

Origin of Higgs

gauge-Higgs unification at LHC/ILC and beyond

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HPNP 2017
Higgs as a Probe of New Physics
University of Toyama, 2 March 2017

Standard Model is successful.

$$\mathcal{L}_{\text{gauge}} = -\frac{1}{2} \text{Tr} G_{\mu\nu} G^{\mu\nu} - \frac{1}{2} \text{Tr} F_{\mu\nu} F^{\mu\nu} - \frac{1}{4} B_{\mu\nu} B^{\mu\nu}$$

$$\mathcal{L}_{\text{Higgs}} = |D_{\mu} \Phi|^2 - V[\Phi]$$

$$\mathcal{L}_{\text{fermion}} = \bar{\psi}_j i \gamma^{\mu} D_{\mu} \psi_j$$

$$\mathcal{L}_{\text{Yukawa}} = y_{jk} \bar{\psi}_j \Phi \psi_k$$

Gauge principle

Lacks principle.

Standard Model

$\mathcal{L}_{\text{gauge}}$

+

$\mathcal{L}_{\text{Higgs}}$

$\mathcal{L}_{\text{fermion}}$

+

$\mathcal{L}_{\text{Yukawa}}$

Gauge-Higgs Unification



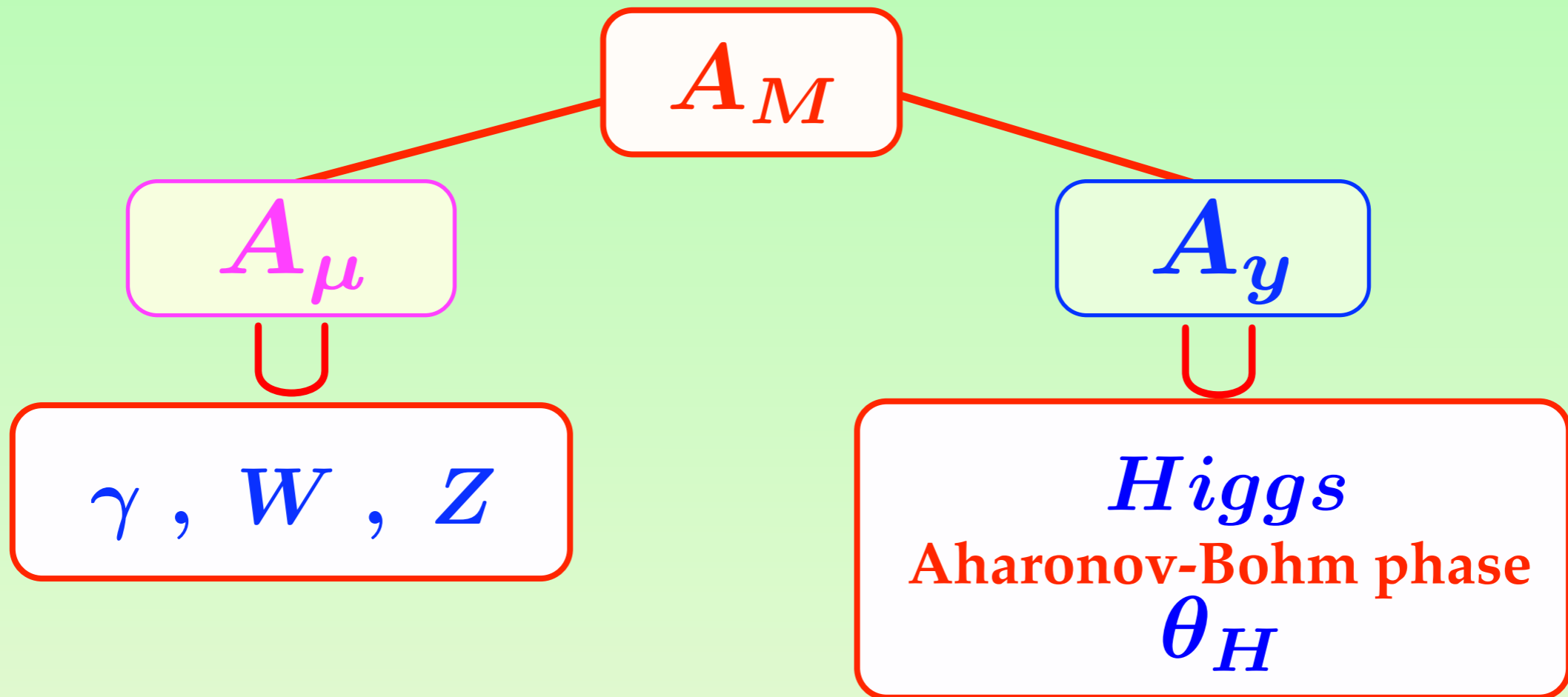
$\mathcal{L}_{\text{gauge}}^{5d}$

gauge principle



$\mathcal{L}_{\text{fermion}}^{5d}$

Gauge-Higgs unification



Gauge-Higgs unification

A_M

A_y

\cup

Higgs

Aharonov-Bohm phase

θ_H

Hosotani mechanism

Dynamical
EW sym breaking

Finite Higgs mass
generated.

Gauge-hierarchy problem
is solved.

Hosotani mechanism

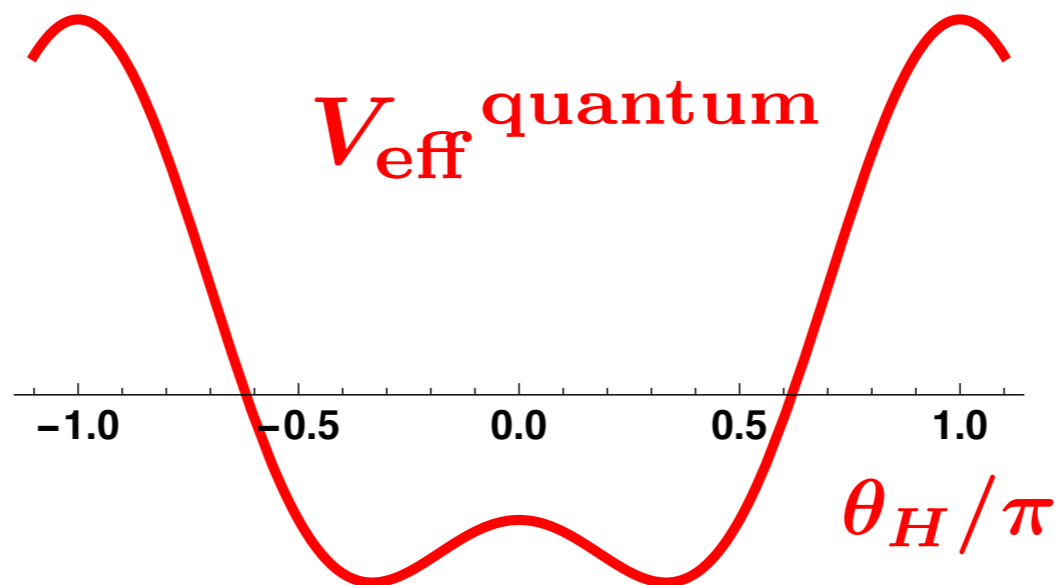
$$\langle P e^{ig \oint dy A_y} \rangle = e^{i\theta_H}$$

AB phase in the 5th dim

Higgs mechanism


$$\langle \Phi \rangle$$

Gauge sym breaking by gauge inv quantities



Hosotani mechanism

$$\theta_H \neq 0 \quad \mathcal{G} \rightarrow \mathcal{H}$$

gauge bosons (W, Z)  massive
quarks, leptons

$$A_y(x, y) = \left\{ f_H \theta_H + H(x) \right\} u_0(y) + \dots$$


4D Higgs

Finite Higgs mass generated.

