# Pick-Ups for bunched Beams

# **Outline:**

- > Signal generation  $\rightarrow$  transfer impedance
- > Capacitive *button* BPM for high frequencies
- > Capacitive *shoe-box* BPM for low frequencies
- Electronics for position evaluation
- > BPMs for measurement of closed orbit, tune and further lattice functions
- > Summary

# Usage of BPMs

# A Beam Position Monitor is an non-destructive device for bunched beams

It has a low cut-off frequency i.e. dc-beam behavior can not be monitored The abbreviation BPM and pick-up PU are synonyms

#### **1. It delivers information about the transverse center of the beam**

- > *Trajectory:* Position of an individual bunch within a transfer line or synchrotron
- Closed orbit: central orbit averaged over a period much longer than a betatron oscillation
- Single bunch position  $\rightarrow$  determination of parameters like tune, chromaticity,  $\beta$ -function
- > Bunch position on a large time scale: bunch-by-bunch  $\rightarrow$  turn-by-turn  $\rightarrow$  averaged position
- > Time evolution of a single bunch can be compared to 'macro-particle tracking' calculations
- Feedback: fast bunch-by-bunch damping *or* precise (and slow) closed orbit correction

2. Information on longitudinal bunch behavior (see next chapter)

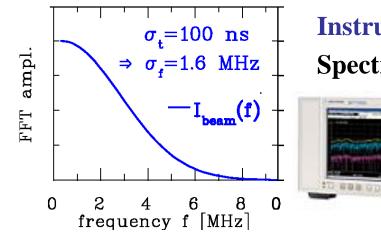
- Bunch shape and evolution during storage and acceleration
- ➢ For proton LINACs: the beam velocity can be determined by two BPMs
- ➢ For electron LINACs: Phase measurement by Bunch Arrival Monitor
- *Relative* low current measurement down to 10 nA.

#### Excurse: Time Domain $\leftrightarrow$ Frequency Domain

#### **Time domain: Recording of a voltage as a function of time:**



**Frequency domain:** Displaying of a voltage as a function of frequency:



Instrument: Spectrum Analyzer

Fourier Transformation of time domain data <u>Care:</u> Contains amplitude <u>and</u> phase

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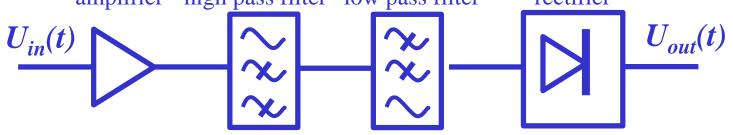
#### Excurse: Properties of Fourier Transformation

**Fourier Transform.:**  $\widetilde{f}(\omega) \equiv \frac{1}{\sqrt{2\pi}} \int_{-\infty}^{\infty} f(t)e^{-i\omega t} dt$  **Inv. F. T.:**  $f(t) \equiv \frac{1}{\sqrt{2\pi}} \int_{-\infty}^{\infty} \widetilde{f}(\omega)e^{i\omega t} d\omega$ tech. *DFT(f)* or *FFT(f)* tech. *DFT(f)* or *FFT(f)*  $\Rightarrow$  a process can be described either with f(t) 'time domain' or  $\tilde{f}(\omega)$  'frequency domain'  $\rightarrow$  tech.: DFT is discrete FT, FFT is a dedicated algorithm for **fast** calculation with 2<sup>n</sup> increments **No loss of information:** If  $\tilde{f}(\omega) = \frac{1}{\sqrt{2\pi}} \int f(t)e^{-i\omega t} dt$  exists, than  $f(t) = \frac{1}{2\pi} \int \int f(\tau)e^{i\omega(t-\tau)} d\omega d\tau$ FT is complex:  $\tilde{f}(\omega) \in C \rightarrow \text{tech. amplitude } A(\omega) = |\tilde{f}(\omega)| \text{ and phase } \varphi$ For  $f(t) \in R \Rightarrow A(\omega)$  is even and  $\varphi(\omega)$  is odd function of  $\omega$ Similarity Law: For  $a \neq 0$  it is for f(at):  $|1/a| \cdot \tilde{f}(\omega/a) = \frac{1}{\sqrt{2\pi}} \int_{0}^{\infty} f(at)e^{-i\omega t} dt$   $\rightarrow$  the properties can be called to  $\tilde{f}(at) = \frac{1}{\sqrt{2\pi}} \int_{0}^{\infty} f(at)e^{-i\omega t} dt$ Re(z) $\rightarrow$  the properties can be scaled to any frequency range; 'shorter time signal have wider FT' **Differentiation Law:**  $(i\omega)^n \cdot \tilde{f}(\omega) = \frac{1}{\sqrt{2\pi}} \int f^{(n)}(t) e^{-i\omega t} dt$  $\rightarrow$  differentiation in time domain corresponds to multiplication with  $i\omega$  in frequency domain **Convolution Law:** For  $f(t) = f_1(t) * f_2(t) \equiv \int f_1(\tau) \cdot f_2(t-\tau) d\tau$  $\Rightarrow \quad \widetilde{f}(\omega) = \widetilde{f}_1(\omega) \cdot \widetilde{f}_2(\omega) \quad \rightarrow \text{ convolution}^\circ \text{ be expressed as multiplication of FT}$ Peter Forck, JUAS Archamps Pick-Ups for bunched Beams

Excurse: Properties of Fourier Trans.  $\rightarrow$  technical Realization

**Convolution Law:** For 
$$f(t) = f_1(t) * f_2(t) \equiv \int_{\infty}^{\infty} f_1(\tau) \cdot f_2(t-\tau) d\tau$$
  
 $\Rightarrow \quad \tilde{f}(\omega) = \tilde{f}_1(\omega) \cdot \tilde{f}_2(\omega)$ 

→ convolution in time domain can be expressed as multiplication of FT in frequency domain Application: Chain of electrical elements calculated in frequency domain more easily parameters are more easy in frequency domain (bandwidth, *f*-dependent amplification....) amplifier high pass filter low pass filter rectifier



**Engineering formulation for <u>finite</u> number of discrete samples:** 

**Digital Fourier Transformation**.: *DFT(f)* 

Fast Fourier Transformation: FFT(f), special numerical algorithm for  $2^n$  samples

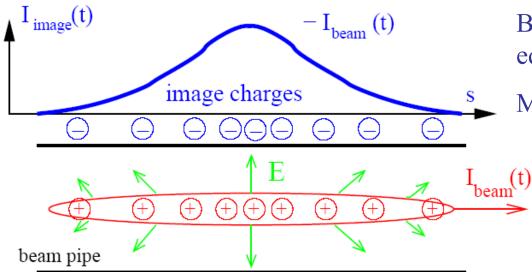
**Transfer function**  $H(\omega)$  and h(t) describe of electrical elements

Calculation with  $H(\omega)$  in frequency domain or

h(t) time domain  $\rightarrow$  'Finite Impulse Response' FIR filter or 'Infinite Impulse Response' IIR filter

# Pick-Ups for bunched Beams

The image current at the beam pipe is monitored on a high frequency basis i.e. the ac-part given by the bunched beam.



Beam Position Monitor **BPM** equals Pick-Up **PU** 

Most frequent used instrument!

For relativistic velocities, the electric field is transversal:

$$E_{\perp,lab}(t) = \gamma \cdot E_{\perp,rest}(t')$$

## Signal treatment for capacitive pick-ups:

Longitudinal bunch shape

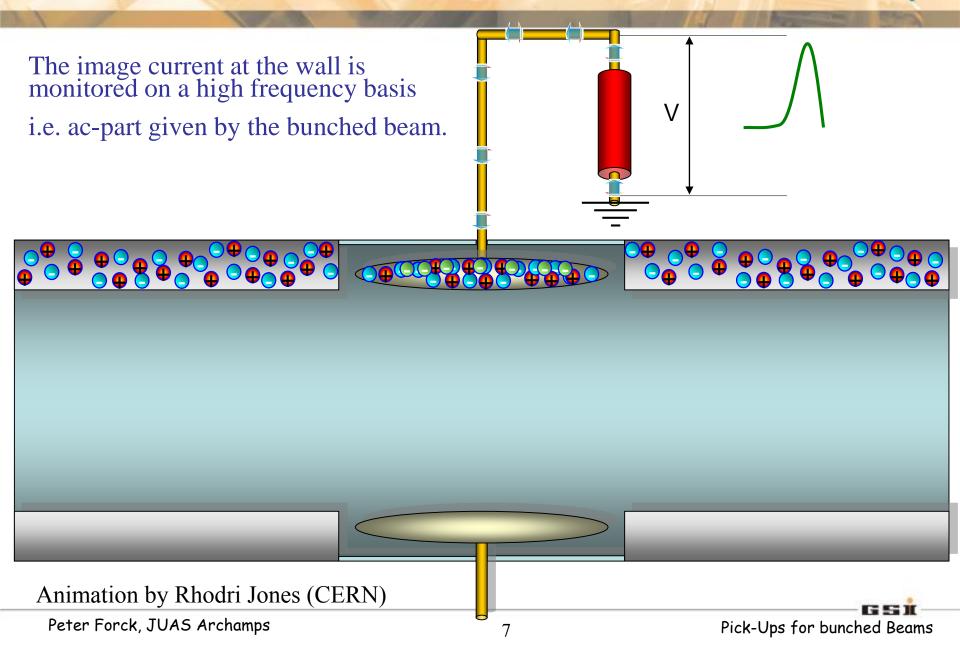
Overview of processing electronics for Beam Position Monitor (BPM)

#### > Measurements:

- Trajectory and closed orbit determination
- > Tune and lattice function measurements (synchrotron only).

