

Jan. 10th, 2017@Tokyo Univ.

Splitting Mass Spectra in Higgs-Anomaly Mediation

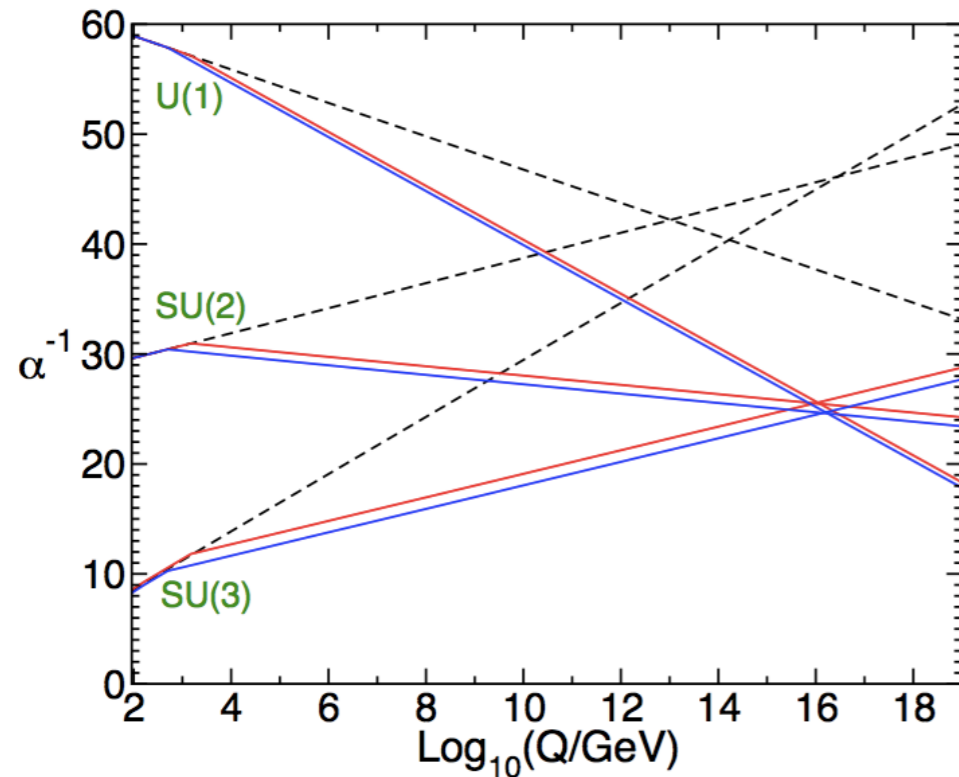
Norimi Yokozaki (Tohoku U.)

Wen Yin, Norimi Yokozaki, arXiv:1607.05705 (PLB)

See also

Tsutomu T. Yanagida, Wen Yin, Norimi Yokozaki, arXiv:1608.06618 (JHEP)

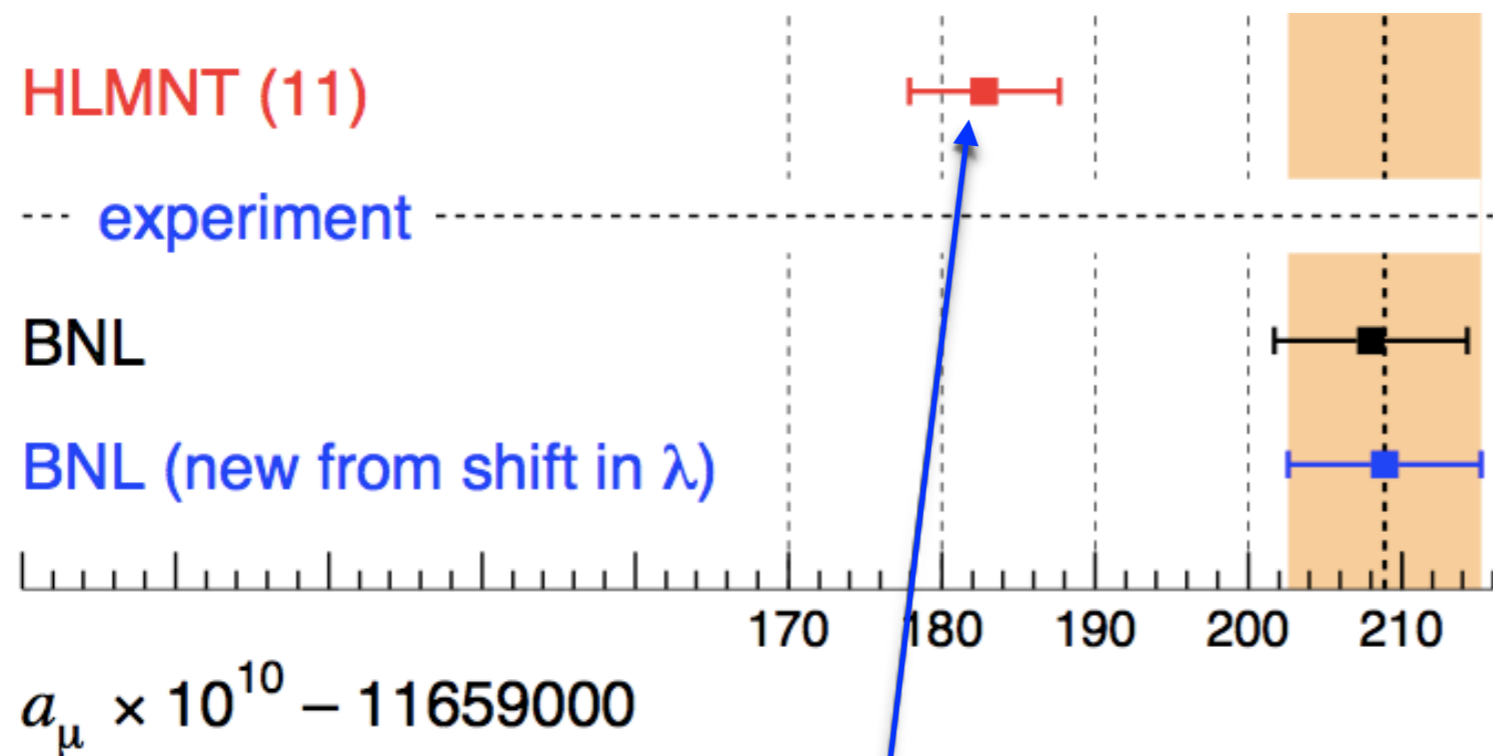
Why SUSY



[from SUSY primer, S. Martin]

- Gauge coupling unification
 - Indicating grand unification
 - Matter unification
 - Charge quantization
- Absence of the quadratic divergences in the scalar potential (SM Higgs, PQ-breaking scalar, inflaton)
- There is another experimental motivation

Muon $g-2$ anomaly



**>3 σ deviation
from SM
prediction!**

[Also, Davier et al., 2016
→ 3.6 σ]

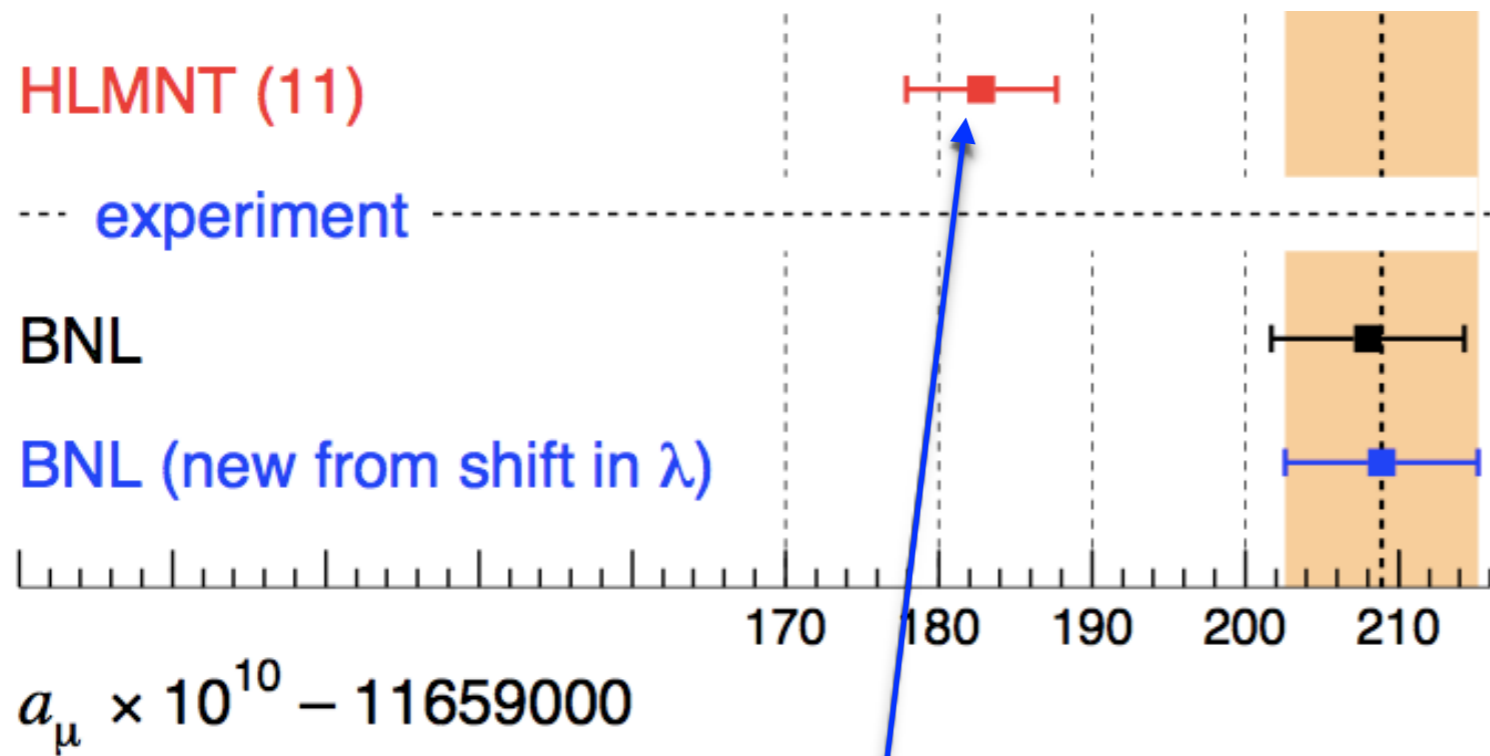
[Hagiwara, Liao, Martin, Nomura, Teubner, J.Phys. G38 (2011) 085003]