Gauge-Higgs EW unification

$$SU(2)_L \times U(1)_Y \rightarrow U(1)_{EM}$$

Higgs : $SU(2)$ doublet $\rightarrow \mathcal{G} \supset SU(2) \times U(1)$

Chiral fermions \rightarrow orbifold

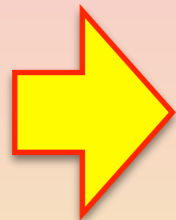
$$SU(3) \quad \text{on } M^4 \times (S^1/Z_2)$$

Kubo, Lim, Yamashita 2002

$$SU(3) \times U(1)_X$$

$$SO(5) \times U(1)_X \text{ in } RS$$

Agashe, Contino, Pomarol 2005



SO(5)×U(1) GHU in Randall-Sundrum

Agashe, Contino, Pomarol 2005

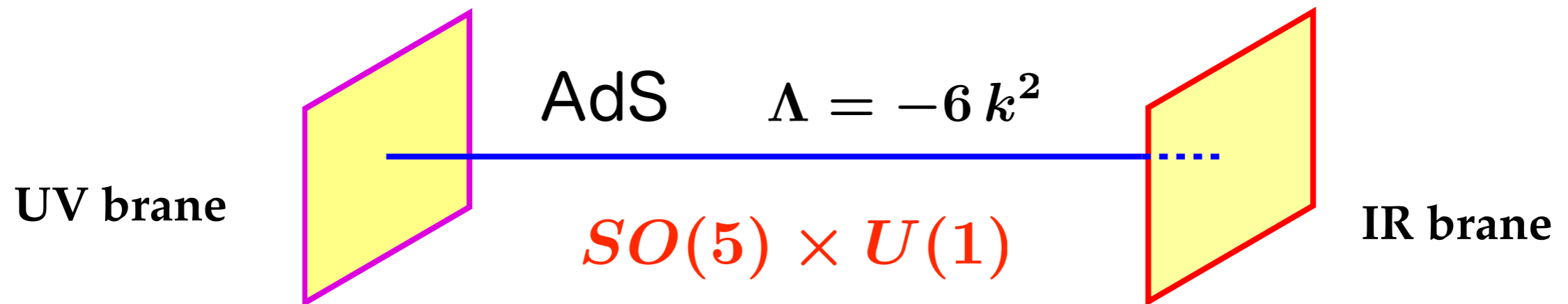
YH, Sakamura 2006

Medina, Shah, Wagner 2007

YH, Oda, Ohnuma, Sakamura 2008

Funatsu, Hatanaka, YH, Orikasa, Shimotani 2013

$$ds^2 = e^{-2k|y|} dx^\mu dx_\mu + dy^2$$



$$\begin{pmatrix} A_\mu \\ A_y \end{pmatrix} (x, y_j - y) = P_j \begin{pmatrix} A_\mu \\ -A_y \end{pmatrix} (x, y_j + y) P_j^\dagger$$

$$(y_0, y_1) = (0, L)$$

4D gauge bosons and Higgs

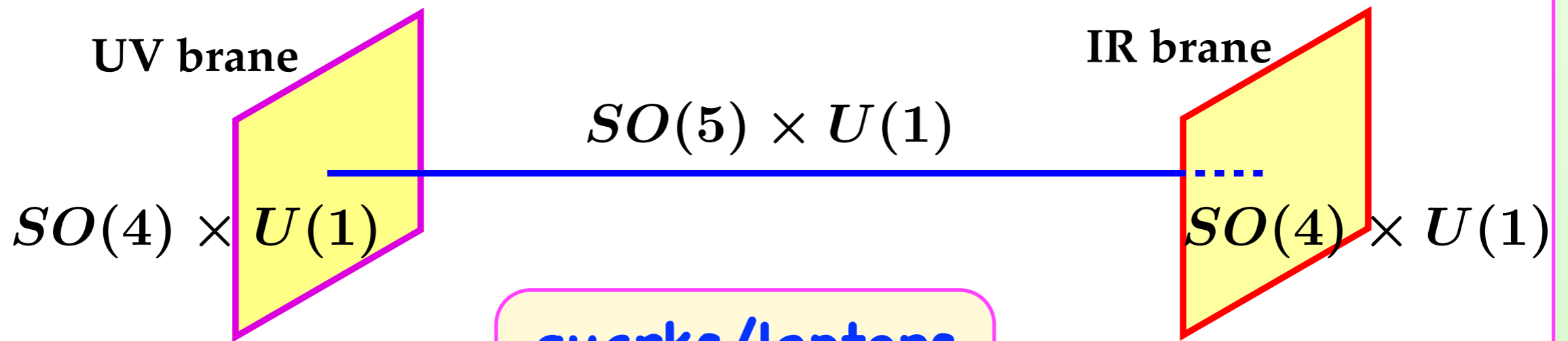
$$P_0 = P_1 = \begin{pmatrix} -1 & & & & \\ & -1 & & & \\ & & -1 & & \\ & & & -1 & \\ & & & & +1 \end{pmatrix}$$

$$SO(5) \rightarrow SO(4) \simeq SU(2)_L \times SU(2)_R$$

$$A_\mu \sim \begin{pmatrix} \boxed{W \ Z \ \gamma} \\ \phantom{\boxed{W \ Z \ \gamma}} \\ \phantom{\boxed{W \ Z \ \gamma}} \\ \phantom{\boxed{W \ Z \ \gamma}} \end{pmatrix}$$

$$A_y \sim \begin{pmatrix} \boxed{\text{Higgs}} \\ \phantom{\boxed{\text{Higgs}}} \\ \phantom{\boxed{\text{Higgs}}} \\ \phantom{\boxed{\text{Higgs}}} \end{pmatrix}$$

$$e^{i\hat{\theta}_H(x)} \sim P \exp \left\{ ig \int dy A_y \right\}$$



quarks/leptons

vector rep

dark fermions

spinor rep

Brane fermion

$$\left(\frac{1}{2}, 0\right)$$

Brane scalar

$$\hat{\Phi} \left(0, \frac{1}{2}\right)$$

$$SU(2)_L \times U(1)_Y$$



$$U(1)_{EM}$$

Success

Gauge principle for Higgs boson

m_H : generated at 1 loop, and finite
Gauge-hierarchy prob. solved.

