

# The Generalized GDH Sum Rule: Measuring the Neutron and $^3\text{He}$ Spin Structure at Low $Q^2$

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For the JLab Hall A and E97-110 Collaborations

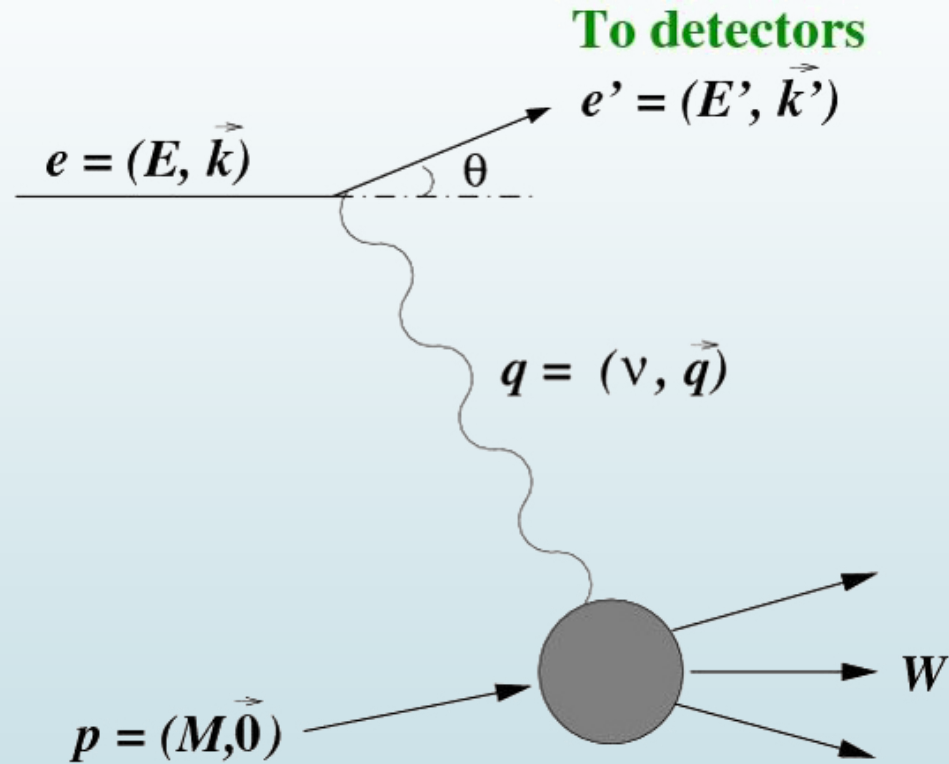
September 26, 2016

22<sup>nd</sup> International Spin Symposium

# Outline

- ▶ Polarized Inclusive Scattering on Nucleon targets
- ▶ Generalized GDH Sum Rule
- ▶ Experimental Progress at low  $Q^2$  (0.02 GeV<sup>2</sup>)
- ▶ Preliminary Results from JLab E97-110

# Polarized Inclusive Scattering



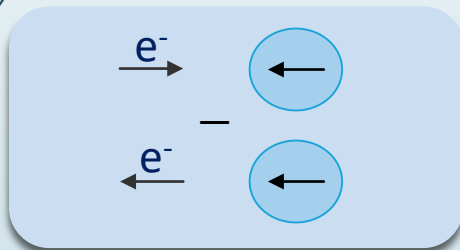
# Cross Sections

$$\sigma_0 = \sigma_{\text{Mott}} [\alpha F_1(x, Q^2) + \beta F_2(x, Q^2) + \gamma g_1(x, Q^2) + \delta g_2(x, Q^2)]$$

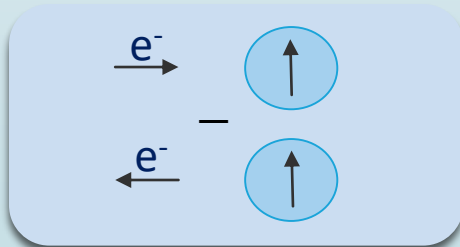
- ▶  $\sigma_0$ : probability of an interaction between incident electron and nucleon target
- ▶  $\sigma_{\text{Mott}}$ : structure-less (point like particles) cross section
- ▶ Structure functions:
  - ▶ Spin averaged  $F_1$  and  $F_2$
  - ▶ Spin dependent  $g_1$  and  $g_2$

# Spin-dependent Structure functions

- Measuring spin-dependent structure functions
  - Asymmetry measurement
  - Electron and target spins are **parallel** (anti-parallel) and **perpendicular**



$$\Delta\sigma^{\parallel} = \frac{4\alpha^2}{MvQ^2} \frac{E'}{E} [(E + E' \cos\theta) g_1 - 2Mx g_2]$$



$$\Delta\sigma^{\perp} = \frac{4\alpha^2}{MvQ^2} \frac{E'^2}{E} \sin\theta [g_1 + \frac{2E}{v} g_2]$$

