

Electroweak Baryogenesis with Flavor Violation

Eibun Senaha (National Taiwan U)
March 4, 2017@HPNP2017

based on

C.-W. Chiang (Natl Taiwan U), K. Fuyuto (UMass-Amherst), E.S., 1607.07316 [PLB]

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Lepton

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Outline

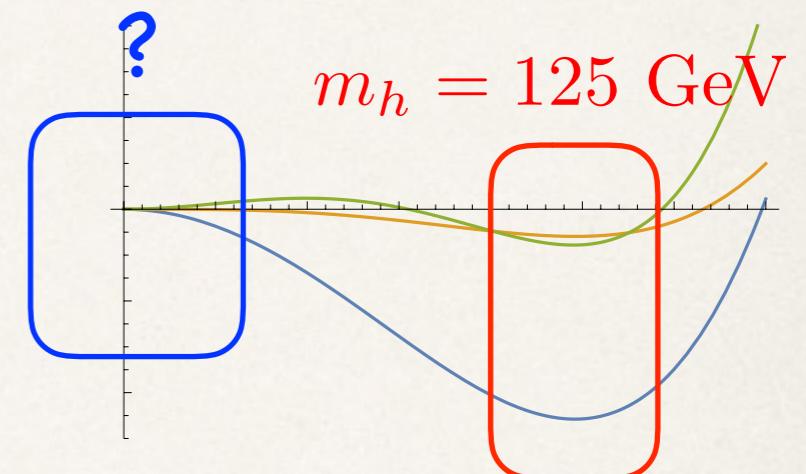
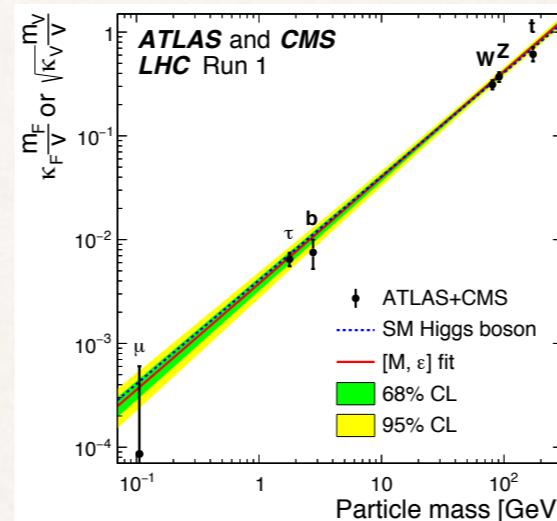
- Introduction
- muon g-2 and $h \rightarrow \mu\tau$ in a 2 Higgs doublet model
- Electroweak baryogenesis (EWBG)
 - Electroweak phase transition (EWPT) and sphaleron
 - Baryon asymmetry
- Summary

Introduction

problems after the Higgs discovery

Does the 125 GeV boson **alone** do the following jobs?

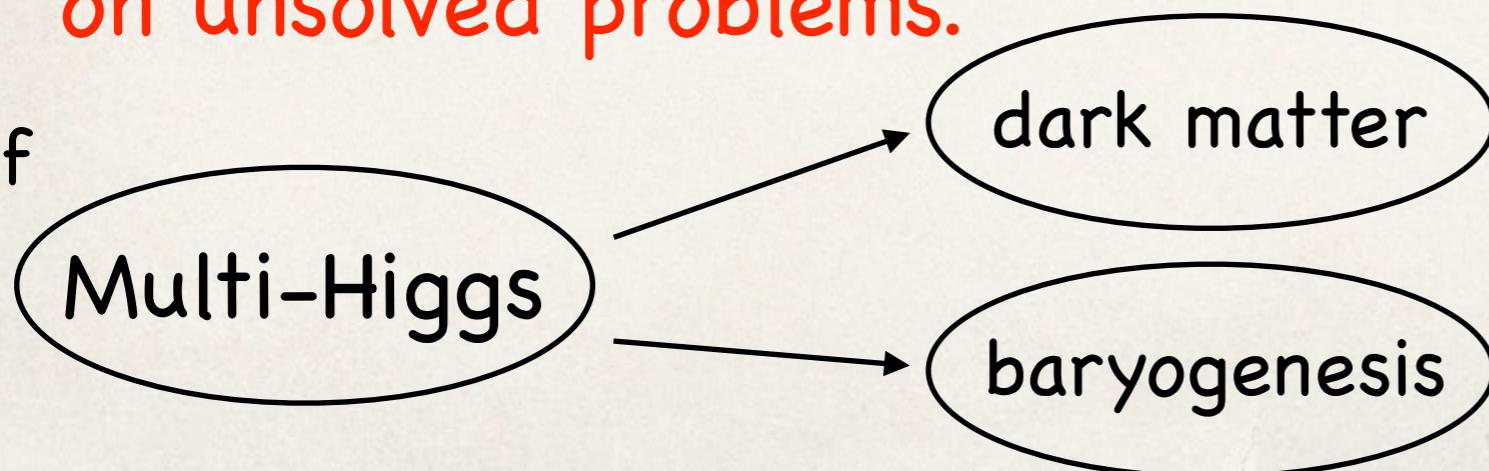
- mass generation
- EW symmetry breaking



Experiments will answer those grand questions in the near future.

Most importantly, those experiments may also shed light on unsolved problems.

If



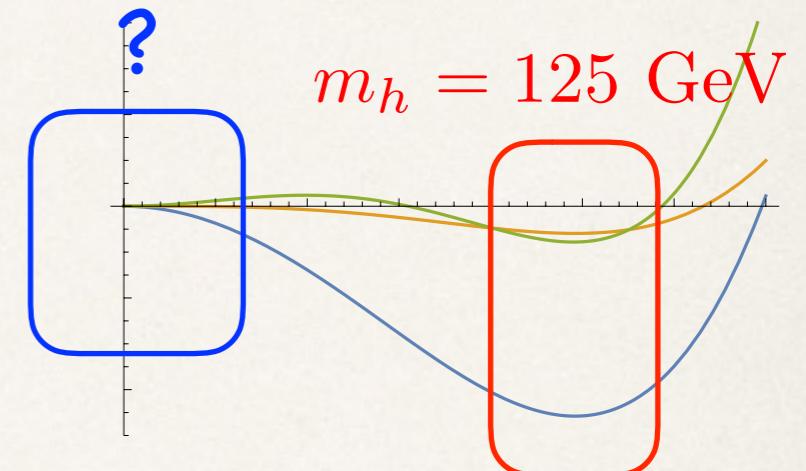
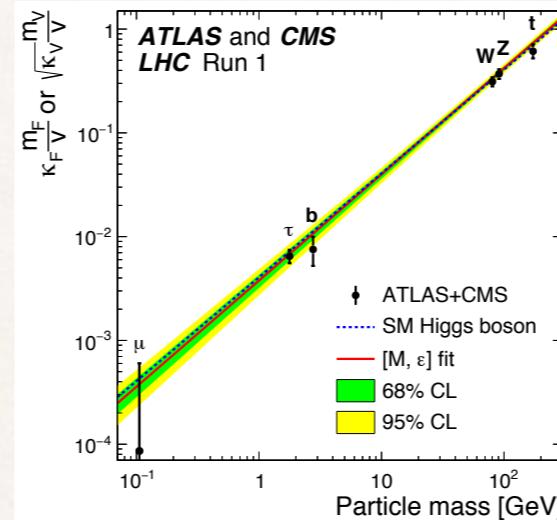
Higgs is a window to new physics.
Let us open the window!!

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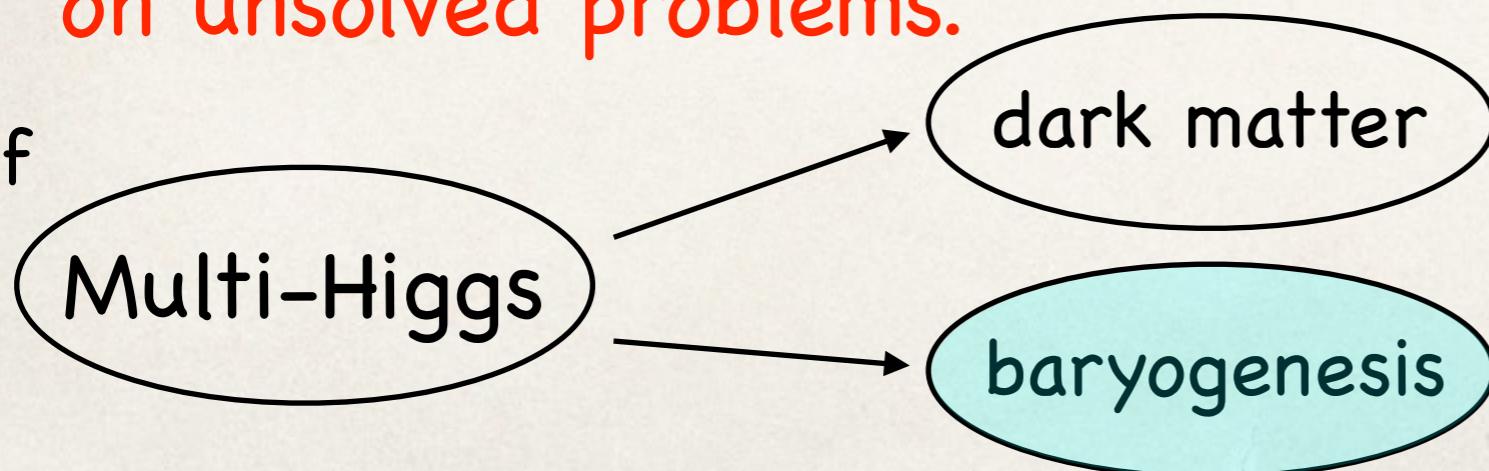
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Hints for new physics?

muon g-2

$$\delta a_\mu = a_\mu^{\text{EXP}} - a_\mu^{\text{SM}} = (26.1 \pm 8.0) \times 10^{-10}$$

Hagiwara et al, 1105.3149.

3.3σ excess

$h \rightarrow \mu\tau$

CMS: $\text{Br}(h \rightarrow \mu\tau) = (0.84^{+0.39}_{-0.37})\%$ 1502.07400 [PLB] 2.4σ excess

Atlas: $\text{Br}(h \rightarrow \mu\tau) = (0.53 \pm 0.51)\%$ 1604.07730

We discuss baryogenesis, g-2, $h \rightarrow \mu\tau$ in a **2 Higgs doublets model (2HDM)** with lepton flavor violation (LFV).

2 Higgs doublet model (2HDM)

Higgs potential:

$$\begin{aligned} V_0(\Phi_1, \Phi_2) = & m_1^2 \Phi_1^\dagger \Phi_1 + m_2^2 \Phi_2^\dagger \Phi_2 - (m_3^2 \Phi_1^\dagger \Phi_2 + \text{h.c.}) \\ & + \frac{\lambda_1}{2} (\Phi_1^\dagger \Phi_1)^2 + \frac{\lambda_2}{2} (\Phi_2^\dagger \Phi_2)^2 + \lambda_3 (\Phi_1^\dagger \Phi_1)(\Phi_2^\dagger \Phi_2) + \lambda_4 (\Phi_1^\dagger \Phi_2)(\Phi_2^\dagger \Phi_1) \\ & + \left[\frac{\lambda_5}{2} (\Phi_1^\dagger \Phi_2)^2 + \left\{ \lambda_6 (\Phi_1^\dagger \Phi_1) + \lambda_7 (\Phi_2^\dagger \Phi_2) \right\} (\Phi_1^\dagger \Phi_2) + \text{h.c.} \right], \end{aligned}$$

$$m_3^2, \lambda_5, \lambda_6, \lambda_7 \in \mathbb{C}$$

Higgs fields: $\Phi_i(x) = \begin{pmatrix} \phi_i^+(x) \\ \frac{1}{\sqrt{2}}(v_i + h_i(x) + ia_i(x)) \end{pmatrix}, \quad i = 1, 2.$

Assumption: CP is NOT violated by the Higgs potential and VEVs.

inputs: $\sin(\beta - \alpha), \tan \beta, m_H, m_A, m_{H^\pm}, M^2 = \frac{m_3^2}{\sin \beta \cos \beta}, \lambda_{6,7}$

2 Higgs doublet model (2HDM)

Lepton Yukawa couplings (Higgs basis):

$$-\mathcal{L}_Y = \bar{l}_{iL} (Y_1 \Phi_1 + Y_2 \Phi_2)_{ij} e_{jR} + \text{h.c.}$$

$$\begin{aligned} & \ni \bar{e}_{iL} \left[\frac{y_i}{\sqrt{2}} \delta_{ij} s_{\beta-\alpha} + \frac{1}{\sqrt{2}} \rho_{ij} c_{\beta-\alpha} \right] e_{jR} h \\ & + \bar{e}_{iL} \left[\frac{y_i}{\sqrt{2}} \delta_{ij} c_{\beta-\alpha} - \frac{1}{\sqrt{2}} \rho_{ij} s_{\beta-\alpha} \right] e_{jR} H + \frac{i}{\sqrt{2}} \bar{e}_{iL} \rho_{ij} e_{jR} A + \text{h.c.} , \end{aligned}$$

- LFV comes from the off-diagonal entries of ρ_{ij} .
- ρ_{ij} are generally complex. $\rho_{ij} \in \mathbb{C} \Rightarrow \text{CPV}$
 $\Rightarrow \text{Baryogenesis!!}$

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h-> $\mu\tau$ and muon g-2

In 2HDM, it is easy to accommodate both h-> $\mu\tau$ and muon g-2.

[Y. Omura, E.S., K.Tobe, JHEP052015028, PRD94,055019(2016)]

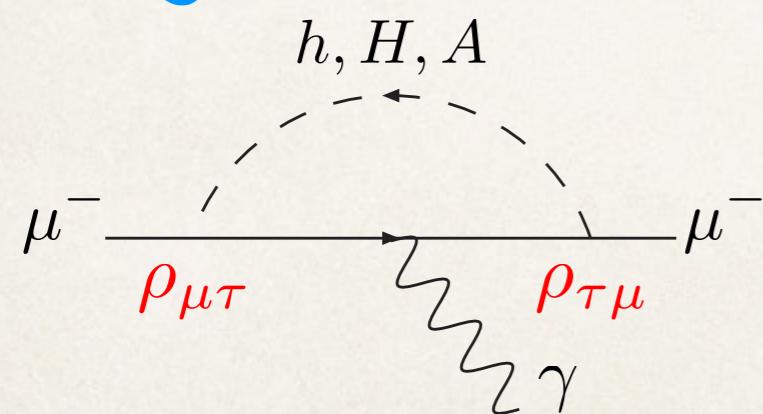
h-> $\mu\tau$

$$\text{Br}(h \rightarrow \mu\tau) = \frac{m_h(|\rho_{\mu\tau}|^2 + |\rho_{\tau\mu}|^2)c_{\beta-\alpha}^2}{16\pi\Gamma_h}, \quad \Gamma_h = 4.1 \text{ MeV}$$

$$\sqrt{\frac{|\rho_{\mu\tau}|^2 + |\rho_{\tau\mu}|^2}{2}} \simeq 0.26 \left(\frac{0.01}{|c_{\beta-\alpha}|} \right) \sqrt{\frac{\text{Br}(h \rightarrow \mu\tau)}{0.84 \times 10^{-2}}}$$

muon g-2

$$\delta a_\mu = a_\mu^{\text{EXP}} - a_\mu^{\text{SM}} = (26.1 \pm 8.0) \times 10^{-10}$$



$$\delta a_\mu = \frac{m_\mu m_\tau \text{Re}(\rho_{\mu\tau}\rho_{\tau\mu})}{16\pi^2}$$

$$\times \left[\frac{c_{\beta-\alpha}^2 f(r_h)}{m_h^2} + \frac{s_{\beta-\alpha}^2 f(r_H)}{m_H^2} - \frac{f(r_A)}{m_A^2} \right]$$

$$f(r) \simeq \ln \frac{1}{r} - \frac{3}{2}$$

Needs: $\rho_{\mu\tau}=\rho_{\tau\mu}\neq 0$ and nonzero mass differences in (m_h, m_H, m_A)

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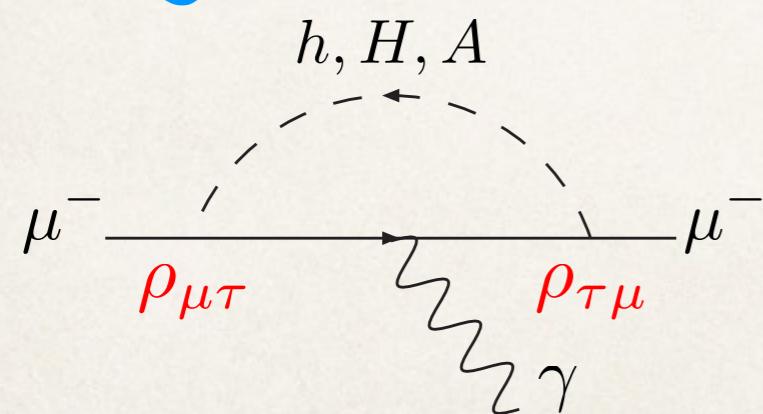
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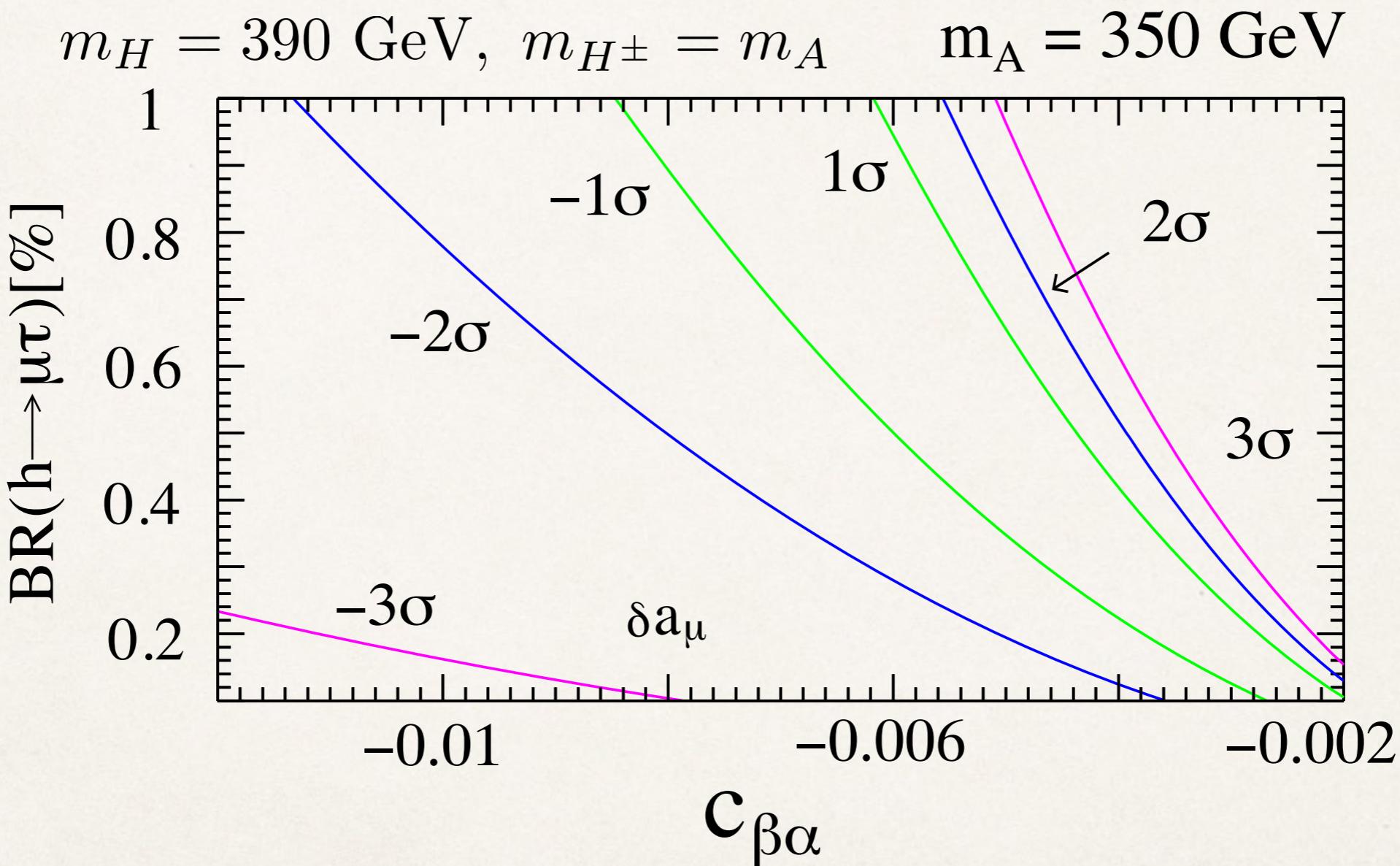
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$h \rightarrow \mu\tau$ and muon g-2

[Y. Omura, E.S., K. Tobe, JHEP052015028, PRD94, 055019 (2016)]



- $\mu\tau$ flavor violation can explain both $h \rightarrow \mu\tau$ and g-2.