Almost SM at low energies for $\theta_H < 0.1$

No vacuum instability

$$V_{\text{eff}}(\theta_H + 2\pi) = V_{\text{eff}}(\theta_H)$$

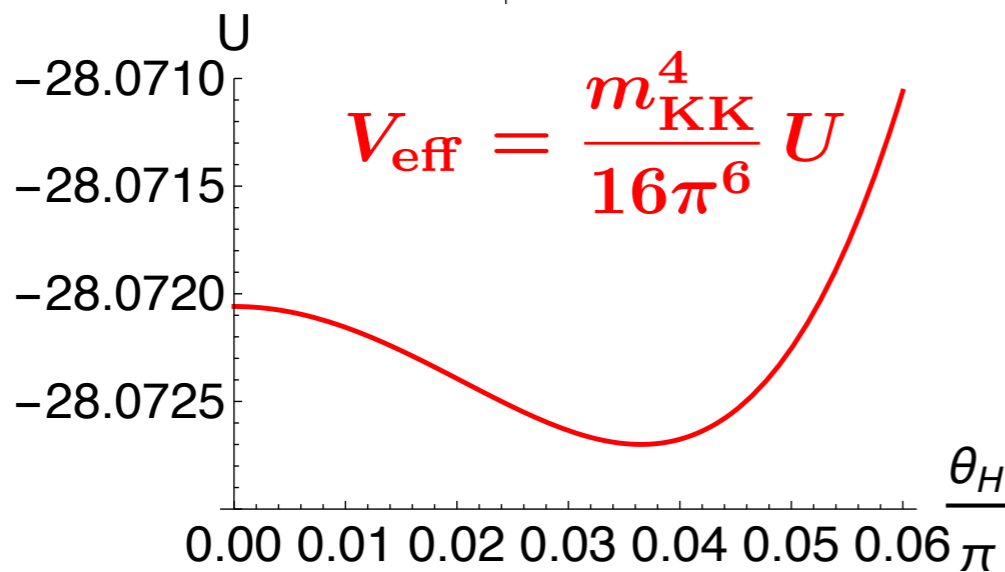
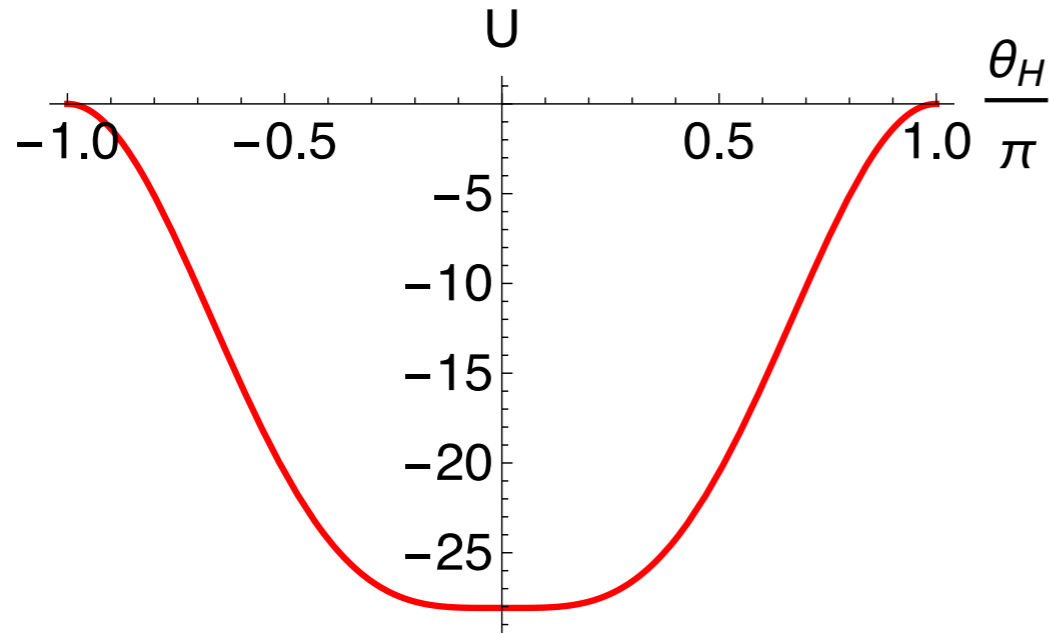
Dynamical EW sym. breaking

Two scales

KK scale $m_{\text{KK}} = \pi k e^{-kL} \sim \frac{\pi \sqrt{kL}}{\sin \theta_H} m_W$
 $\sim 7 - 10 \text{ TeV}$

Weak scale $m_W \sim 80 \text{ GeV}$

EW sym breaking



$$z_L = 10^5, \theta_H = 0.115$$

$$\theta_H = 0.115 \text{ (example)}$$

$$m_Z, \alpha, \sin^2 \theta_W$$

$$\rightarrow m_{KK} = 7.41 \text{ TeV}$$

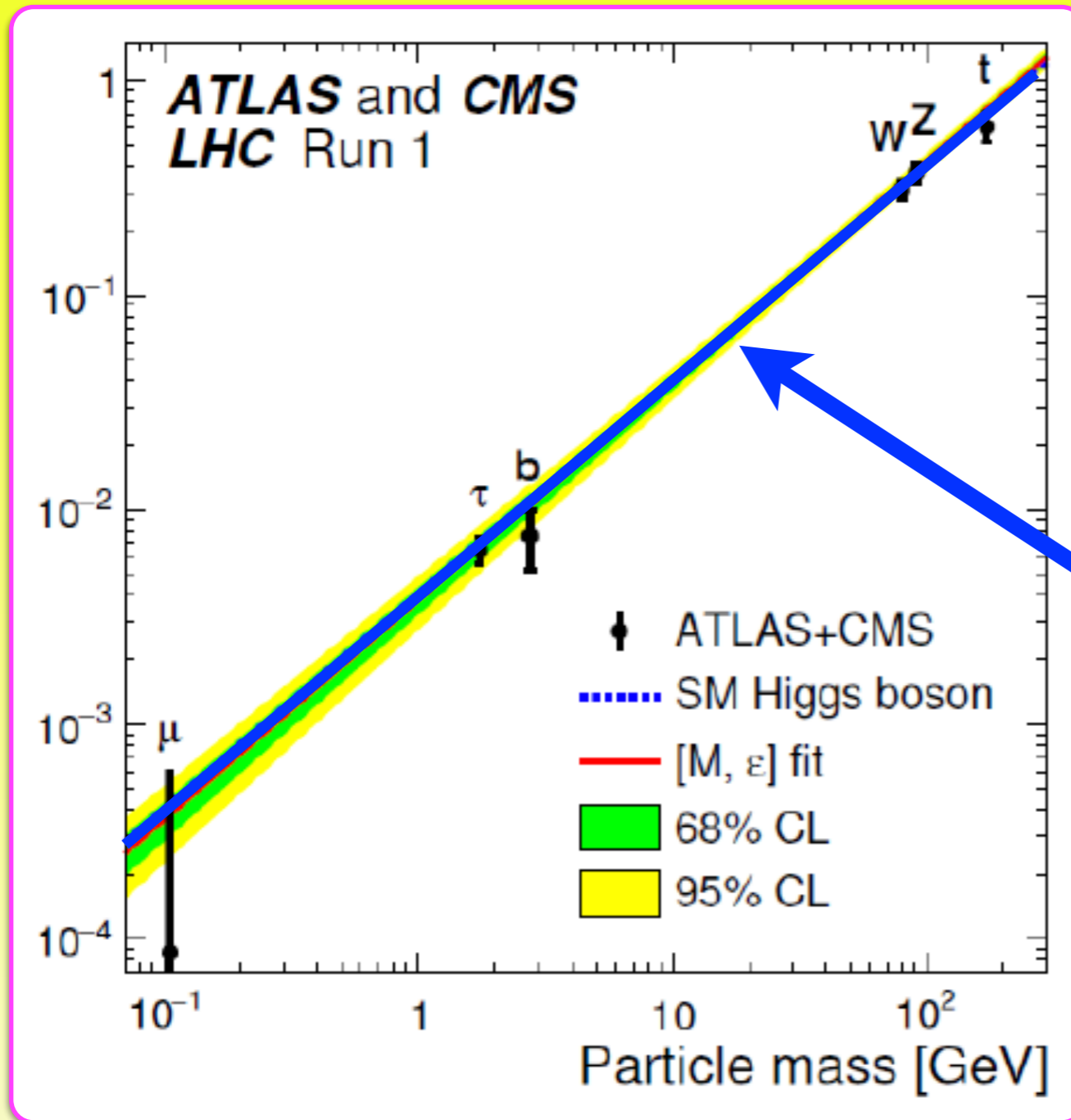
$$m_t = 171 \text{ GeV}, m_H = 125 \text{ GeV}$$