SM value

$$\mathcal{L} = \frac{e}{4m_\mu} (a_\mu)^{\text{NP}} \bar{\mu} \sigma_{\alpha\beta} \mu F^{\alpha\beta}$$

$$(a_\mu)^{\text{NP}} \approx 2 \times 10^{-9} \text{ is required}$$

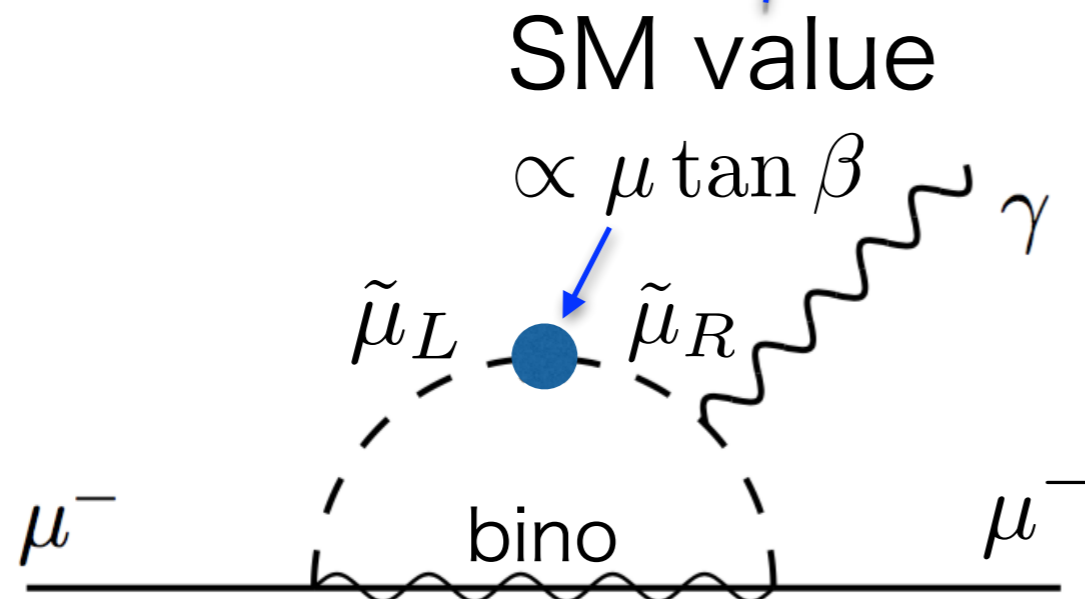
Muon $g-2$ anomaly



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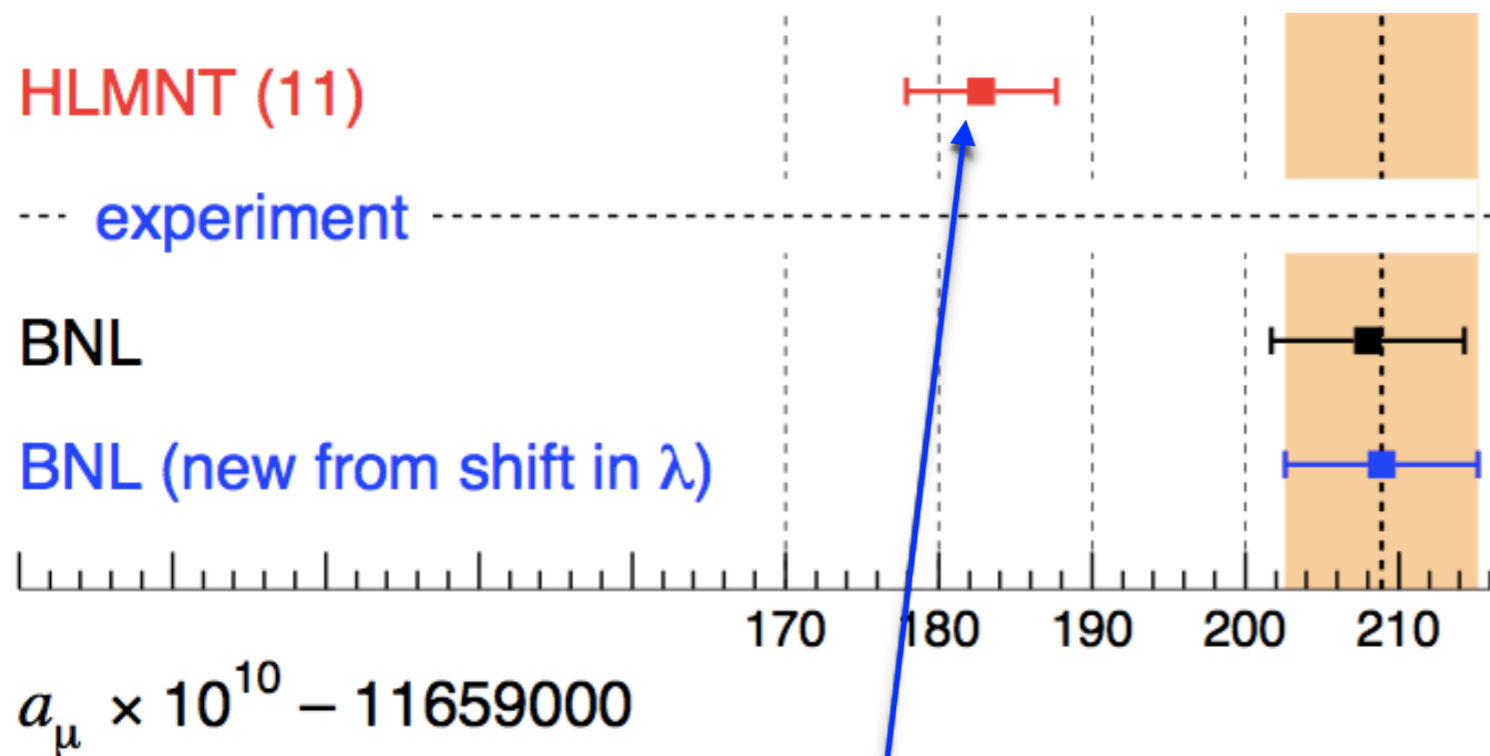
[Hagiwara, Liao, Martin, Nomura, Teubner, J.Phys. G38 (2011) 085003]



Relevant SUSY particles
should be light as $O(100)$ GeV

[Lopez, Nanopoulos and Wang, 1994;
Chattopadhyay and Nath, 1996;
Moroi, 1996]

Muon $g-2$ anomaly



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[Hagiwara, Liao, Martin, Nomura, Teubner, J.Phys. G38 (2011) 085003]

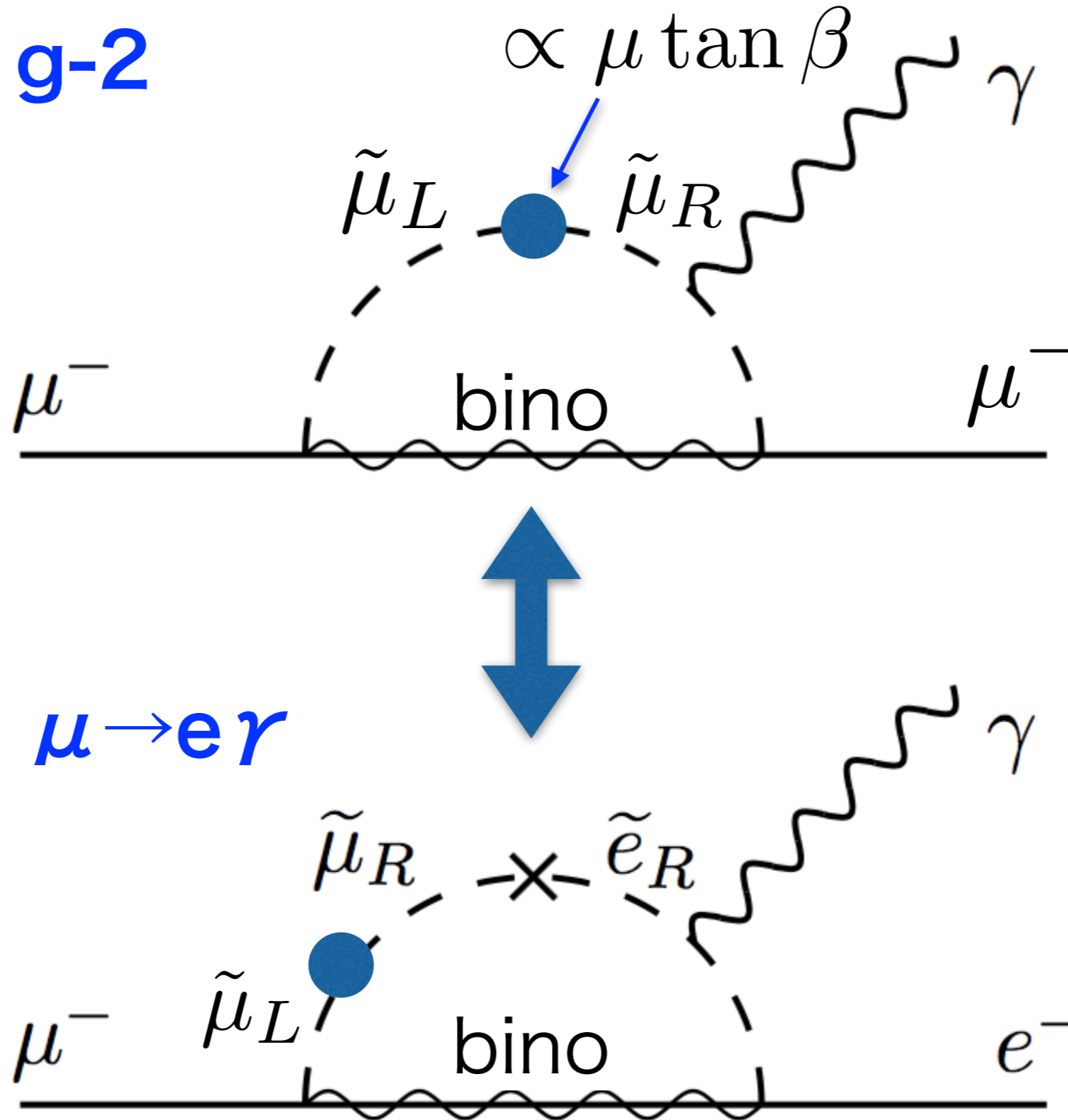
SM value

However, it is not easy to explain the muon $g-2$ in MSSM, in a way consistent with GUT.

Difficulties

- LHC SUSY search
→ heavy squarks and gluino of $>1.4 - 1.8$ TeV
- Higgs boson mass of 125 GeV → heavy stops of ~ 10 TeV
- Muon $g-2$
→ light sleptons and neutralino/chargino of $\sim 100-500$ GeV
- Grand Unification → Slepton and squarks live in same GUT multiplet, $\mathbf{10}=(Q, U^*, E^*)$ $\mathbf{5}^*=(L, D^*)$
It is natural that their masses are degenerated at the tree level. GUT breaking effects may be required.
- Naively, gaugino masses also unify:
 $g_1=g_2=g_3=g_5 \rightarrow \mathbf{M_1=M_2=M_3=M_5}$

Flavor problem



In general, if muon g-2 enhanced
→ LFV is also enhanced

Higgs-Anomaly mediation

- We considered a simple model explaining the muon $g-2$, without difficulties concerning the GUT embedding and flavor violation ([Yin-Yokozaki, 2016](#))

In our model, sfermion and gaugino masses originate from anomaly mediation and Higgs loop effects; therefore, no SUSY flavor problem arises

Refs for Anomaly mediation:

[Giudice, Luty, Murayama, Rattazzi; Randall, Sundrum, 1999]

Higgs-Anomaly mediation

- We considered a simple model explaining the muon $g-2$, without difficulties concerning the GUT embedding and flavor violation (Yin-Yokozaki, 2016)

Recipe:

- 1, Sequestering the matter fields and SUSY breaking field
→ squarks and sleptons are massless at the tree level
(gauginos are also massless)
- 2, Making the gravitino heavy (~ 100 TeV)
→ Anomaly mediation becomes effective, inducing GUT breaking effects
- 3, Coupling only Higgs fields and SUSY breaking field directly. **(Note: Higgs soft masses are tachyonic)**

Solving the
flavor problem

Relaxing the
gravitino
problem

Our setup

$$K = -3M_P^2 \ln \left[1 - \frac{f(Z, Z^\dagger) + \phi_i^\dagger \phi_i + \Delta K}{3M_P^2} \right],$$