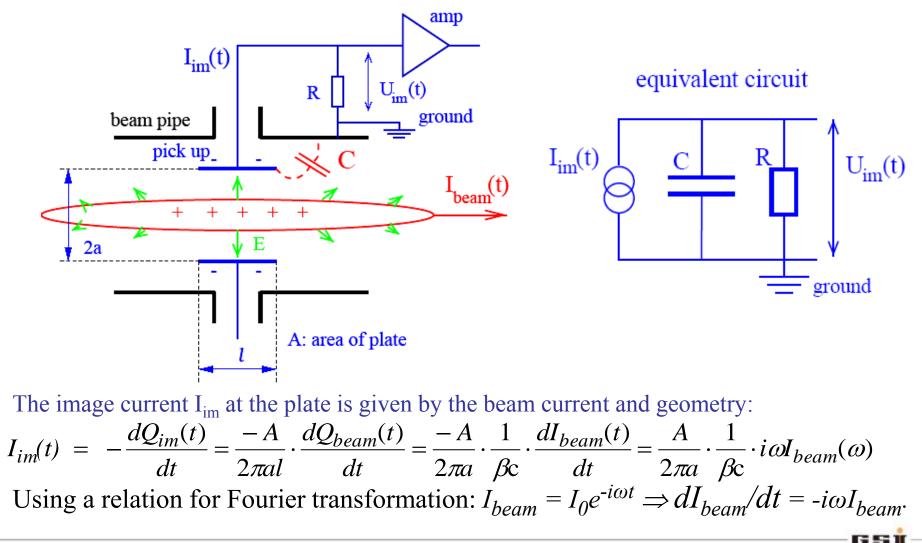
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### Principle of Signal Generation of capacitive BPMs



### Model for Signal Treatment of capacitive BPMs

The wall current is monitored by a plate or ring inserted in the beam pipe:



At a resistor **R** the voltage  $U_{im}$  from the image current is measured. The transfer impedance  $Z_t$  is the ratio between voltage  $U_{im}$  and beam current  $I_{beam}$ in *frequency domain*:  $U_{im}(\omega) = R \cdot I_{im}(\omega) = Z_t(\omega, \beta) \cdot I_{beam}(\omega)$ .

#### Capacitive BPM:

1

- ➤ The pick-up capacitance C: plate ↔ vacuum-pipe and cable.
- > The amplifier with input resistor R.

> The beam is a high-impedance current source:

$$U_{im} = \frac{R}{1 + i\omega RC} \cdot I_{im}$$
$$= \frac{A}{2\pi a} \cdot \frac{1}{\beta c} \cdot \frac{1}{C} \cdot \frac{i\omega RC}{1 + i\omega RC} \cdot I_{beam}$$
$$\equiv Z_t(\omega, \beta) \cdot I_{beam}$$

This is a high-pass characteristic with  $\omega_{cut} = 1/RC$ :

**Amplitude**: 
$$|Z_t(\omega)| = \frac{A}{2\pi a} \cdot \frac{1}{\beta c} \cdot \frac{1}{C} \cdot \frac{\omega / \omega_{cut}}{\sqrt{1 + \omega^2 / \omega_{cut}^2}}$$
 **Phase:**  $\varphi(\omega) = \arctan(\omega_{cut} / \omega)$ 

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 $I_{im}(t)$ 

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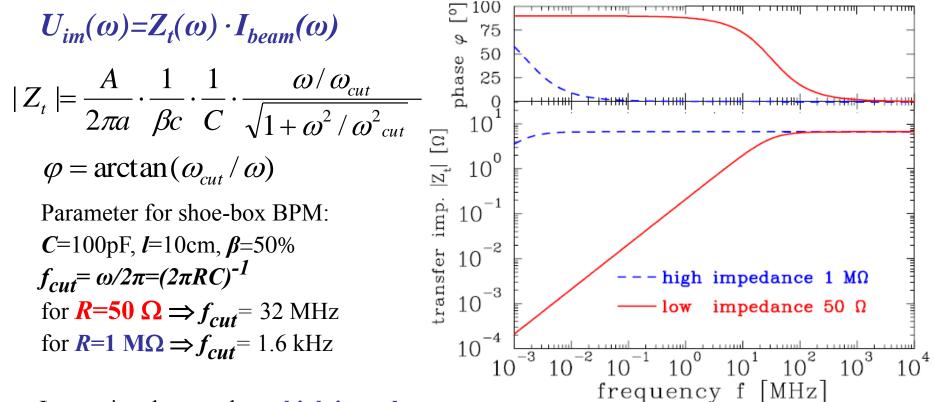
ground

equivalent circuit

 $\frac{1}{Z} = \frac{1}{R} + i\omega C \Leftrightarrow Z = \frac{R}{1 + i\omega BC}$ 

#### Example of Transfer Impedance for Proton Synchrotron

The high-pass characteristic for typical synchrotron BPM:



Large signal strength  $\rightarrow$  high impedance Smooth signal transmission  $\rightarrow$  50  $\Omega$ 

#### Signal Shape for capacitive BPMs: differentiated $\leftrightarrow$ proportional



Depending on the frequency range *and* termination the signal looks different:  $\Rightarrow$  High frequency range  $\omega \gg \omega_{cut}$ :  $1 \quad 1 \quad A$ 

$$Z_t \propto \frac{i\omega/\omega_{cut}}{1+i\omega/\omega_{cut}} \to 1 \Longrightarrow U_{im}(t) = \frac{1}{C} \cdot \frac{1}{\beta c} \cdot \frac{A}{2\pi a} \cdot I_{beam}(t)$$

 $\Rightarrow$  direct image of the bunch. Signal strength  $Z_t \propto A/C$  i.e. nearly independent on length

$$\sum_{t} \sum_{t} \frac{i\omega}{\omega_{cut}} + i\omega/\omega_{cut} \rightarrow i\frac{\omega}{\omega_{cut}} \Rightarrow U_{im}(t) = R \cdot \frac{A}{\beta c \cdot 2\pi a} \cdot i\omega I_{beam}(t) = R \cdot \frac{A}{\beta c \cdot 2\pi a} \cdot \frac{dI_{beam}}{dt}$$

 $\Rightarrow$  derivative of bunch, single strength  $Z_t \propto A$ , i.e. (nearly) independent on C

> Intermediate frequency range  $\omega \approx \omega_{cut}$ : Calculation using Fourier transformation

Example from synchrotron BPM with 50  $\Omega$  termination (reality at p-synchrotron :  $\sigma >>1$  ns): intermediate proportional derivative  $\sigma = 100 \text{ns}$  $\sim \sigma = 10$ ns  $\sigma = 1 \text{ns}$  $I_{beam}(t)$  $U_{im}(t)$ ×10 im 0.6 0.8 1.0 20 80 40 100 2 8 10 0.0 0.2 0.4 60 4 time  $[\mu s]$ time [ns] time [ns]

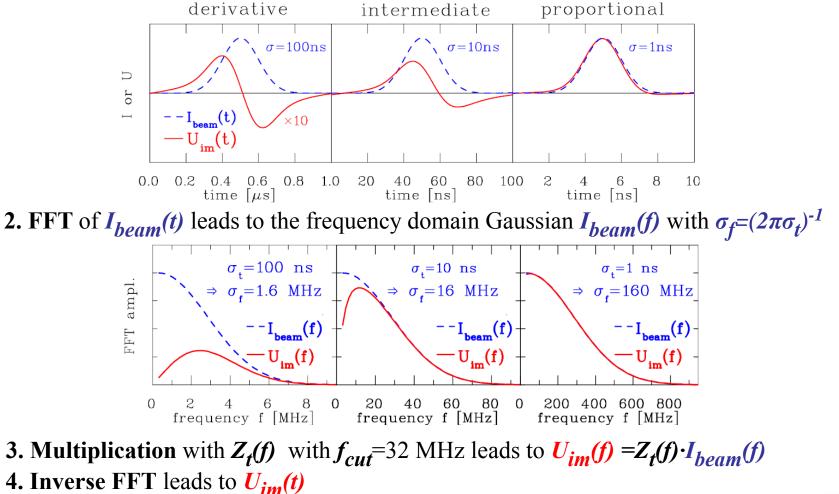
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## Calculation of Signal Shape (here single bunch)

The transfer impedance is used in frequency domain! The following is performed:

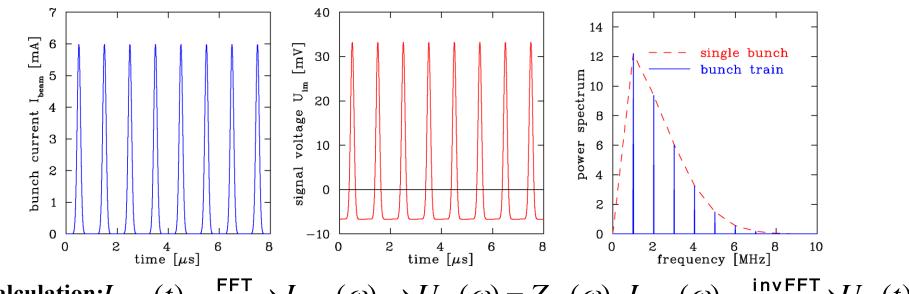
**1. Start:** Time domain Gaussian function  $I_{heam}(t)$  having a width of  $\sigma_t$ 



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#### Calculation of Signal Shape: Bunch Train

Example for low energy proton synchr.: Train of bunches with R=1 M $\Omega \Rightarrow f >> f_{cut}$ 



 $\mathbf{Calculation:} I_{beam}(t) \xrightarrow{\mathsf{FFT}} I_{beam}(\omega) \to U_{im}(\omega) = Z_{tot}(\omega) \cdot I_{beam}(\omega) \xrightarrow{\mathsf{invFFT}} U_{im}(t)$ 

Parameter: R=1 M $\Omega \Rightarrow f_{cut}=2$ kHz,  $Z_t=5\Omega$  all buckets filled, no amp

C=100pF, *l*=10cm,  $\beta$ =50%,  $\sigma_t$ =100 ns  $\Rightarrow \sigma_l$ =15m

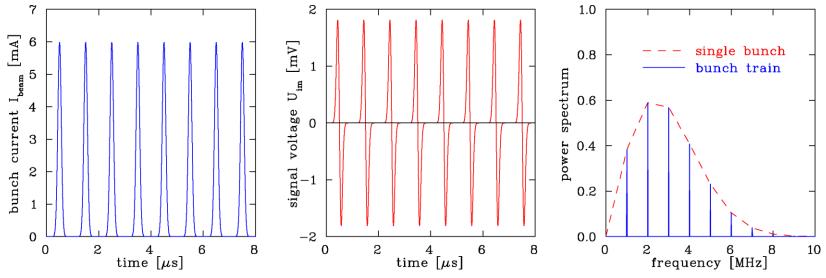
- > Fourier spectrum is composed of lines separated by acceleration  $f_{rf}$
- Envelope given by single bunch Fourier transformation
- ➤ Baseline shift due to ac-coupling

