

Various structures of the neutron-rich nucleus ^{31}Mg investigated by β - γ spectroscopy of spin-polarized ^{31}Na

Hiroki Nishibata

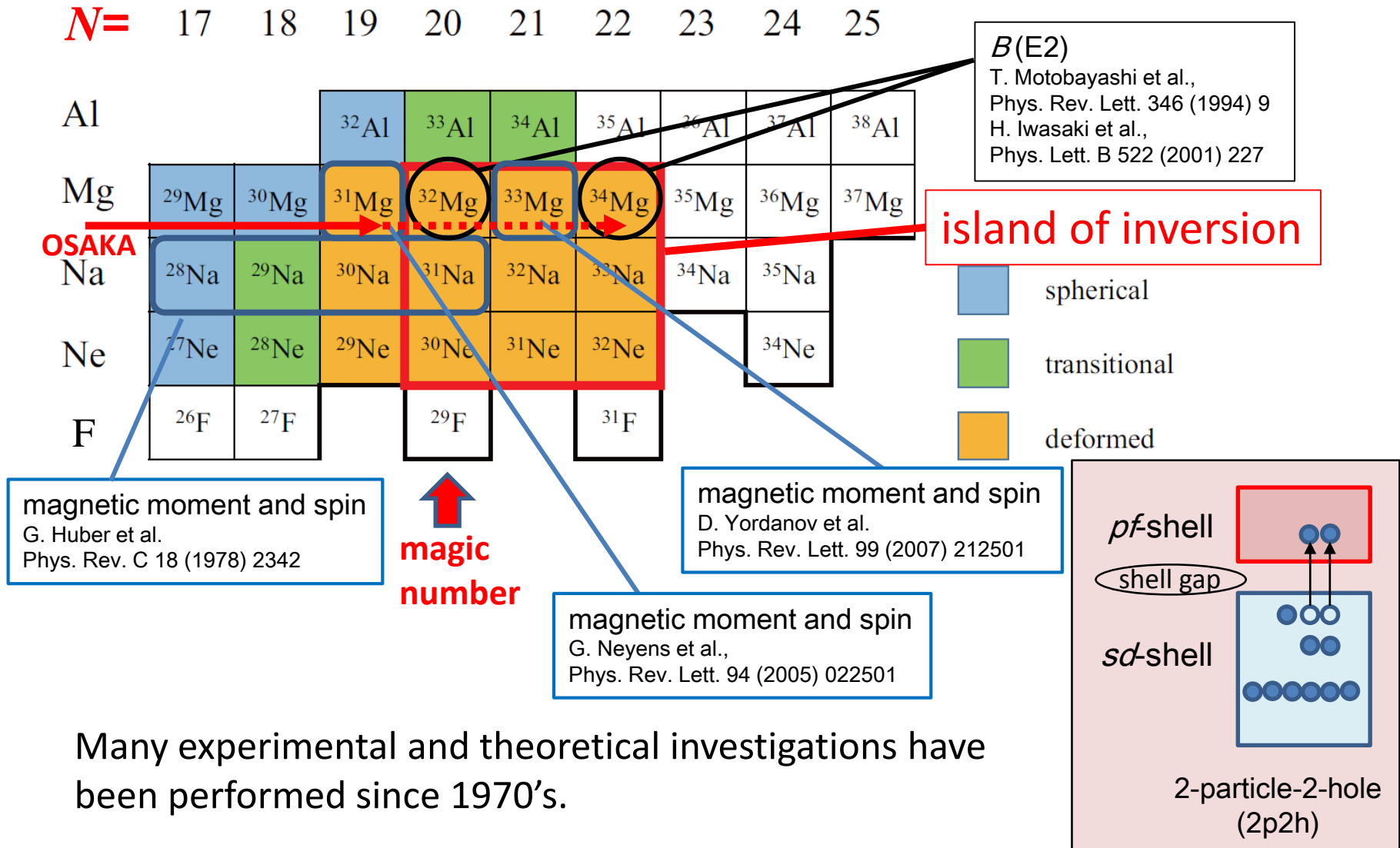
Nuclear Spectroscopy Laboratory, RIKEN

PhD work
at Osaka Univ.

- Applications of **spin polarization** to nuclear structure study.
- Unique method to **assign spin-parity** of excited levels based on β - γ spectroscopy of **spin-polarized Na isotopes**.
- Investigation of **nuclear structure of their daughters, i.e., Mg isotopes**.

Physics motivation

Deformed ground states of neutron rich nuclei with $N \sim 20$



Large-scale Shell Model calculations

Caurier et al., Phys.Rev. C 90 (2014) 014302

SDPF-U-MIX interaction

model space **n: sd-pf**, p: sd across the $N=20$ “shell gap”

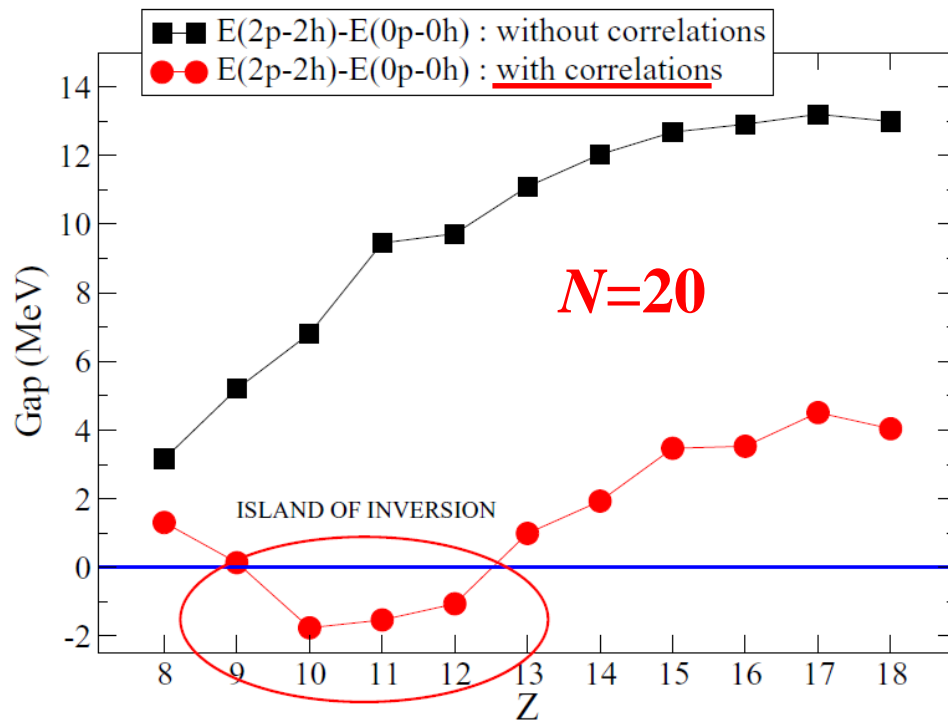


FIG. 5. (Color online) The gap between the 0p-0h and the 2p-2h configurations at $N = 20$, without correlations (squares) and including correlations (circles). Nuclei close to or below the zero line are candidates to belong to the island of inversion.

- Nuclear correlations pull down the (2p-2h) level energies, and in some cases they become lower than the normal (0p-0h) level energies.
- The existence of islands of inversion or deformation are explained as the result of the competition between
 - (1) the spherical mean field
 - and
 - (2) nuclear correlations which favor the deformed configurations.

Shape coexistence

competition between spherical mean field
and nuclear correlation which drives
deformation



investigation of **shape coexistence** in the low
excitation energy region



comparison of the experimental and
theoretical levels **on the level-by-level basis**

Today's talk : ^{31}Mg (N=19)

Various structures in ^{31}Mg

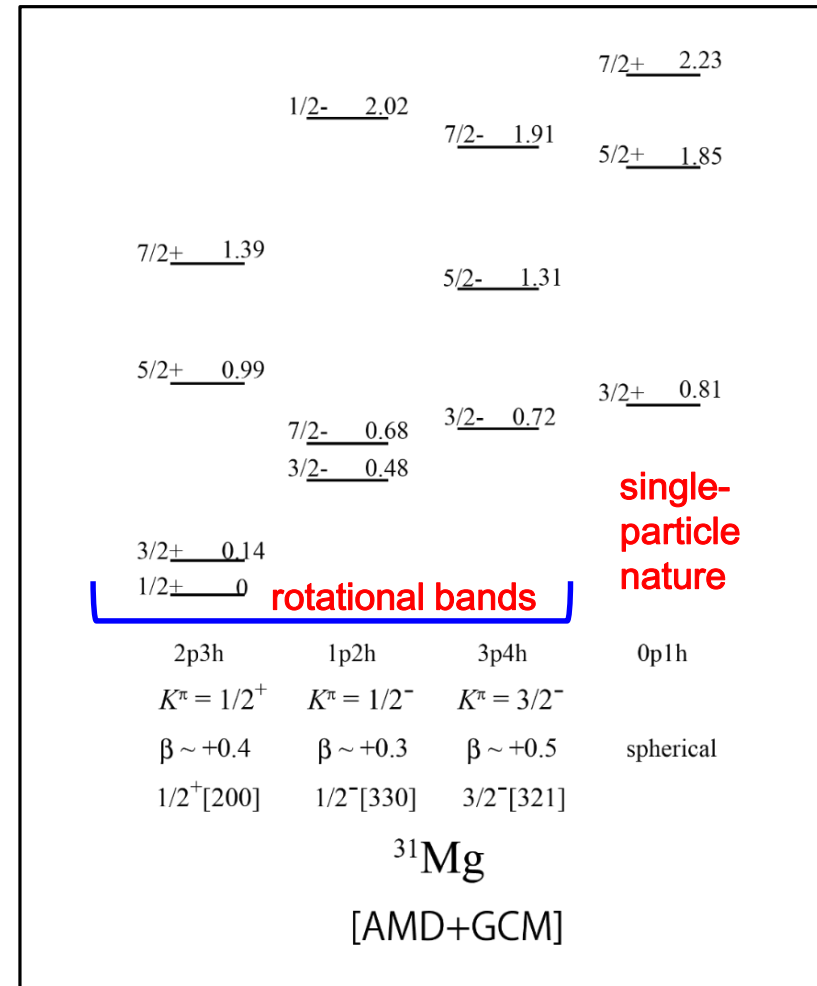
predicted by anti-symmetrized molecular dynamics
plus generator coordinate method (AMD+GCM)

With assuming **neither deformation** nor **mean field**, this theory predicts both **collective structures** and **single-particle structures** in low excitation energy region.

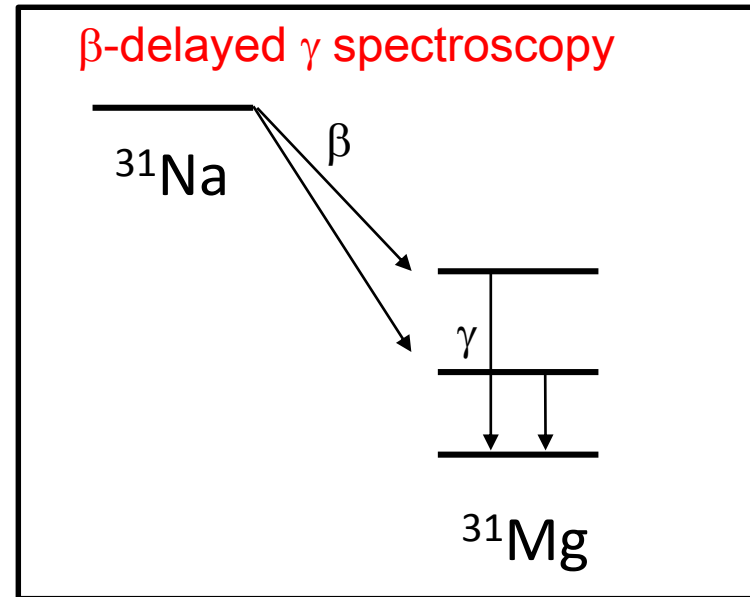
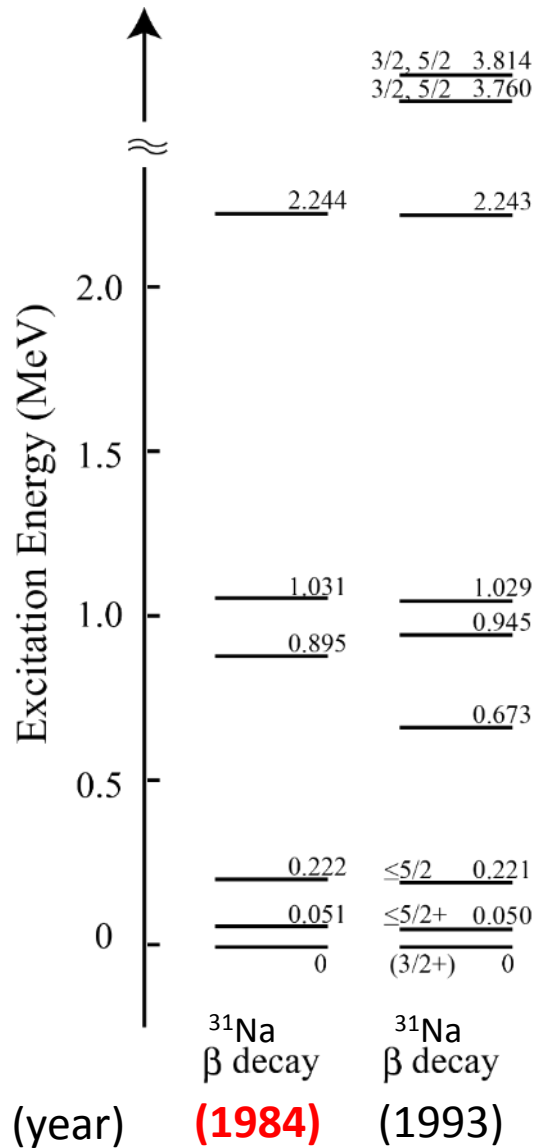
The **$1/2^+$ ground state** is
successfully predicted.

shape coexistence in ^{31}Mg

M. Kimura,
Phys. Rev. C 75(2007)041303(R)



Discovery history of ^{31}Mg levels

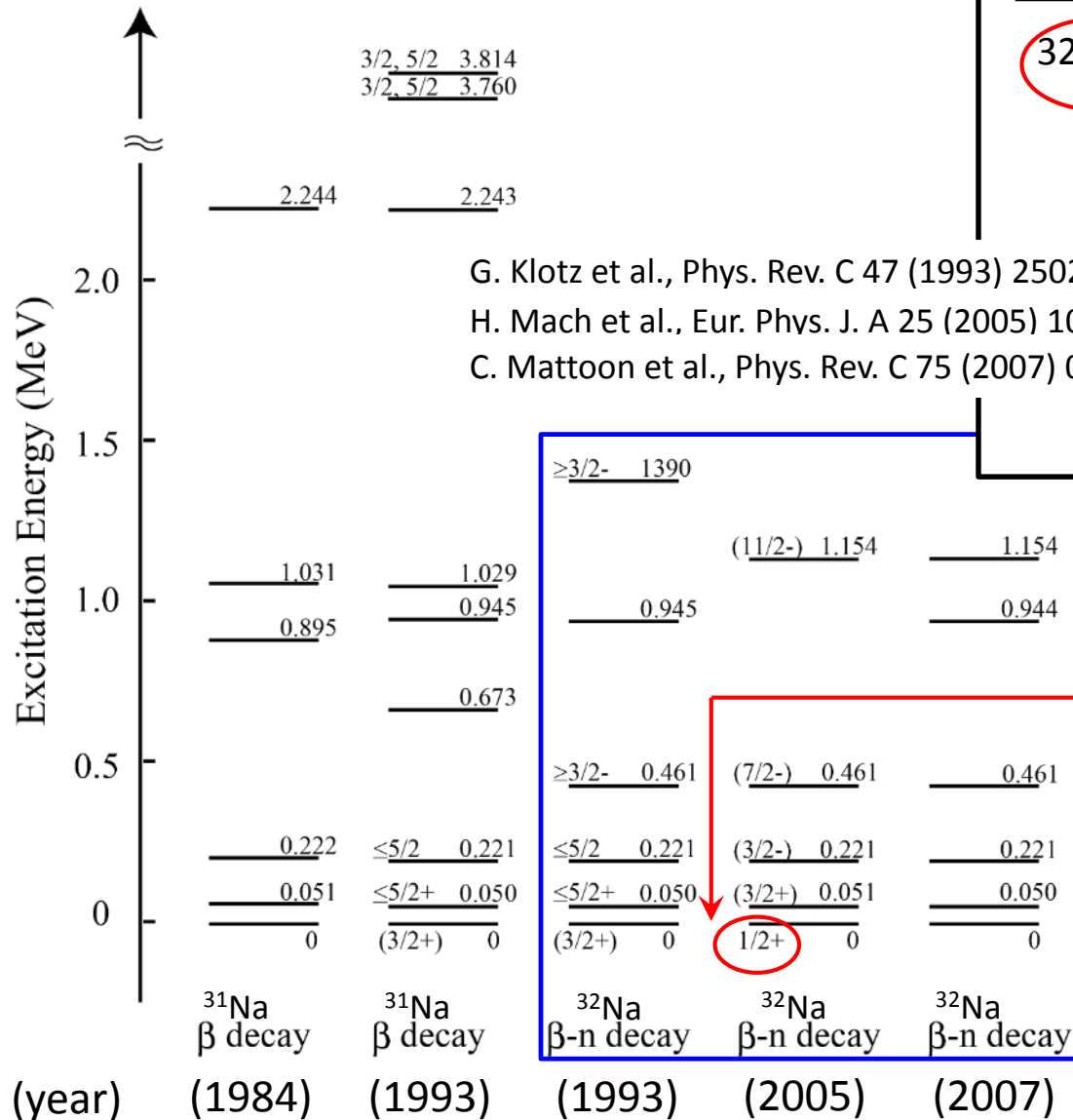


no spin-parity assignments

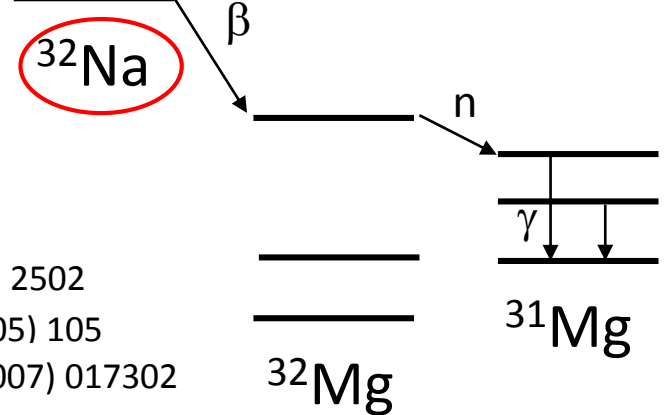
D. Guillemaud-Mueller et al., Nucl. Phys. A426 (1984) 37

G. Klotz et al., Phys. Rev. C 47 (1993) 2502

Discovery history of ^{31}Mg levels



β -delayed n- γ spectroscopy

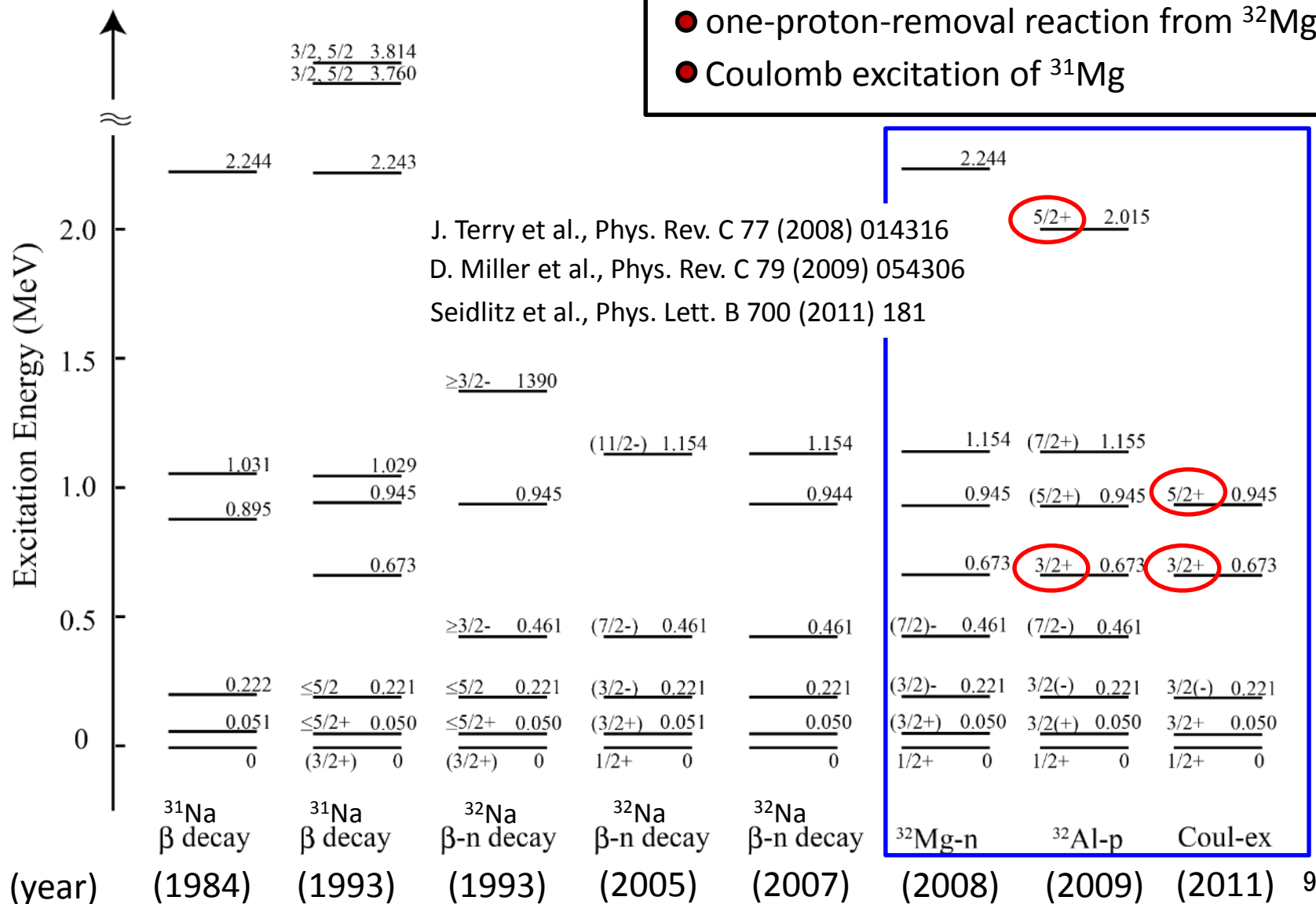


Unexpected spin-parity $1/2+$ was determined in 2005 by combined measurements of hyperfine-structure and β -NMR.

