

March 5th, 2017@Toyama Univ.

# Splitting Mass Spectra and Muon $g-2$ in Higgs- Anomaly Mediation

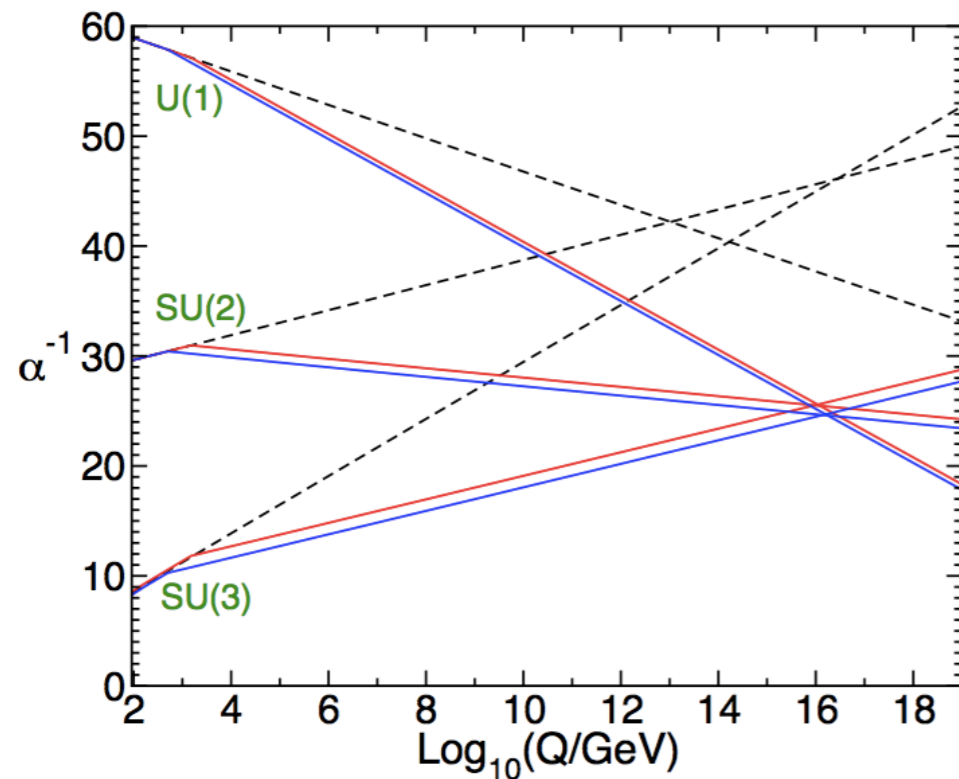
Norimi Yokozaki (Tohoku U.)

Wen Yin, Norimi Yokozaki, arXiv:1607.05705 (PLB)

See also

Tsutomu T. Yanagida, Wen Yin, Norimi Yokozaki, arXiv:1608.06618 (JHEP)

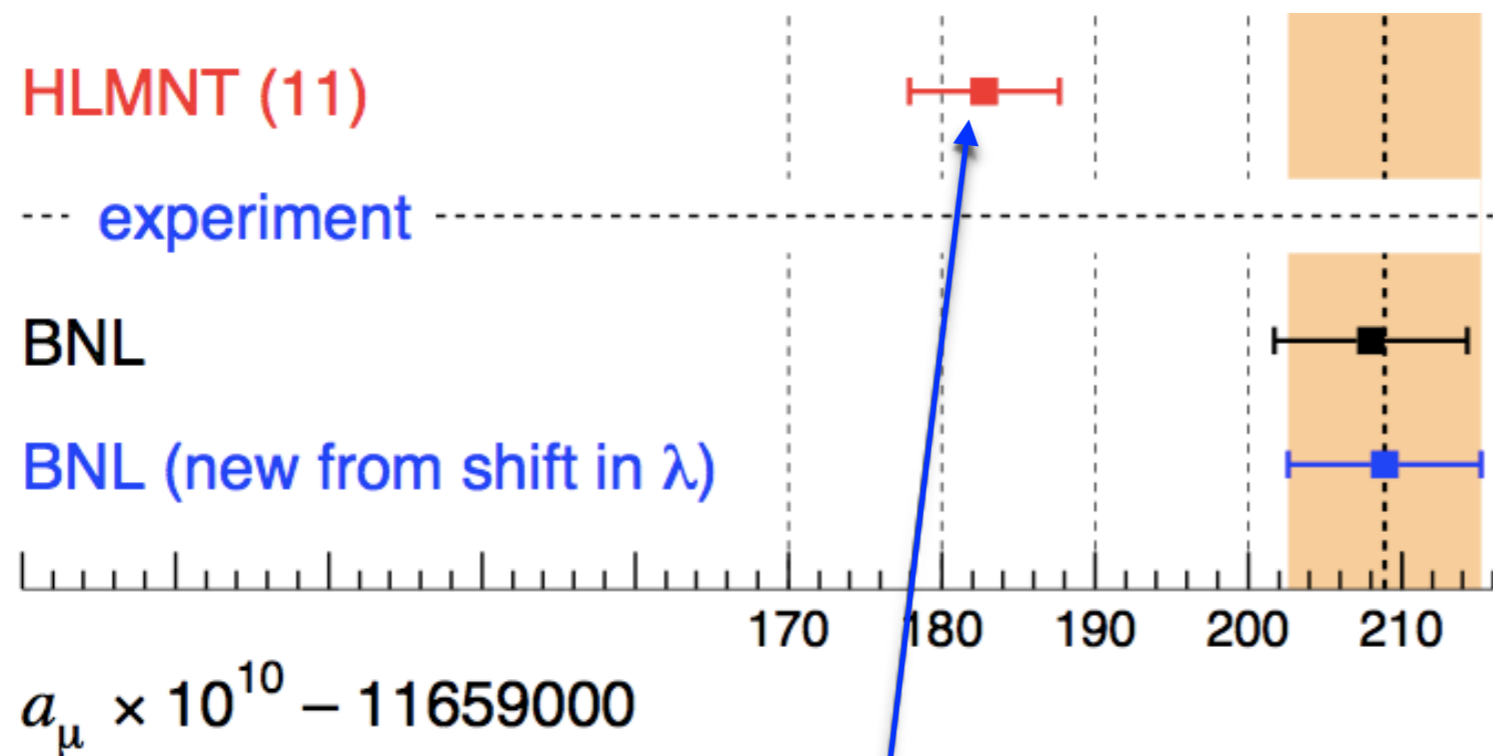
# Why SUSY



[from SUSY primer, S. Martin]

- Gauge coupling unification
  - Indicating grand unification
  - Matter unification
  - Charge quantization
- Absence of the quadratic divergences in the scalar potential (SM Higgs, PQ-breaking scalar, inflaton)
- There is another experimental motivation

# Muon g-2 anomaly



**>3  $\sigma$  deviation  
from SM  
prediction!**

[Also, Davier et al., 2016  
→ 3.6  $\sigma$ ]

