}$
- physical motivations \Rightarrow favored energy regions:

- High :
$$\begin{cases} M_P^* \simeq 10^{18} \text{ GeV} & \text{Heterotic scale} \\ M_{\text{GUT}} \simeq 10^{16} \text{ GeV} & \text{Unification scale} \end{cases}$$
- Intermediate : around 10^{11} GeV ($M_s^2/M_P \sim \text{TeV}$)
SUSY breaking, strong CP axion, see-saw scale
- Low : TeV (hierarchy problem)

Problem of scales



① possible connections

- M_I could be near the EW scale, such as in Higgs inflation
but large non minimal coupling to explain
- M_{Planck} could be emergent from the EW scale
in models of low-scale gravity and TeV strings

What about M_I ? can it be at the TeV scale?

Can we infer M_I from cosmological data? [25]

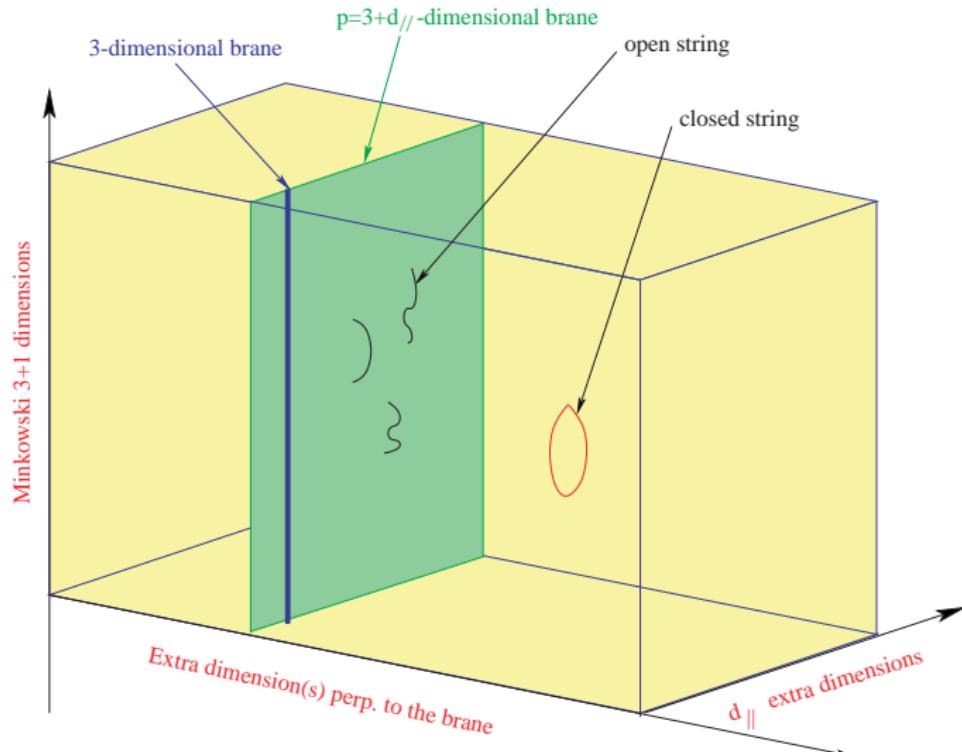
I.A.-Patil '14 and '15

② they are independent

Braneworld

2 types of compact extra dimensions:

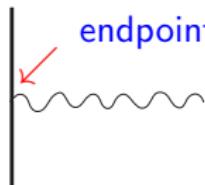
- parallel (d_{\parallel}): $\lesssim 10^{-16}$ cm (TeV) [14]
- transverse (\perp): $\lesssim 0.1$ mm (meV)



D-brane spectrum

Generic spectrum: N coincident branes $\Rightarrow U(N)$

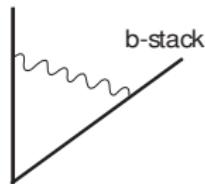
a-stack



endpoint transformation: N_a or \bar{N}_a $U(1)_a$ charge: +1 or -1
 \Rightarrow "baryon" number

- open strings from the same stack \Rightarrow adjoint gauge multiplets of $U(N_a)$
- stretched between two stacks \Rightarrow bifundamentals of $U(N_a) \times U(N_b)$

a-stack



non-oriented strings \Rightarrow also:

- orthogonal and symplectic groups $SO(N), Sp(N)$
- matter in antisymmetric + symmetric reps