G. Neyens et al,
Phys. Rev. Lett. 94 (2005) 022501

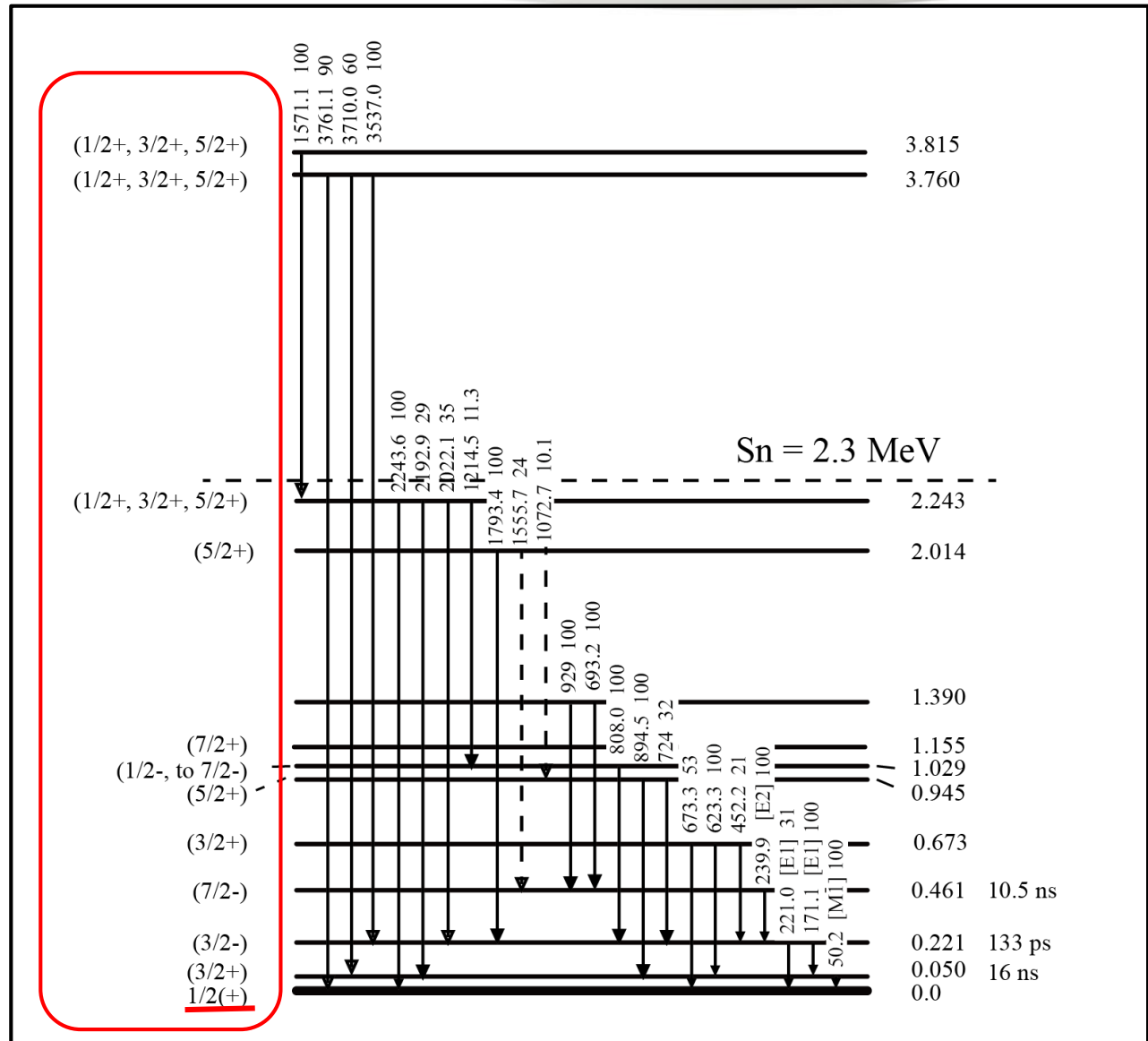
Discovery history of ^{31}Mg levels

- one-neutron-removal reaction from ^{32}Al
- one-proton-removal reaction from ^{32}Mg
- Coulomb excitation of ^{31}Mg



Adopted levels in ^{31}Mg by NNDC (updated in 2013)

Most of the spins and parities are unassigned, except for the $1/2^+$ ground state.



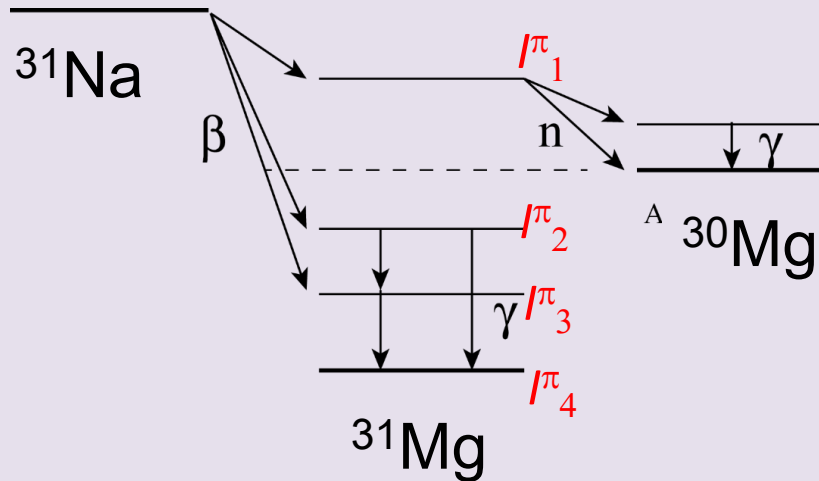
Firm spin-parity assignments are essential to understand the structure of ^{31}Mg .

Our method uses spin-polarized ^{31}Na to unambiguously assign the spins and parities of the levels in ^{31}Mg .

Principle of the measurement and Experiment

How to assign spin-parity of ^{31}Mg states

polarized



angular distribution of β -rays
from polarized nucleus

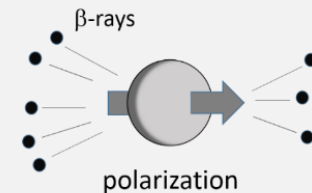
allowed transition

$$W(\theta) \cong 1 + AP\cos\theta$$

A : asymmetry parameter of β -decay

P : spin polarization of parent nucleus

θ : emission angle of β -rays with
respect to polarization axis



in the case

$$A=-1, P=0.5 \Rightarrow W(180^\circ) / W(0^\circ) = 3$$

Asymmetry parameter A

The asymmetry parameter A is a constant depending on the daughter state spin value.

allowed transition

$$A(I_i, I_f) \begin{cases} = \frac{I_i}{I_i + 1} & (\text{for } I_f = I_i + 1) \\ \simeq \frac{-1}{I_i + 1} & (\text{for } I_f = I_i) \\ = -1 & (\text{for } I_f = I_i - 1) \end{cases}$$

I_i : the parent spin

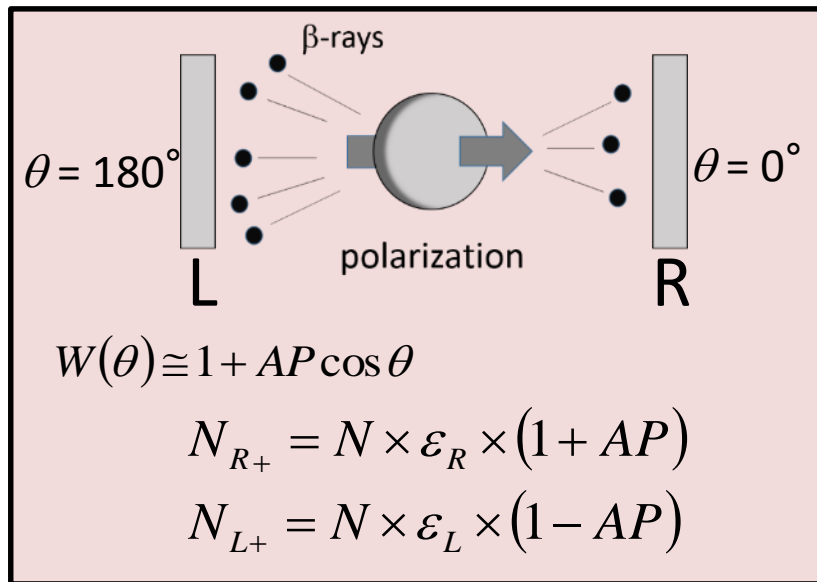
I_f : the daughter state spin

very discrete values

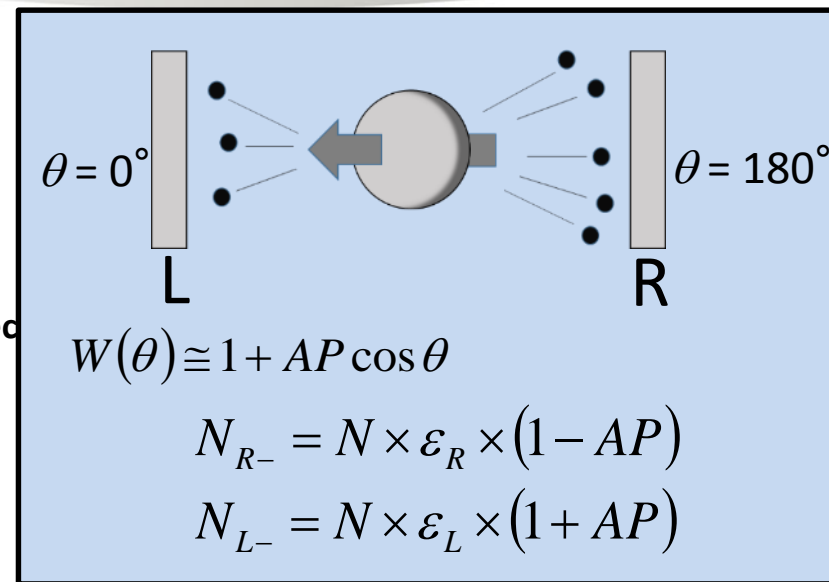
I_i^π (³¹ Na)	I_f^π (³¹ Mg)	A
	5/2+	+0.6
3/2+	3/2+	-0.4
	1/2+	-1.0

experimental A  spin of ³¹Mg state
parity = + for allowed transitions

How to measure asymmetry parameter A



spin flip
every 100sec



ε : efficiency N : Total β decay counts

AP -values are measured **freely from instrumental asymmetry**.

$$AP = \frac{\sqrt{R}-1}{\sqrt{R}+1} \quad \left(R = \frac{N_{L+}/N_{R+}}{N_{L-}/N_{R-}} \right)$$

P is common for all β -transitions
and can be determined by comparing two transitions.

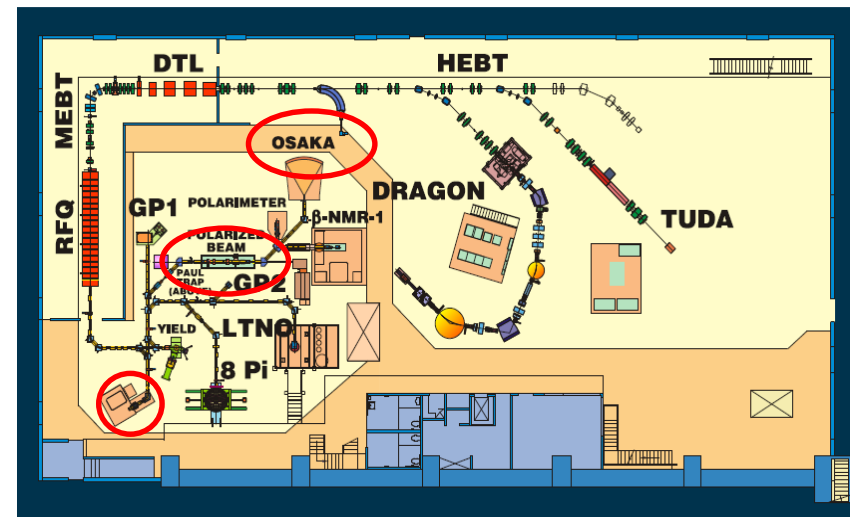
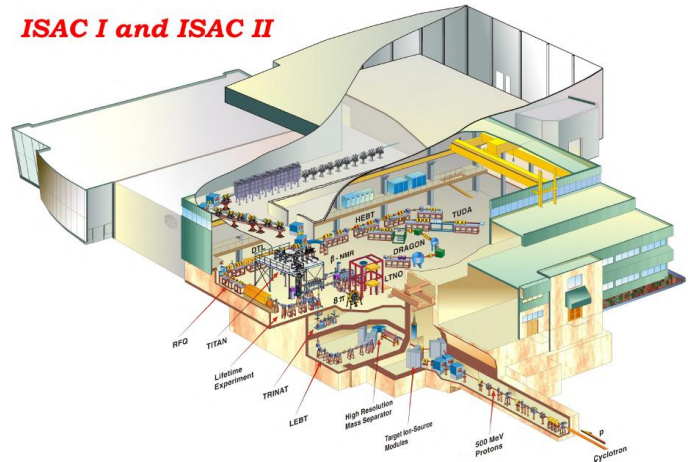
Polarized ^{31}Na beam at TRIUMF in Canada

Target fragmentation:

500 MeV $10\ \mu\text{A}$ proton beam
with UCx target

$^{31}\text{Na}^+$ ion beam intensity:

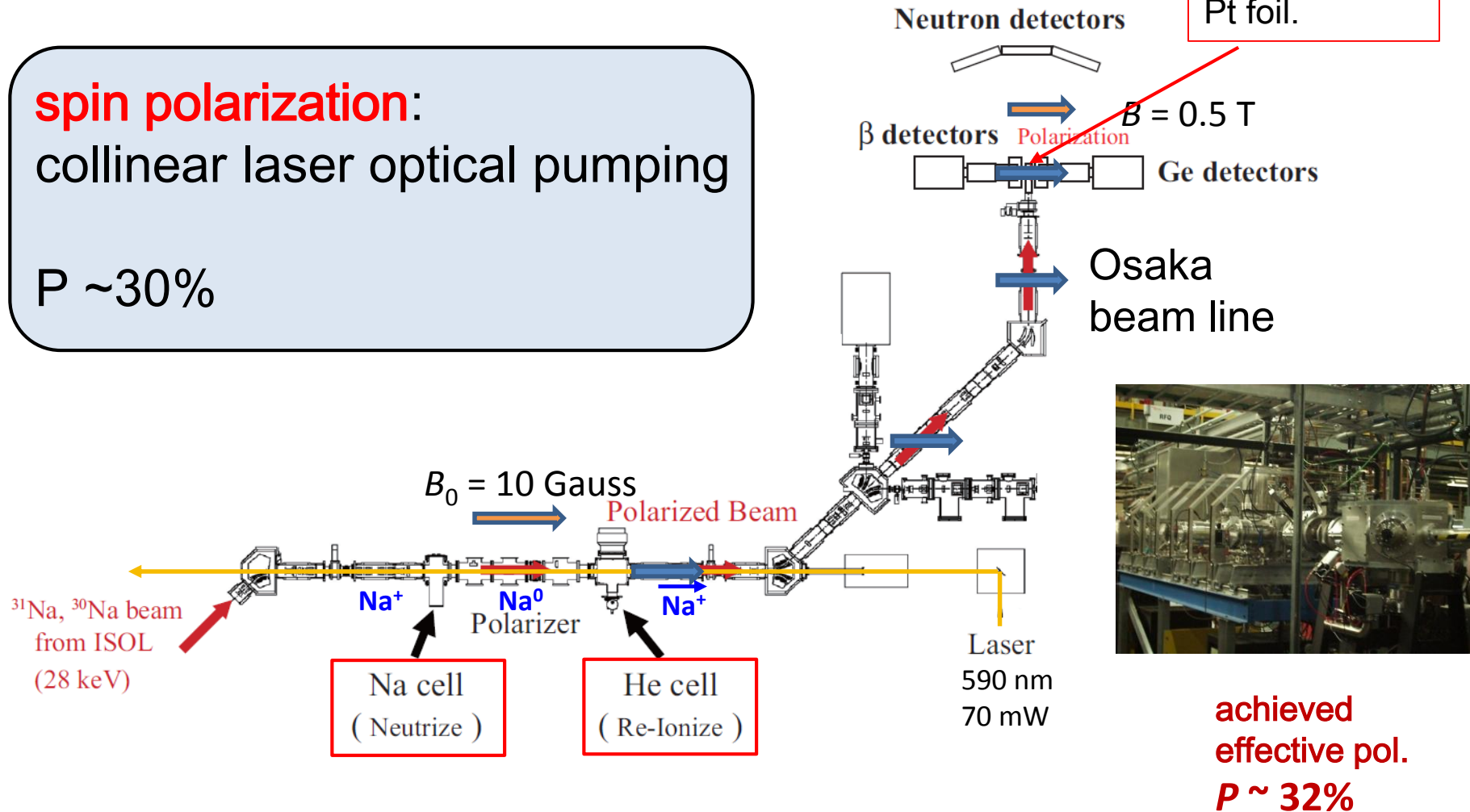
~ 800 pps (extracted), 28keV
 ~ 200 pps (after polarizer)