# GDH Sum Rule

- Gerasimov-Drell-Hearn (GDH) Sum Rule

$$I_{\text{GDH}} = \int_{\nu_{\text{th}}}^{\infty} \frac{\sigma_{\frac{1}{2}}(\nu) - \sigma_{\frac{3}{2}}(\nu)}{\nu} d\nu = -2\pi^2 \alpha \left(\frac{\kappa}{M}\right)^2$$

- Circularly polarized photons on a longitudinally polarized target with  $1/2$  spin
- Relate the photo-absorption cross sections to the anomalous magnetic moment
- Derived from general principles

# GDH Measurements

	$M[\text{GeV}]$	Spin	$\kappa$	$I_{\text{GDH}}[\mu\text{ b}]$
Proton	0.938	$\frac{1}{2}$	1.79	-204.8
Neutron	0.940	$\frac{1}{2}$	-1.91	-233.2
Deuteron	1.876	1	-0.14	-0.65
Helium-3	2.809	$\frac{1}{2}$	-8.38	-498.0

- Proton, verified: Mainz, Bonn, LEGS
- Neutron, in progress: Mainz, Bonn, LEGS, HIGS
- Measurements on Deuteron and  $^3\text{He}$

# Generalized GDH Integral

- Generalized for virtual photon

$$I_{GDH}(Q^2 \neq 0) = \frac{16\pi^2\alpha}{Q^2} \int_0^{x_{th}} g_1(x, Q^2) dx = \frac{16\pi^2\alpha}{Q^2} \Gamma_1 = 2\pi^2\alpha S_1(0, Q^2)$$

**Ji and Osborne, J. Phys. G27, 127 (2001)**

- Expressed as the integral of  $g_1(x, Q^2)$
- Related to the forward spin-dependent Compton amplitude  $S_1(0, Q^2)$
- $Q^2 = 0$ , GDH sum rule
- $Q^2 \rightarrow \infty$ , Bjorken sum rule



# First Moment of $g_1$

- First Moment of  $g_1$

$$\Gamma_1(Q^2) = \int_0^1 g_1(x, Q^2) dx$$

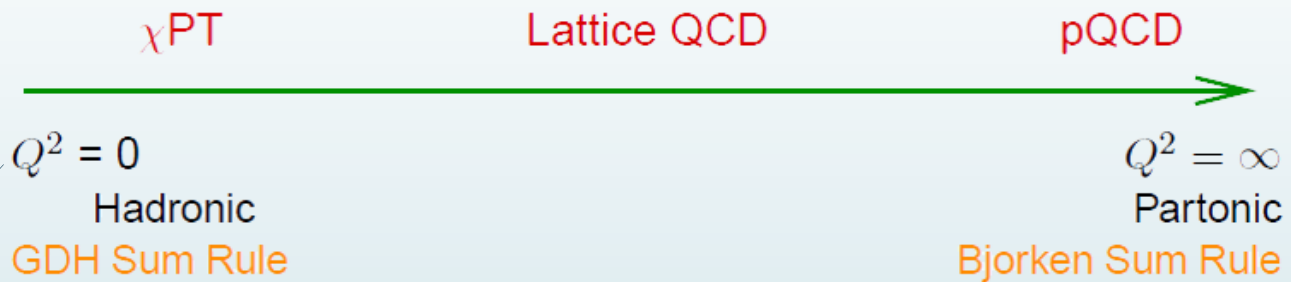
- Connects to the total spin carried by the quarks
- Relates to the GDH sum rule as  $Q^2 \rightarrow 0$

- Bjorken Sum Rule

$$\Gamma_1^P(Q^2) - \Gamma_1^N(Q^2) = \frac{g_A}{6} + O(\alpha_s(Q^2)) + O\left(\frac{1}{Q^2}\right)$$

- $g_A$ , nucleon axial charge
- Consistent with experimental result in 10%

# Importance of Generalized GDH Sum Rule



- Constrained at the two ends
- Calculable at any  $Q^2$ , can be tested by experiments over the measurable range
- Study the transition region from non-perturbative to perturbative QCD