Minimal Standard Model embedding

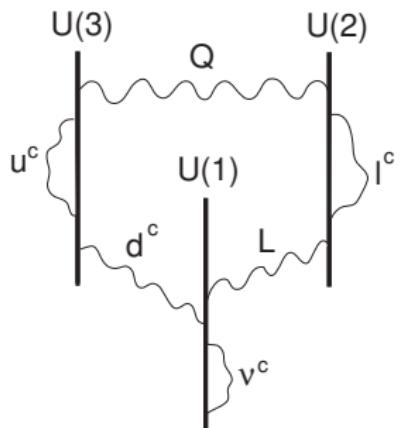
General analysis using 3 brane stacks [21]

$$\Rightarrow U(3) \times U(2) \times U(1)$$

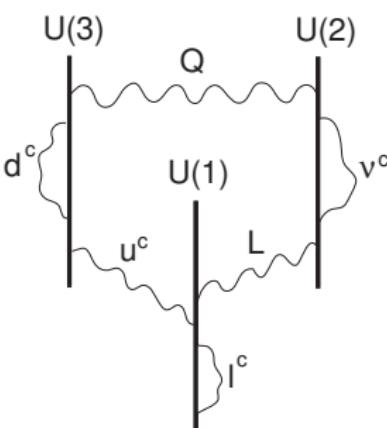
antiquarks u^c, d^c ($\bar{3}, 1$) :

antisymmetric of $U(3)$ or bifundamental $U(3) \leftrightarrow U(1)$

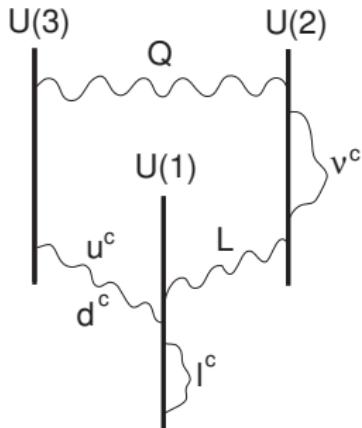
\Rightarrow 3 models: antisymmetric is u^c, d^c or none



Model A

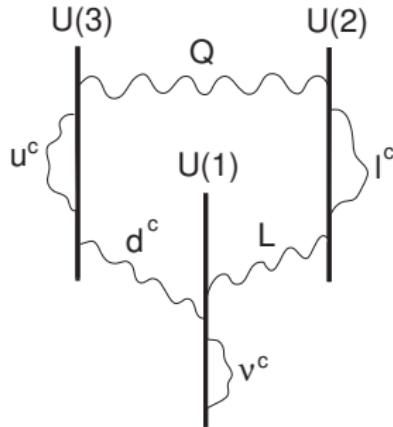


Model B

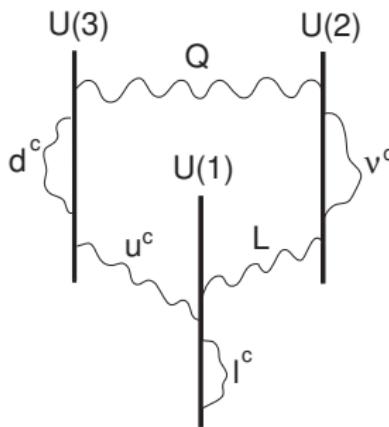


Model C

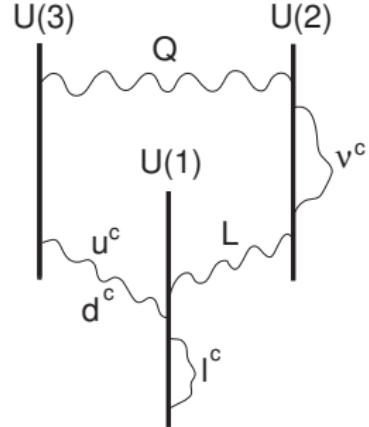
Q	$(\mathbf{3}, \mathbf{2}; 1, 1, 0)_{1/6}$	$(\mathbf{3}, \mathbf{2}; 1, \varepsilon_Q, 0)_{1/6}$	$(\mathbf{3}, \mathbf{2}; 1, \varepsilon_Q, 0)_{1/6}$
u^c	$(\bar{\mathbf{3}}, \mathbf{1}; 2, 0, 0)_{-2/3}$	$(\bar{\mathbf{3}}, \mathbf{1}; -1, 0, 1)_{-2/3}$	$(\bar{\mathbf{3}}, \mathbf{1}; -1, 0, 1)_{-2/3}$
d^c	$(\bar{\mathbf{3}}, \mathbf{1}; -1, 0, \varepsilon_d)_{1/3}$	$(\bar{\mathbf{3}}, \mathbf{1}; 2, 0, 0)_{1/3}$	$(\bar{\mathbf{3}}, \mathbf{1}; -1, 0, -1)_{1/3}$
L	$(\mathbf{1}, \mathbf{2}; 0, -1, \varepsilon_L)_{-1/2}$	$(\mathbf{1}, \mathbf{2}; 0, \varepsilon_L, 1)_{-1/2}$	$(\mathbf{1}, \mathbf{2}; 0, \varepsilon_L, 1)_{-1/2}$
I^c	$(\mathbf{1}, \mathbf{1}; 0, 2, 0)_1$	$(\mathbf{1}, \mathbf{1}; 0, 0, -2)_1$	$(\mathbf{1}, \mathbf{1}; 0, 0, -2)_1$
ν^c	$(\mathbf{1}, \mathbf{1}; 0, 0, 2\varepsilon_\nu)_0$	$(\mathbf{1}, \mathbf{1}; 0, 2\varepsilon_\nu, 0)_0$	$(\mathbf{1}, \mathbf{1}; 0, 2\varepsilon_\nu, 0)_0$