Polarizer at ISAC TRIUMF

spin polarization:
collinear laser optical pumping

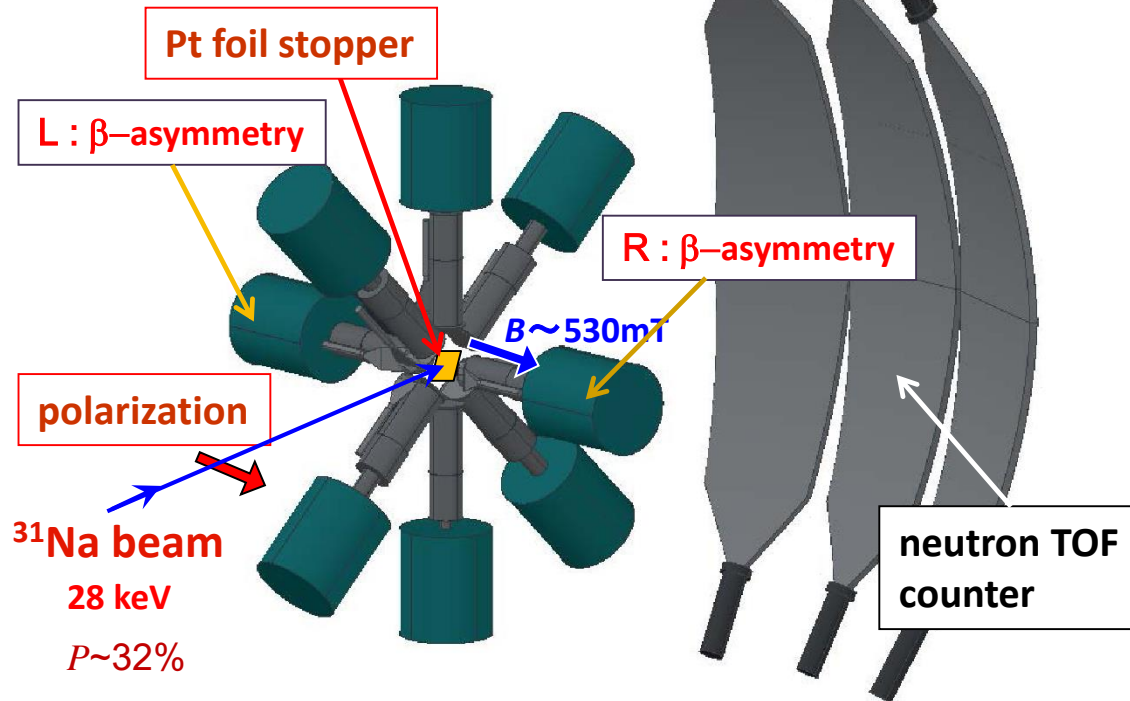
$P \sim 30\%$



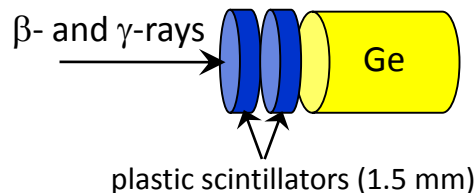
achieved
effective pol.
 $P \sim 32\%$

Detector Setup

β -asymmetry: β - γ , β - γ - γ , β -n
coincidence: γ - γ , n- γ

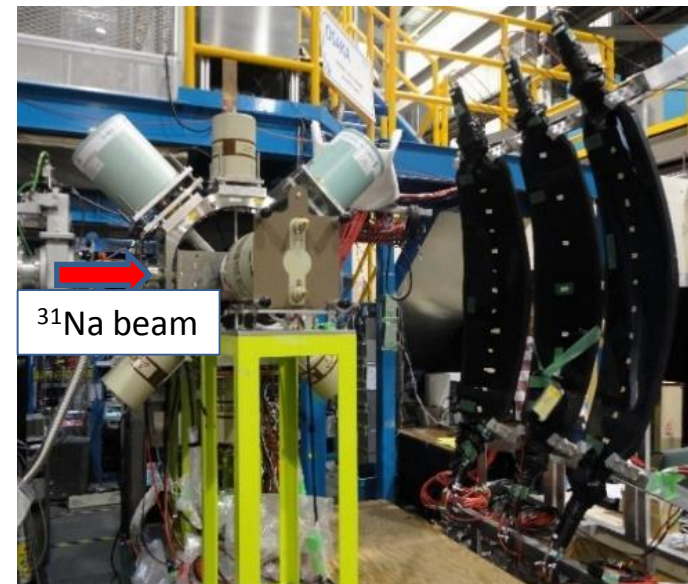


β , γ identification and β -ray energy measurement



8 x (HPGe + 2 plastic)
3 neutron TOF counters

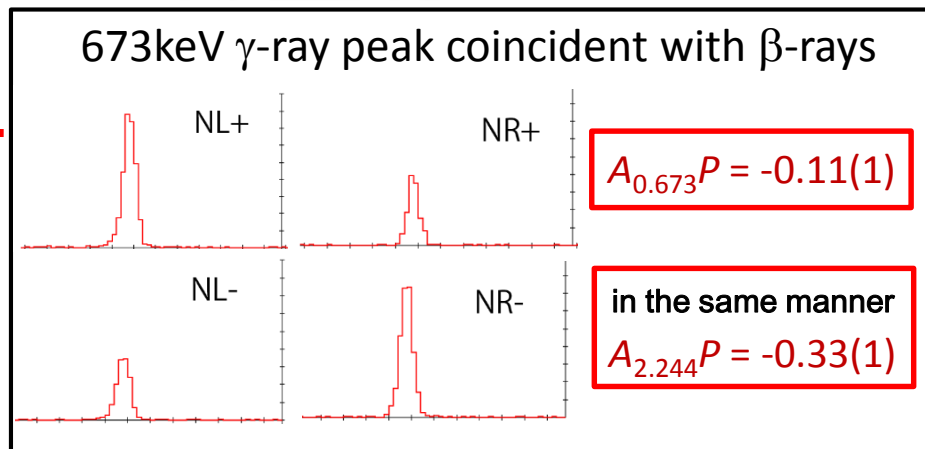
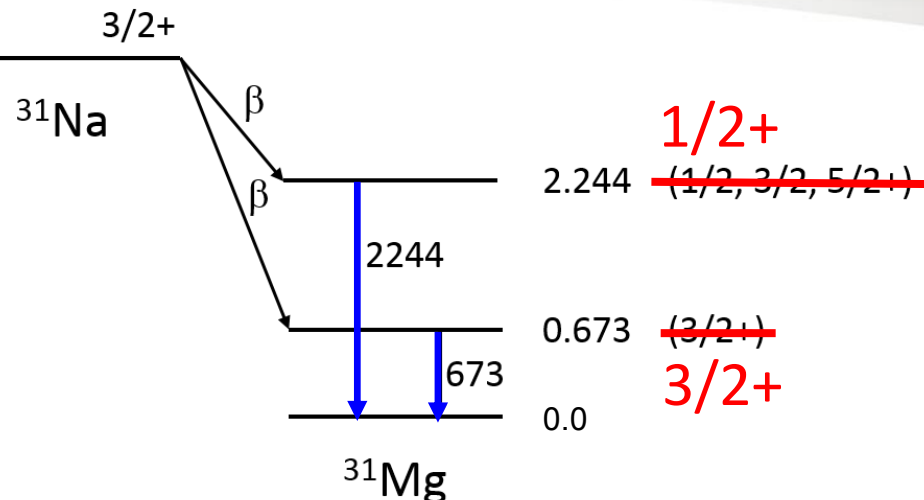
β -detection efficiency: 15%
 γ -detection efficiency: 2.9% @1333keV
n-detection efficiency: 0.2% @2MeV



Experimental Results

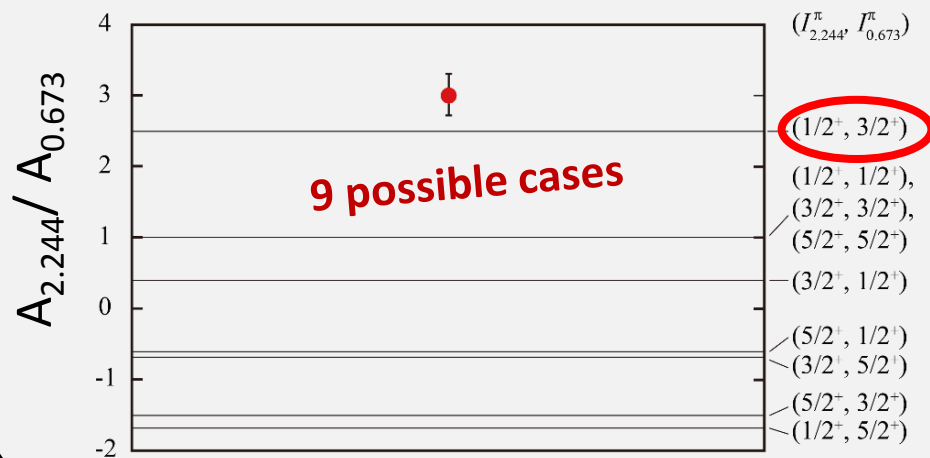
β - γ measurement: $^{31}\text{Na} \rightarrow ^{31}\text{Mg}$

Determination of polarization P



ratio of two AP values to cancel out P

$$(A_{2.244}P) / (A_{0.673}P) = A_{2.244} / A_{0.673} = 3.0(3)$$



$$I_{0.673}^{\pi} = 3/2^+ \Rightarrow A_{0.673} = -0.4$$

$$I_{2.244}^{\pi} = 1/2^+ \Rightarrow A_{2.244} = -1.0$$

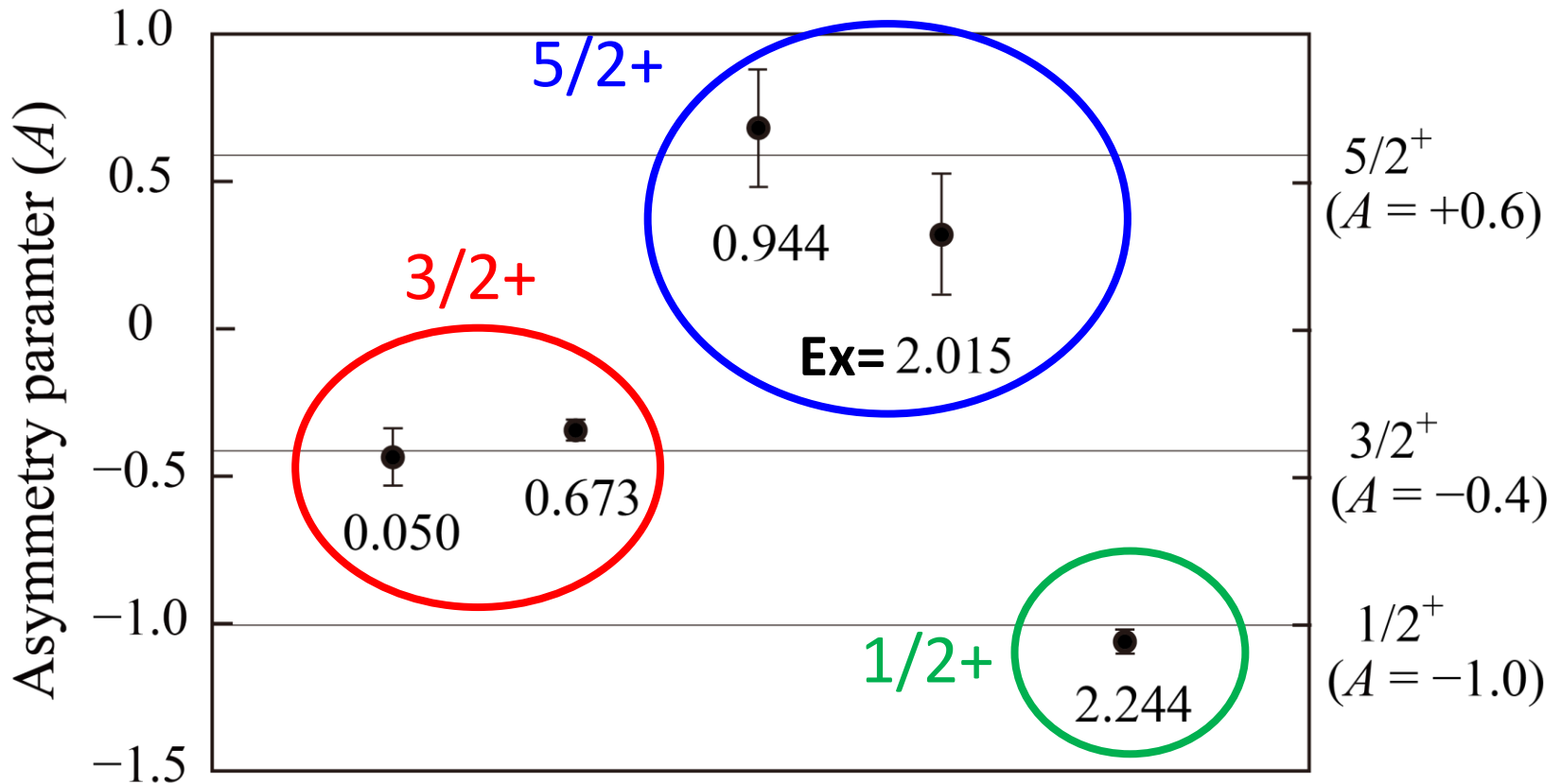
$$A_{0.673}P = -0.11(1) \Rightarrow P = 28(3) \%$$

$$A_{2.244}P = -0.33(1) \Rightarrow P = 33(1) \%$$

$$P = 32(1)\%$$

Spin-parity assignments of ^{31}Mg levels

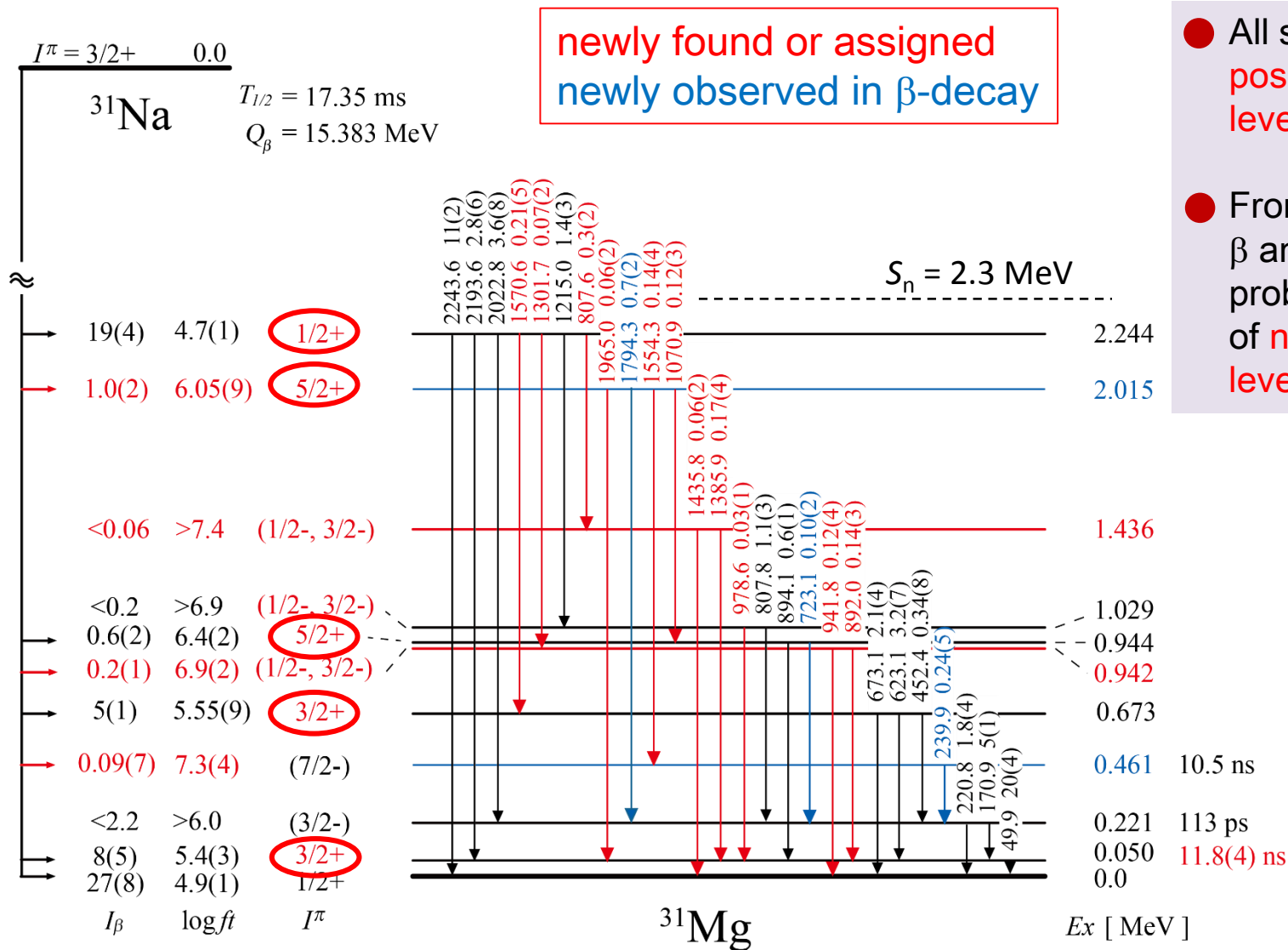
experimental AP values and polarization $P = 32(1)\%$ ➡ **A**



5 levels are firmly assigned!

The 50 keV level was assigned as $3/2^+$ for the first time.

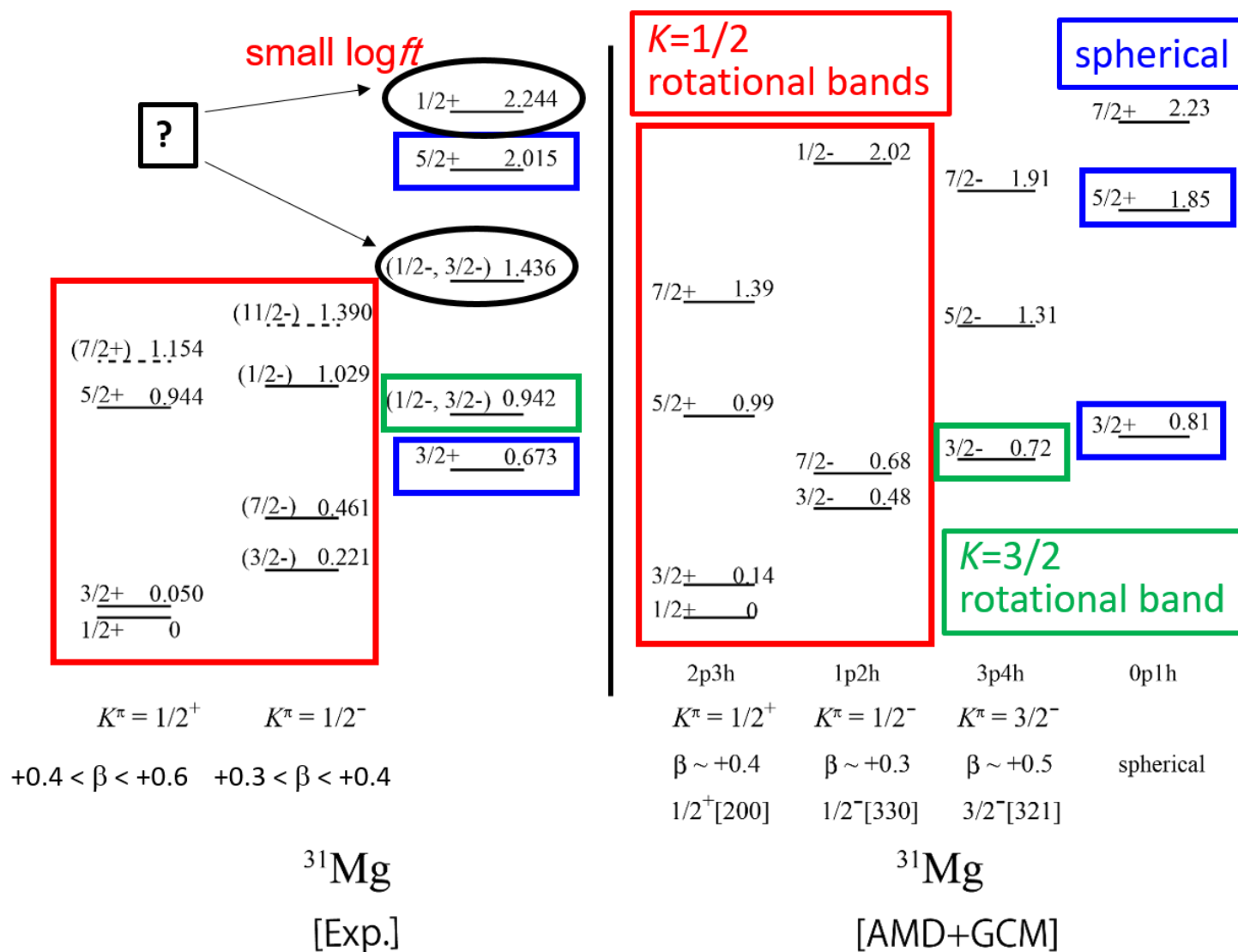
Decay scheme of $^{31}\text{Na} \rightarrow ^{31}\text{Mg}$



- All spins of the **positive-parity levels** are assigned.
- From the detailed β and γ transition probabilities, spins of **negative parity-levels** are proposed.