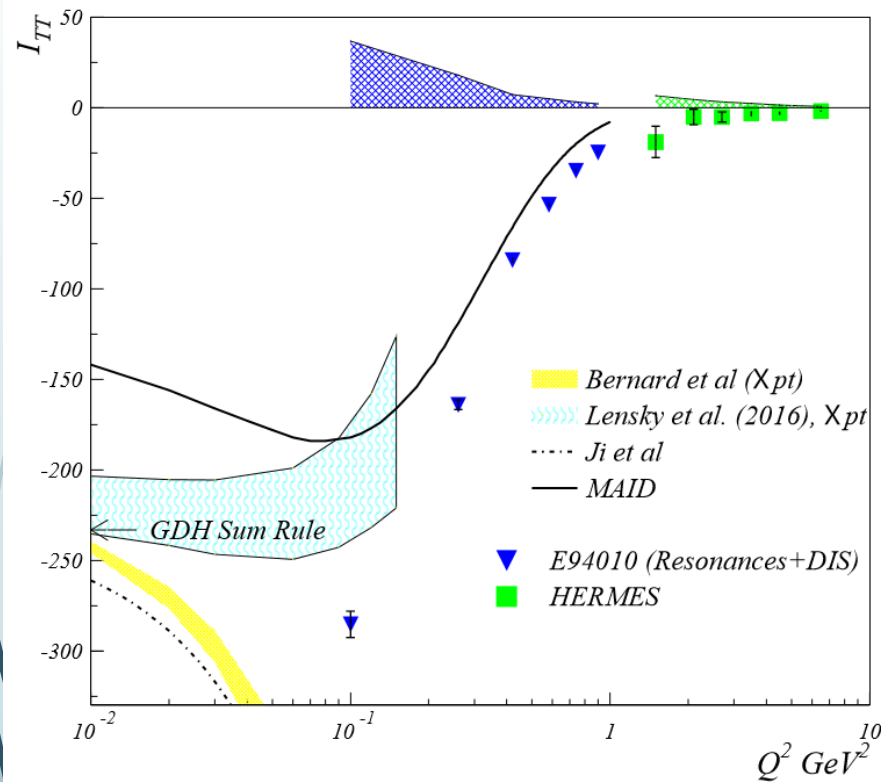
# Experimental progress

Observable	H target	D target	<sup>3</sup> He target
$g_1, g_2, \Gamma_1$ & $\Gamma_2$ at high $Q^2$	SLAC  JLAB SANE	SLAC	SLAC JLAB E97-117 JLAB E01-012 JLAB E06-014
$g_1$ & $\Gamma_1$ at high $Q^2$	SMC HERMES JLAB EG1	SMC HERMES JLAB EG1	HERMES
$\Gamma_1$ & $\Gamma_2$ at low $Q^2$	JLab RSS	JLab RSS	JLab E94-010 JLab E97-103
$\Gamma_1$ at low $Q^2$	SLAC HERMES JLAB EG1	SLAC HERMES JLAB EG1	HERMES
$\Gamma_1, Q^2 \ll 1 \text{ GeV}^2$	JLab EG4	JLab EG4	JLab E97-110
$\Gamma_2, Q^2 \ll 1 \text{ GeV}^2$	JLab E08-027		JLab E97-110

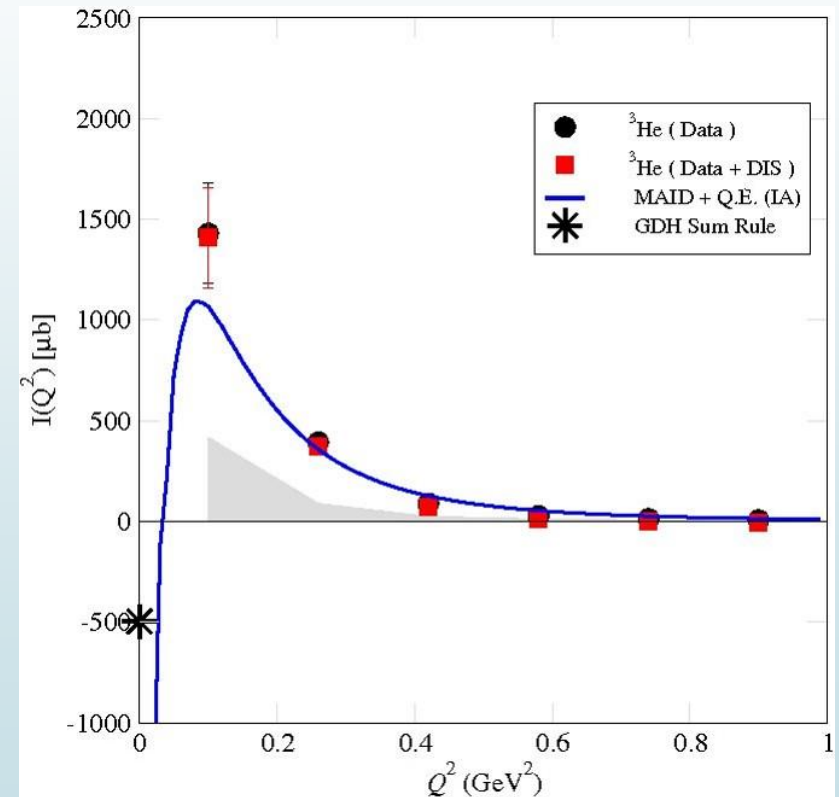
Other related JLab experiments are covered in the talks from V. Burkert, A. Deur, K. Slifer and etc.