Model A



Model B



Model C

$$Y_A = -\frac{1}{3}Q_3 + \frac{1}{2}Q_2$$

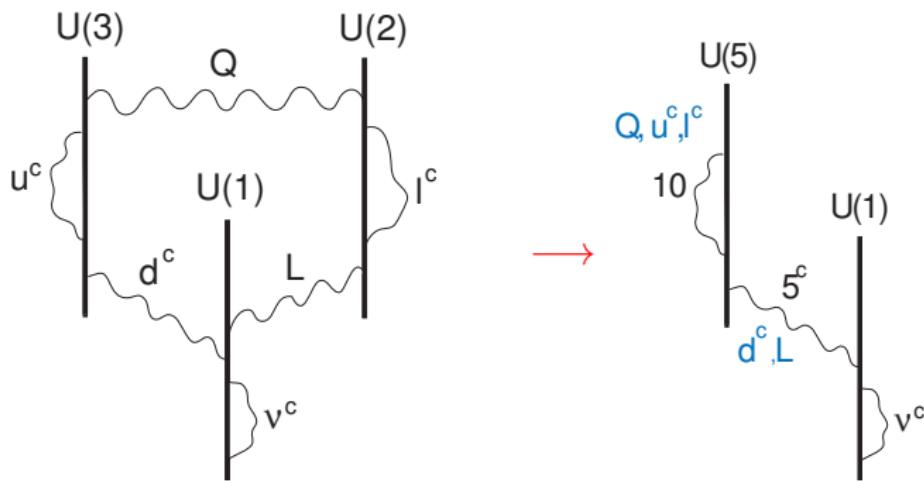
$$Y_{B,C} = \frac{1}{6}Q_3 - \frac{1}{2}Q_1$$

$$\sin^2 \theta_W = \frac{1}{2 + 2\alpha_2/3\alpha_3} \Big|_{\alpha_2=\alpha_3} = \frac{3}{8}$$

$$\frac{1}{1 + \alpha_2/2\alpha_1 + \alpha_2/6\alpha_3} \Big|_{\alpha_2=\alpha_3} = \frac{6}{7 + 3\alpha_2/\alpha_1}$$

[8]

$SU(5)$ GUT



Accelerator signatures of low-scale strings: 4 different scales

- Gravitational radiation in the bulk \Rightarrow missing energy

present LHC bounds: $M_* \gtrsim 4 - 9 \text{ TeV}$

- Massive string vibrations \Rightarrow e.g. resonances in dijet distribution [16]

$$M_j^2 = M_0^2 + M_s^2 j \quad ; \quad \text{maximal spin : } j+1$$

higher spin excitations of quarks and gluons with strong interactions

present LHC limits: $M_s \gtrsim 7 \text{ TeV}$

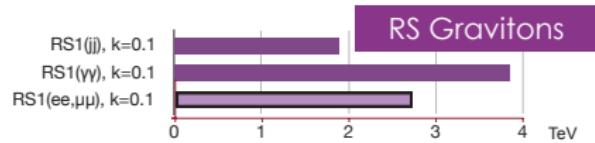
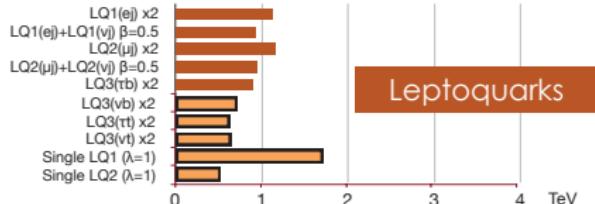
- Large TeV dimensions \Rightarrow KK resonances of SM gauge bosons I.A. '90