Baryogenesis

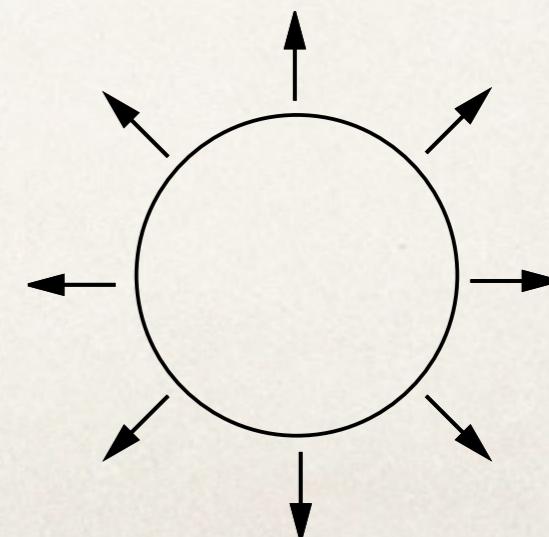
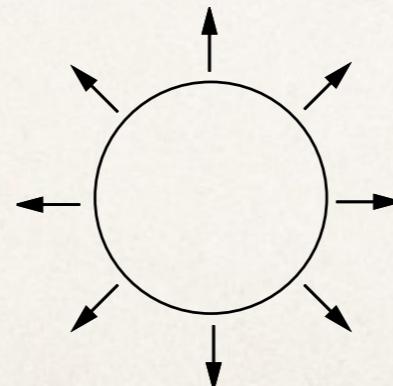
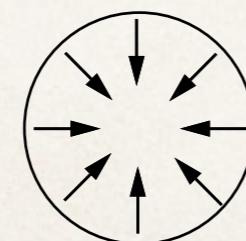
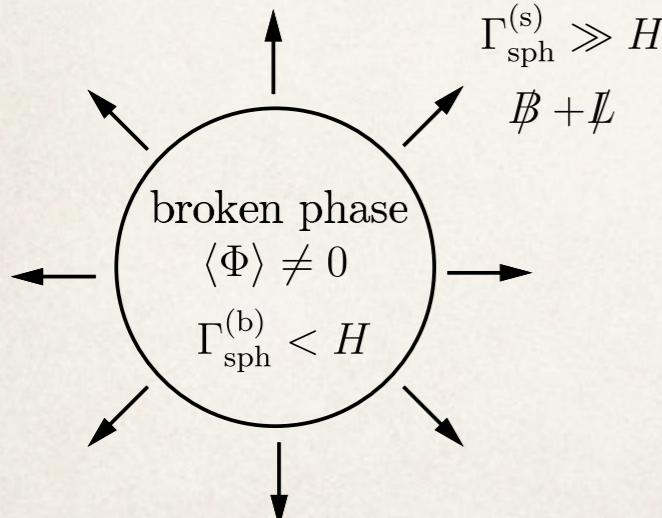
Electroweak baryogenesis

[Kuzmin, Rubakov, Shaposhnikov, PLB155,36 ('85)]

Sakharov's conditions

- * **B violation:** anomalous (sphaleron) process $0 \leftrightarrow \sum_{i=1,2,3} (3q_L^i + l_L^i)$ (LH fermions)
- * **C violation:** chiral gauge interaction
- * **CP violation:** KM phase and/or other sources in beyond the SM
- * **Out of equilibrium:** 1st order EW phase transition (EWPT) with expanding bubble walls

symmetric phase $\langle \Phi \rangle = 0$



BAU can arise by the growing bubbles.

$$\Gamma_B^{(b)} < H$$

B-changing rate in the broken phase is

$$\Gamma_B^{(b)} \simeq (\text{prefactor}) e^{-E_{\text{sph}}/T}$$

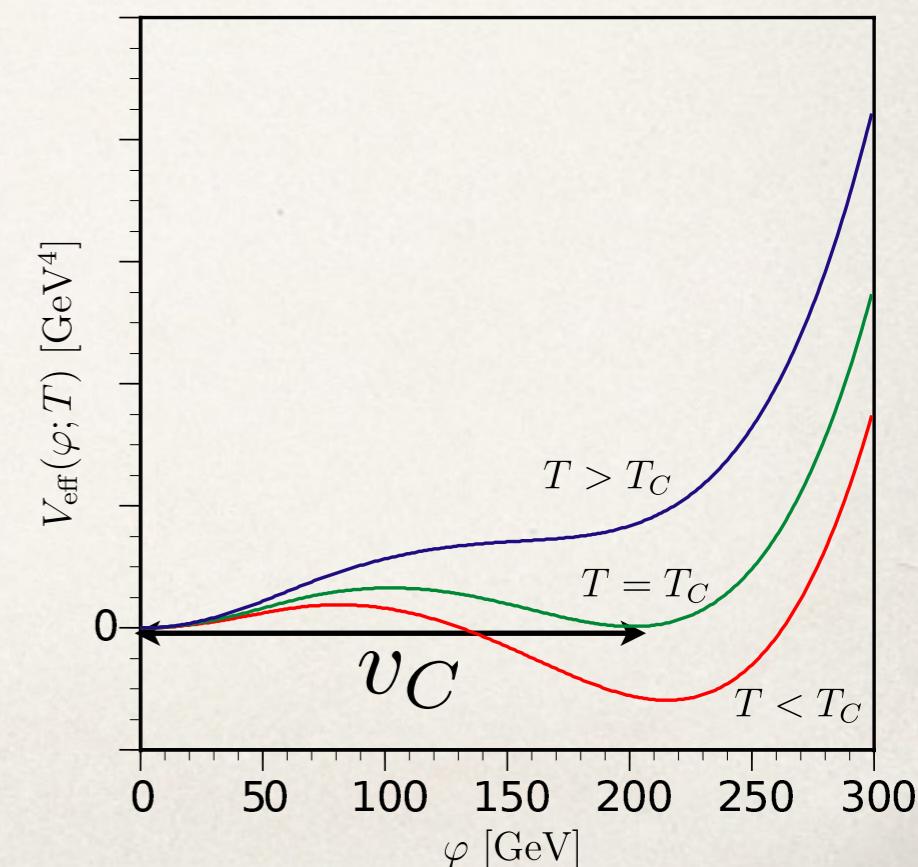
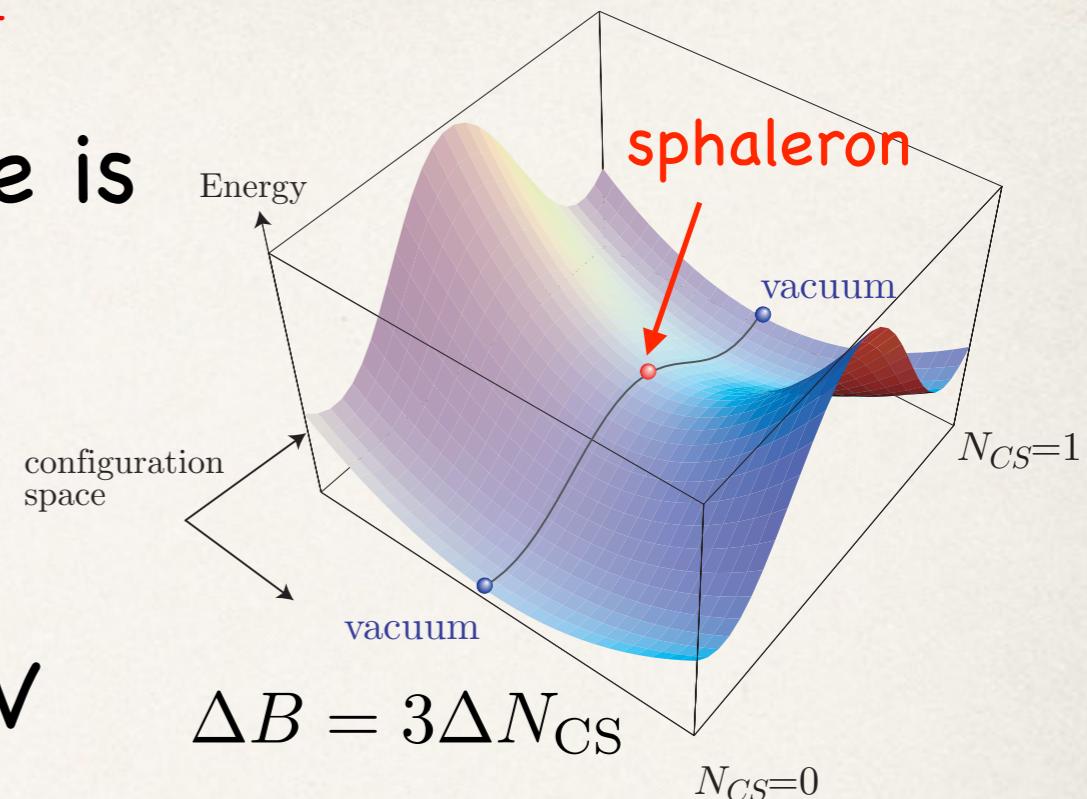
E_{sph} is proportional to the Higgs VEV

$$E_{\text{sph}} \propto v(T)$$

what we need is

large Higgs VEV after the EWPT

→ EWPT has to be “strong” 1st order!!



$$\Gamma_B^{(b)} < H$$

$$\Gamma_B^{(b)}(T) \simeq (\text{prefactor}) e^{-E_{\text{sph}}(T)/T} < H(T) \simeq 1.66 \sqrt{g_*} T^2 / m_P$$

$E_{\text{sph}}(T) = 4\pi v(T) \mathcal{E} / g_2$ (g_2 : SU(2) gauge coupling),

→ $\frac{v(T)}{T} > \frac{g_2}{4\pi \mathcal{E}} [42.97 + \text{log corrections}] = \zeta_{\text{sph}}$

- dominant effect: sphaleron energy.

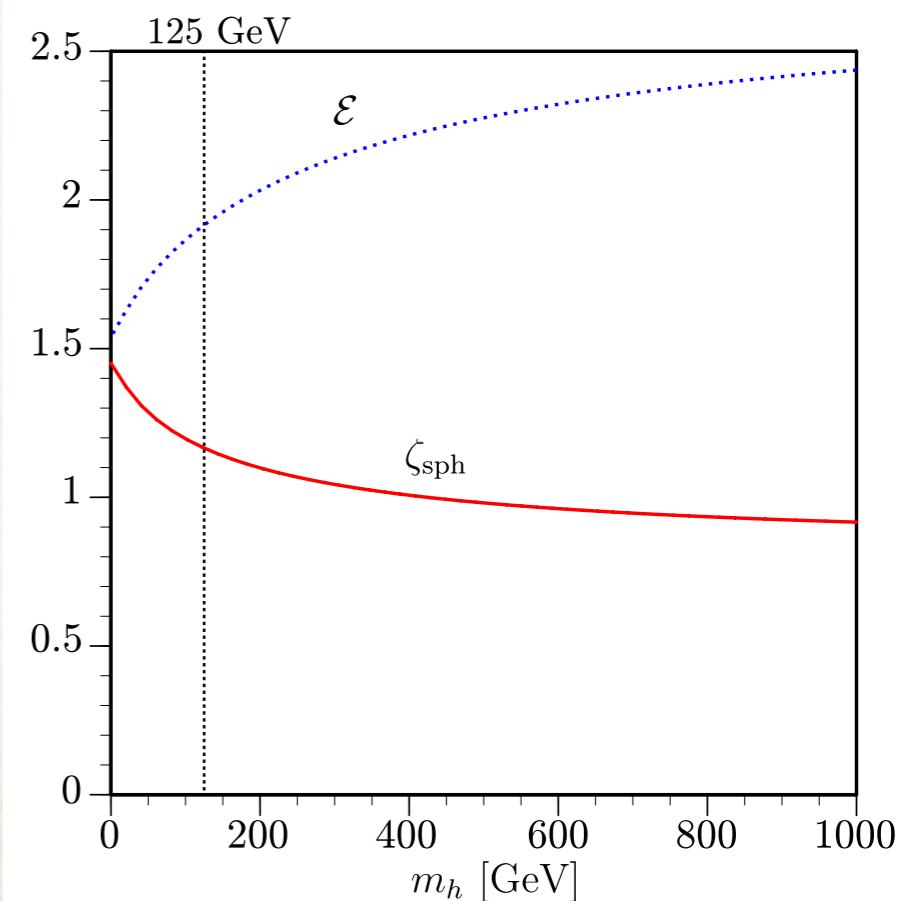
For 2HDM with alignment limit:

$$\mathcal{E} \rightarrow \mathcal{E}_{\text{SM}} = 1.92$$

@tree level

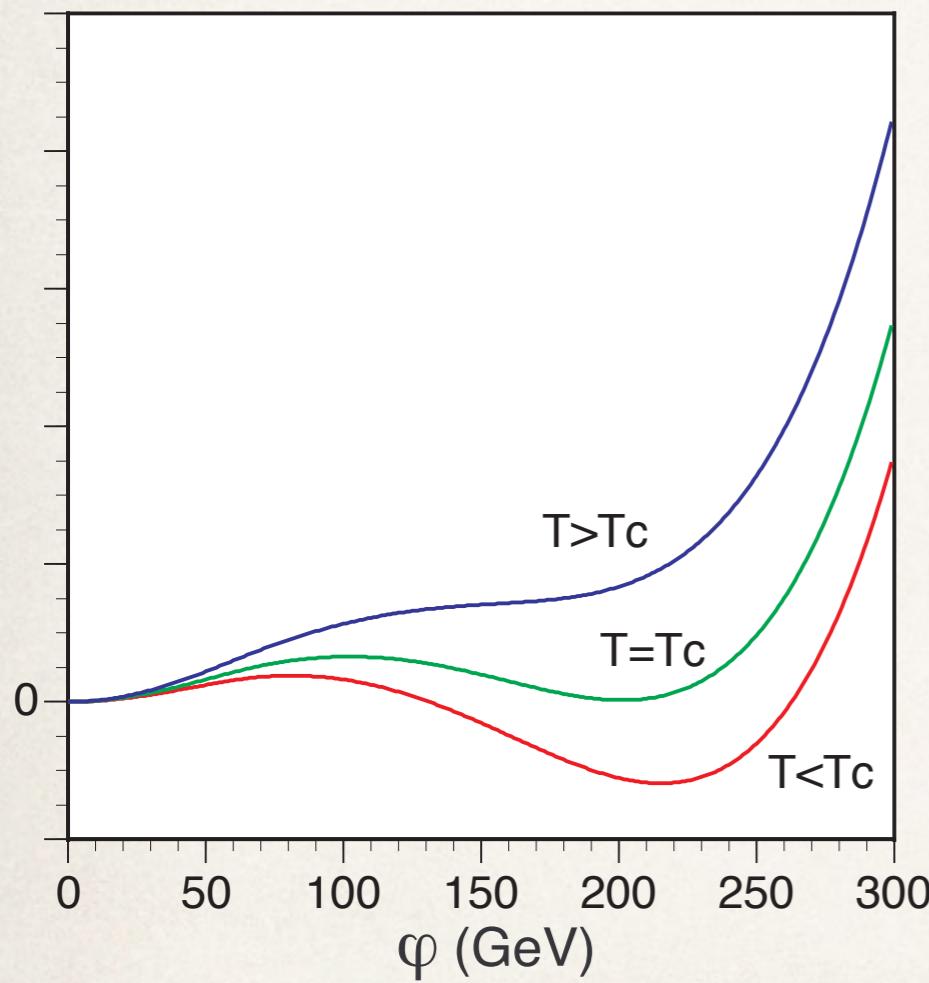
$$\frac{v(T)}{T} > 1.17$$

For a band structure effect on Γ_B ,
see [K.Funakubo, K.Fuyuto, E.S., arXiv:1612.05431]



1st-order phase transition

$$V_{\text{eff}} \simeq D(T^2 - T_0^2)\varphi^2 - ET\varphi^3 + \frac{\lambda_T}{4}\varphi^4 \xrightarrow{T=T_C} \frac{\lambda_{T_C}}{4}\varphi^2(\varphi - v_C)^2$$



$$v_C = \frac{2ET_C}{\lambda_{T_C}} \quad \Rightarrow \quad \frac{v_C}{T_C} = \frac{2E}{\lambda_{T_C}}$$

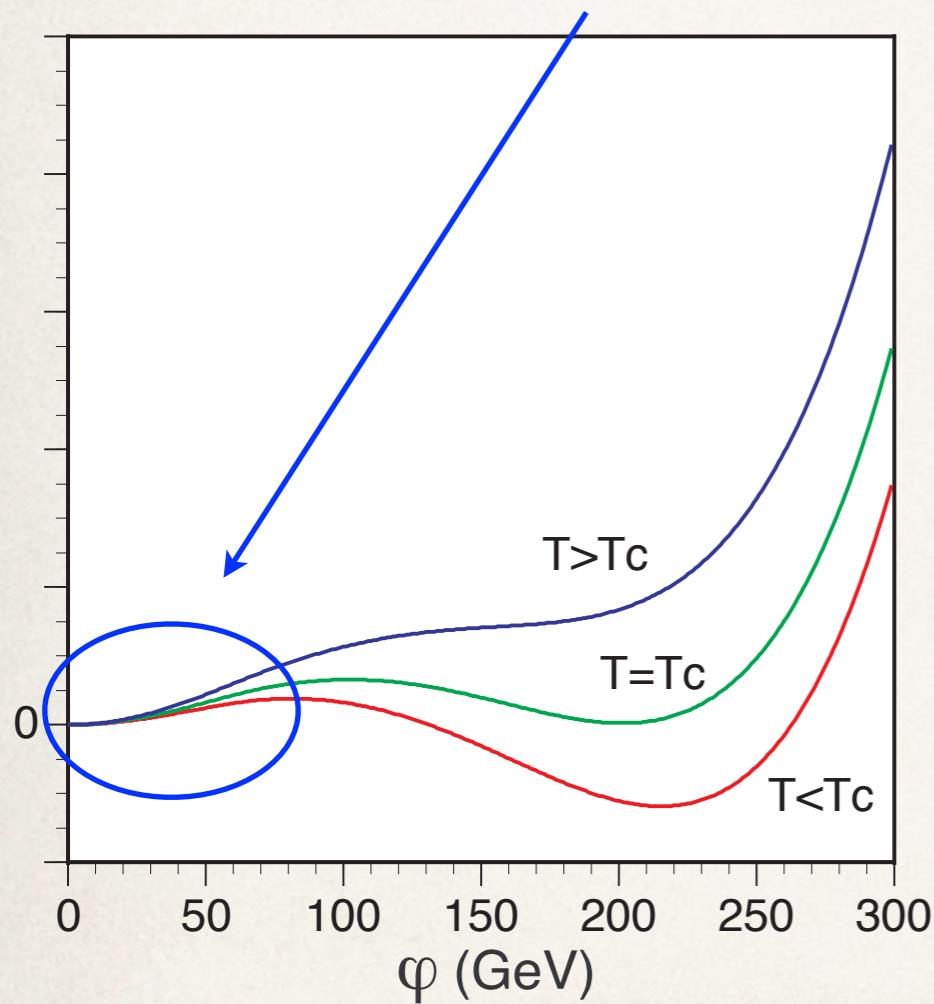
- Heavy Higgs loops can enhance E .

$$m_{i=H,A,H^\pm}^2 = M^2 + \tilde{\lambda}_i \varphi^2$$

$$V_{\text{eff}} \ni \begin{cases} -\tilde{\lambda}^{3/2}T\varphi^3 \left(1 + \frac{M^2}{\tilde{\lambda}\varphi^2}\right)^{3/2}, & \text{for } M^2 \ll \tilde{\lambda}\varphi^2, \\ -|M|^3T \left(1 + \frac{\tilde{\lambda}\varphi^2}{M^2}\right)^{3/2}, & \text{for } M^2 \gtrsim \tilde{\lambda}\varphi^2. \end{cases}$$