# Neutron and $^3\text{He}$ Results

## Neutron

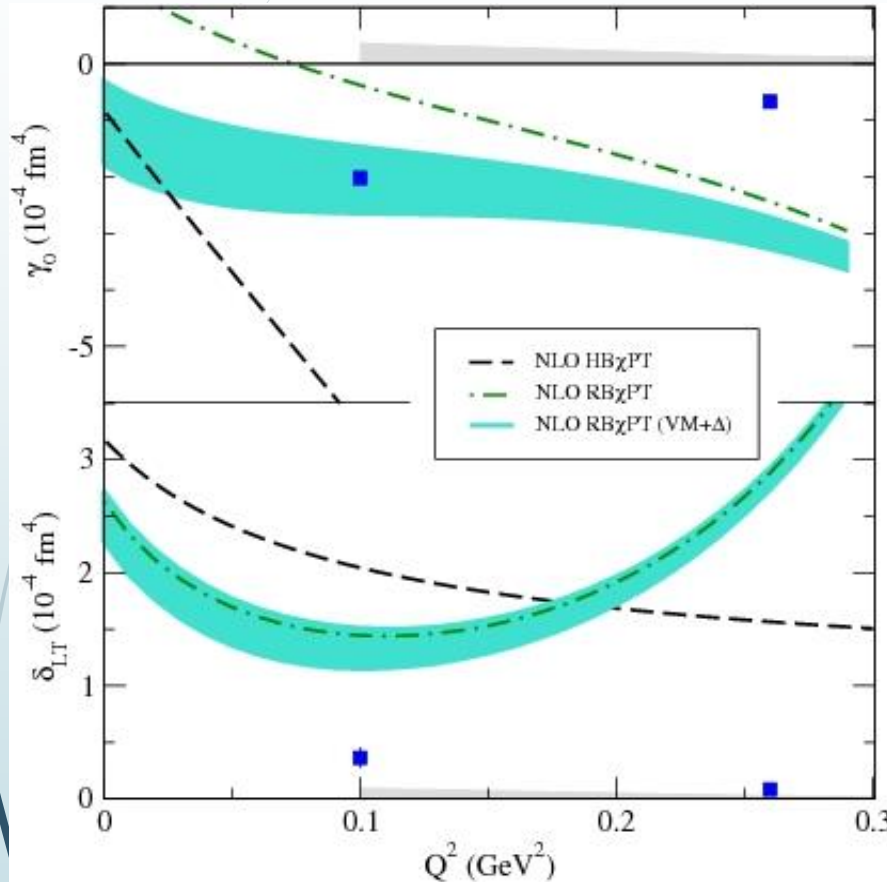


## Helium-3



MAID: phenomenological model with only resonance contributions

# Neutron Spin Polarizabilities



$$\gamma_0 = \frac{16\alpha M^2}{Q^6} \int_0^{x_0} x^2 \left[ g_1 - \frac{4M^2}{Q^2} x^2 g_2 \right]$$

$$\delta_{LT} = \frac{16\alpha M^2}{Q^6} \int_0^{x_0} x^2 [g_1 + g_2]$$

**Failure of  $\chi$ PT calculations?**

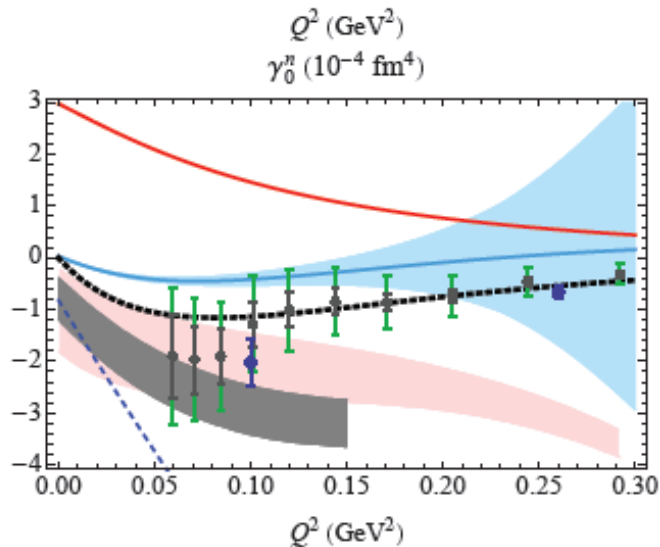
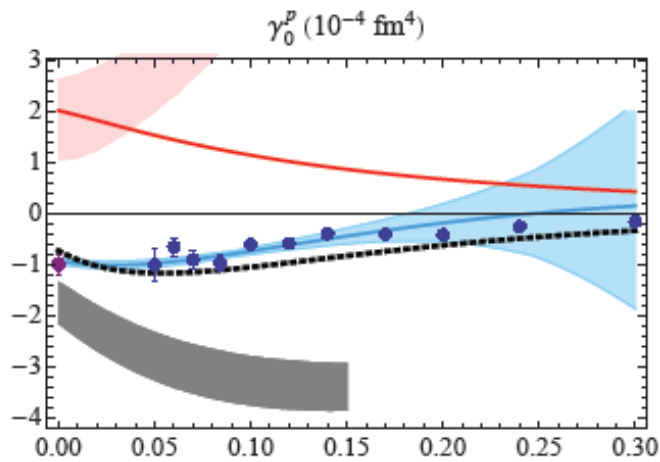
## Heavy Baryon $\chi$ PT Calculation