$$M_k^2 = M_0^2 + k^2/R^2 \quad ; \quad k = \pm 1, \pm 2, \dots$$

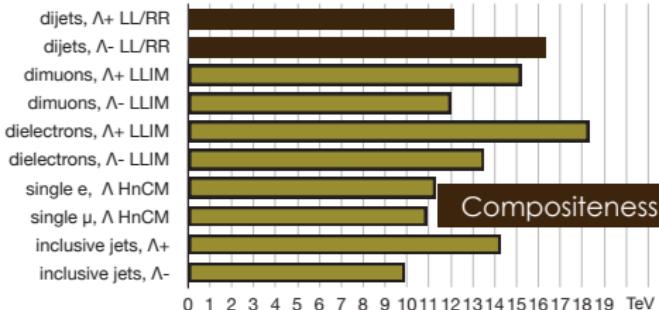
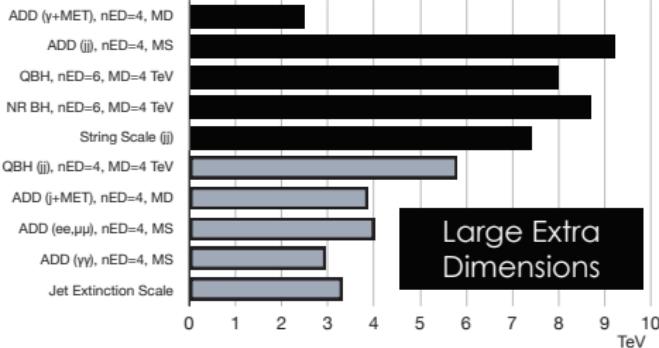
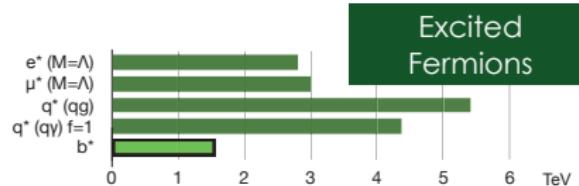
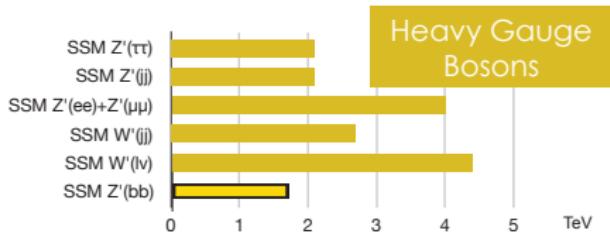
experimental limits: $R^{-1} \gtrsim 0.5 - 4 \text{ TeV}$ (UED - localized fermions)

- extra $U(1)$'s and anomaly induced terms

masses suppressed by a loop factor from M_s [19]

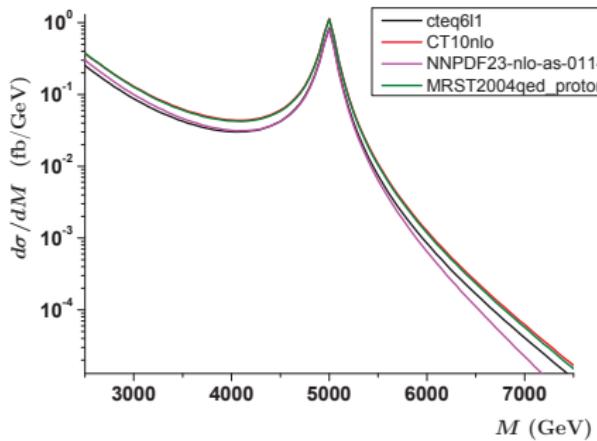


CMS Preliminary

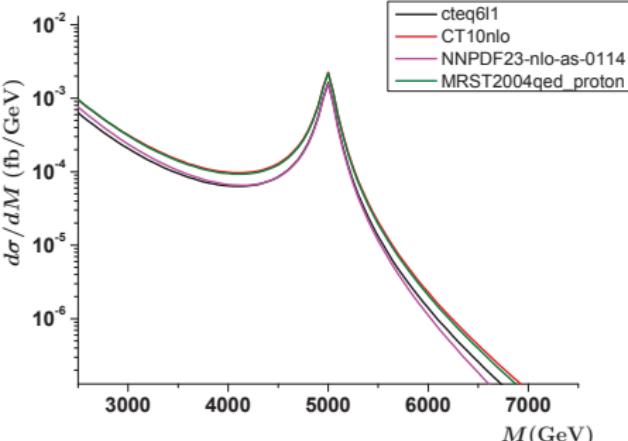


String Resonances production at Hadron Colliders

I.A.-Anchordoqui-Dai-Feng-Goldberg-Huang-Lüst-Stojkovic-Taylor '14



$M_s = 5$ TeV: dijet at LHC14



$\gamma +$ jet

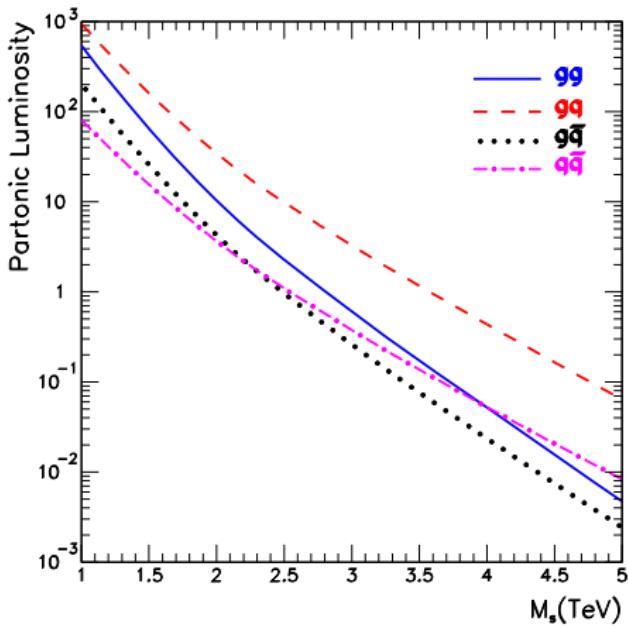
Tree level superstring amplitudes involving at most 2 fermions and gluons:
model independent for any compactification, # of susy's, even none
no intermediate exchange of KK, windings or graviton emmission
Universal sum over infinite exchange of string (Regge) excitations