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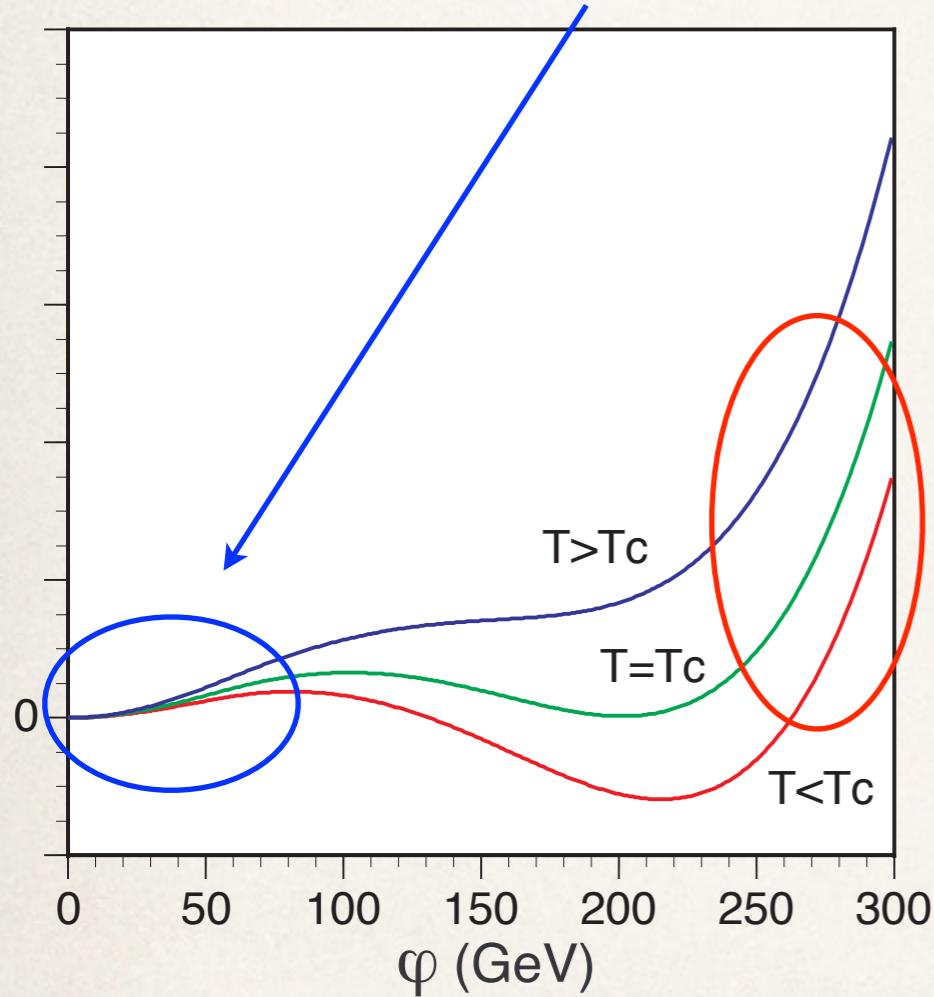
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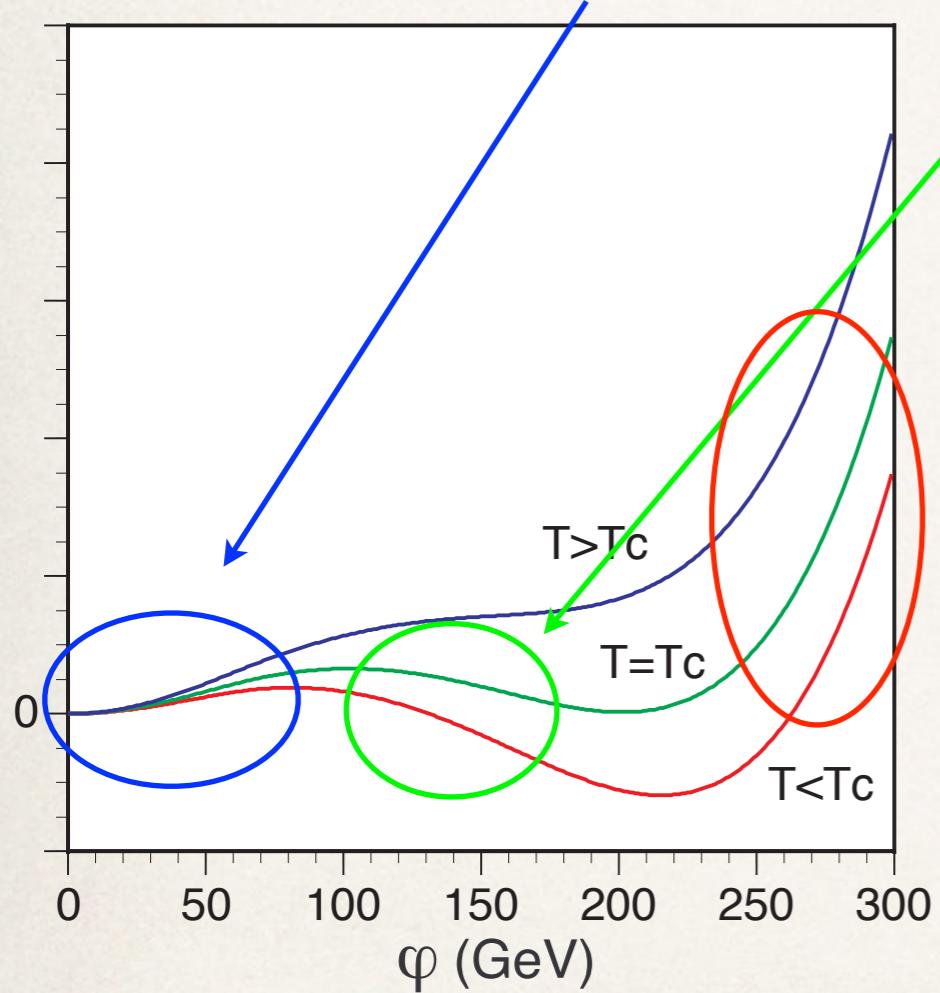
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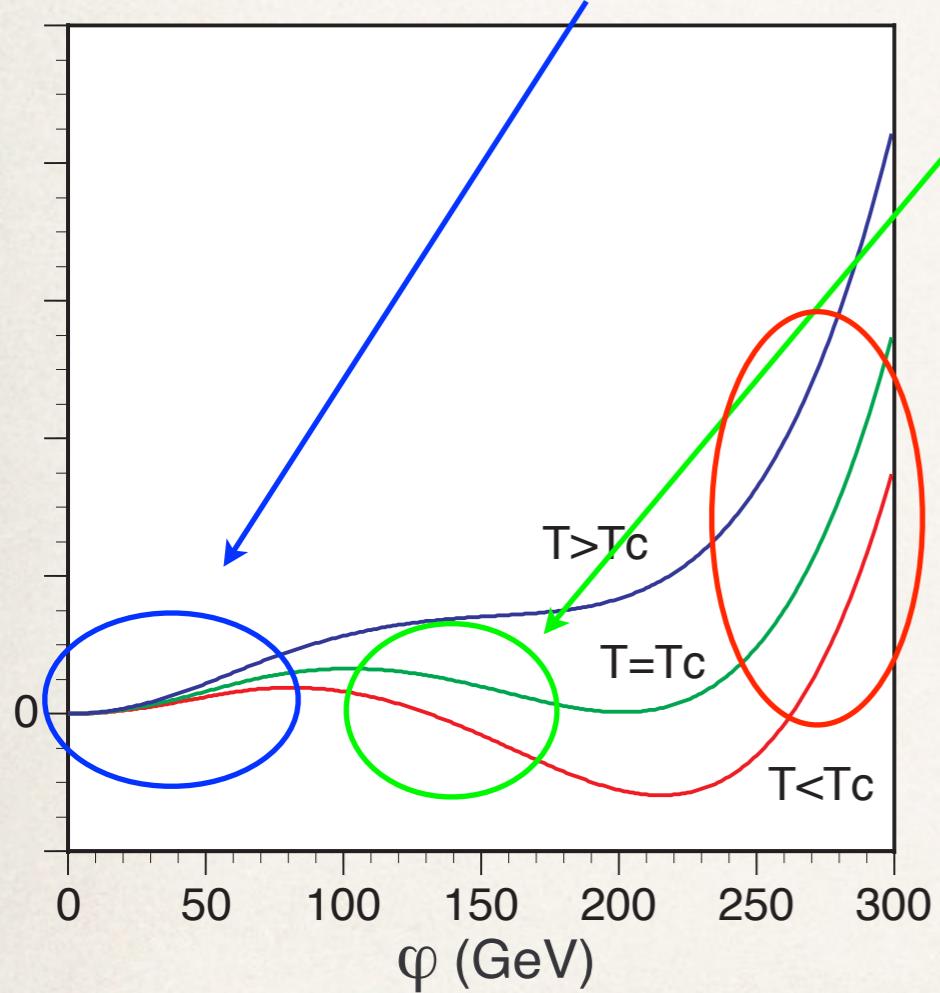
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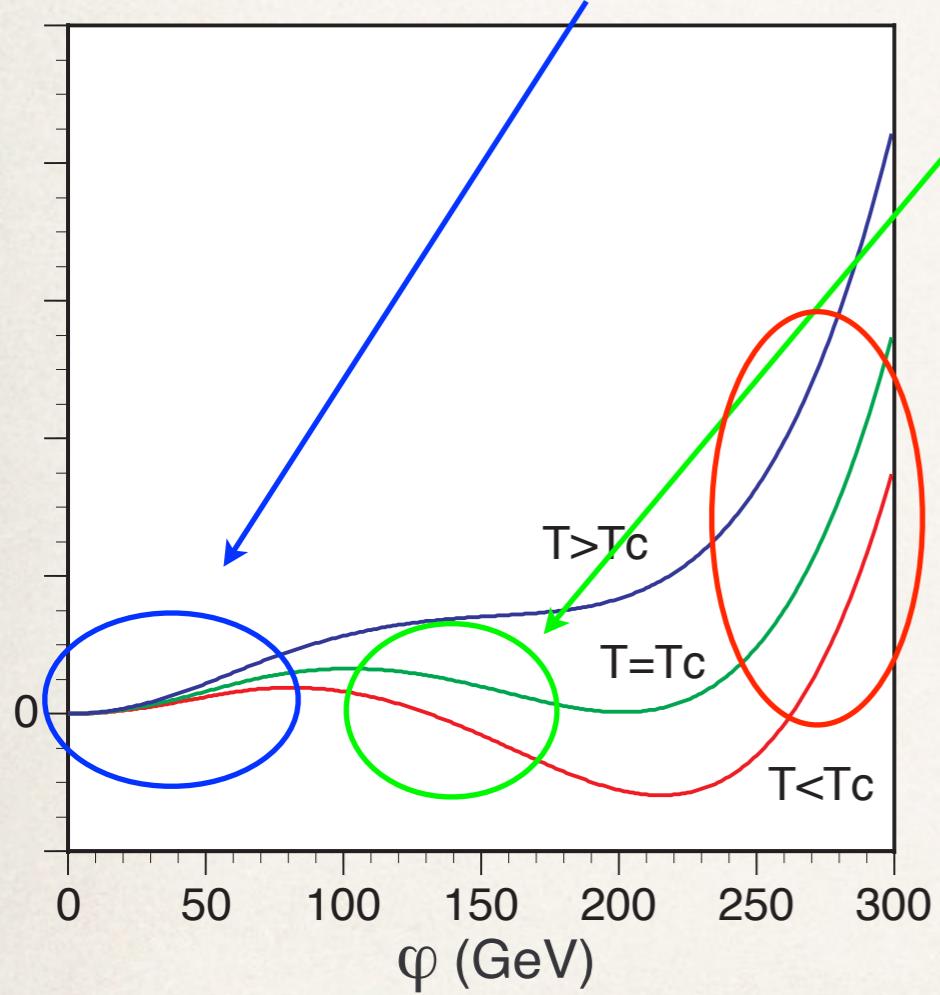
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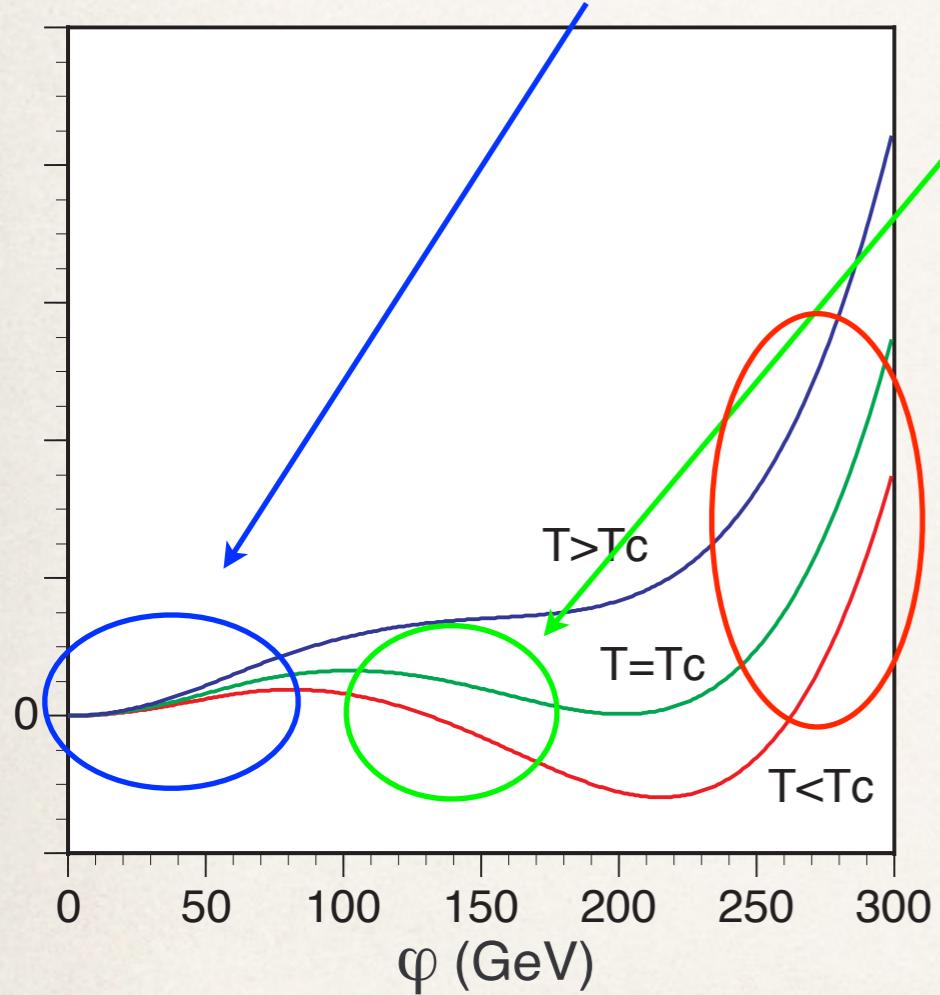
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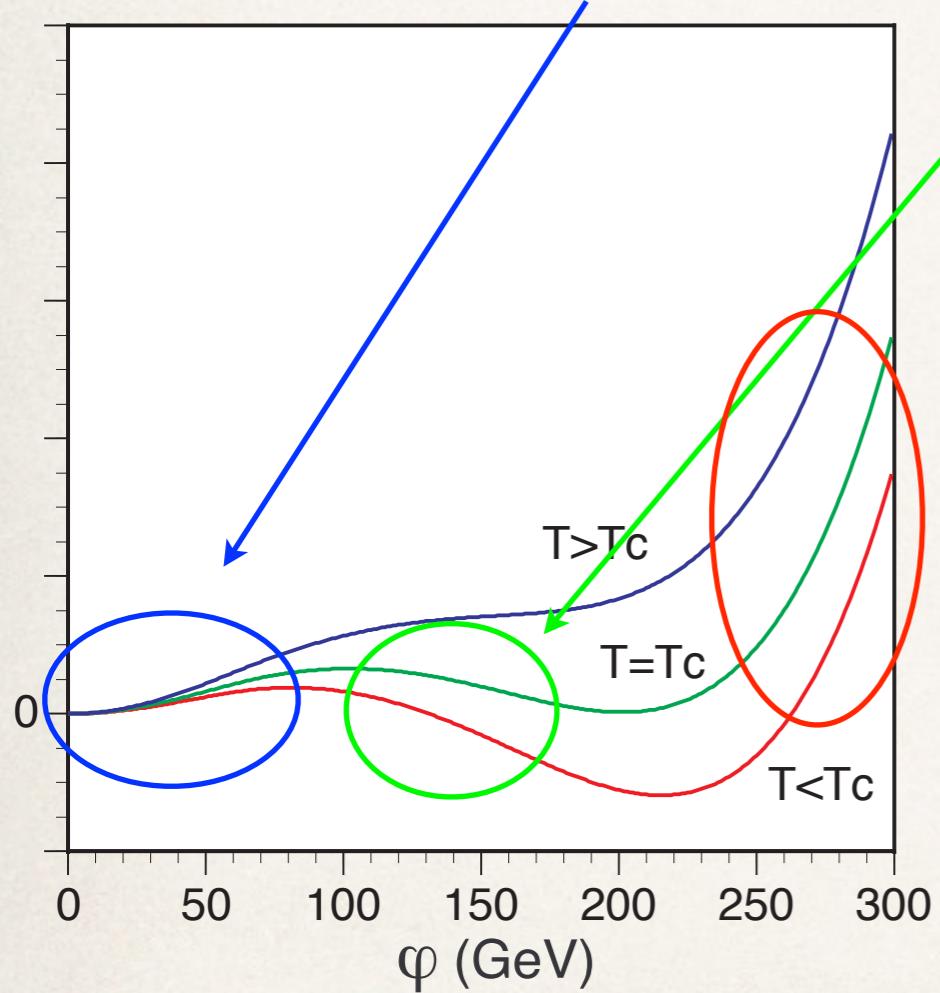
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decoupling

Non-decoupling heavy Higgs bosons play a central role in enhancing E .

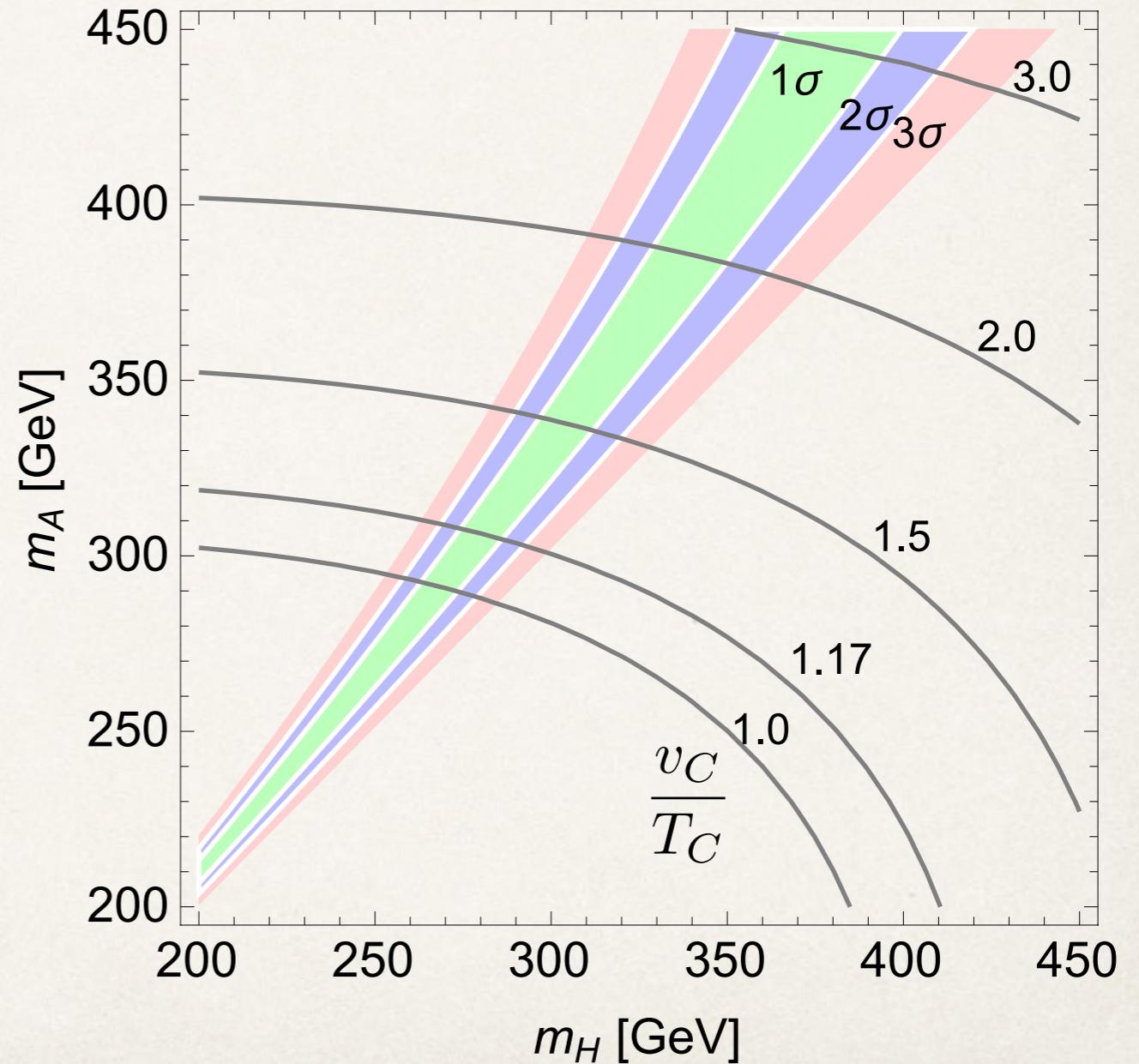
EWBG and LFV

[C-W. Chiang, K.Fuyuto, E.S., arXiv:1607.07316 (PLB)]

benchmark point:

- $\text{Br}(h \rightarrow \mu\tau) = 0.84\%$
- g-2 favored region
 $m_A \gtrsim m_H$
for $\text{Re}(\rho_{\tau\mu}\rho_{\mu\tau}) > 0$.
- EWBG-viable region
 $v_C/T_C > 1.17$

$m_A = m_{H^\pm}$, $M = 100$ GeV, $\tan \beta = 1$, $c_{\beta-\alpha} = 0.006$
 $|\rho_{\tau\mu}| = |\rho_{\mu\tau}|$, $\phi_{\tau\mu} + \phi_{\mu\tau} = \pi/4$, $\lambda_{6,7} = 0$ $\text{Br}(h \rightarrow \mu\tau) = 0.84\%$