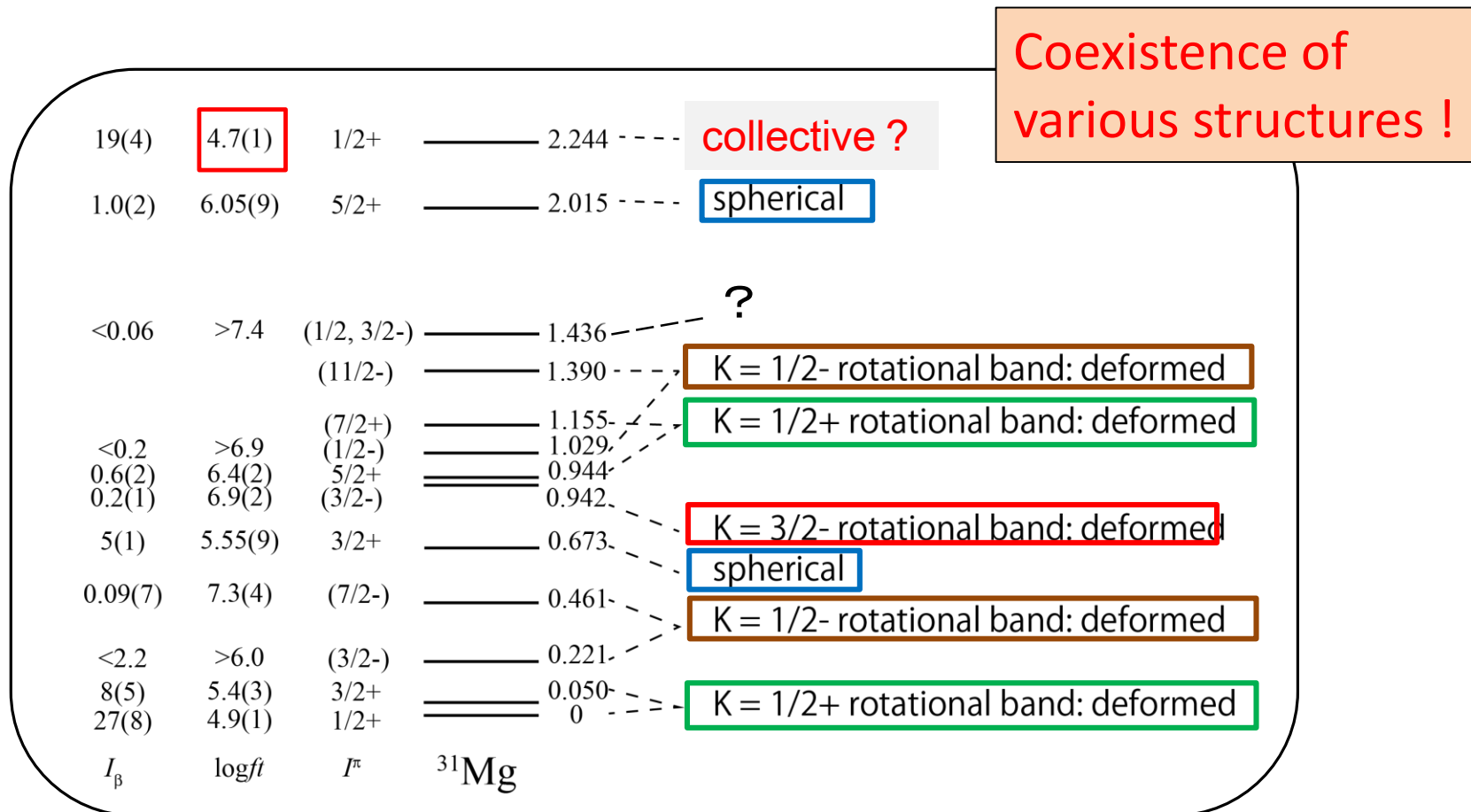
Comparison with predictions
by Antisymmetrized Molecular Dynamics
(AMD+GCM) theory

Comparison of energy levels



Summary

- We confirmed three types of rotational bands and spherical states.
- This is the experimental evidence of the coexistence of various structures.



Collaborators of TRIUMF experiment S1391 (Aug. 2014)

Osaka University, Japan

H. Nishibata, T. Shimoda, A. Odahara, S. Morimoto, S. Kanaya, Y. Yagi,
H. Kanaoka

TRIUMF, Canada

M. Pearson, C. D. P. Levy



Thank you for your attention.

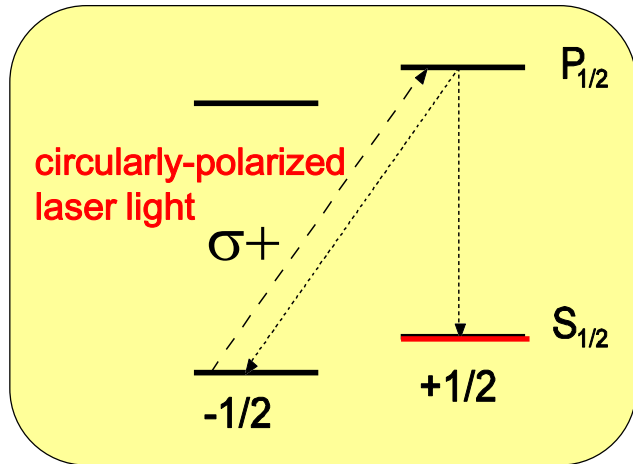
End of presentation

Optical Pumping

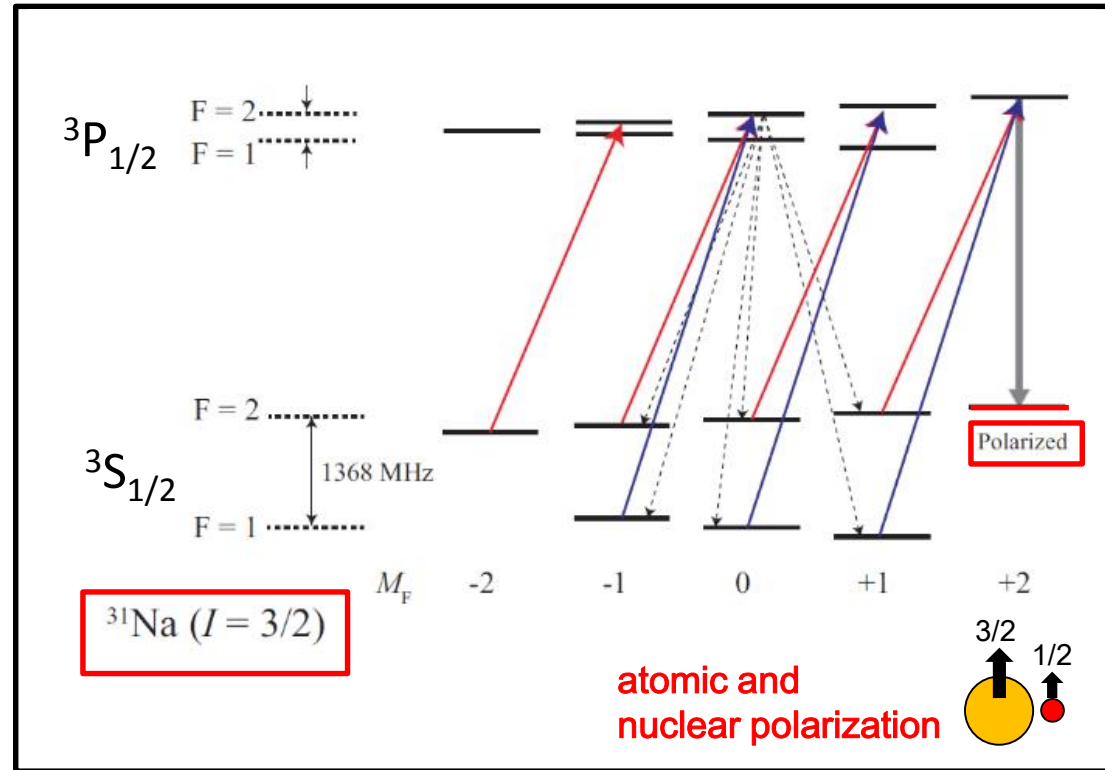
alkali atom

with hyperfine int.

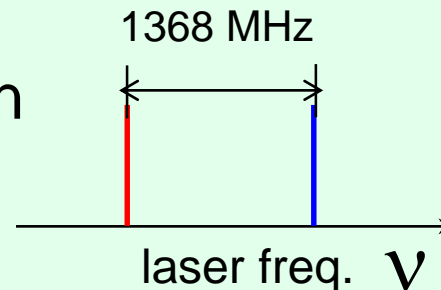
without hyperfine int.



atomic polarization

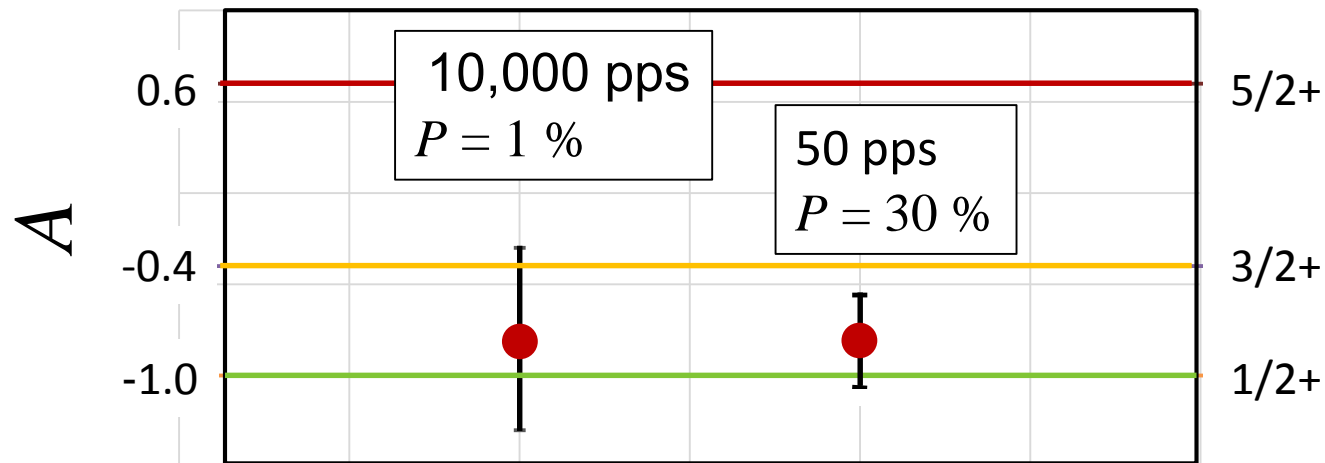


To achieve high polarization we need two laser beams.



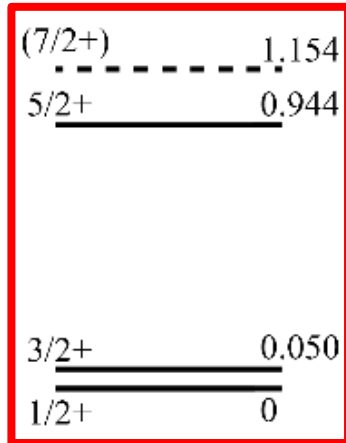
How to assign spin-parity of ^{31}Mg states

High polarization is essential for radioactive nuclear beams.

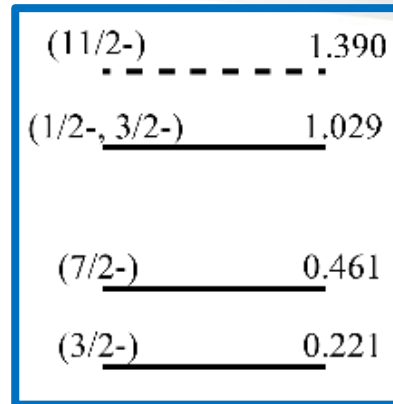


β -branch: 1%, γ -detection efficiency 1%, 24 hrs accumulation time

$K=1/2$ rotational bands in ^{31}Mg



Positive-parity states



Negative-parity states

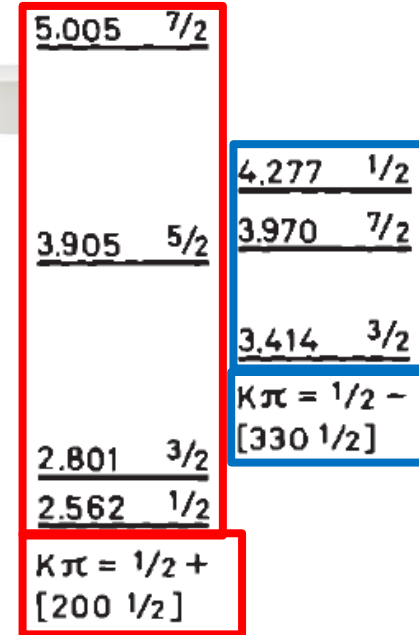
$$a = -0.8$$

$$K=1/2+$$

 ^{31}Mg

$$a = -4.4$$

$$K=1/2-$$

 ^{25}Mg

$$a = -0.8$$

$$K=1/2+$$

$$a = -3.5$$

$$K=1/2-$$

 a : decoupling parameter

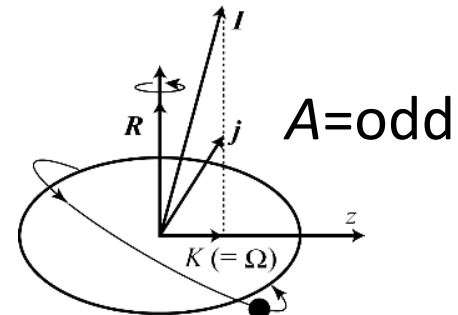
^{31}Mg $K=1/2$ rotational bands

Positive $1/2+[200]$

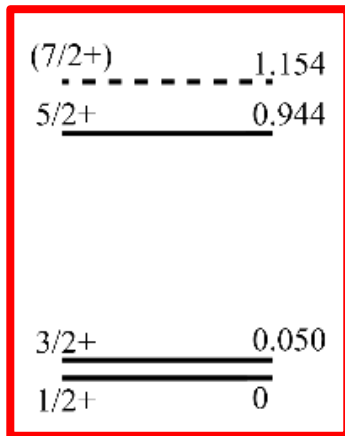
$$+0.4 < \beta < +0.6$$

Negative $1/2-[330]$

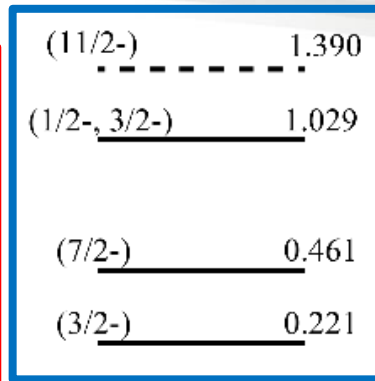
$$+0.3 < \beta < +0.4$$



$K=1/2$ rotational bands in ^{31}Mg



Positive-parity states



Negative-parity states

^{31}Mg

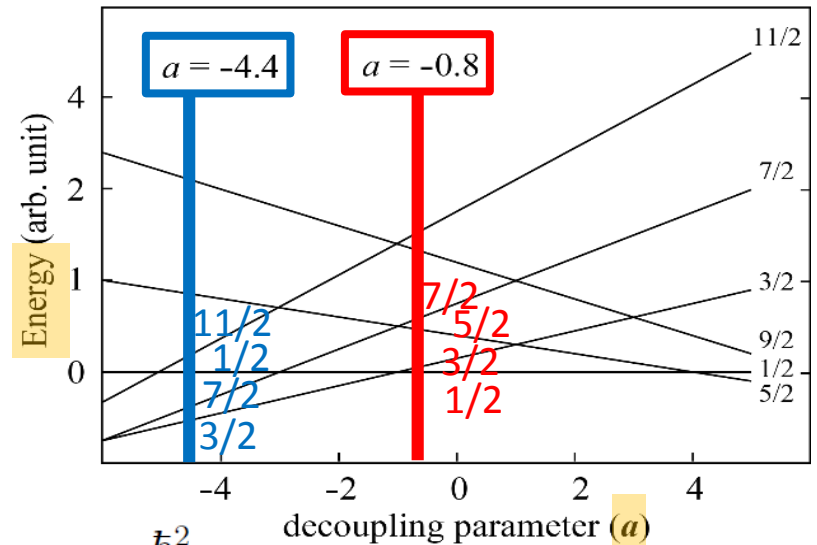
$a = -0.8$

$a = -4.4$

Decoupling parameter a depends on the orbit occupied by the unpaired nucleon.



Configuration could be estimated from the $K=1/2$ rotational band observed in ^{25}Mg .



$$E(I) = \frac{\hbar^2}{2\mathcal{J}} [I(I+1) + a(-1)^{I+1/2}(I+1/2)]$$

a : decoupling parameter

from the ordering of spins and energy difference between states

rotational motion in odd-A nuclei

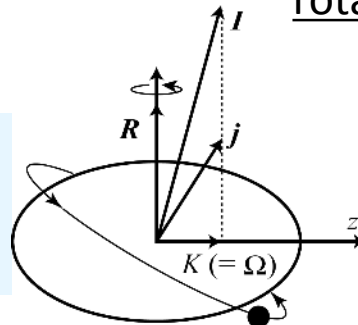
z : symmetry axis

j : particle angular momentum

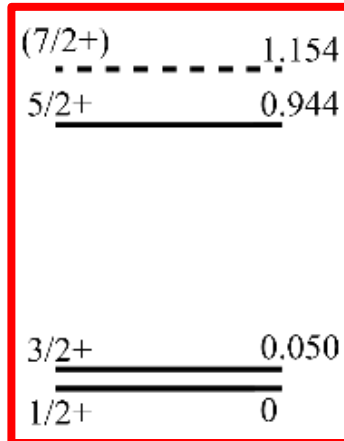
R : rotational angular momentum

K : projection of the total angular momentum on the symmetry axis

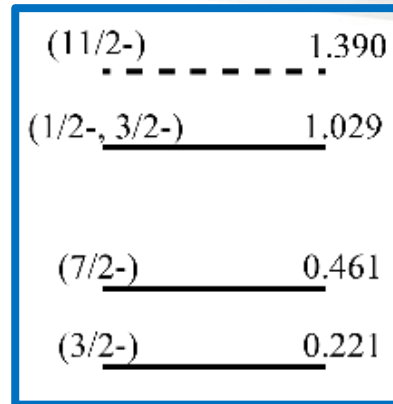
I : total angular momentum



$K=1/2$ rotational bands in ^{31}Mg



Positive-parity states



Negative-parity states

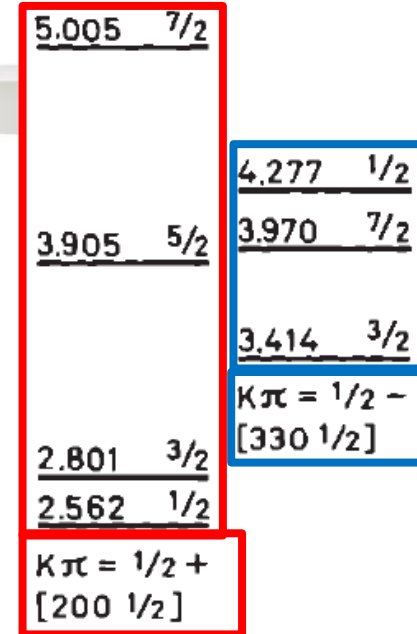
$$a = -0.8$$

$$K=1/2^+$$

 ^{31}Mg

$$a = -4.4$$

$$K=1/2^-$$

 ^{25}Mg

$$a = -0.8$$

$$K=1/2^+$$

$$a = -3.5$$

$$K=1/2^-$$

Values of decoupling parameter a
 Is in good agreement with each other.

