

22nd International Spin Symposium

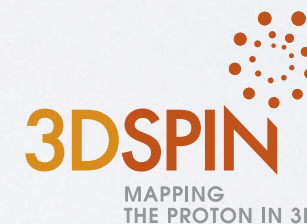
September 25-20, 2016 at UIUC



Di-hadron production in p-p collisions and the universality of transversity



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INFN - Pavia



in collaboration with

- A. Bacchetta (Univ. Pavia)
- A. Courtoy (Univ. Guanajuato - Mexico)
- A. Mukherjee (IITB - Mumbai - India)

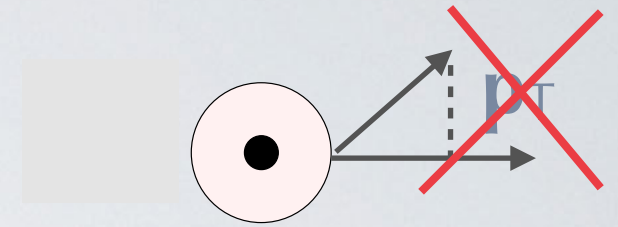
based on Master th. of
A.M. Ricci (Univ. Pavia)

leading-twist TMD map \longrightarrow PDF map

quark polarization

	U	L	T
U	\mathbf{f}_1		h_1^\perp
L		\mathbf{g}_{1L}	h_{1L}^\perp
T	f_{1T}^\perp	g_{1T}	$\mathbf{h}_1 \quad h_{1T}^\perp$

nucleon polarization



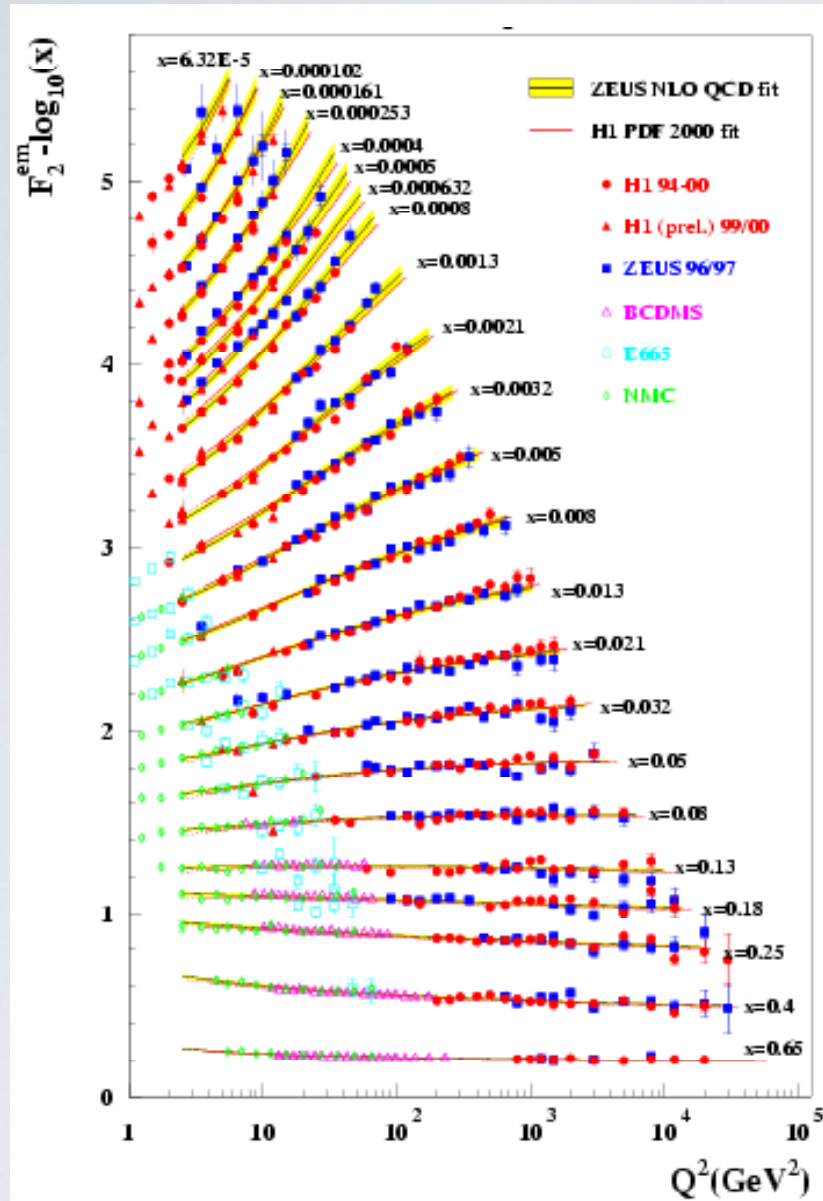
$$f_1 = \text{diagram of a circle with a black dot}$$

$$g_1 = \text{diagram of a circle with a black dot and a red arrow pointing right} - \text{diagram of a circle with a black dot and a red arrow pointing left}$$

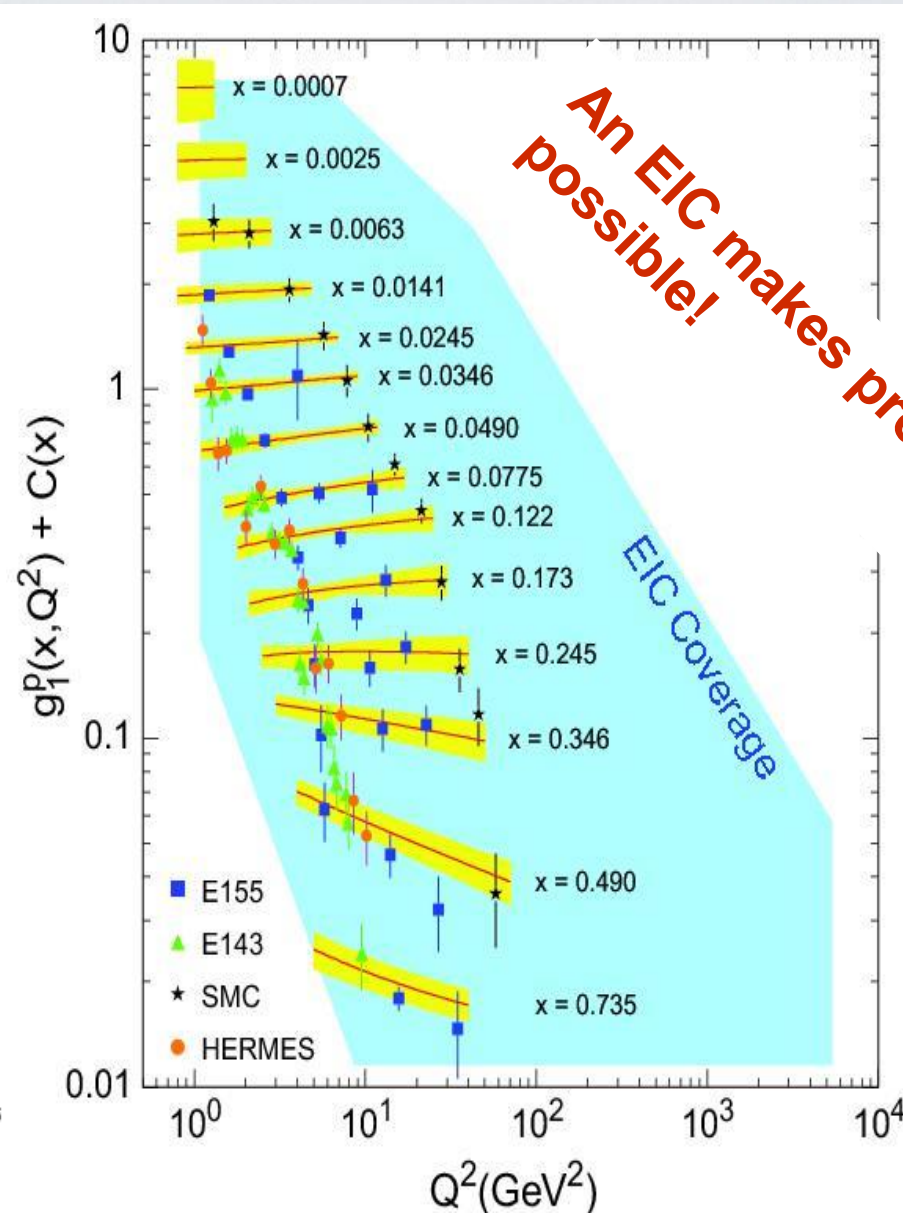
$$h_1 = \text{diagram of a circle with a black dot and a red arrow pointing up} - \text{diagram of a circle with a black dot and a red arrow pointing down}$$

\mathbf{h}_1 transversity distribution

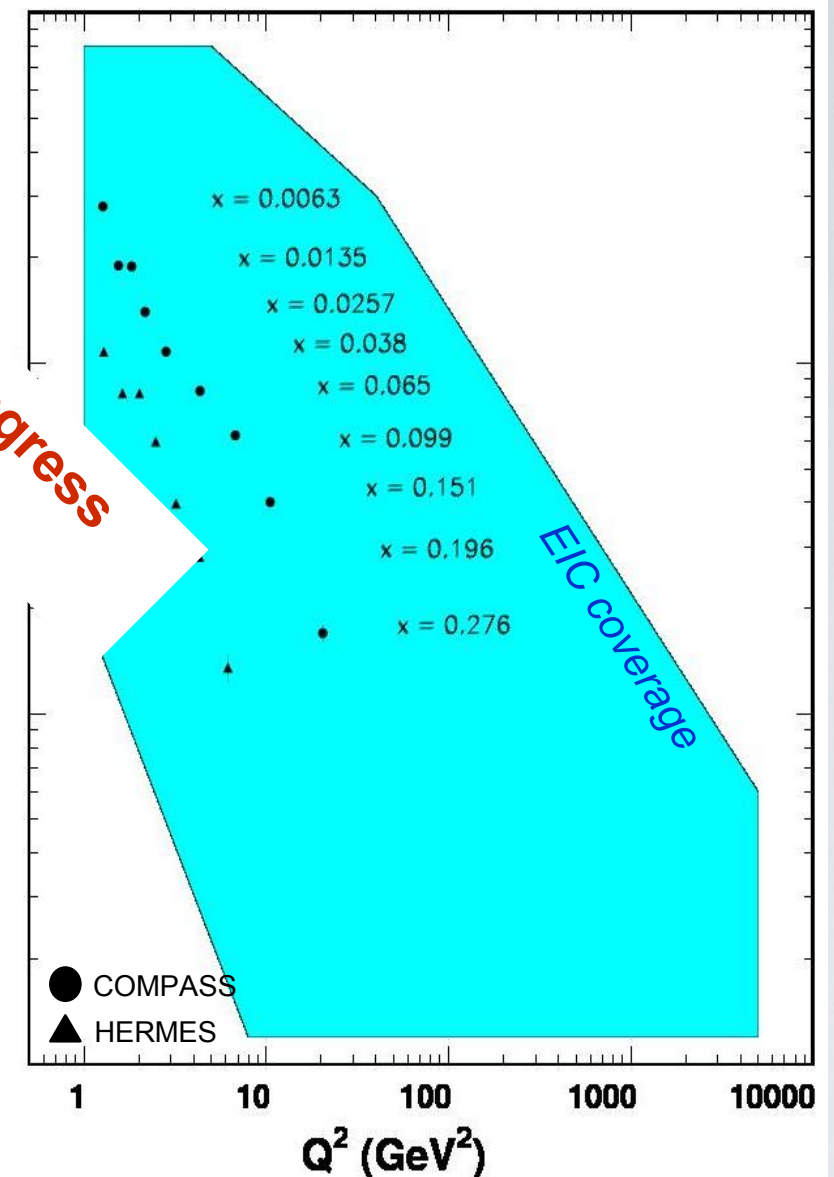
Transversity poorly known, but how much ?



World data for F_2^p
 f_1 from fits of
thousands data



World data for g_1^p
 g_1 from fits of
hundreds data



World data for **h_1**
 from fits of **tens** data

slide from H.Montgomery, QCD Evolution 2016

Tensor Charge

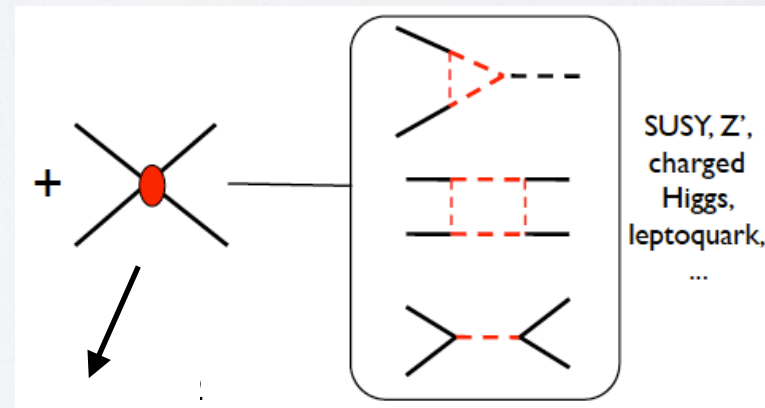
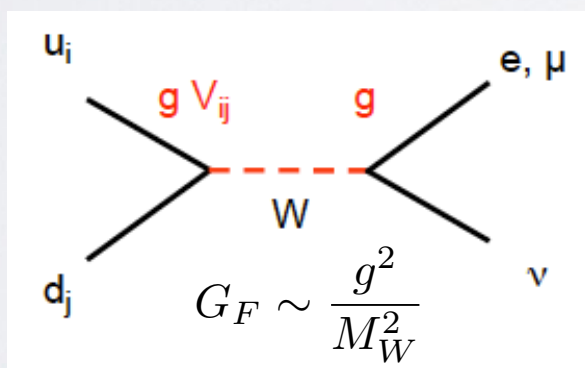
- 1st Mellin moment of transversity \Rightarrow tensor “charge”

$$\delta q \equiv g_T^q = \int_0^1 dx \left[h_1^q(x, Q^2) - h_1^{\bar{q}}(x, Q^2) \right]$$

tensor charge not directly accessible in \mathcal{L}_{SM}
low-energy footprint of new physics at higher scales ?

Example: neutron β -decay $n \rightarrow p e^- \bar{\nu}_e$

SM



BSM

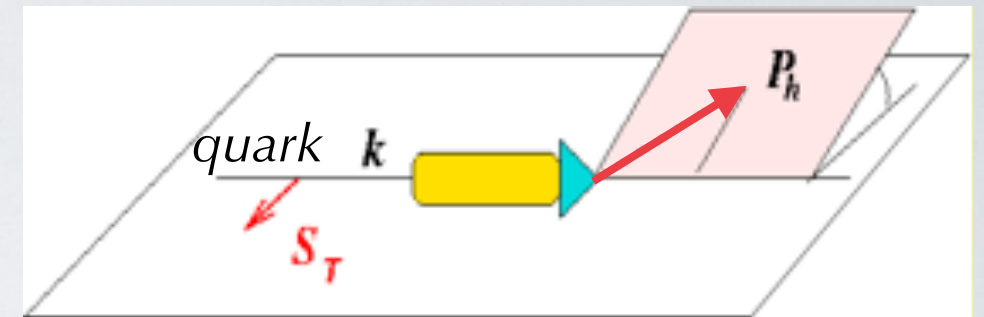
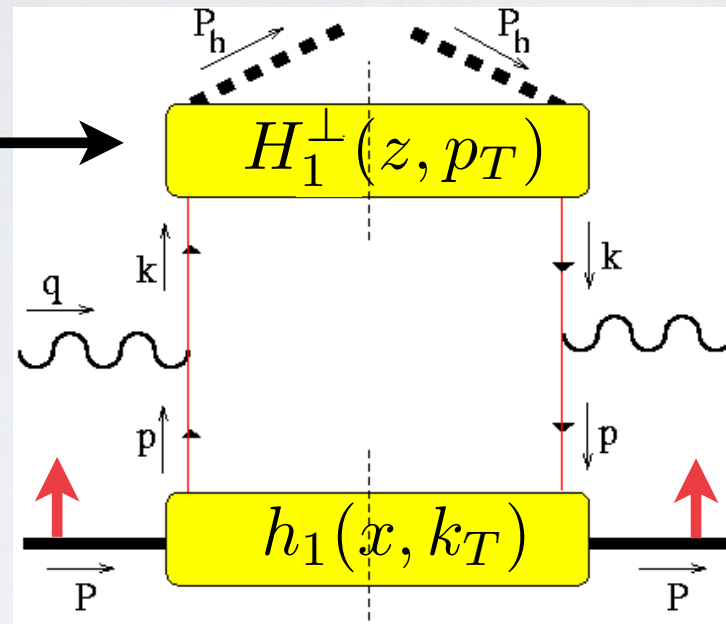
$$\epsilon_T g_T \approx M_W^2 / M_{\text{BSM}}^2$$

precision of 0.1% \Rightarrow [3-5] TeV bound for BSM scale

First extractions of transversity: the Collins effect

one-hadron SIDIS

Collins function



correlation S_T and P_{hT}
 \rightarrow azimuthal asymmetry

TMD
 factorization

h_1 "considered"
 as a TMD

$$A_{\text{SIDIS}}^{\sin(\phi_h + \phi_S)}(x, z, P_T^2) \sim \frac{\sum_q e_q^2 h_1^q(x, \mathbf{k}_\perp^2) \otimes H_{1,q}^\perp(z, \mathbf{p}_\perp^2)}{\sum_q e_q^2 f_1^q(x, \mathbf{k}_\perp^2) \otimes D_{1,q}(z, \mathbf{p}_\perp^2)}$$

..... Anselmino et al., P.R. D**87** (13) 094019
 [Anselmino et al., P.R. D**92** (15) 114023]

very
 compatible

Kang et al.,
 P.R. D**93** (16) 014009

also "quasi-transversity" on lattice (LaMET)

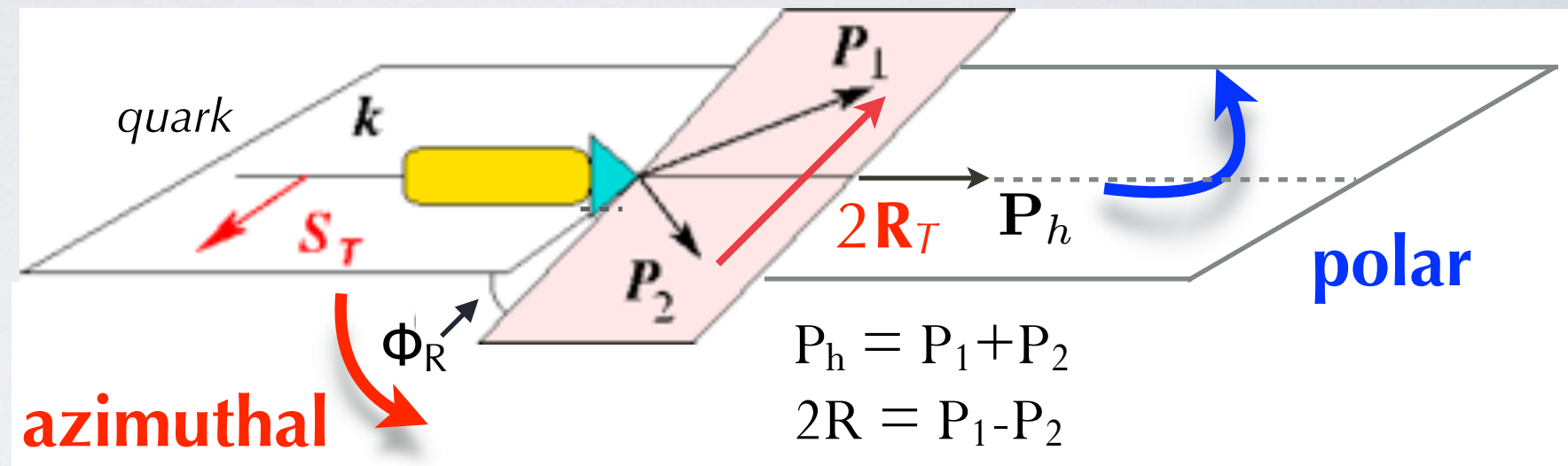
forward limit of chiral-odd GPD H_T

Chen et al., arXiv:1603.06664

Goldstein, Gonzalez and Liuti,
 P.R. D**91** (15) 114013

di-hadron fragmentation (DiFF)

Collins, Heppelman, Ladinsky, N.P. B420 (94)



correlation between quark pol. \mathbf{S}_T and $2\mathbf{R}_T$

→ azimuthal asymmetry

survives even if polar symmetry ($\int d\mathbf{P}_{hT}$)