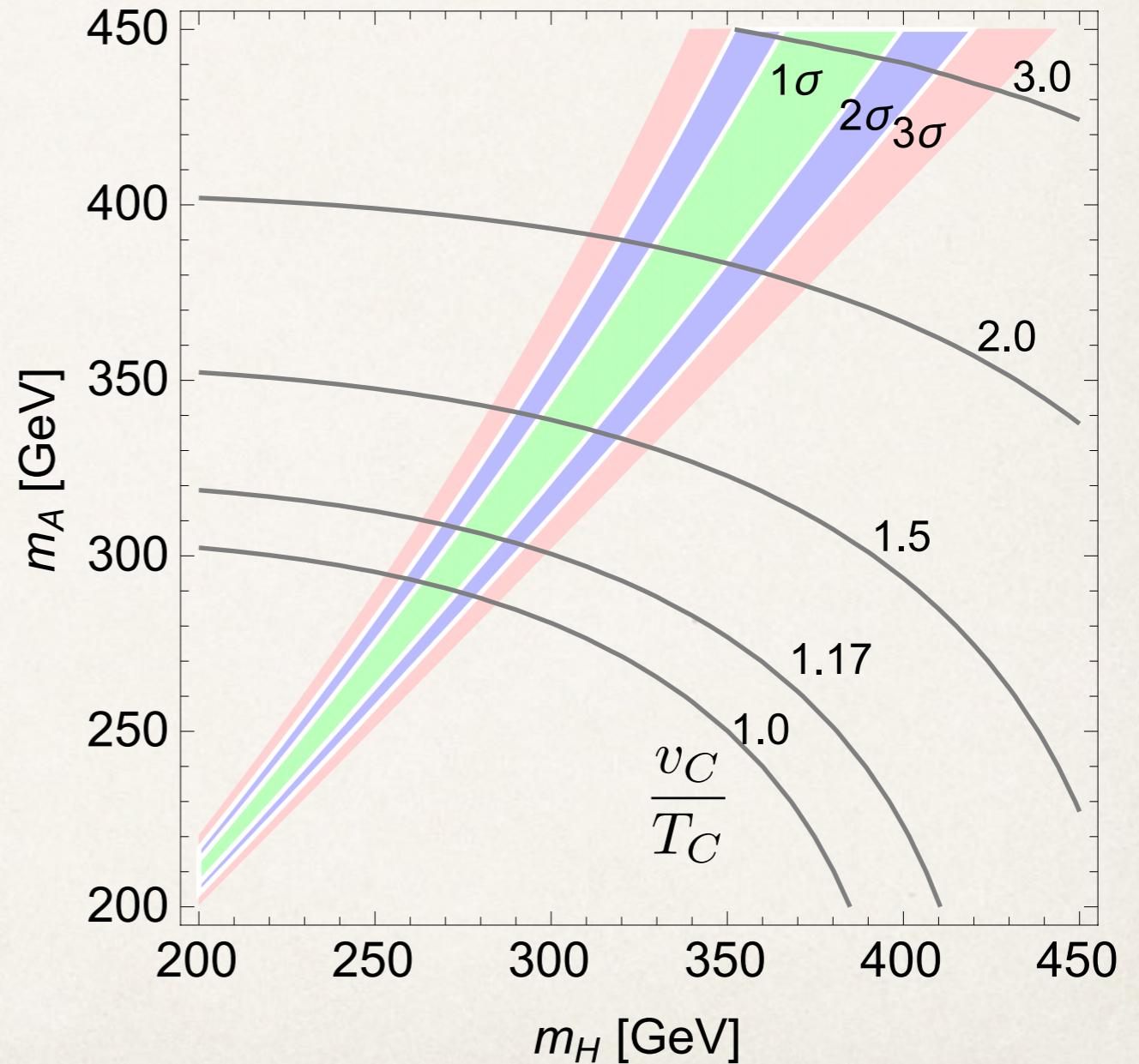
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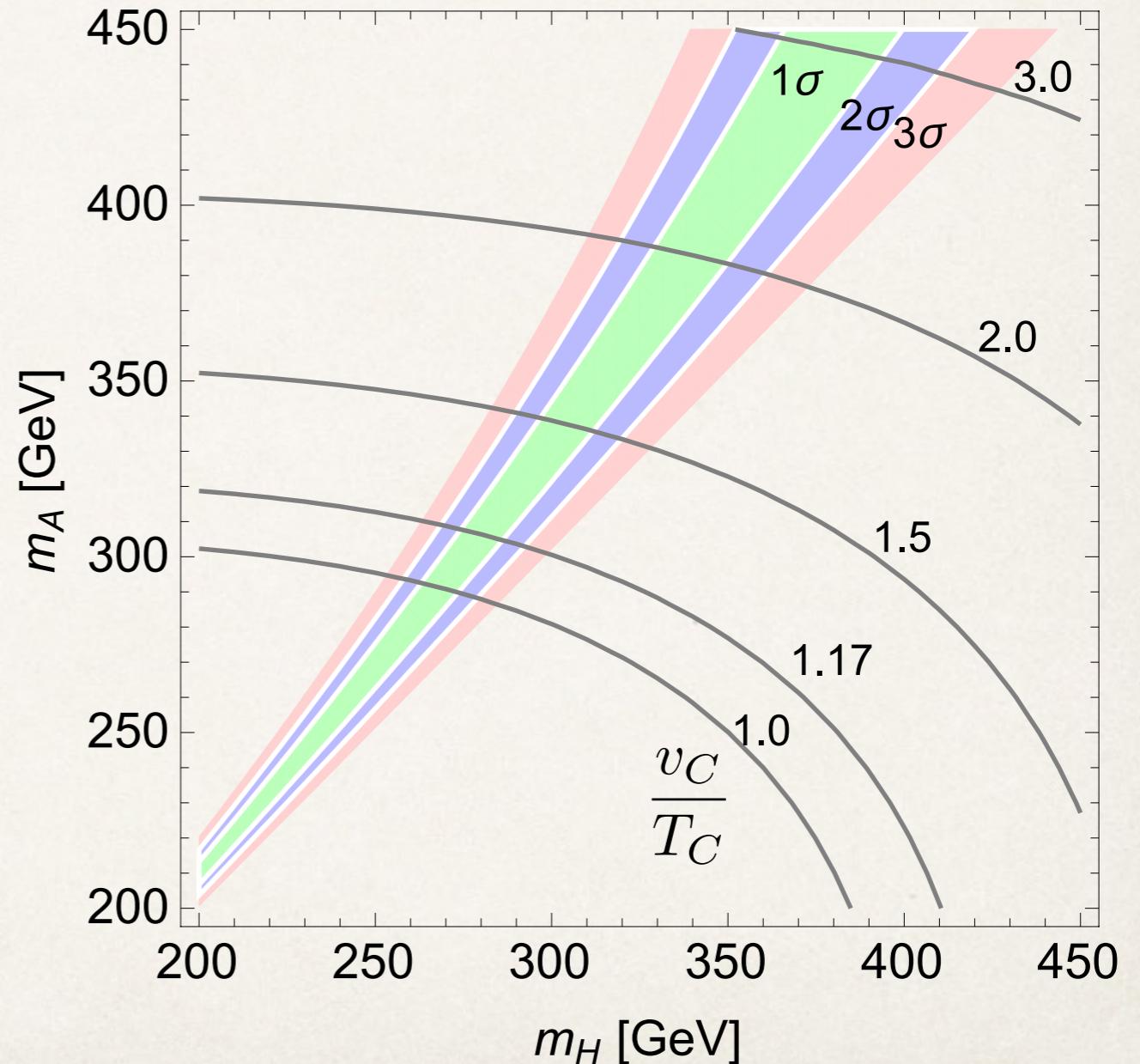
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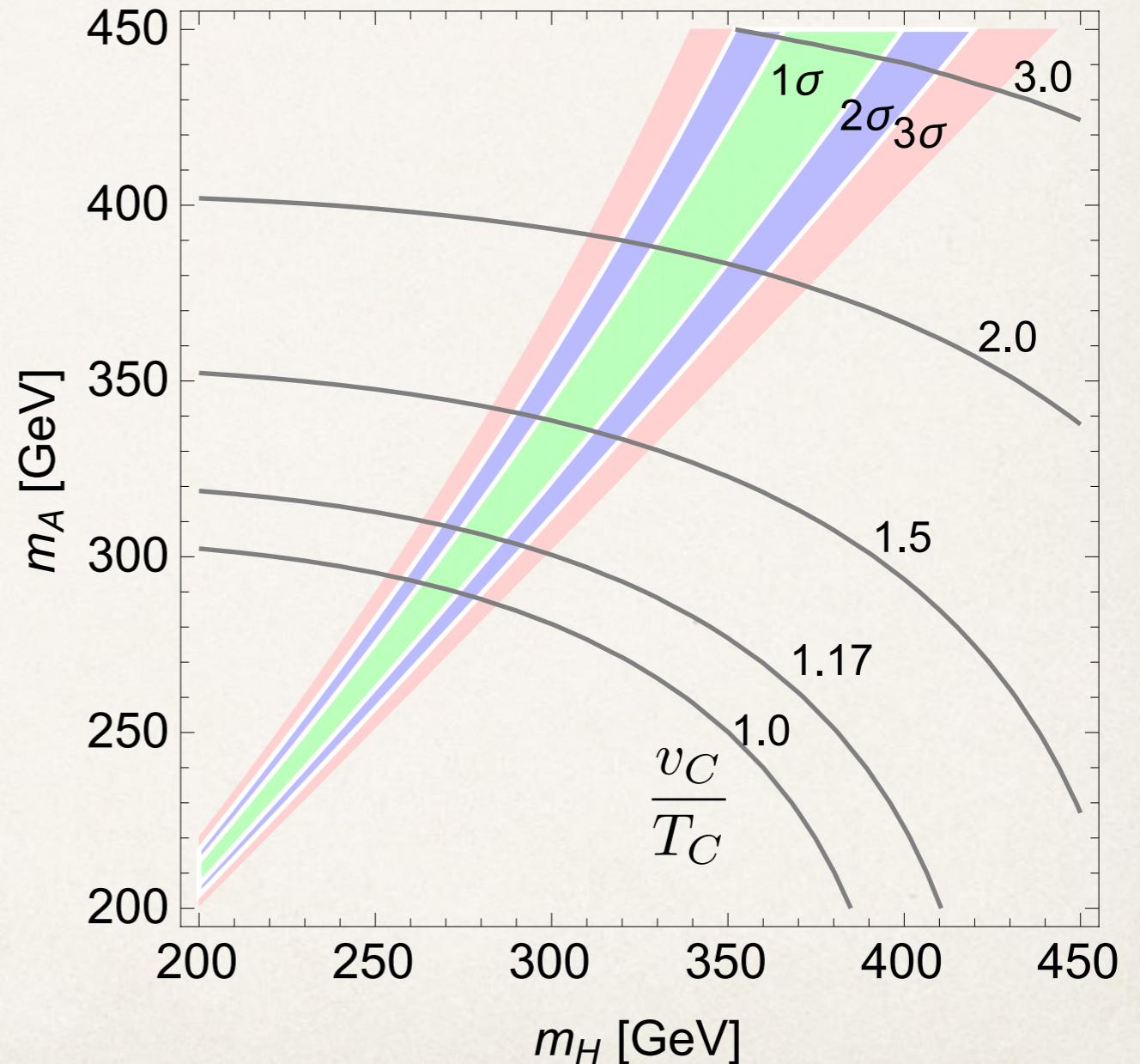
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$$\frac{m_A = m_{H^\pm}, M = 100 \text{ GeV}, \tan \beta = 1, c_{\beta-\alpha} = 0.006}{|\rho_{\tau\mu}| = |\rho_{\mu\tau}|, \phi_{\tau\mu} + \phi_{\mu\tau} = \pi/4, \lambda_{6,7} = 0} \text{ Br}(h \rightarrow \mu\tau) = 0.84 \%$$



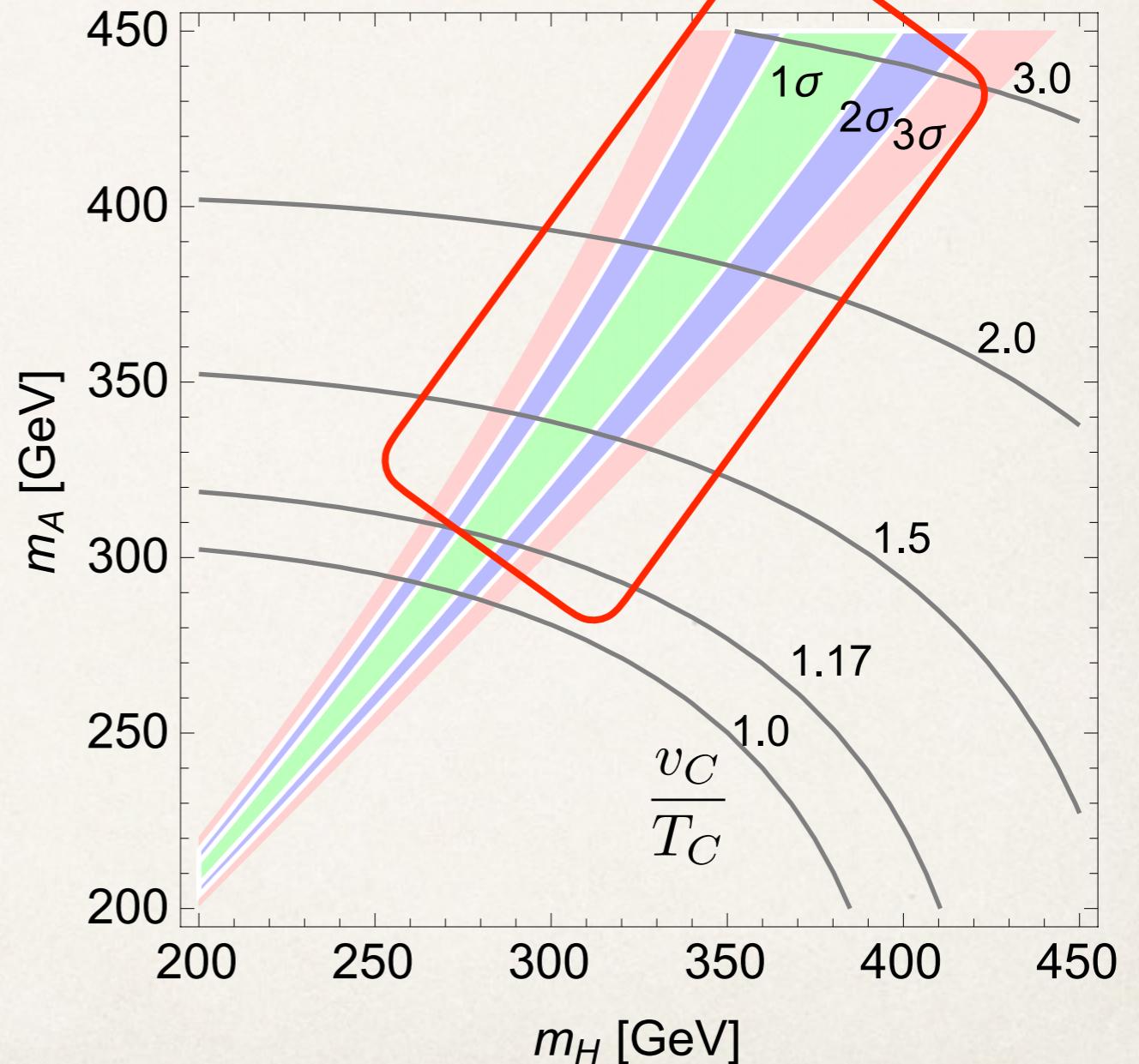
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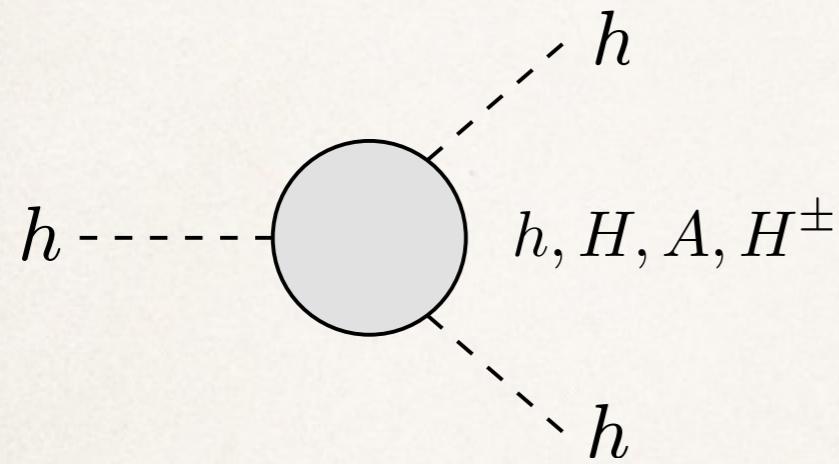
$$\begin{aligned} m_A &= m_{H^\pm}, M = 100 \text{ GeV}, \tan \beta = 1, c_{\beta-\alpha} = 0.006 \\ |\rho_{\tau\mu}| &= |\rho_{\mu\tau}|, \phi_{\tau\mu} + \phi_{\mu\tau} = \pi/4, \lambda_{6,7} = 0 \quad \text{Br}(h \rightarrow \mu\tau) = 0.84 \% \end{aligned}$$



Combined: $300 \text{ GeV} \lesssim m_H \lesssim m_A \lesssim 450 \text{ GeV}$

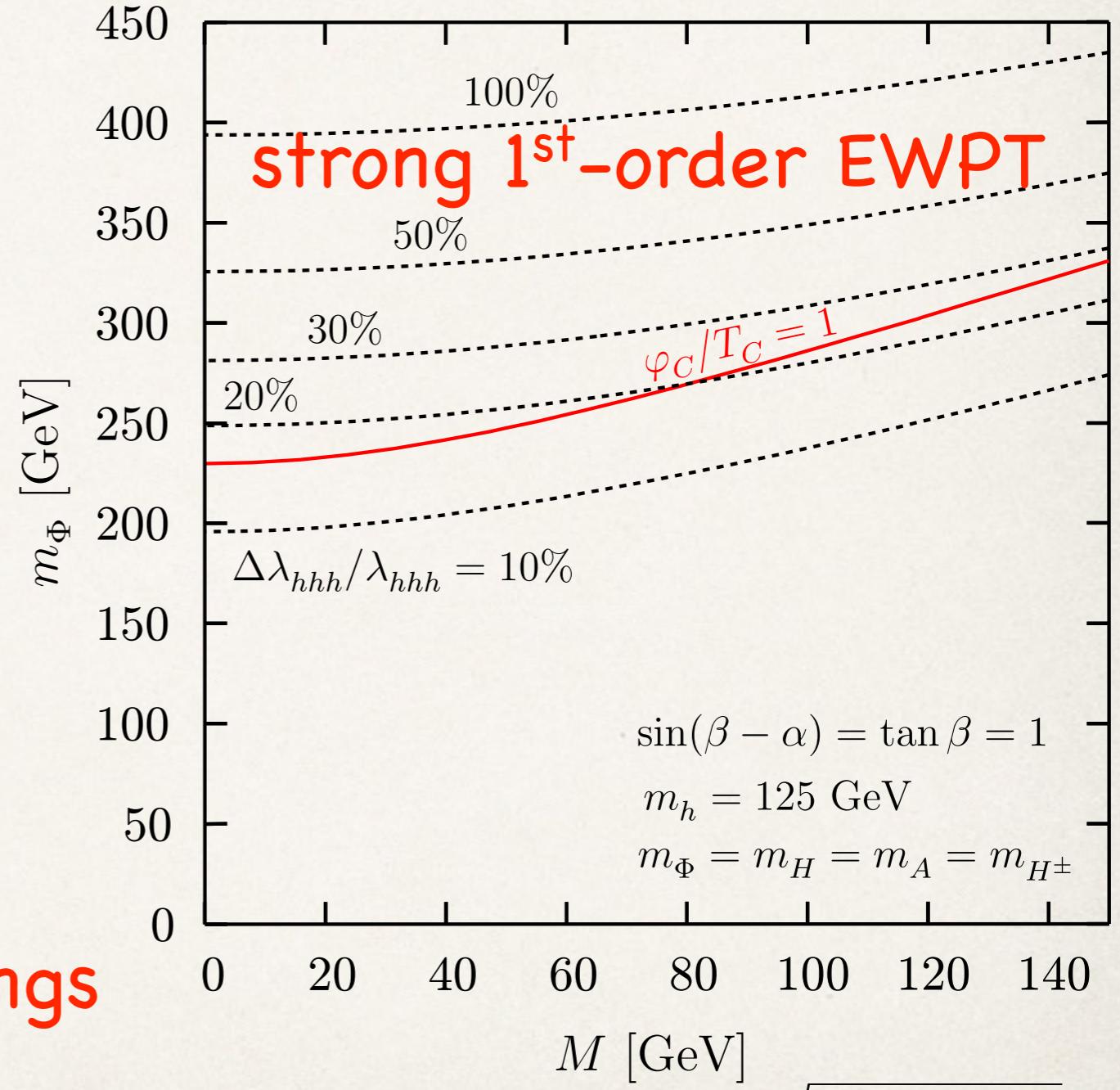
λ_{hhh} in the 2HDM

[update of Kanemura, Okada, E.S., PLB606,(2005)361]



- Non-decoupling heavy Higgs loop can modify λ_{hhh} .