$$\rightarrow c_t = 0.227, c_F = 0.332$$

$$m_\tau, m_e = 0.511 \text{ MeV}$$

$$\rightarrow c_\tau = 0.950, c_e = 1.72$$

Predictions



**Higgs
Hff, HWW, HZZ
couplings**

$$\sim (\text{SM}) \times \cos \theta_H$$

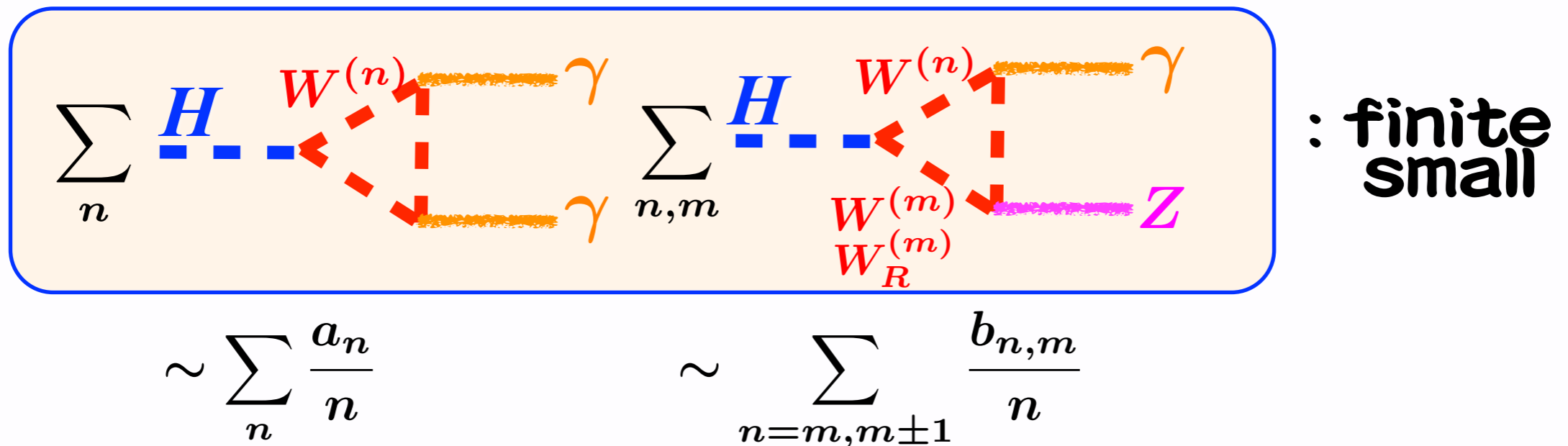
Gauge-Higgs

$$(\theta_H \sim 0.1)$$

Higgs decay $H \rightarrow j$

$$\mu \sim \mu_{\text{SM}} \cdot \cos^2 \theta_H$$

$$BR \sim BR_{\text{SM}}$$

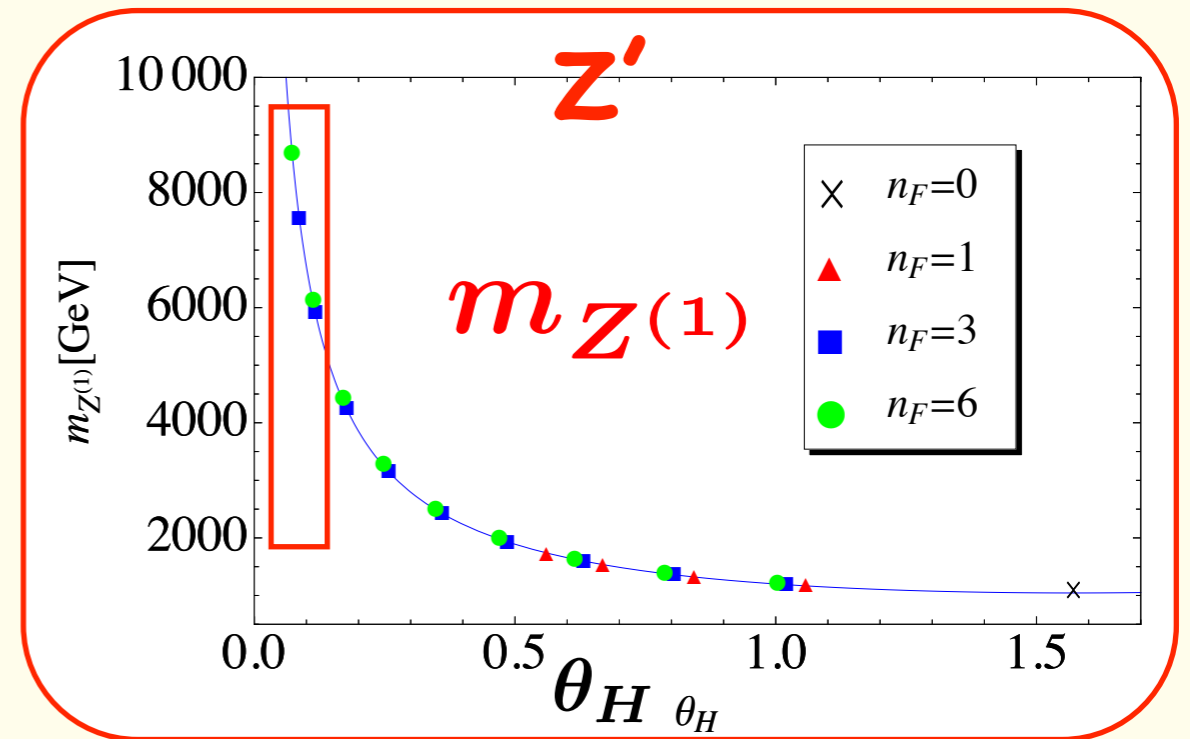
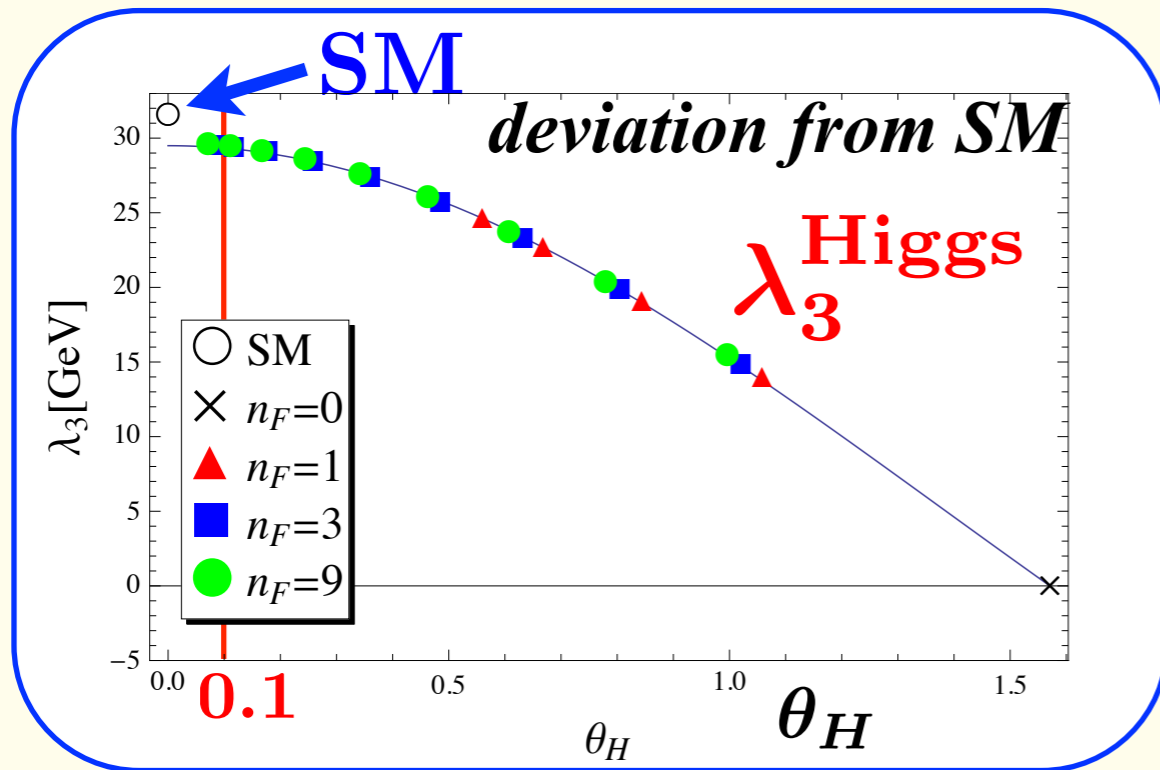


Funatsu, Hatanaka, YH, Oriksa, Shimotani 1301.1744 (PLB)