**Remark:** 1 MHz $< f_{rf} <$ 10MHz  $\Rightarrow$  Bandwidth  $\approx$ 100MHz=10 $\cdot f_{rf}$  for broadband observation

### Calculation of Signal Shape: repetitive Bunch in a Synchrotron



Synchrotron filled with 8 bunches accelerated with  $f_{acc}=1$  MHz BPM terminated with  $R=50 \Omega \Rightarrow f_{acc} \ll f_{cut}$ :



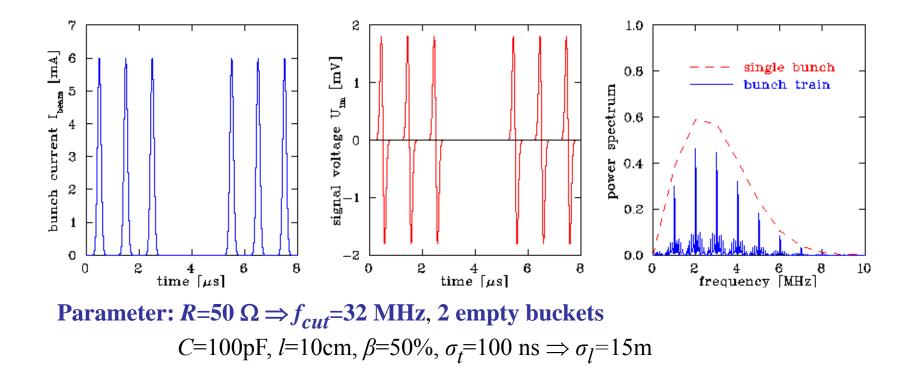
Parameter:  $R=50 \ \Omega \Rightarrow f_{cut}=32 \text{ MHz}$ , all buckets filled C=100 pF, l=10 cm,  $\beta=50\%$ ,  $\sigma_t=100 \text{ ns} \Rightarrow \sigma_l=15 \text{m}$ 

Fourier spectrum is concentrated at acceleration harmonics with single bunch spectrum as an envelope.

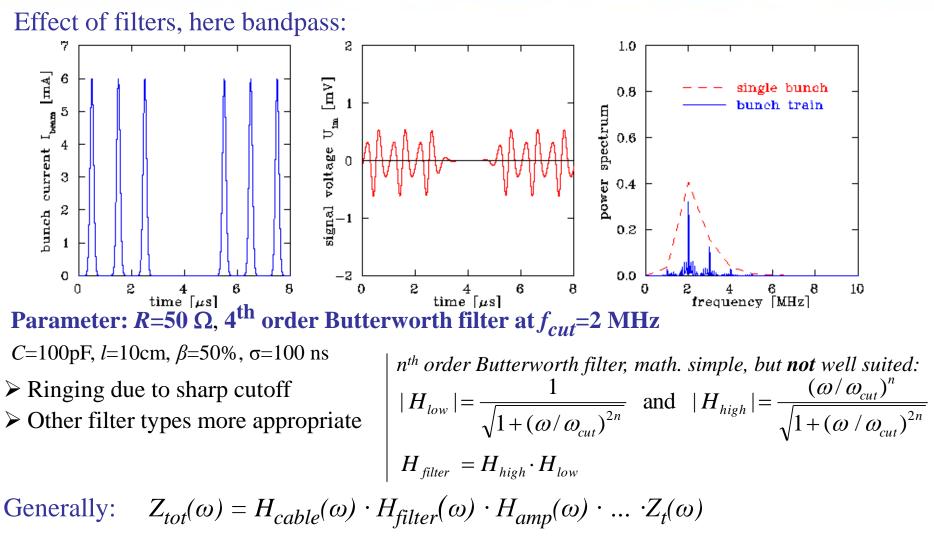
> Bandwidth up to typically  $10*f_{acc}$ 

#### Calculation of Signal Shape: Bunch Train with empty Buckets

#### Synchrotron during filling: Empty buckets, $R=50 \Omega$ :



> Fourier spectrum is more complex, harmonics are broader due to sidebands

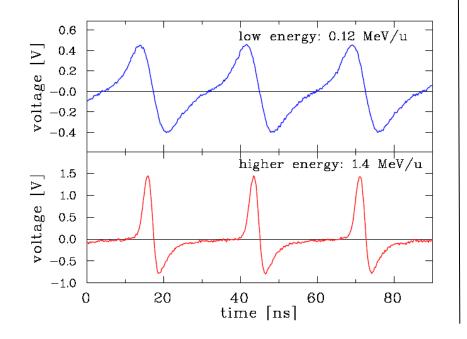


Remark: For numerical calculations, time domain filters (FIR and IIR) are more appropriate

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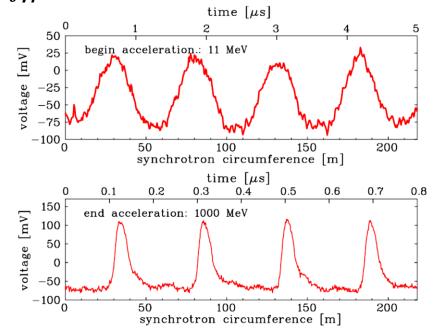
## Examples for differentiated & proportional Shape

### **Proton LINAC, e<sup>-</sup>-LINAC&synchtrotron:** 100 MHz $< f_{rf} < 1$ GHz typically R=50 $\Omega$ processing to reach bandwidth $C \approx 5$ pF $\Rightarrow f_{cut} = 1/(2\pi RC) \approx 700$ MHz *Example:* 36 MHz GSI ion LINAC



#### **Proton synchtrotron:**

1 MHz  $< f_{rf} < 30$  MHz typically R=1 M $\Omega$  for large signal i.e. large  $Z_t$   $C\approx 100$  pF  $\Rightarrow f_{cut} = 1/(2\pi RC) \approx 10$  kHz *Example:* non-relativistic GSI synchrotron  $f_{rf}: 0.8$  MHz  $\rightarrow 5$  MHz



Remark: During acceleration the bunching-factor is increased: 'adiabatic damping'.

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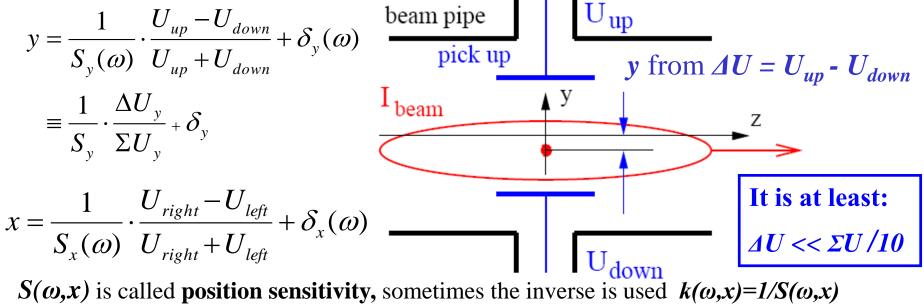
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## Principle of Position Determination by a BPM

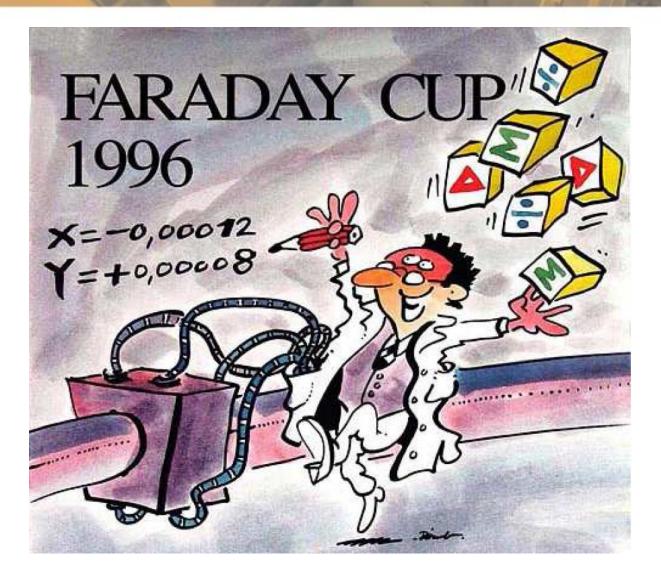
The difference voltage between plates gives the beam's center-of-mass  $\rightarrow$ most frequent application

'Proximity' effect leads to different voltages at the plates:



*S* is a geometry dependent, non-linear function, which have to be optimized Units: S = [%/mm] and sometimes S = [dB/mm] or k = [mm].

#### The Artist View of a BPM





# **Outline:**

- $\succ$  Signal generation  $\rightarrow$  transfer impedance
- Capacitive <u>button</u> BPM for high frequencies

used at most proton LINACs and electron accelerators

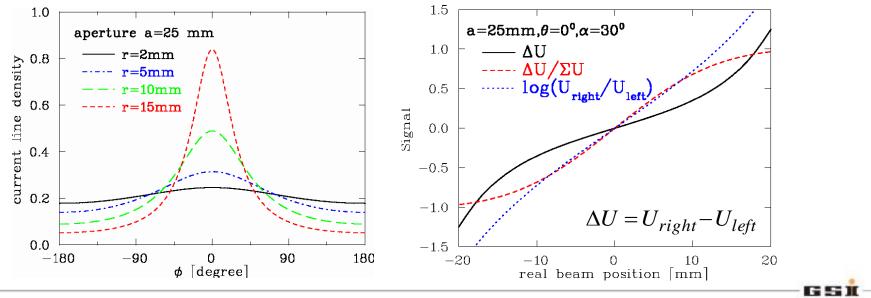
- Capacitive shoe-box BPM for low frequencies
- Electronics for position evaluation
- > BPMs for measurement of closed orbit, tune and further lattice functions
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## 2-dim Model for a Button BPM

**'Proximity effect': larger signal for closer plate Ideal 2-dim model:** Cylindrical pipe  $\rightarrow$  image current density via 'image charge method' for 'pensile' beam:

$$j_{im}(\phi) = \frac{I_{beam}}{2\pi a} \cdot \left(\frac{a^2 - r^2}{a^2 + r^2 - 2ar \cdot \cos(\phi - \theta)}\right)$$

Image current: Integration of finite BPM size:  $I_{im} = a \cdot \int_{-\alpha/2}^{\alpha/2} j_{im}(\phi) d\phi$ 