- Even if hVV and hff couplings are SM-like, $\Delta\lambda_{hhh} > (15-20)\%$

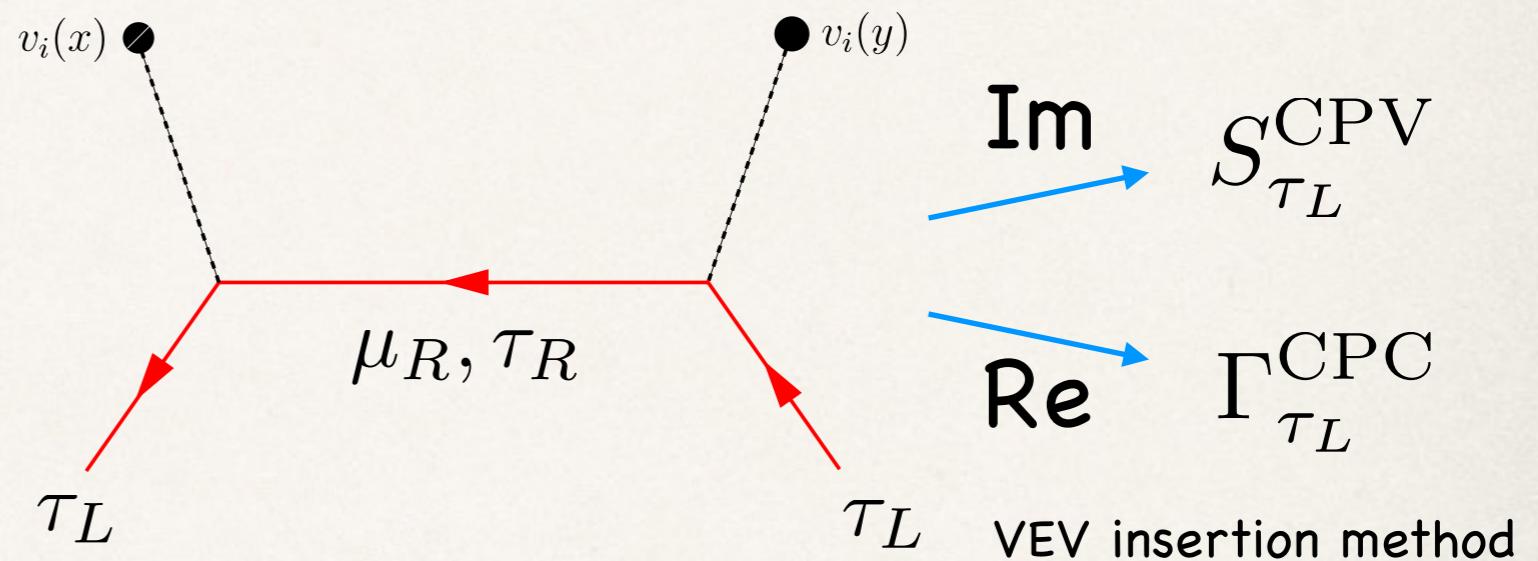
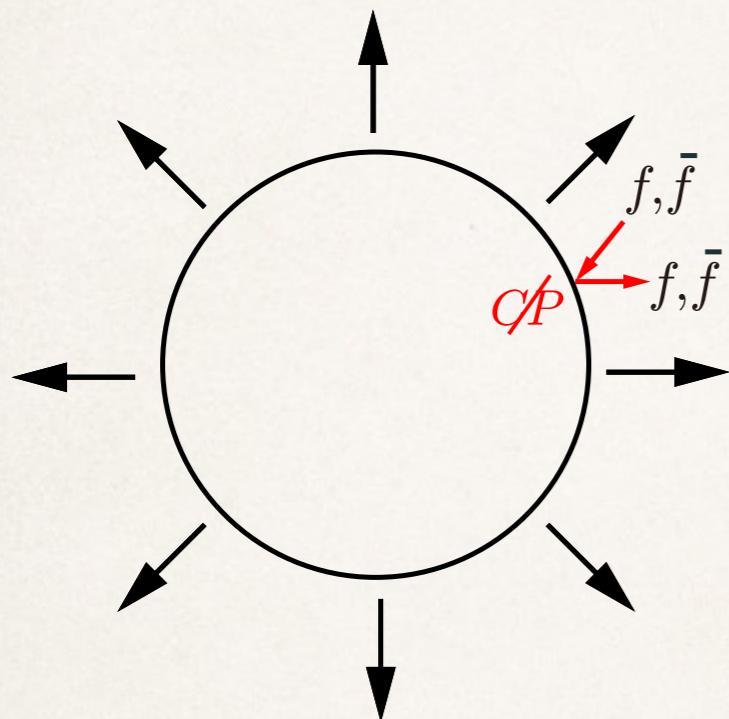


$$M = \sqrt{\frac{m_3^2}{\sin \beta \cos \beta}}$$

Baryon number density

We evaluate BAU using closed-time-path formalism.

$$-\mathcal{L}_Y = \bar{l}_{iL} (Y_1 \Phi_1 + Y_2 \Phi_2)_{ij} e_{jR} + \text{h.c.}$$



$$S_{\tau_L}^{\text{CPV}}(X) = \text{Im} \left[(Y_1)_{\tau j} (Y_2)_{\tau j}^* \right] v^2(X) \partial_{t_X} \beta(X), \quad j = \mu, \tau$$

After solving coupled diffusion equations,

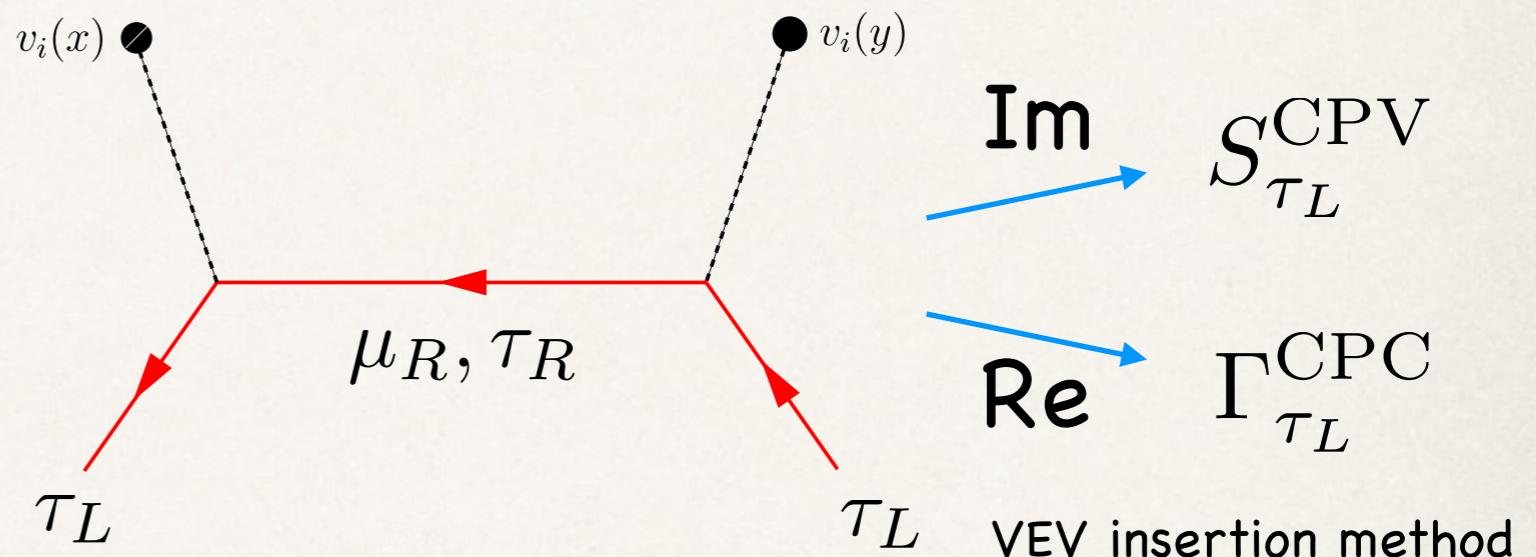
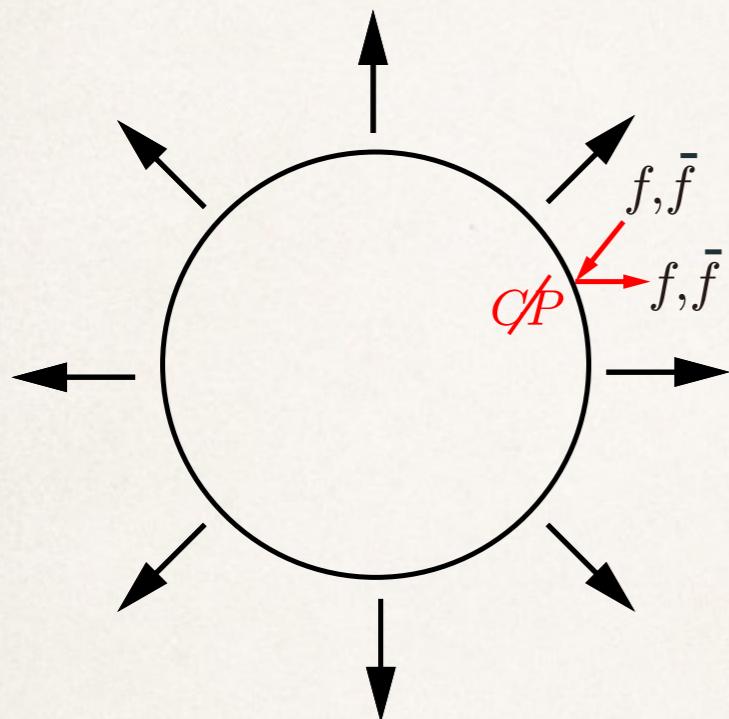
$$n_B \simeq \kappa_B \frac{S^{\text{CPV}}}{\sqrt{\Gamma^{\text{CPC}}}}$$

κ_B : coefficient

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BAU-related CPV in the broken phase

$$V_L^{e\dagger} (Y_1 c_\beta + Y_2 s_\beta) V_R^e = Y_D = \text{diag}(y_e, y_\mu, y_\tau),$$

$$V_L^{e\dagger} (-Y_1 s_\beta + Y_2 c_\beta) V_R^e = \rho$$

$\tau\text{-}\mu$ case

$$\rightarrow \text{Im} \left[(Y_1)_{\tau\mu} (Y_2)_{\tau\mu}^* \right] = \text{Im} \left[(V_L^e Y_D V_R^{e\dagger})_{32} (V_L^e \rho V_R^{e\dagger})_{32}^* \right]$$

Simplified case: Guo et al, 1609.09849.

$$Y_{i=1,2} = \begin{pmatrix} (Y_i)_{ee} & 0 & 0 \\ 0 & 0 & 0 \\ 0 & (Y_i)_{\tau\mu} & (Y_i)_{\tau\tau} \end{pmatrix}, \quad \tan \beta = 1, \quad (Y_1)_{\tau\tau} = (Y_2)_{\tau\tau}$$

$$\rightarrow \text{Im} \left[(Y_1)_{\tau\mu} (Y_2)_{\tau\mu}^* \right] = -y_\tau \text{Im}(\rho_{\tau\tau}), \quad \rho_{\mu\tau} = 0.$$

To explain muon g-2, both $\rho_{\tau\mu}$ and $\rho_{\mu\tau}$ must be nonzero.

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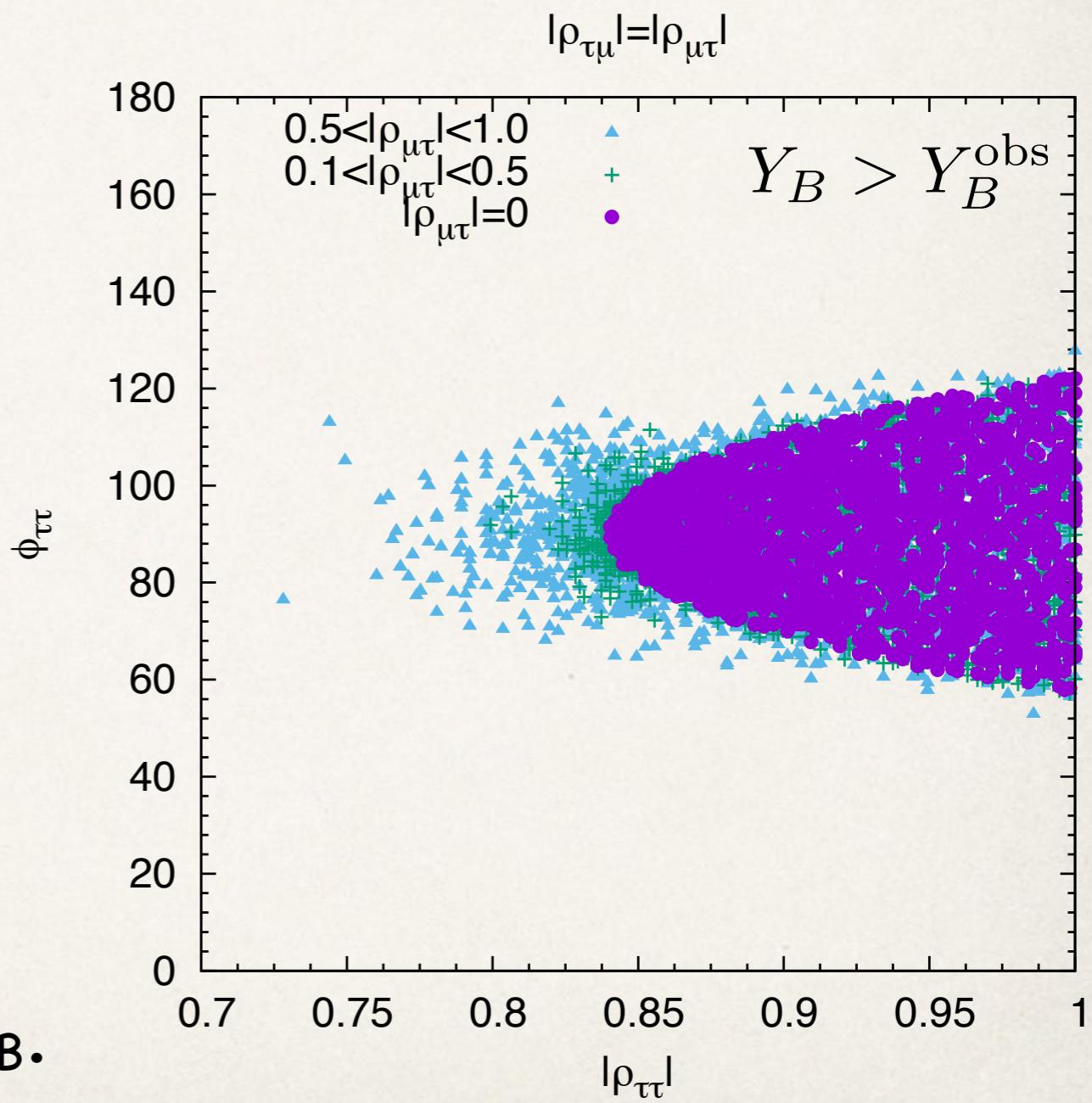
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To explain muon g-2, both $\rho_{\tau\mu}$ and $\rho_{\mu\tau}$ must be nonzero.

Random scan

- Yukawa couplings ($Y_{1,2}$) are randomly scanned.
- **Leading effect** on Y_B :
 $\rho_{\tau\tau}$
- **Subleading effect**:
 $\rho_{\tau\mu}$ and $\rho_{\mu\tau}$.
- Yukawa textures with $\rho_{\mu\tau} \neq 0$ can give visible effects on Y_B .



Benchmark

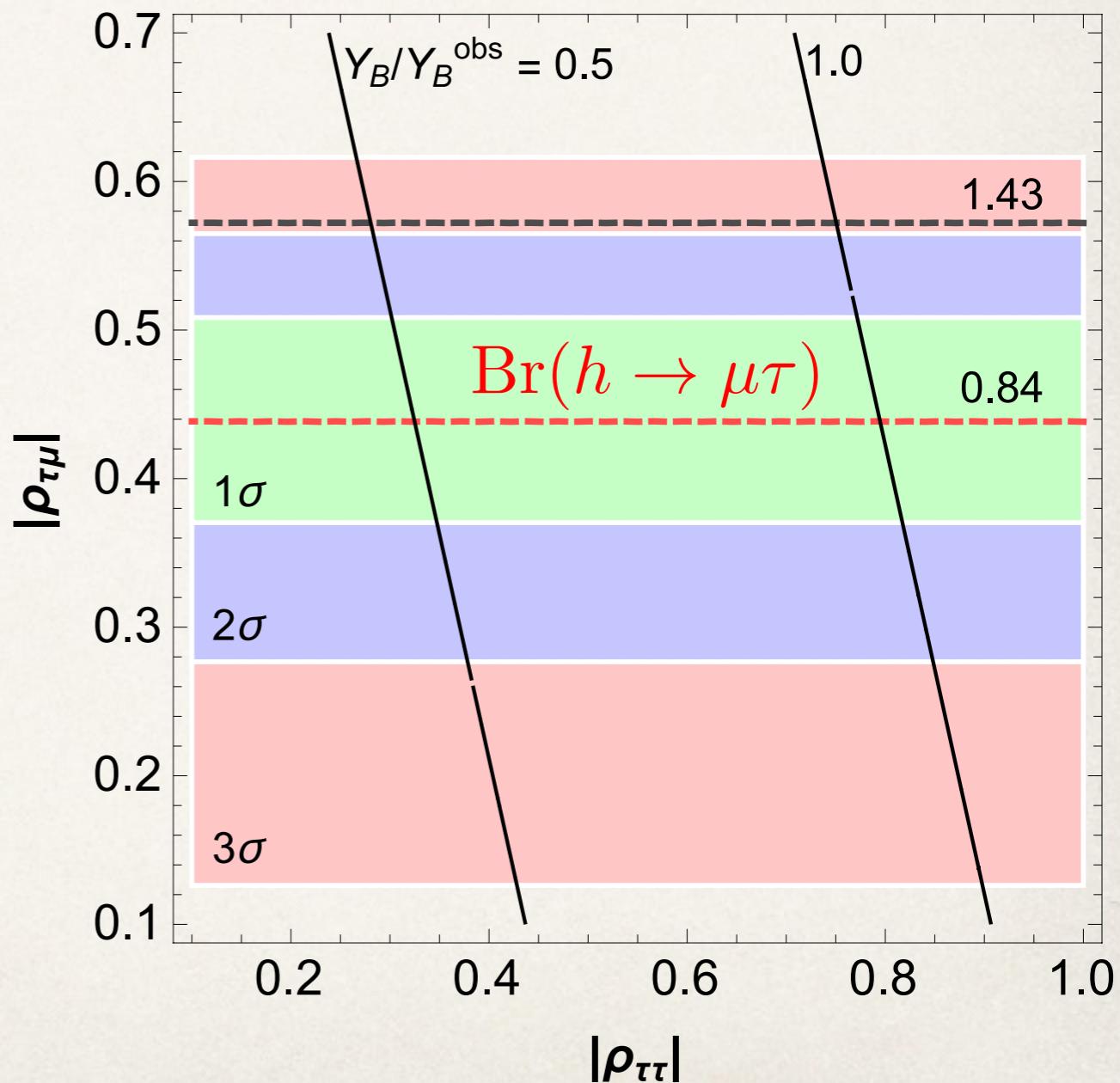
$m_H = 350$ GeV, $m_A = m_{H^\pm} = 400$ GeV, $c_{\beta-\alpha} = 0.006$, $|\rho_{\mu\tau}| = |\rho_{\tau\mu}|$
 $\phi_{\tau\mu} + \phi_{\mu\tau} = \pi/4$, $\phi_{\tau\tau} = \pi/2$

$$Y^{\text{SM}} = Y_1 c_\beta + Y_2 s_\beta$$

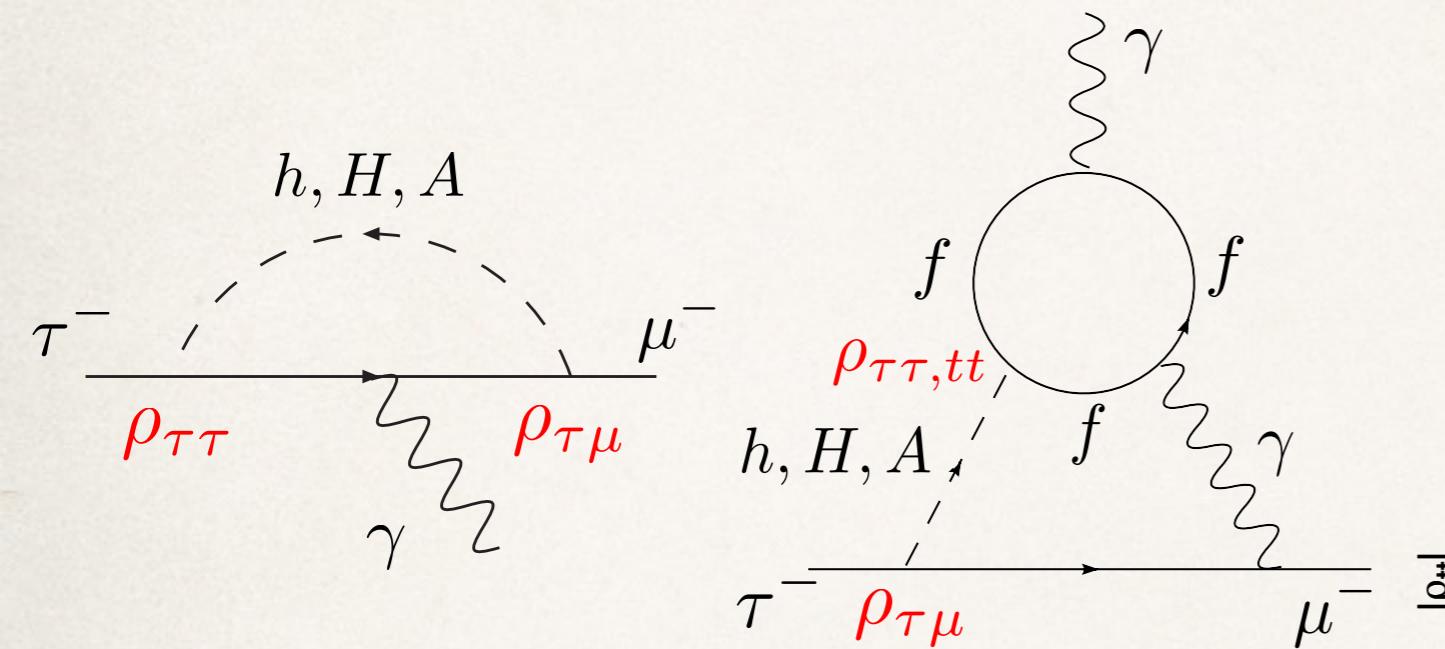
$$= \begin{pmatrix} \sqrt{2}m_e/v & 0 & 0 \\ 0 & 3.31 \times 10^{-3} & -6.81i \times 10^{-4} \\ 0 & 8.91i \times 10^{-3} & 3.70 \times 10^{-3} \end{pmatrix},$$

$$V_R^e = \begin{pmatrix} 1 & 0 & 0 \\ 0 & -0.365i & -0.931i \\ 0 & -0.931 & 0.365 \end{pmatrix}, \quad V_L^e = \begin{pmatrix} 1 & 0 & 0 \\ 0 & -0.945i & -0.327i \\ 0 & -0.327 & 0.945 \end{pmatrix}$$

2HDM with LFV explains
 $h \rightarrow \mu\tau$, muon g-2, and BAU.