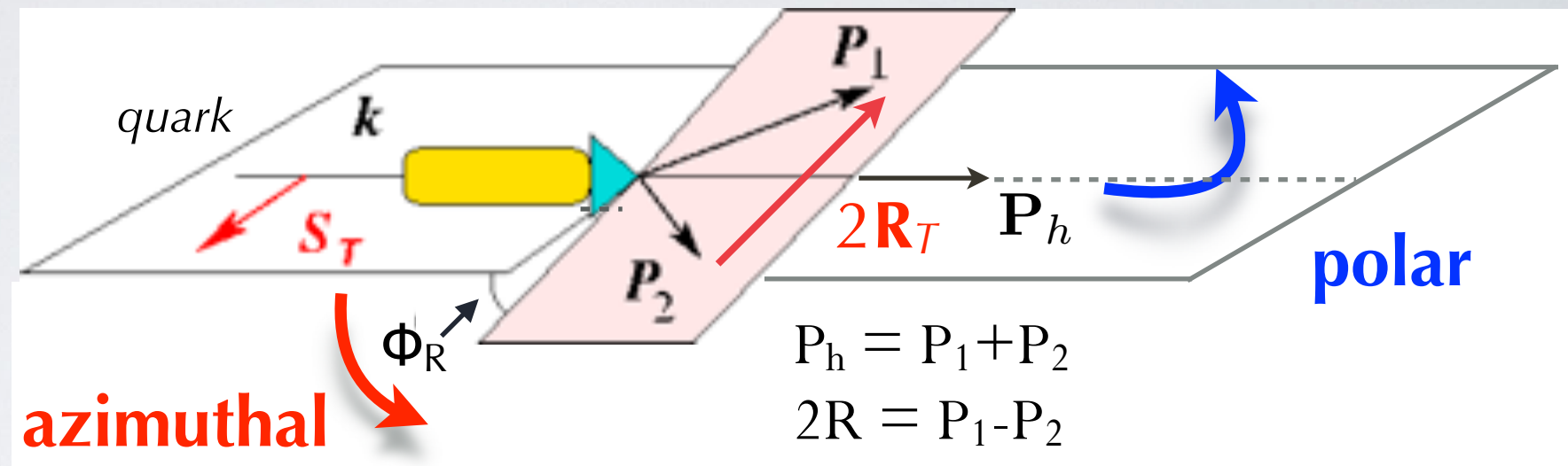
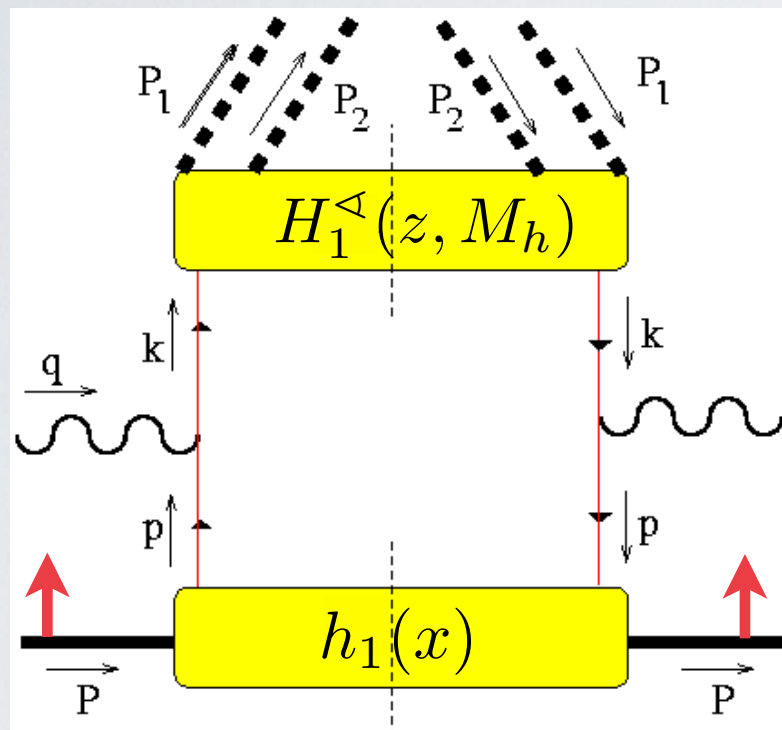
equivalent to take $\mathbf{P}_h \parallel \mathbf{k} \rightarrow \text{no } \mathbf{k}_T$

collinear factorization

di-hadron fragmentation (DiFF)

Collins, Heppelman, Ladinsky, N.P. **B420** (94)

two-hadron SIDIS



correlation between quark pol. \mathbf{S}_T and $2\mathbf{R}_T$
 \rightarrow azimuthal asymmetry
 survives even if polar symmetry ($\int d\mathbf{P}_{hT}$)
 equivalent to take $\mathbf{P}_h \parallel \mathbf{k} \rightarrow$ no \mathbf{k}_T

collinear factorization

$$A_{\text{SIDIS}}^{\sin(\phi_R + \phi_S)}(x, z, M_h^2) \sim - \frac{\sum_q e_q^2 h_1^q(x) \frac{|\mathbf{R}_T|}{M_h} H_{1,q}^<(z, M_h^2)}{\sum_q e_q^2 f_1^q(x) D_{1,q}(z, M_h^2)}$$

x-dep. of SSA given by PDFs only

chiral-odd DiFF

$$z = z_1 + z_2$$

price to pay: dependence
on $(\pi\pi)$ invariant mass M_h

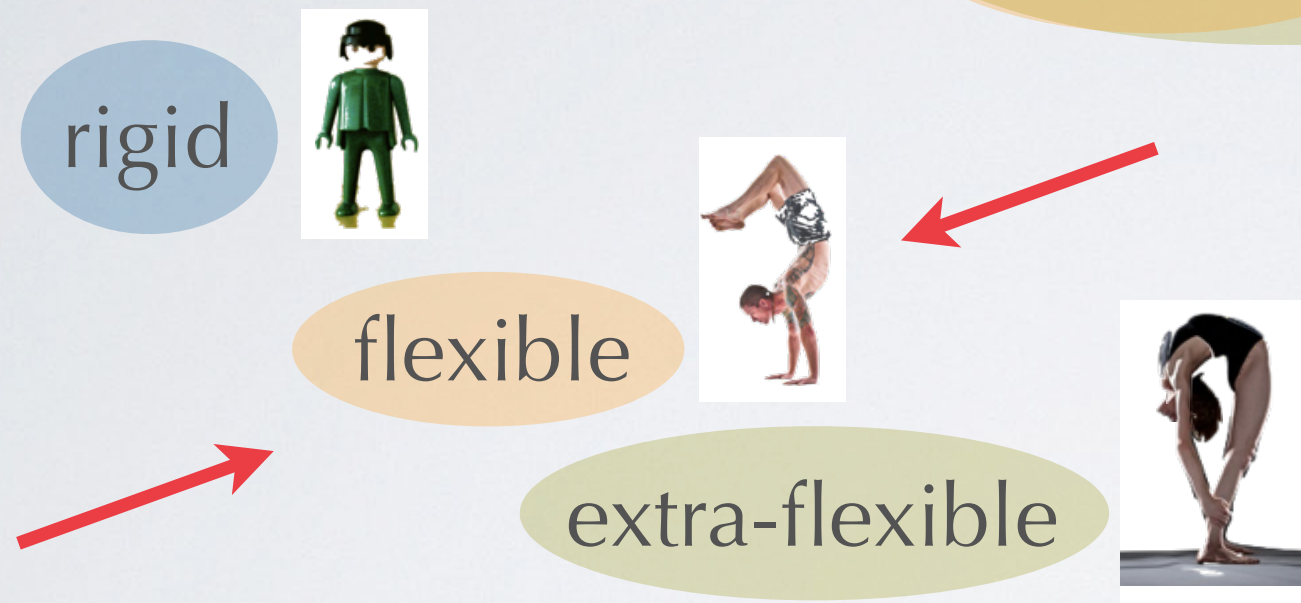
the Pavia fit

- parametrization at $Q_0^2 = 1 \text{ GeV}^2$

$$xh_1^{qv}(x) = \tanh \left[\sqrt{x} \left(A_q + B_q x + C_q x^2 + D_q x^3 \right) \right] \left[x \text{SB}_q(x) + x \overline{\text{SB}}_{\bar{q}}(x) \right]$$

satisfies **Soffer Bound** at any Q^2

$$2|h_1^q(x, Q^2)| \leq 2 \text{SB}_q(x) = |f_1^q(x) + g_1^q(x)|$$



- SIDIS data from  and 

*Airapetian et al.,
JHEP **0806** (08) 017*

*Adolph et al.,
P.L. **B713** (12)*

*Braun et al.,
E.P.J. Web Conf. **85** (15) 02018*

history of upgrading fits

*Bacchetta, Courtoy, Radici,
P.R.L. **107** (11) 012001*

*Bacchetta, Courtoy, Radici,
JHEP **1303** (13) 119*

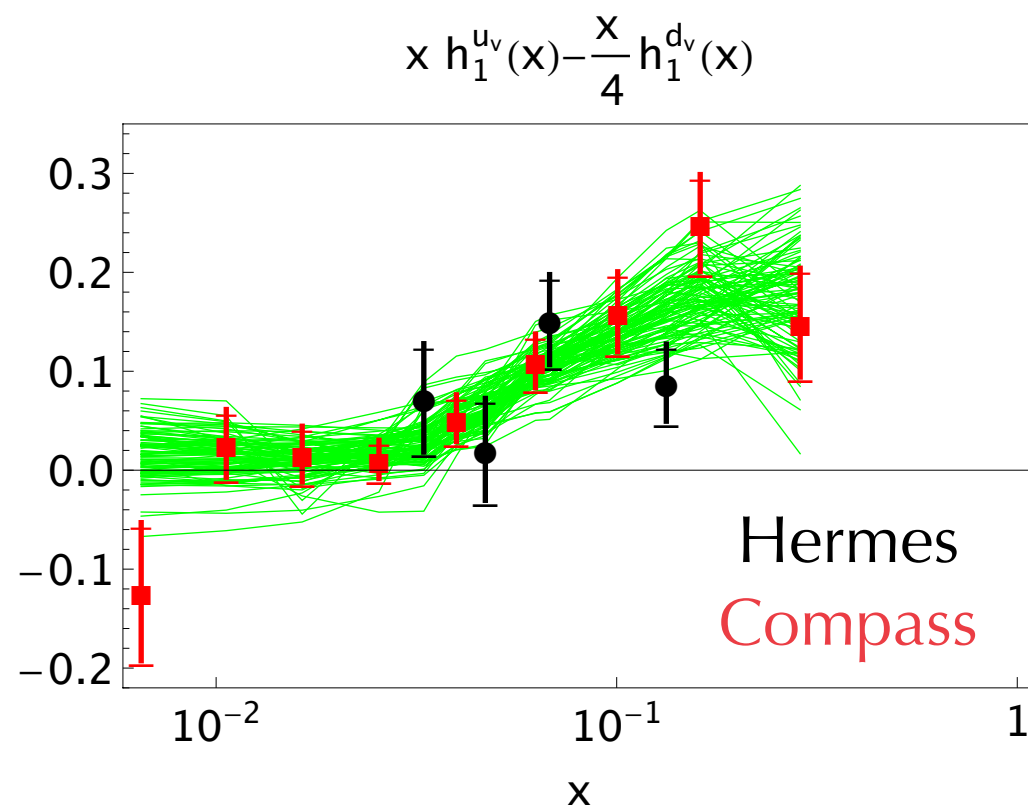
*Radici et al.,
JHEP **1505** (15) 123*

error analysis : the replica method

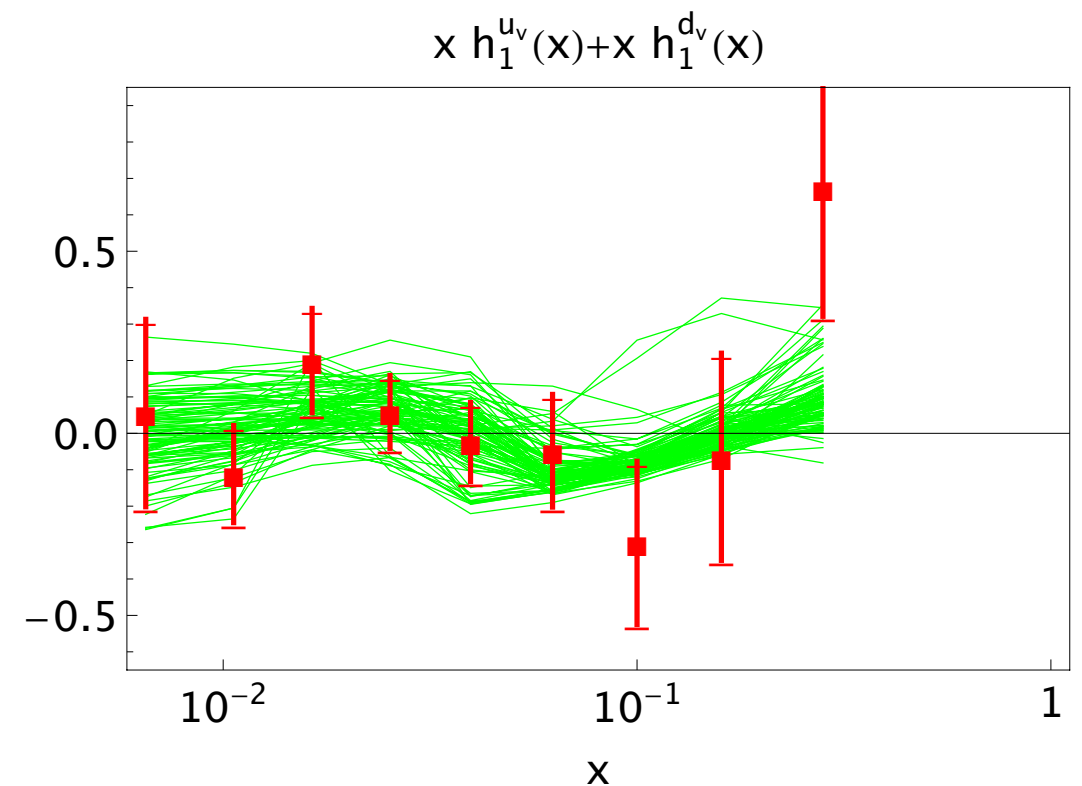
alter data with random noise and fit them

100 replicas

proton

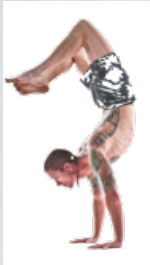


deuteron



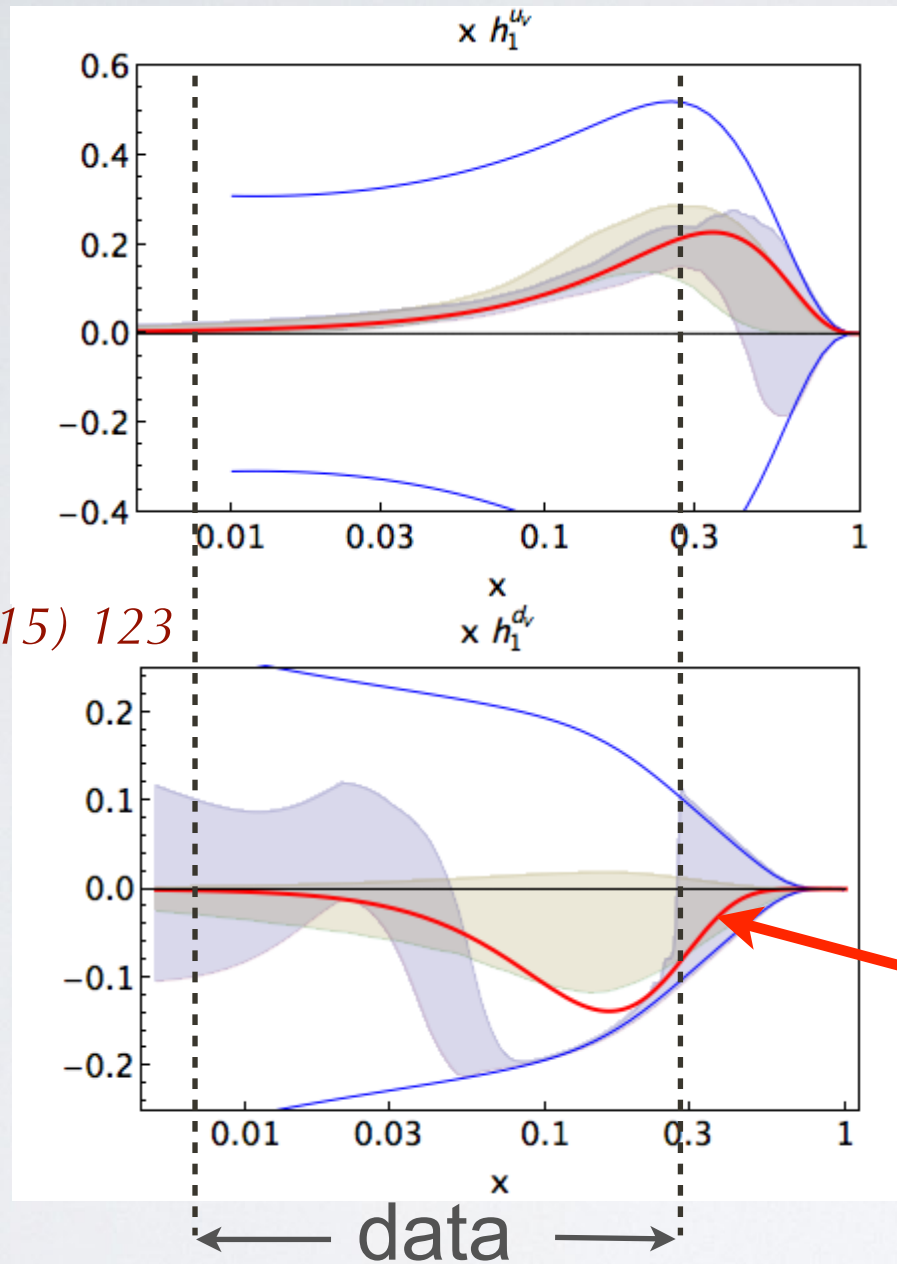
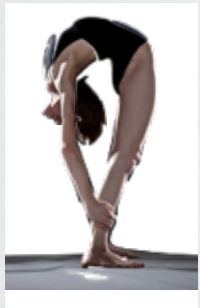
comparison with Collins effect