Parton luminosities in pp above TeV

are dominated by gq, gg

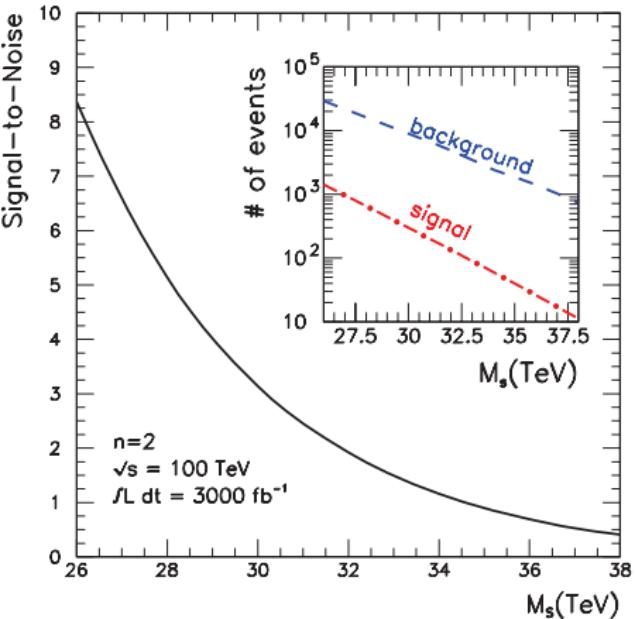
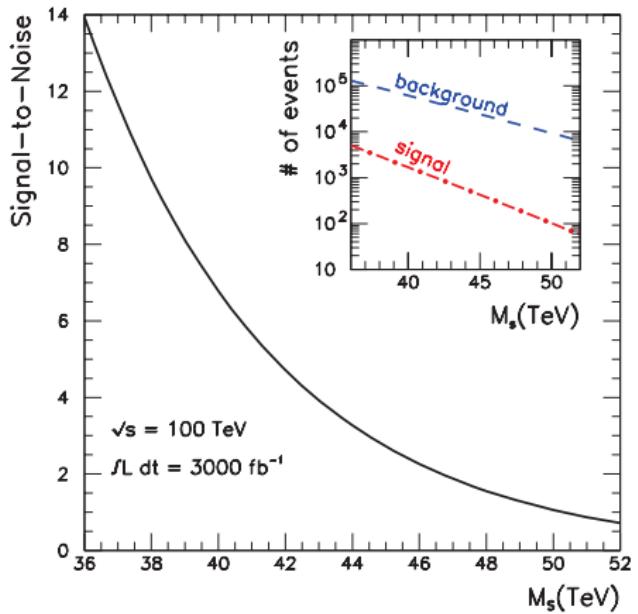
⇒ model independent

$gq \rightarrow gq, gg \rightarrow gg, gg \rightarrow q\bar{q}$



String Resonances production at Hadron Colliders

I.A.-Anchordoqui-Dai-Feng-Goldberg-Huang-Lüst-Stojkovic-Taylor '14



[14]

Extra $U(1)$'s and anomaly induced terms

masses suppressed by a loop factor

usually associated to known global symmetries of the SM

(anomalous or not) such as (combinations of)

Baryon and Lepton number, or PQ symmetry

Two kinds of massive $U(1)$'s:

I.A.-Kiritsis-Rizos '02

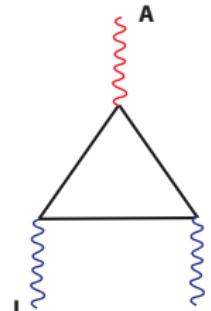
- 4d anomalous $U(1)$'s: $M_A \simeq g_A M_s$

- 4d non-anomalous $U(1)$'s: (but masses related to 6d anomalies)

$$M_{NA} \simeq g_A M_s V_2 \xleftarrow{(6d \rightarrow 4d) \text{ internal space}} \Rightarrow M_{NA} \geq M_A$$

or massless in the absence of such anomalies [21]

