

# Threshold corrections to the heavy Higgs decay

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# Introduction: Heavy Higgs Searches

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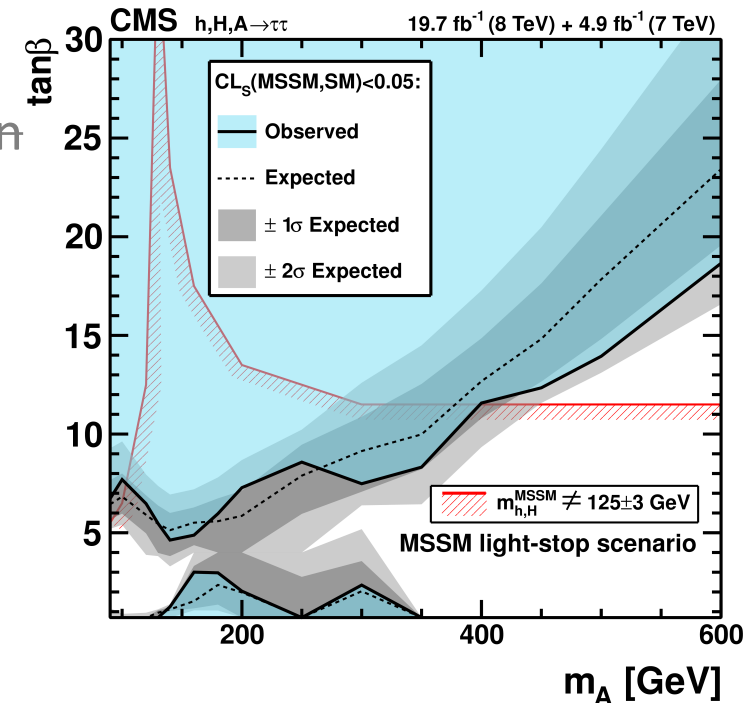
At the LHC experiments, we have found only the 125 GeV Higgs so far. ~~2 TeV diboson, 750 GeV diphoton~~

Searches for heavy Higgs bosons in the extended Higgs sector (2HDM, HTM, HSM, ...):

$$H, A, H^\pm, H^{\pm\pm}, S, \dots$$

MSSM neutral Higgs searches in  $H/A \rightarrow \tau\tau$  mode  
→ stringent bound in the  $m_A$ - $\tan\beta$  plane.

**$m_A \sim 2m_t$  still open for  $\tan\beta \sim \mathcal{O}(1)$**



CMS-HIG-13-021, ATLAS-CONF-2016-085, ...

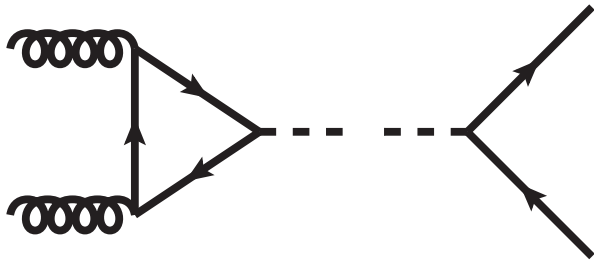
We study the threshold effects to the production and decays of neutral Higgs bosons with  $m_A \sim 2m_t$ .

[focus on pseudoscalar (S-wave), but neglect scalar (P-wave)]

Mixing of A and  $t\bar{t}$  bound-states / interference effects in the production-decay are not implemented yet.

Drees, Hikasa(90), talk by C. Zhang

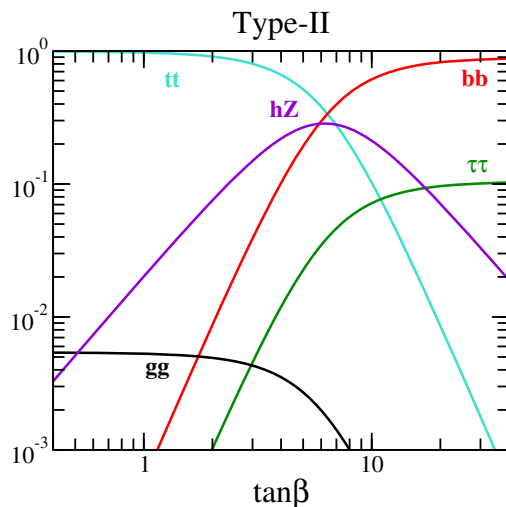
# Heavy Higgs Production & Decay



Yukawa interactions [in 2HDM]