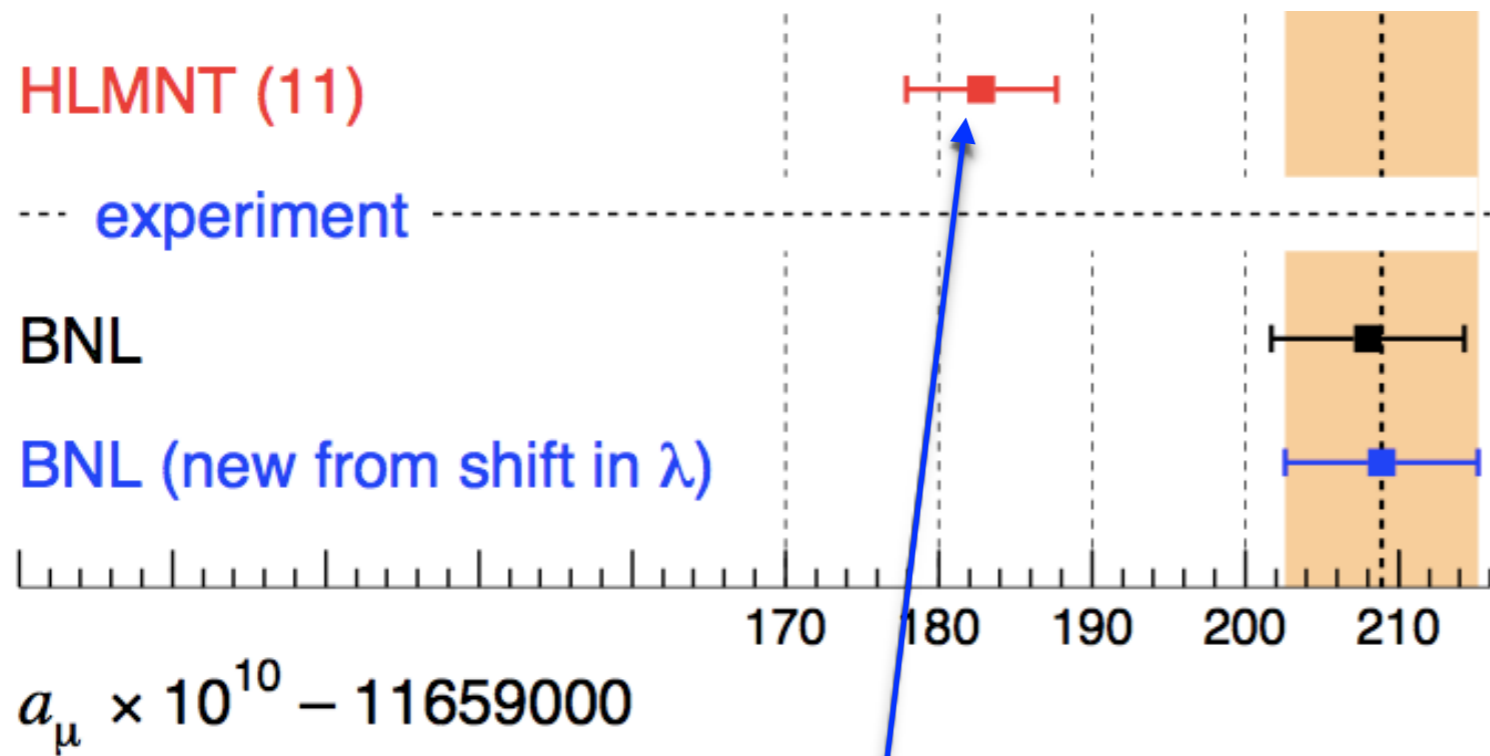
[Hagiwara, Liao, Martin, Nomura, Teubner, J.Phys. G38 (2011) 085003]

SM value

$$\mathcal{L} = \frac{e}{4m_\mu} (a_\mu)^{\text{NP}} \bar{\mu} \sigma_{\alpha\beta} \mu F^{\alpha\beta}$$