Green-Schwarz anomaly cancellation


$$= k_I^A \sim \text{Tr} Q_A Q_I^2 \rightarrow \text{axion } \theta : \delta A = d\Lambda \quad \delta\theta = -m_A \Lambda$$
$$-\frac{1}{4g_I^2} F_I^2 - \frac{1}{2} (d\theta + m_A A)^2 + \frac{\theta}{m_A} k_I^A \text{Tr} F_I \wedge F_I$$

cancel the anomaly

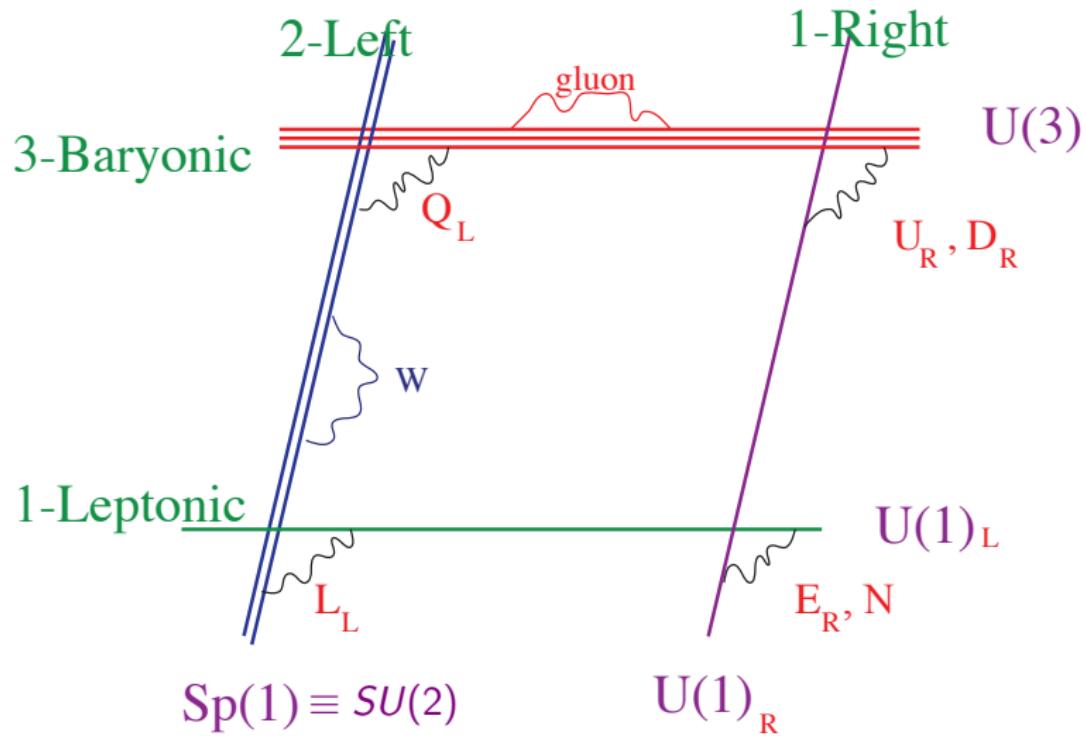
D-brane models: $U(1)_A$ gauge boson acquires a mass

but global symmetry remains in perturbation theory [23]

GS anomaly cancellation \Rightarrow extra scalars and axion-like particles (ALP)

- coupled to gauge kinetic terms
- lighter than the string scale (masses loop-factor suppressed)

Standard Model on D-branes : SM⁺⁺



$$U(1)^3 \Rightarrow \text{hypercharge } (Y = \frac{1}{2}(R - L) + \frac{1}{6}B) + B, L$$

global symmetries

- B and L become massive due to anomalies

Green-Schwarz terms

- the global symmetries remain in perturbation

- Baryon number \Rightarrow proton stability

- Lepton number \Rightarrow protect small neutrino masses

no Lepton number $\Rightarrow \frac{1}{M_s} LLHH \rightarrow$ Majorana mass: $\frac{\langle H \rangle^2}{M_s} LL$

~ GeV

- $B, L \Rightarrow$ extra Z' 's [7]

Exotic $U(1)$ anomaly induced couplings

I.A.-Boyarsky-Ruchayskiy '06, '07

Non trivial anomaly cancellation \rightarrow new **dimensionless** couplings

mixed $U(1)$ anomalies

$\Rightarrow Z'$ may couple to SM gauge bosons with no mass suppression

$$A \wedge X \wedge F_X \quad A \equiv Z', X \equiv W, Y$$

2 axionic phases: $A \rightarrow \theta_A, X \rightarrow \theta_X \equiv \text{SM Higgs} \Rightarrow$ [20]

$$D\theta_A \wedge D\theta_X \wedge F_X \rightarrow \mathcal{L}_{\text{eff}} = c_1 D\theta_A \frac{H^\dagger D H}{|H|^2} F_Y + c_2 D\theta_A \frac{H F_W D H^\dagger}{|H|^2}$$

D'Hoker-Farhi type terms

$$c_2 \rightarrow A W^+ W^- \quad c_1 \rightarrow A Z Y \quad (AZ\gamma, AZZ) \quad \text{vertices}$$

$$\Gamma(Z' \rightarrow ZZ) = \frac{c_1^2 \sin^2 \theta_W M_{Z'}^3}{192\pi M_Z^2} \left(1 - \frac{4M_Z^2}{M_{Z'}^2}\right)^{5/2}$$

$$\Gamma(Z' \rightarrow W^+ W^-) = \frac{c_2^2 M_{Z'}^3}{48\pi M_W^2} \left(1 - \frac{4M_W^2}{M_{Z'}^2}\right)^{5/2}$$

$$\Gamma(Z' \rightarrow Z\gamma) = \frac{c_1^2 \cos^2 \theta_W M_{Z'}^3}{96\pi M_Z^2} \left(1 - \frac{M_Z^2}{M_{Z'}^2}\right)^3 \left(1 + \frac{M_Z^2}{M_{Z'}^2}\right)$$