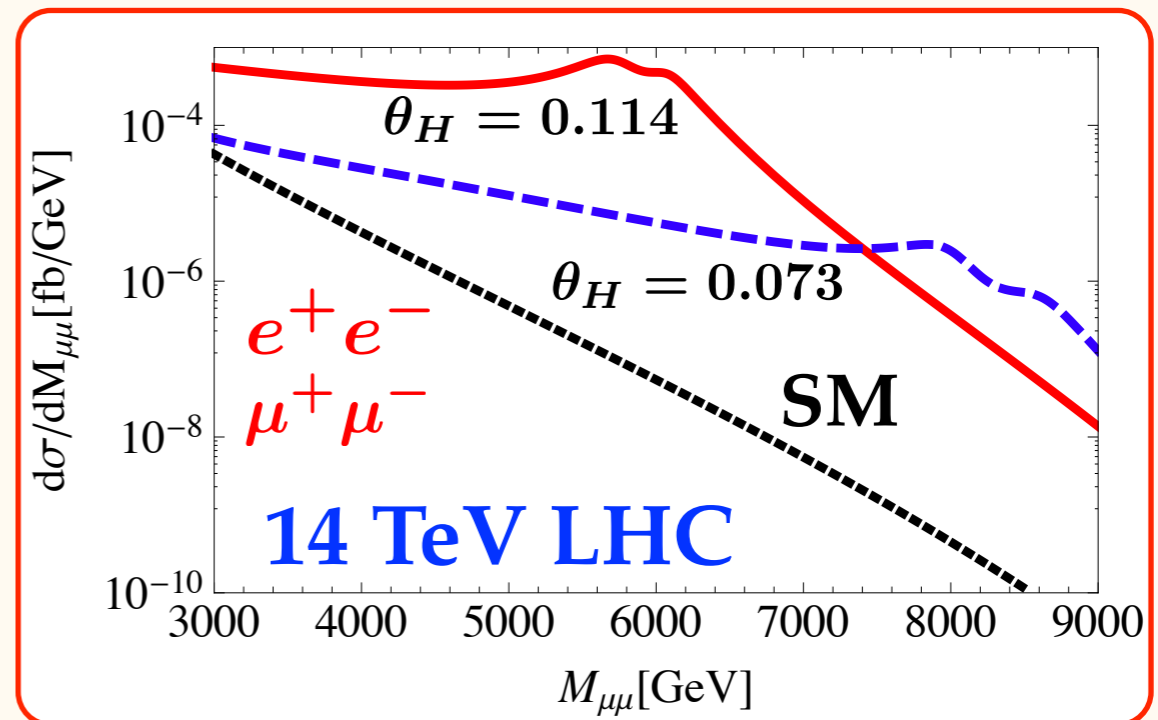
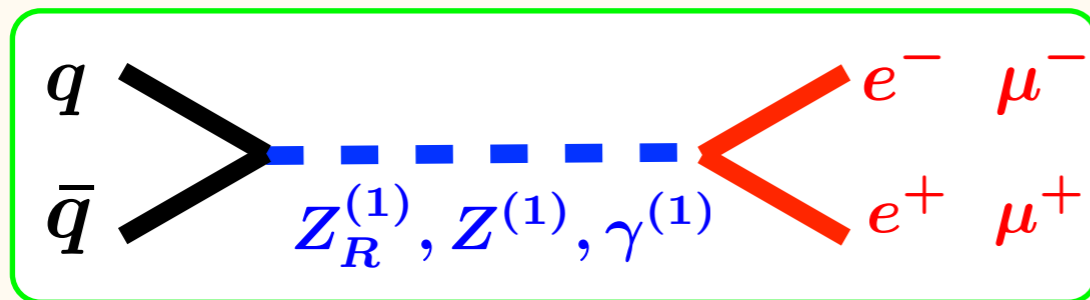
Funatsu, Hatanaka, YH 1510.06550 (PRD)

Universality

$$m_{KK}(\theta_H), m_{Z^{(1)}}(\theta_H), \lambda_3^H(\theta_H), \lambda_4^H(\theta_H)$$