$(a_\mu)^{\text{NP}} \approx 2 \times 10^{-9}$  is required

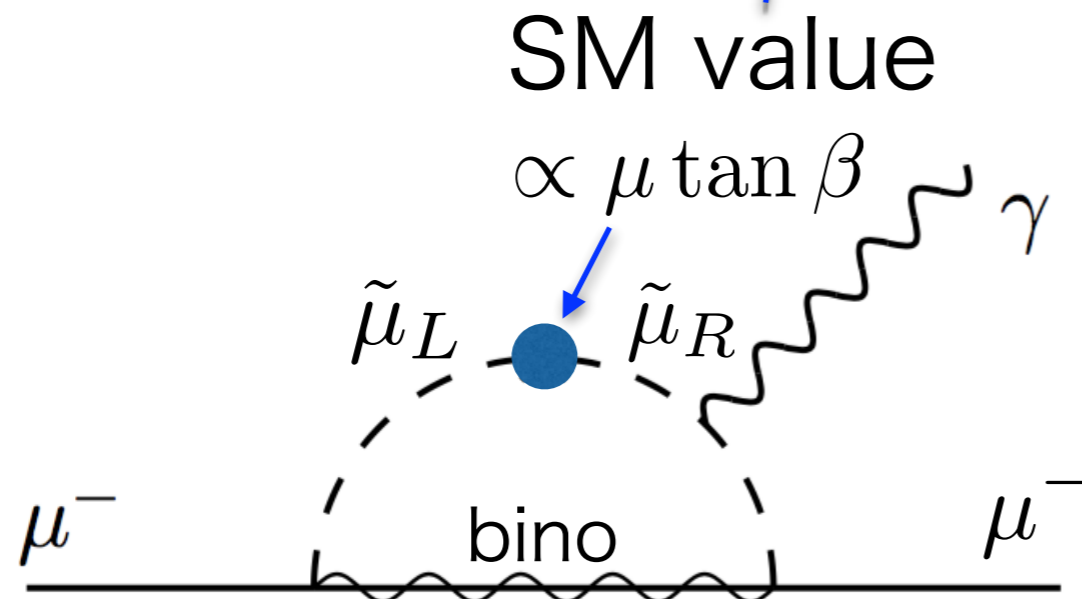
# Muon $g-2$ anomaly



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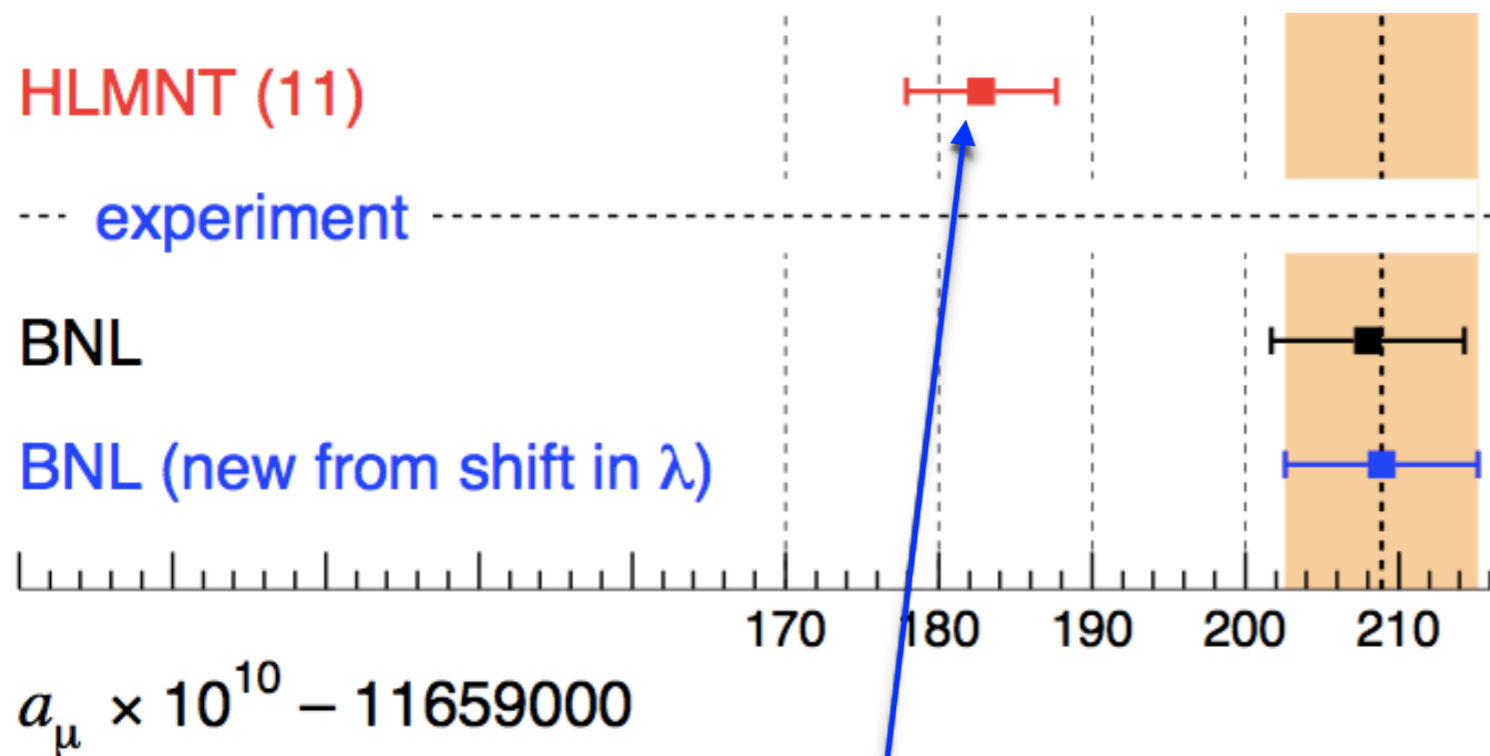
[Hagiwara, Liao, Martin, Nomura, Teubner, J.Phys. G38 (2011) 085003]



Relevant SUSY particles  
should be light as  $O(100)$  GeV

[Lopez, Nanopoulos and Wang, 1994;  
Chattopadhyay and Nath, 1996;  
Moroi, 1996]

# Muon $g-2$ anomaly



**>3  $\sigma$  deviation  
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prediction!**

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[Hagiwara, Liao, Martin, Nomura, Teubner, J.Phys. G38 (2011) 085003]

SM value

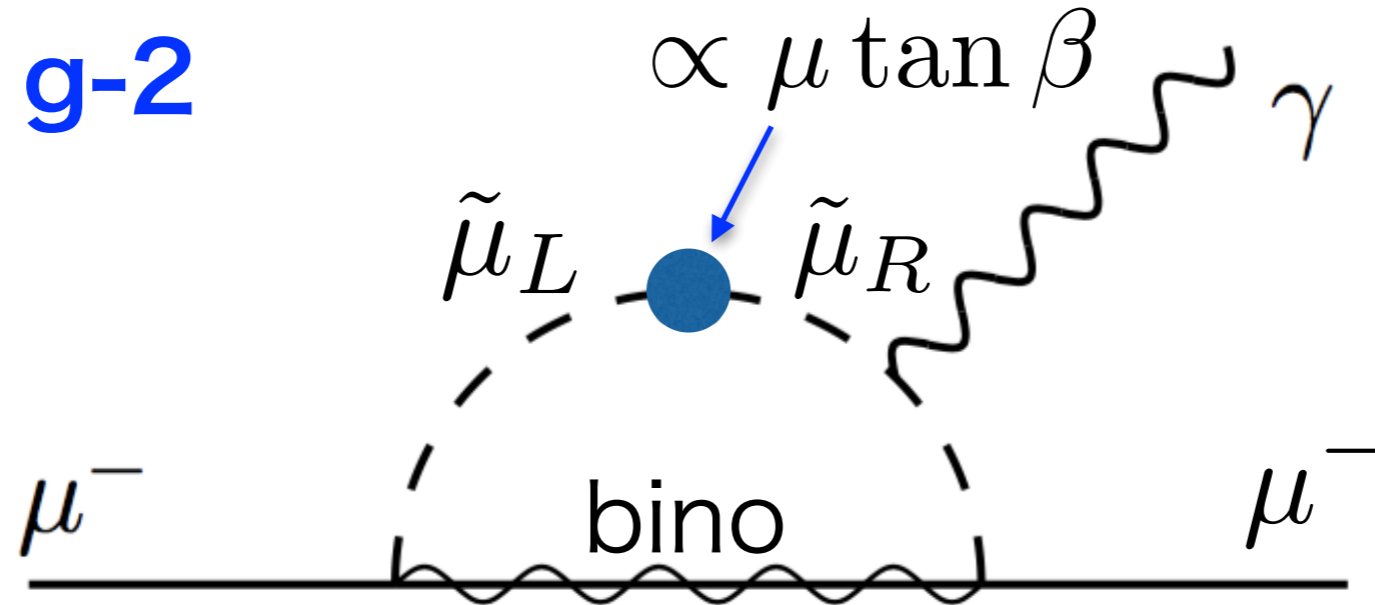
However, it is not easy to explain the muon  $g-2$  in MSSM, in a way consistent with GUT.