Kao, Spitzenberg, Vanderhaeghen  
PRD 67:016001(2003)

## Relativistic Baryon $\chi$ PT

Bernard, Hemmert, Meissner  
PRD 67:076008(2003)

# Theoretical Developments



**Curves:**

..... MAID (empir.)

- - - - LO-HBChPT

- - - - NLO-HBChPT

■ NLO-IRBChPT  
[Bernard et al (2006)]

— LO-BChPT

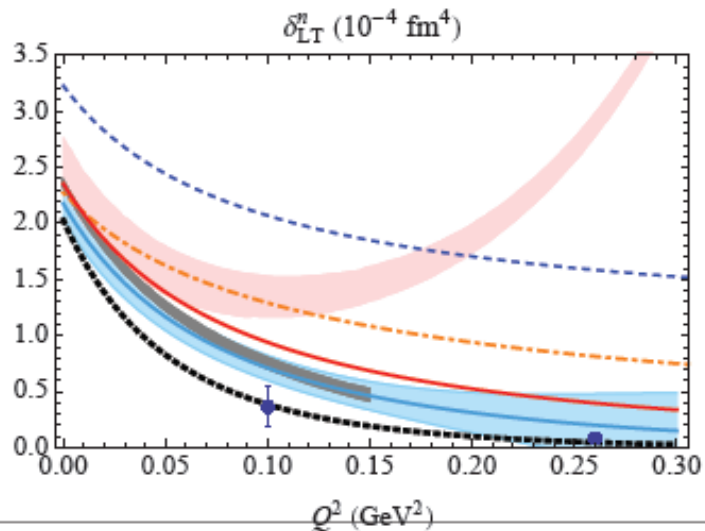
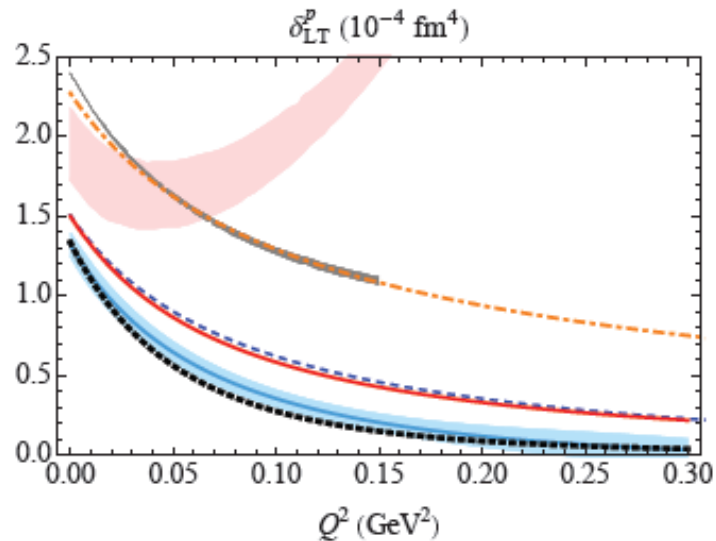
■ NLO-BChPT  
[Lensky, Alarcon & V.P.,  
PRC (2014)]