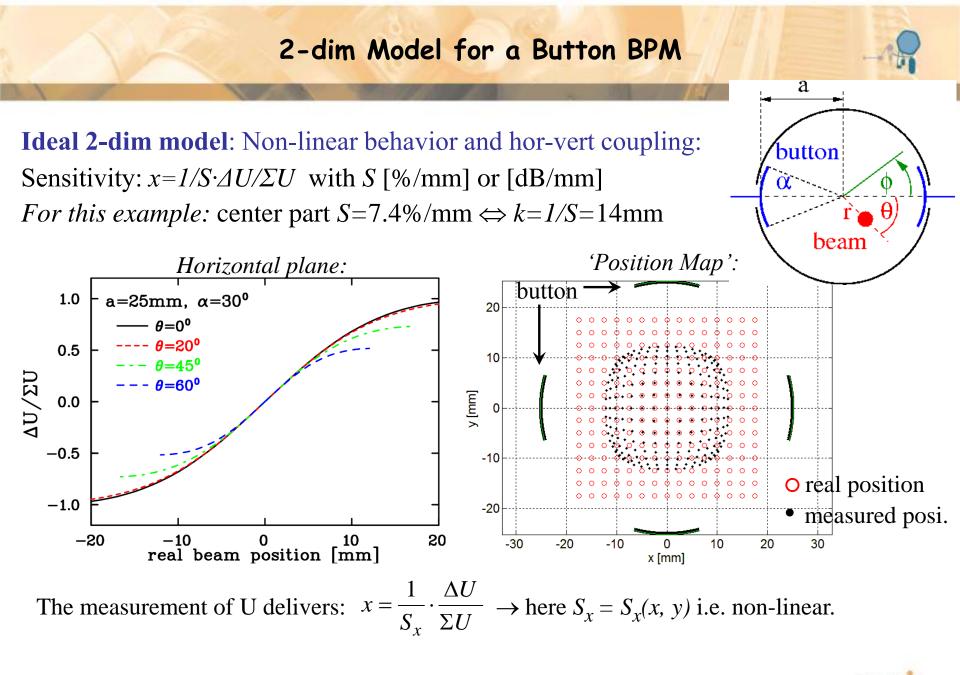
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a

button

beam



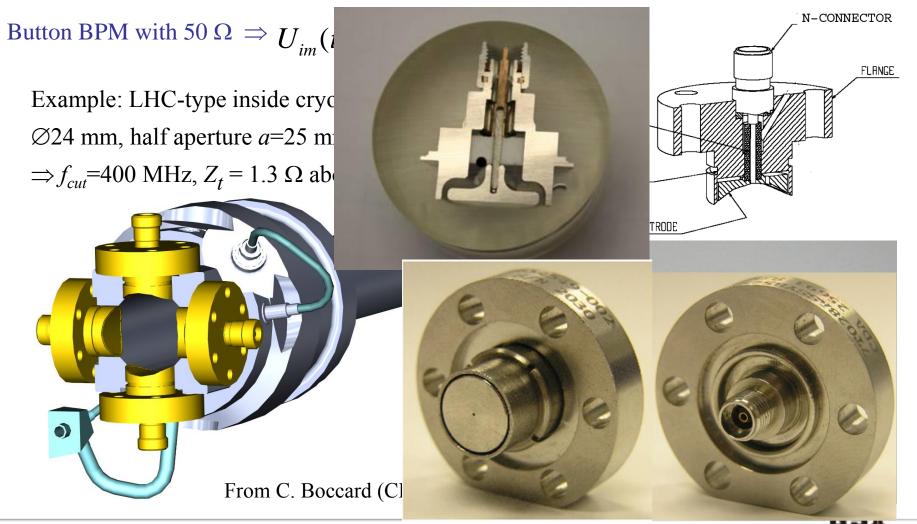
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### **Button BPM Realization**



LINACs, e<sup>-</sup>-synchrotrons: 100 MHz  $< f_{rf} < 3$  GHz  $\rightarrow$  bunch length  $\approx$  BPM length

 $\rightarrow$  50  $\Omega$  signal path to prevent reflections



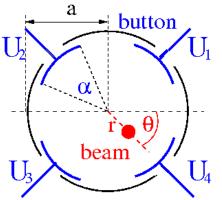
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## Button BPM at Synchrotron Light Sources

The button BPM can be rotated by  $45^0$  to avoid exposure by synchrotron light:

Frequently used at boosters for light sources



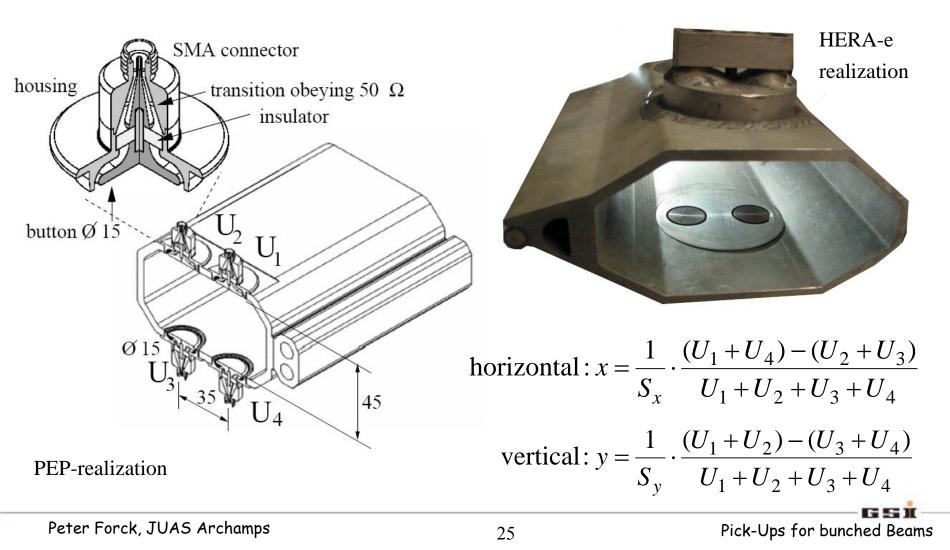
horizontal: 
$$x = \frac{1}{S} \cdot \frac{(U_1 + U_4) - (U_2 + U_3)}{U_1 + U_2 + U_3 + U_4}$$
  
vertical:  $y = \frac{1}{S} \cdot \frac{(U_1 + U_2) - (U_3 + U_4)}{U_1 + U_2 + U_3 + U_4}$ 

#### Example: Booster of ALS, Berkeley



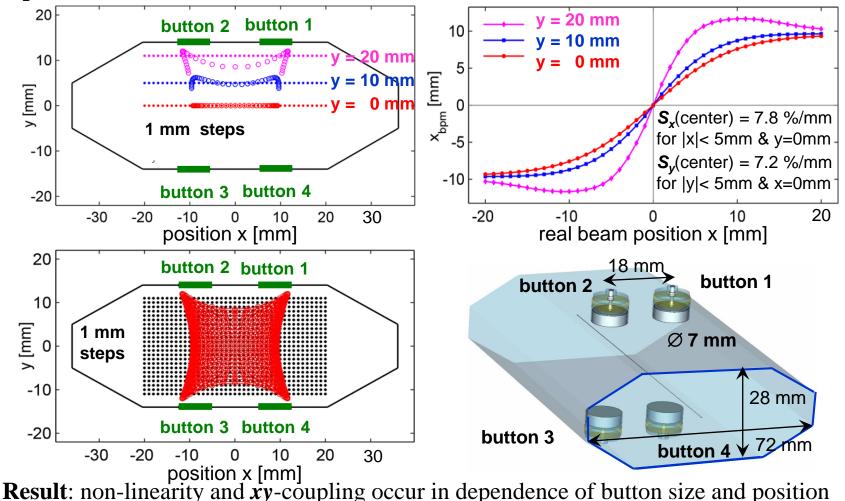
# Button BPM at Synchrotron Light Sources

Due to synchrotron radiation, the button insulation might be destroyed  $\Rightarrow$  buttons only in vertical plane possible  $\Rightarrow$  increased non-linearity



# Simulations for Button BPM at Synchrotron Light Sources

*Example:* Simulation for ALBA light source for 72 x 28 mm<sup>2</sup> chamber **Optimization:** horizontal distance and size of buttons



GSI



# **Outline:**

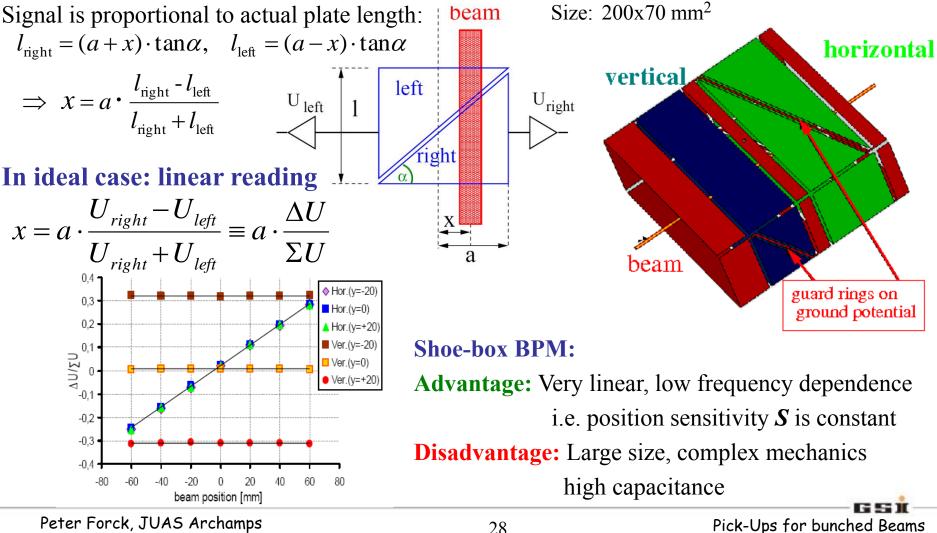
- $\succ$  Signal generation  $\rightarrow$  transfer impedance
- Capacitive button BPM for high frequencies used at most proton LINACs and electron accelerators
- Capacitive <u>shoe-box</u> BPM for low frequencies

used at most proton synchrotrons due to linear position reading

- Electronics for position evaluation
- > BPMs for measurement of closed orbit, tune and further lattice functions
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#### Shoe-box BPM for Proton Synchrotrons

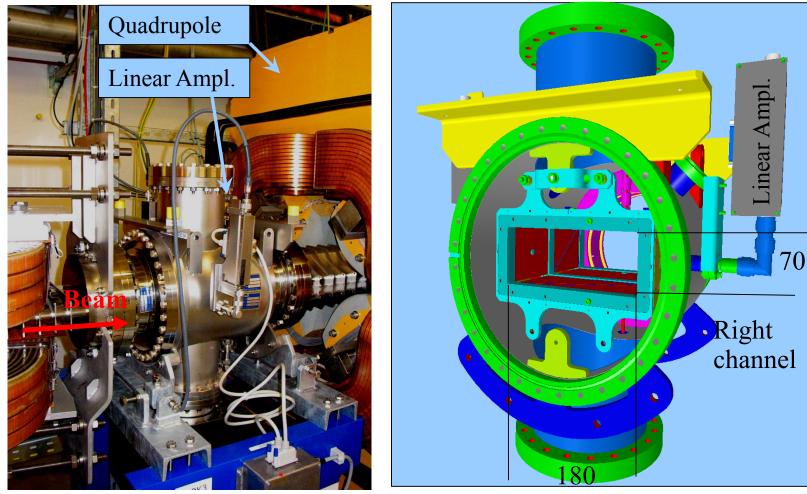
## Frequency range: 1 MHz $< f_{rf} < 10$ MHz $\Rightarrow$ bunch-length >> BPM length.