# Difficulties

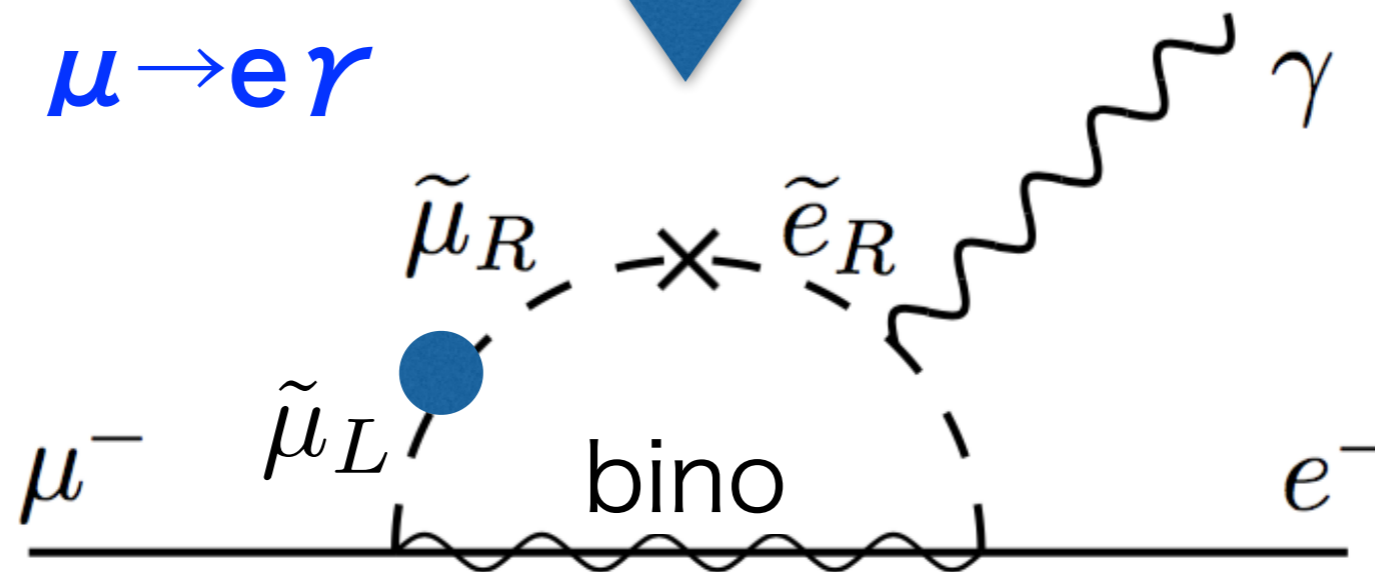
- LHC SUSY search  
→ heavy squarks and gluino of  $>1.4 - 1.8$  TeV
- Higgs boson mass of 125 GeV → heavy stops of  $\sim 10$  TeV
- Muon  $g-2$   
→ light sleptons and neutralino/chargino of  $\sim 100-500$  GeV
- Grand Unification → Slepton and squarks live in same GUT multiplet,  $\mathbf{10}=(Q, U^*, E^*)$   $\mathbf{5}^*=(L, D^*)$   
**It is natural that their masses are degenerated at the tree level. GUT breaking effects may be required.**
- Naively, gaugino masses also unify:  
 $g_1=g_2=g_3=g_5 \rightarrow \mathbf{M_1=M_2=M_3=M_5}$

# Flavor problem

$g-2$



$\mu \rightarrow e \gamma$



In general, if muon  $g-2$  enhanced  
 $\rightarrow$  LFV is also enhanced

# Higgs-Anomaly mediation

- We considered a simple model explaining the muon  $g-2$ , without difficulties concerning the GUT embedding and flavor violation ([Yin-Yokozaki, 2016](#))

In our model, sfermion and gaugino masses originate from anomaly mediation and Higgs loop effects; therefore, no SUSY flavor problem arises

Refs for Anomaly mediation:

[Giudice, Luty, Murayama, Rattazzi; Randall, Sundrum, 1999]



# Higgs-Anomaly mediation

- We considered a simple model explaining the muon  $g-2$ , without difficulties concerning the GUT embedding and flavor violation ([Yin-Yokozaki, 2016](#))

## Recipe:

- 1, Sequestering the matter fields and SUSY breaking field  
→ squarks and sleptons are massless at the tree level  
(gauginos are also massless)
- 2, Making the gravitino heavy ( $\sim 100$  TeV)  
→ Anomaly mediation becomes effective, inducing GUT breaking effects
- 3, Coupling only Higgs fields and SUSY breaking field directly. **(Note: Higgs soft masses are tachyonic)**

Solving the  
flavor problem

Relaxing the  
gravitino  
problem

# Our setup

$$K = -3M_P^2 \ln \left[ 1 - \frac{f(Z, Z^\dagger) + \phi_i^\dagger \phi_i + \Delta K}{3M_P^2} \right],$$

SUSY breaking field

(quark, lepton, Higgs)

$$\Delta K = c_Z \frac{|Z|^2}{M_P^2} (|H_u|^2 + |H_d|^2),$$

$c_Z > 0$

# Our setup

$$K = -3M_P^2 \ln \left[ 1 - \frac{f(Z, Z^\dagger) + \phi_i^\dagger \phi_i}{3M_P^2} \right],$$

SUSY breaking field

(quark, lepton, Higgs)

**First, we start with a sequestered form**

Sfermion masses vanish at the tree-level

**Simple and important assumption to solve  
SUSY flavor problem**

(gaugino masses also vanish at the tree-level)

Ref. for sequestered form [Randall, Sundrum, 1999]

# Our setup

$$K = -3M_P^2 \ln \left[ 1 - \frac{f(Z, Z^\dagger) + \phi_i^\dagger \phi_i}{3M_P^2} \right],$$

SUSY breaking field

(quark, lepton, Higgs)

Sfermion masses vanish at the tree-level

From anomaly mediation effects, sfermion get masses at the two-loop level. However, slepton mass becomes tachyonic

$$m_{\bar{E}}^2 \approx -22g_Y^4 \frac{m_{3/2}^2}{16\pi^2}$$

(Left-handed slepton has also tachyonic mass)

# Our setup

$$K = -3M_P^2 \ln \left[ 1 - \frac{f(Z, Z^\dagger) + \phi_i^\dagger \phi_i}{3M_P^2} \right],$$

SUSY breaking field

(quark, lepton, Higgs)

Sfermion masses vanish at the tree-level

From anomaly mediation effects, sfermion get masses at the two-loop level. However, slepton mass becomes tachyonic

**Tachyonic slepton problem in anomaly mediation**

→ From another perspective, slepton can be light which is favored for the muon  $g-2$

**GUT breaking effects are naturally included**

# Our setup

$$K = -3M_P^2 \ln \left[ 1 - \frac{f(Z, Z^\dagger) + \phi_i^\dagger \phi_i + \Delta K}{3M_P^2} \right],$$

SUSY breaking field

(quark, lepton, Higgs)

$$\Delta K = c_Z \frac{|Z|^2}{M_P^2} (|H_u|^2 + |H_d|^2),$$

$c_Z > 0$

Only Higgs doublets couple to the SUSY breaking field directly

(Solving tachyonic slepton problem and making third generation sfermion heavy)

# Our setup

$$K = -3M_P^2 \ln \left[ 1 - \frac{f(Z, Z^\dagger) + \phi_i^\dagger \phi_i + \Delta K}{3M_P^2} \right],$$