SUSY breaking field

(quark, lepton, Higgs)

$$\Delta K = c_Z \frac{|Z|^2}{M_P^2} (|H_u|^2 + |H_d|^2),$$

$c_Z > 0$

Our setup

$$K = -3M_P^2 \ln \left[1 - \frac{f(Z, Z^\dagger) + \phi_i^\dagger \phi_i}{3M_P^2} \right],$$

SUSY breaking field

(quark, lepton, Higgs)

First, we start with a sequestered form

Sfermion masses vanish at the tree-level

**Simple and important assumption to solve
SUSY flavor problem**

(gaugino masses also vanish at the tree-level)

Ref. for sequestered form [Randall, Sundrum, 1999]

Our setup

$$K = -3M_P^2 \ln \left[1 - \frac{f(Z, Z^\dagger) + \phi_i^\dagger \phi_i}{3M_P^2} \right],$$

SUSY breaking field

(quark, lepton, Higgs)

$$M_1 \simeq \frac{33}{5} \frac{g_1^2}{16\pi^2} m_{3/2}, \quad M_2 \simeq \frac{g_2^2}{16\pi^2} m_{3/2}, \quad M_3 \simeq -3 \frac{g_3^2}{16\pi^2} m_{3/2},$$

(gaugino masses also vanish at the tree-level)

Ref. for sequestered form [Randall, Sundrum, 1999]

Our setup

$$K = -3M_P^2 \ln \left[1 - \frac{f(Z, Z^\dagger) + \phi_i^\dagger \phi_i}{3M_P^2} \right],$$

SUSY breaking field

(quark, lepton, Higgs)

Sfermion masses vanish at the tree-level

From anomaly mediation effects, sfermion get masses at the two-loop level. However, slepton mass become tachyonic

$$m_{\bar{E}}^2 \approx -22g_Y^4 \frac{m_{3/2}^2}{16\pi^2}$$

(Left-handed slepton has also tachyonic mass)

Our setup

$$K = -3M_P^2 \ln \left[1 - \frac{f(Z, Z^\dagger) + \phi_i^\dagger \phi_i}{3M_P^2} \right],$$

SUSY breaking field

(quark, lepton, Higgs)

Sfermion masses vanish at the tree-level

From anomaly mediation effects, sfermion get masses at the two-loop level. However, slepton mass become tachyonic

Tachyonic slepton problem in anomaly mediation

→ From another perspective, slepton can be light which is favored for the muon $g-2$

GUT breaking effects are naturally included

Our setup

$$K = -3M_P^2 \ln \left[1 - \frac{f(Z, Z^\dagger) + \phi_i^\dagger \phi_i + \Delta K}{3M_P^2} \right],$$

SUSY breaking field

(quark, lepton, Higgs)

$$\Delta K = c_Z \frac{|Z|^2}{M_P^2} (|H_u|^2 + |H_d|^2),$$

$c_Z > 0$

Only Higgs doublets couple to the SUSY breaking field directly

(Solving tachyonic slepton problem and making third generation sfermion heavy)

Our setup

$$K = -3M_P^2 \ln \left[1 - \frac{f(Z, Z^\dagger) + \phi_i^\dagger \phi_i + \Delta K}{3M_P^2} \right],$$

SUSY breaking field

(quark, lepton, Higgs)

$$\Delta K = c_Z \frac{|Z|^2}{M_P^2} (|H_u|^2 + |H_d|^2),$$

$c_Z > 0$

Only Higgs doublets couple to the SUSY breaking field directly

Negative Higgs soft mass squares are important!

$$\frac{dm_{Q_3}^2}{d \ln \mu_R} \ni \frac{1}{8\pi^2} (Y_t^2 m_{H_u}^2 + Y_b^2 m_{H_d}^2) < 0$$

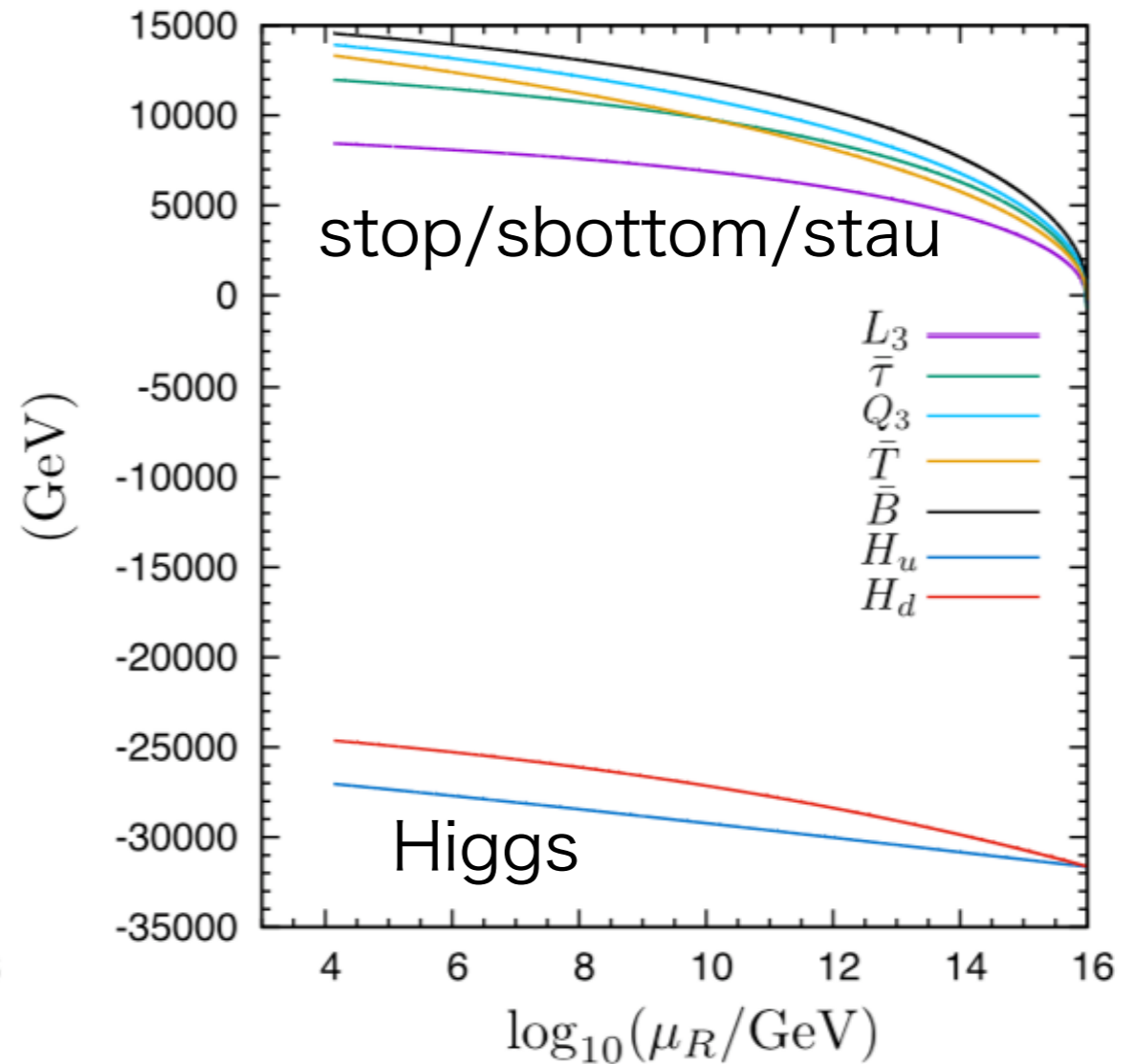
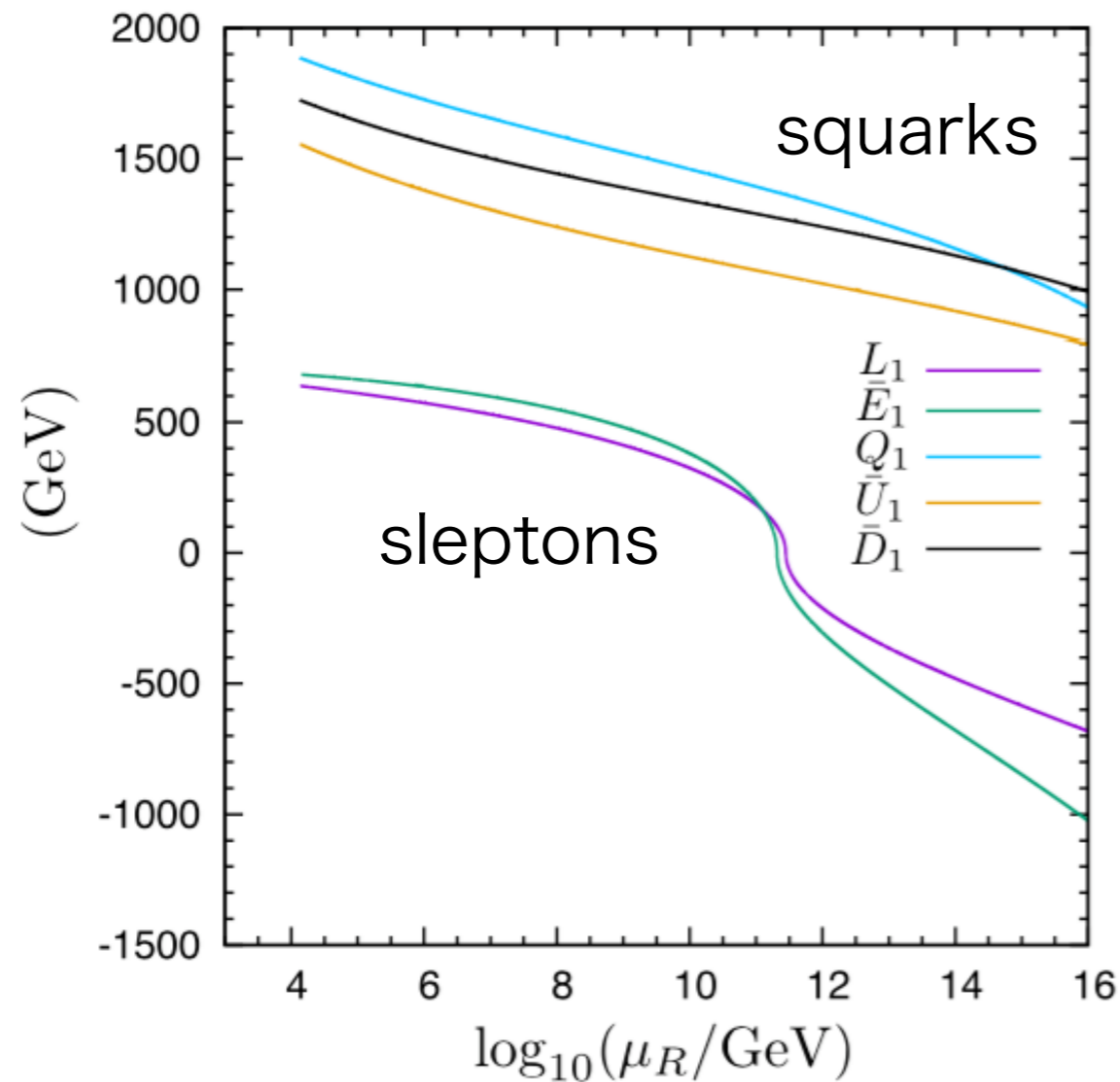
Lifting up 3rd generation sfermion masses at one-loop level
Important for the Higgs mass of 125 GeV

e.g.

$$\frac{dm_{\bar{E}}^2}{d \ln \mu_R} \ni \frac{1}{(16\pi^2)^2} \left[\frac{36}{25} g_1^4 (m_{H_u}^2 + m_{H_d}^2) \right] < 0$$

Lifting up slepton masses, avoiding the tachyonic slepton problem at two-loop level

RGE runnings of soft mass parameters



$$m_{3/2} = 120 \text{ TeV}, \tan \beta = 48, \text{ and } m_H = -10^9 \text{ GeV}^2.$$

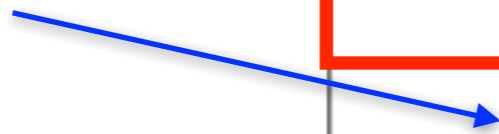
(Still D-flat direction of the Higgs potential is safe!)