■ NLO-BChPT  
[Bernard et al (2013)]  
see talk by H. Krebs

**Data points:**

K. Slifer, J.-P. Chen, S. Kuhn, et al  
[Jefferson Lab spin program]

# Theoretical Developments



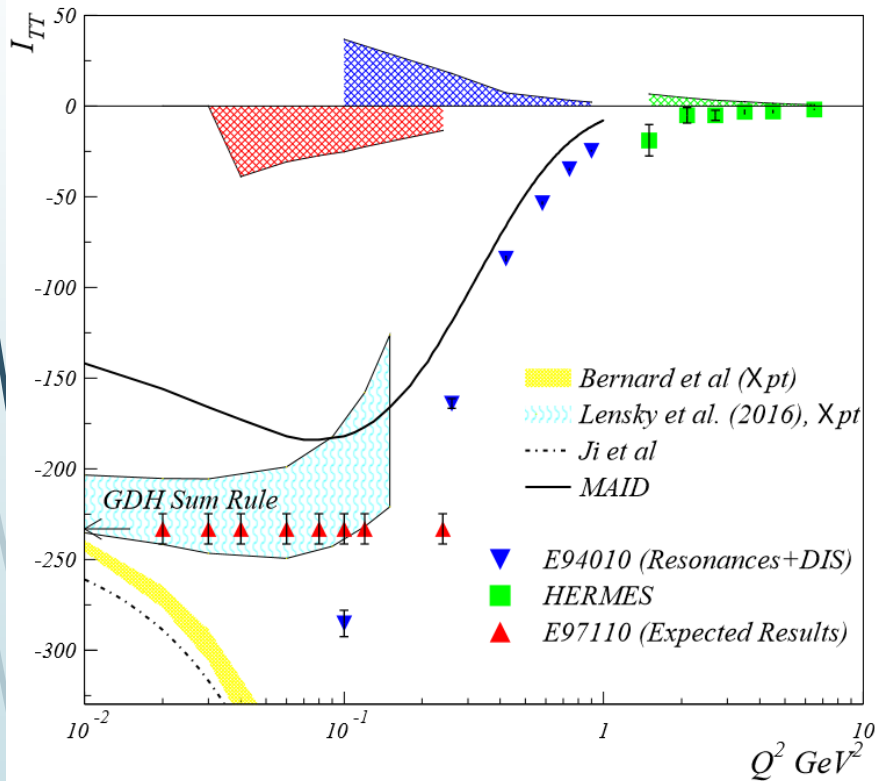
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# E97-110 at Jefferson Lab