SUSY breaking field

(quark, lepton, Higgs)

$$\Delta K = c_Z \frac{|Z|^2}{M_P^2} (|H_u|^2 + |H_d|^2),$$

$c_Z > 0$

**Only Higgs doublets couple to the SUSY breaking field directly**

**Negative Higgs soft mass squares are important!**

$$\frac{dm_{Q_3}^2}{d \ln \mu_R} \ni \frac{1}{8\pi^2} (Y_t^2 m_{H_u}^2 + Y_b^2 m_{H_d}^2) < 0$$

**Lifting up 3rd generation sfermion masses at one-loop level**  
**Important for the Higgs mass of 125 GeV**

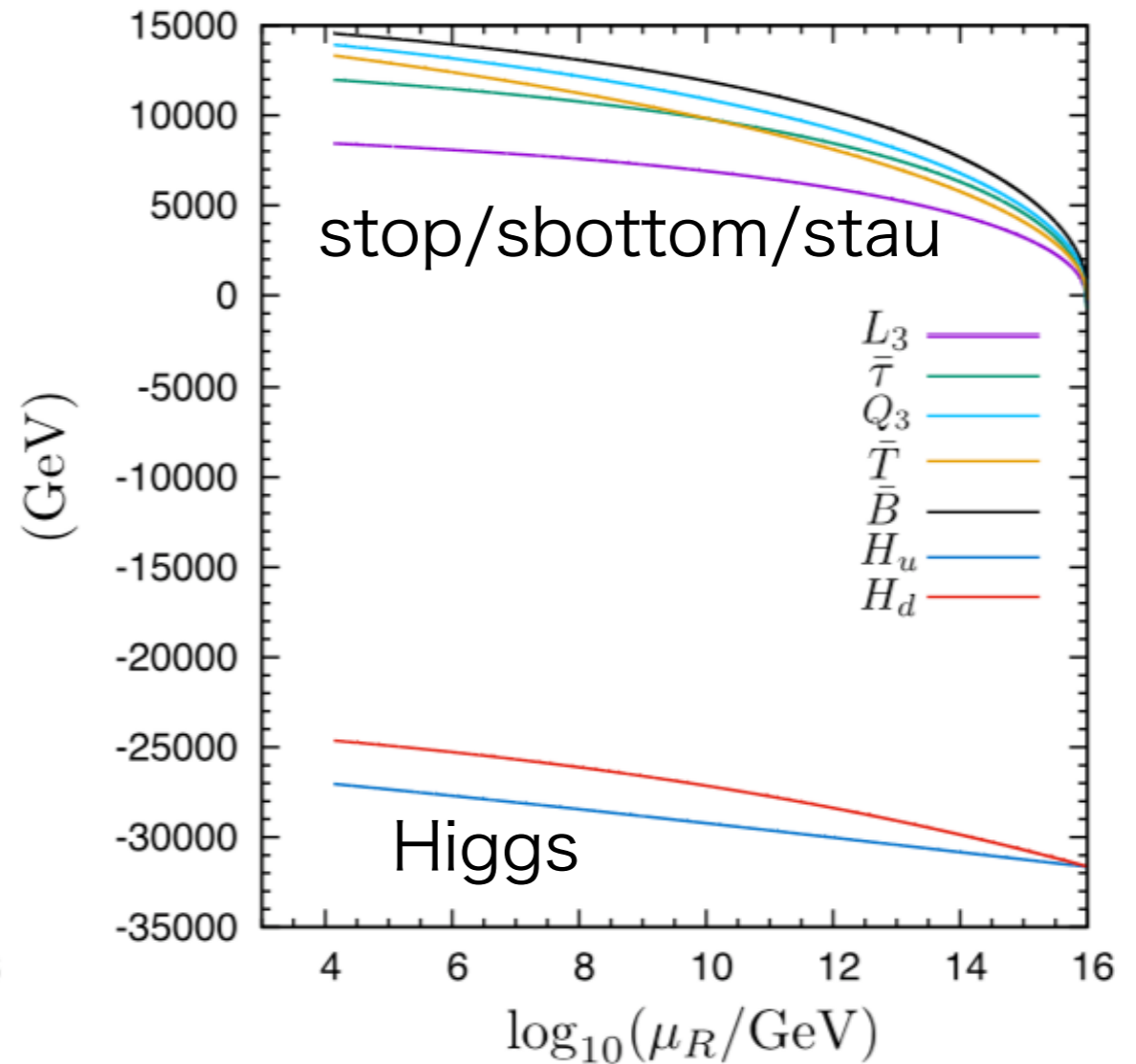
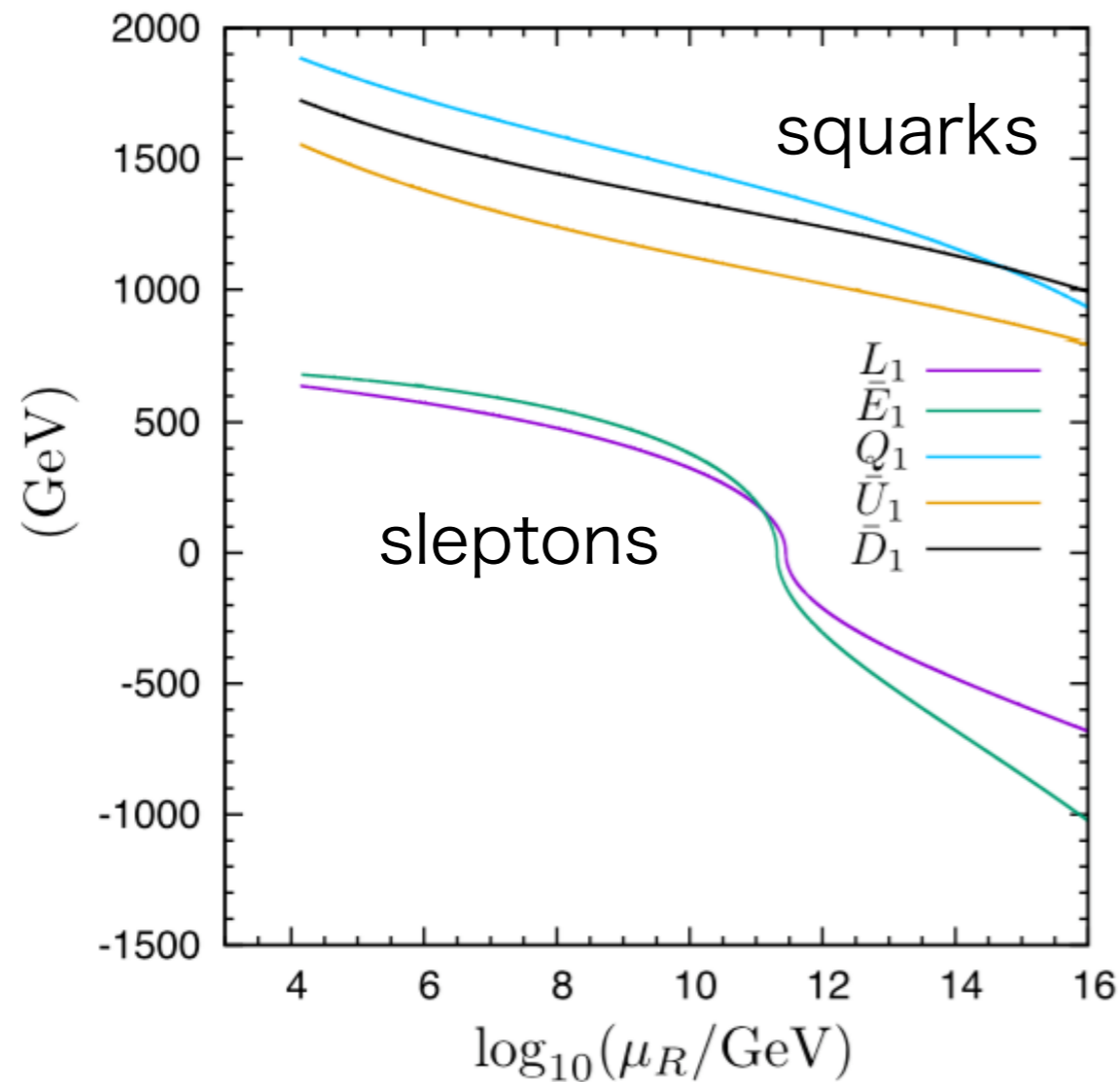
e.g.