$$\mathcal{L}_Y = \sum_f \xi_A^f \frac{y_f}{\sqrt{2}} \bar{f} [i\gamma_5] f A$$

$\xi_A^t = \cot \beta,$   
 (Type-II)  $\xi_A^{b,\tau} = \tan \beta$



Example:

$$m_A = 400 \text{ GeV},$$

$$\sin(\beta - \alpha) = 0.99,$$

$$m_H, m_{H^\pm} \gtrsim m_A$$

## Production processes

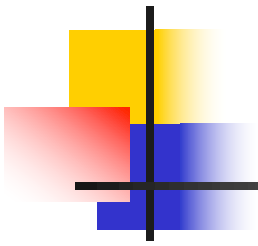
- ☺  $gg \rightarrow A$ , **loop-induced, the largest**
- $q\bar{q} \rightarrow HA$ ,
- $q\bar{q}' \rightarrow H^\pm A$ ,
- $gg(q\bar{q}) \rightarrow q\bar{q}A$ ,

...

☺ threshold corrections

## Decay channels

- ☺  $A \rightarrow t\bar{t}$ ,
  - $A \rightarrow b\bar{b}$ ,
  - $A \rightarrow \tau^- \tau^+$ ,
  - $A \rightarrow hZ$ , **gauge coupling [ $\propto \cos(\beta - \alpha)$ ]**
- } Yukawa couplings
- ☺  $A \rightarrow gg$ ,
  - ☺  $A \rightarrow \gamma\gamma$ ,
  - ☺  $A \rightarrow Z\gamma$ ,
- } loop-induced
- ...



# A → tt: Perturbative Calculations

$$A \rightarrow t\bar{t}^{(*)}$$

Important even below  $m_A \sim 2m_t$   
through off-shell top-quarks

$$\Gamma_{A \rightarrow t\bar{t}} \simeq \text{Im} \left[ \text{---} \bigcirc \text{---} \right]$$

**LO, NLO** calc. for tt/bWbW

Drees,Hikasa(90); MG5\_aMC@NLO

$$\Gamma_{A \rightarrow t\bar{t}} \simeq m_A \beta \left[ 1 + \frac{\alpha_s}{\pi} C_F \left( \frac{\pi^2}{2\beta} - 3 + \dots \right) + \dots \right]$$

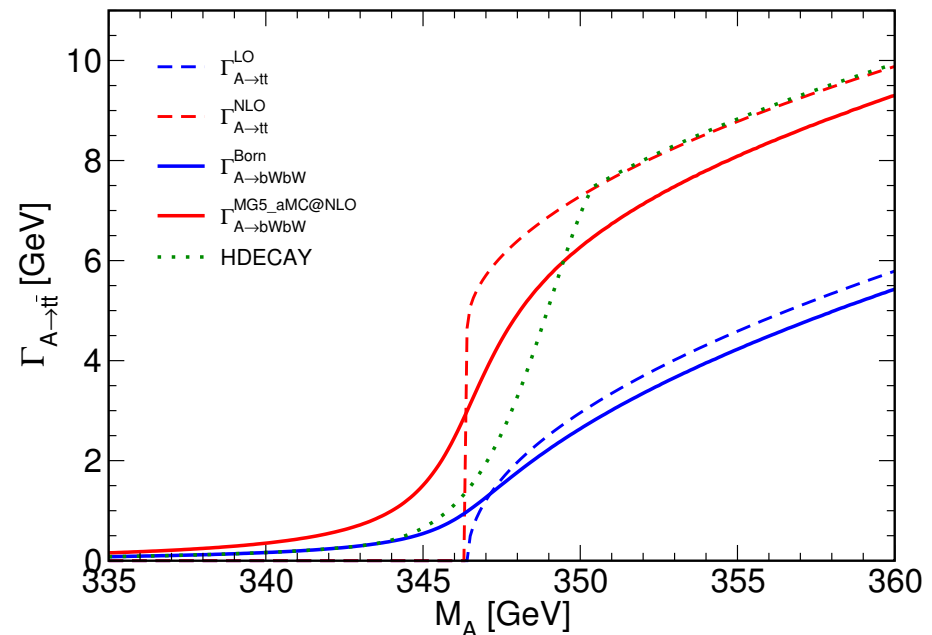
$$\beta = \sqrt{1 - \frac{4m_t^2}{m_A^2}}$$