up

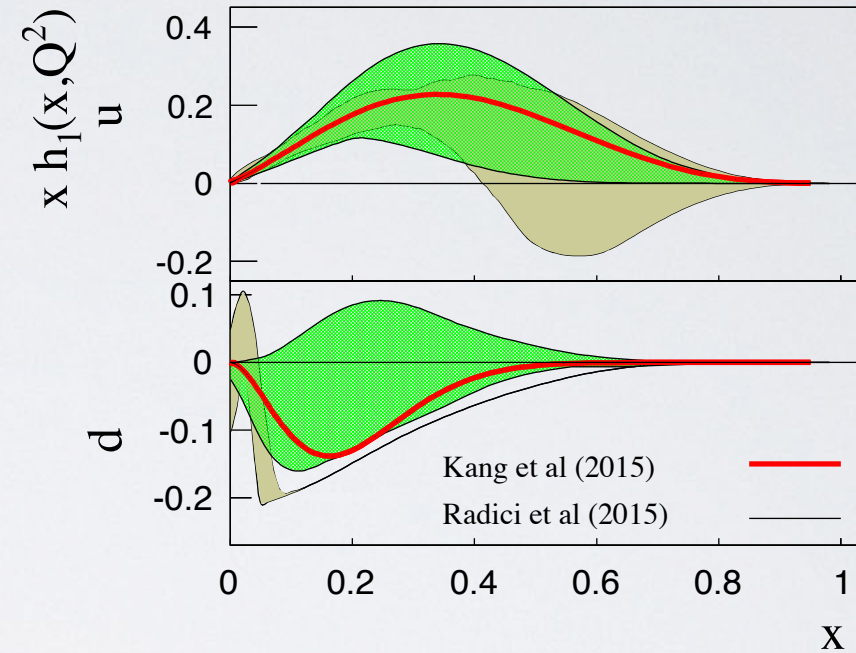


*Radici et al.,
JHEP 1505 (15) 123*

down

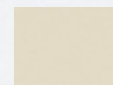


Kang et al. 2016 \leftrightarrow Pavia 2015



$Q^2 = 2.4 \text{ GeV}^2$

linear
scale

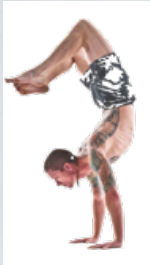


Anselmino et al., 2013

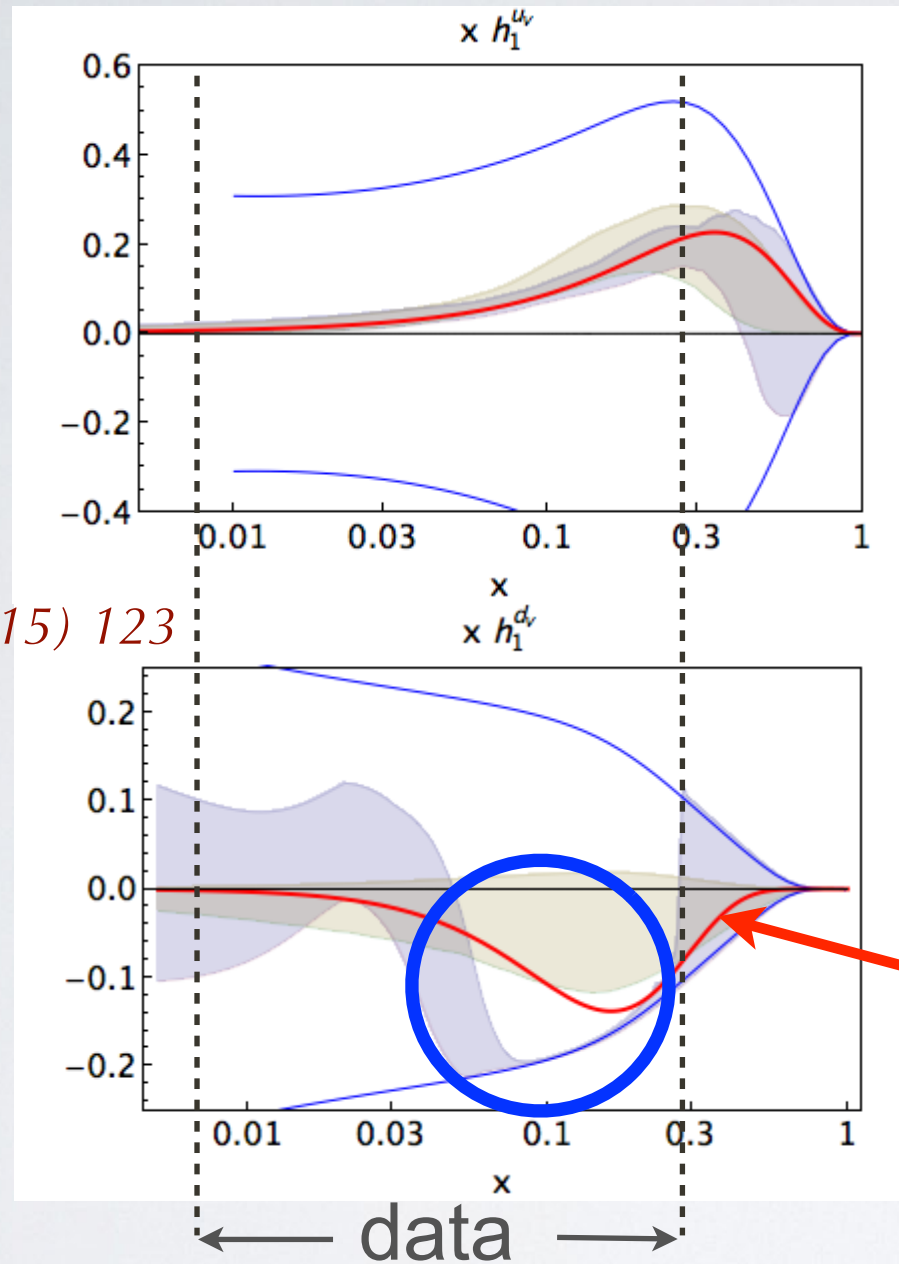
Kang et al., 2015

comparison with Collins effect

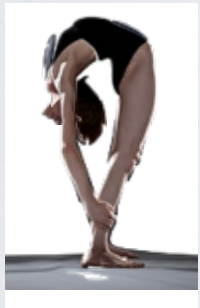
up



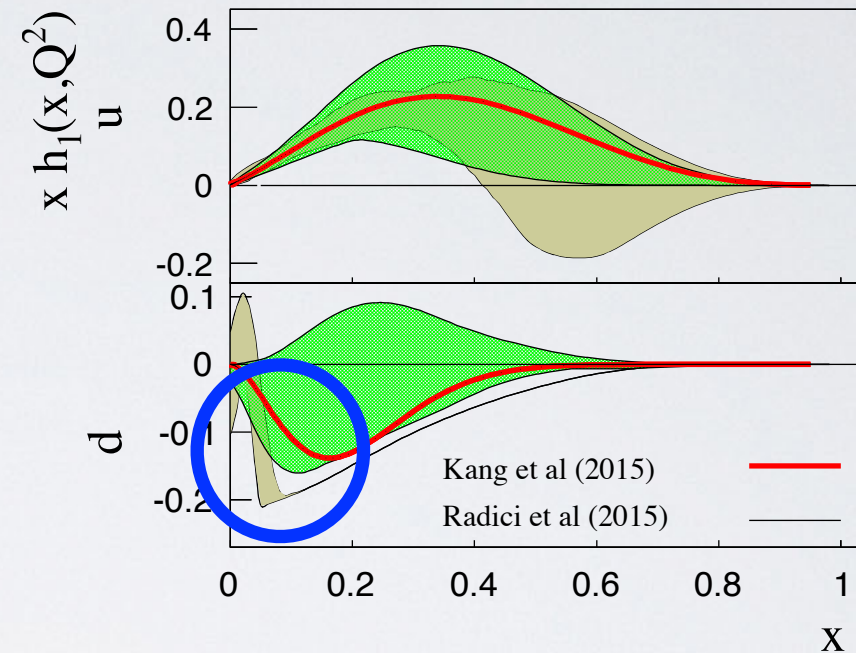
*Radici et al.,
JHEP 1505 (15) 123*



down



Kang et al. 2015 \leftrightarrow Pavia 2015



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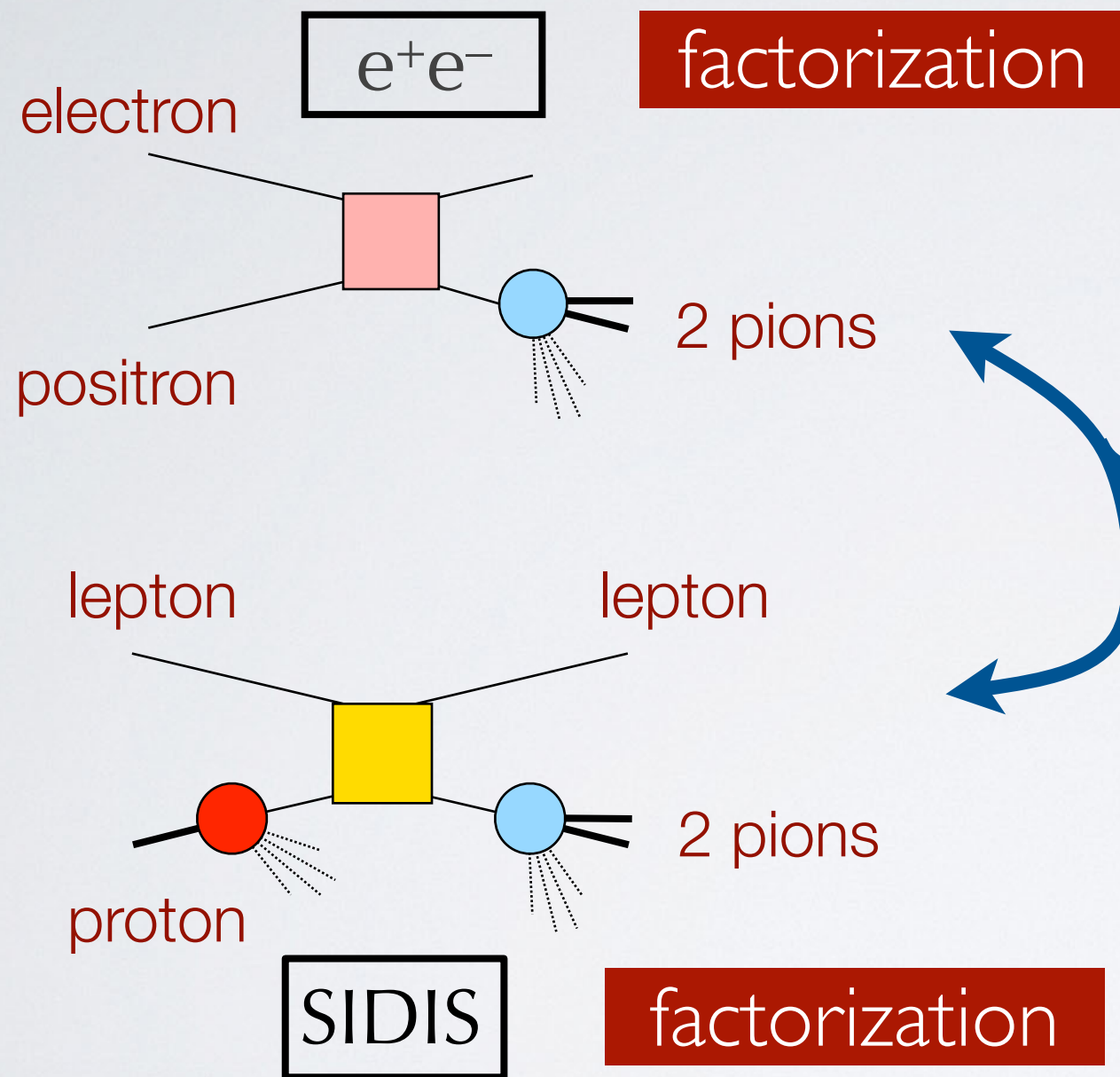
Anselmino et al., 2013

Kang et al., 2015

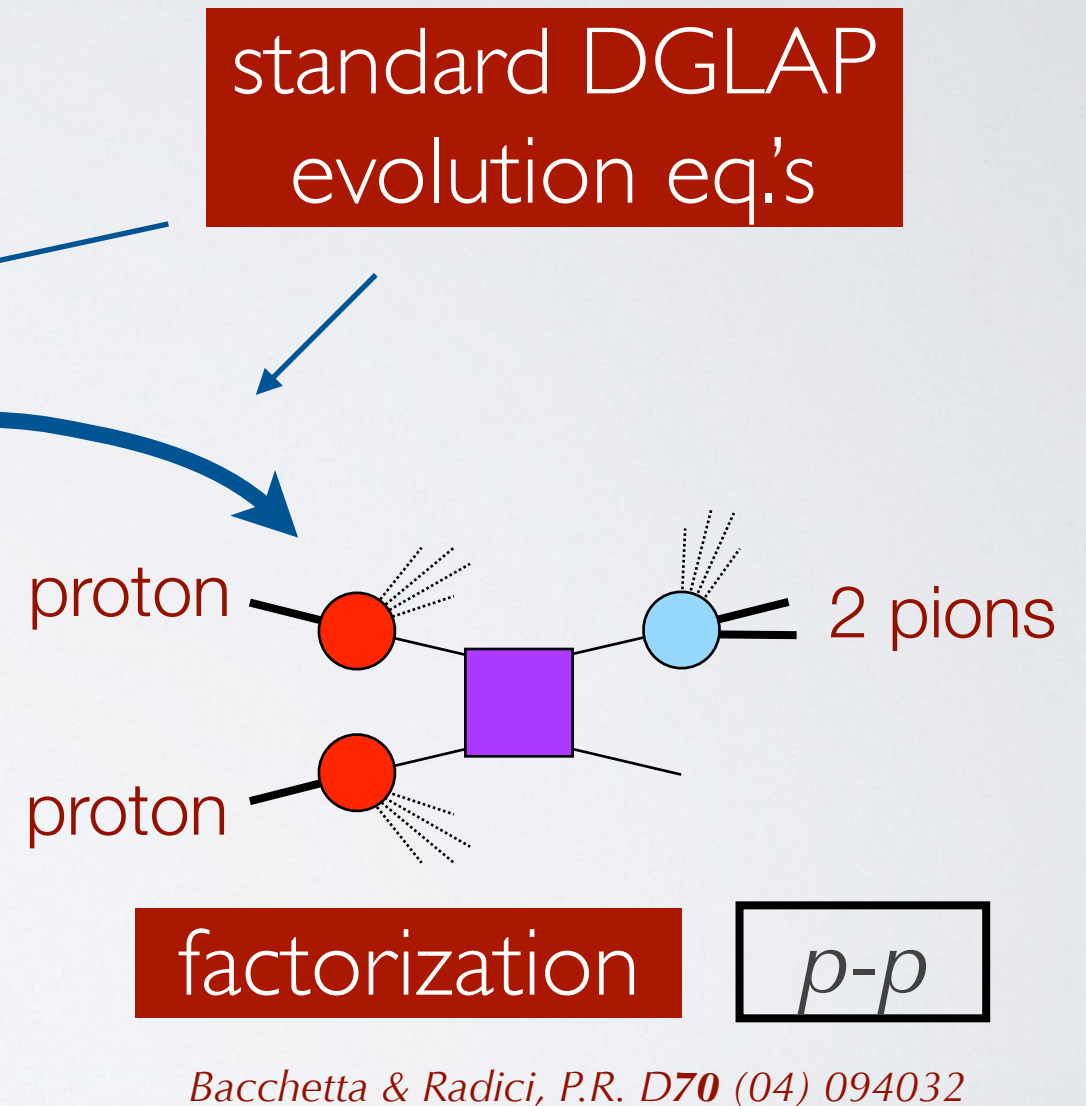
unusual saturation of
Soffer bound for down

collinear factorization in hard processes

Artru & Collins, *Z.Phys.* **C69** (96) 277
Boer, Jakob, Radici, *P.R.D***67** (03) 094003



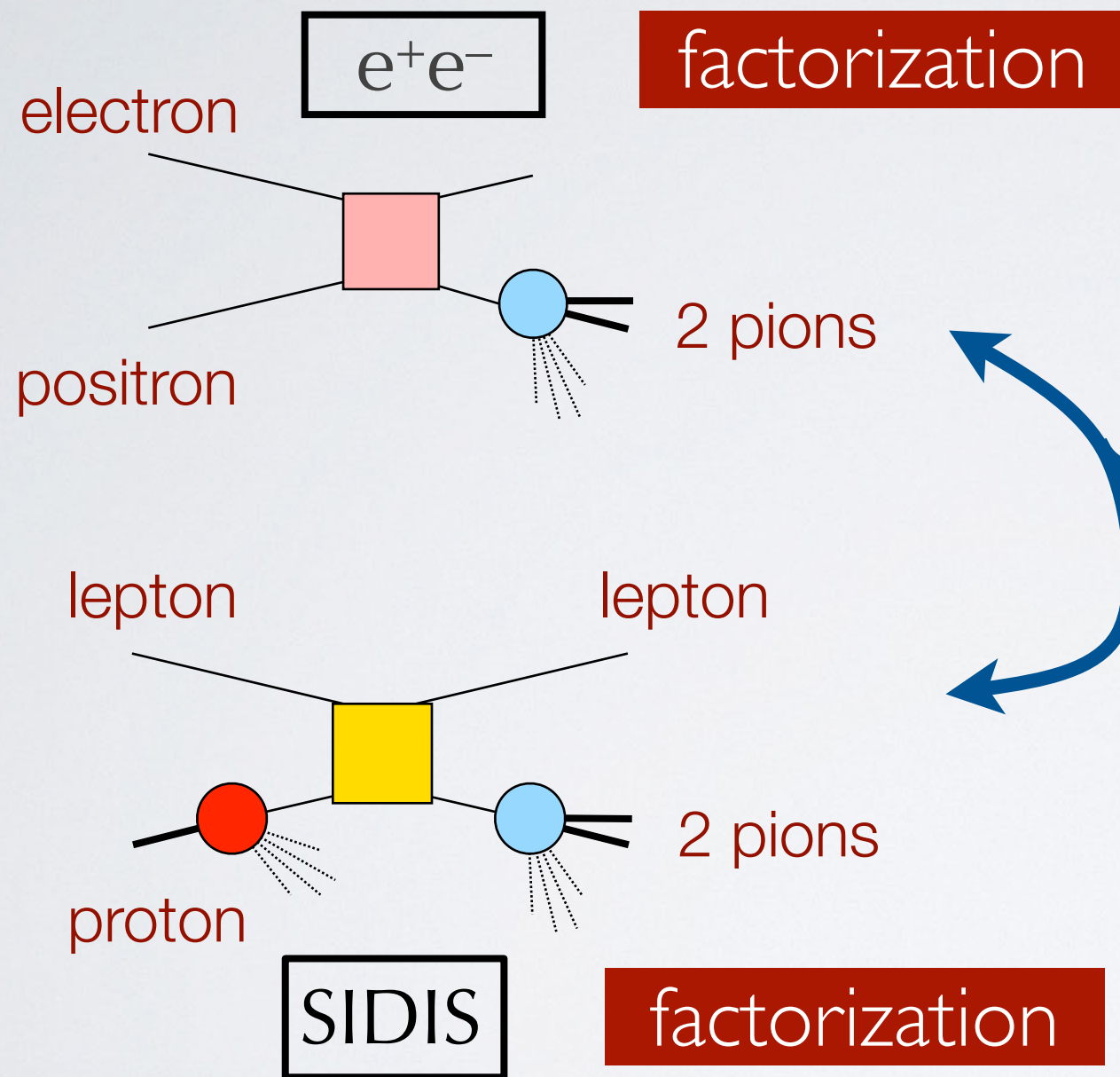
DeFlorian & Vanni, *P.L.***B578** (04) 139
Ceccopieri, Radici, Bacchetta, *P.L.***B650** (07) 81
(see also
Zhou and Metz, *P.R.L.* **106** (11) 172001
for M_h —evolution of DiFFs)



Jaffe, Jin, Tang, *P.R.L.***80** (98) 1166
Radici, Jakob, Bianconi, *P.R.D***65** (02) 074031
Bacchetta & Radici, *P.R. D***67** (03) 094002

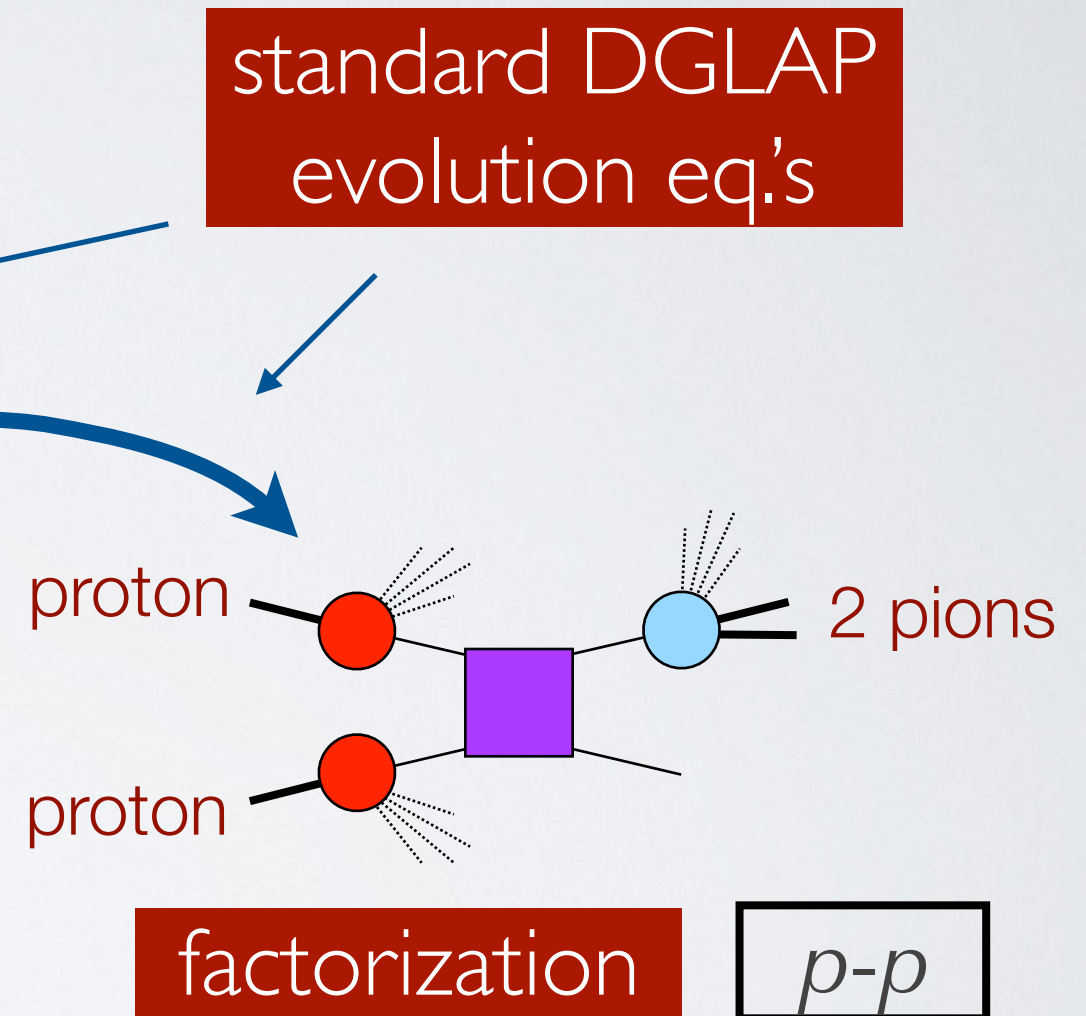
collinear factorization in hard processes

Artru & Collins, *Z.Phys.* **C69** (96) 277
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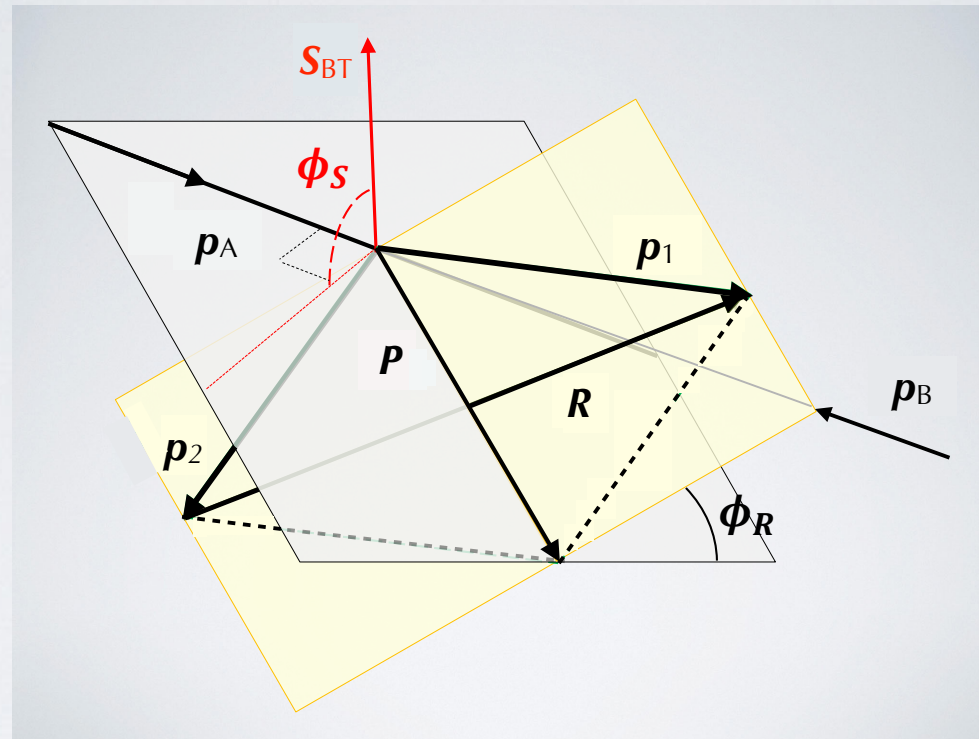
Bacchetta & Radici, *P.R. D***70** (04) 094032