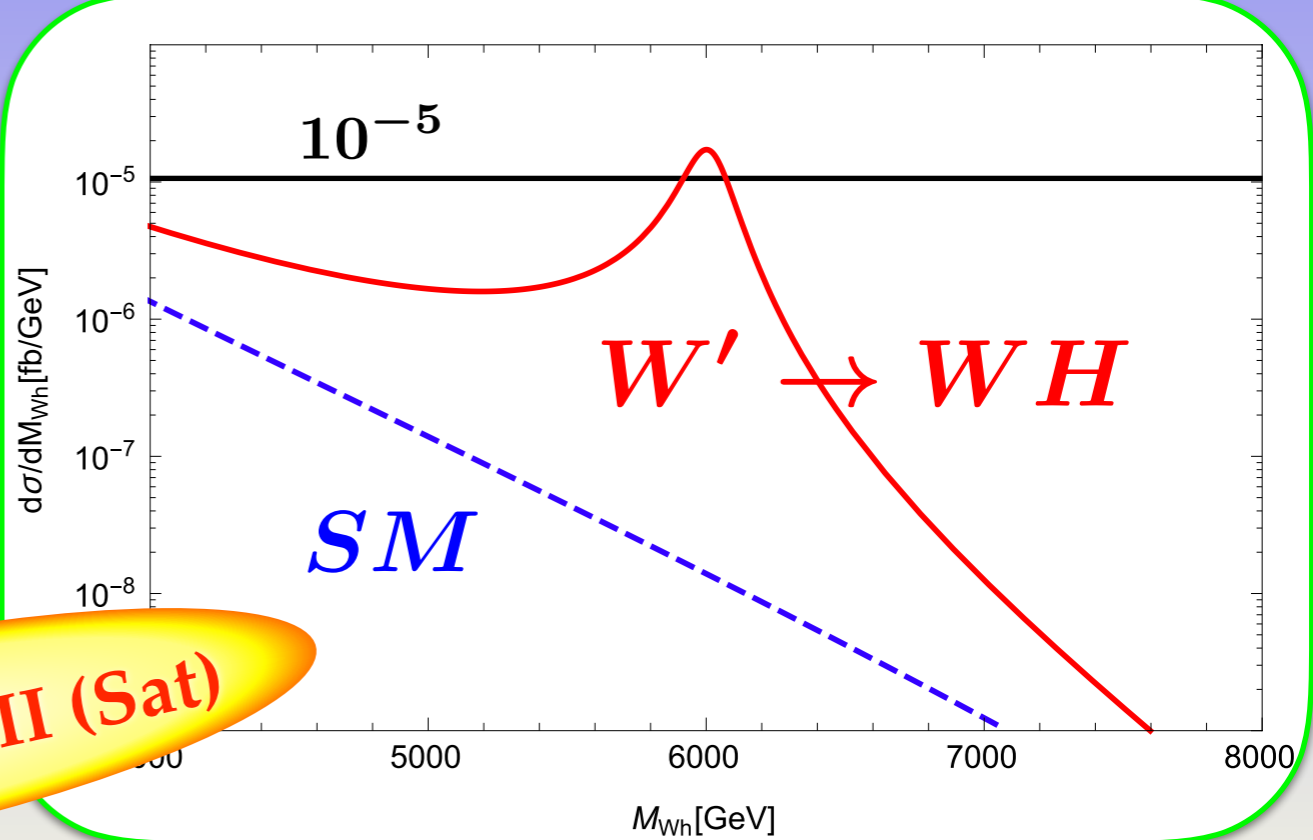
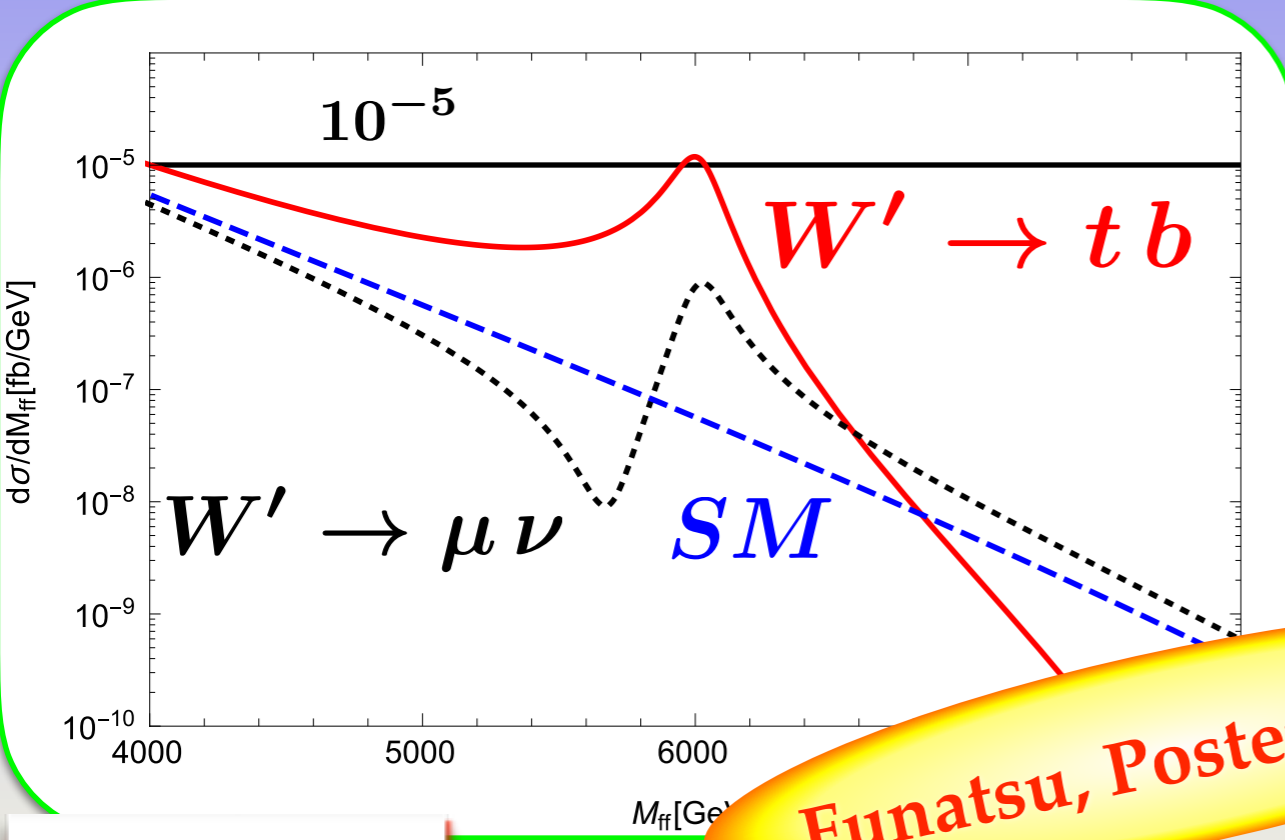
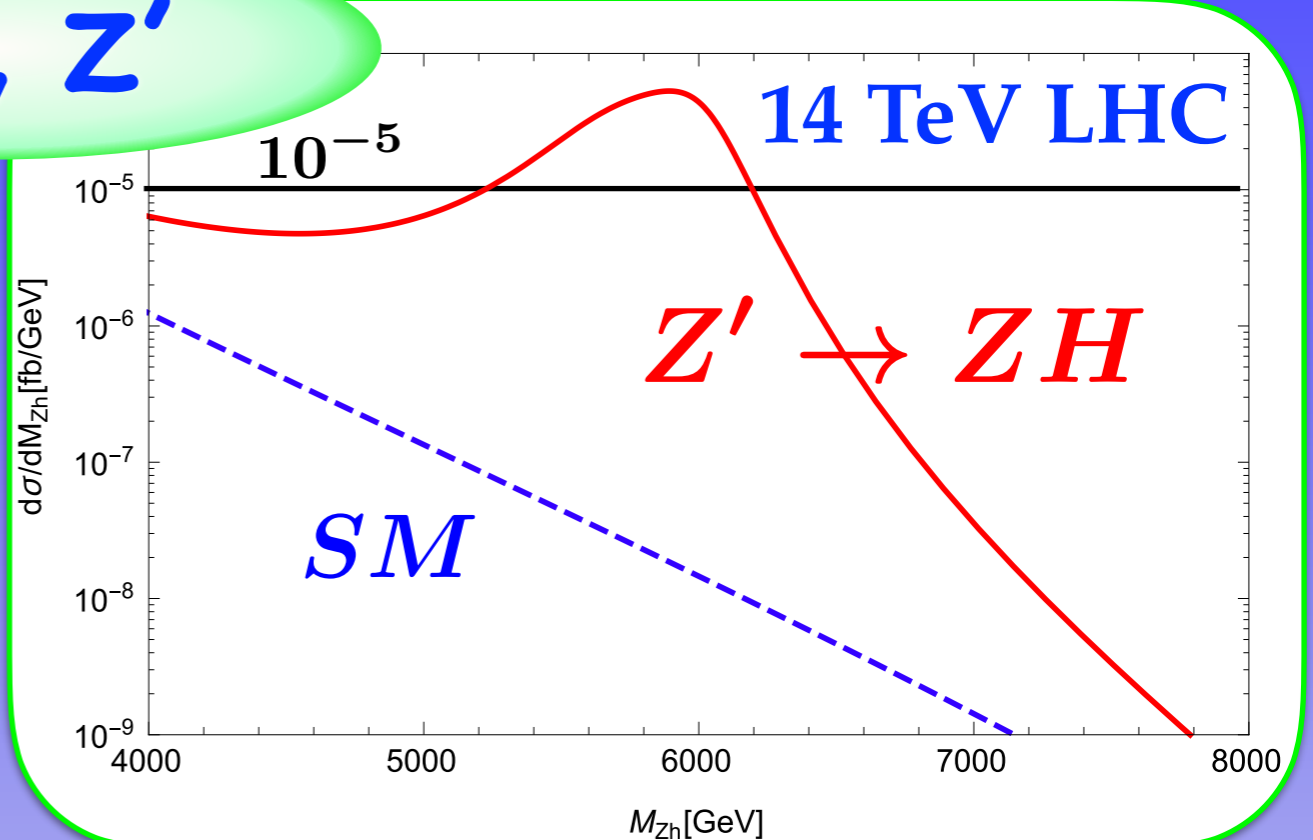
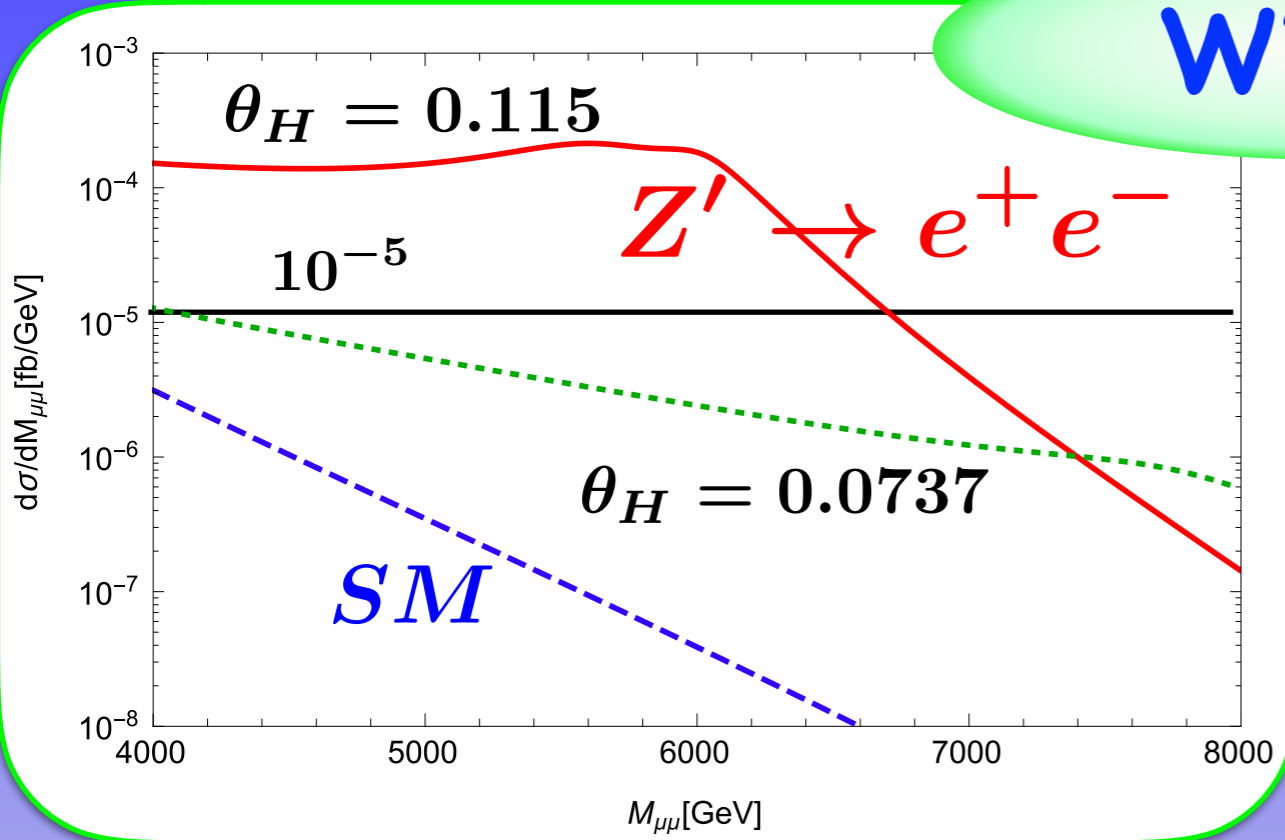
Z'