K^π : projection of the total angular momentum on the symmetry axis

N : principal quantum number

n_z : number of nodes in the wave function in the z direction

Λ : projection of the orbital angular momentum on the symmetry axis

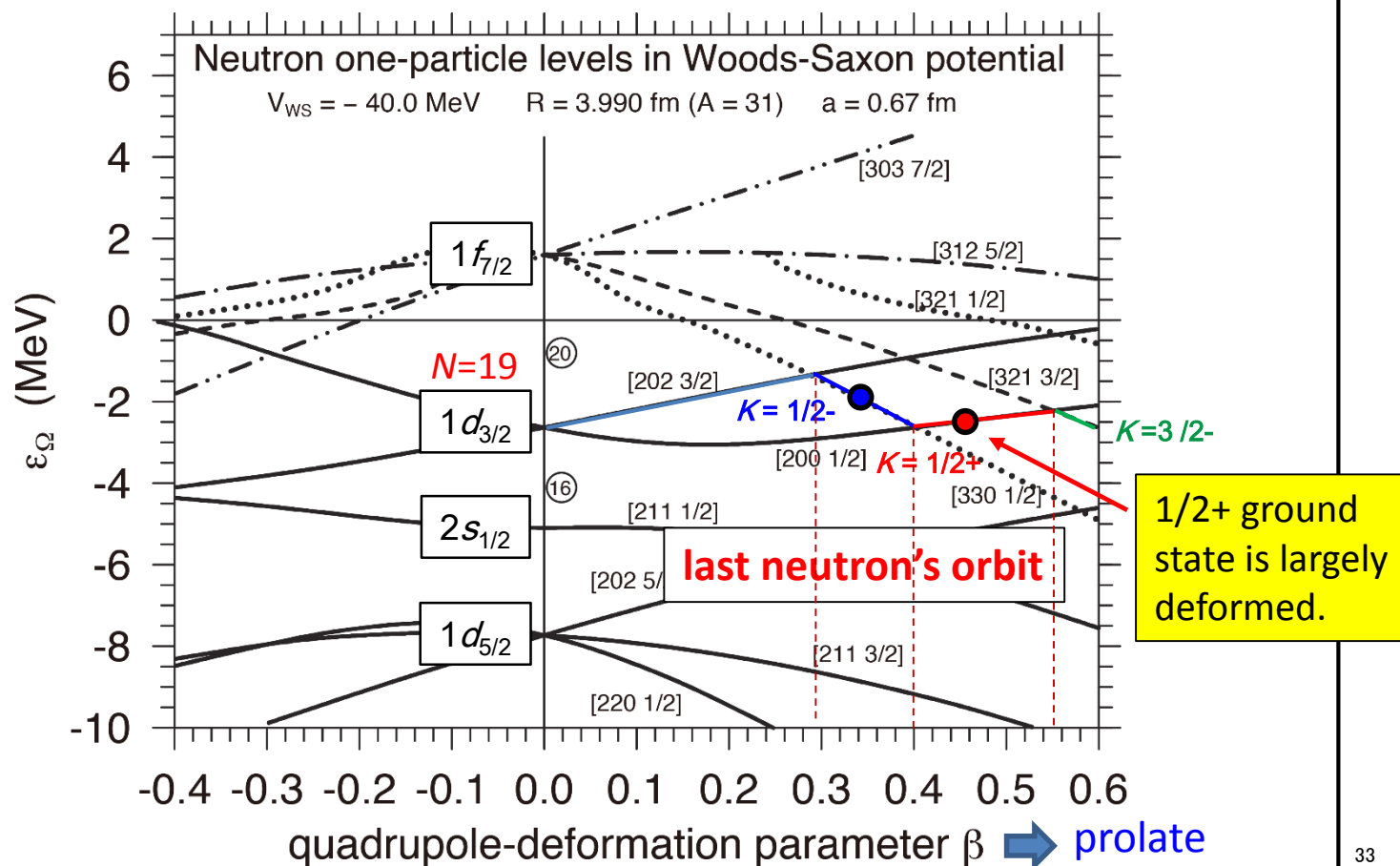
^{31}Mg $K=1/2$ rotational band
 Positive $1/2^+[200]$
 Negative $1/2^-[330]$

$$K^\pi[Nn_z\Lambda]$$

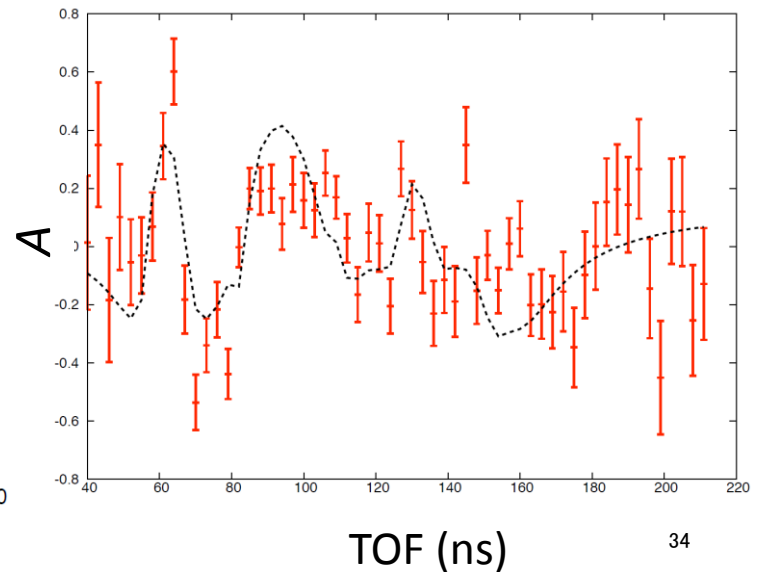
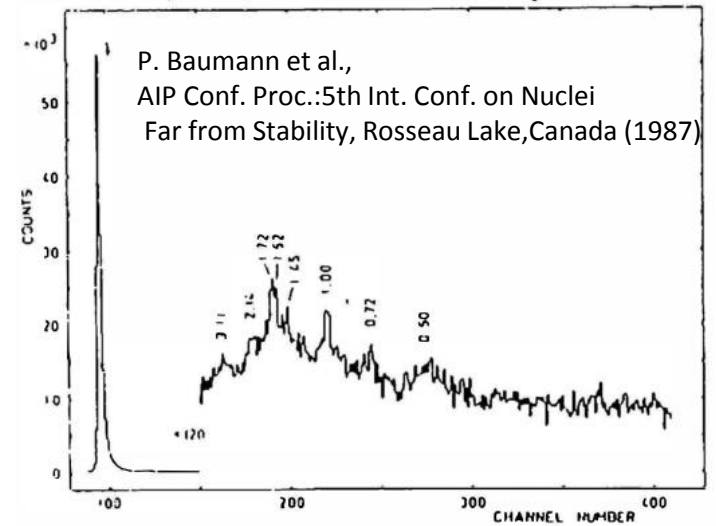
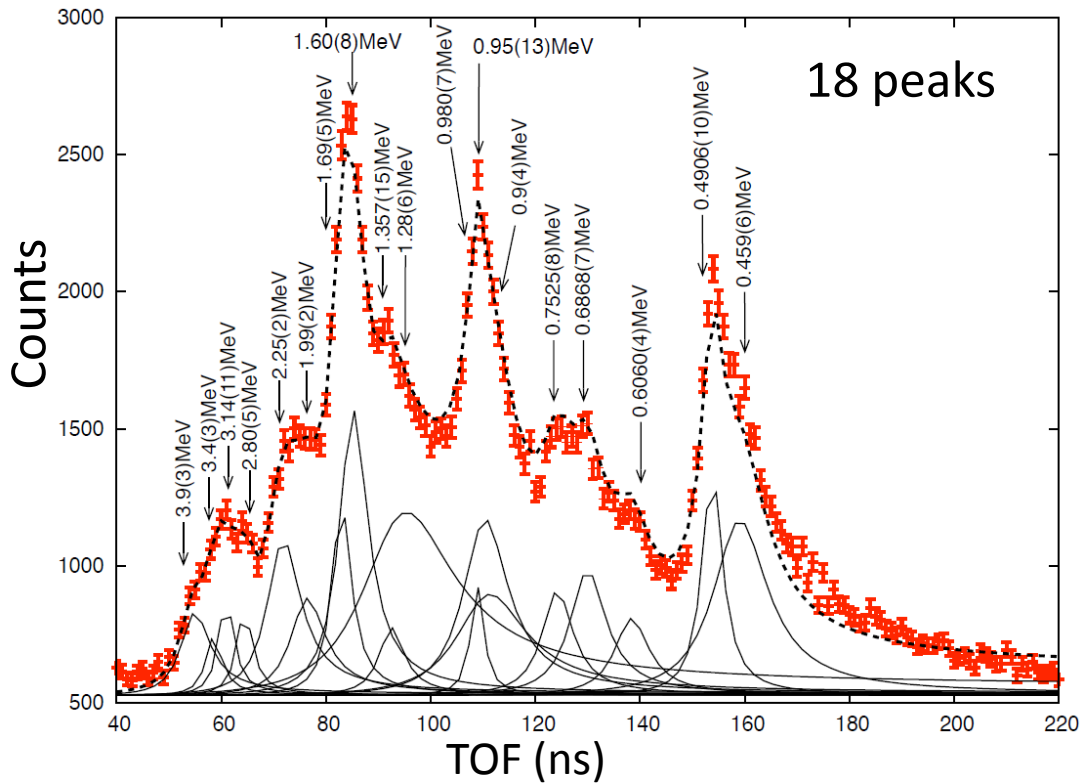
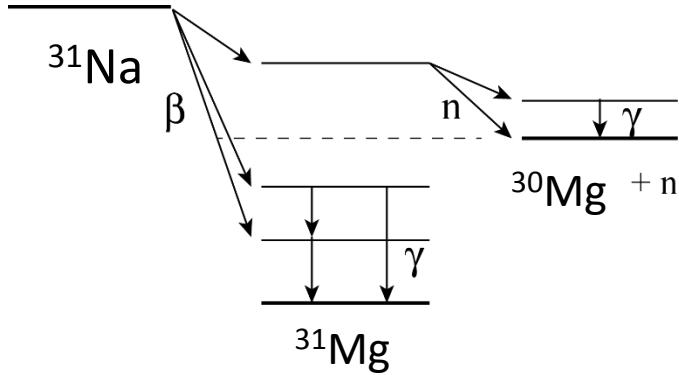
Nilsson diagrams for ^{31}Mg

Ikuko Hamamoto, Phys. Rev. C **76** (2007) 054319

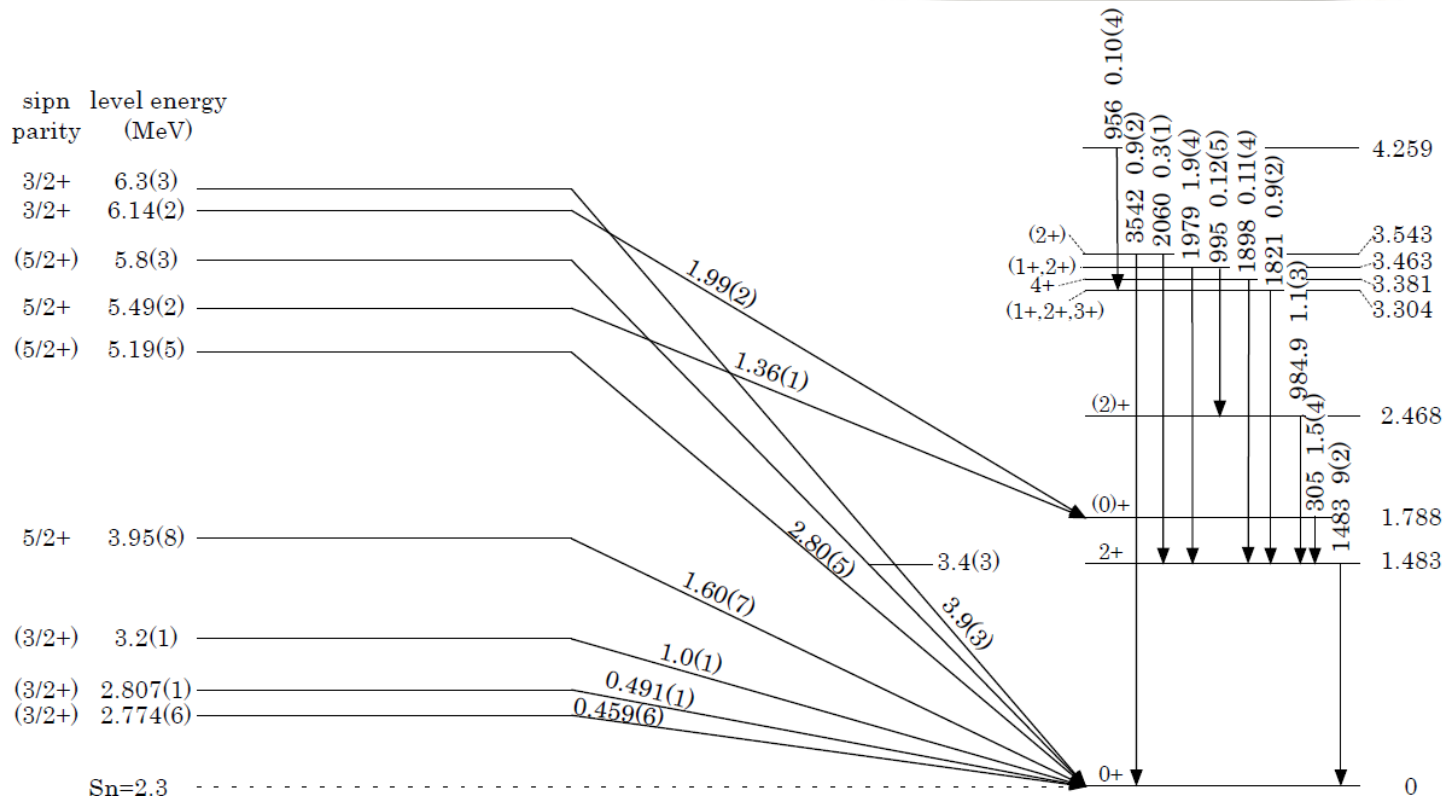
neutron one-particle levels in ^{31}Mg



β -delayed neutrons



levels above S_n



tentatively proposed

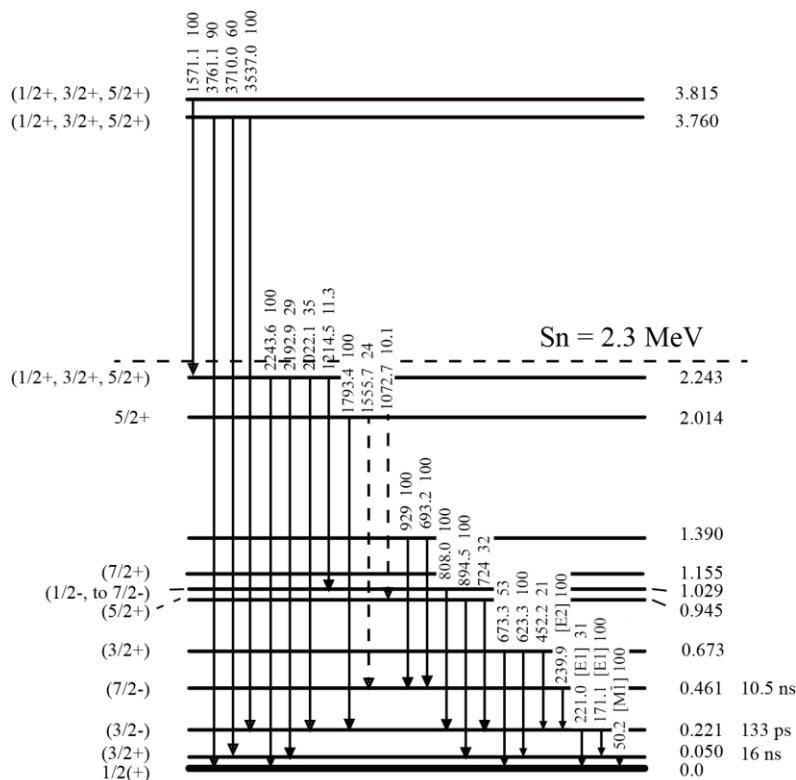
g.s. —————

^{31}Mg

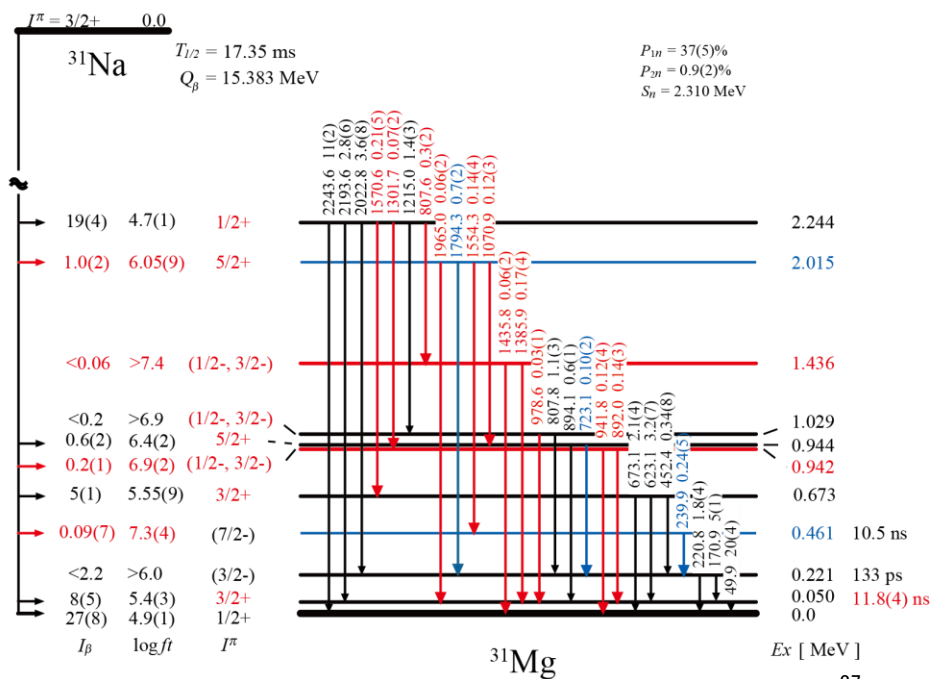
Analysis in progress

How is the level scheme of ^{31}Mg revised?