**HDECAY**: (above thr.) tt@NLO

(below thr.) tbW@LO

Djouadi,Kalinowski,Spira(97)

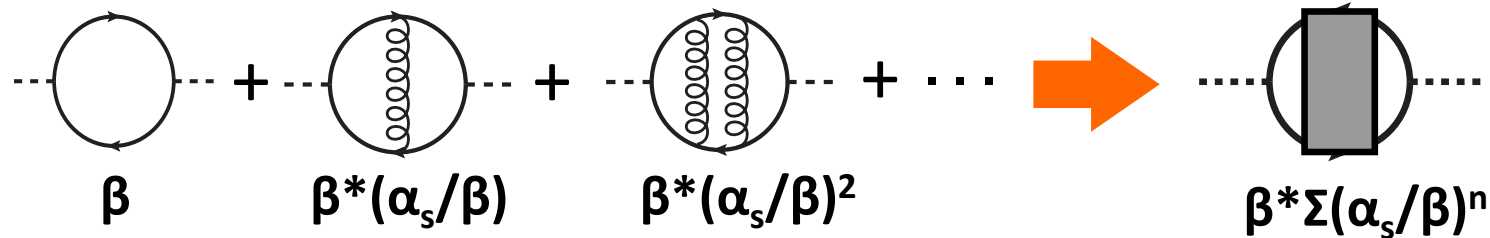
Large QCD correction near threshold,  
because of Coulomb singularity.



# A → tt: Coulomb Resummation

Non-relativistic Green function

$$G(E) \simeq \frac{i}{2N_c} \int d^4x e^{iEt} \langle 0 | T \{ j_p(x) j_p(0) \} | 0 \rangle$$



$$\Gamma_{A \rightarrow t\bar{t}} \simeq y_t^2 \text{Im}[G(E)]$$

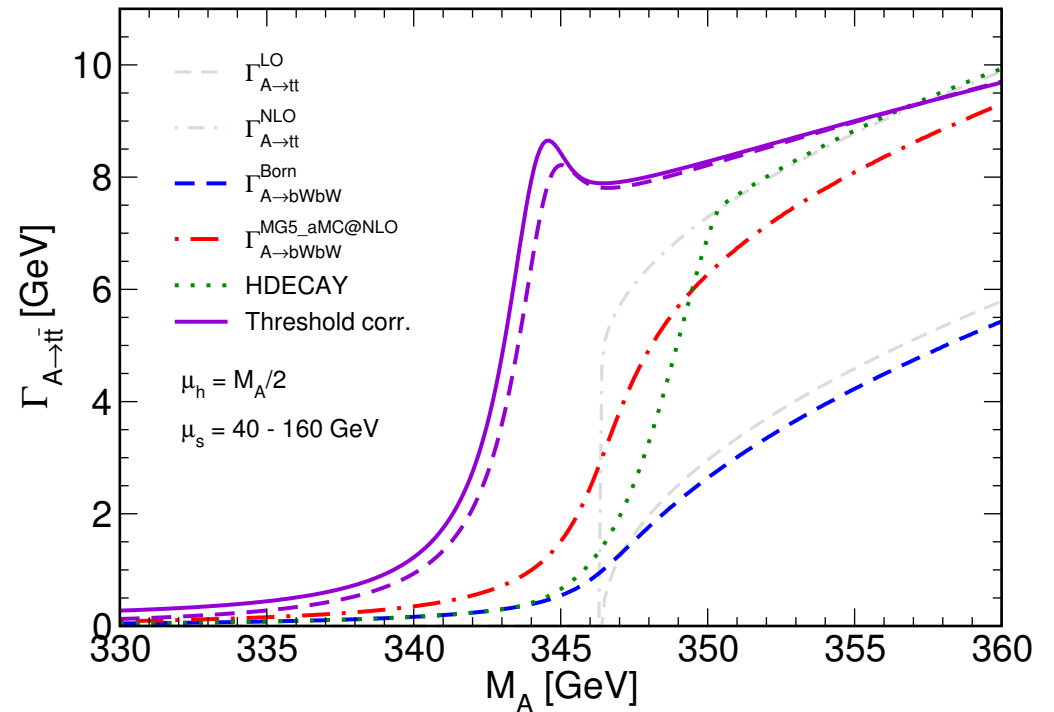
**Schrodinger Eq.** with QCD potential:

Fadin, Khoze (87,88)

$$\left[ \left\{ -\frac{\nabla^2}{m_t} + V(r) \right\} - \mathcal{E} \right] G_c(\vec{r}, \mathcal{E}) = \delta^3(\vec{r})$$

$$\mathcal{E} = E + i\Gamma_t$$

$$V(r) = -C_F \frac{\alpha_s}{r} \left[ 1 + \frac{\alpha_s}{4\pi} \{ \dots \} + \dots \right]$$



# Loop-induced decays

$$A \rightarrow \gamma\gamma, gg, Z\gamma$$

Spira,Djouadi,Graudenz,Zerwas(95);  
Harlander,Kant(05);  
Aglietti,Bonciani,Degrassi,Vicini(07);

1-loop/2-loop top-loop func.

$\gamma\gamma$ : analytic 2-loop correction known  
 $gg/Z\gamma$ : 2-loop numerically (we use 1-loop amp.)

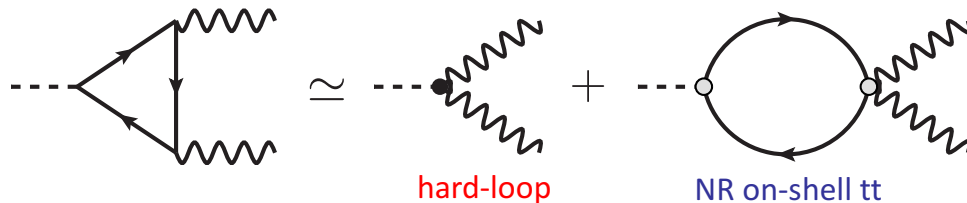
Re[F]

$$\mathcal{F}_{A \rightarrow \gamma\gamma,t}(v) = \mathcal{F}_t^{(0)}(v) + \frac{\alpha_s}{\pi} \mathcal{F}_t^{(1)}(v)$$

$$v = \sqrt{1 - \tau}, \quad \tau = 4m_t^2/m_A^2$$

Im[F]

**Threshold expansion  $\rightarrow$  Coulomb summation**



$$\mathcal{F}_{A \rightarrow \gamma\gamma,t}^{\text{NR}}(v) = \mathcal{A}_t(\alpha_s) + \mathcal{B}_t(\alpha_s)G(E)$$

Melnikov,Spira,Yakovlev(94)



# Numerical Results

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$$\boxed{\Gamma^{\text{thr.}} / \Gamma^{\text{pert.}}} \quad \text{for } A \rightarrow t\bar{t}, \gamma\gamma, gg, Z\gamma$$

thr./LO

thr./NLO

Production:  $\sigma(gg \rightarrow A)$  also roughly  $\times 2 \sim 3$

# Summary and Outlook

- We studied the threshold corrections to the heavy Higgs decays and production for  $m_A \sim 2m_t$ .
- Near the heavy quark mass threshold, large Coulomb corrections arise, which have to be resummed to all orders in  $\alpha_s$ .
- We formulated the threshold-correction based on NRQCD, and investigated a numerical impact of these corrections.

$$\frac{\Gamma_{A \rightarrow t\bar{t}}^{\text{thr.}}}{\Gamma_{A \rightarrow t\bar{t}}^{\text{pert.}}} \simeq 10 - 20 \quad \frac{\Gamma_{A \rightarrow \gamma\gamma, gg, Z\gamma}^{\text{thr.}}}{\Gamma_{A \rightarrow \gamma\gamma, gg, Z\gamma}^{\text{pert.}}} \simeq 2 - 3 \quad @ m_A \sim 2m_t$$

- For a phenomenological application, both the production and decay have to be considered simultaneously.  
 $\Rightarrow$  mixing of A &  $t\bar{t}$ -state / large interference effects.