	$\theta_H = 0.114$		$\theta_H = 0.073$	
Z'	m (TeV)	Γ (GeV)	m (TeV)	Γ (GeV)
$Z_R^{(1)}$	5.73	482	8.00	553
$Z^{(1)}$	6.07	342	8.61	494
$\gamma^{(1)}$	6.08	886	8.61	1040

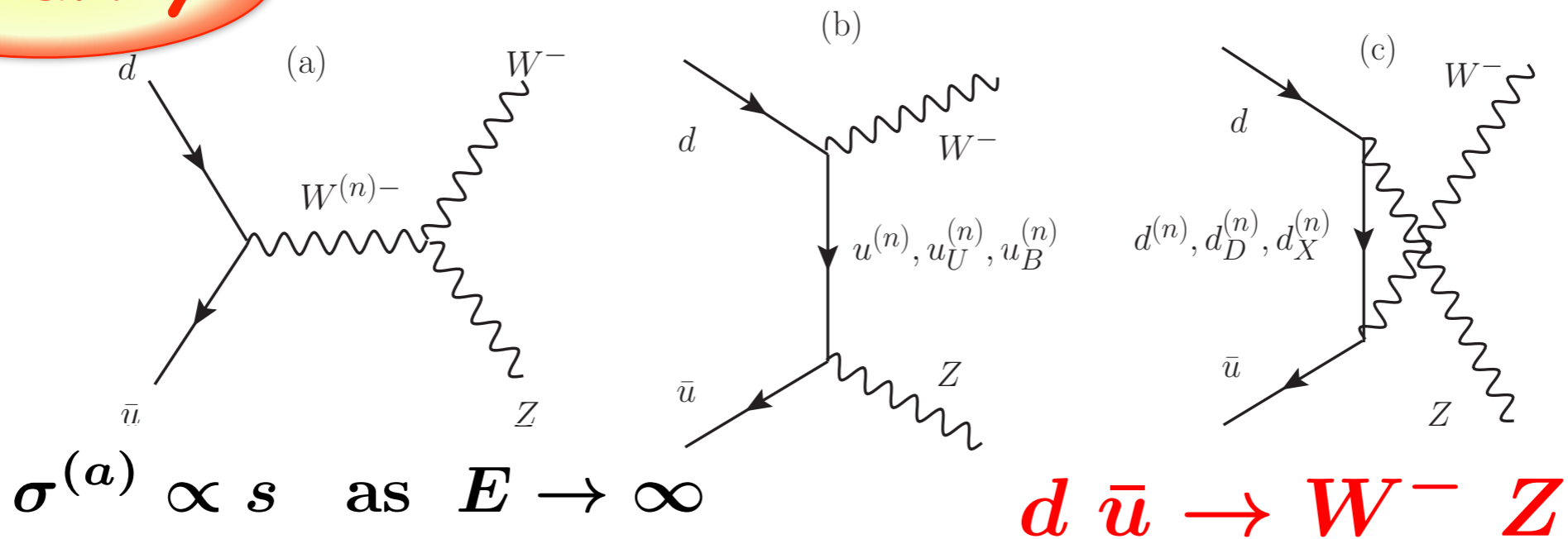
Funatsu, Hatanaka, YH, Oriksa, Shimotani 1404.2748 (PRD)

W', Z'



Funatsu, Poster II (Sat)

Unitarity



Canceled in $\mathcal{M}_s + \mathcal{M}_t + \mathcal{M}_u$?

$$\sum_{n=0}^{\infty} g_{W^{(n)}ud}^L g_{W^{(n)}WZ} \simeq \sum_{u'} g_{Wdu'}^L g_{Zuu'}^L - \sum_{D'} g_{ZdD'}^L g_{WuD'}^L$$

$$\sum_{n=0}^4 \rightarrow 0.877162 g_w^2 / \sqrt{2} \qquad 0.877163 g_w^2 / \sqrt{2}$$

(for $\theta_H = 0.115$)

$$g_{W^{(n)}ud}^L / (g_w / \sqrt{2}) = 1.00019 (n=0), \quad -0.3455 (n=1)$$

$$g_{W^{(n)}WZ} / (g_w \cos \theta_W) = 0.99999998 (n=0), \quad -7.35 \times 10^{-4} (n=1)$$

What is next?

ILC

Forward-backward asymmetry

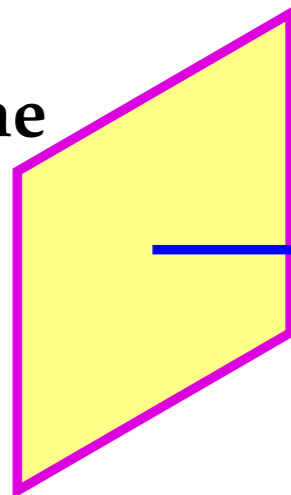
at 500 GeV, 1 TeV

Funatsu, Hatanaka, YH, Orikasa

Gauge-Higgs grand unification

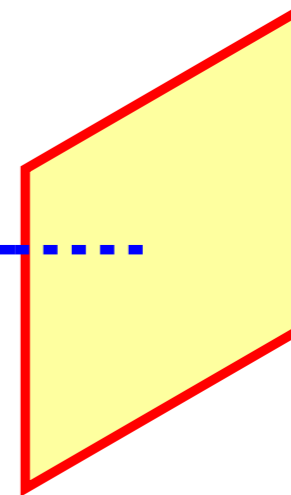
Gauge-Higgs grand unification in 5d/6d

UV brane



SO(11) GHU in 5d RS

IR brane



$$ds^2 = e^{-2k|y|} dx^\mu dx_\mu + dy^2$$

YH, Yamatsu, 1504.03817 (PTEP)
Furui, YH, Yamatsu, 1606.07222 (PTEP)