Rogers & Mulders,
*P.R. D***81** (10) 094006

not possible in
 $p+p \rightarrow \pi+\pi+X$

the process $p + p^\uparrow \rightarrow (\pi \pi) + X$

Bacchetta & Radici,
P.R. D70 (04) 094032



B beam polarized

forward
polarized particles
at $\eta < 0$

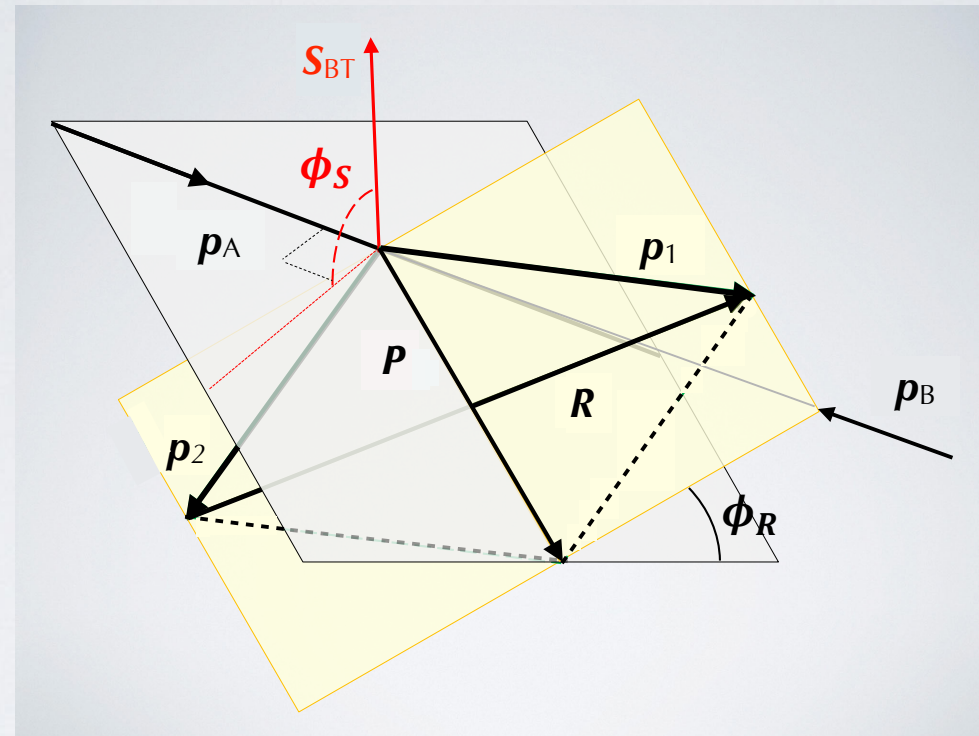
$$d\sigma \sim d\sigma^0 + \sin(\phi_S - \phi_R) d\sigma_{UT}$$

$$\frac{d\sigma^0}{d\eta d|\mathbf{P}_T| dM} = 2 |\mathbf{P}_T| \sum_{a,b,c,d} \int \frac{dx_a dx_b}{8\pi^2 \bar{z}} f_1^a(x_a) f_1^b(x_b) \frac{d\hat{\sigma}_{ab \rightarrow cd}}{d\hat{t}} D_1^c(\bar{z}, M)$$

$$\hat{t} = t x_a / \bar{z}$$

the process $p + p^\uparrow \rightarrow (\pi \pi) + X$

Bacchetta & Radici,
P.R. D70 (04) 094032



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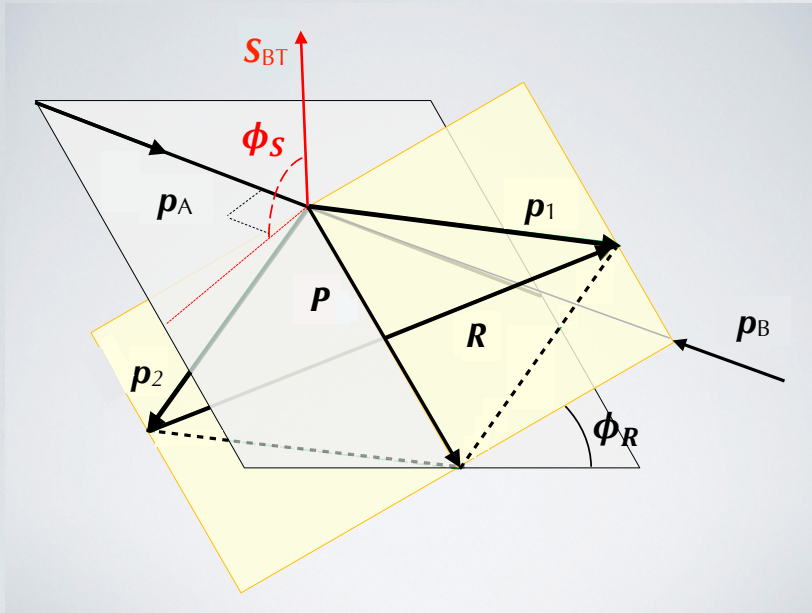
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$$\hat{t} = t x_a / \bar{z}$$

$$\frac{d\sigma_{UT}}{d\eta d|\mathbf{P}_T| dM} = |\mathbf{S}_{BT}| 2 |\mathbf{P}_T| \frac{|\mathbf{R}|}{M} \sin \theta \sum_{a,b,c,d} \int \frac{dx_a dx_b}{8\pi^2 \bar{z}} f_1^a(x_a) h_1^b(x_b) \frac{d\Delta \hat{\sigma}_{ab \uparrow \rightarrow c \uparrow d}}{d\hat{t}} H_1^{\triangleleft c}(\bar{z}, M)$$

Our prediction: asymmetry given by same mechanism active in SIDIS

the process $p + p^\uparrow \rightarrow (\pi \pi) + X$



Bacchetta & Radici, P.R. D70 (04) 094032

$$d\sigma \sim d\sigma^0 + \sin(\phi_S - \phi_R) d\sigma_{UT}$$

B beam polarized



forward
polarized particles
at $\eta < 0$

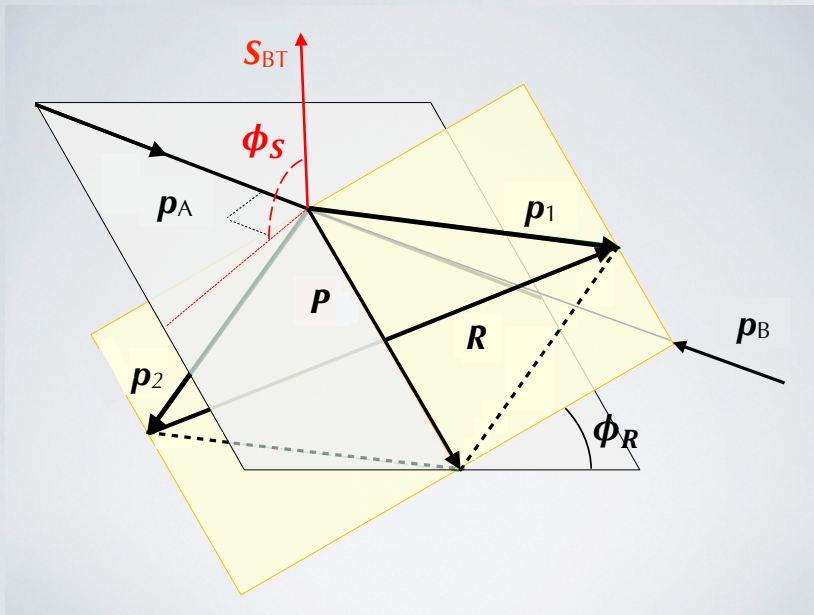
$$\frac{d\sigma^0}{d\eta d|\mathbf{P}_T| dM} = 2 |\mathbf{P}_T| \sum_{a,b,c,d} \int \frac{dx_a dx_b}{8\pi^2 \bar{z}} f_1^a(x_a) f_1^b(x_b) \frac{d\hat{\sigma}_{ab \rightarrow cd}}{d\hat{t}} D_1^c(\bar{z}, M) \quad \hat{t} = t x_a / \bar{z}$$

$$\frac{d\sigma_{UT}}{d\eta d|\mathbf{P}_T| dM} = |S_{BT}| 2 |\mathbf{P}_T| \frac{|\mathbf{R}|}{M} \sin \theta \sum_{a,b,c,d} \int \frac{dx_a dx_b}{8\pi^2 \bar{z}} f_1^a(x_a) h_1^b(x_b) \frac{d\Delta\hat{\sigma}_{ab^\uparrow \rightarrow c^\uparrow d}}{d\hat{t}} H_1^{\leq c}(\bar{z}, M)$$

$$\frac{|\mathbf{R}|}{M} = \frac{1}{2} \sqrt{1 - 4 \frac{m_\pi^2}{M^2}}$$

$M =$ invariant mass of $(\pi \pi)$

the process $p + p^\uparrow \rightarrow (\pi \pi) + X$



Bacchetta & Radici, P.R. D70 (04) 094032

$$d\sigma \sim d\sigma^0 + \sin(\Phi_S - \Phi_R) d\sigma_{UT}$$

B beam polarized



forward
polarized particles
at $\eta < 0$

$$\frac{d\sigma^0}{d\eta d|\mathbf{P}_T| dM} = 2 |\mathbf{P}_T| \sum_{a,b,c,d} \int \frac{dx_a dx_b}{8\pi^2 \bar{z}} f_1^a(x_a) f_1^b(x_b) \frac{d\hat{\sigma}_{ab \rightarrow cd}}{d\hat{t}} D((\bar{z}, M)) \quad \hat{t} = t x_a / \bar{z}$$

$$\frac{d\sigma_{UT}}{d\eta d|\mathbf{P}_T| dM} = |\mathbf{S}_{BT}| 2 |\mathbf{P}_T| \frac{|\mathbf{R}|}{M} \sin \theta \sum_{a,b,c,d} \int \frac{dx_a dx_b}{8\pi^2 \bar{z}} f_1^a(x_a) h_1^b(x_b) \frac{d\Delta\hat{\sigma}_{ab^\uparrow \rightarrow c^\uparrow d}}{d\hat{t}} H_1^<((\bar{z}, M))$$

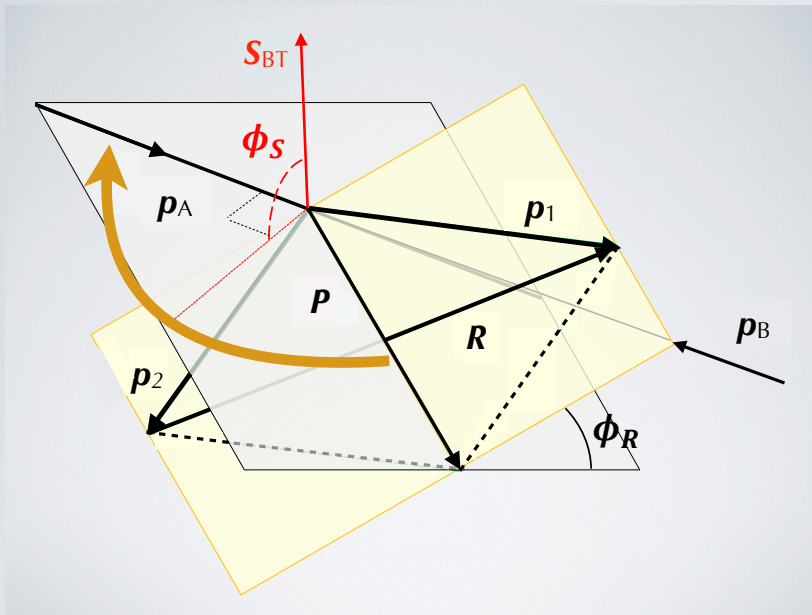
conservation of momenta in $ab \rightarrow cd$

\Rightarrow $(\pi\pi)$ fract. energy fixed to

η = pseudorapidity

$$\bar{z} = \frac{|\mathbf{P}_T|}{\sqrt{s}} \frac{x_a e^{-\eta} + x_b e^{\eta}}{x_a x_b}$$

the process $p + p^\uparrow \rightarrow (\pi \pi) + X$



Bacchetta & Radici, P.R. D70 (04) 094032

$$d\sigma \sim d\sigma^0 + \sin(\Phi_S - \Phi_R) d\sigma_{UT}$$

B beam polarized



forward
polarized particles
at $\eta < 0$

$$\frac{d\sigma^0}{d\eta d|\mathbf{P}_T| dM} = 2|\mathbf{P}_T| \sum_{a,b,c,d} \int \frac{dx_a dx_b}{8\gamma^2 \bar{z}} f_1^a(x_a) f_1^b(x_b) \frac{d\hat{\sigma}_{ab \rightarrow cd}}{d\hat{t}} D^i(\bar{z}, M) \quad \hat{t} = t x_a / \bar{z}$$

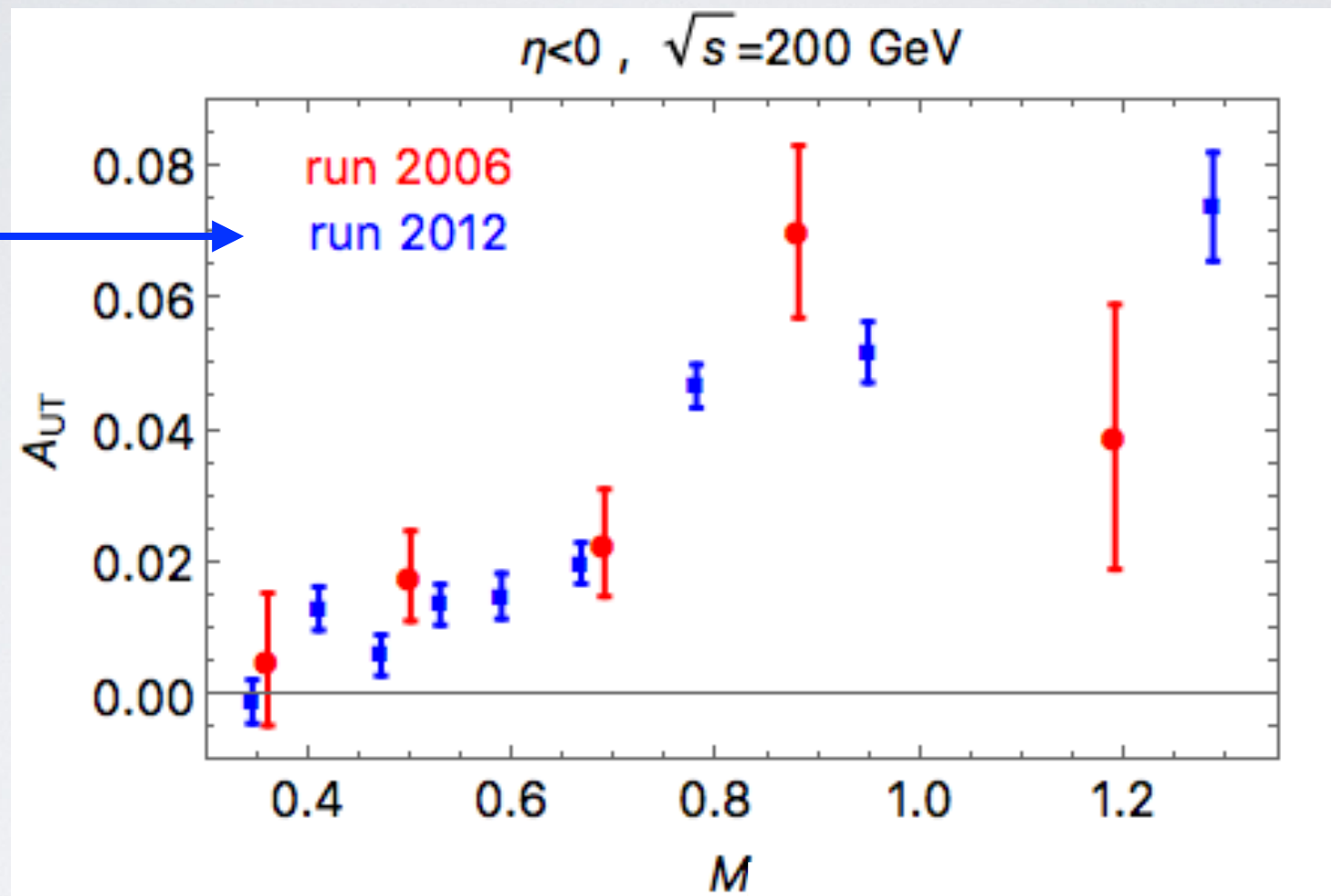
$$\frac{d\sigma_{UT}}{d\eta d|\mathbf{P}_T| dM} = |S_{BT}| |\mathbf{P}_T| \frac{|\mathbf{R}|}{M} \sin \theta \sum_{a,b,c,d} \int \frac{dx_a dx_b}{8\gamma^2 \bar{z}} f_1^a(x_a) h_1^b(x_b) \frac{d\Delta\hat{\sigma}_{ab^\uparrow \rightarrow c^\uparrow d}}{d\hat{t}} H_1^{\leq i}(\bar{z}, M)$$

$|\mathbf{P}_T|$ = transverse component of
pair total momentum
with respect to A beam

hard scale $|\mathbf{P}_T| \gg M, M_A, M_B$

forward $A_{UT}(M)$: STAR data

PRELIMINARY



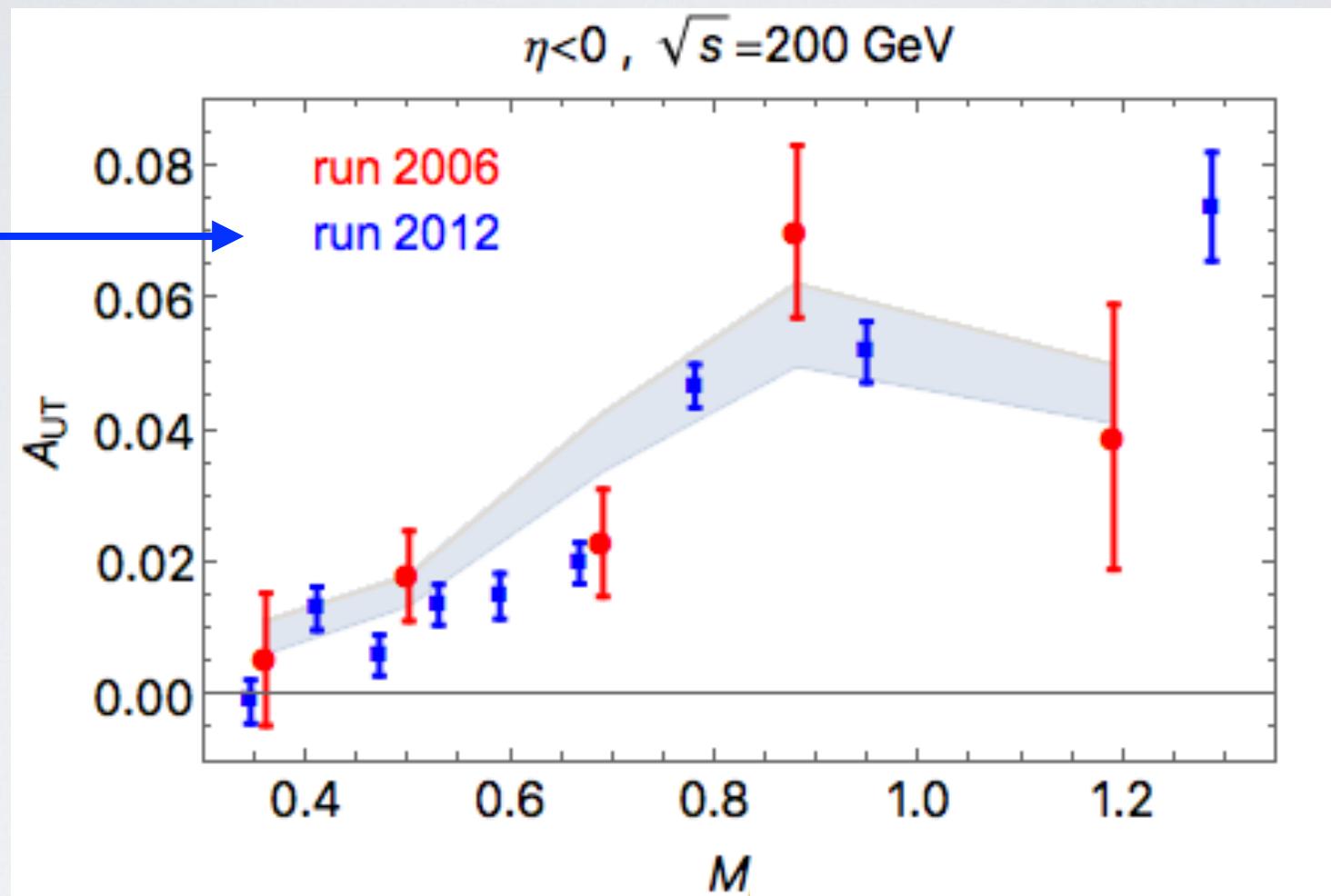
run 2006 Adamczyk et al. (STAR), P.R.L. **115** (2015) 242501

run 2012 K. Landry, talk at APS 2015

forward $A_{UT}(M)$: our prediction vs. STAR data

*Radici et al.,
P.R. D94 (16) 034012*

PRELIMINARY



band = prediction using central 68% of replicas from SIDIS fit

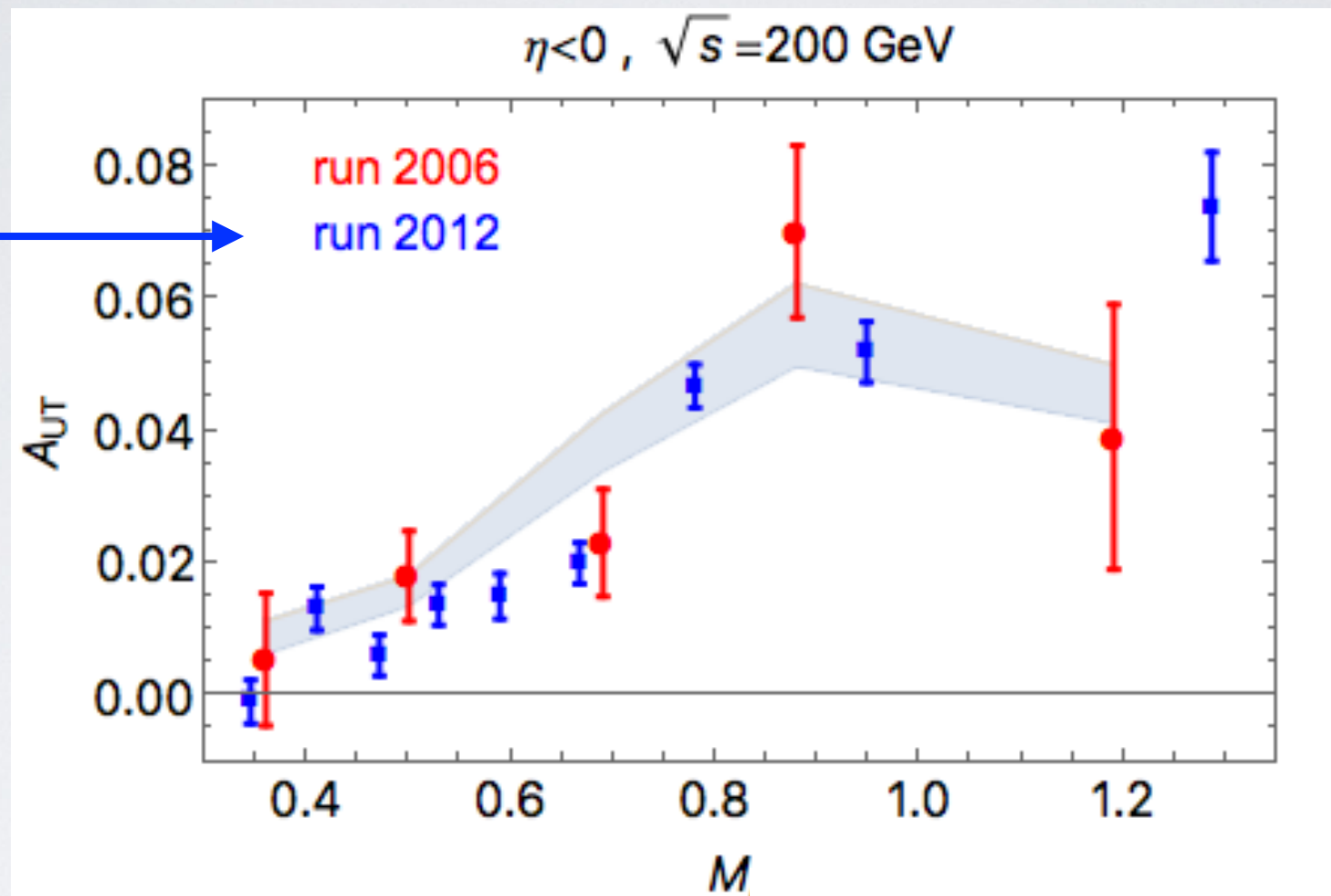
run 2006 *Adamczyk et al. (STAR), P.R.L. 115 (2015) 242501*