Mass spectrum and muon $g-2$

(Including leading two-loop corrections)

Parameters	Point I
$m_{3/2}$ (TeV)	120
m_H^2 (GeV ²)	-9×10^8
$\tan \beta$	48
Particles	Mass (GeV)
\tilde{g}	2550
\tilde{q}	1830 - 2110
$\tilde{\chi}_1^0 / \tilde{\chi}_1^\pm$	378
$\tilde{\chi}_2^0$	1100
$\tilde{e}_{L,R}$	549, 682
$\tilde{\mu}_{L,R}$	609, 778
$\tilde{t}_{2,1}$ (TeV)	13.1, 12.5
$\tilde{b}_{2,1}$ (TeV)	14.2, 13.4
$\tilde{\tau}_{2,1}$ (TeV)	11.4, 8.0
H^\pm (TeV)	10.9
μ (TeV)	25.8
$(a_\mu)_{\text{SUSY}}$ (10^{-10})	18.6

~wino



~bino



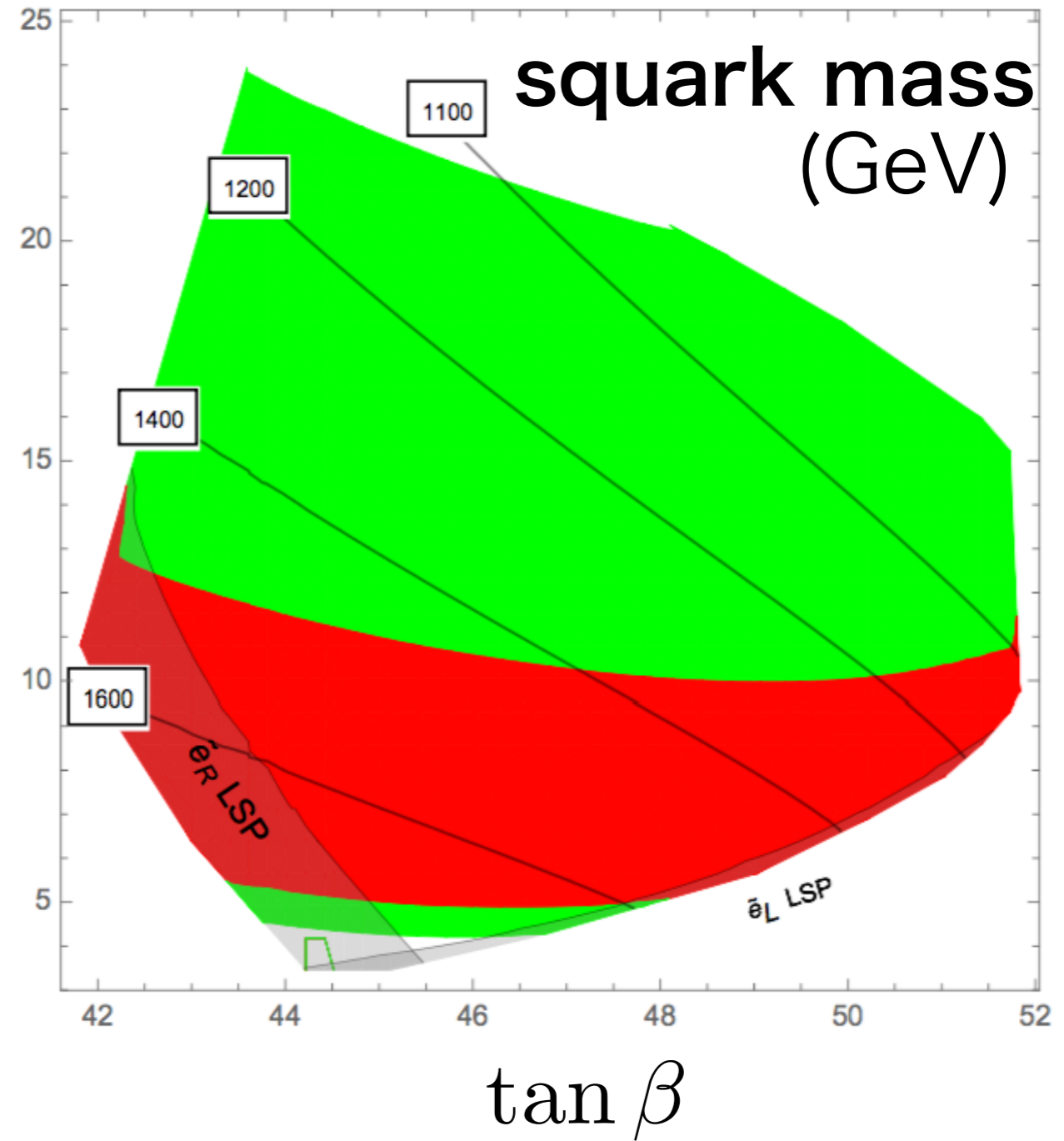
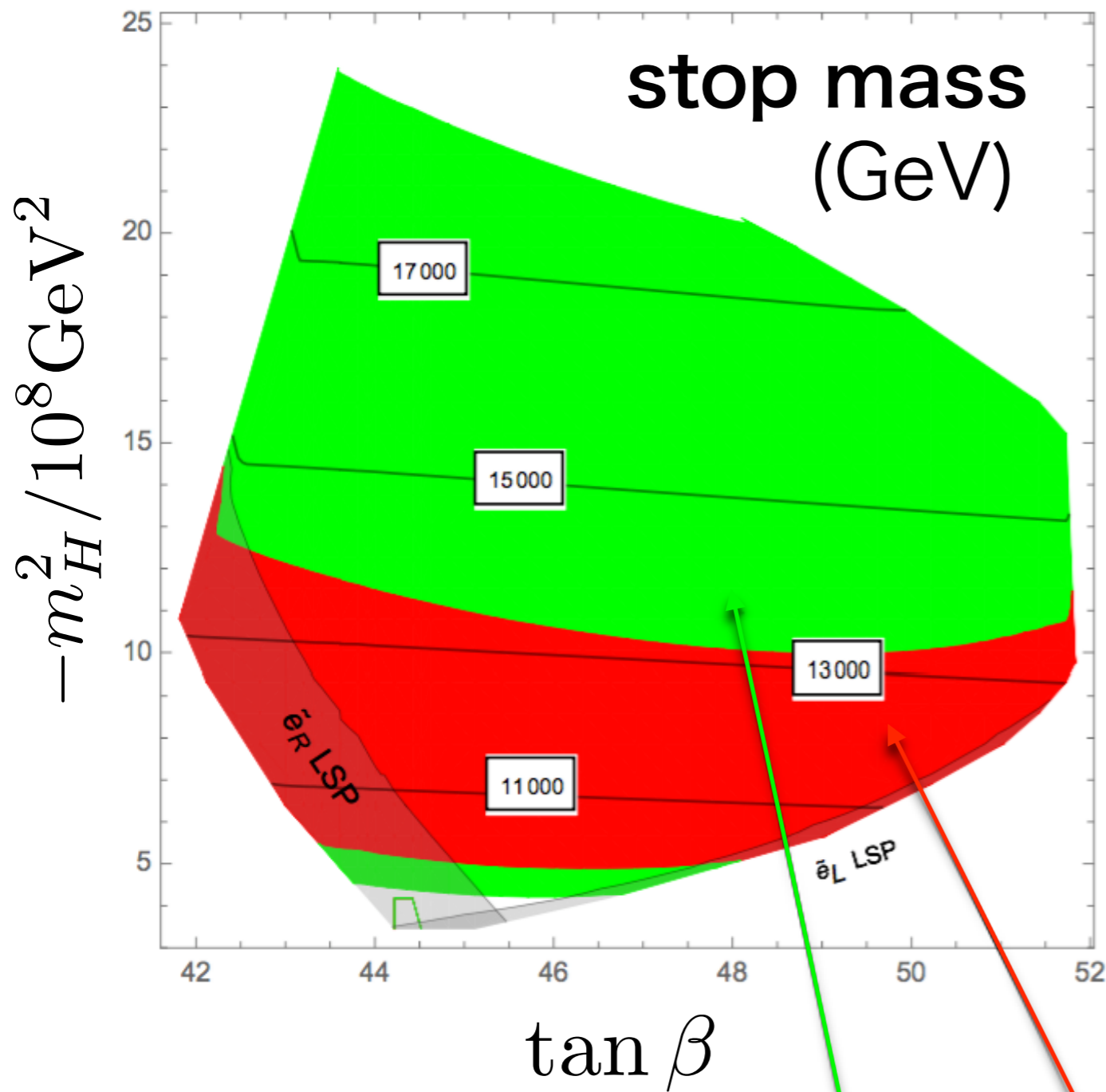
~ 2-2.5TeV