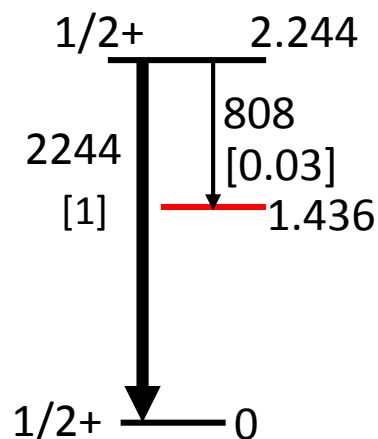
NNDC in 2013



Present work
(TRIUMF experiment S1391 in 2014)



spin-parity assignment of the levels at 1.436 and 0.942 MeV

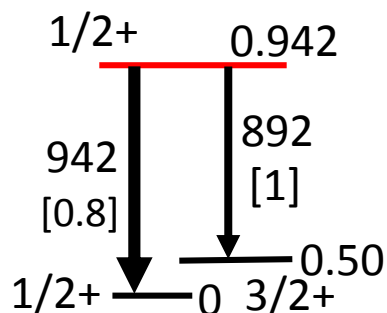


(1) 1.436-MeV level

E_γ (keV)	$E_i \rightarrow E_f$ (MeV)	I_{exp} (relative)	$I^\pi(1.436 \text{ MeV})$	$\sigma\lambda$	$T_{W.e.} (\sigma\lambda)$ (s)	$I_{W.e.}$ (relative)
2244	2.244 \rightarrow g.s.	1		<u>M1</u>	<u>2.0×10^{-15}</u>	<u>1</u>
808	2.244 \rightarrow 1.436	0.03(2)	7/2 ⁻	E3	9.4×10^{-5}	2.1×10^{-11}
			5/2 ⁻	M2	9.1×10^{-9}	2.1×10^{-7}
			<u>1/2⁻, 3/2⁻</u>	<u>E1</u>	<u>1.3×10^{-15}</u>	<u>6.7×10^{-1}</u>

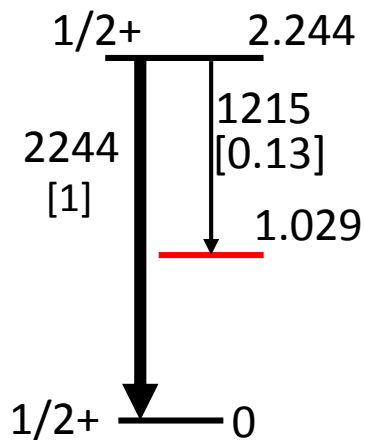
hindrance factor of E1 : $\sim 10^{-2}$ from 2.244 \rightarrow 0.221 MeV
(1/2+) (3/2-)

(2) 0.942-MeV level



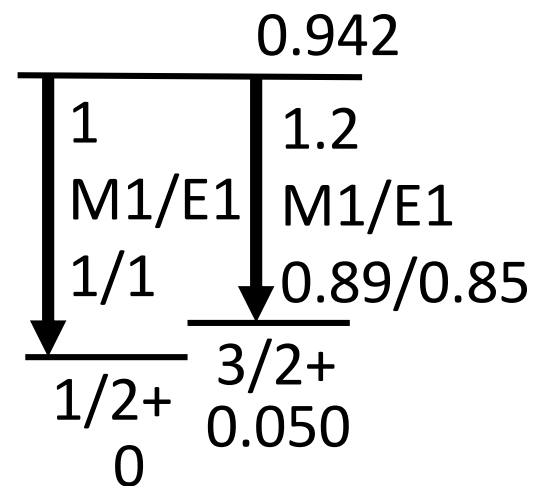
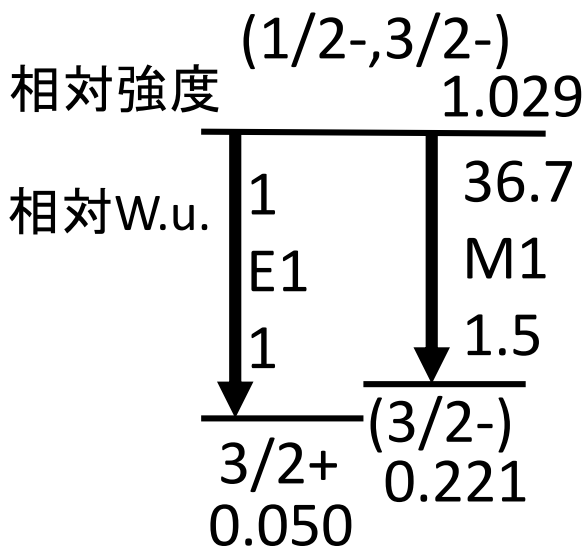
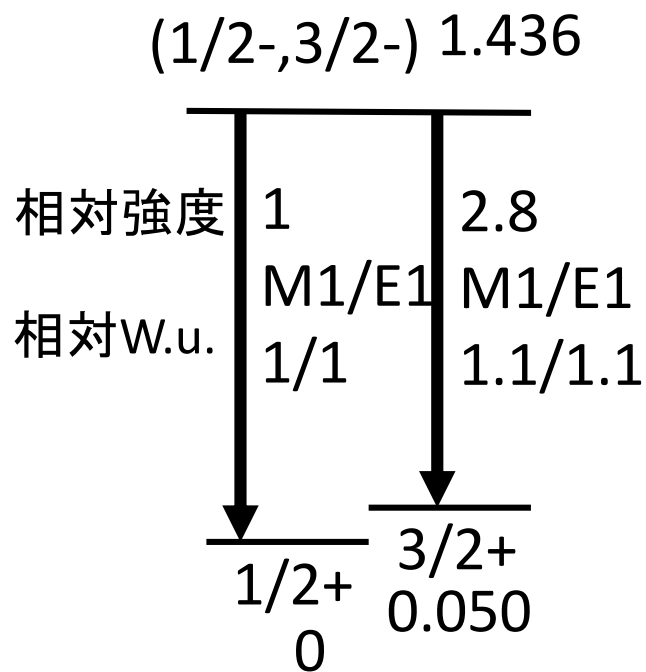
E_γ (keV)	$E_i \rightarrow E_f$ (MeV)	I_{exp} (relative)	$I^\pi(0.942 \text{ MeV})$	$\sigma\lambda$	$T_{W.e.} (\sigma\lambda)$ (s)	$I_{W.e.}$ (relative)
892	0.942 \rightarrow 0.50	1	7/2 ⁻	M2	5.6×10^{-9}	1
942	0.942 \rightarrow g.s.	0.8(3)	7/2 ⁻	E3	3.2×10^{-5}	1.9×10^{-4}
892	0.942 \rightarrow 0.50	1	<u>1/2⁻, 3/2⁻, 5/2⁻</u>	<u>E1</u>	<u>9.7×10^{-16}</u>	<u>1</u>
942	0.942 \rightarrow g.s.	0.8(3)	5/2 ⁻	M2	3.4×10^{-6}	2.9×10^{-10}
			<u>1/2⁻, 3/2⁻</u>	<u>E1</u>	<u>8.2×10^{-16}</u>	<u>1.2×10^0</u>

spin-parity assignment of the level at 1.029 MeV

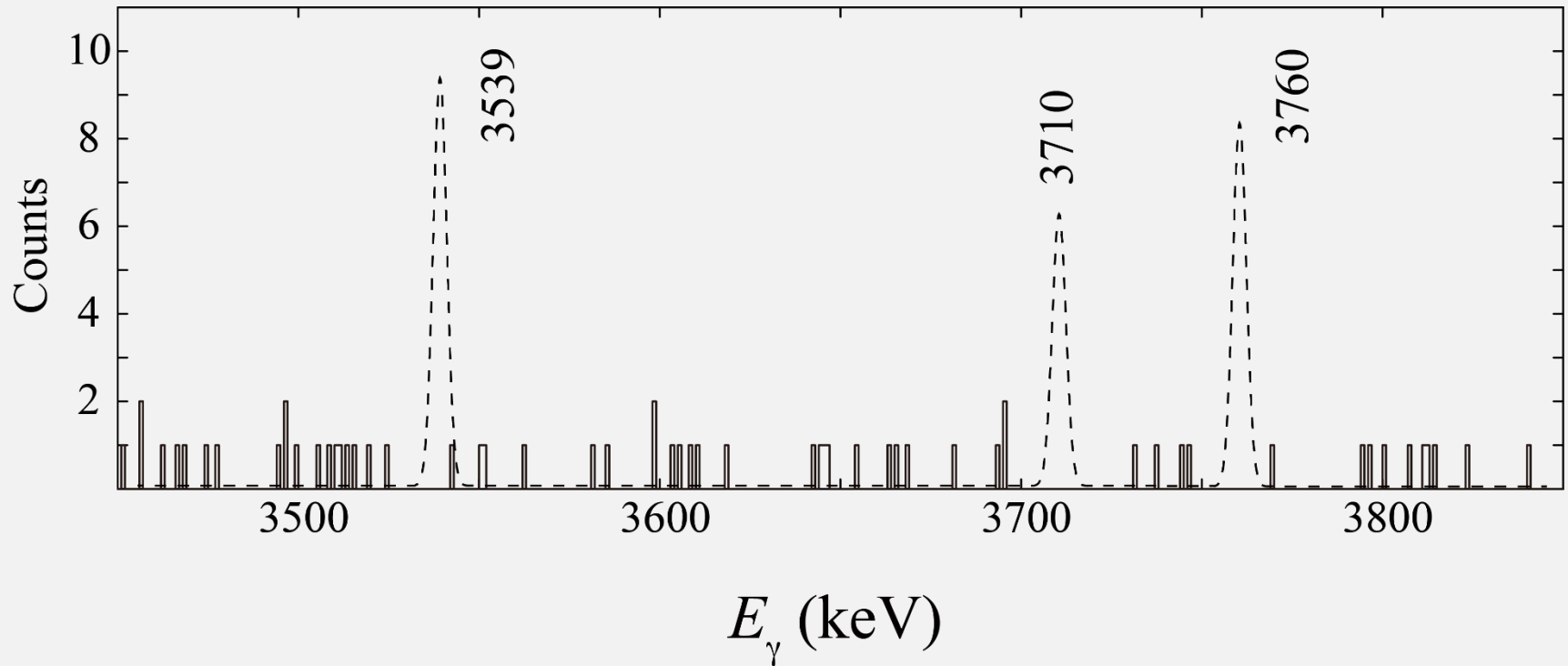


E_γ (keV)	$E_i \rightarrow E_f$ (MeV)	I_{exp} (relative)	$I^\pi(1.436 \text{ MeV})$	$\sigma\lambda$	$T_{\text{W.e.}} (\sigma\lambda)$ (s)	$I_{\text{W.e.}}$ (relative)
2244	2.244 \rightarrow g.s.	1		<u>M1</u>	2.0×10^{-15}	<u>1</u>
1215	2.244 \rightarrow 1.029	0.13(3)	$7/2^-$	E3	5.4×10^{-6}	3.6×10^{-10}
			$5/2^-$	M2	1.2×10^{-9}	1.6×10^{-6}
			<u>$1/2^-, 3/2^-$</u>	<u>E1</u>	3.8×10^{-16}	5.1×10^0

hindrance factor of E1 : $\sim 10^{-2}$ from 2.244 \rightarrow 0.221 MeV
 (1/2+) (3/2-)



No such high-energy γ -rays were observed.

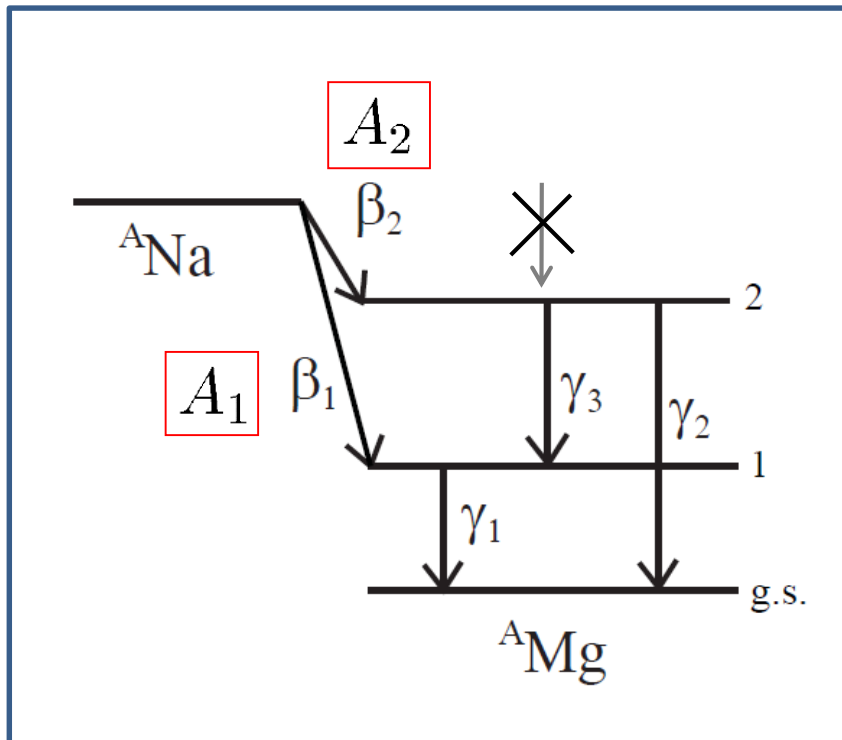


Enlarged β - γ coincidence spectrum for ^{31}Mg gated by β rays with more than 8 MeV indicated by solid line and the expected spectrum from the level scheme of Ref. [KLO93] shown in the dashed line.

Detection efficiency with β -gate is taken into account.

In the case of cascade feeding

Deduced A from β - γ coincidence is affected by the feeding from upper levels.



measured from β - γ_1 coincidence

$$A_1^\gamma = A_2 \times \frac{I_{\gamma_3}}{I_{\gamma_1}} + A_1 \times \frac{I_{\beta_1}}{I_{\gamma_1}},$$

known
unknown



$$A_1 = A_1^\gamma \times \frac{I_{\gamma_1}}{I_{\beta_1}} - A_2 \times \frac{I_{\gamma_3}}{I_{\beta_1}}.$$

Achieved polarization

Phil Levy @TRIUMF

^8Li : 80%, ^9Li : 56%, ^{11}Li : 55%,

^{20}Na : 57%, ^{21}Na : 56%, ^{26}Na : 55%,
 ^{27}Na : 51%, ^{28}Na : 45%,

Corrected for spin-relaxation
K. Minamisonno et al.,
Nucl. Phys. A746(2004)673c

^{28}Na : 28%, ^{29}Na : 36%,
 ^{30}Na : 31%, ^{31}Na : 32%

Uncorrected for spin-relaxation,
attenuation due to solid angle

Spin Relaxation

Pt $B_0 = 0.5 \text{ T}$

^{20}Na 22.0(19) s

^{26}Na 0.78(8) s

Korringa's relation

$$T_1 \times T \propto (Ih/\mu)^2$$

^{30}Na 600 ms 48 ms

^{31}Na 400 ms 17 ms

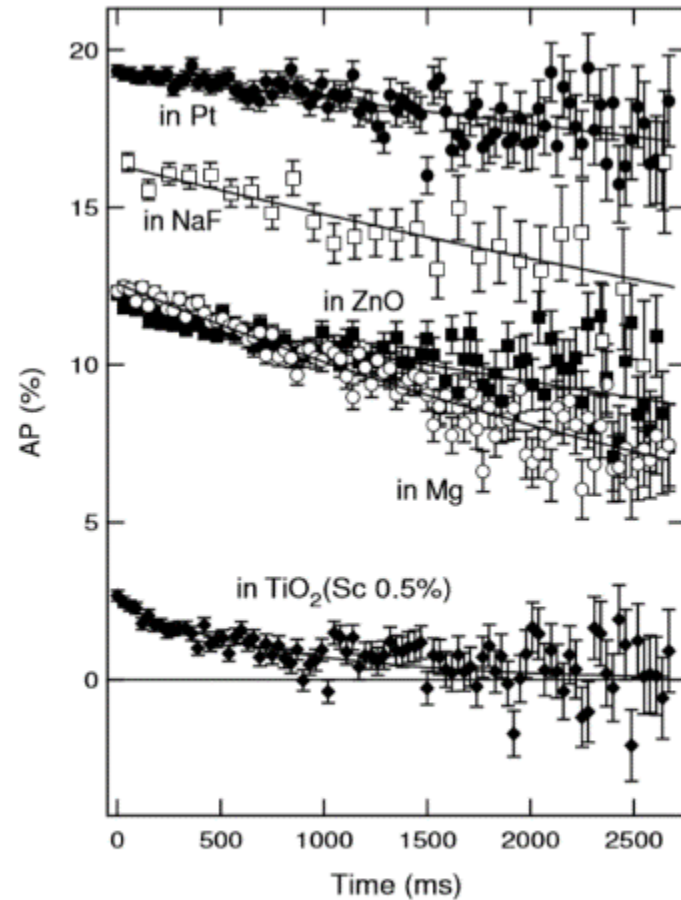
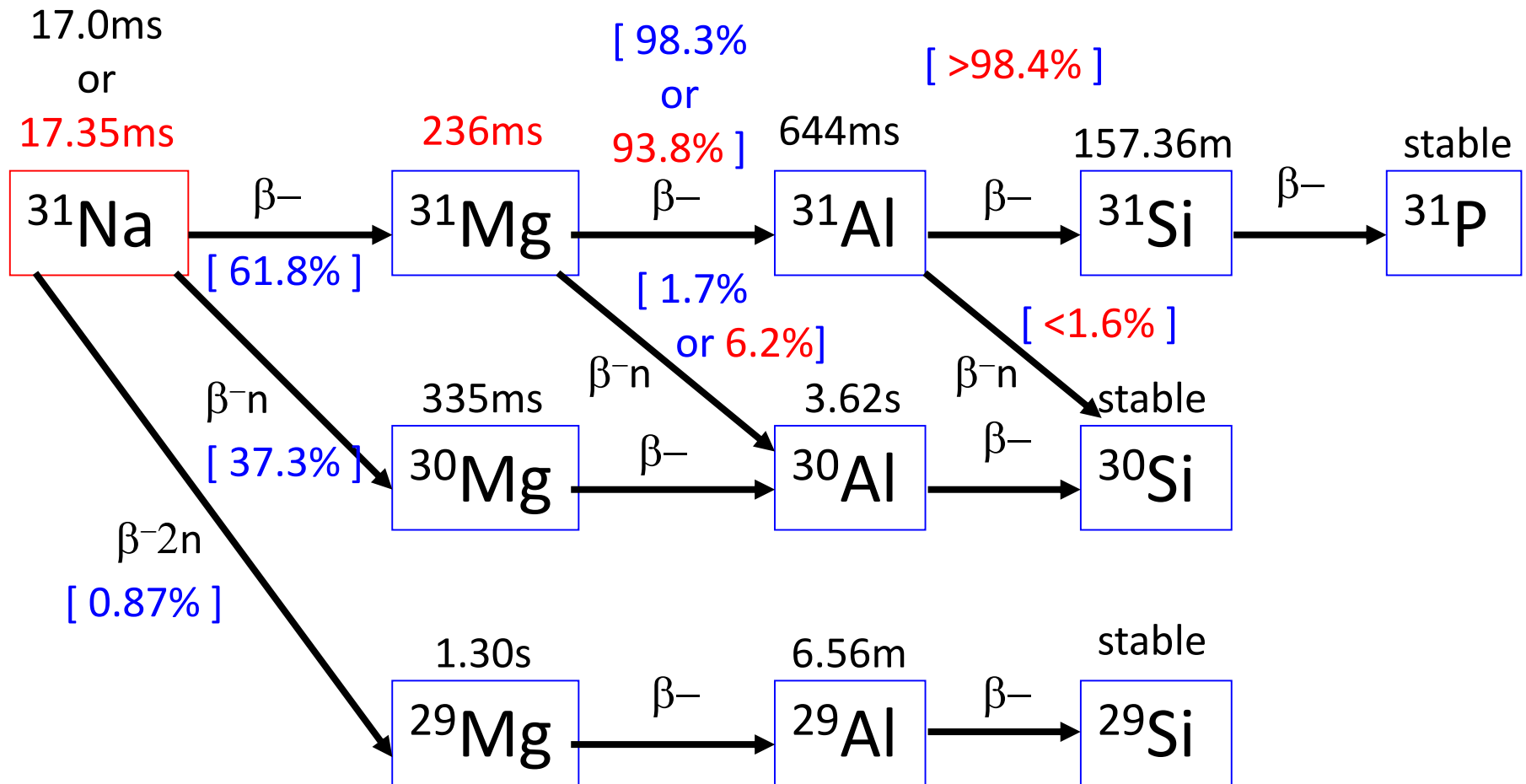


Figure 1: Time spectra of ^{20}Na polarization in several catchers.