[7]

More general framework: large number of species

N particle species \Rightarrow lower quantum gravity scale : $M_*^2 = M_p^2/N$

Dvali '07, Dvali, Redi, Brustein, Veneziano, Gomez, Lüst '07-'10

derivation from: black hole evaporation or quantum information storage

$$M_* \simeq 1 \text{ TeV} \Rightarrow N \sim 10^{32} \text{ particle species !}$$

- Large extra dimensions SM on D-branes

$$N = R_\perp^n I_s^n : \text{number of KK modes up to energies of order } M_* \simeq M_s$$

- $M_s \sim \text{TeV} \Rightarrow$ low inflation scale

allowed by the data since cosmological observables are dimensionless
in units of the effective gravity scale

I.A.-Patil '14

Cosmological observables

Power spectrum of temperature anisotropies

(adiabatic curvature perturbations \mathcal{R})

$$\mathcal{P}_{\mathcal{R}} = \frac{H^2}{8\pi^2 M_*^2 \epsilon} \simeq \mathcal{A} \times 10^{-10} \quad ; \quad \mathcal{A} \approx 22$$

\downarrow
 $-H/\dot{H}$

Power spectrum of primordial tensor anisotropies $\mathcal{P}_t = 2 \frac{H^2}{\pi^2 M_*^2}$

$$\Rightarrow \text{tensor to scalar ratio } r = \mathcal{P}_t / \mathcal{P}_{\mathcal{R}} = 16\epsilon$$

measurement of \mathcal{A} and $r \Rightarrow$ fix the scale of inflation

$$H \text{ in terms of } M_* \quad : \quad \frac{H}{M_*} = \left(\frac{\pi^2 \mathcal{A} r}{2 \times 10^{10}} \right)^{1/2} \equiv \Upsilon \approx 1.05\sqrt{r} \times 10^{-4}$$

- M_* may be different than M_{Planck} at the time of inflation

Effective Planck mass and the scale of inflation

I.A.-Patil '14, '15

Explicit realisation:

Flat extra dimensions: obstruction due to the de Sitter bound:

$$M_{\text{spin 2}}^2 \geq 2H^2$$

Higuchi '87

⇒ no KK-excitations with mass less than Hubble scale

Kleban-Mirbabayi-Porrati '15

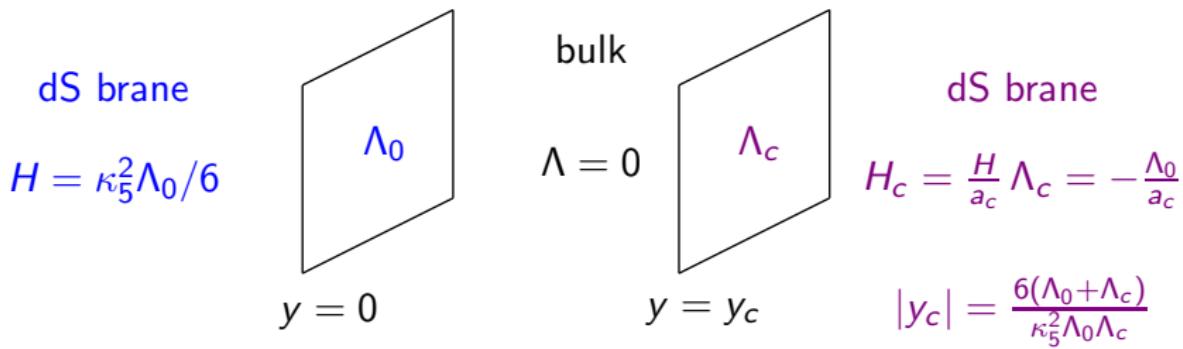
However in warped extra dimensions:

KK-modes couple much stronger than 0-mode

5D brane-world realisation: empty bulk with two boundary dS branes [30]