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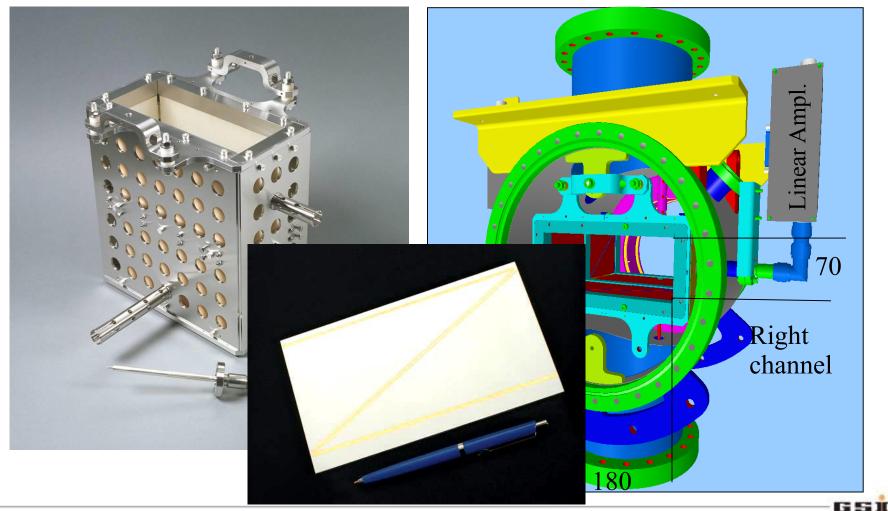
# Technical Realization of a Shoe-Box BPM

Technical realization at HIT synchrotron of 46 m length for 7 MeV/u $\rightarrow$  440 MeV/u BPM clearance: 180x70 mm<sup>2</sup>, standard beam pipe diameter: 200 mm.



## Technical Realization of a Shoe-Box BPM

Technical realization at HIT synchrotron of 46 m length for 7 MeV/u $\rightarrow$  440 MeV/u BPM clearance: 180x70 mm<sup>2</sup>, standard beam pipe diameter: 200 mm.



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# Comparison Shoe-Box and Button BPM



	Shoe-Box BPM	Button BPM
Precaution	Bunches longer than BPM	Bunch length comparable to BPM
<b>BPM length (typical)</b>	10 to 20 cm length per plane	$\varnothing$ 1 to 5 cm per button
Shape	Rectangular or cut cylinder	Orthogonal or planar orientation
Bandwidth (typical)	0.1 to 100 MHz	100 MHz to 5 GHz
Coupling	1 M $\Omega$ or $\approx$ 1 k $\Omega$ (transformer)	50 Ω
Cutoff frequency (typical)	0.01 10 MHz ( <i>C</i> =30100pF)	0.3 1 GHz ( <i>C</i> =210pF)
Linearity	Very good, no x-y coupling	Non-linear, x-y coupling
Sensitivity	Good, care: plate cross talk	Good, care: signal matching
Usage	At proton synchrotrons, $f_{rf} < 10 \text{ MHz}$	All electron acc., proton Linacs, $f_{rf} > 100 \text{ MHz}$
horizontal vertical beam		
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# **Outline:**

- $\succ$  Signal generation  $\rightarrow$  transfer impedance
- Capacitive *button* BPM for high frequencies used at most proton LINACs and electron accelerators
- Capacitive shoe-box BPM for low frequencies used at most proton synchrotrons due to linear position reading
- Electronics for position evaluation
  - analog signal conditioning to achieve small signal processing
- > BPMs for measurement of closed orbit, tune and further lattice functions
   > Summary

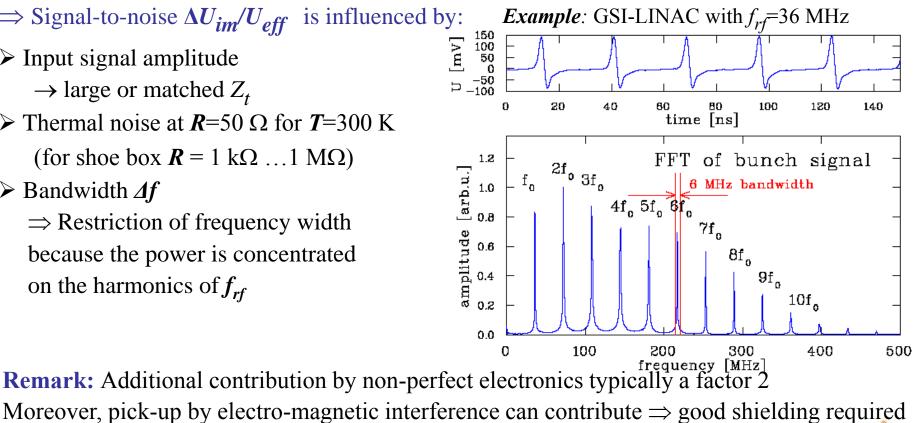
#### General: Noise Consideration

- 1. Signal voltage given by:  $U_{im}(f) = Z_t(f) \cdot I_{beam}(f)$
- 2. Position information from voltage difference:  $x = 1/S \cdot \Delta U / \Sigma U$
- 3. Thermal noise voltage given by:  $U_{eff}(R,\Delta f) = \sqrt{4k_B \cdot T \cdot R \cdot \Delta f}$

 $\Rightarrow$  Signal-to-noise  $\Delta U_{im}/U_{eff}$  is influenced by:

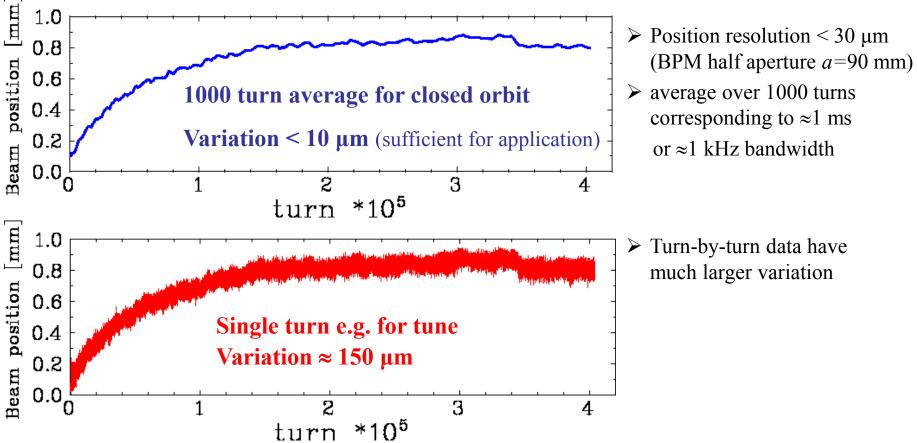
- > Input signal amplitude  $\rightarrow$  large or matched  $Z_t$
- $\blacktriangleright$  Thermal noise at *R*=50  $\Omega$  for *T*=300 K (for shoe box  $\mathbf{R} = 1 \text{ k}\Omega \dots 1 \text{ M}\Omega$ )
- $\succ$  Bandwidth  $\Delta f$

 $\Rightarrow$  Restriction of frequency width because the power is concentrated on the harmonics of  $f_{rf}$ 



#### Comparison: Filtered Signal ↔ Single Turn

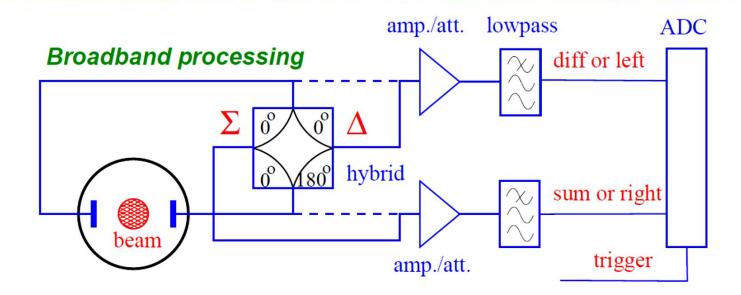
*Example:* GSI Synchr.:  $U^{73+}$ ,  $E_{inj}=11.5$  MeV/u $\rightarrow$  250 MeV/u within 0.5 s, 10<sup>9</sup> ions



*However:* not only noise contributes but additionally **beam movement** by betatron oscillation ⇒ broadband processing i.e. turn-by-turn readout for tune determination.