SO(11) GHU in 6d hybrid-warped space

$$ds^2 = e^{-2k|y|} (dx^\mu dx_\mu + dv^2) + dy^2$$

6th dim

5th dim

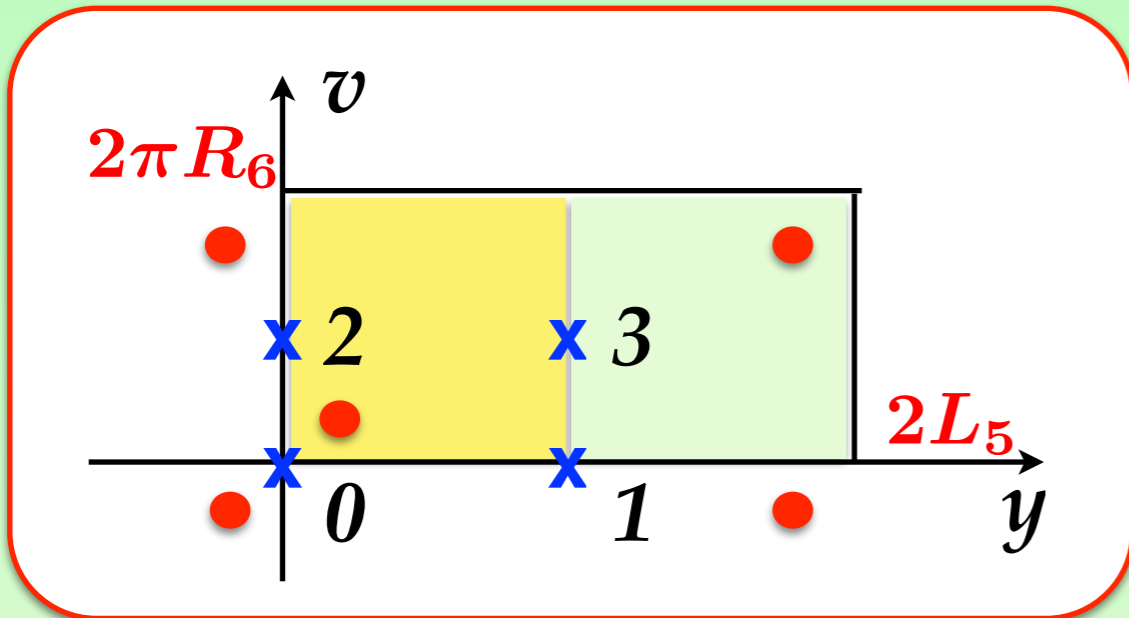
$$v \sim v + 2\pi R_6$$

$$y \sim y + 2L_5$$

$$(-y, -v) \sim (y, v)$$

YH, Yamatsu (in preparation)

In 6d

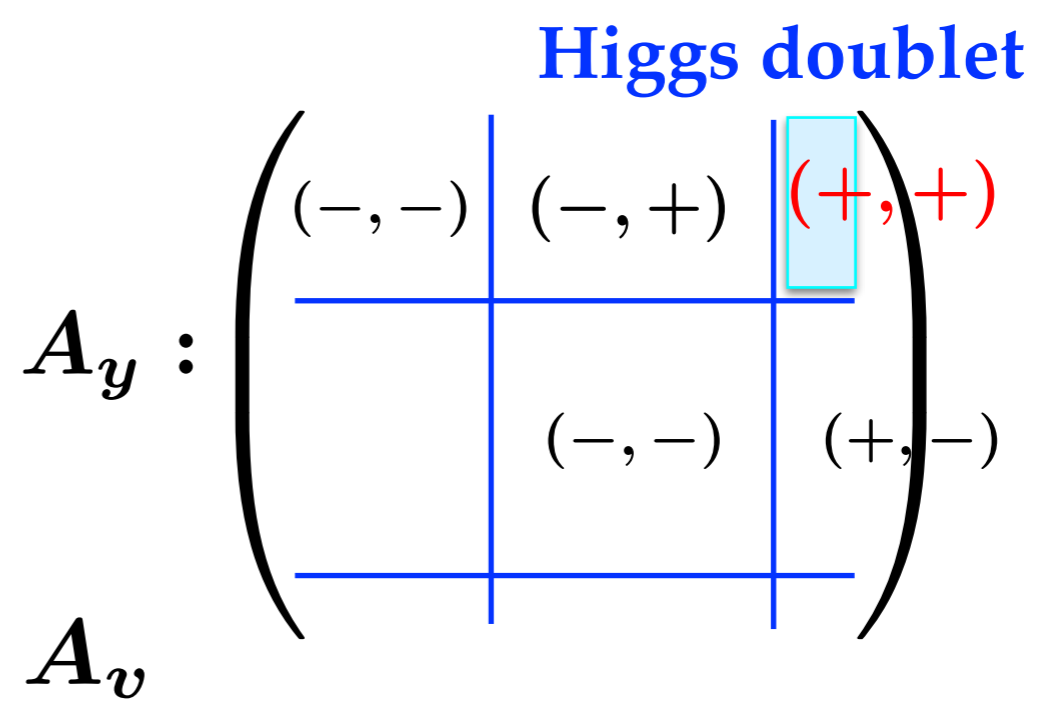
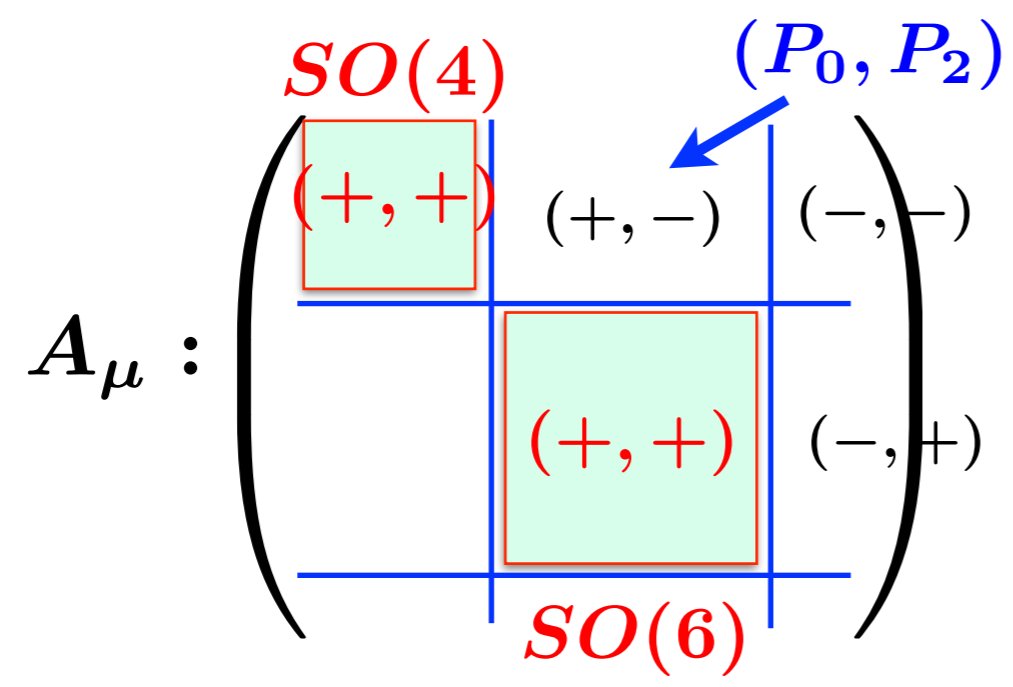


$$P_0 = P_1 = \begin{pmatrix} I_4 & \\ & -I_7 \end{pmatrix}$$

$$P_2 = P_3 = \begin{pmatrix} I_{10} & \\ & -1 \end{pmatrix}$$

$$m_{KK}^{(5)} = \pi k e^{-kL_5} \ll \frac{1}{R_6}$$

~ 10 TeV GUT scale



Matter content

In 6d bulk

$$\Psi_{32} \quad \Psi_{11}$$

Quarks & Leptons

In 5d UV brane
at $y=0$

$$\Psi_1$$

$$\Phi_{32} \quad SO(10) \rightarrow SU(5)$$

$$\Psi_{32} = \begin{pmatrix} \Psi_{16} \\ \Psi_{\overline{16}} \end{pmatrix}$$

$$\Psi_{16} = \begin{pmatrix} \nu \\ e \\ \hat{e} \\ \hat{\nu} \\ u_j \\ d_j \\ \hat{d}_j \\ \hat{u}_j \end{pmatrix} \begin{pmatrix} \nu_L \\ e_L \\ \text{zero modes} \\ u_{jL} \\ d_{jL} \end{pmatrix}$$

$$\Psi_{\overline{16}} = \begin{pmatrix} \nu' \\ e' \\ \hat{e}' \\ \hat{\nu}' \\ u'_j \\ d'_j \\ \hat{d}'_j \\ \hat{u}'_j \end{pmatrix} \begin{pmatrix} \nu_R \\ e_R \\ \text{zero modes} \\ u_{jR} \\ d_{jR} \end{pmatrix}$$

$$p \not\rightarrow \pi^0 e^+$$

$$N_\Psi = 3 \quad N_\Psi = -1$$

no proton decay

in the absence of Ψ_1

**Gauge-Higgs seesaw mechanism
for neutrino masses**

with Ψ_1

Summary

$SO(5) \times U(1)$ gauge-Higgs EW unification

Higgs = gauge boson in 5d

13/14 TeV LHC: Higgs, Z' , W' (6 - 8 TeV)

$SO(11)$ gauge-Higgs grand unification