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forward $A_{UT}(M)$: our prediction vs. STAR data

*Radici et al.,
P.R. D94 (16) 034012*

PRELIMINARY



band = prediction using central 68% of replicas from SIDIS fit

same mechanism produces asymmetries in SIDIS and pp collisions
 \Rightarrow likely to be universal

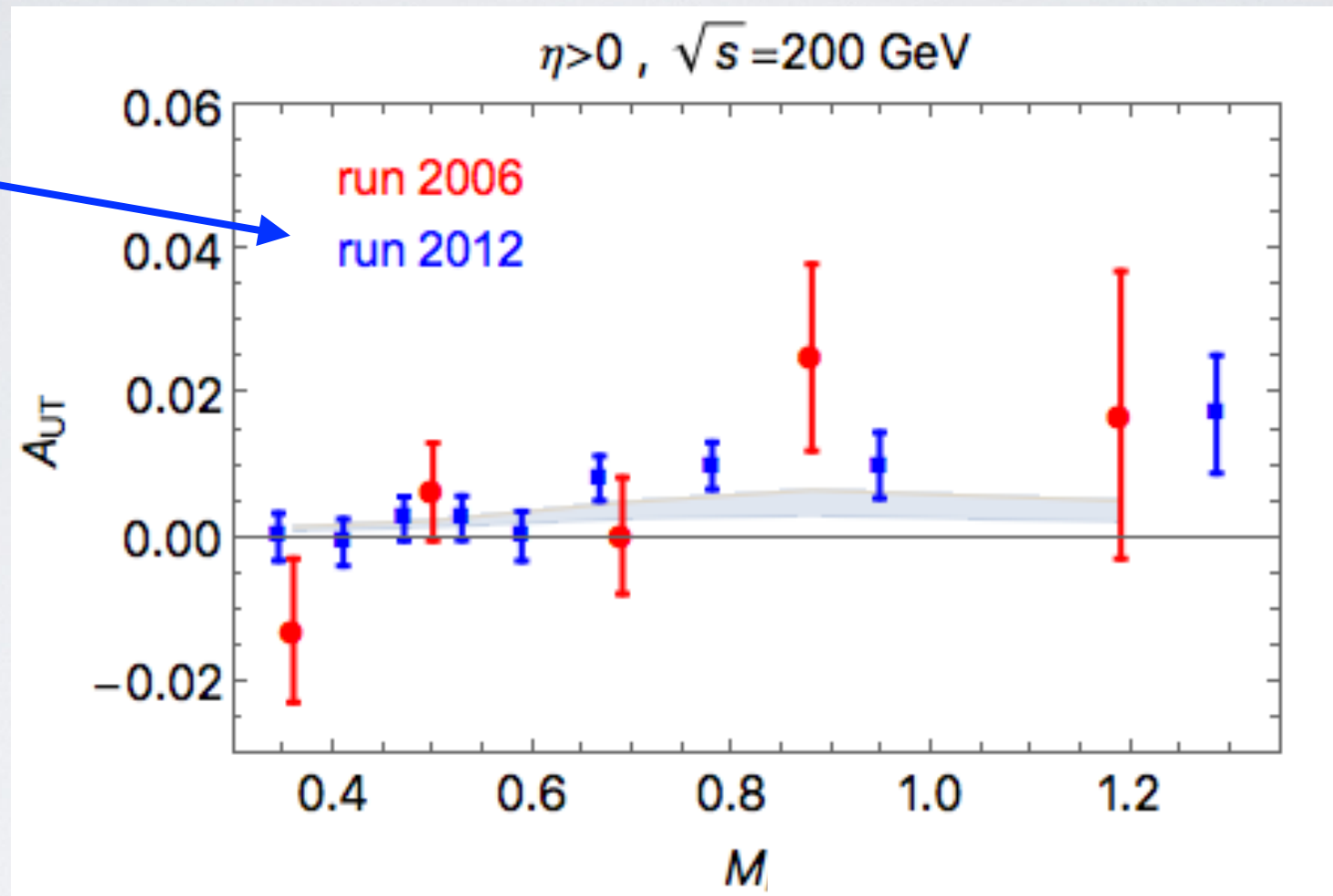
run 2006 *Adamczyk et al. (STAR), P.R.L. 115 (2015) 242501*

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backward $A_{UT}(M)$

*Radici et al.,
P.R. D94 (16) 034012*

PRELIMINARY



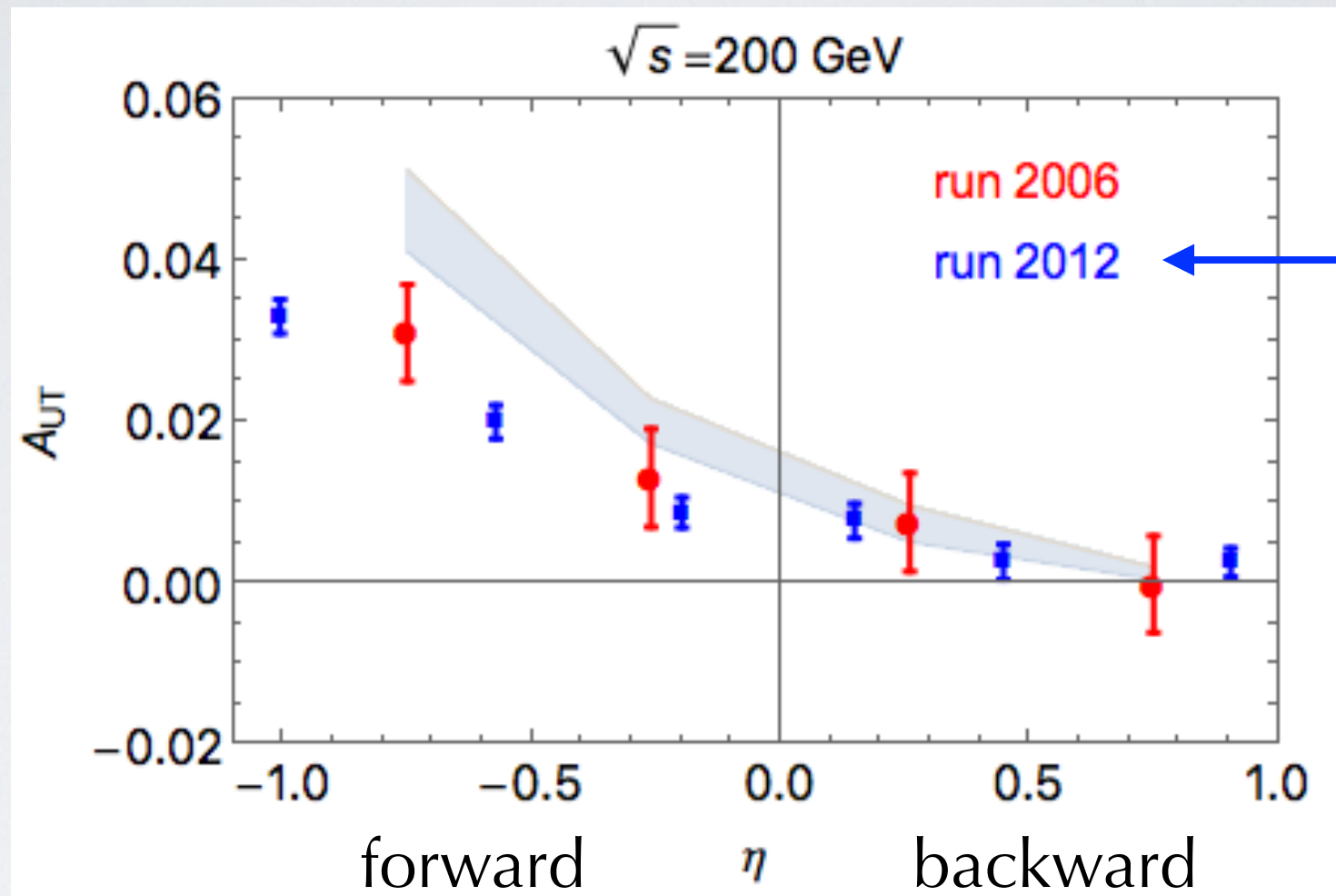
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$A_{UT}(\eta)$

*Radici et al.,
P.R. D94 (16) 034012*



PRELIMINARY

band = prediction using central 68% of replicas from SIDIS fit

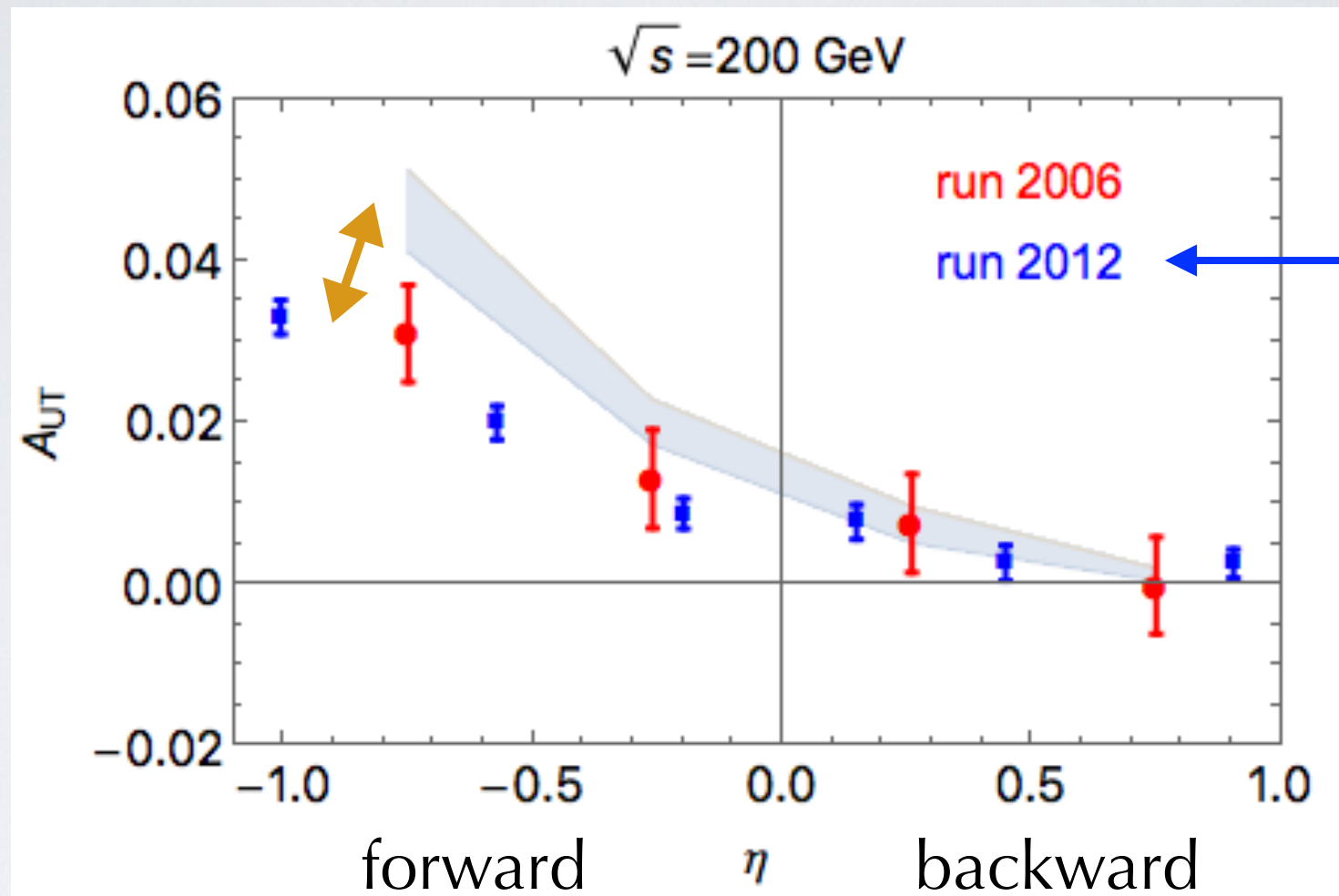
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run 2012 *K. Landry, talk at APS 2015*

$A_{UT}(\eta)$

*Radici et al.,
P.R. D94 (16) 034012*

problem ?



band = prediction using central 68% of replicas from SIDIS fit

run 2006 *Adamczyk et al. (STAR), P.R.L. 115 (2015) 242501*

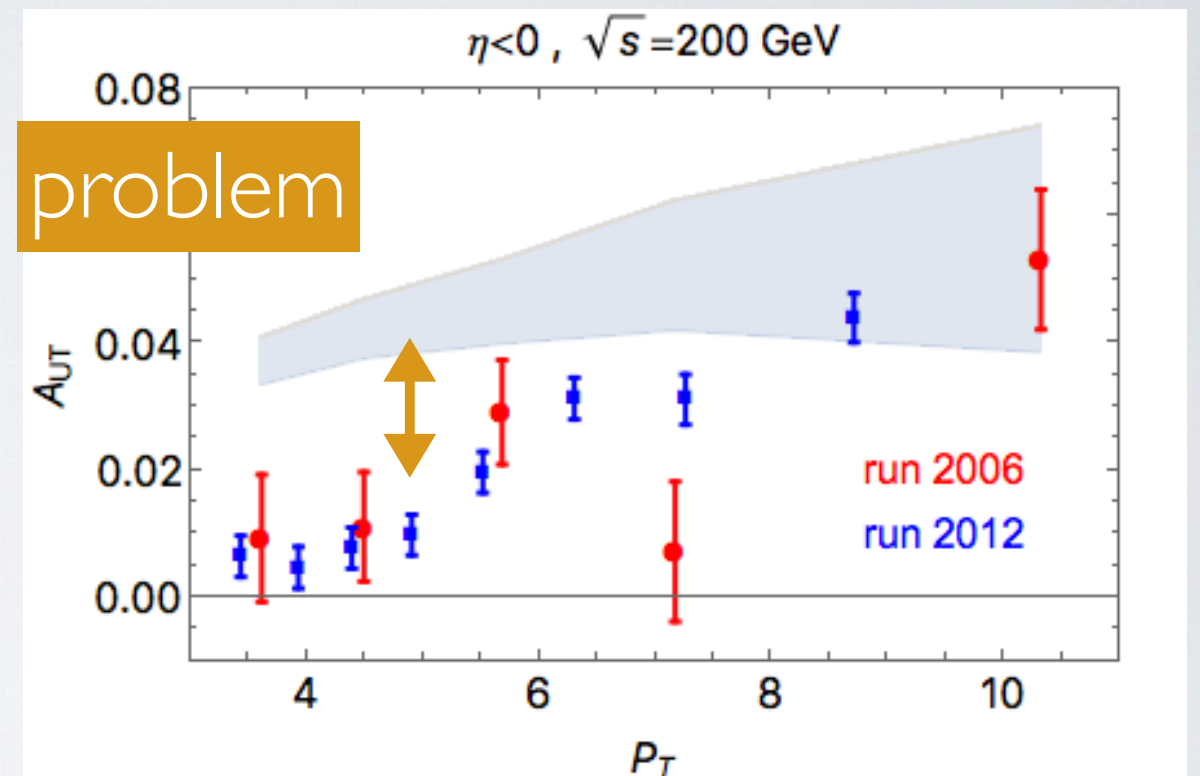
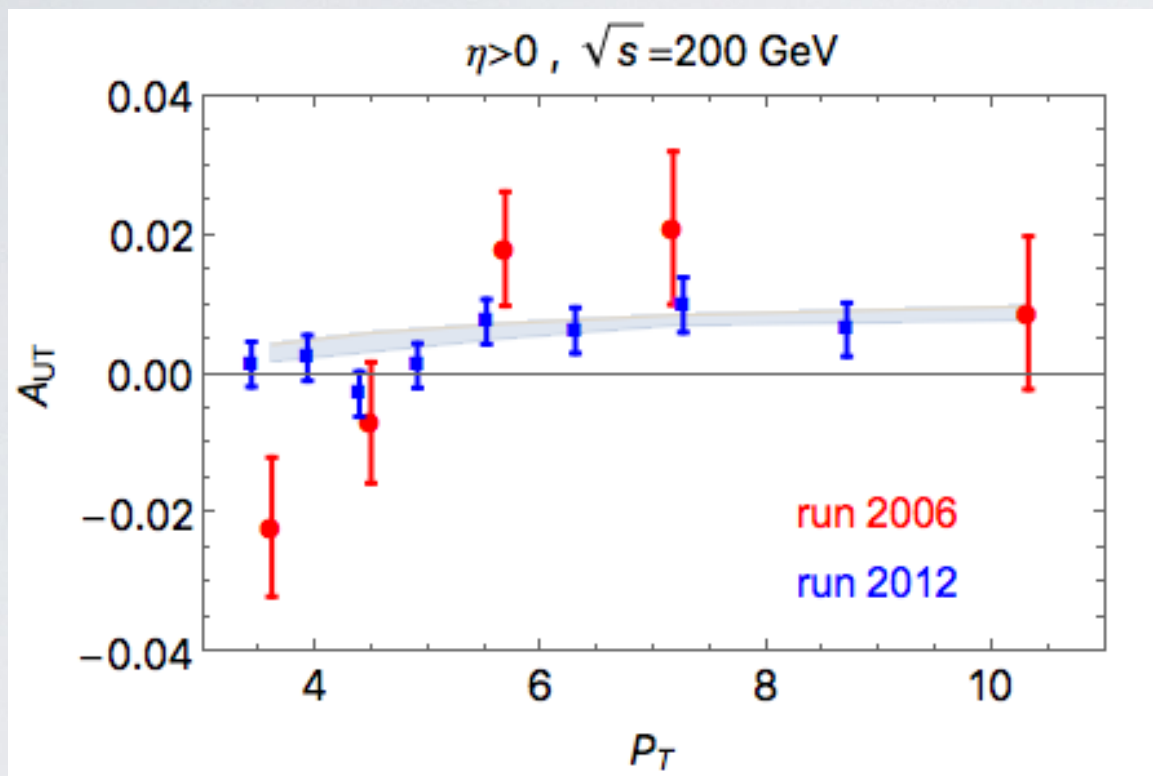
run 2012 *K. Landry, talk at APS 2015*

$A_{UT}(P_T)$

*Radici et al.,
P.R. D94 (16) 034012*

backward

forward



band = prediction using central 68% of replicas from SIDIS fit

PRELIMINARY → **run 2006** Adamczyk et al. (STAR), P.R.L. **115** (2015) 242501
run 2012 K. Landry, talk at APS 2015

problem : K factor ?

$$d\sigma \sim d\sigma^0 + \sin(\Phi_S - \Phi_R) d\sigma_{UT}$$

no data yet for unpol. cross section

$$d\sigma^0 : p+p \rightarrow (\pi\pi) X$$

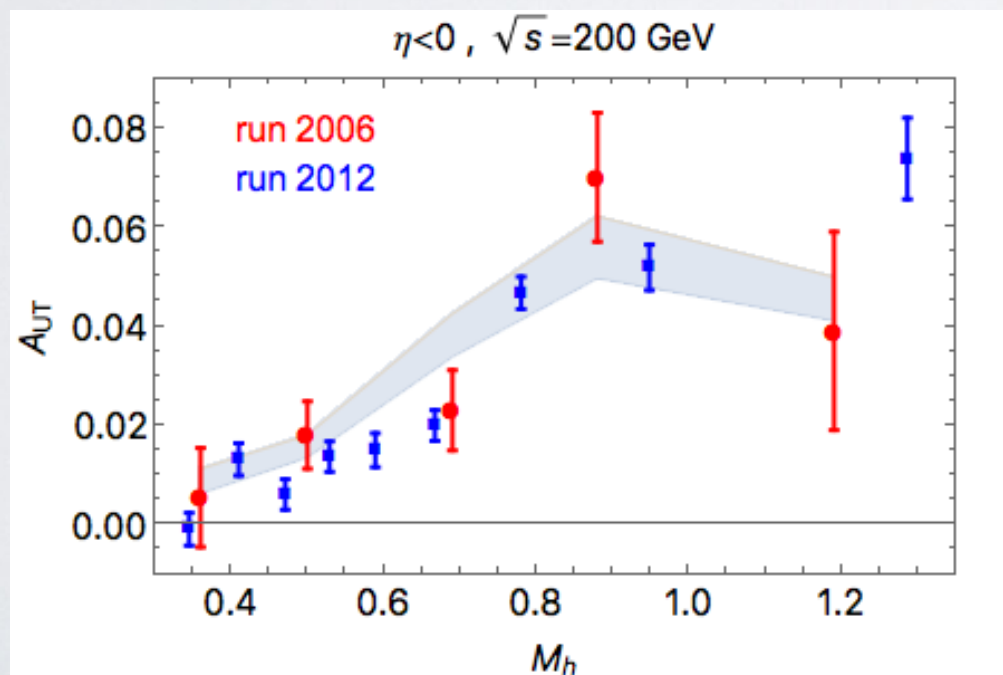
gluon channel unconstrained

only from
DGLAP

$$\frac{d\sigma^0}{d\eta d|\mathbf{P}_T| dM} = 2 |\mathbf{P}_T| \sum_{a,b,c,d} \int \frac{dx_a dx_b}{8\pi^2 \bar{z}} f_1^a(x_a) f_1^b(x_b) \frac{d\hat{\sigma}_{ab \rightarrow cd}}{d\hat{t}} D_1^c(\bar{z}, M)$$

possible large K factor in $d\sigma^0$
(but not in $d\sigma_{UT}$!)