~ 600GeV

~ 10TeV

~ g-2: 1 σ

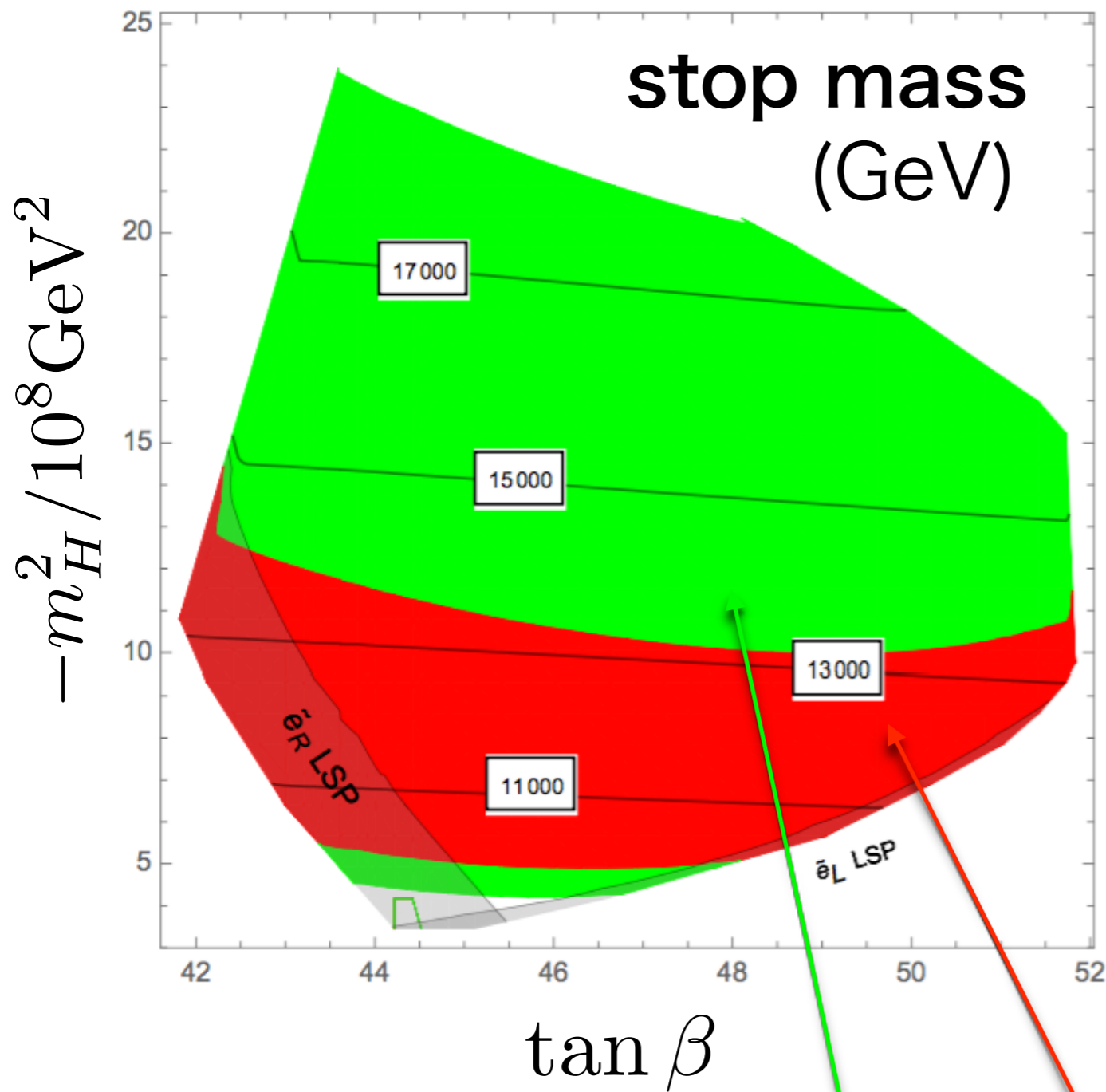
$m_{3/2}=100$ TeV



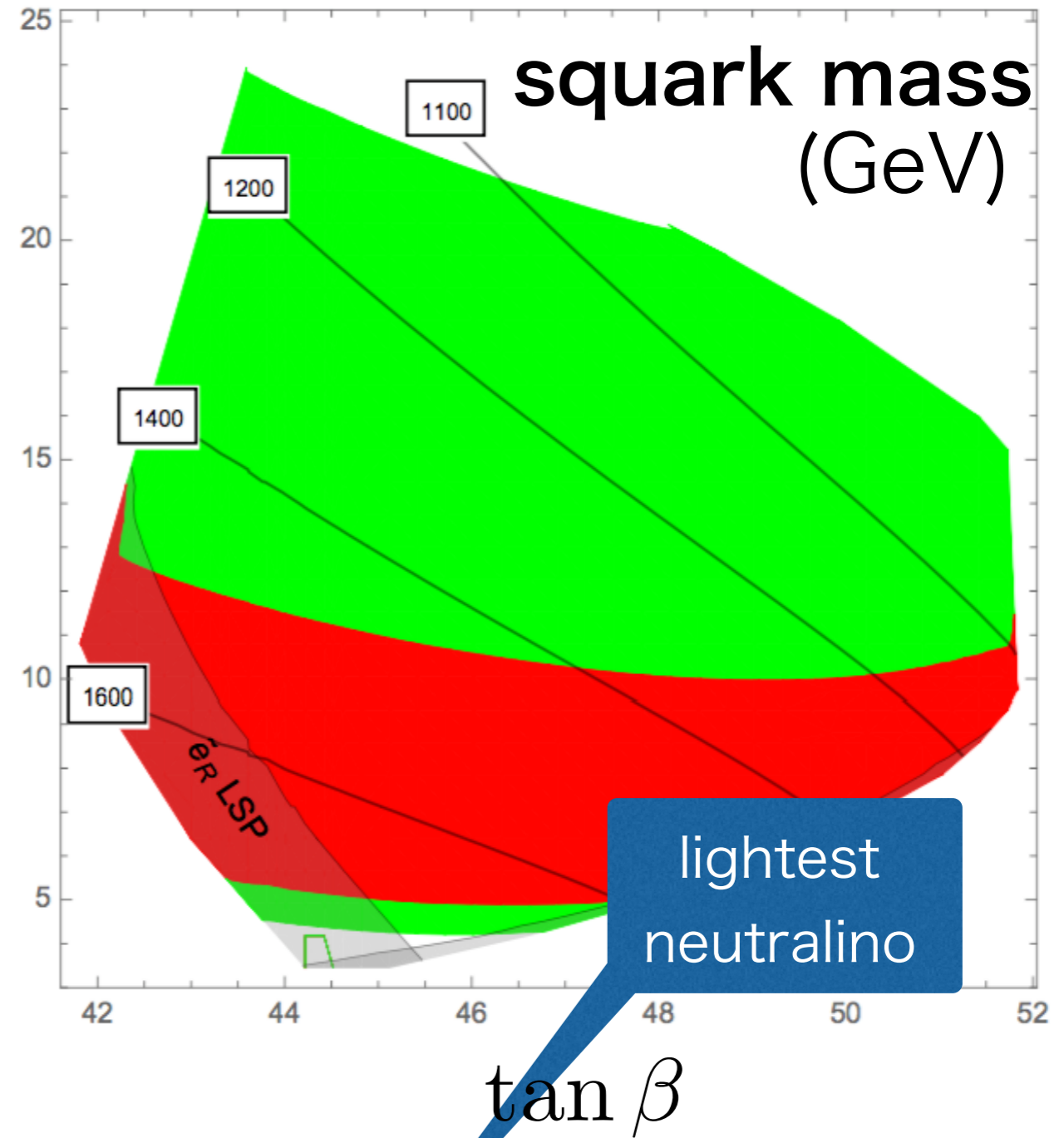
2σ $g-2: 1\sigma$

gluino mass: 2.2 TeV
wino mass: 320 GeV

$m_{3/2}=100$ TeV

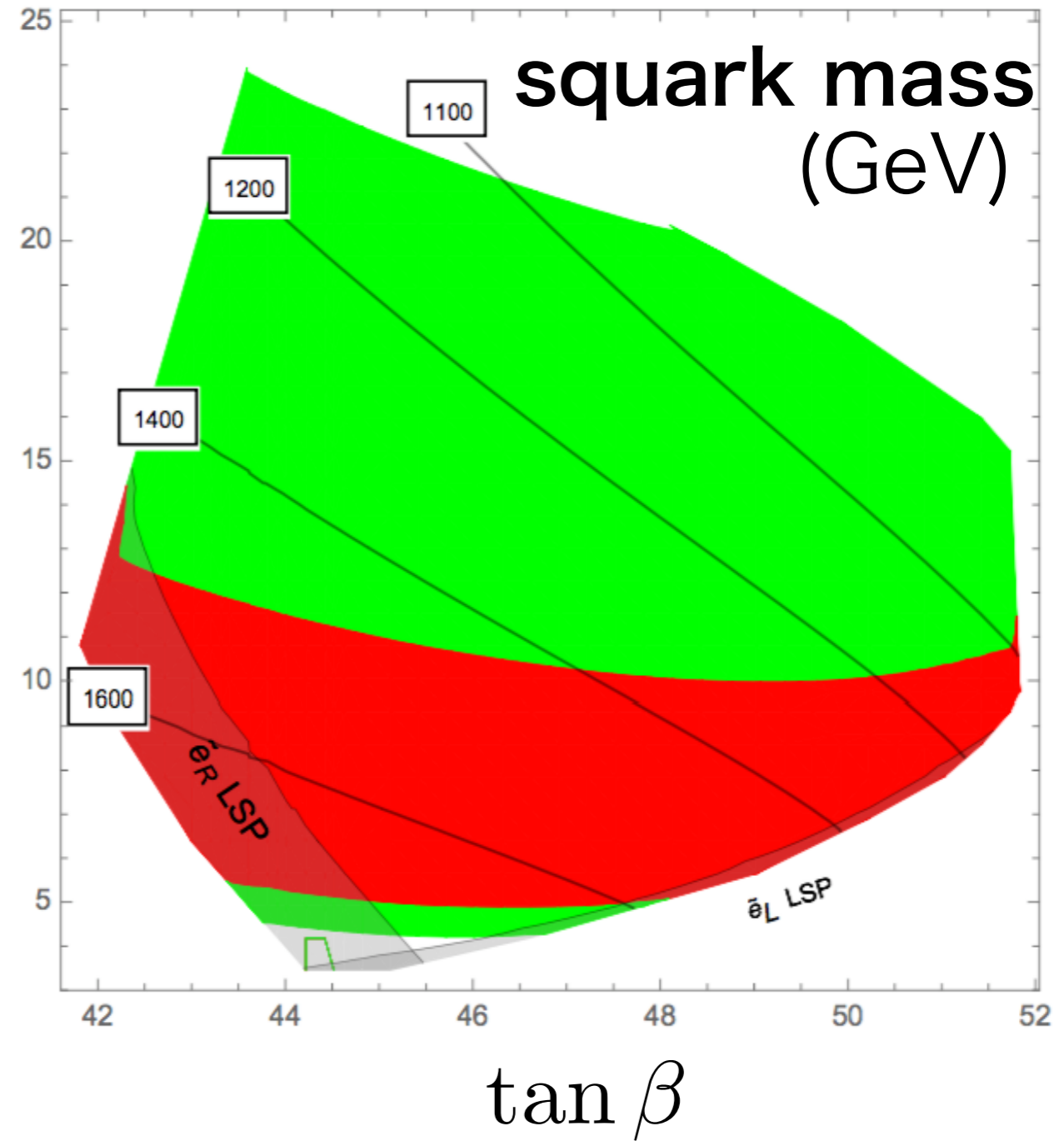
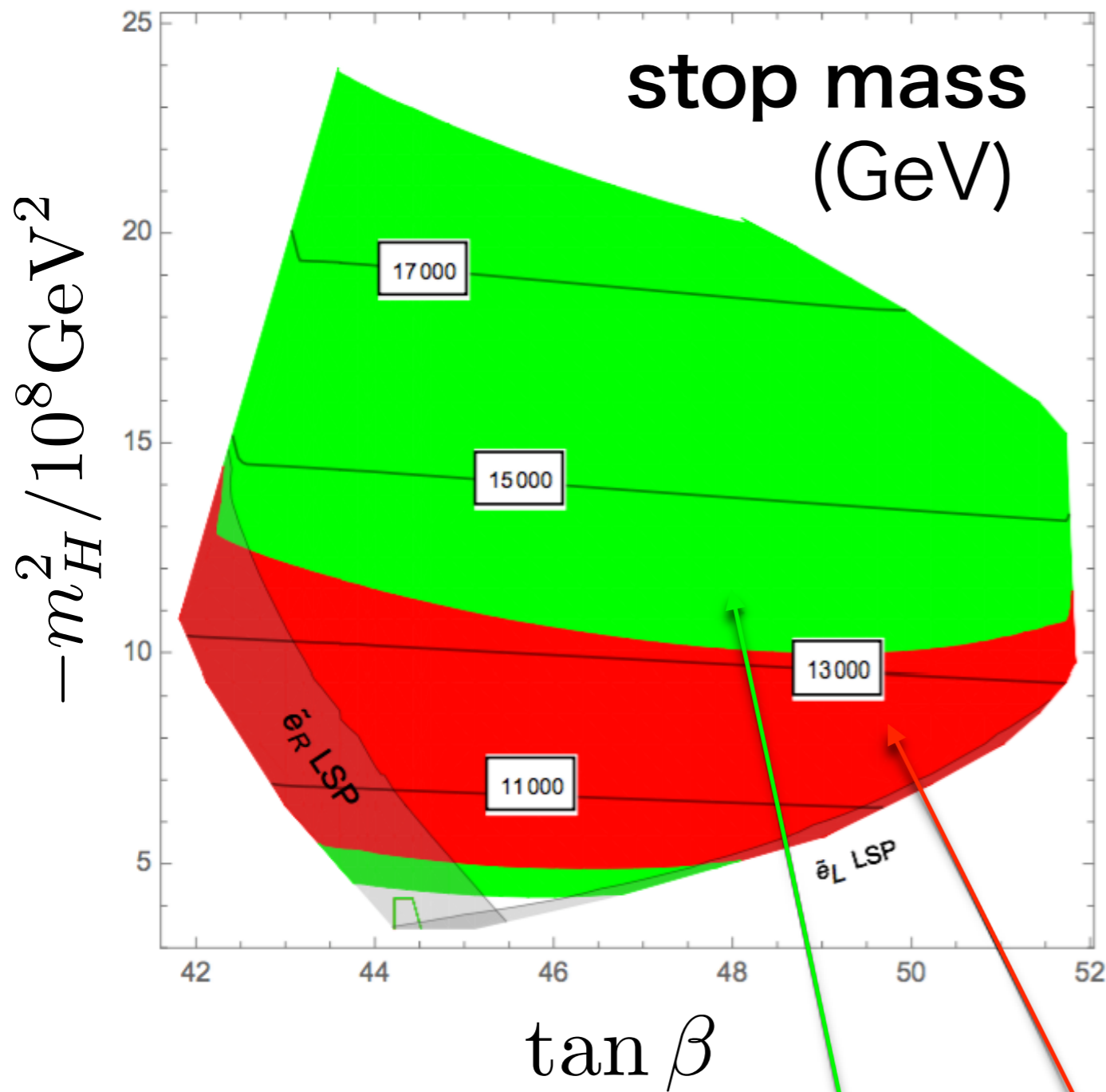