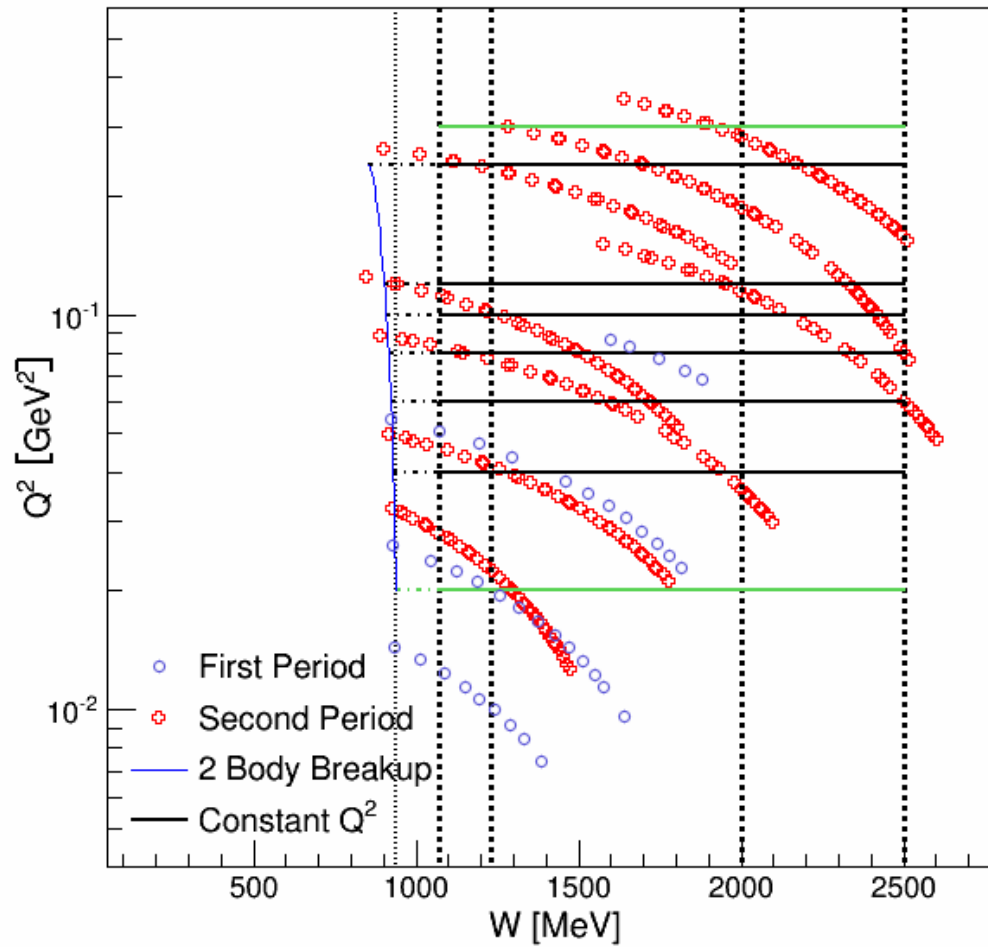


- Inclusive measurement,  $^3\text{He}(e, e')X$ 
  - Scattering angles:  $6^\circ$  and  $9^\circ$
  - Polarized electron beam,  $P_{\text{beam}} = 75\%$
  - Polarized  $^3\text{He}$  target,  $P_{\text{target}} = 40\%$
- Measured the differences of polarized cross sections
  - **Parallel** (anti-parallel)
  - **Perpendicular**

**Spokespersons: J.-P. Chen, A. Deur, F. Garibaldi**  
**Graduate students: J. Singh, V. Sulkosky, J. Yuan,**  
**C. Peng, N. Ton**