$$\frac{dm_{\bar{E}}^2}{d \ln \mu_R} \ni \frac{1}{(16\pi^2)^2} \left[ \frac{36}{25} g_1^4 (m_{H_u}^2 + m_{H_d}^2) \right] < 0$$

**Lifting up slepton masses, avoiding the tachyonic slepton problem at two-loop level**



# RGE runnings of soft mass parameters



$$m_{3/2} = 120 \text{ TeV}, \tan \beta = 48, \text{ and } m_H = -10^9 \text{ GeV}^2.$$

(Still D-flat direction of the Higgs potential is safe!)

# Mass spectrum and muon $g-2$

(Including leading two-loop corrections)

Parameters	Point I	Point II
$m_{3/2}$ (TeV)	120	140
$m_H^2$ (GeV <sup>2</sup> )	$-9 \times 10^8$	$-9 \times 10^8$
$\tan \beta$	48	46.7
Particles	Mass (GeV)	Mass (GeV)
$\tilde{g}$	2550	2930
$\tilde{q}$	1830 - 2110	2240 - 2470
$t_{2,1}$ (TeV)	13.1, 12.5	13.1, 12.6
$\tilde{b}_{2,1}$ (TeV)	14.2, 13.4	14.2, 13.5
$\tilde{\chi}_1^0 / \tilde{\chi}_1^\pm$	378	440
$\tilde{\chi}_2^0$	1100	1290
$\tilde{e}_{L,R}$	549, 682	485, 586
$\tilde{\mu}_{L,R}$	609, 778	544, 680
$\tilde{\tau}_{2,1}$ (TeV)	11.4, 8.0	11.1, 7.8
$H^\pm$ (TeV)	10.9	10.7
$h_{\text{SM-like}}$	127.3	125.1
$\mu$ (TeV)	25.8	25.8
$(a_\mu)_{\text{SUSY}}$ ( $10^{-10}$ )	18.6	18.1