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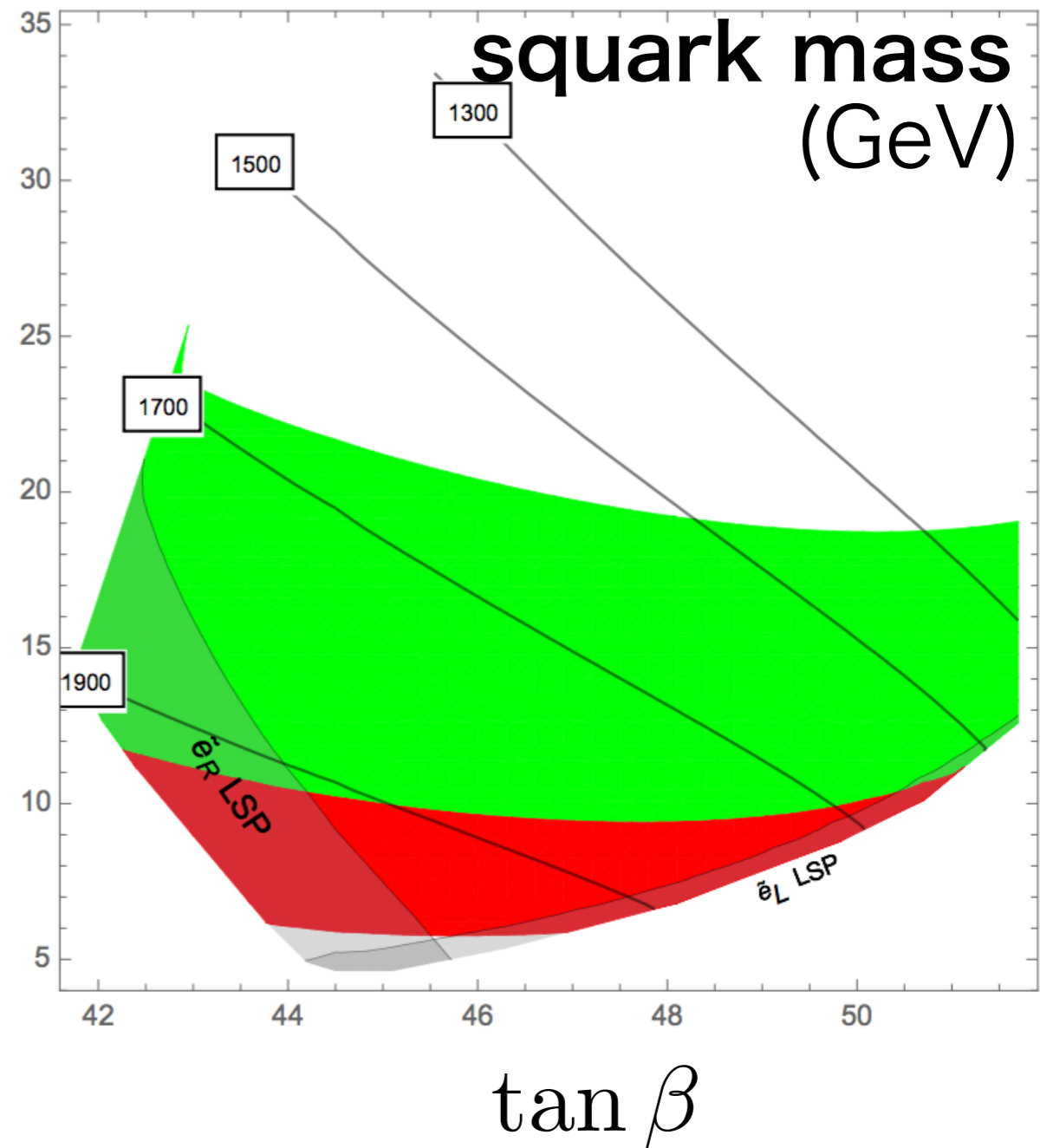
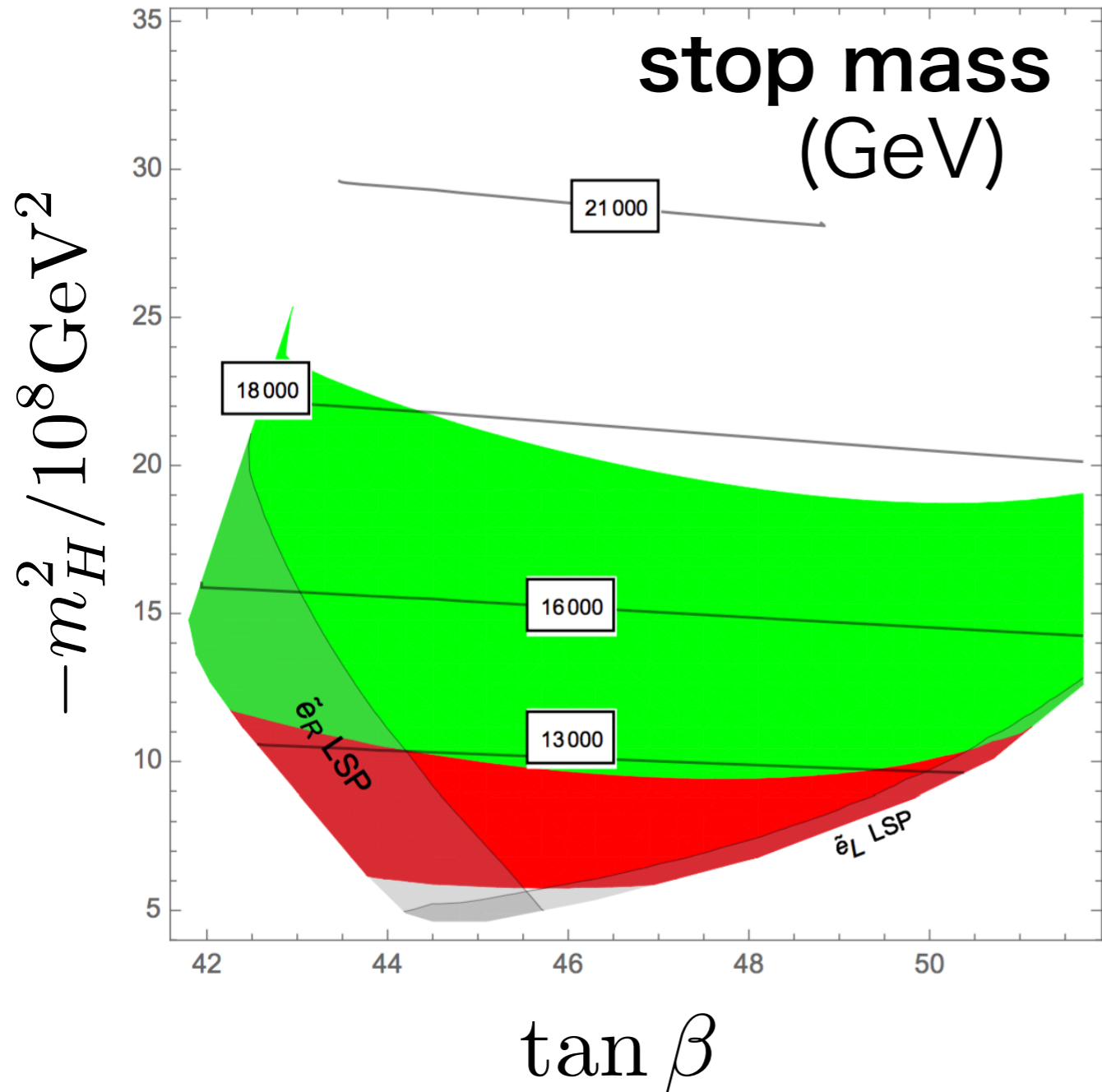
$m_{3/2}=100$ TeV