uncertainty band
probably underestimated



problem : K factor ?

$$d\sigma \sim d\sigma^0 + \sin(\Phi_S - \Phi_R) d\sigma_{UT}$$

no data yet for unpol. cross section

$$d\sigma^0 : p+p \rightarrow (\pi\pi) X$$

gluon channel unconstrained

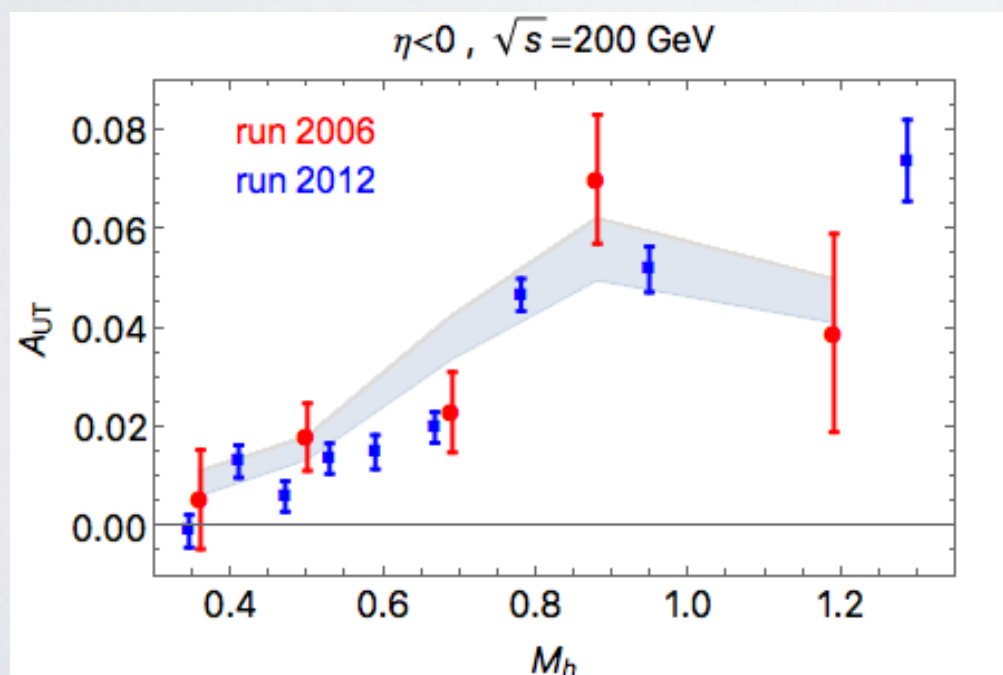
only from
DGLAP

$$\frac{d\sigma^0}{d\eta d|\mathbf{P}_T| dM} = 2 |\mathbf{P}_T| \sum_{a,b,c,d} \int \frac{dx_a dx_b}{8\pi^2 \bar{z}} f_1^a(x_a) f_1^b(x_b) \frac{d\hat{\sigma}_{ab \rightarrow cd}}{d\hat{t}} D_1^c(\bar{z}, M)$$

possible large K factor in $d\sigma^0$
(but not in $d\sigma_{UT}$)

uncertainty band
probably underestimated

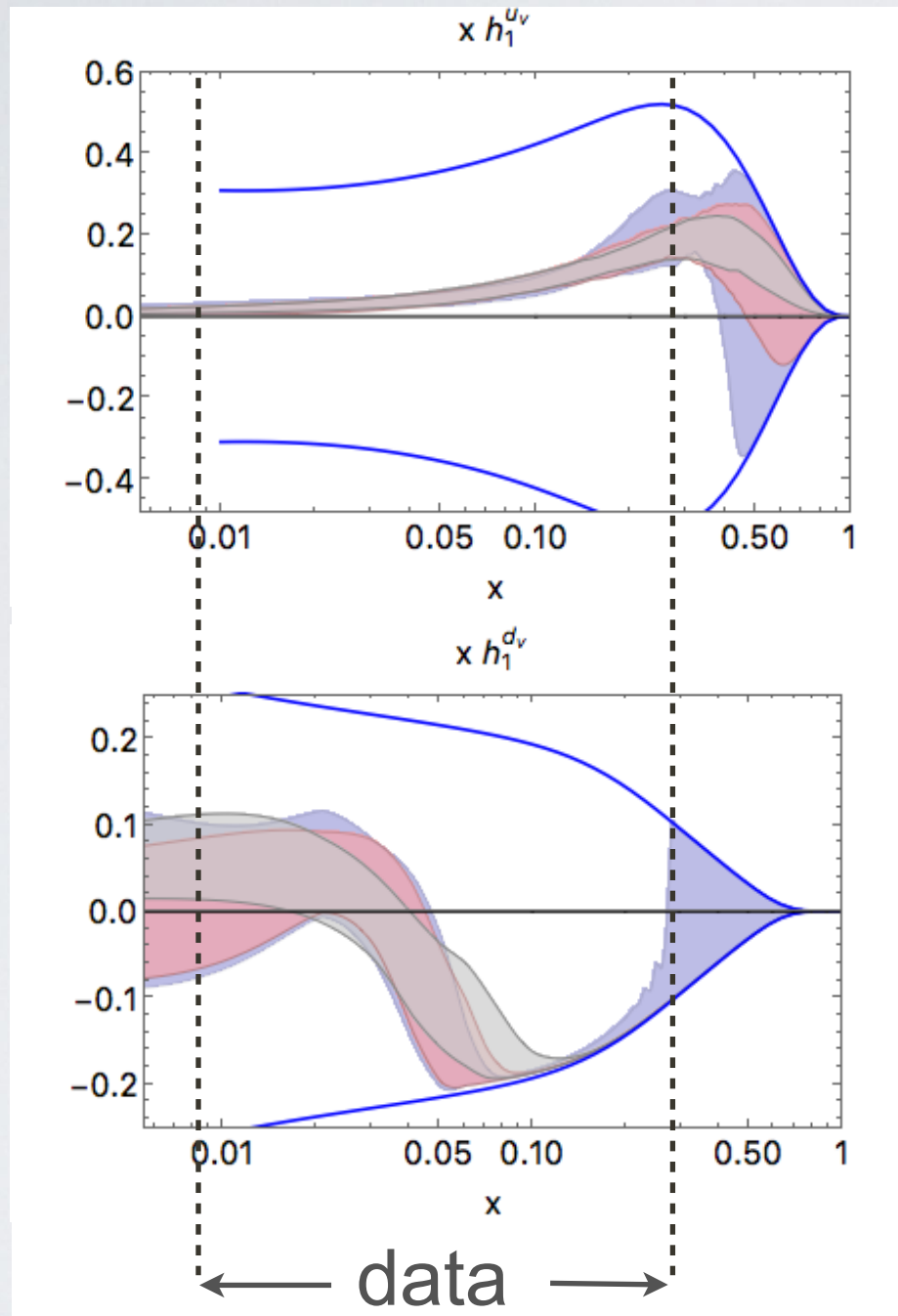
but no K factor can change
sign and trend of $A_{UT}(M)$



stability and saturation of Soffer bound

$$Q^2 = 2.4 \text{ GeV}^2$$

up

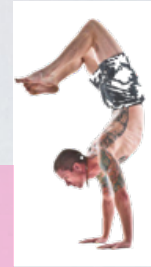


down

rigid



flexible



extra-flexible



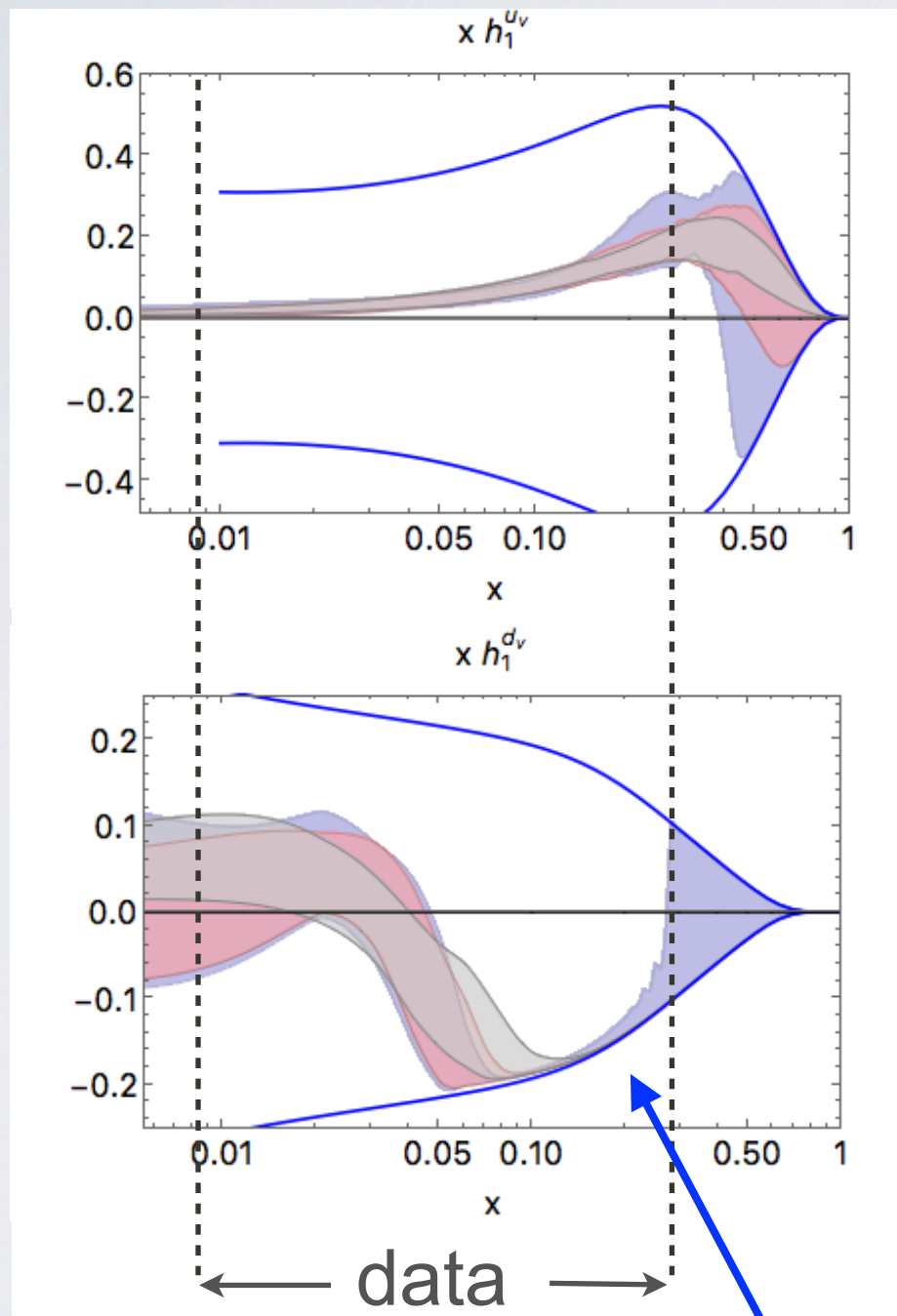
stable results in range of SIDIS data

*Radici et al.,
JHEP **1505** (15) 123*

stability and saturation of Soffer bound

$$Q^2 = 2.4 \text{ GeV}^2$$

up

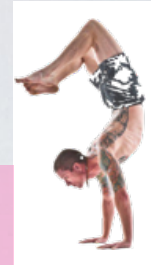


down

rigid



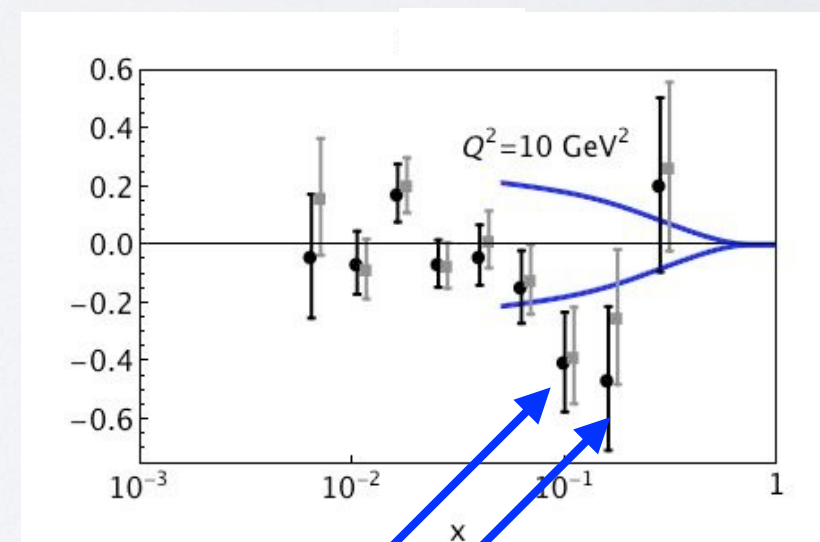
flexible



extra-flexible



stable results in range of SIDIS data
but **unusual saturation of Soffer bound**
for down, due to 2 deuteron bins