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#### **Broadband Signal Processing**



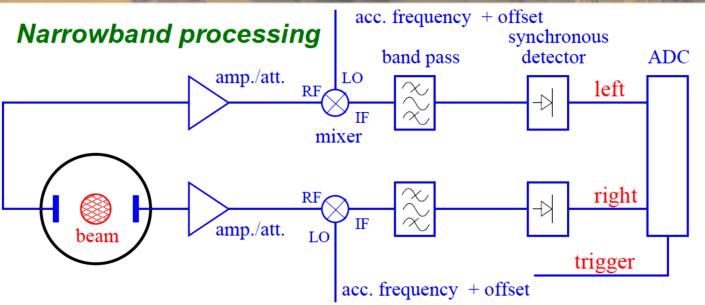
> Hybrid or transformer close to beam pipe for analog  $\Delta U \& \Sigma U$  generation or  $U_{left} \& U_{right}$ 

- Attenuator/amplifier
- Filter to get the wanted harmonics and to suppress stray signals
- ightarrow ADC: digitalization  $\rightarrow$  followed by calculation of of  $\Delta U/\Sigma U$
- Advantage: Bunch-by-bunch possible, versatile post-processing possible

**Disadvantage:** Resolution down to  $\approx 100 \ \mu m$  for shoe box type , i.e.  $\approx 0.1\%$  of aperture,

resolution is worse than narrowband processing

## Narrowband Processing for improved Signal-to-Noise



Narrowband processing equals heterodyne receiver (e.g. AM-radio or spectrum analyzer)

- Attenuator/amplifier
- > Mixing with accelerating frequency  $f_{rf} \Rightarrow$  signal with sum and difference frequency
- ➤ Bandpass filter of the mixed signal (e.g at 10.7 MHz)
- Rectifier: synchronous detector
- → ADC: digitalization → followed calculation of  $\Delta U/\Sigma U$

Advantage: spatial resolution about 100 time better than broadband processing

**Disadvantage:** No turn-by-turn diagnosis, due to mixing = 'long averaging time'

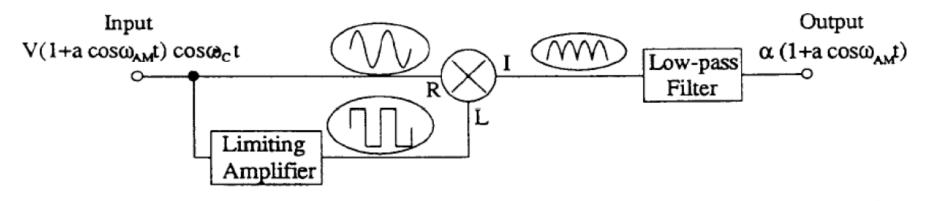
For non-relativistic p-synchrotron:  $\rightarrow$  variable  $f_{rf}$  leads via mixing to constant intermediate freq.

Mixer: A passive rf device with

- > Input RF (radio frequency): Signal of investigation  $A_{RF}(t) = A_{RF} \cos \omega_{RF} t$
- > Input LO (local oscillator): Fixed frequency  $A_{LO}(t) = A_{LO} \cos \omega_{LO} t$
- ✓ Output IF (intermediate frequency)  $A_{IF}(t) = A_{RF} \cdot A_{LO} \cos \omega_{RF} t \cdot \cos \omega_{LO} t$   $= A_{RF} \cdot A_{LO} \left[ \cos(\omega_{RF} \omega_{LO})t + \cos(\omega_{RF} + \omega_{LO})t \right]$

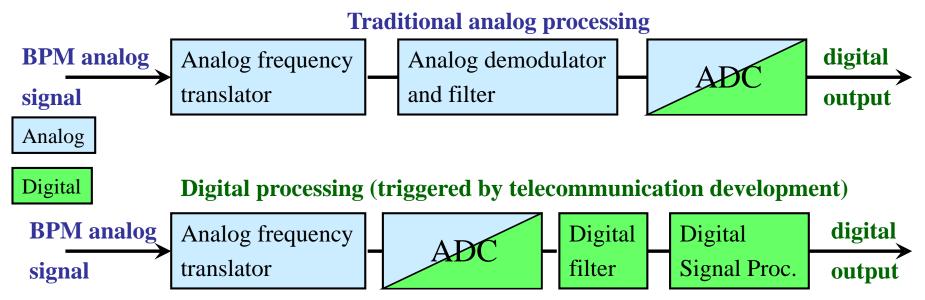
 $\Rightarrow$  Multiplication of both input signals, containing the sum and difference frequency.

Synchronous detector: A phase sensitive rectifier



# Analog versus Digital Signal Processing

Modern instrumentation uses **digital** techniques with extended functionality.



#### Digital receiver as modern successor of super heterodyne receiver

- ➢ Basic functionality is preserved but implementation is very different
- Digital transition just after the amplifier & filter or mixing unit
- ➢ Signal conditioning (filter, decimation, averaging) on FPGA

Advantage of DSP: Versatile operation, flexible adoption without hardware modification **Disadvantage of DSP: non**, good engineering skill requires for development, expensive

Туре	Usage	Precaution	Advantage	Disadvantage
Broadband	p-sychr.	Long bunches	Bunch structure signal Post-processing possible Required for fast feedback	Resolution limited by noise
Narrowband	all synchr.	Stable beams >100 rf-periods	High resolution	No turn-by-turn Complex electronics
Digital Signal Processing	all	Several bunches ADC 125 MS/s	Very flexible High resolution <b>Trendsetting technology</b> <b>for future demands</b>	Limited time resolution by ADC $\rightarrow$ undersampling complex and expensive



# **Outline:**

- $\succ$  Signal generation  $\rightarrow$  transfer impedance
- Capacitive *button* BPM for high frequencies used at most proton LINACs and electron accelerators
- Capacitive shoe-box BPM for low frequencies used at most proton synchrotrons due to linear position reading
- Electronics for position evaluation analog signal conditioning to achieve small signal processing
- > BPMs for measurement of closed orbit, tune and further lattice functions frequent application of BPMs
- > Summary

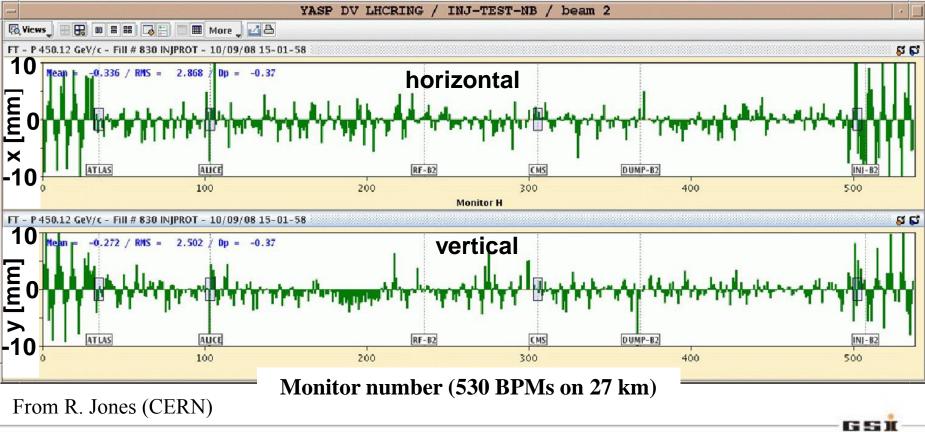
### Trajectory Measurement with BPMs

#### **Trajectory:**

The position delivered by an **individual bunch** within a transfer line or a synchrotron.

Main task: Control of matching (center and angle), first-turn diagnostics

*Example:* LHC injection 10/09/08 i.e. first day of operation !

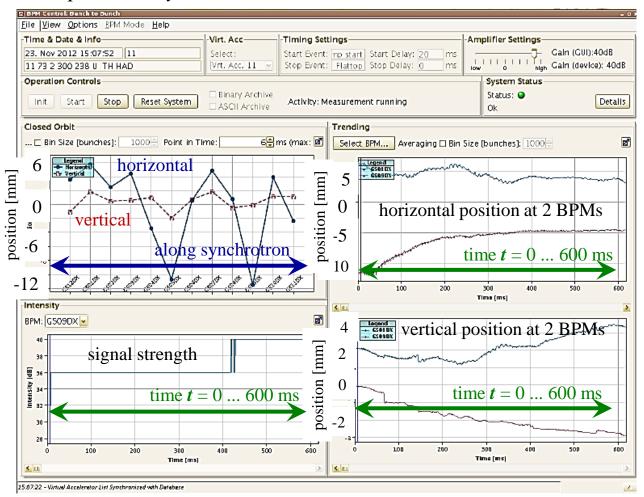


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### **Close Orbit Measurement with BPMs**



Single bunch position averaged over 1000 bunches  $\rightarrow$  closed orbit with ms time steps. It differs from ideal orbit by misalignments of the beam or components. *Example: GSI-synchrotron at two BPM locations, 1000 turn average during acceleration:* 



#### **Closed orbit:**

Beam position averaged over many turns (i.e. betatron oscillations). The result is the basic tool for alignment & stabilzation

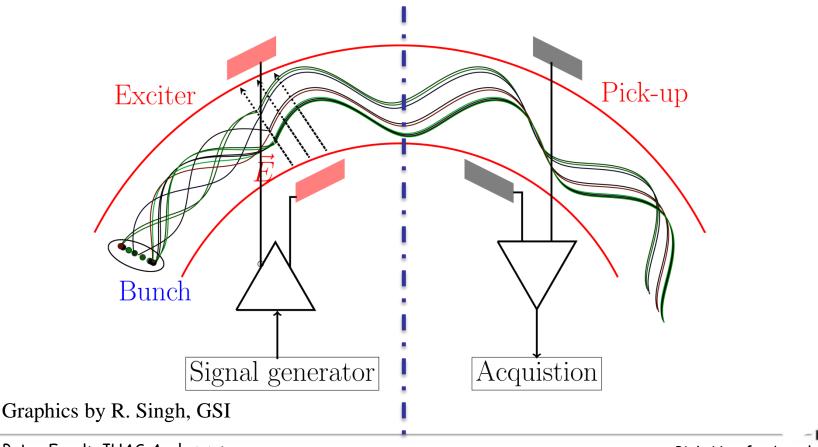
**Remark as a <u>role of thumb</u>:** Number of BPMs within a synchrotron:  $N_{BPM} \approx 4 \cdot Q$ Relation BPMs  $\leftrightarrow$  tune due to close orbit stabilization feedback (justification outside of the scope of this lecture)

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#### **Tune Measurement: General Considerations**

Coherent excitations are required for the detection by a BPM Beam particle's *in-coherent* motion  $\Rightarrow$  center-of-mass stays constant Excitation of **all** particles by rf  $\Rightarrow$  *coherent* motion  $\Rightarrow$  center-of-mass variation turn-by-turn

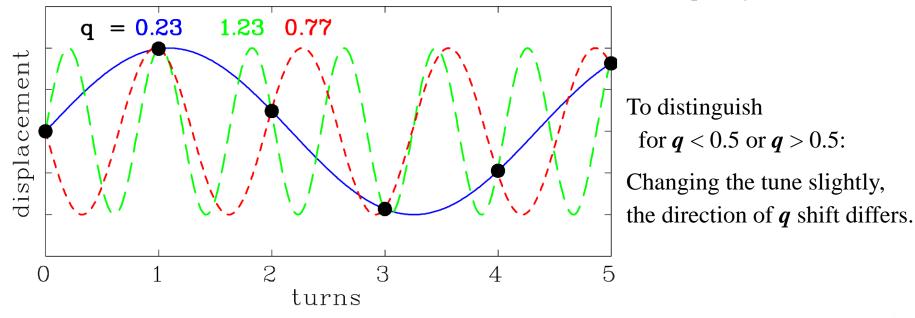


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The tune Q is the number of betatron oscillations per turn. The betatron frequency is  $f_{\beta} = Qf_{0}$ . **Measurement:** excitation of *coherent* betatron oscillations + position from one BPM.