^{31}Na β -decay



TRIUMF Mass separator

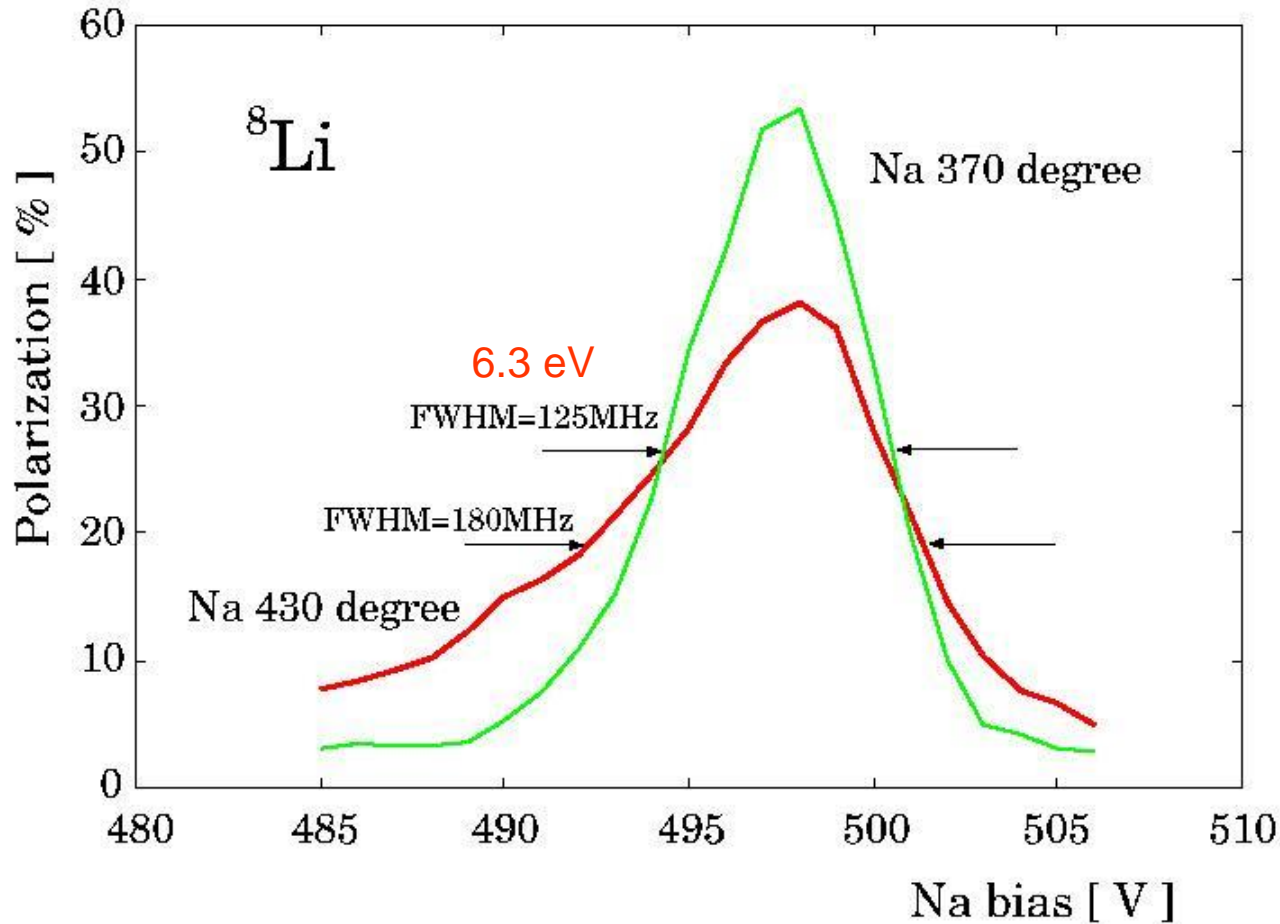
TRIUMF Mass separator

$$\Delta M/M \sim 1/10000$$

$$^{31}\text{Na}-^{31}\text{Mg} \quad \Delta M/M \sim 1/1825$$

$$^{31}\text{Na}-^{31}\text{Al} \quad \Delta M/M \sim 1/1050$$

energy (Doppler) broadening of the neutralized beam



>> laser line width
~ 1 MHz

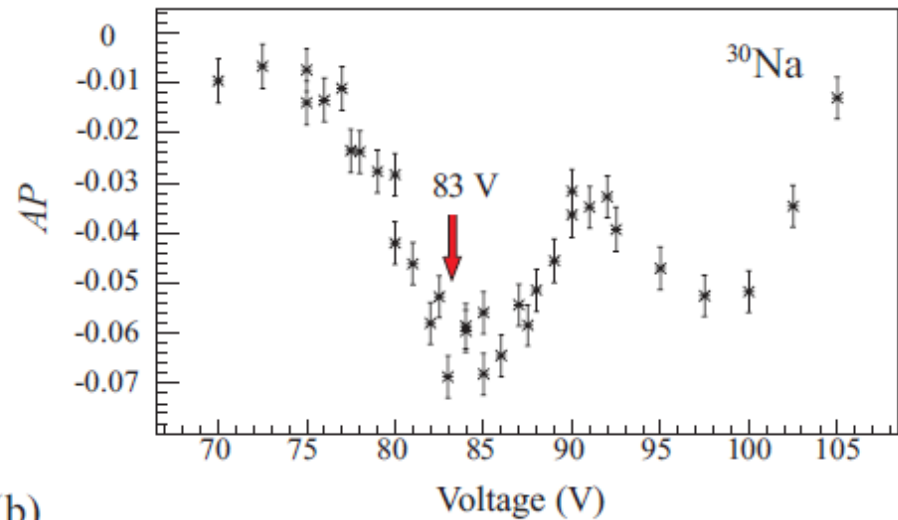
multiple collisions with Na atoms in the neutralizer

Beam tuning

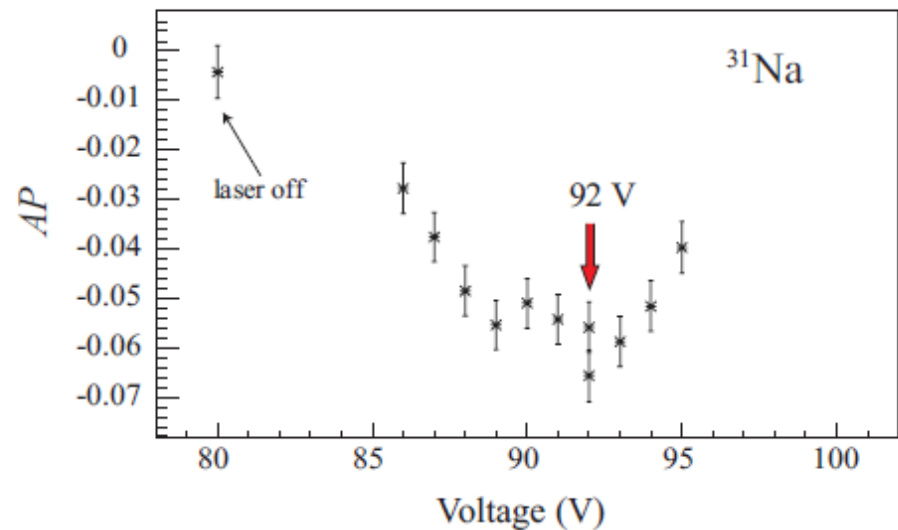
共鳴点のサーチ

Na cellのvoltage
をかえる

(a)



(b)



Doppler-shift tuning

deceleration bias (Na vapor cell)
tuning to adjust ion beam velocity
so as to meet the Doppler shift

absorption line

scanning velocity



v

v_1

905MHz

v_2

905MHz

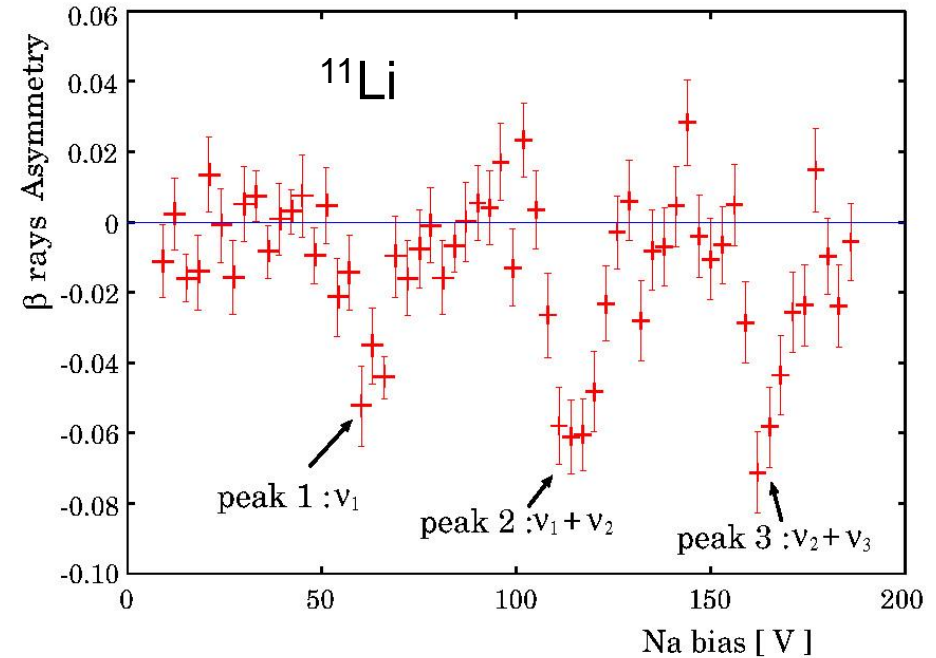
v_3

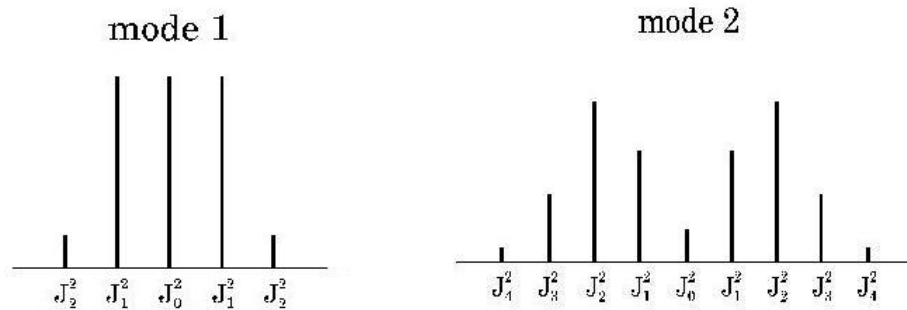
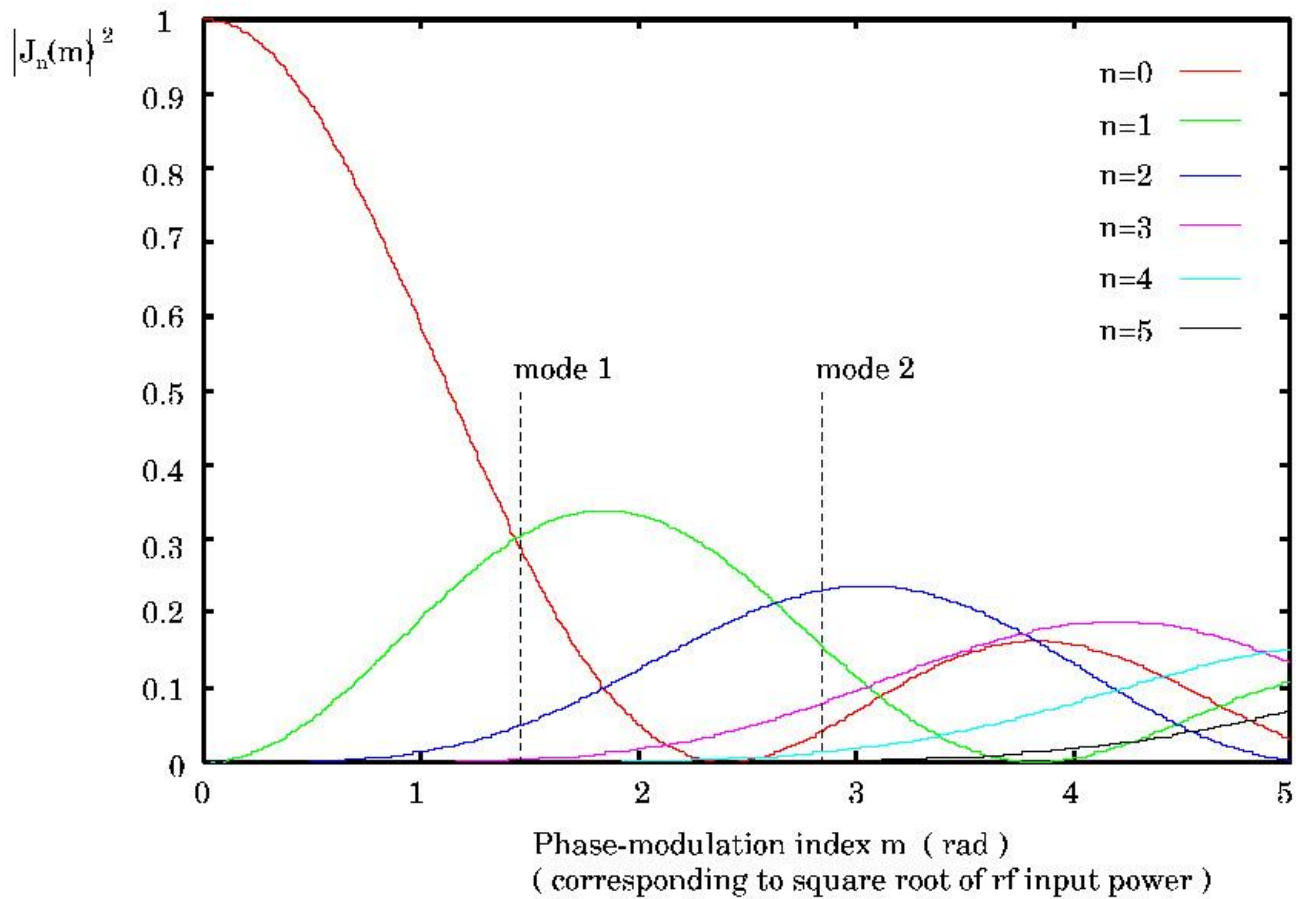
fixed

laser frequency

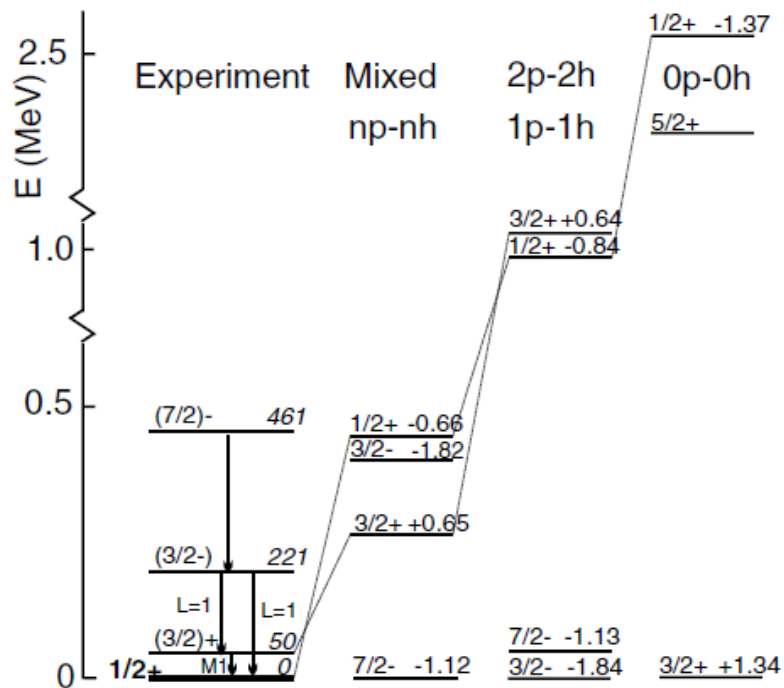
v

beta-decay asymmetry

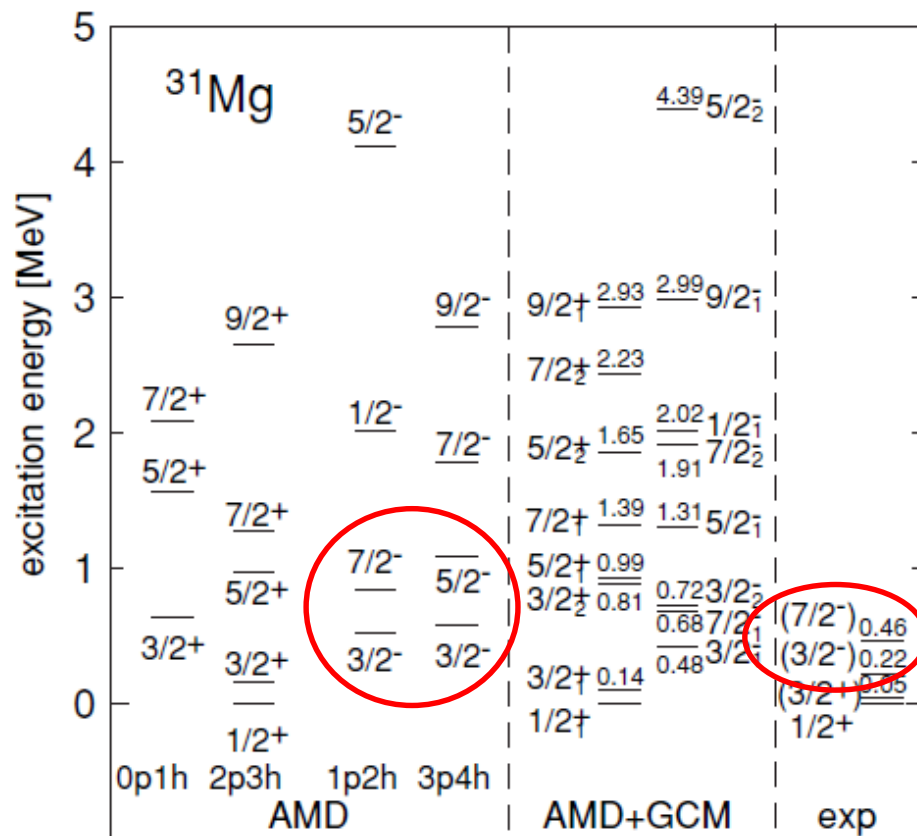




Comparison with shell model calculation



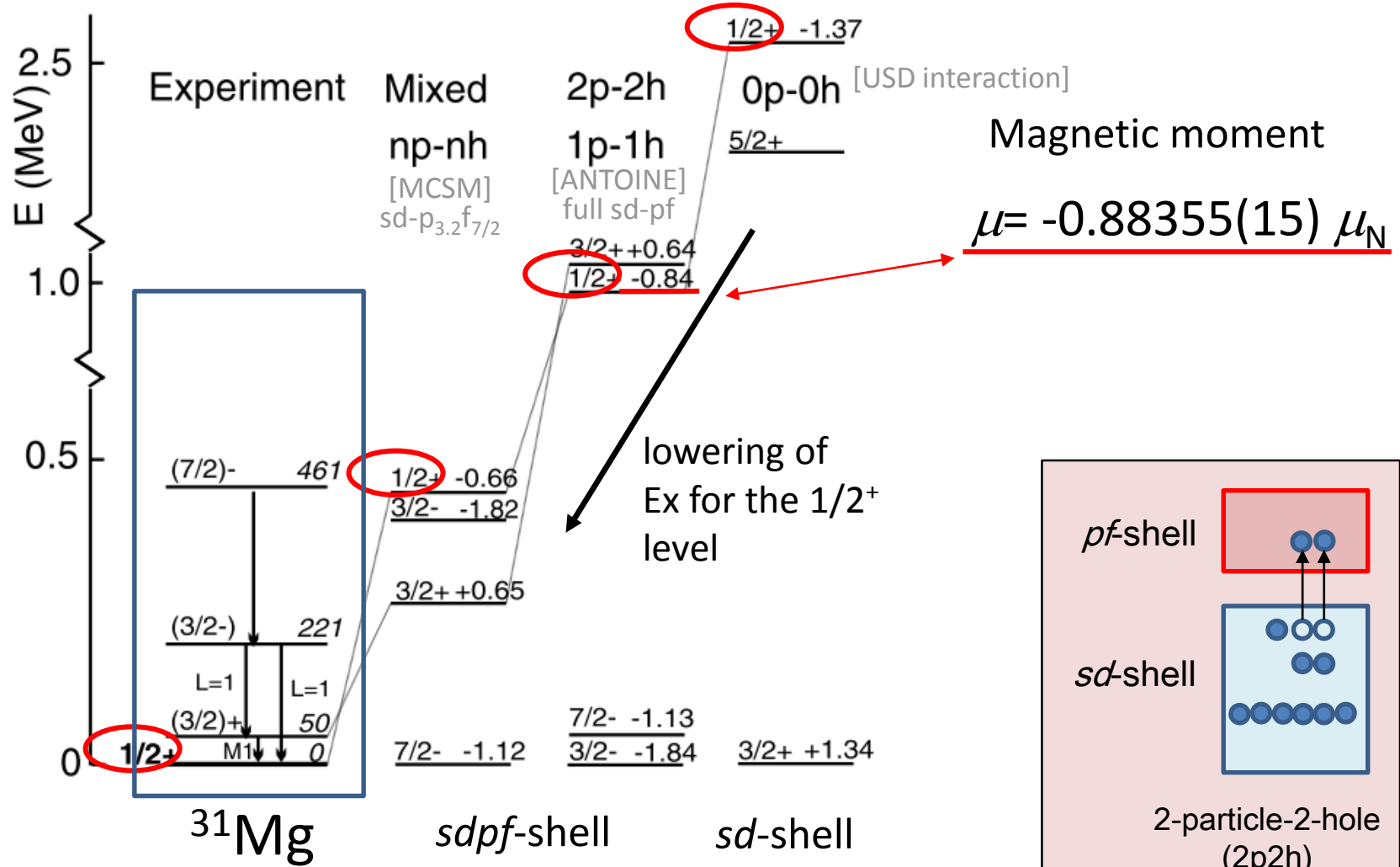
G. Neyens et al., Phys. Rev. Lett. 94, 022501(2005)



M. Kimura, Phys. Rev. C75, 041302(R) (2007)

spin-parity of the ground state in ^{31}Mg :

understanding from the shell model



G. Neyens et al., Phys. Rev. Lett. 94, 022501 (2005)

Negative-parity states in ^{31}Mg

Lifetime measurement in ^{31}Na β decay

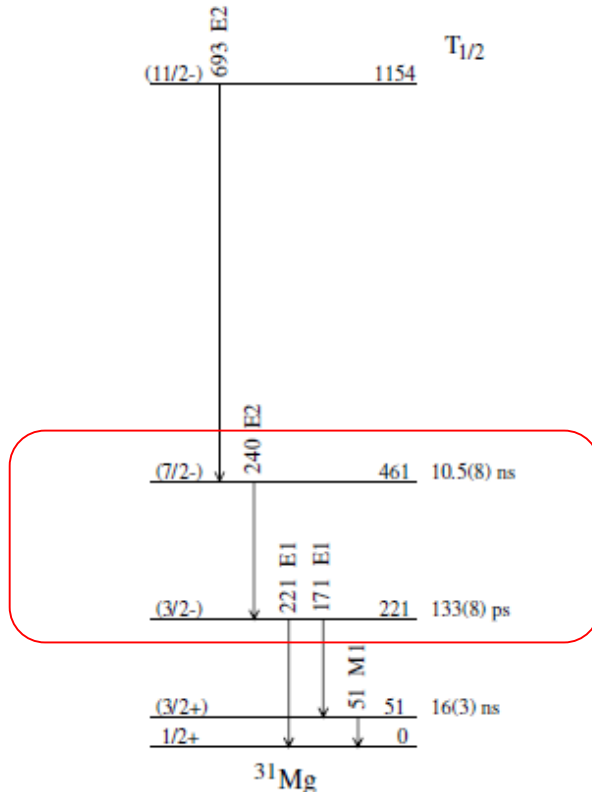
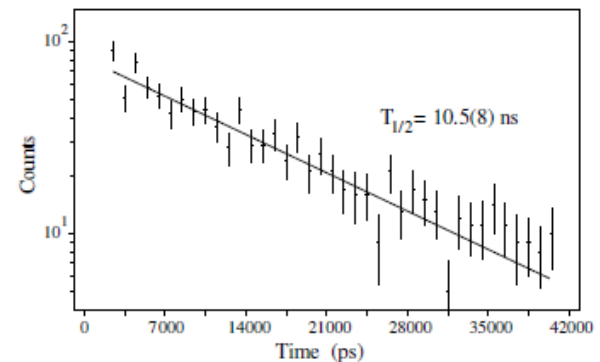
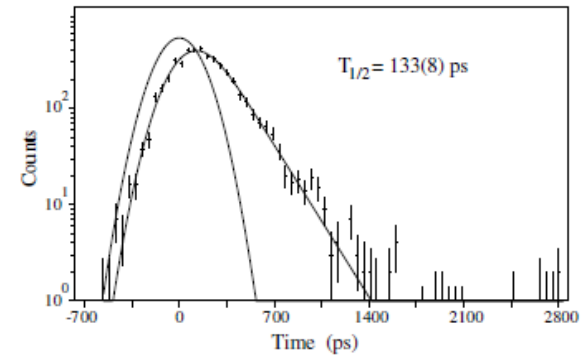


Fig. 2. A partial level scheme of ^{31}Mg and preliminary level lifetimes established in this work, except for the 51 keV level, which is taken from [2]. The suggested spin/parity assignments for the excited levels and transition multipolarities are model dependent [2] although supported by the observed transition rates.