$\tau \rightarrow \mu \gamma$

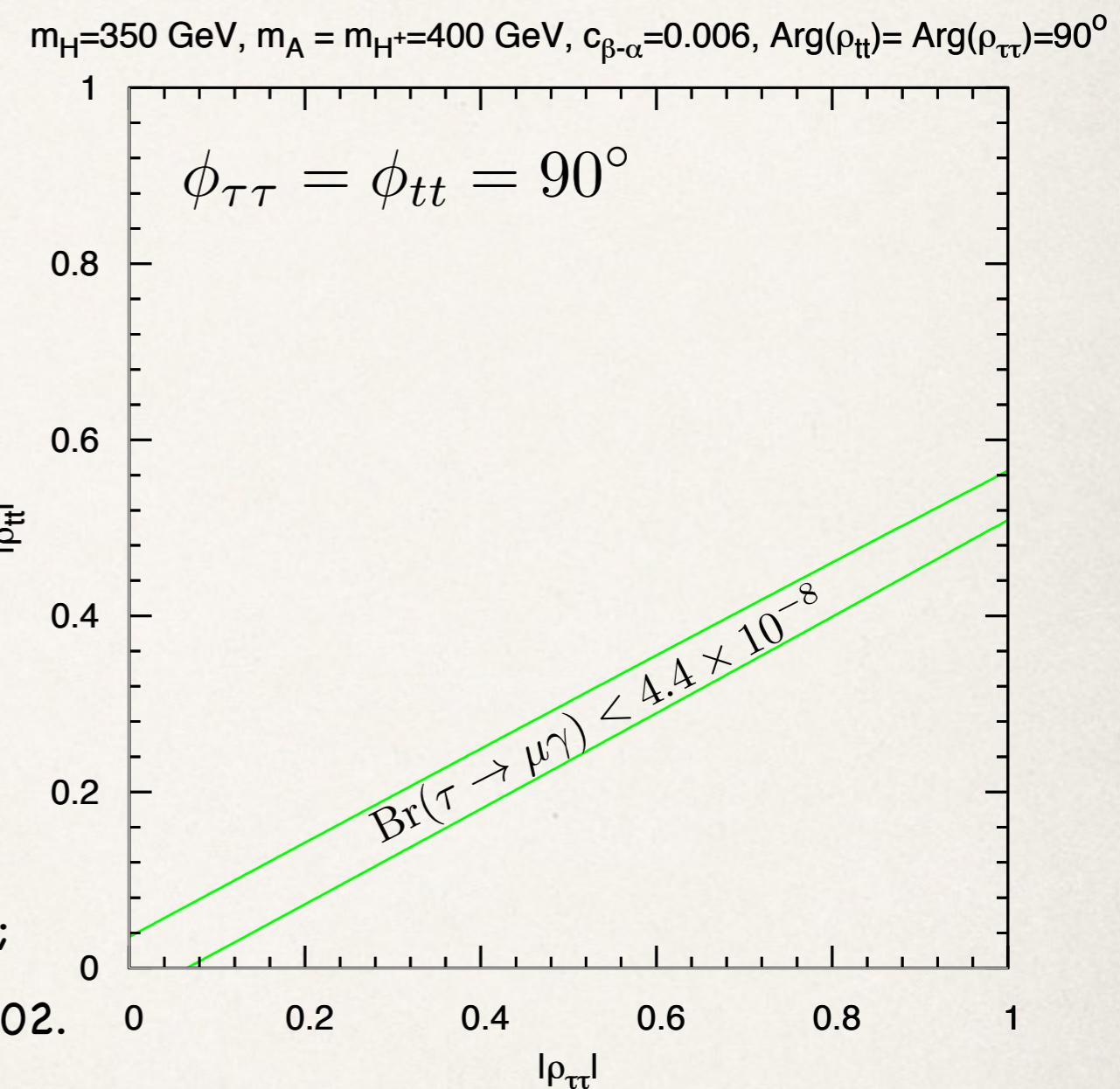


current bound:

$$\text{Br}(\tau \rightarrow \mu \gamma) < 4.4 \times 10^{-8}$$

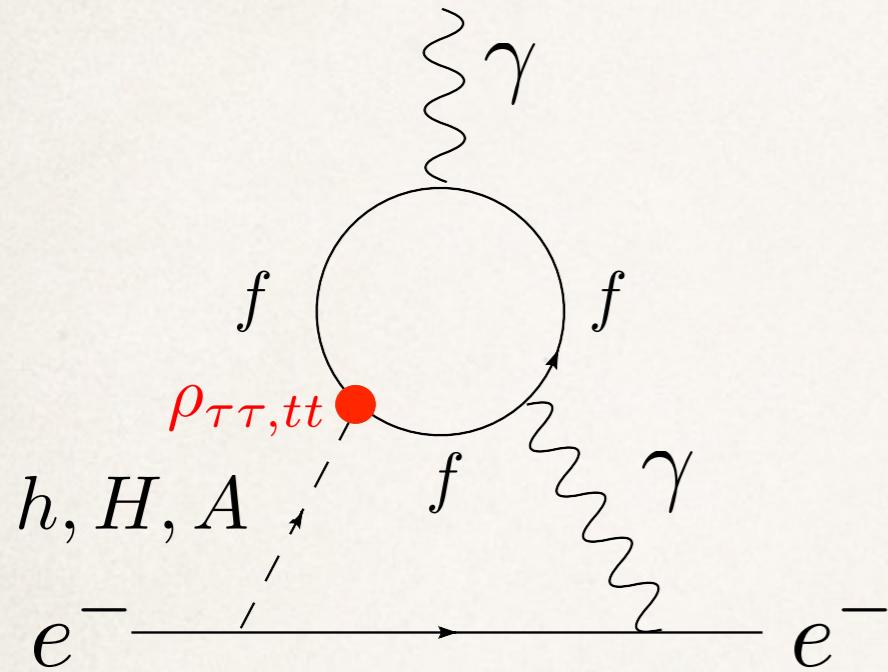
K. Hayasaka et al. [Belle Collaboration], PLB666 (2008) 16;

B. Aubert et al. [BaBar Collaboration], PRL104 (2010) 021802.



Cancellation between 1- and 2-loop diagrams can happen.

electron EDM

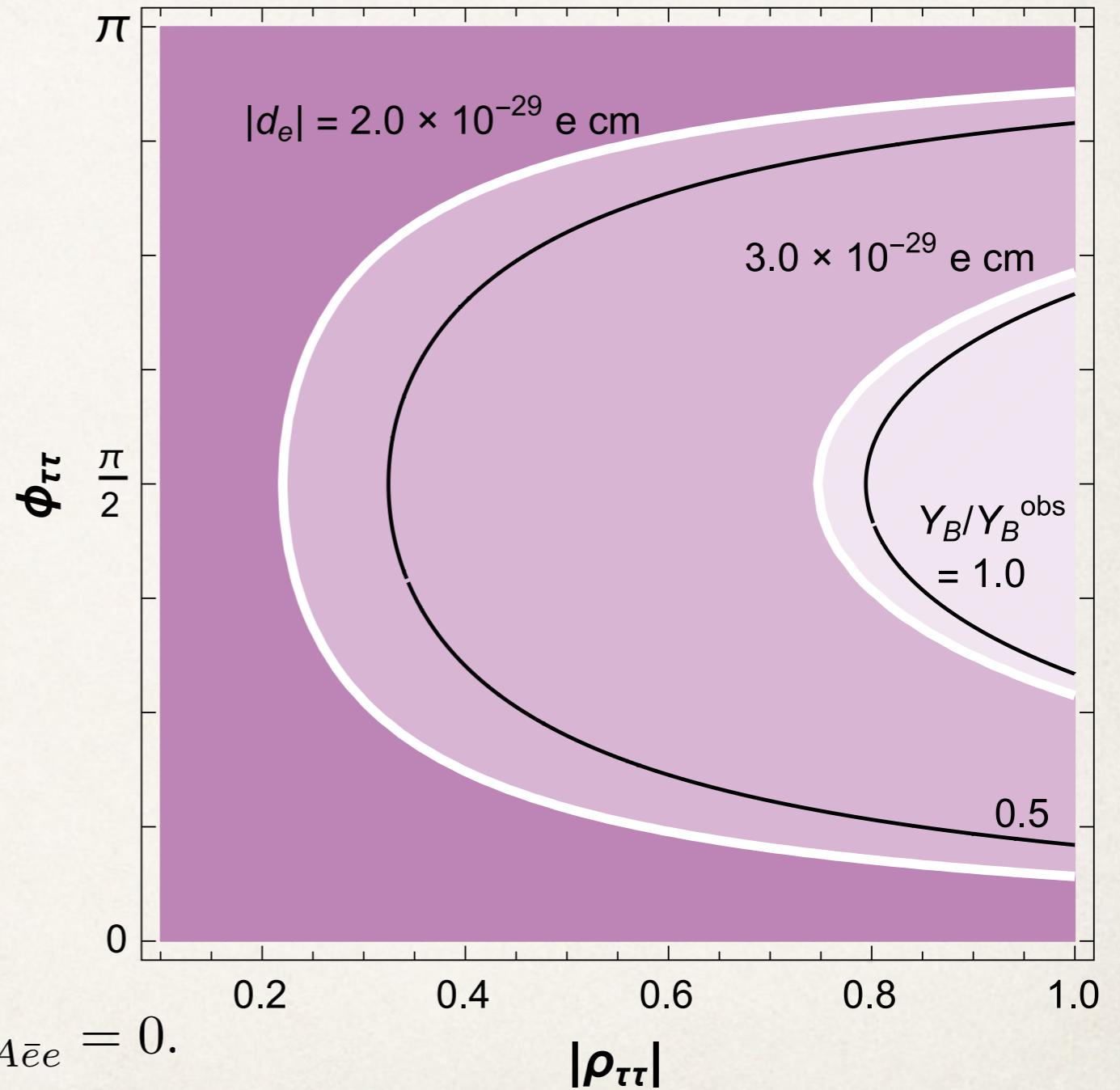


current eEDM bound:

$$|d_e| < 8.7 \times 10^{-29} \text{ e cm}$$

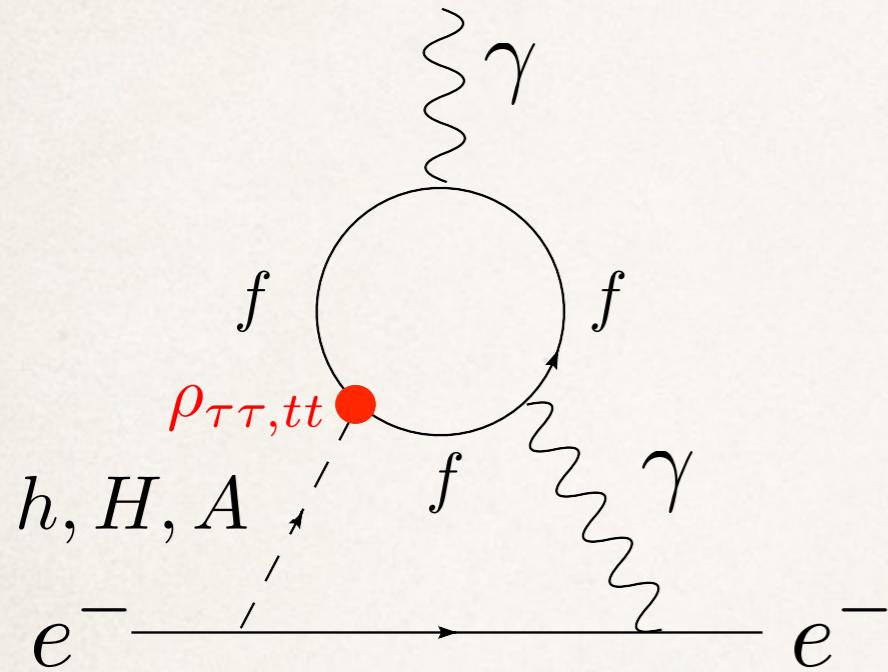
We take $\rho_{ee} = 0$

$$g_{h\bar{e}e} = \frac{m_e}{v} s_{\beta-\alpha}, \quad g_{H\bar{e}e} = \frac{m_e}{v} c_{\beta-\alpha}, \quad g_{A\bar{e}e} = 0.$$



Future eEDM experiment can probe the EWBG-viable region.

electron EDM

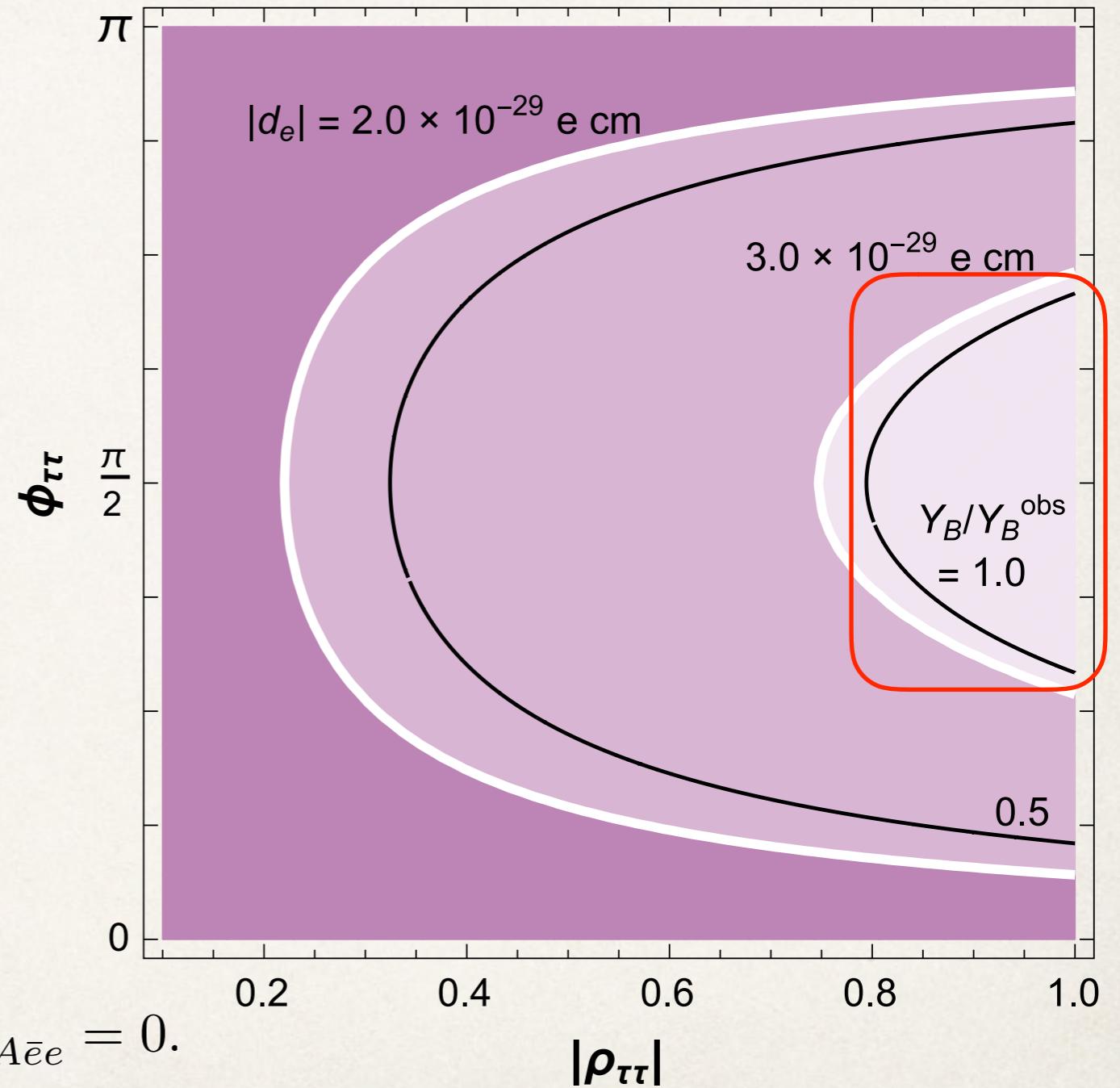


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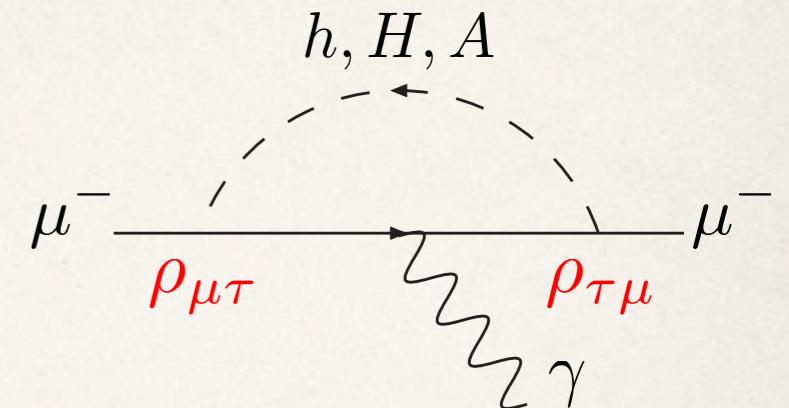
$$g_{h\bar{e}e} = \frac{m_e}{v} s_{\beta-\alpha}, \quad g_{H\bar{e}e} = \frac{m_e}{v} c_{\beta-\alpha}, \quad g_{A\bar{e}e} = 0.$$



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muon EDM

muon EDM is induced by 1-loop diagram.



$$\begin{aligned} \frac{d_\mu}{|e|} &= -\frac{m_\tau}{32\pi^2} \text{Im}(\rho_{\mu\tau}\rho_{\tau\mu}) \left[\frac{c_{\beta-\alpha}^2 f(r_h)}{m_h^2} + \frac{s_{\beta-\alpha}^2 f(r_H)}{m_H^2} - \frac{f(r_A)}{m_A^2} \right] \\ &= -\frac{1}{2m_\mu} \text{Arg}(\rho_{\mu\tau}\rho_{\tau\mu}) \delta a_\mu, \quad r_\phi = m_\tau^2/m_\phi^2, \quad f(r) \simeq \ln \frac{1}{r} - \frac{3}{2}. \end{aligned}$$

$$\rightarrow d_\mu \simeq -3 \times 10^{-22} e \text{ cm} \times \left(\frac{\text{Arg}(\rho_{\mu\tau}\rho_{\tau\mu})}{1} \right) \times \left(\frac{\delta a_\mu}{3 \times 10^{-9}} \right)$$

current muon EDM bound:

$$|d_\mu| < 1.9 \times 10^{-19} e \text{ cm}$$

A → ττ

ATLAS-CONF-2016-085

In our EWBG scenario,

- $|\rho_{\tau\mu}| = |\rho_{\mu\tau}| = 0.1 - 0.6$,
- $|\rho_{\tau\tau}| = 0.8 - 0.9$.
- $|\rho_{tt}| = 0.5$.

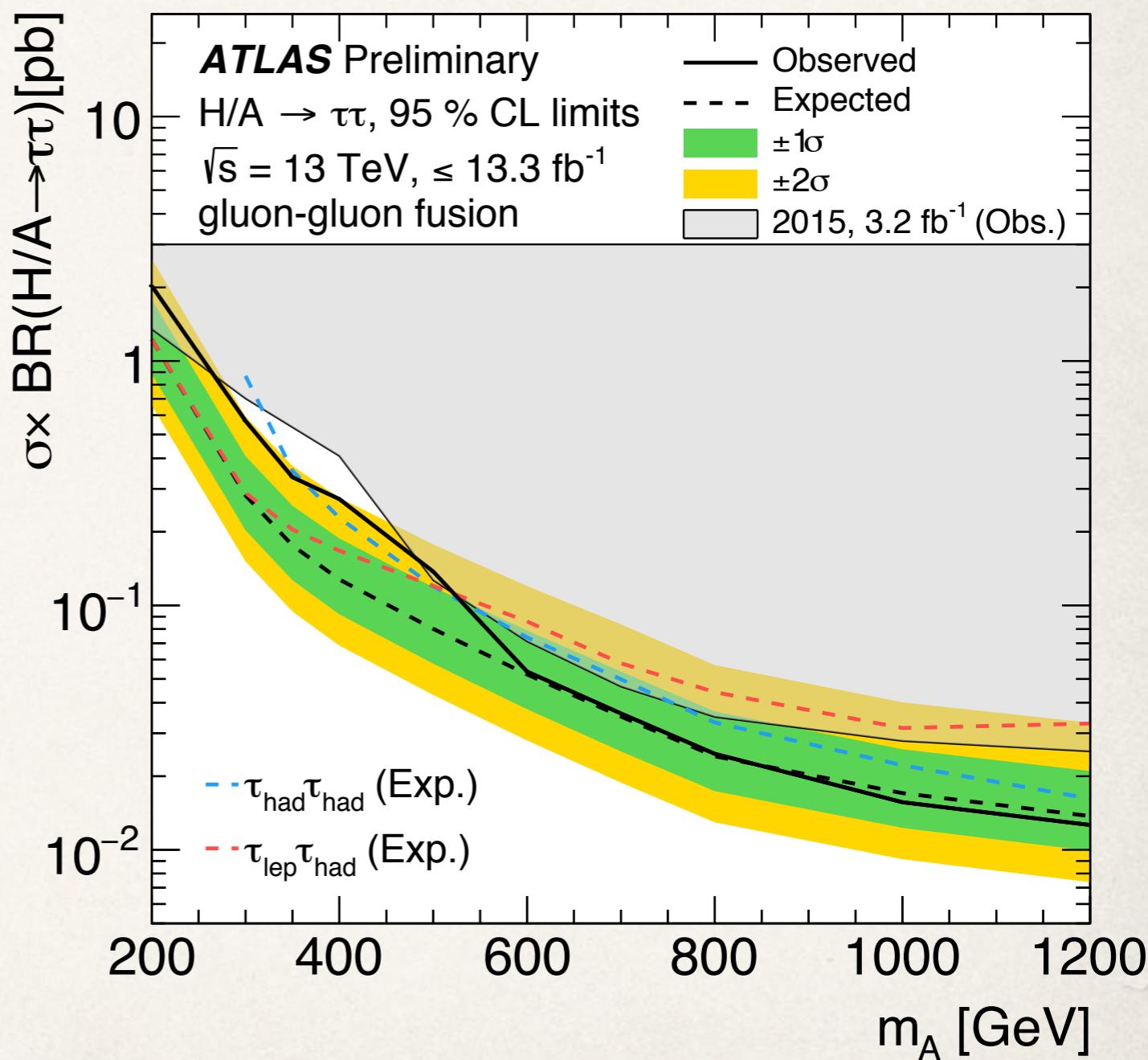
→ sizable $\text{Br}(A \rightarrow \tau\tau)$

e.g.

$$\sigma_{gg \rightarrow A} \times \text{BR}(A \rightarrow \tau\tau) \simeq 0.82 \text{ pb}$$

$\sim 70\%$

→ tension with data!