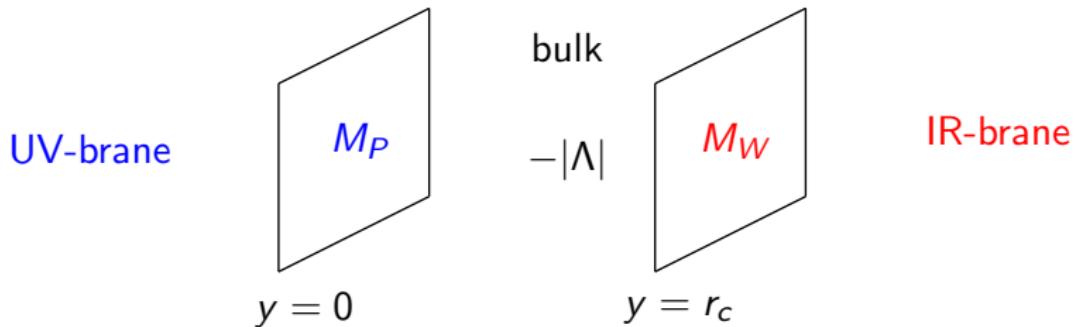
$$ds^2 = \frac{(1 - H|y|)^2}{H^2\tau^2} (-d\tau^2 + dx_1^2 + dx_2^2 + dx_3^2) + dy^2$$

$|y| < 1/H$: avoid Riddler horizon $a(y) = 1 - H|y| > 0$



Randal Sundrum models

spacetime = slice of AdS₅ : $ds^2 = e^{-2k|y|} \eta_{\mu\nu} dx^\mu dx^\nu + dy^2$ $k^2 \sim \Lambda/M_5^3$



- fine-tuned tensions: $T = -T' = 24M_5^3 k$
- exponential hierarchy: $M_W = M_P e^{-2kr_c}$ $M_P^2 \sim M_5^3/k$ $M_5 \sim M_{GUT}$
- 4d gravity localized on the UV-brane, but KK gravitons on the IR

$$m_n = c_n k e^{-2kr_c} \sim \text{TeV} \quad c_n \simeq (n + 1/4) \text{ for large } n$$

spectrum and couplings

4d Planck mass: $M_{Pl} \sim 1/(2H\kappa_5^2)$ y_c large

Spectrum:

0-mode (4d graviton): wave function $\phi_0 \sim (2H)^{1/2} e^{-2z}$ $z \equiv -\ln a(y) > 0$

KK-modes: $m_n^2 = H_y^2 \left(\frac{9}{4} + \pi^2 \frac{n^2}{z_c^2} \right)$ $H_y \equiv H/a(y)$: Hubble constant at y

wave functions $\phi_n \sim \frac{H}{2m_n} \left(\frac{H}{z_c} \right)^{1/2} e^{-z/2} \left[3 \sin \left(\frac{n\pi z}{z_c} \right) + \frac{2\pi n}{z_c} \cos \left(\frac{n\pi z}{z_c} \right) \right]$

⇒ KK-modes couple much stronger than 0-mode at y_c :

$$|\phi_n|/|\phi_0| = \frac{\pi n}{\sqrt{2} z_c^{3/2}} \frac{H_c}{m_n} e^{3z_c/2}$$

similar result for bulk scalars

Power spectrum

0-mode as before:

$$\mathcal{P}_0 = \frac{2}{\pi^2} \frac{H_c^2}{M_{Pl}^2}$$

KK-modes:

$$\mathcal{P}_n = \mathcal{P}_0 \frac{\pi^2 n^2}{2z_c^3} e^{3z_c} \left(\frac{H_c}{m_n} \right)^3 \left(\frac{k}{a_{dS} H_c} \right)^3 \simeq \mathcal{P}_0 \frac{\pi^2 n^2}{2z_c^3} \left(\frac{H_c}{m_n} \right)^3 e^{3(z_c - N)}$$

N : number of e-foldings

Riotto '02

$$\mathcal{P}_0 \lesssim \mathcal{P}_n \Rightarrow e^N \lesssim e^{z_c} / z_c$$

$$\mathcal{P}_{KK} = \sum_n^{m_n < M_5} \mathcal{P}_n = \mathcal{P}_0 e^{3(z_c - N)} \frac{1}{2\pi} \ln \frac{M_5 z_c}{\pi H_c}$$
$$\gtrsim \mathcal{P}_0 \Rightarrow N \lesssim z_c$$

Power spectrum

Allowed range of parameters:

$$M_{Pl}^2 \simeq \frac{M_5^3}{H_c} e^{z_c} \Rightarrow e^{z_c} \simeq \frac{M_{Pl}^2 H_c}{M_5^3} \lesssim \frac{M_{Pl}^2}{M_5^2} \quad H_c \lesssim M_5$$

$$e^{N_{\min}} = 10^{13} \times \frac{H_c}{1 \text{ GeV}} \lesssim e^{z_c}$$

$$\Rightarrow 1 \text{ TeV} \lesssim H_c \lesssim 10^8 \text{ GeV} \text{ and } 1 \text{ TeV} \lesssim M_5 \lesssim 10^{10} \text{ GeV}$$

Conclusions

String phenomenology:

Consistent framework for particle physics and cosmology

Challenge of scales: at least three very different (besides M_{Planck})
electroweak, dark energy, inflation, SUSY?

their origins may be connected or independent

Low scale gravity and strings at the (multi-)TeV scale:

offer connection of scales and spectacular new physics to discover

Inflation scale: cannot be determined from observation of B-modes
unknown gravity scale at the time of inflation