~wino

~bino

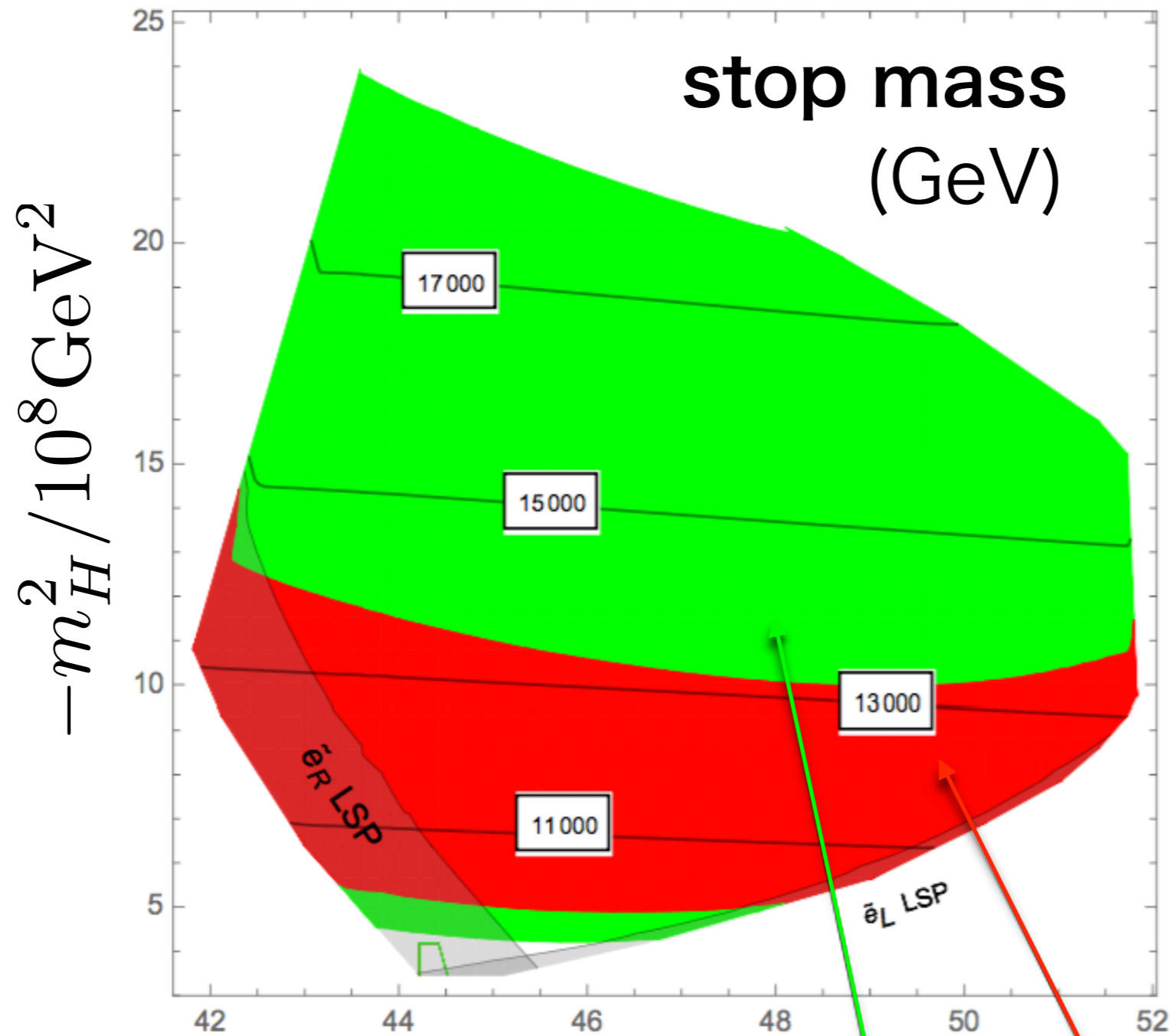
~ 2-3TeV

~ 10TeV

~ 600GeV

~ g-2: 1  $\sigma$

# $m_{3/2} = 100 \text{ TeV}$



gluino mass: 2.2 TeV  $\tan \beta$

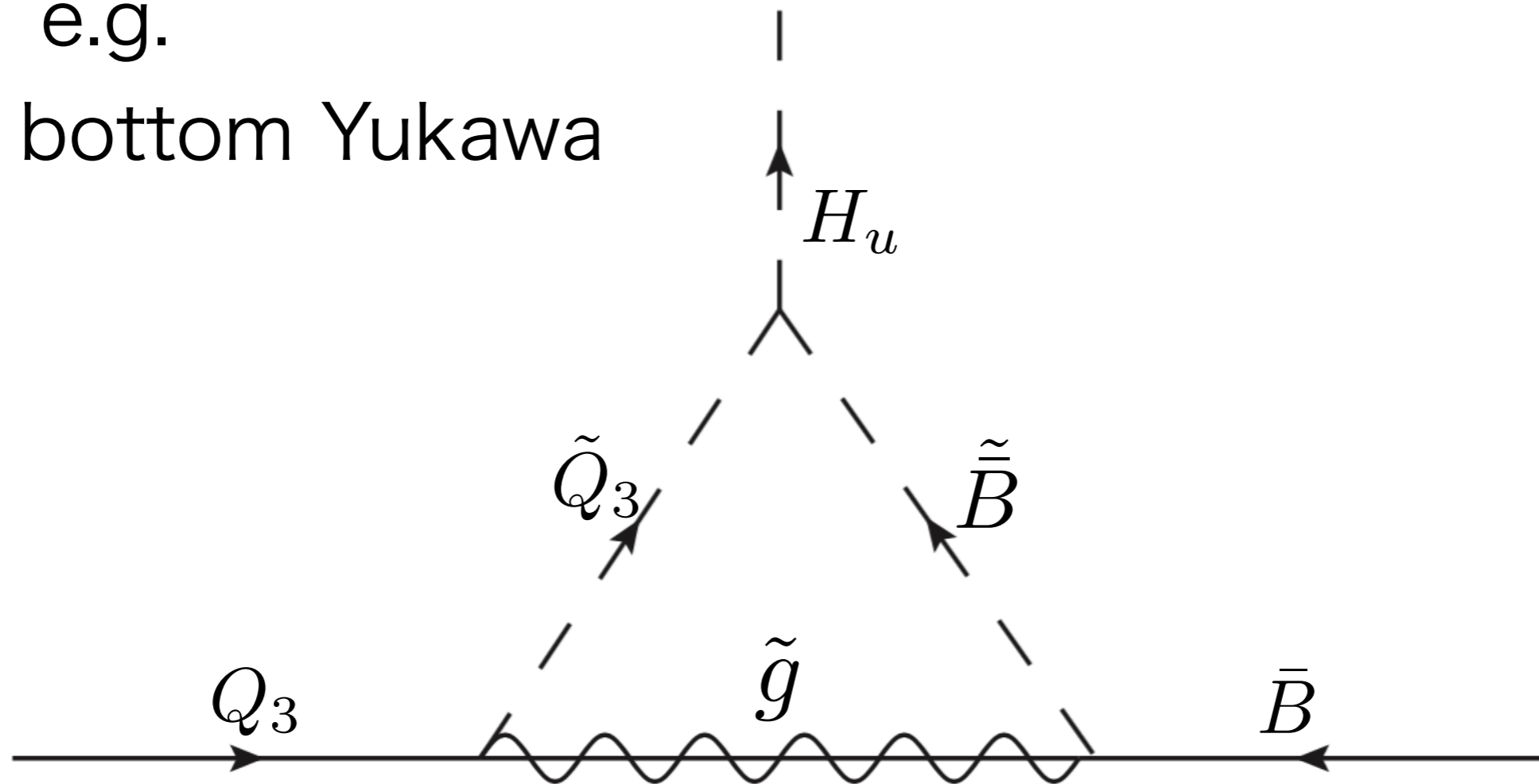
wino mass (LSP): 320 GeV

$2\sigma$

$g-2: 1\sigma$

# Yukawa coupling unification

e.g.  
bottom Yukawa



With important threshold corrections

# Bottom-Tau unification

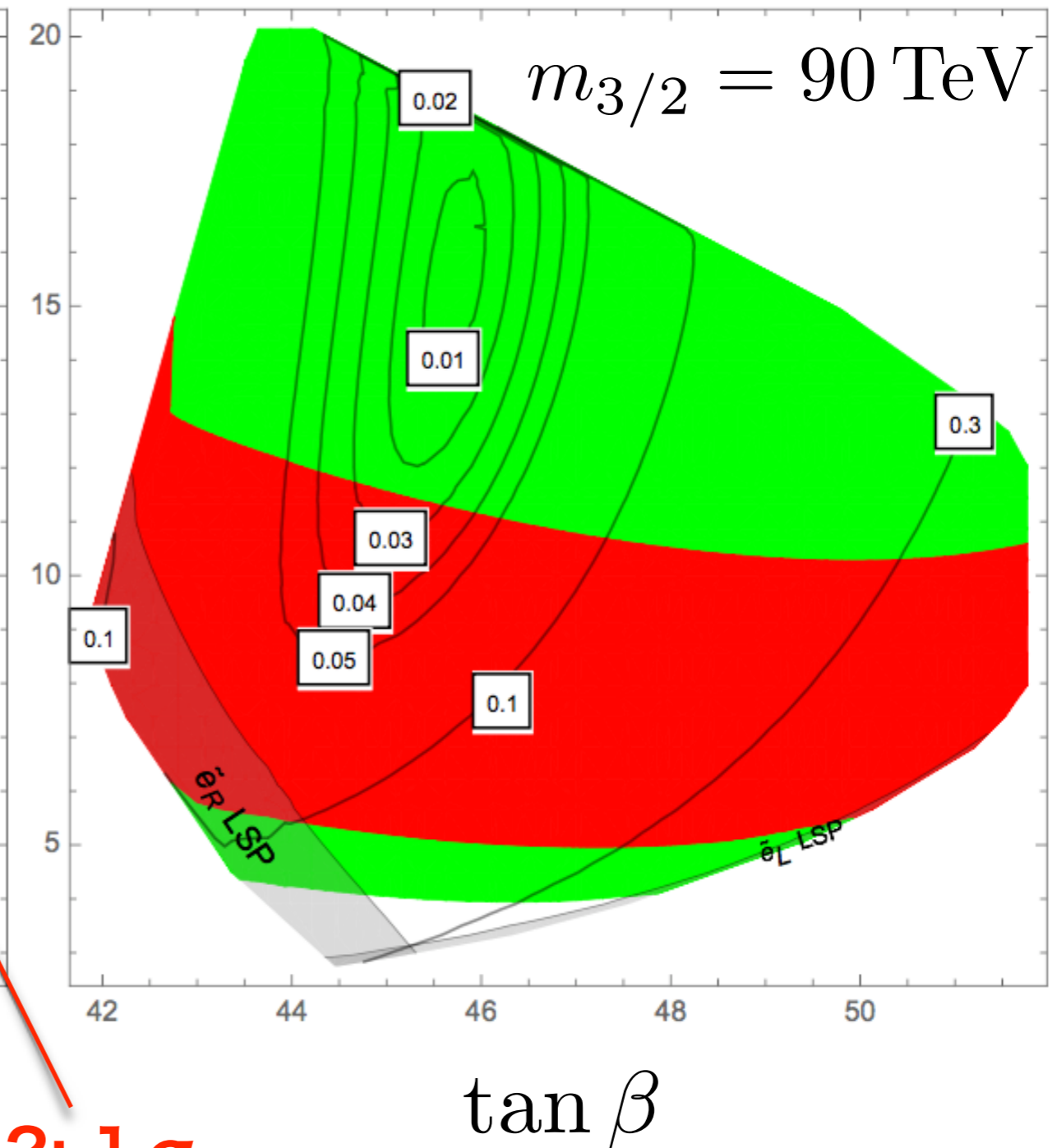
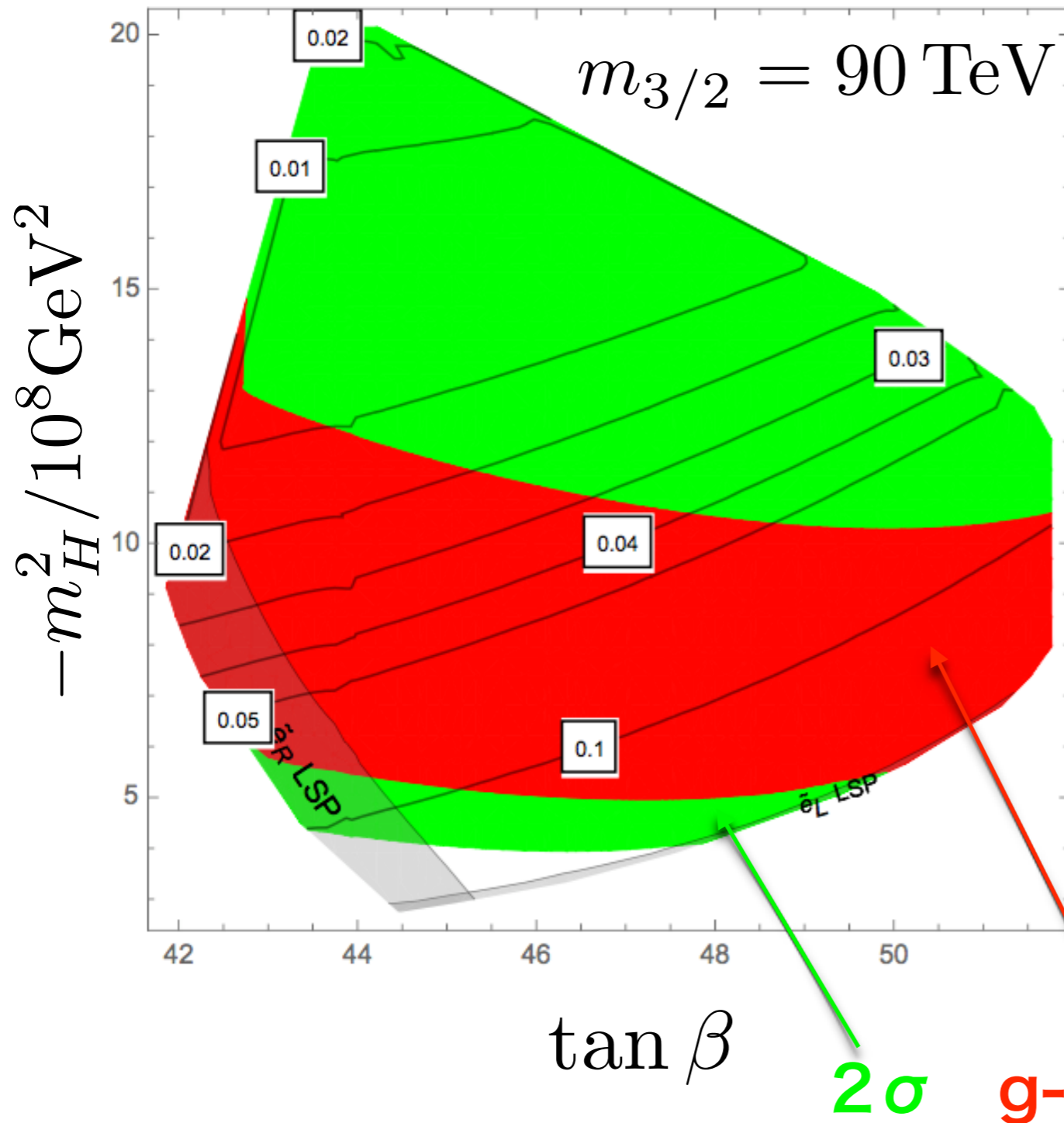
Motivated by SU(5)

$$\sqrt{(Y_b - Y_\tau)^2}$$

# Bottom-Tau-Top unification

Motivated by SO(10)

$$\sqrt{(Y_b - Y_\tau)^2 + (Y_t - Y_\tau)^2 + (Y_t - Y_b)^2}$$



# Summary

- We have found a simple model which has many benefits
  - Muon  $g-2$  is explained.
  - The Higgs boson mass of 125 GeV is explained with  $\sim 10$  TeV stops.
  - No SUSY flavor problem
  - Tachyonic slepton problem is solved
  - Gravitino problem is significantly relaxed with  $\sim 100$  TeV gravitino

# Summary

- Wino, squarks and gluino can be seen at the LHC.
- Yukawa coupling unification is realized.
- No singlet SUSY breaking field is required.  
→ Polonyi problem may be relaxed.
- Massless sfermions may be regarded as NG bosons, which may enable us to understand the origin of the family number, three. ([Kugo, Yanagida, 1984](#) ... [Yanagida, Win, Yokozaki, 2016](#))



- Squarks and sleptons get masses from Higgs soft masses, and their hierarchical masses originate from the structure of the Yukawa couplings



Our scenario

- Quarks and leptons get masses from the VEV of the Higgs field, and their hierarchical masses originate from the structure of the Yukawa couplings.

Standard model

The structure seems natural.