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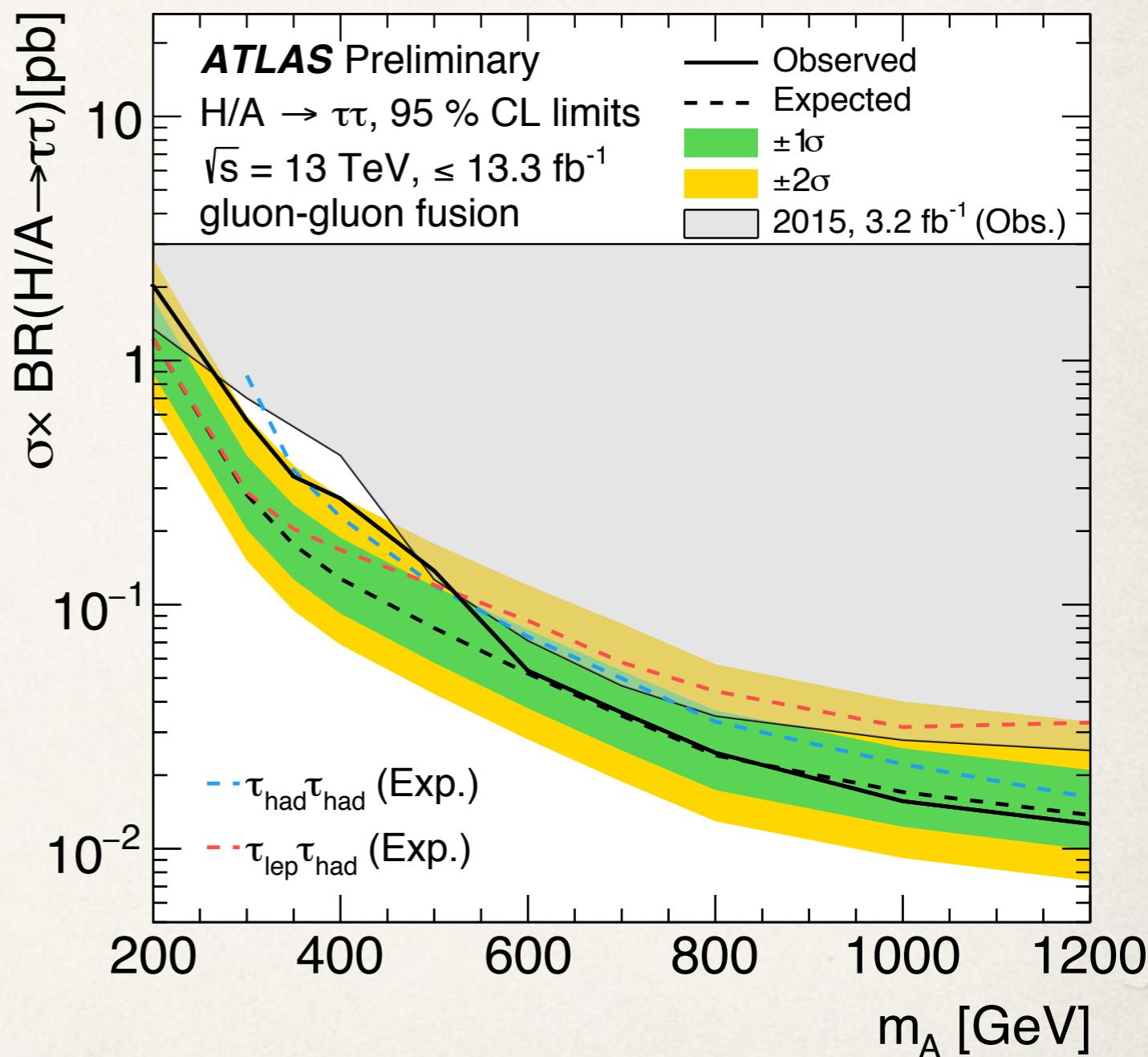
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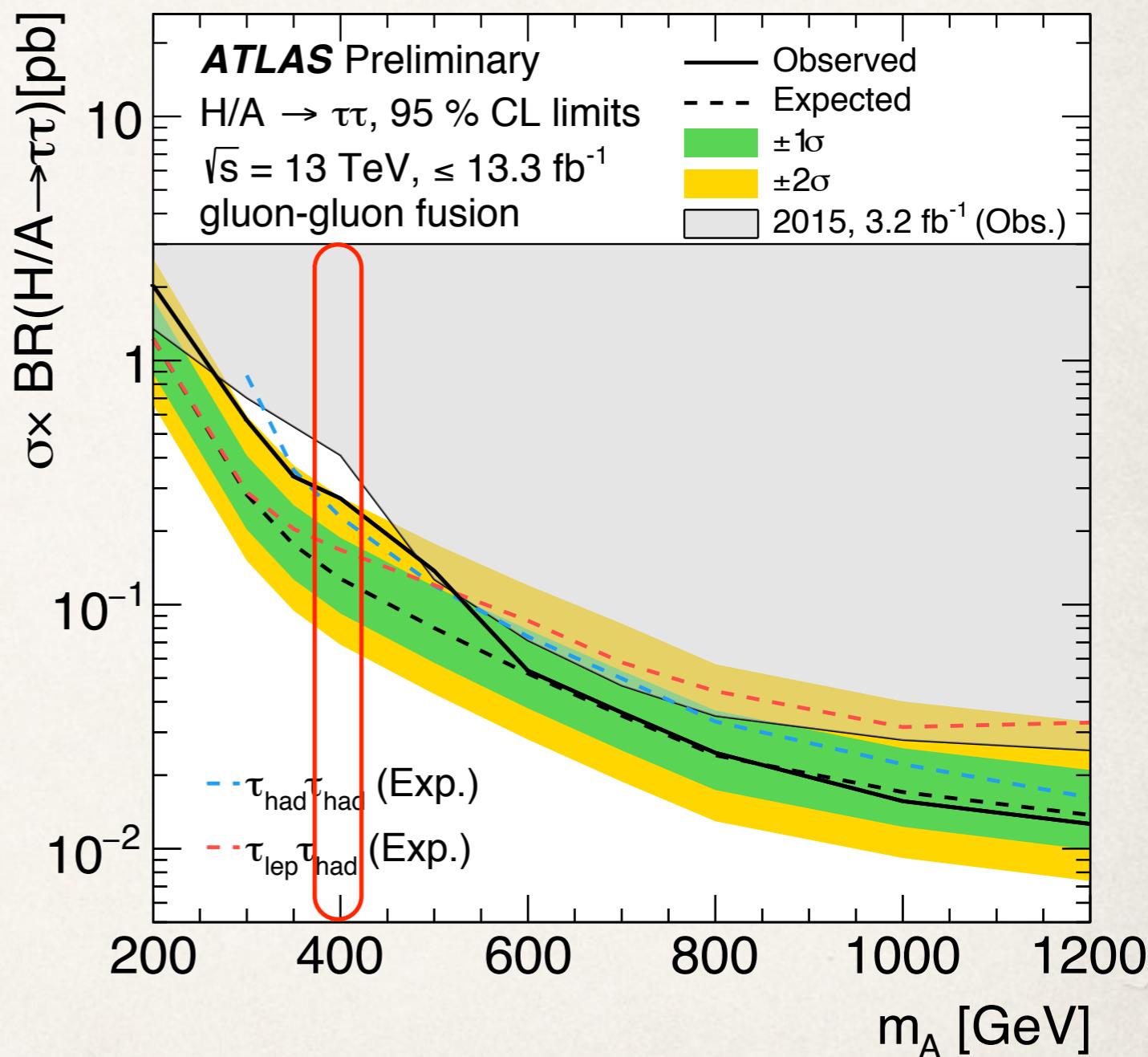
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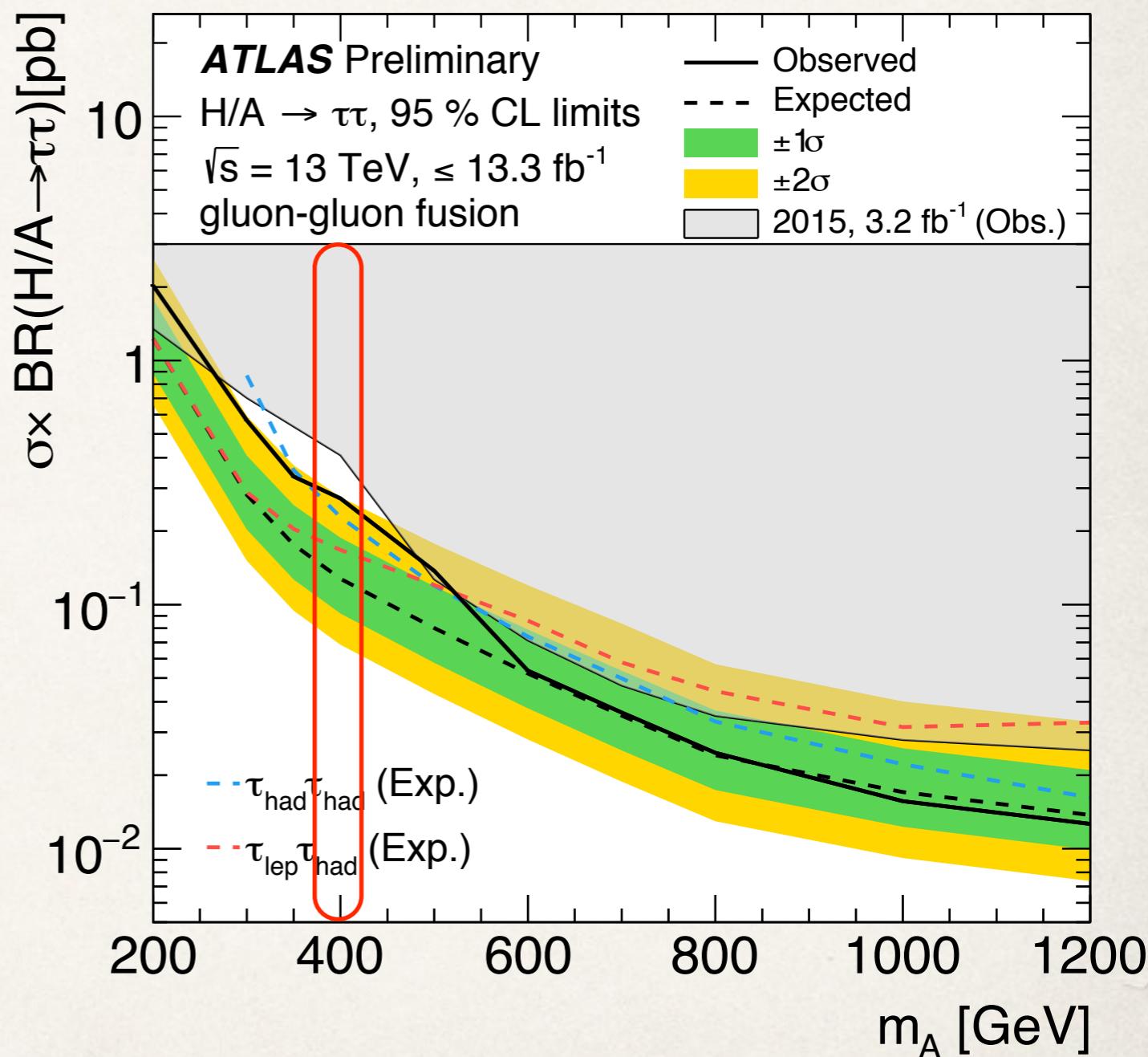
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$\sim 70\%$

→ tension with data!

way-out: $\text{Br}(A \rightarrow \tau\tau)$ can be reduced if other ρ couplings are nonzero.

$\rho_{tc} < 1.5$, $\rho_{ct} < 0.1$ [Altunkaynak, Hou, Kao, Kohda, MacKoy, 1506.00651 [PLB]]



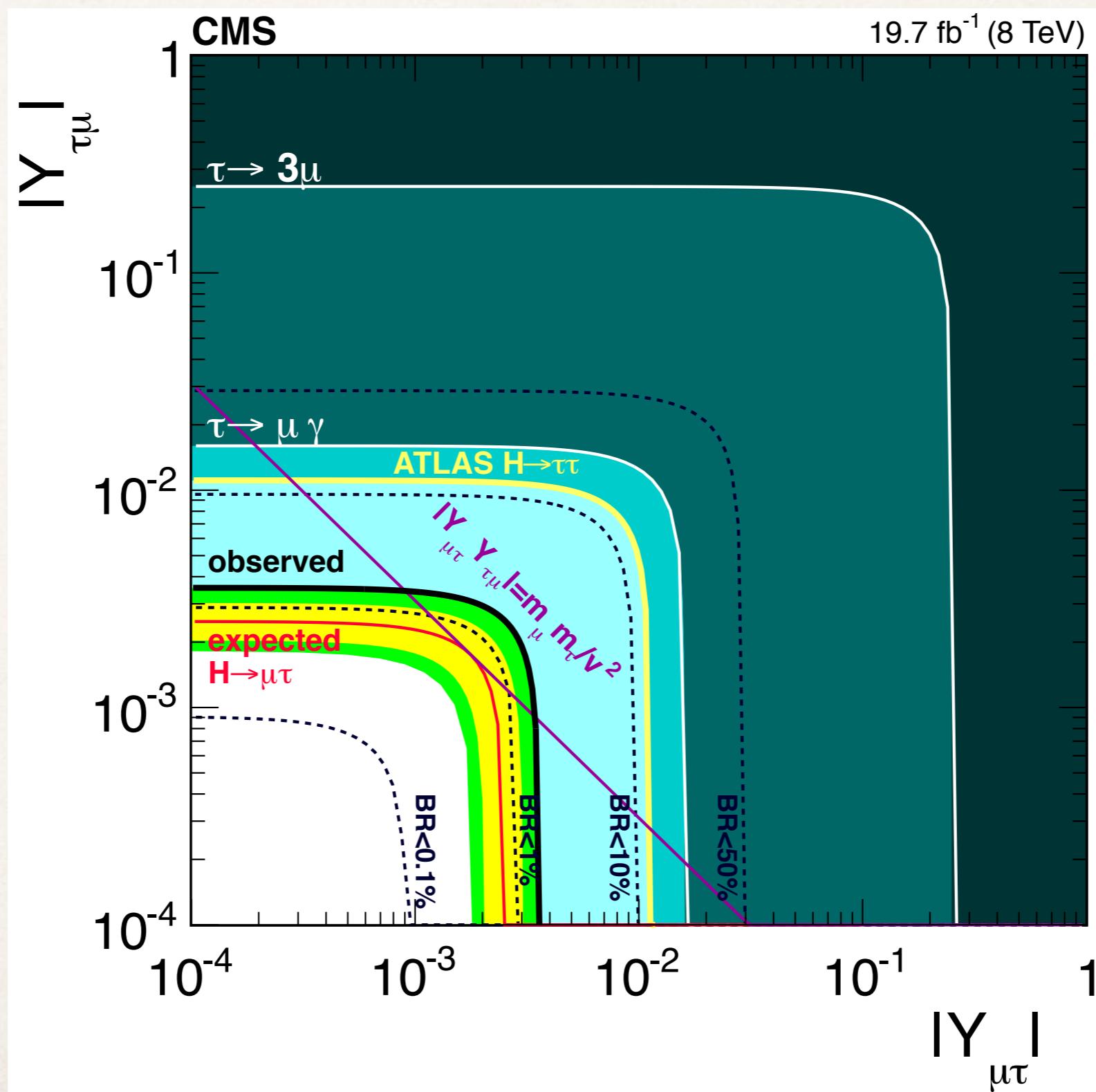
Summary

- We have discussed EWBG with LFV in the general 2HDM.
- Strong 1st-order EWPT and muon g-2 favored region:
 $300 \text{ GeV} \lesssim m_H \lesssim m_A$ for $\text{Re}(\rho_{\tau\mu}\rho_{\mu\tau}) > 0$.
- BAU can be explained if $|\rho_{\tau\tau}| = 0.8 - 0.9$, $|\rho_{\tau\mu}| = |\rho_{\mu\tau}| = 0.1 - 0.6$, $|\rho_{tt}| = 0.5$.
- gg- $\rightarrow A \rightarrow \tau\tau$ is now in tension with the LHC data
→ $\rho_{tc} = O(1)$.

Backup

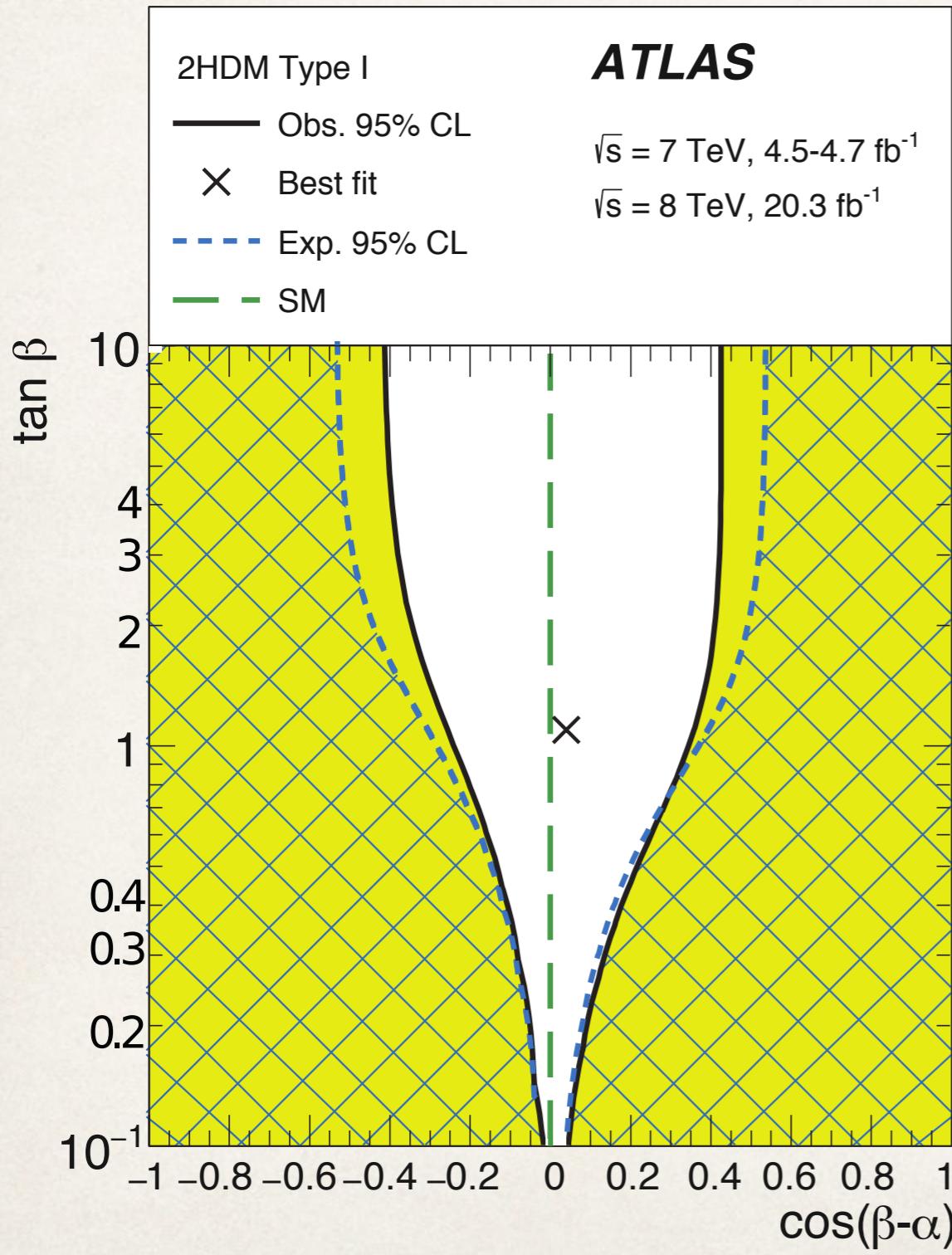
Constraint on μ - τ coupling

1502.07400

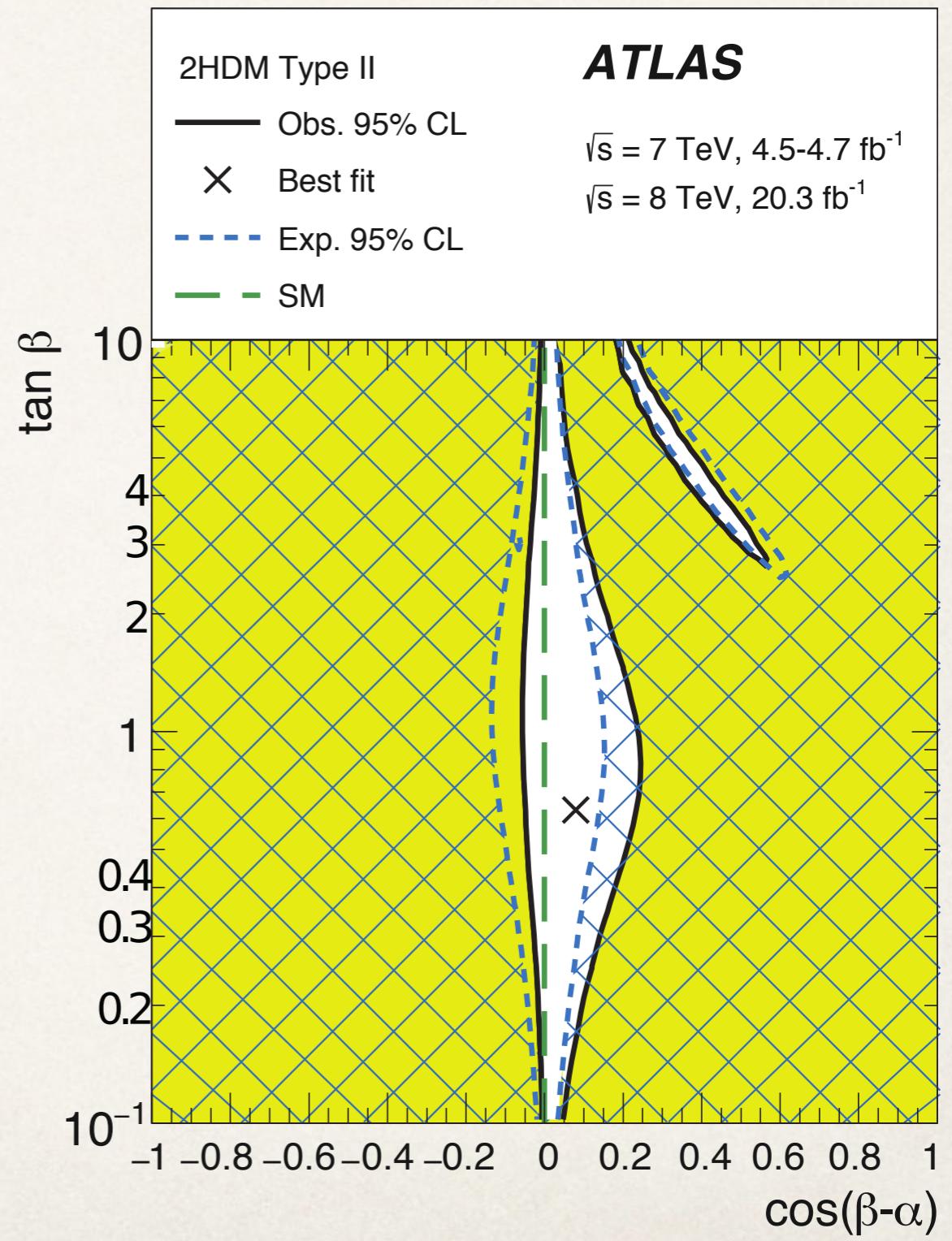


Constraints in $(\cos(\beta - \alpha), \tan \beta)$ plane

arXiv:1509.00672

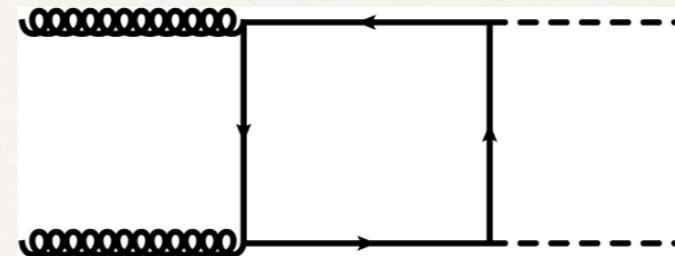
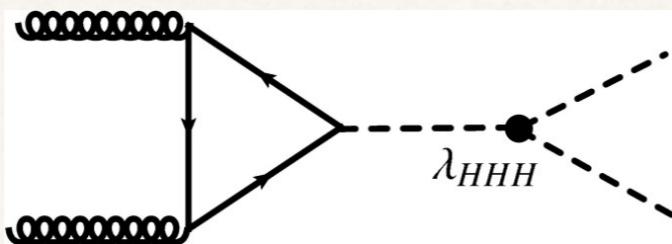