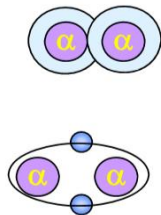


BaF₂ detector

anti-symmetrized molecular dynamics plus generator coordinate method (AMD+GCM)

AMD Antisymmetrized Molecular Dynamics

Reasonably describes
cluster states such as
 ^{12}Be



Y. Kanada-En'yo et al.,
Phys. Rev. C 68, 014319 (2003)

A Slater determinant of single particle wave packets.

$$\Phi_{\text{int}} = \frac{1}{\sqrt{A!}} \det\{\varphi_i(\mathbf{r}_j)\}$$

$$\varphi_i(\mathbf{r}) = \phi_i(\mathbf{r}) \cdot \chi_i \cdot \xi_i$$

$$\text{spatial: } \phi_i(\mathbf{r}) = \exp\{-(\mathbf{r} - \mathbf{Z}_i)\mathbf{M}(\mathbf{r} - \mathbf{Z}_i)\}$$

$$\text{spin: } \chi_i = \alpha_i \chi_{\uparrow} + \beta_i \chi_{\downarrow}$$

$$\text{isospin: } \xi_i = \text{proton or neutron}$$

$$\hat{H} = \hat{T} - \hat{T}_g + \hat{V}_{\text{Gogny}} + \hat{V}_{\text{Coulomb}}$$

GCM Generator Coordinate Method

treats collective motion

Theoretical Framework of AMD+GCM

Wave function of AMD

Variational wave function:

The parity is projected before the variation.

$$\Phi^\pi = \hat{P}^\pi \Phi_{\text{int}}$$

Intrinsic wave function:

A Slater determinant of single particle wave packets.

$$\Phi_{\text{int}} = \frac{1}{\sqrt{A!}} \det\{\varphi_i(\mathbf{r}_j)\}$$

$$\varphi_i(\mathbf{r}) = \phi_i(\mathbf{r}) \cdot \chi_i \cdot \xi_i$$

$$\text{spatial: } \phi_i(\mathbf{r}) = \exp\{-(\mathbf{r} - \mathbf{Z}_i)\mathbf{M}(\mathbf{r} - \mathbf{Z}_i)\}$$

$$\text{spin: } \chi_i = \alpha_i \chi_\uparrow + \beta_i \chi_\downarrow$$

$$\text{isospin: } \xi_i = \text{proton or neutron}$$

Variational parameters:

size and deformation of Gaussian \mathbf{M} :

3x3 real sym. matrix

centroids of Gaussian $\mathbf{Z}_i (i = 1, \dots, A)$:

complex 3d vectors

direction of spin α_i and $\beta_i (i = 1, \dots, A)$:

complex numbers

Variation after parity projection

Hamiltonian and energy:

$$\hat{H} = \hat{T} - \hat{T}_g + \hat{V}_{\text{Gogny}} + \hat{V}_{\text{Coulomb}}$$

$$E_{MK}^{J\pi} = \langle \Phi_{MK}^{J\pi} | \hat{H} | \Phi_{MK}^{J\pi} \rangle / \langle \Phi_{MK}^{J\pi} | \Phi_{MK}^{J\pi} \rangle$$

Frictional cooling method:

$$\dot{X}_i = (\mu + i\nu) c_{ij} \frac{\partial E_{MK}^{J\pi}}{\partial X_j}$$

Ang. Mom. Proj. and GCM

Ang. Mom. Proj.:

$$\Phi_{MK}^{J\pi}(m^{\text{th}}) = \hat{P}_{MK}^J \Phi^\pi(m^{\text{th}})$$

GCM:

$$\Psi_\alpha^{J\pi} = \sum_{m=1}^n f_m^\alpha \Phi_{MK}^{J\pi}(m^{\text{th}})$$

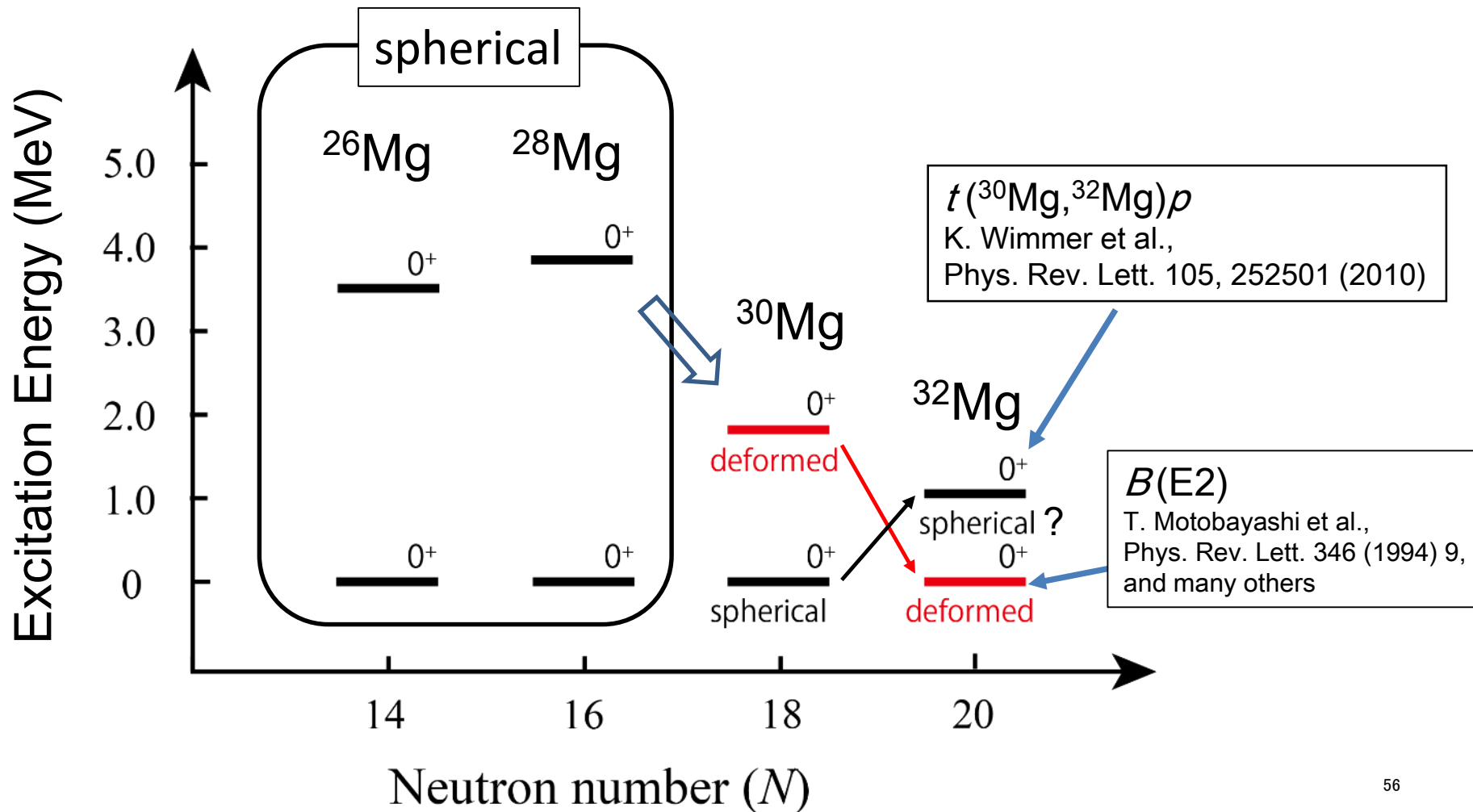
$$(H_{mm'} - E^\alpha N_{mm'}) f_m^\alpha = 0$$

$$H_{mm'} = \langle \Phi_{MK}^{J\pi}(m^{\text{th}}) | \hat{H} | \Phi_{MK}^{J\pi}(m'^{\text{th}}) \rangle,$$

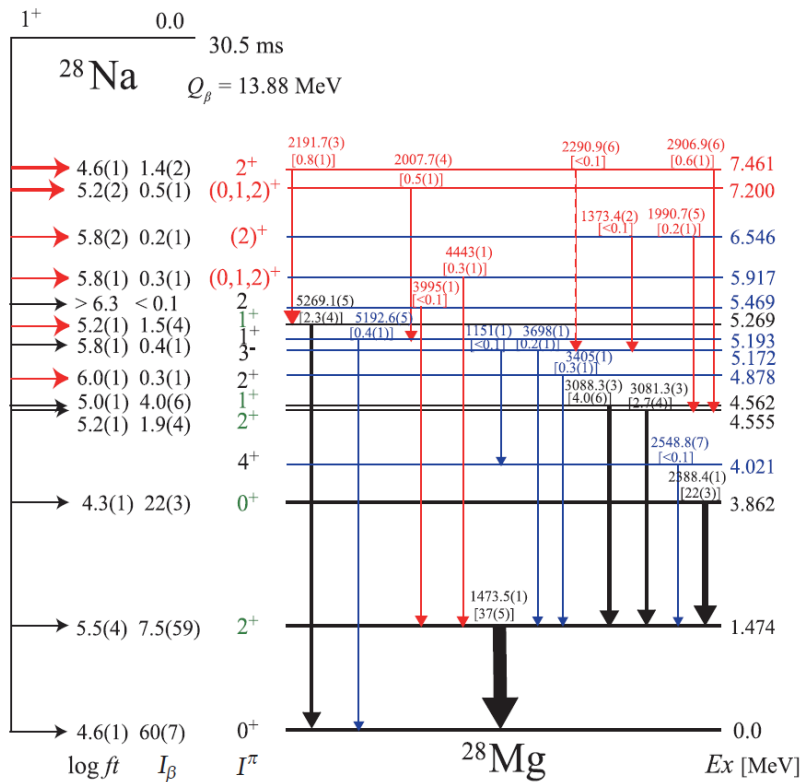
$$N_{mm'} = \langle \Phi_{MK}^{J\pi}(m^{\text{th}}) | \Phi_{MK}^{J\pi}(m'^{\text{th}}) \rangle$$

Excited States in even-mass Mg isotopes

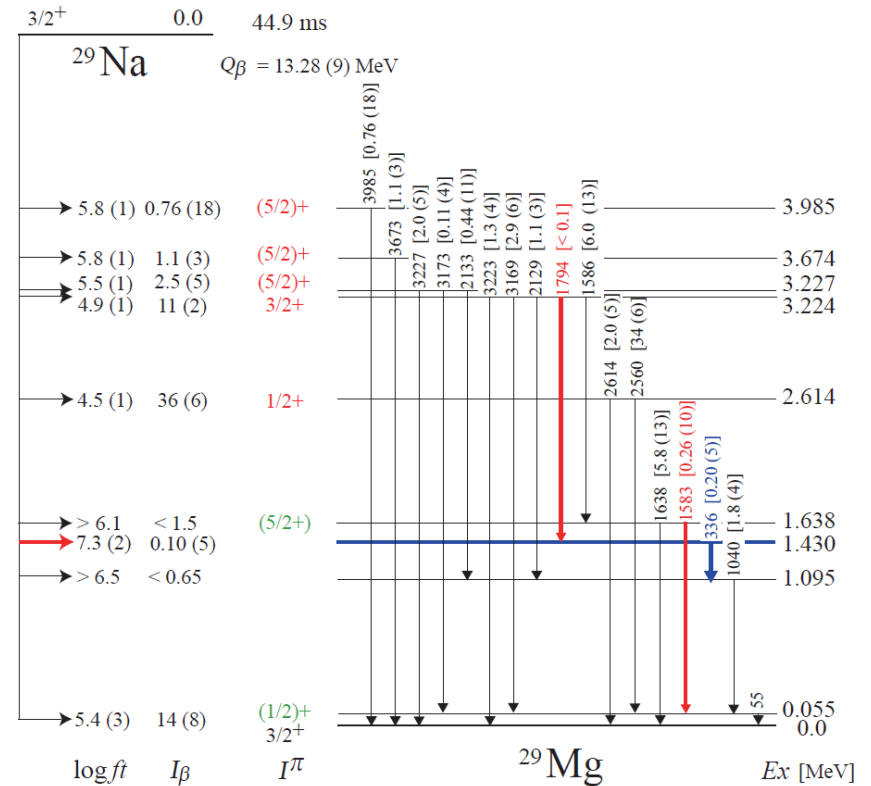
Examples: 0^+ states with different shapes



Revised Decay Scheme of $^{28,29}\text{Na}$ and New Levels in $^{28,29}\text{Mg}$

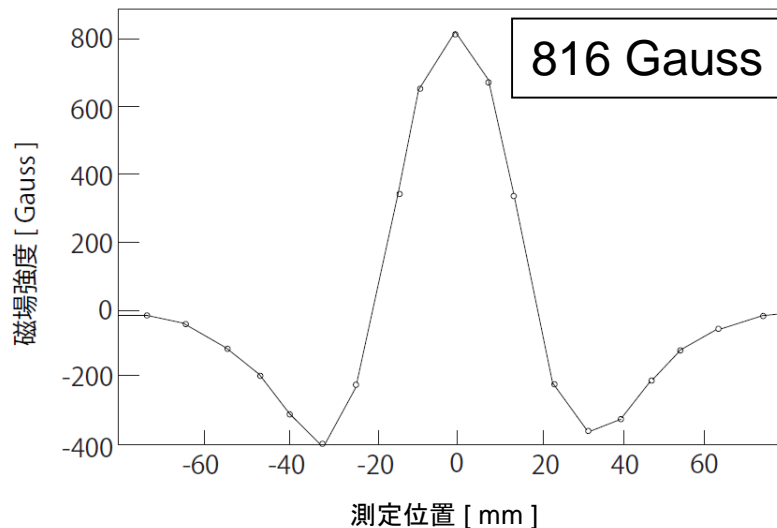
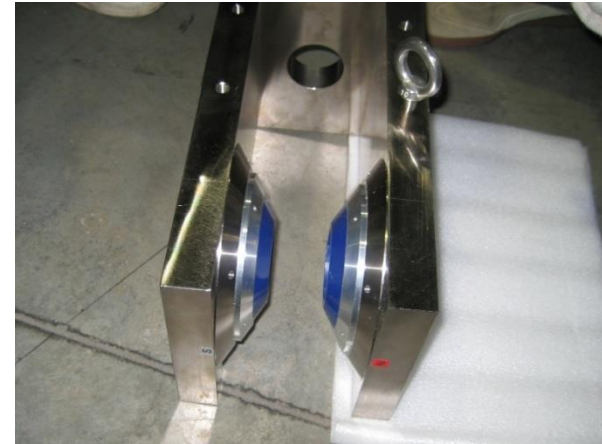
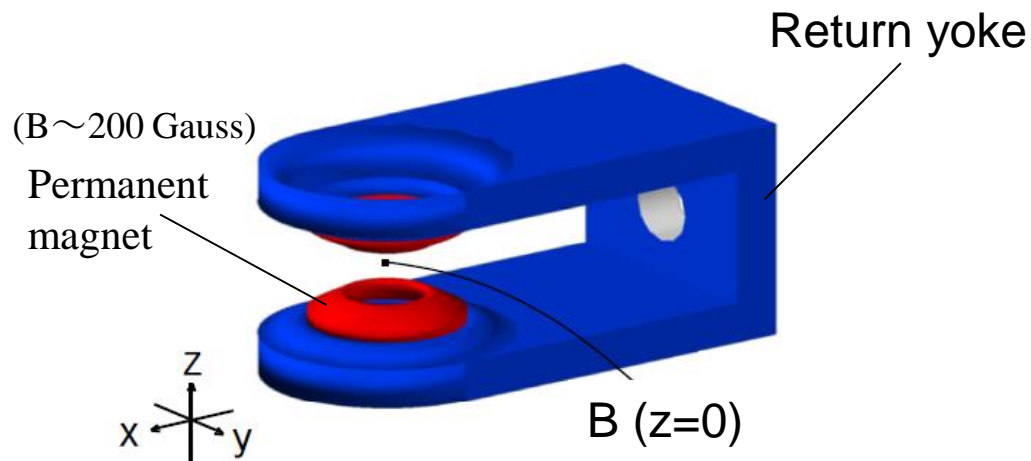


13 γ rays & 9 energy levels
Spins & parities of 4 levels

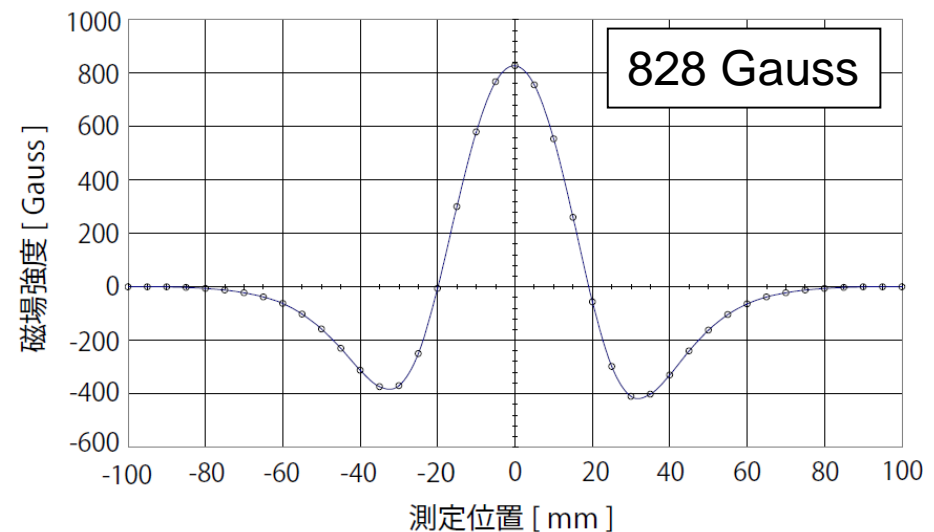


3 γ rays & 1 energy levels
Spins & parities of 7 levels

Enlargement of the magnetic field by magnet



TOSCA
simulation



Exp.

static magnet to preserve polarization