2σ $g-2: 1\sigma$

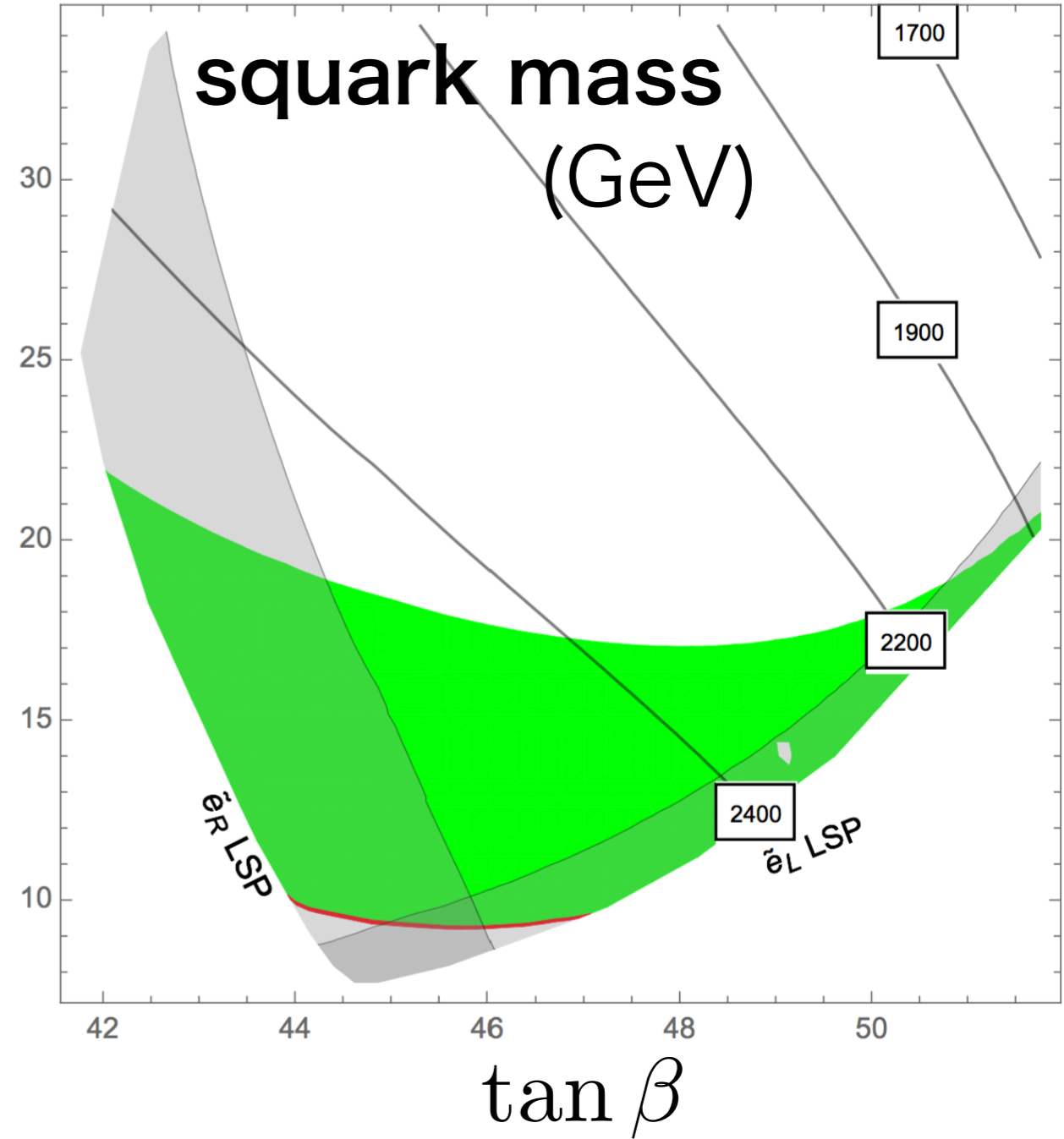
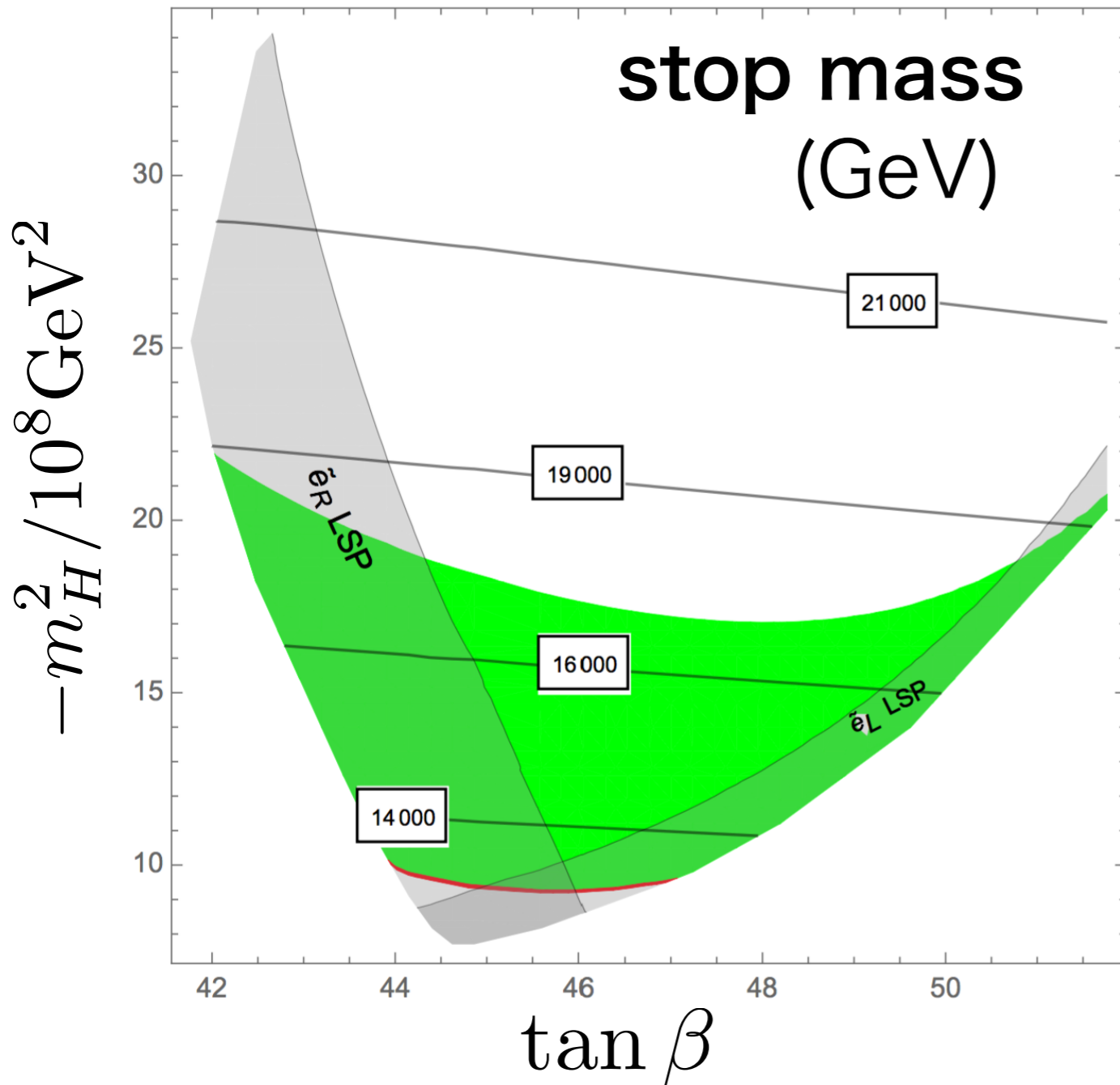
gluino mass: 2.2 TeV
wino mass: 320 GeV