From a measurement one gets only the non-integer part q of Q with  $Q=n\pm q$ . Moreover, only 0 < q < 0.5 is the unique result.

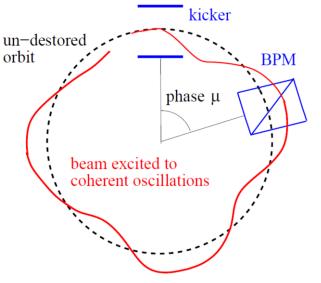
*Example:* Tune measurement for six turns with the three lowest frequency fits:



### Tune Measurement: The Kick-Method in Time Domain

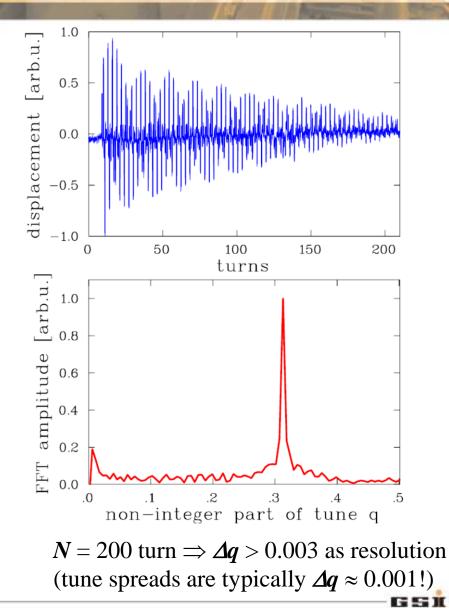
The beam is excited to coherent betatron oscillation → the beam position measured each revolution ('turn-by-turn') → Fourier Trans. gives the non-integer tune *q*.

Short kick compared to revolution.



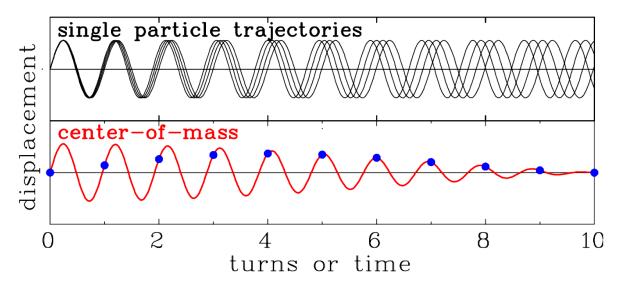
The de-coherence time limits the **resolution**:

- N non-zero samples
- $\Rightarrow$  General limit of discrete FFT:  $\Delta q > \frac{1}{2N}$



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The particles are excited to betatron oscillations, but due to the spread in the betatron frequency, they getting out of phase ('Landau damping'):



Scheme of the individual trajectories of four particles after a kick (top) and the resulting *coherent* signal as measured by a pick-up (bottom).  $\Rightarrow$  Kick excitation leads to limited resolution

Remark: The tune spread is much lower for a real machine.

# Tune Measurement: Beam Transfer Function in Frequency Domain

Instead of one kick, the beam can be excited by a sweep of a sine wave, called 'chirp'

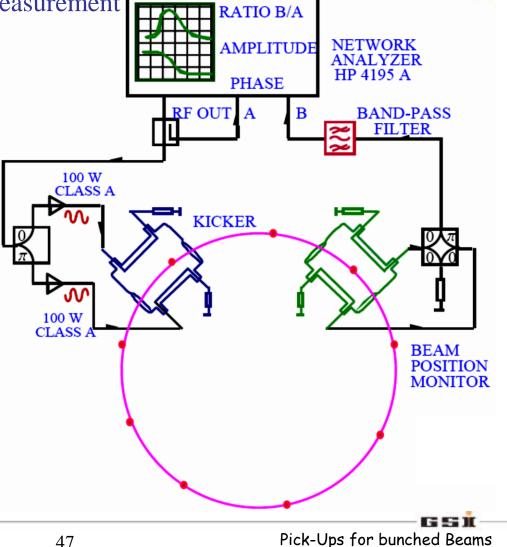
 $\rightarrow$  Beam Transfer Function (BTF) Measurement as the velocity response to a kick

# **Prinziple:**

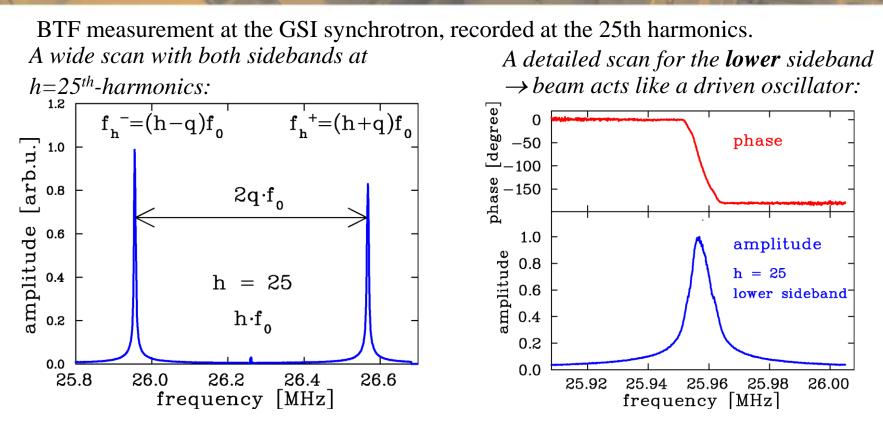
# Beam acts like a driven oscillator!

Using a network analyzer:

- $\triangleright$  RF OUT is feed to the beam by a kicker (reversed powered as a BPM)
- $\blacktriangleright$  The position is measured at one BPM
- > Network analyzer: amplitude and phase of the response
- $\blacktriangleright$  Sweep time up to seconds due to de-coherence time per band
- $\blacktriangleright$  resolution in tune: up to  $10^{-4}$



#### Tune Measurement: Result for BTF Measurement



From the position of the sidebands q = 0.306 is determined. From the width  $\Delta f/f \approx 5 \cdot 10^{-4}$  the tune spread can be calculated via  $\Delta f_h^- = \eta \frac{\Delta p}{p} \cdot h f_0 \left( h - q + \frac{\xi}{\eta} Q \right)$ 

Advantage: High resolution for tune and tune spread (also for de-bunched beams) Disadvantage: Long sweep time (up to several seconds).

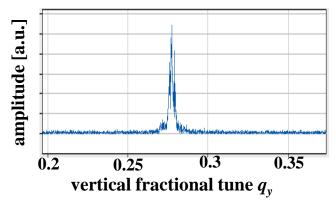
# Tune Measurement: Gentle Excitation with Wideband Noise



Instead of a sine wave, noise with adequate bandwidth can be applied

 $\rightarrow$  beam picks out its resonance frequency: *Example:* Vertical tune within 4096 turn

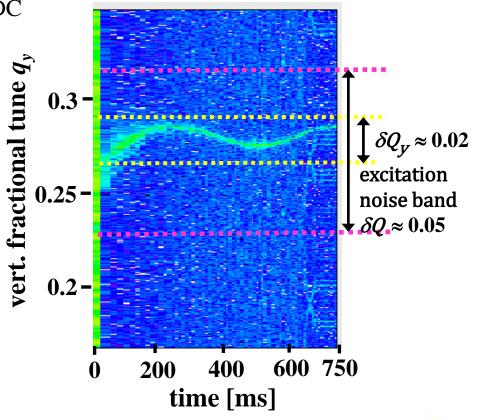
- ➢ broadband excitation with white noise of ≈ 10 kHz bandwidth
- ➤ turn-by-turn position measurement by fast ADC
- $\blacktriangleright$  Fourier transformation of the recorded data
- ⇒ Continues monitoring with low disturbance vertical tune at fixed time ≈ 15ms



#### Advantage:

Fast scan with good time resolution **Disadvantage:** Lower precision

*Example:* Vertical tune within 4096 turn duration  $\approx 15$  ms at GSI synchrotron 11  $\rightarrow$  300 MeV/u in 0.7 s vertical tune versus time



# Excurse: Example of Lattice Functions



The position of dipoles and quadrupoles

- ➢ give the linear lattice functions
- $\blacktriangleright$  at injection point D = 0 is favored
- $\blacktriangleright$  chromatic correction with sextupoles,

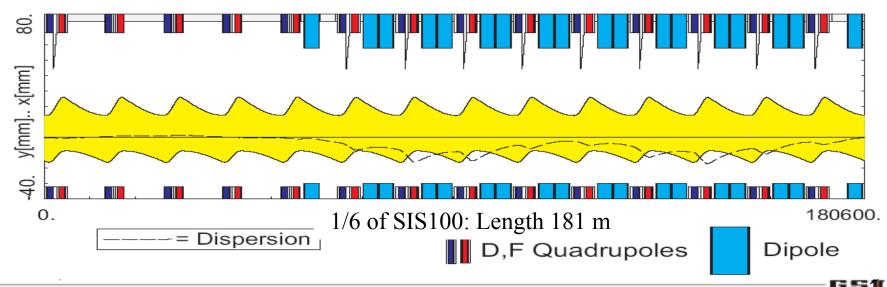
Definition of dispersion *D*(*s*):

 $x_D(s) = D(s) \cdot \Delta p/p_0$ Definition of chromaticity  $\xi$  per turn:

 $\Delta Q/Q_0 = \xi \cdot \Delta p/p_0$ 

#### *Example*: GSI SIS100 ion synchrotron

Length [m]		1086
Energy [GeV]		$0.2 \rightarrow 2$
Tune	h/v	18.84 / 18.73
Max. dispersion /D/ [m]		1.73
Max. $\beta$ –function [m]	h/v	19.6 / 19.6
Natural chromaticity $\xi$	h/v	-1.19 / -1.20
Injected emittance $\varepsilon$ [mm mrad]	h/v	35 / 15
Injected $\Delta p/p_0$ [%]		0.05



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Pick-Ups for bunched Beams

# $\beta$ -Function Measurement from Bunch-by-Bunch BPM Data



Excitation of coherent betatron oscillations: From the position deviation  $x_{ik}$  at the BPM *i* and turn *k* the  $\beta$ -function  $\beta(s_i)$  can be evaluated.