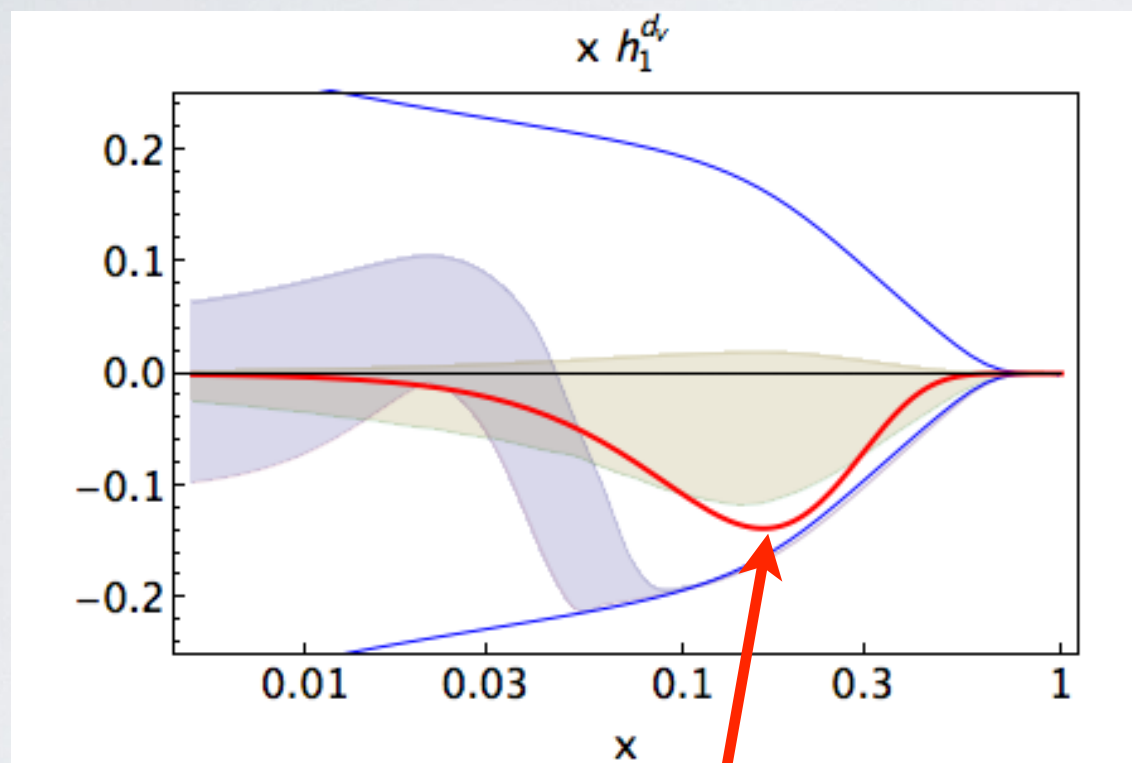


Radici et al.,
JHEP **1505** (15) 123

bins #7,8

origin of saturation of Soffer bound

full SIDIS fit

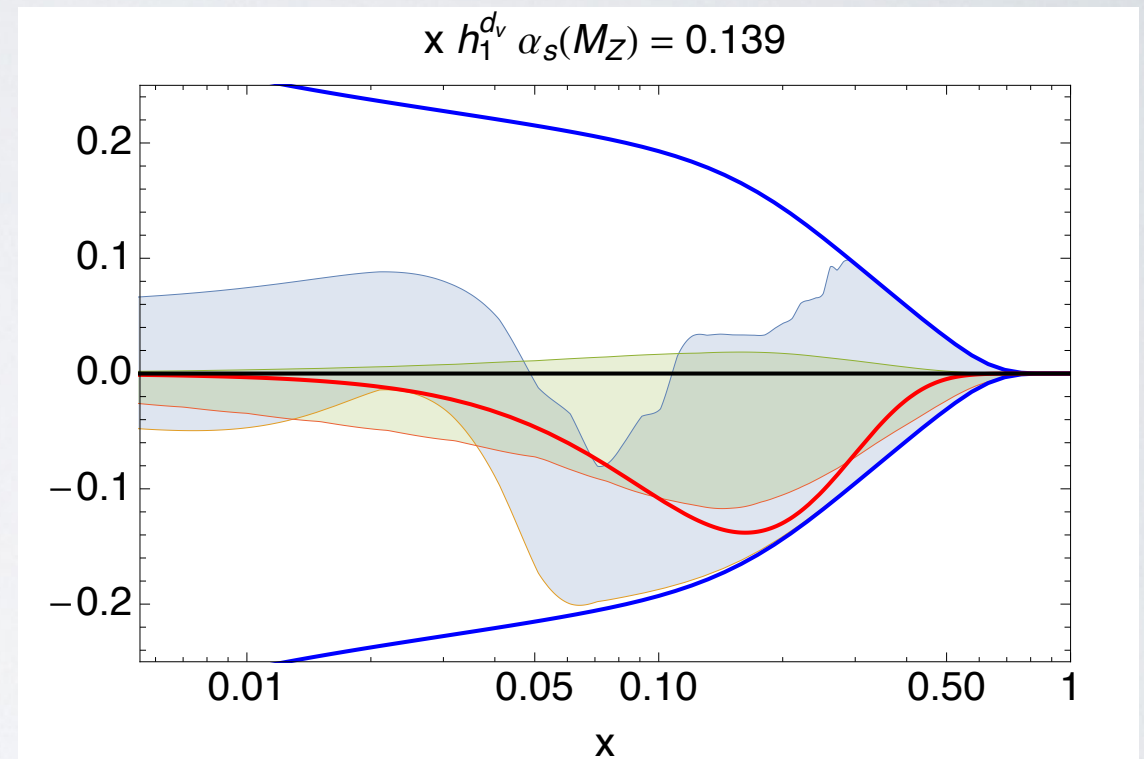


Kang et al.,
P.R. D93 (16) 014009

Radici et al.,
JHEP 1505 (15) 123

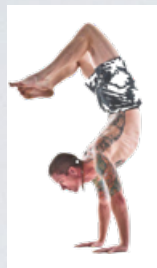
Anselmino et al.,
P.R. D87 (13) 094019

“reduced” SIDIS fit :
no bins #7,8 with deuteron



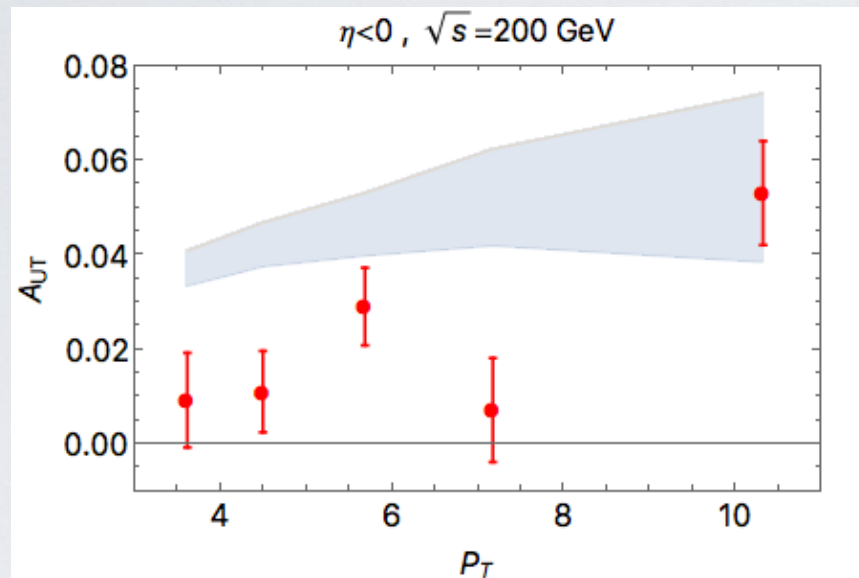
more flexibility
for down

no appreciable difference
for up

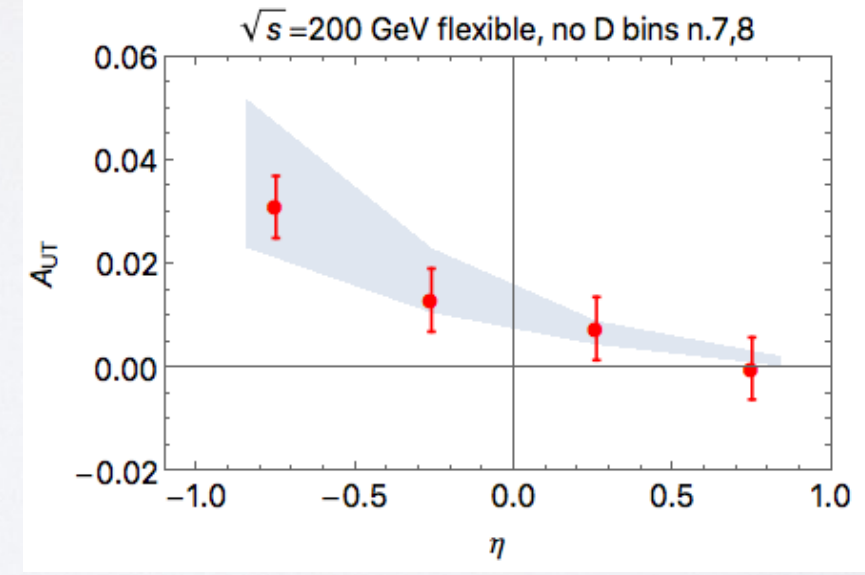
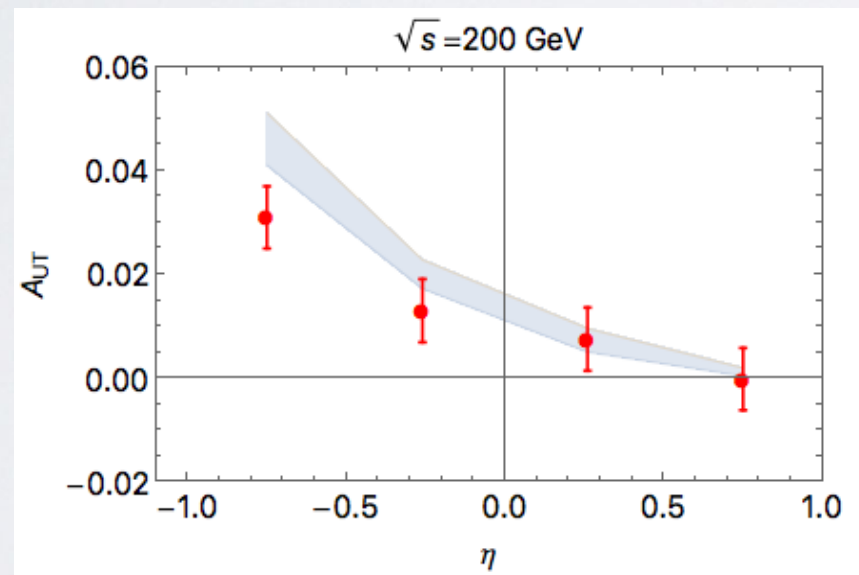
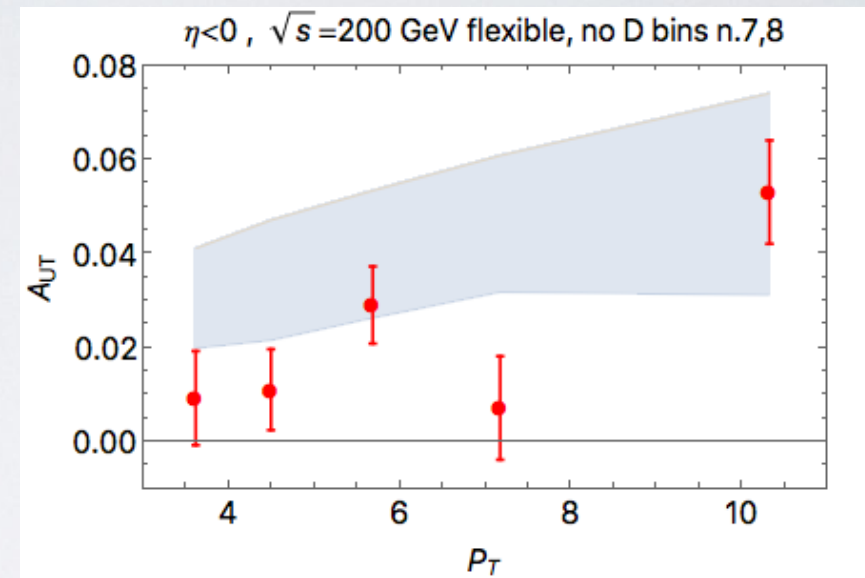


forward $A_{UT}(P_T)$ and $A_{UT}(\eta)$ with “reduced” fit

full SIDIS fit

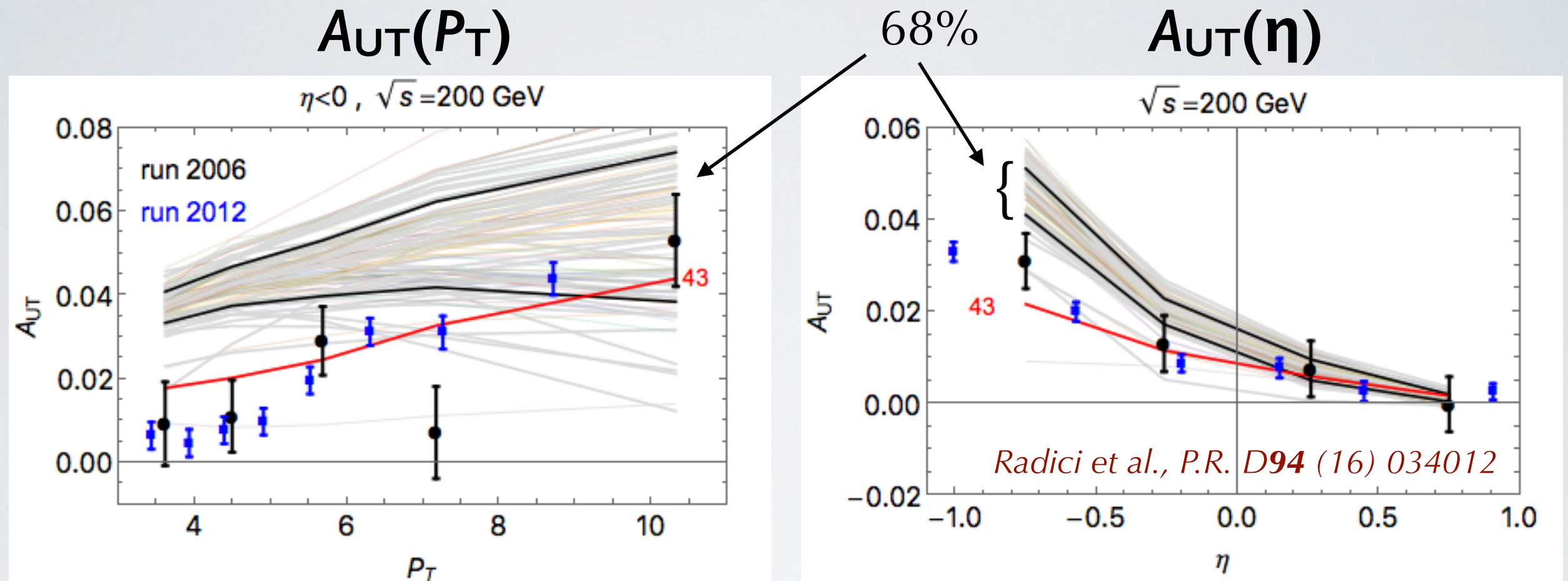


“reduced” SIDIS fit



“reduced” fit : more flexibility \Rightarrow better compatibility

reconsider **problem** in forward kin.



some replicas outside the 68% band from SIDIS fit
show compatibility with p-p data in forward kin.

selectivity of p-p data on results from SIDIS fit

need global fit
work in progress

run 2006

Adamczyk et al. (STAR), P.R.L. 115 (15) 242501

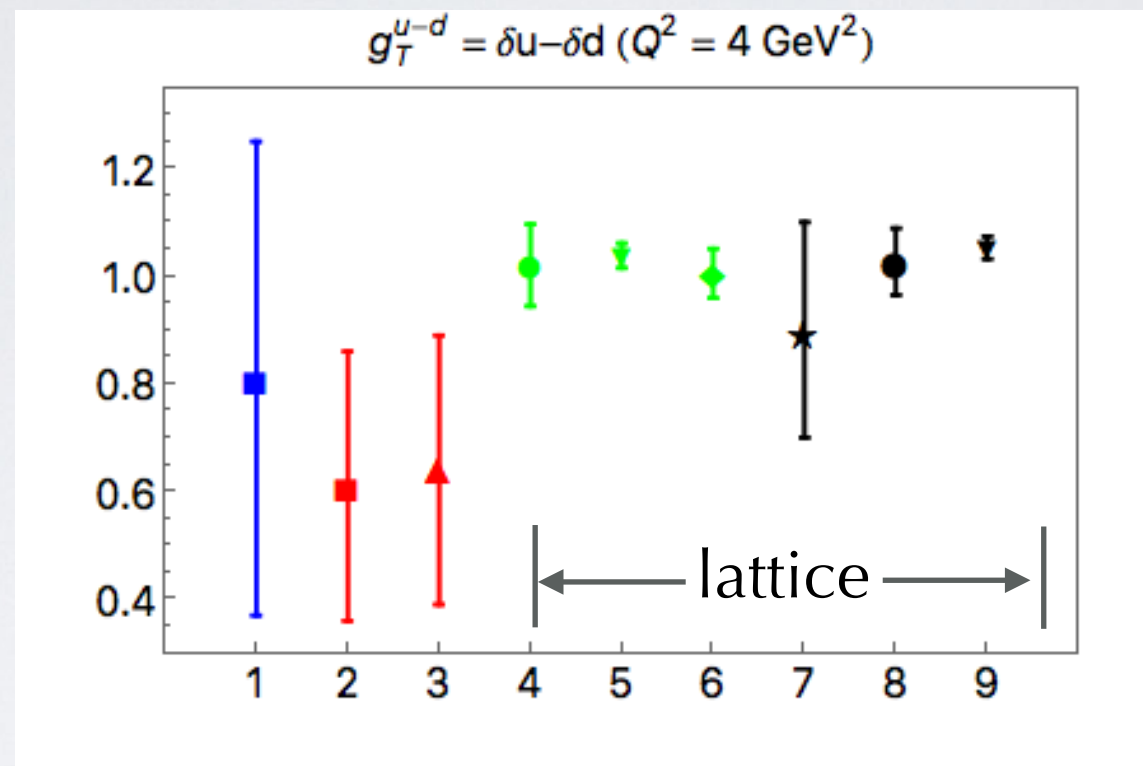
PRELIMINARY →

run 2012

K. Landry, talk at APS 2015

neutron β -decay \longleftrightarrow isovector tensor charge

g_T^{u-d} affects tensor coupling in β -decay



$Q^2 = 4 \text{ GeV}^2$

4) **PNDME '15** *Bhattacharya et al., P.R. D92 (15)*

5) **LHPC '12** *Green et al., P.R. D86 (12)*

6) **RQCD '14** *Bali et al., P.R. D91 (15)*

7) **RBC-UKQCD** *Aoki et al., P.R. D82 (10)*

8) **ETMC '15** *Abdel-Rehim et al., P.R. D92 (15);*

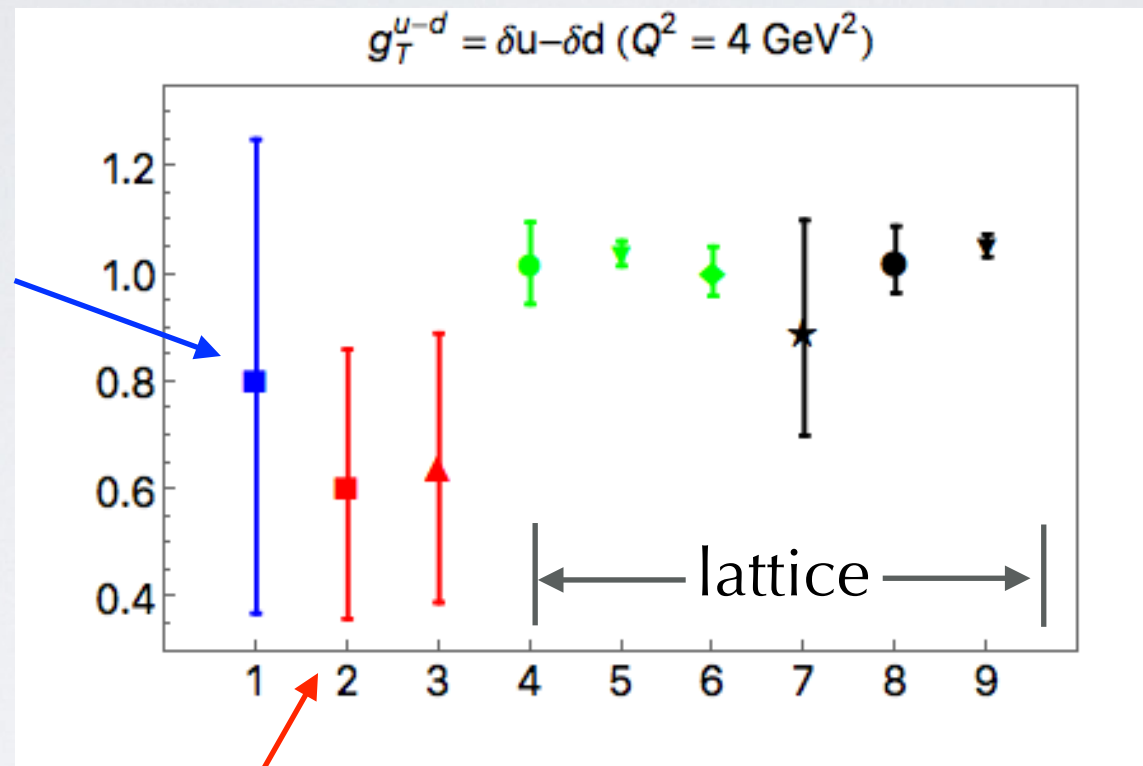
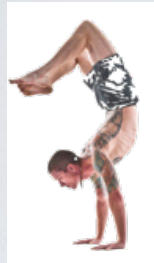
E P.R. D93 (16)

9) **ETMC '15**

neutron β -decay \longleftrightarrow isovector tensor charge

g_T^{u-d} affects tensor coupling in β -decay

1) Radici et al. 2015



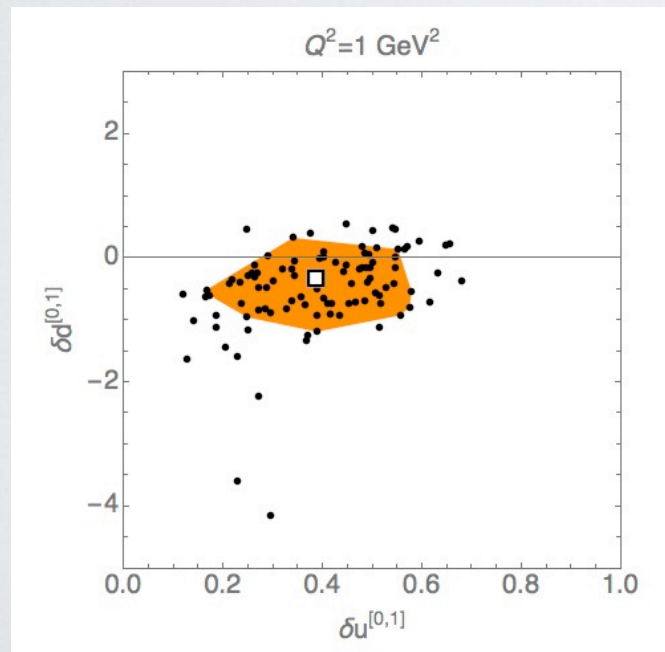
$Q^2 = 4 \text{ GeV}^2$

2) Kang et al. 2016

$Q^2 = 10$

3) Anselmino et al. 2013

$Q^2 = 0.8$



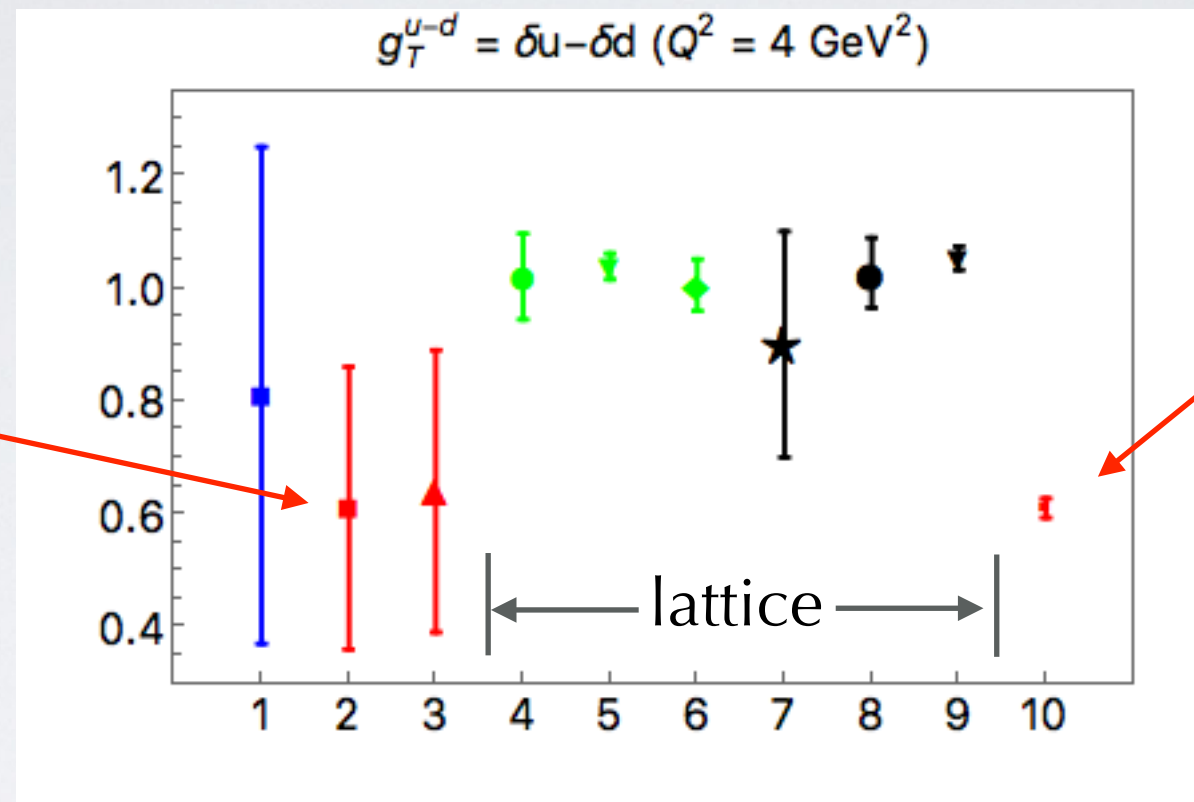
neutron β -decay \longleftrightarrow isovector tensor charge

g_T^{u-d} affects tensor coupling in β -decay

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$Q^2 = 10$



10) SoLID 2016

pseudo-data based
on 2) Kang et al. 2016

$Q^2 = 10$

Ye et al., arXiv:1609.02449

caveat:

SoLID acceptance

$\rightarrow x \in [0.05, 0.6]$

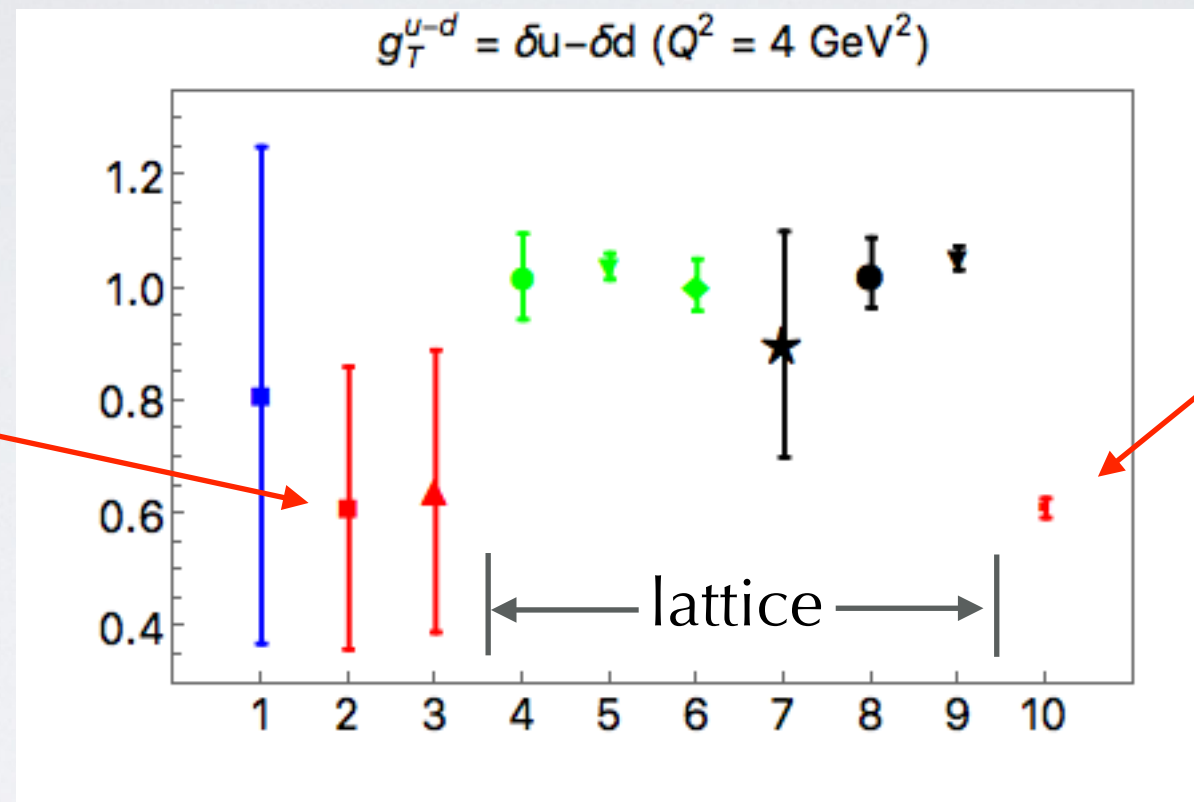
neutron β -decay \longleftrightarrow isovector tensor charge

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10) SoLID 2016

pseudo-data based
on 2) Kang et al. 2016
 $Q^2 = 10$

Ye et al., arXiv:1609.02449

caveat:

SoLID acceptance
 $\rightarrow x \in [0.05, 0.6]$

current most stringent constraints
on BSM tensor coupling from
 $\pi^+ \rightarrow e^+ \nu_e \gamma$ and neutron β -decay is

$$|\epsilon_T g_T| \lesssim 5 \times 10^{-4}$$

Bychkov et al. (PIBETA), P.R.L. 103 (09) 051802

Pattie et al., P.R. C88 (13) 048501

potential of SoLID can bring
precision to level of
modern lattice calculations
and β -decay measurements

Conclusions

- transversity can be reliably extracted from data using semi-inclusive di-hadron production
- di-hadron method works in collinear factorization
 - cross-check of Collins effect in TMD factorization
 - extension to p-p collisions → check universality
global fit in progress

Next: complete global fit of existing 2h-SIDIS & p-p data

- tensor charge useful for low-energy explorations of BSM new physics

need more data at (very) large and (very) small x
“short run”: RHIC & JLAB12 “long run”: EIC

Backup slides

reweighting the replicas

NNPDF Collaboration, N.P. **B849** (11) 112; E **B854** (12) 926; E **B855** (12) 927; arXiv:1012.0836v4

- each **replica h_k** ($k=1, \dots, N$) carries equal weight (important sampling)
- effect of set of new independent n data by assigning **new weights w_k**
 $w_k \Leftrightarrow$ probability for each **replica h_k** to agree with **new n data** (χ_k^2)

$$w_k = \frac{(\chi_k^2)^{\frac{1}{2}(n-1)} e^{-\frac{1}{2}\chi_k^2}}{\frac{1}{N} \sum_{k=1}^N (\chi_k^2)^{\frac{1}{2}(n-1)} e^{-\frac{1}{2}\chi_k^2}}$$

- **price to pay:** replica k with **very low w_k** is statistically irrelevant
loss of efficiency quantifiable through Shannon entropy

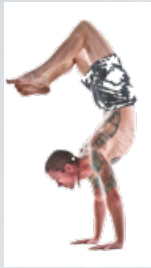
$$N_{\text{eff}} = \exp \left\{ \frac{1}{N} \sum_{k=1}^N w_k \ln \left(\frac{N}{w_k} \right) \right\} \leq N$$

- χ^2 -profile of reweighted replicas

$$P[A_\chi = \{\chi^2 \leq \chi_k^2 < \chi^2 + d\chi^2\}] = \sum_{k \in A_\chi} w_k$$

if $P[A_\chi]$ peaked at $\chi \sim O(1)$
new data bring new info
otherwise are inconsistent

χ^2 -profile of reweighted replicas



“reduced” SIDIS fit
flexible param.