$m_{3/2}=120$ TeV



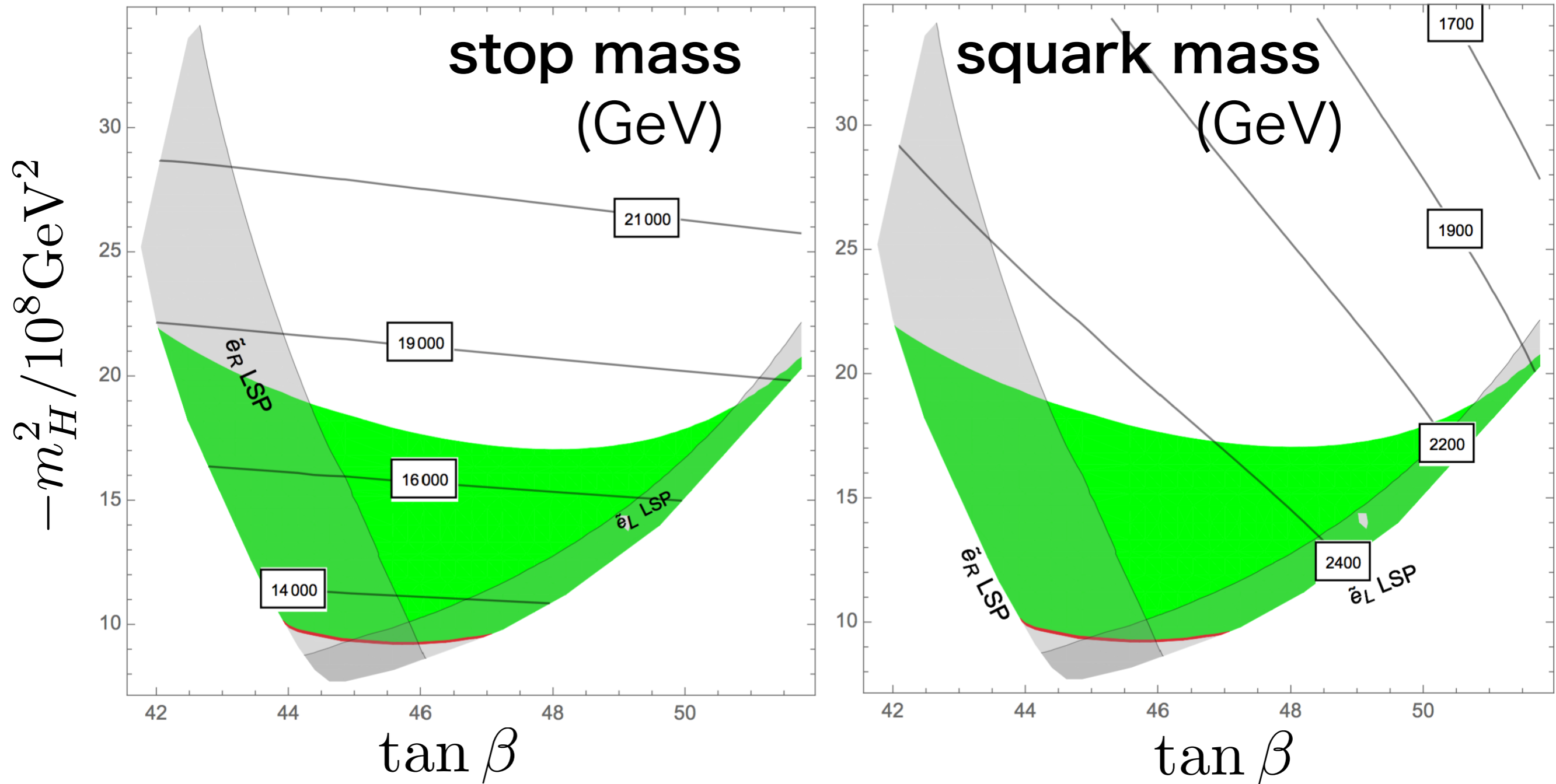
gluino mass: 2.5 TeV
wino mass: 380 GeV

$m_{3/2} = 160 \text{ TeV}$



gluino mass: 3.3 TeV
wino mass: 500 GeV

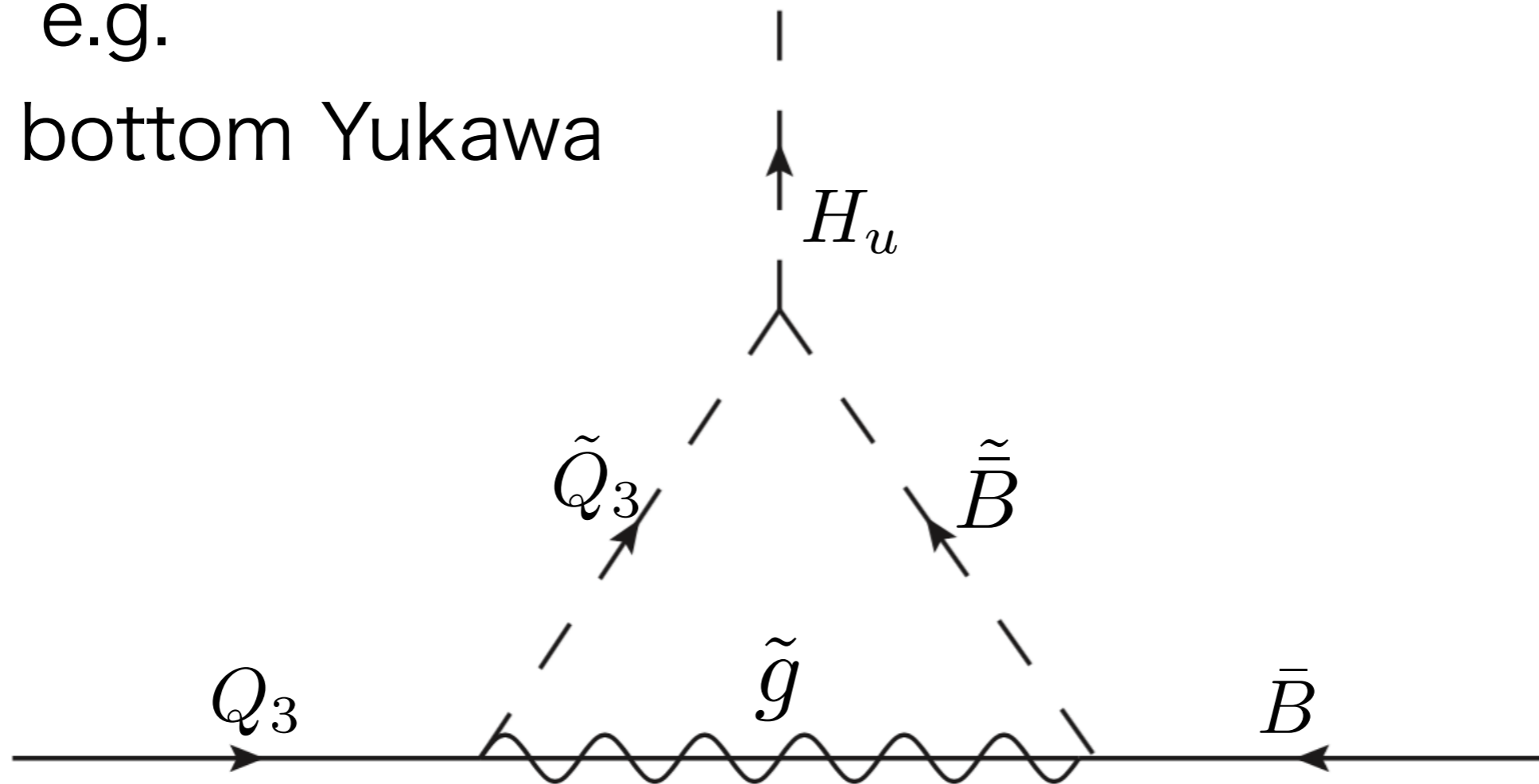
$m_{3/2}=160$ TeV



Wino search at the LHC can cover the region consistent with the muon $g-2$ (1σ)

Yukawa coupling unification

e.g.
bottom Yukawa

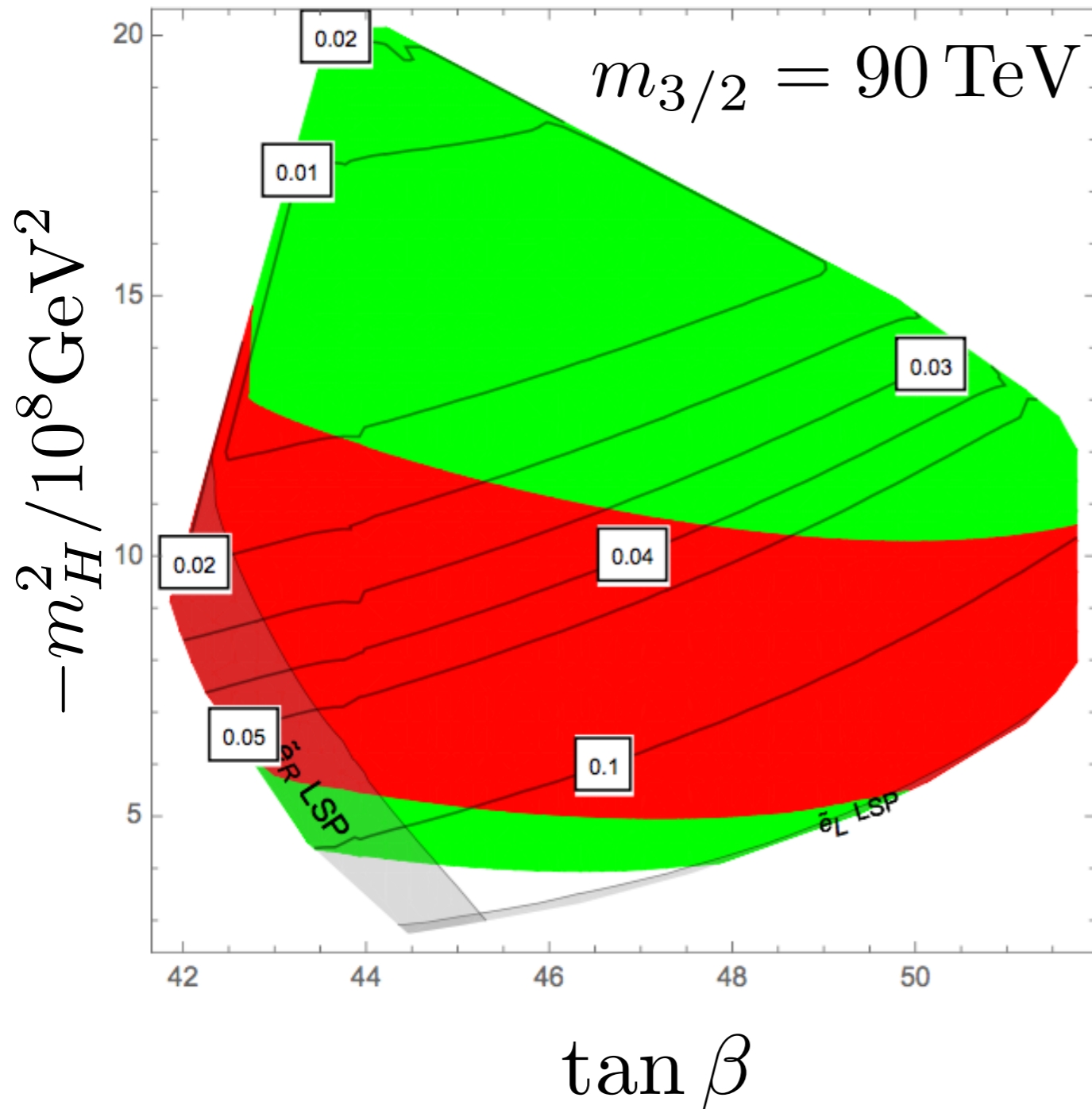


With important threshold corrections

Bottom-Tau unification

Motivated by SU(5)

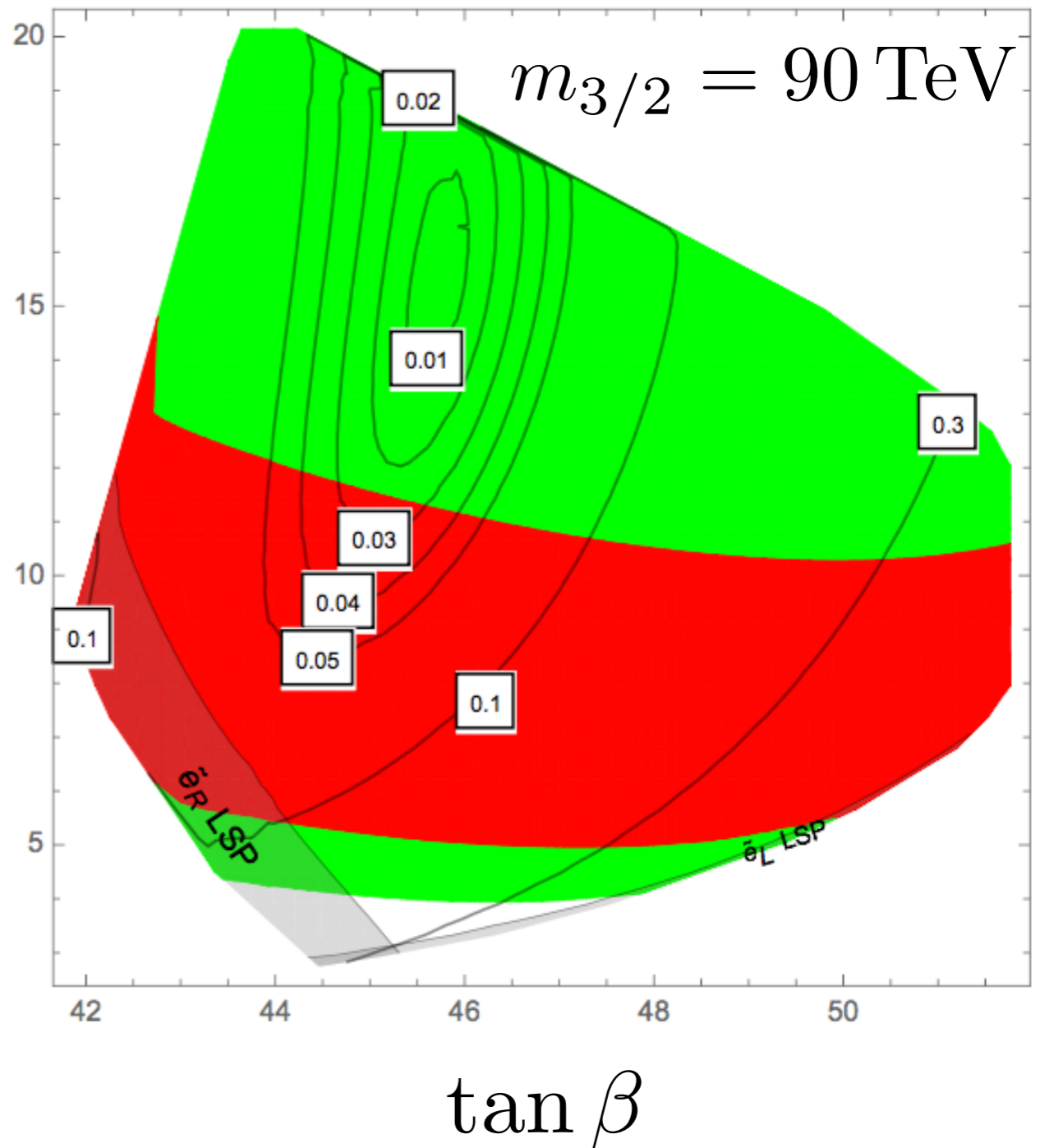
$$\sqrt{(Y_b - Y_\tau)^2}$$



Bottom-Tau-Top unification

Motivated by SO(10)

$$\sqrt{(Y_b - Y_\tau)^2 + (Y_t - Y_\tau)^2 + (Y_t - Y_b)^2}$$



Summary

- We have found a simple model which has many benefits
 - Muon $g-2$ is explained.
 - The Higgs boson mass of 125 GeV is explained with ~ 10 TeV stops.
 - No SUSY flavor problem
 - Tachyonic slepton problem is solved
 - Gravitino problem is significantly relaxed with ~ 100 TeV gravitino

Summary

- Wino, squarks and gluino can be seen at the LHC.
- Yukawa coupling unification is realized.
- No singlet SUSY breaking field is required.
→ Polonyi problem may be relaxed.
- Massless sfermions may be regarded as NG bosons, which may enable us to understand the origin of the family number, three. ([Kugo, Yanagida, 1984](#) ... [Yanagida, Win, Yokozaki, 2016](#))

- Squarks and sleptons get masses from Higgs soft masses, and their hierarchical masses originate from the structure of the Yukawa couplings



Our scenario

- Quarks and leptons get masses from the VEV of the Higgs field, and their hierarchical masses originate from the structure of the Yukawa couplings.

Standard model

The structure seems natural.