The position reading is: ( $\hat{x}_i$  amplitude,  $\mu_i$  phase at i, Q tune,  $s_0$  reference location)

$$x_{ik} = \hat{x}_i \cdot \cos\left(2\pi Qk + \mu_i\right) = \hat{x}_0 \cdot \sqrt{\beta(s_i)/\beta(s_0)} \cdot \cos\left(2\pi Qk + \mu_i\right)$$

 $\rightarrow$  a turn-by-turn position reading at many location (4 per unit of tune) is required. The ratio of  $\beta$ -functions at different location:

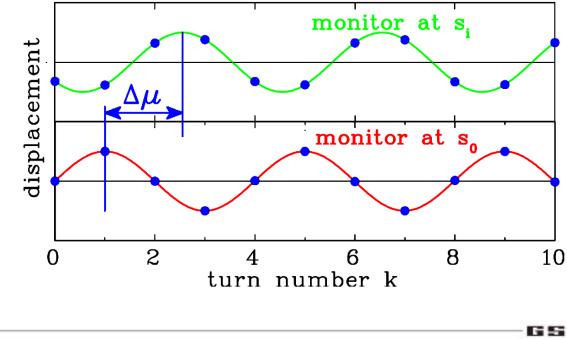
$$\frac{\beta(s_i)}{\beta(s_0)} = \left(\frac{\hat{x}_i}{\hat{x}_0}\right)^2$$

The phase advance is:

$$\Delta \mu = \mu_i - \mu_0$$

Without absolute calibration,  $\beta$ -function is more precise:

$$\Delta \mu = \int_{S0}^{Si} \frac{ds}{\beta(s)}$$



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**Dispersion**  $D(s_i)$ : Excitation of coherent betatron oscillations and change of momentum p by detuned rf-cavity:  $\Delta p$ 

 $\rightarrow$  Position reading at one location:  $x_i = D(s_i) \cdot \frac{\Delta p}{p}$ 

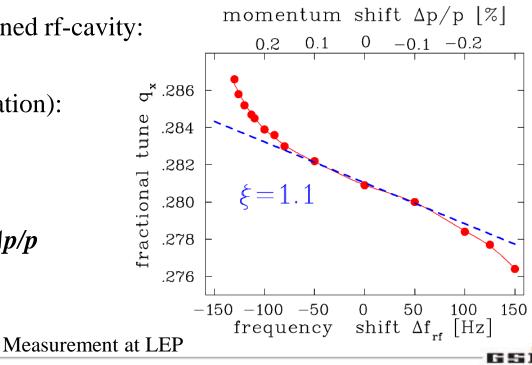
 $\rightarrow$  Result from plot of  $x_i$  as a function of  $\Delta p/p \Rightarrow$  slope is local dispersion  $D(s_i)$ .

*Chromaticity*  $\xi$ : Excitation of coherent betatron oscillations and change of momentum *p* by detuned rf-cavity:

→ Tune measurement (kick-method, BTF, noise excitation):

$$\frac{\Delta Q}{Q} = \xi \cdot \frac{\Delta p}{p}$$

Plot of  $\Delta Q/Q$  as a function of  $\Delta p/p$  $\Rightarrow$  slope is dispersion  $\xi$ .



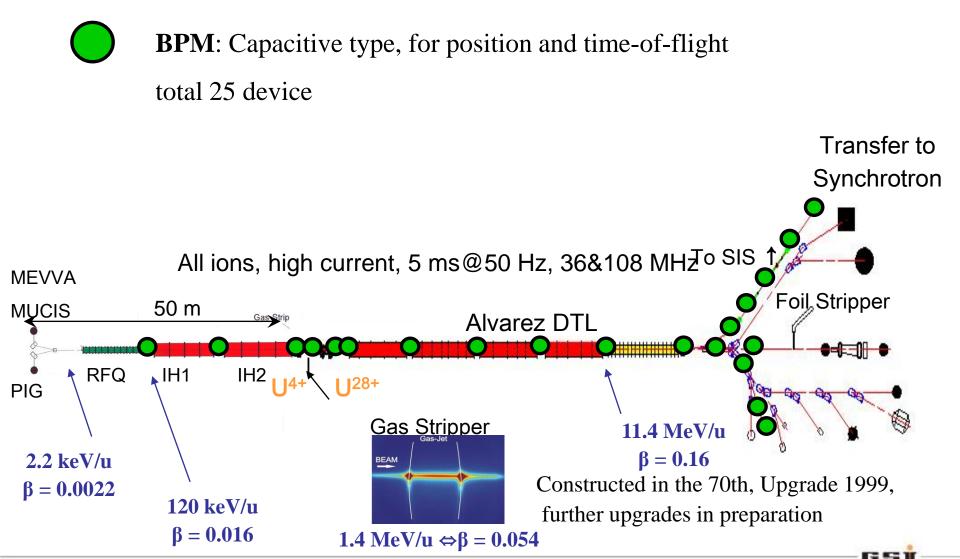
The electric field is monitored for bunched beams using rf-technologies ('frequency domain'). Beside transfromers they are the most often used instruments! **Differentiated or proportional signal:** rf-bandwidth  $\leftrightarrow$  beam parameters **Proton synchrotron:** 1 to 100 MHz, mostly 1 M $\Omega \rightarrow$  proportional shape LINAC, e--synchrotron: 0.1 to 3 GHz, 50  $\Omega \rightarrow$  differentiated shape Important quantity: transfer impedance  $Z_t(\omega, \beta)$ .

**Types of capacitive pick-ups:** 

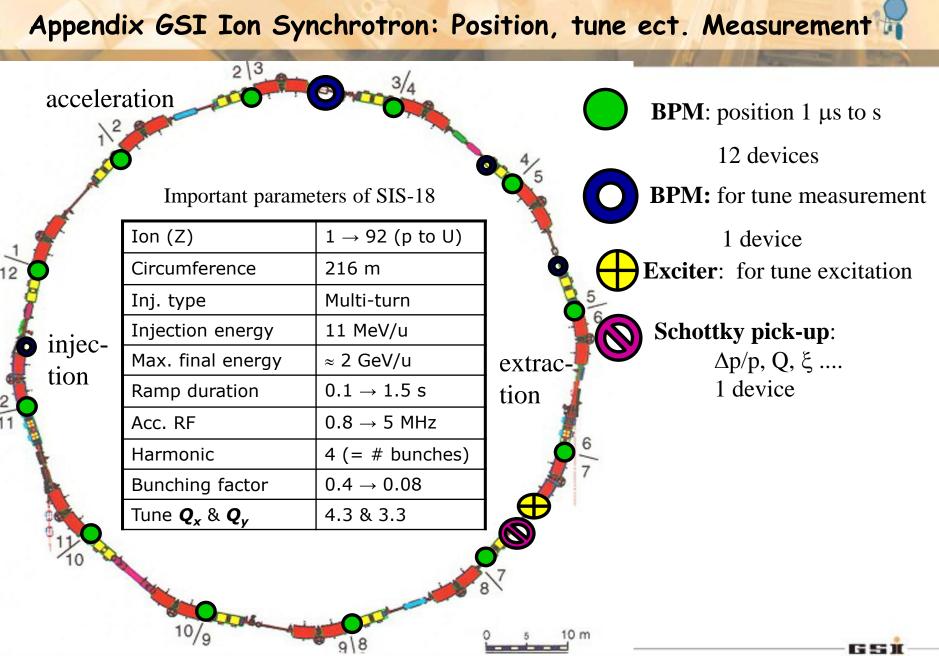
Shoe-box (p-synch.), button (p-LINAC, e–-LINAC and synch.)*Remark:* Stripline BPM as traveling wave devices are frequently used**Position reading:** difference signal of four pick-up plates (BPM):

- Excitation of *coherent betatron oscillations* and response measurement excitation by short kick, white noise or sine-wave (BTF)
  - $\rightarrow$  tune *q*, chromaticity  $\xi$ , dispersion *D* etc.

Appendix GSI Ion LINAC: Position and mean beam energy Meas.

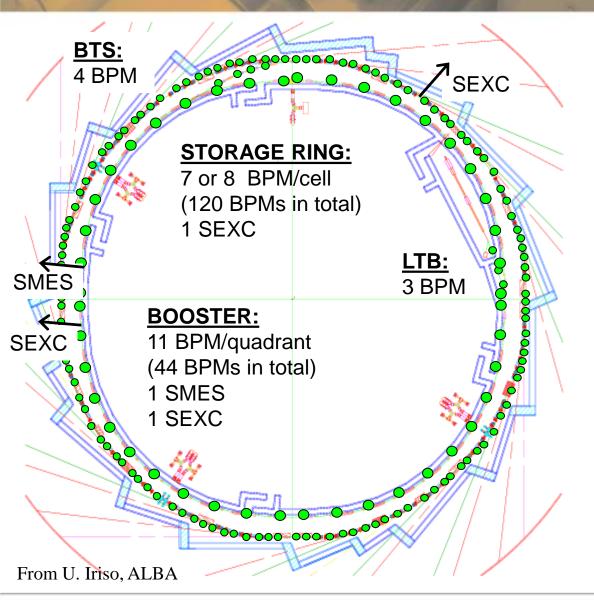


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# Appendix: Synchrotron Light F.ALBA: 'Position, tune ect. Meas.



#### **Beam position:**

Center of mass
≻Many locations!
≻Frequent operating tool
≻For position stabilization i.e. closed otbit feedback

#### **Abbreviation:**

Meas. Stripline  $\rightarrow$  SMES Exc. Stripline  $\rightarrow$  SEXC Button BPMs  $\rightarrow$  BPM