(a) Type I

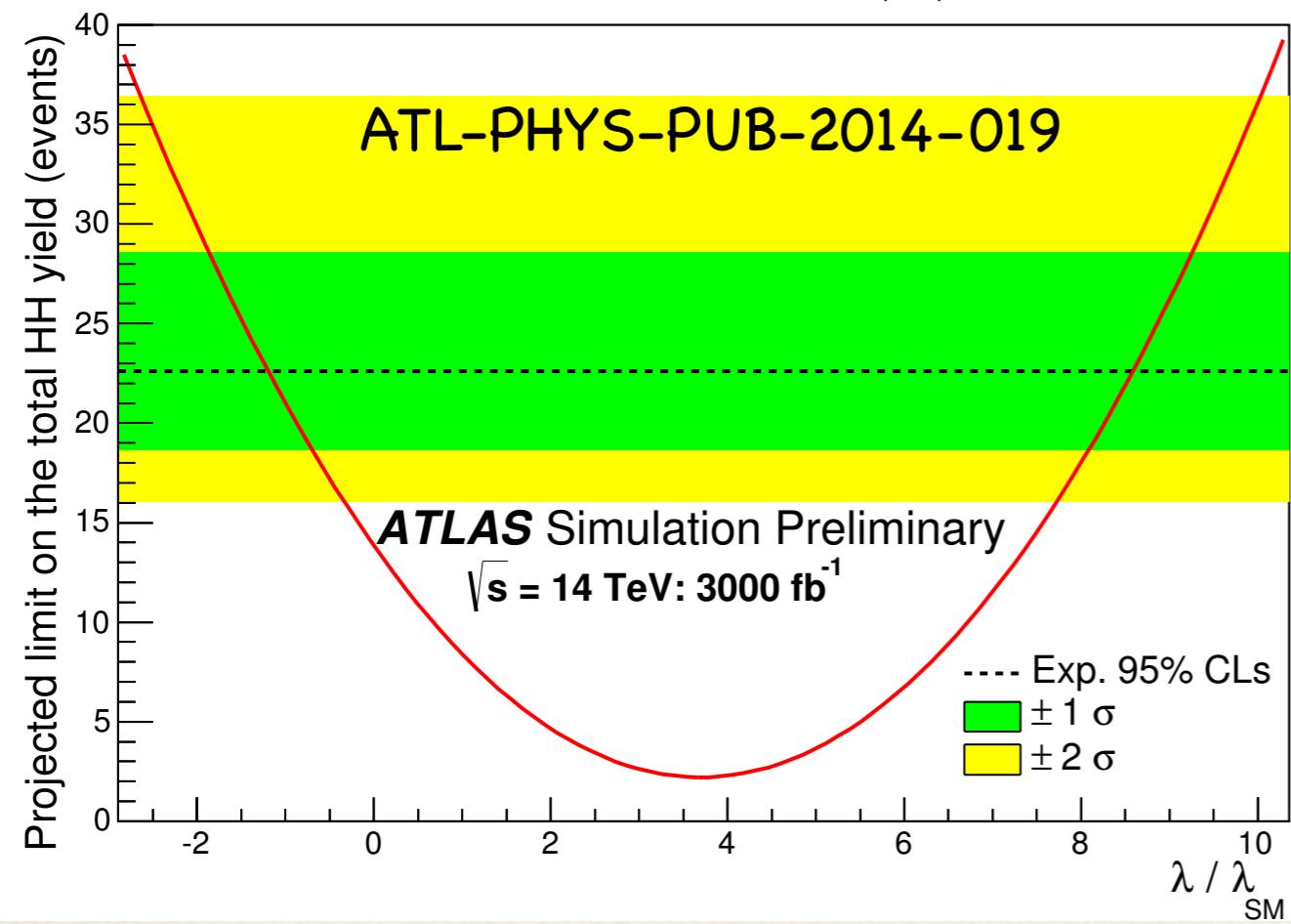


(b) Type II

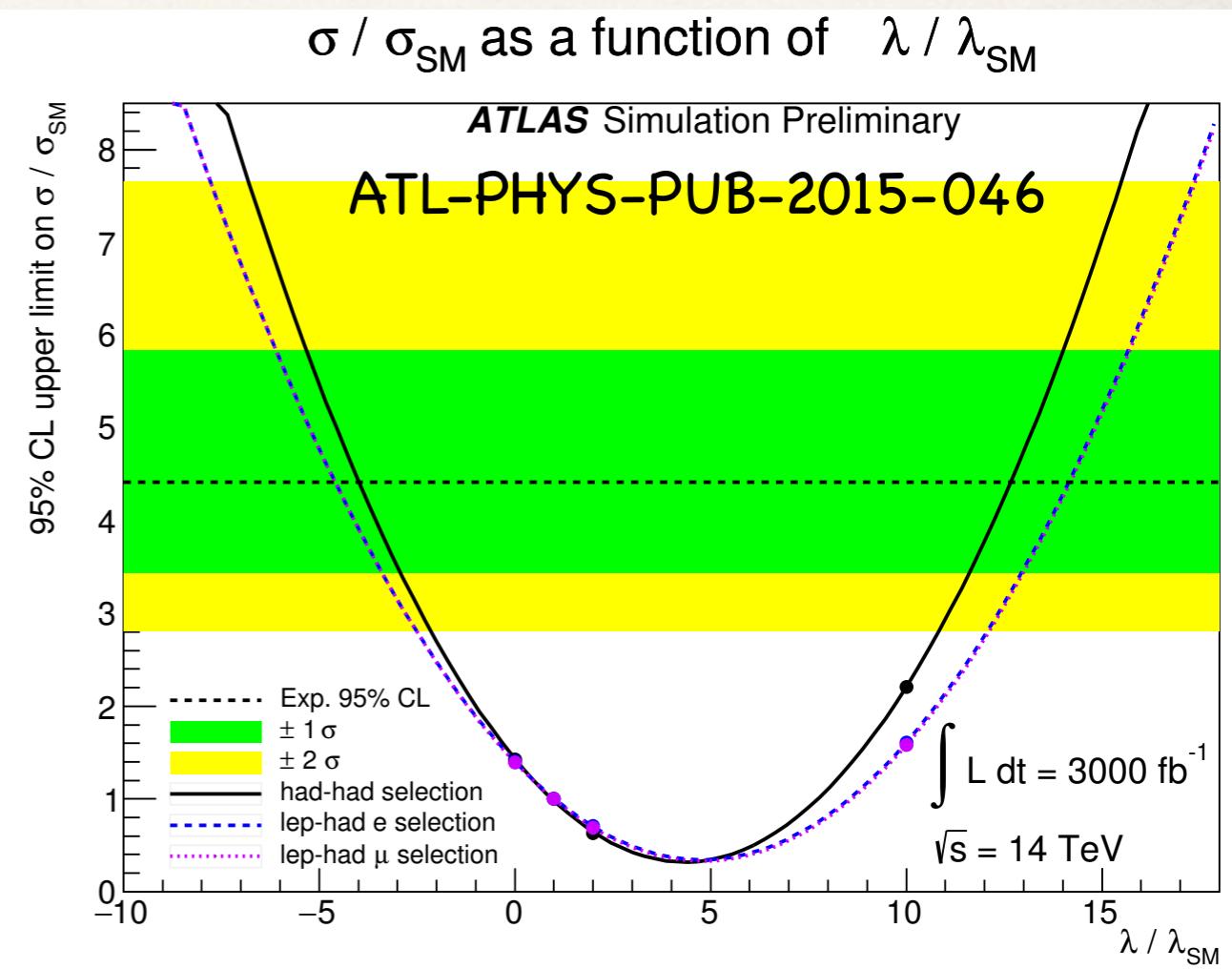
hhh coupling at LHC



$HH \rightarrow bb\gamma\gamma$

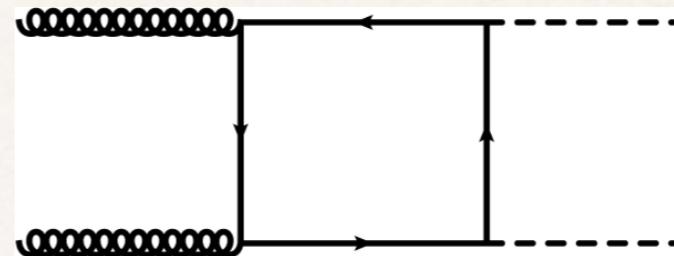
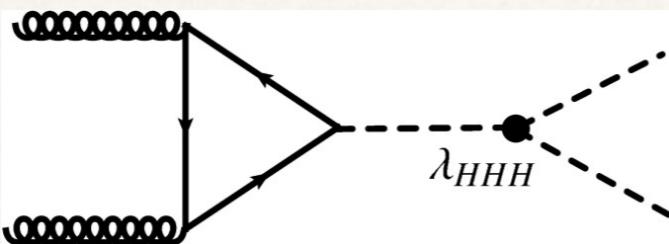


$HH \rightarrow bb\tau\tau$
 σ / σ_{SM} as a function of λ / λ_{SM}

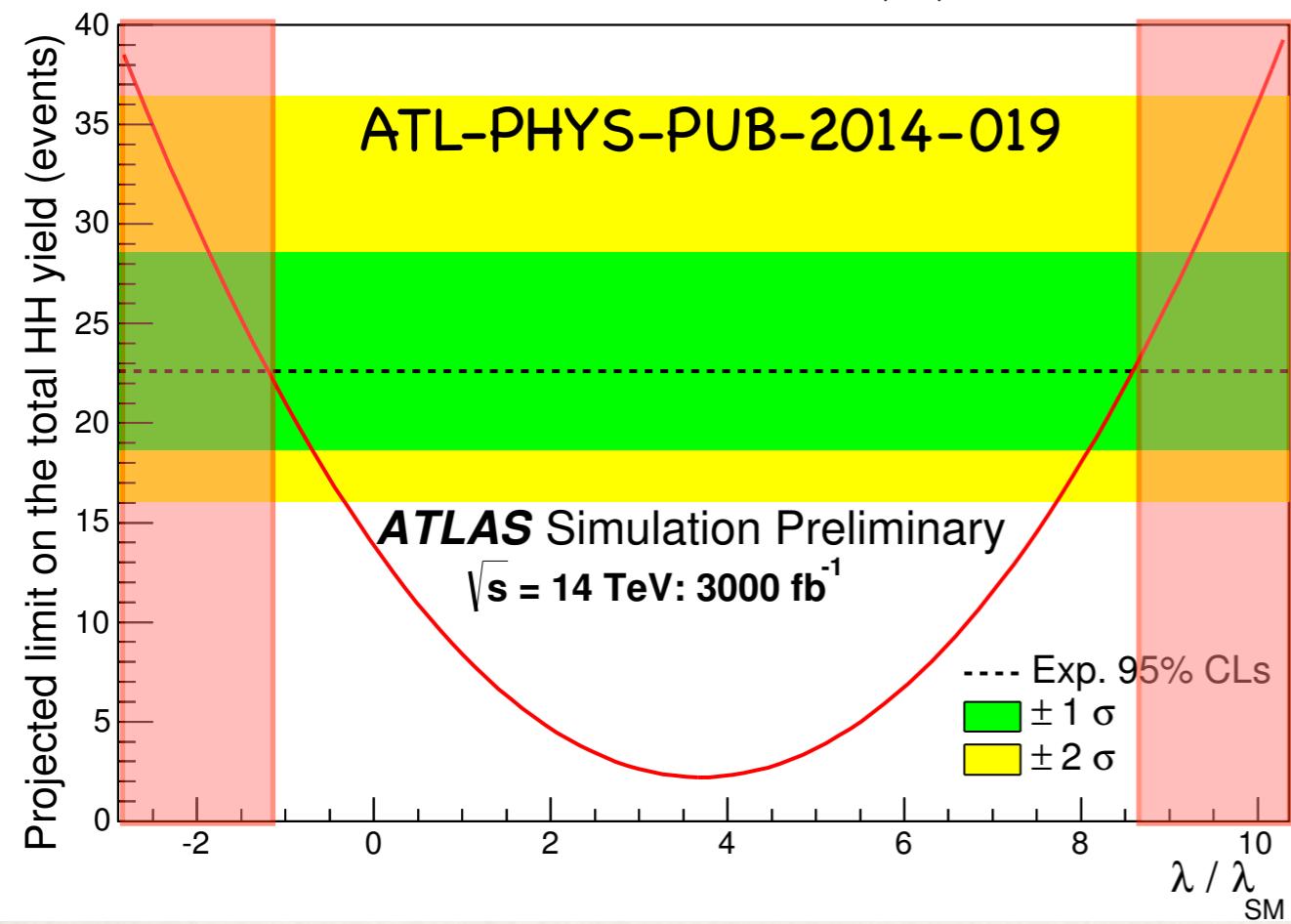


Access to λ_{hhh} of 2HDM at the LHC is challenging.

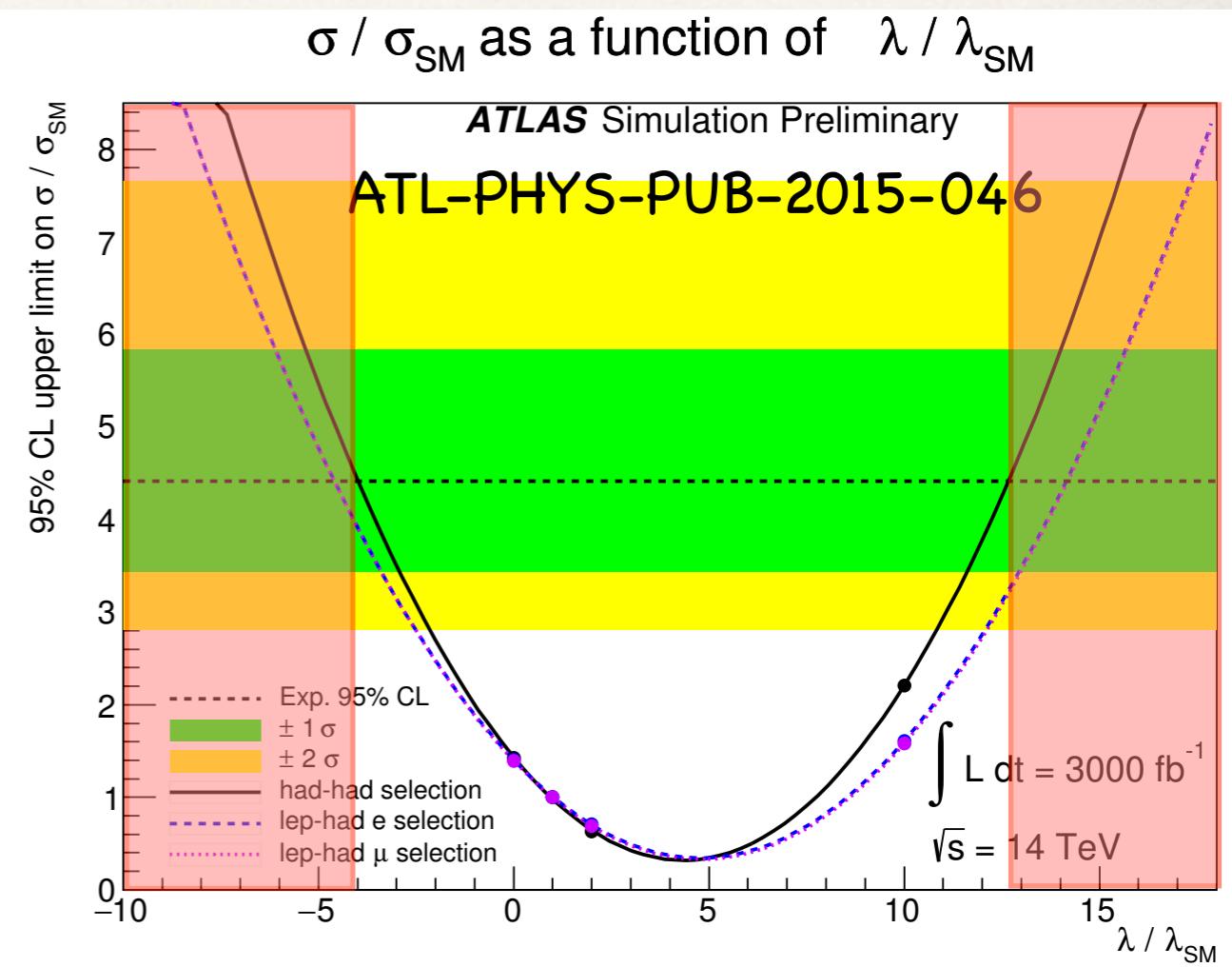
hhh coupling at LHC



$HH \rightarrow bb\gamma\gamma$



$HH \rightarrow b\bar{b}\tau\tau$
 σ / σ_{SM} as a function of λ / λ_{SM}



Access to λ_{hhh} of 2HDM at the LHC is challenging.

Higgs couplings measurements@ILC

ILC white paper, 1310.0763

	ILC(250)	ILC(500)	ILC(1000)	ILC(LumUp)
\sqrt{s} (GeV)	250	250+500	250+500+1000	250+500+1000
L (fb $^{-1}$)	250	250+500	250+500+1000	1150+1600+2500
$\gamma\gamma$	18 %	8.4 %	4.0 %	2.4 %
gg	6.4 %	2.3 %	1.6 %	0.9 %
WW	4.8 %	1.1 %	1.1 %	0.6 %
ZZ	1.3 %	1.0 %	1.0 %	0.5 %
$t\bar{t}$	–	14 %	3.1 %	1.9 %
$b\bar{b}$	5.3 %	1.6 %	1.3 %	0.7 %
$\tau^+\tau^-$	5.7 %	2.3 %	1.6 %	0.9 %
$c\bar{c}$	6.8 %	2.8 %	1.8 %	1.0 %
$\mu^+\mu^-$	91%	91%	16 %	10 %
$\Gamma_T(h)$	12 %	4.9 %	4.5 %	2.3 %
hhh	–	83 %	21 %	13 %
BR(invis.)	< 0.9 %	< 0.9 %	< 0.9 %	< 0.4 %

Higgs couplings measurements@ILC

ILC white paper, 1310.0763

	ILC(250)	ILC(500)	ILC(1000)	ILC(LumUp)
\sqrt{s} (GeV)	250	250+500	250+500+1000	250+500+1000
L (fb^{-1})	250	250+500	250+500+1000	1150+1600+2500
$\gamma\gamma$	18 %	8.4 %	4.0 %	2.4 %
gg	6.4 %	2.3 %	1.6 %	0.9 %
WW	4.8 %	1.1 %	1.1 %	0.6 %
ZZ	1.3 %	1.0 %	1.0 %	0.5 %
$t\bar{t}$	—	14 %	3.1 %	1.9 %
$b\bar{b}$	5.3 %	1.6 %	1.3 %	0.7 %
$\tau^+\tau^-$	5.7 %	2.3 %	1.6 %	0.9 %
$c\bar{c}$	6.8 %	2.8 %	1.8 %	1.0 %
$\mu^+\mu^-$	91%	91%	16 %	10 %
$\Gamma_T(h)$	12 %	4.9 %	4.5 %	2.3 %
hhh	—	83 %	21 %	13 %
BR(invis.)	< 0.9 %	< 0.9 %	< 0.9 %	< 0.4 %