

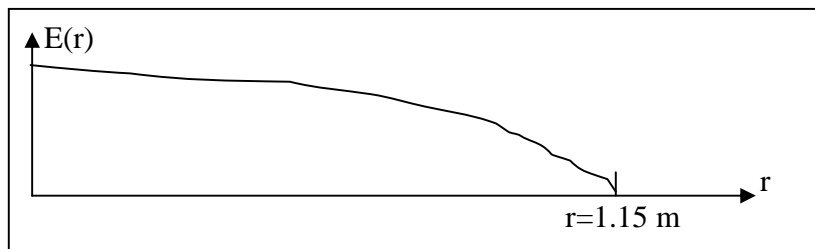
1 For a given pillbox cavity with a radius $R = 1.15$ meter and a height $H=0.5$ meter (7P)
determine

1.1 the resonance frequency for the fundamental mode (TM₀₁₀ type) (1P)

$$f = c_0 / (2.61a) = 100 \text{ MHz}$$

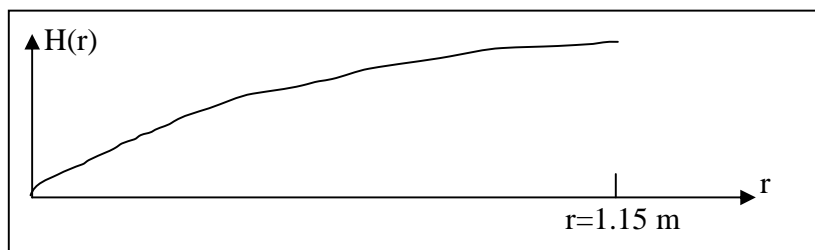
1.2 Indicate qualitatively below the electric field strength $E(r)$ as a function of radius. It is proportional to which function? (1P)

To I_0 (Bessel function of 0th order).



1.3 Indicate qualitatively below the magnetic field strength $H(r)$ as a function of radius. It is proportional to which function? (1P)

To I_1 (Bessel function of first order).



1.4 Which are the ONLY present E- and H- field components in the cavity for the mode mentioned above? (r,φ and z coordinates) (1P)

$$H_r, H_\phi, E_r, E_\phi, E_z$$

1.5 Calculate (general expression and numerical solution) the R/Q and the Q value assuming that the cavity is made from normal copper at room temperature. Neglect the transit time factor! (2P)

$$R/Q = 370 * (H/2) / R = 80.4, Q = 0.383 / \sigma * (1 + 0.192 \lambda / (H/2))^{-1} = 52700$$

1.6 What is the decay time τ of cavity version 1. (general expression using the Q value and numerical result) (1P)

$$t = Q / (\pi * f) = 168 \mu s$$

2 Fill in all the missing fields in the tables below (7P)

2.1 (2P)

Voltage ratio	Power ratio	dB
3.1623	10	10
10	100	20
100	10000	40

2.2 (2P)

dBm (50 Ohm)	RMS Voltage	milli Watt
0	0.224 V	1
+30	7.1 V	1000
-60	0.224 mV	1e-6
20	2.4 V	100

2.3 (1P)

We have got part of the S-matrix of an ideal attenuator. Fill in the missing elements. How many dB are written on this attenuator for its nominal attenuation?

$$[S] = \begin{bmatrix} 0 & 0.1 \\ 0.1 & 0 \end{bmatrix}$$

2.4 (2P)

Now we have an ideal amplifier with perfect input and output match (i.e. input and output impedance are both 50 Ohm) a gain of 40 dB and no reverse transmission. (import: port 1, output: port 2)

$$[S] = \begin{bmatrix} 0 & 0 \\ 100 & 0 \end{bmatrix}$$

3. The locus of impedance of a parallel RLC resonant circuit (without additional transformers) (6P) is given in the complex w-plane (left) [w-plane = normalized z-plane, normalization to 50 Ohm].

- 3.1 Transform this locus of impedance into the Smith Chart. See Smith Chart (1P)
- 3.2 Mark the resonance frequency both in the w-plane and in the Smith Chart (1P)
- (select between f1, f2, f3). Point C (f2)
- 3.3 Show (with a mark) the -3dB points (for unloaded Q) both in the w-plane and (1P)
- in the Smith Chart (select between f1, f2, f3). *Points B and C (f1 and f3)*
- 3.4 Determine R and Q and subsequently L and C for this resonator. (2P)
- 3.5 What is R/Q for this resonator? (1P)

$Q = 10, R = 100\text{ Ohms}, R/Q = 10, L = 79.6\text{ microH}, C = 796\text{ pF}$

Smith Chart