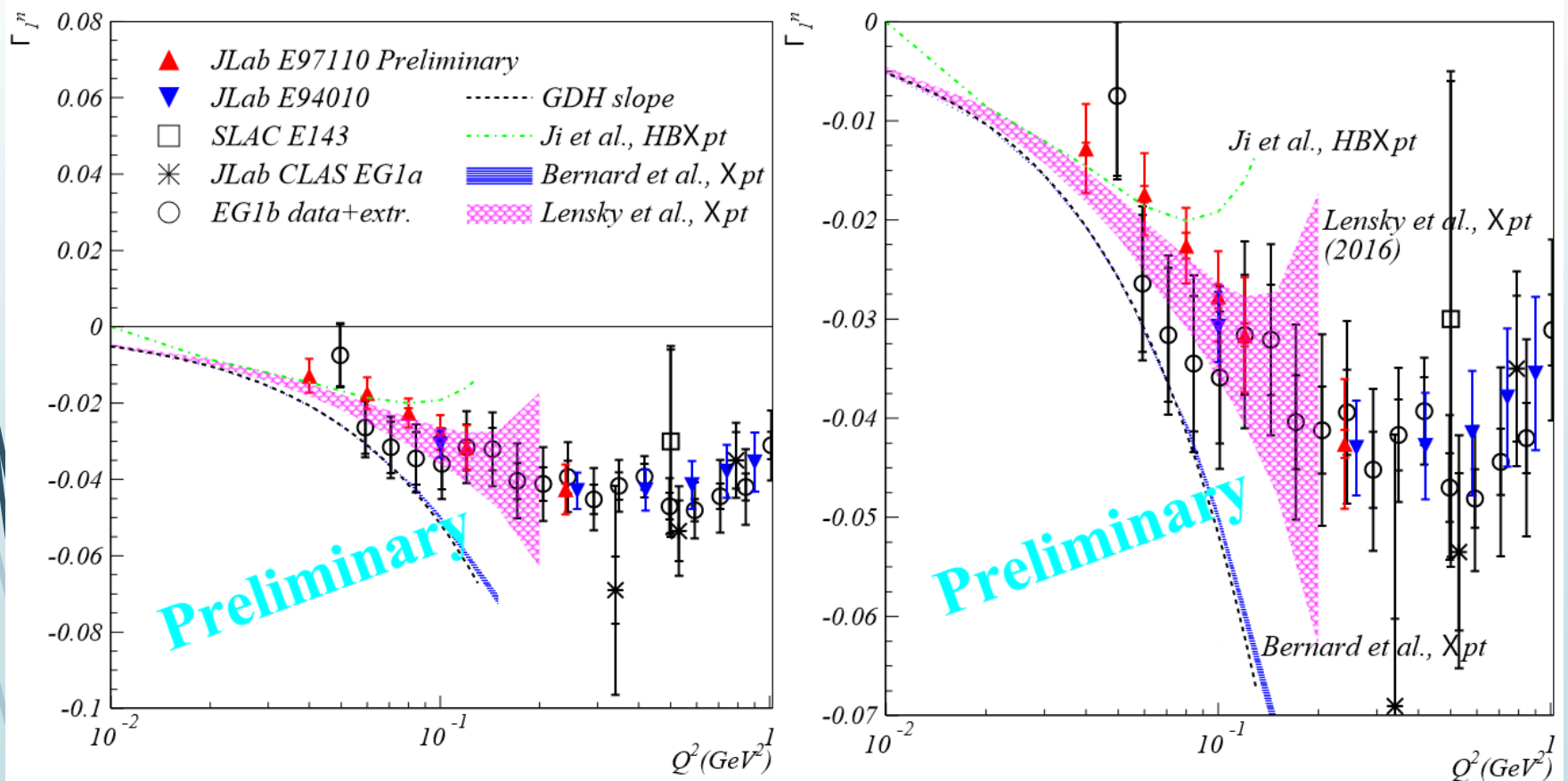


# Kinematic Coverage



# Preliminary Result

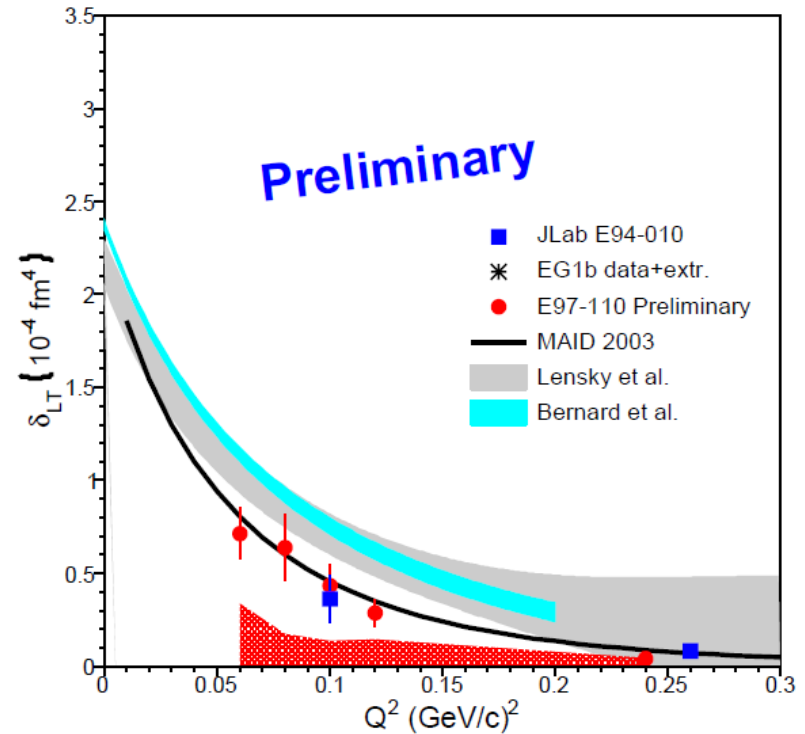
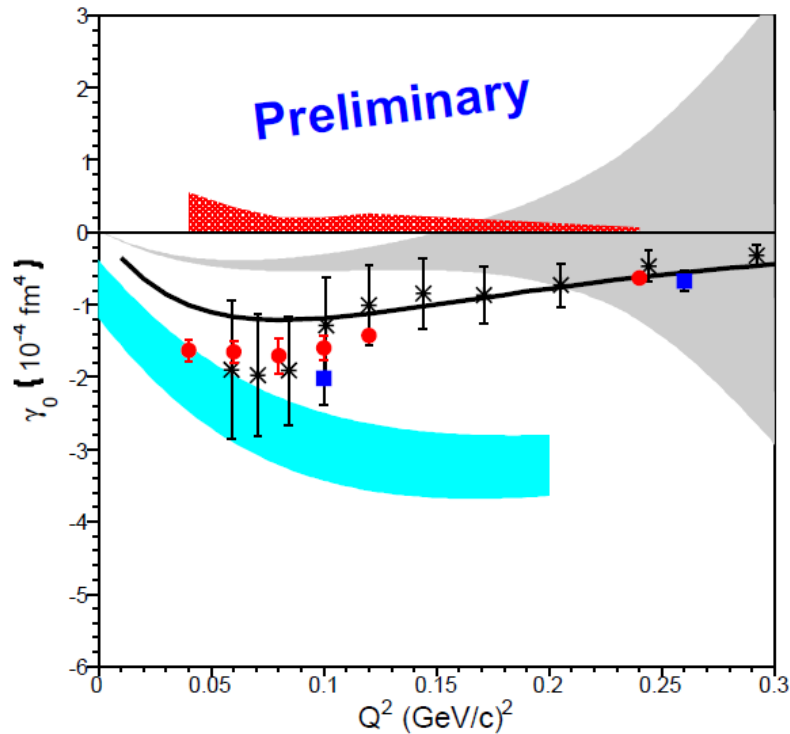
► First moment of  $g_1$



# Neutron Spin Polarizabilities

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# Summary

- ▶ Generalized GDH sum rule is useful to study the transition region
- ▶ New high precision data at low  $Q^2$ 
  - ▶ E97-110:  $g_1$  and  $g_2$  on neutron, soon to be published
- ▶ Preliminary result for neutron data from E97-110 still indicate a discrepancy with the theoretical calculations
- ▶ Acknowledgement
  - ▶ Thanks for Vincent Sulkosky providing the plots
  - ▶ The work is supported in part by US DOE grant DE-FG02-03ER41231

Thank you