N=100 replicas

χ^2 -profile

n=24 RHIC data

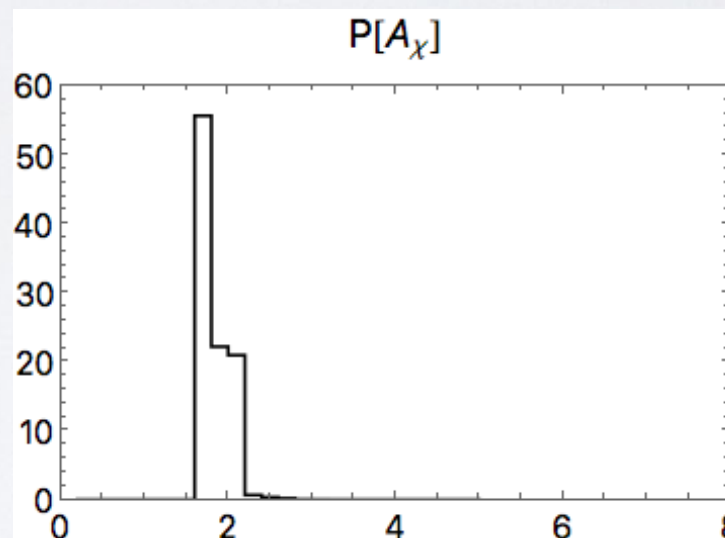
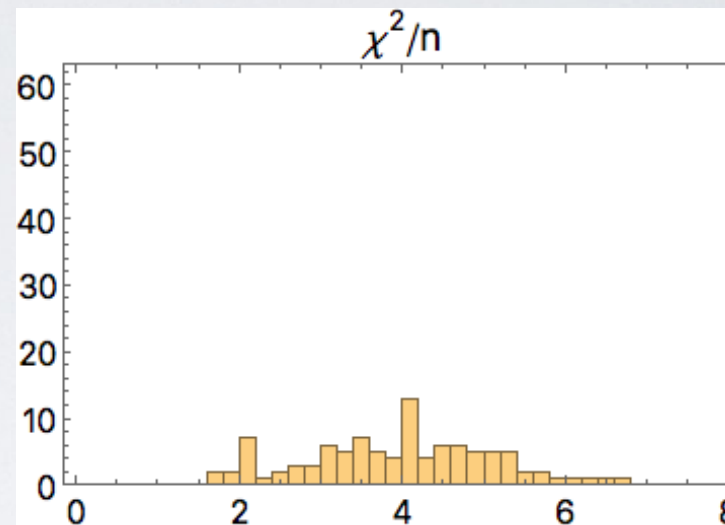
from run 2006

*Adamczyk et al. (STAR),
P.R.L. **115** (15) 242501*

N_{eff} = 7

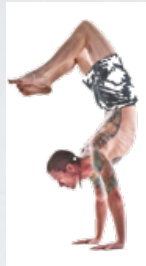
χ^2 -profile

reweighted replicas

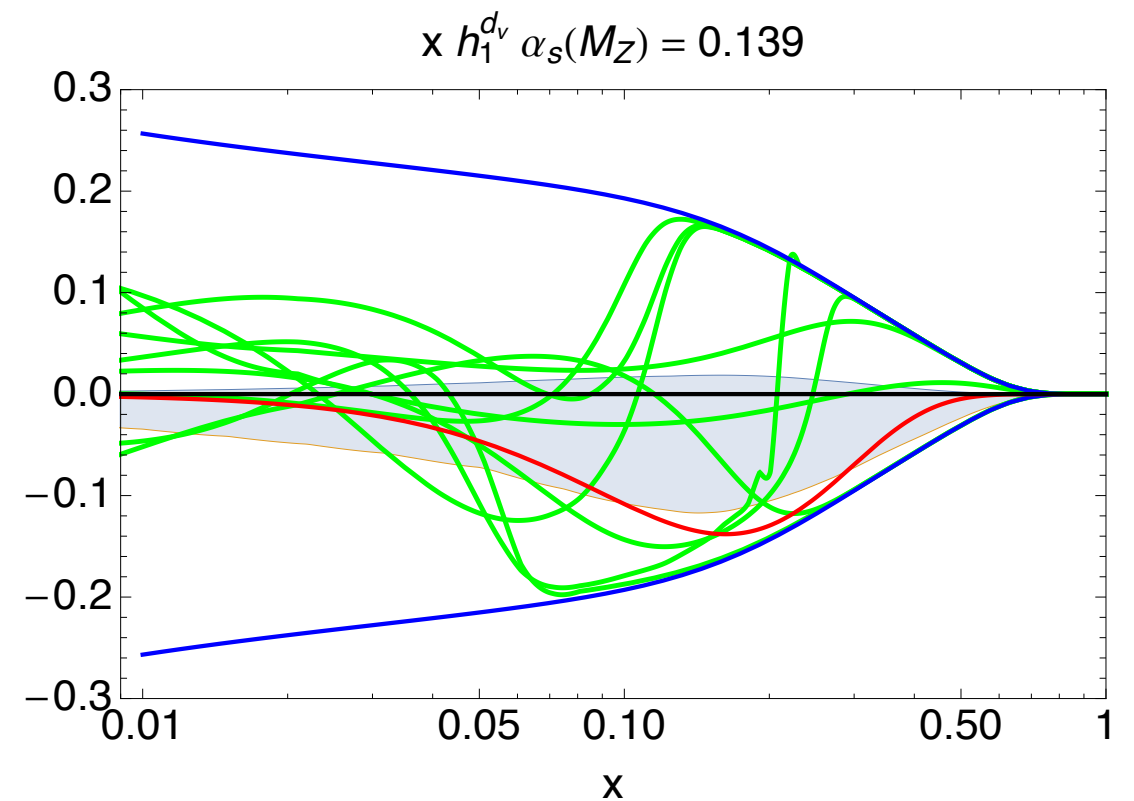
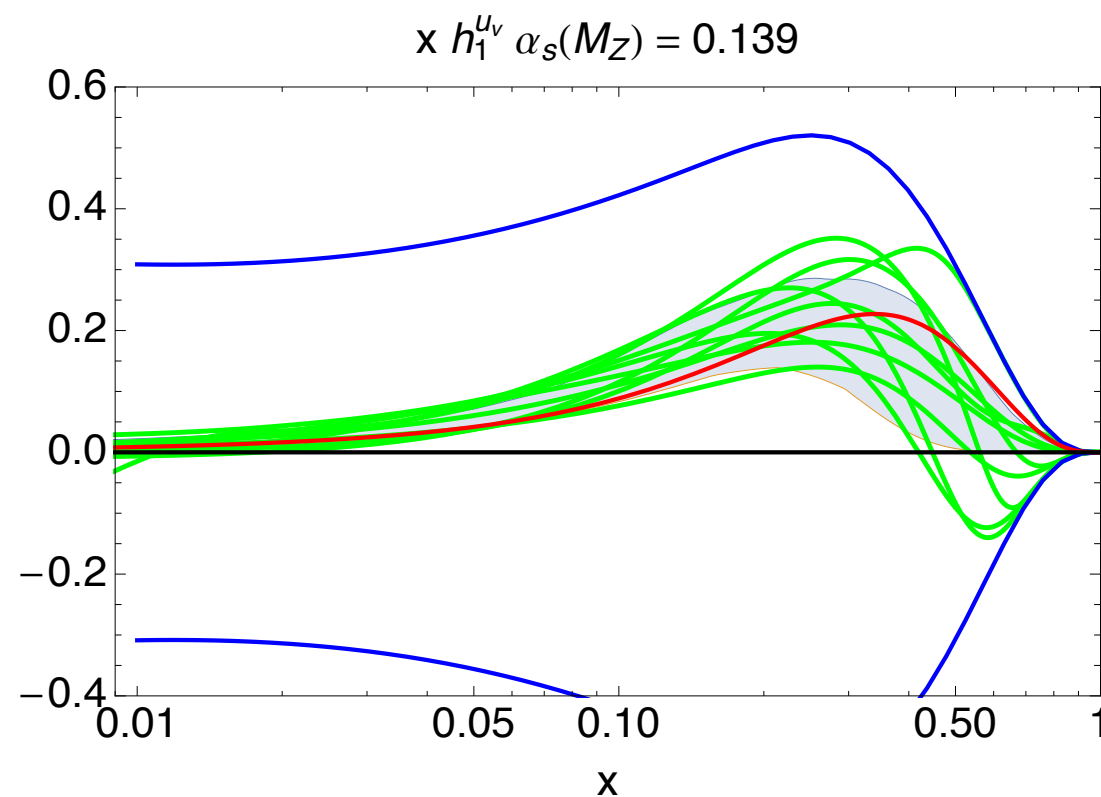


STAR data very selective on “reduced” SIDIS fit:
reduce the number of statistically relevant replicas by factor ≈ 10

statistically most relevant replicas



flexible param.



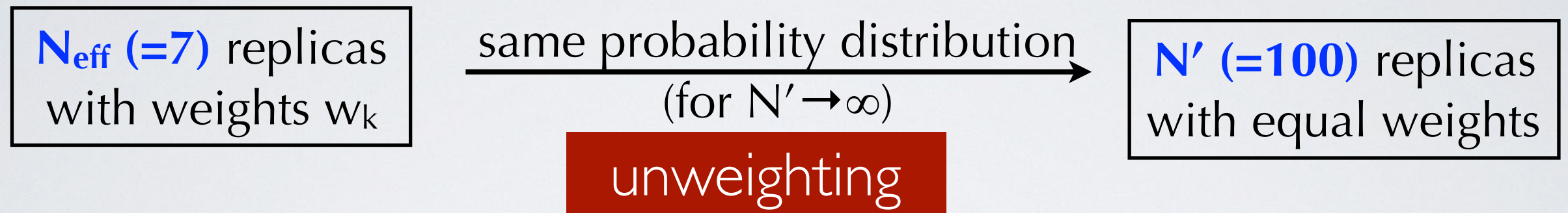
— reweighted replicas

— Kang et al.,
P.R. D**93** (16) 014009

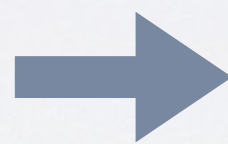
— Anselmino et al.,
P.R. D**87** (13) 094019

reweighting replicas on deuteron bins #7,8

- “reduced” SIDIS fit: **$N=100$** replicas with equal weights
- **reweighting** on STAR data (run 2006) \rightarrow **$N_{\text{eff}}=7$** replicas with weights w_k



replica with large w_k
with small w_k



take it w'_k times
discard it

*NNPDF Collaboration,
N.P. **B855** (12) 608;
arXiv:1108.1758v2*

- reweighting **$N'=100$** replicas on bins #7,8 \rightarrow **$N'_{\text{eff}}=73$** replicas
but χ^2 profile of reweighted replicas not peaked at $\sim O(1)$

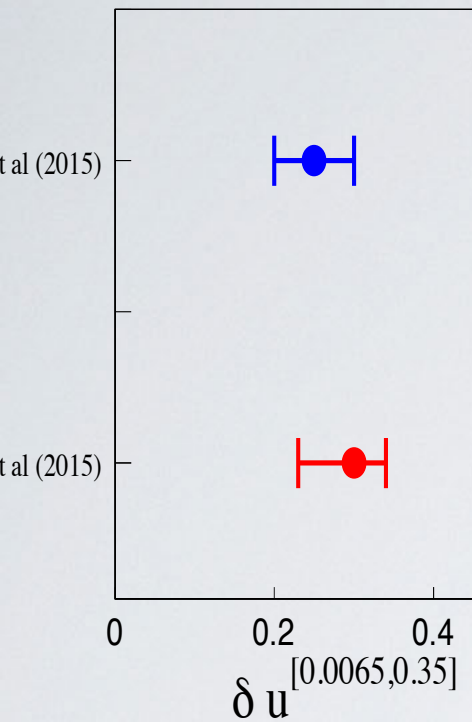
global fit of SIDIS and p-p data in progress...

back to tensor charge

$$Q^2 = 10 \text{ GeV}^2$$

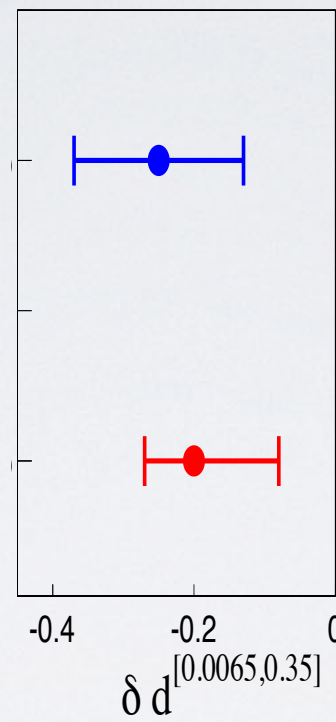
$$\delta q \equiv g_T^q = \int_0^1 dx [h_1^q(x, Q^2) - h_1^{\bar{q}}(x, Q^2)]$$

truncated to data range
 $x \in [0.0065, 0.35]$



Radici et al. 2015

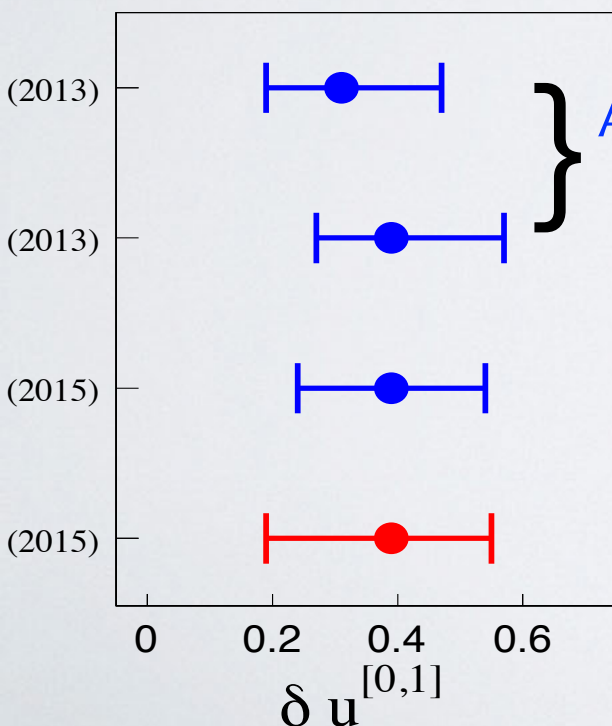
Kang et al. 2016



extrapolation to $[0,1]$

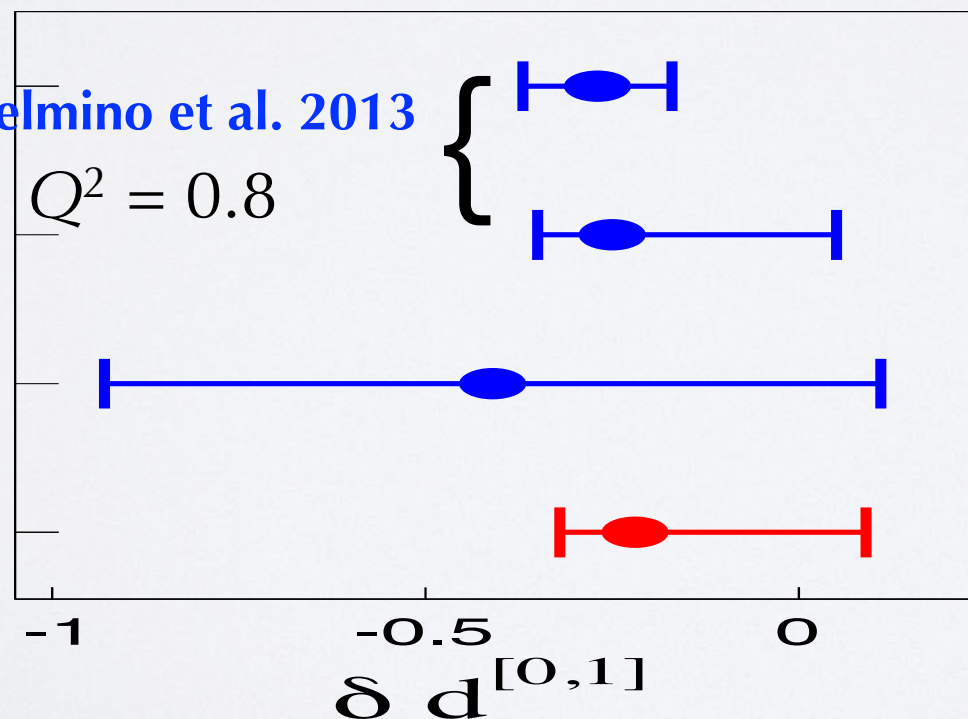


expect larger uncertainties



Anselmino et al. 2013

$$Q^2 = 0.8$$



Radici et al. 2015

$$Q^2 = 1$$

Kang et al. 2016

$$Q^2 = 10$$

- extrapolated tensor charges for TO2013: upper for standard param., lower for polynomial param.

precision of g_T^{u-d}

current most stringent constraints on BSM tensor coupling come from

- Dalitz-plot study of radiative pion decay $\pi^+ \rightarrow e^+ \nu_e \gamma$

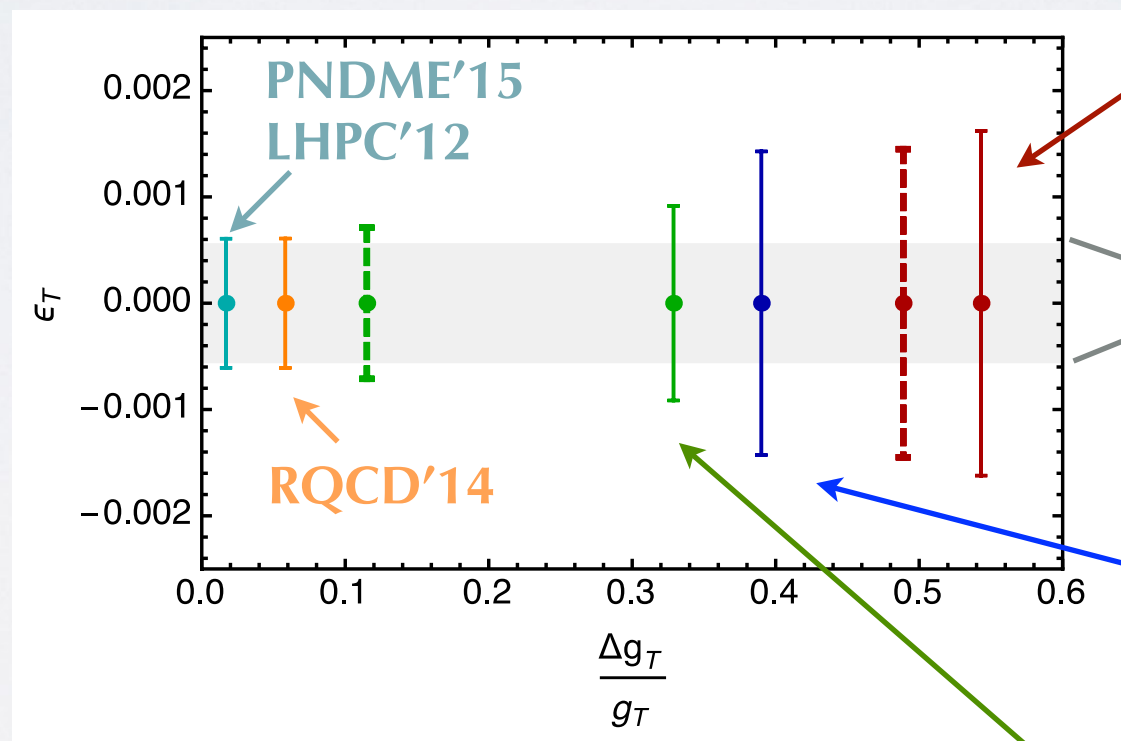
Bychkov et al. (PIBETA), P.R.L. 103 (09) 051802

- measurement of correlation parameters in neutron β -decay of various nuclei

Pattie et al., P.R. C88 (13) 048501

$$|\epsilon_T g_T| \lesssim 5 \times 10^{-4}$$

need to adapt
phenomenology
to precision of
measurements
and lattice
JLAB12 is
good opportunity



Courtoy et al., P.R.L. 115 (2015) 162001

Goldstein et al., arXiv:1401.0438