

Natural SUSY at the ILC: from MZ to the GUT scale

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Outline

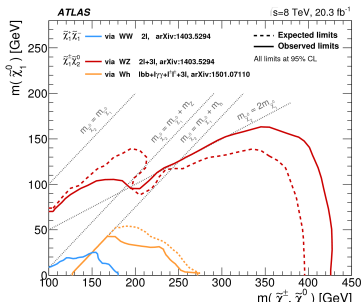
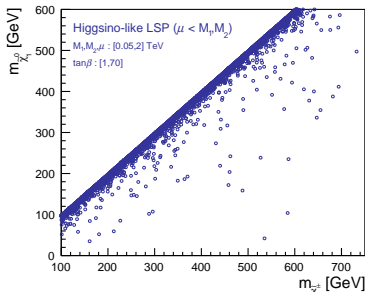
- 1 Light higgsinos: Motivation
- 2 The ILC
- 3 Measurements at the International Linear Collider
- 4 Probing the GUT-scale at ILC (& LHC)
 - Need to add the Higgs
 - Unification, Discrimination, Prediction
- 5 Conclusions

Why study light higgsinos

- The superpartners of un-coloured SM bosons mix to $\tilde{\chi}_{1-4}^0$ and $\tilde{\chi}_{1-2}^\pm$, governed by μ , M_1 , M_2 , $\tan\beta$.
- Naturalness and small fine tuning require μ parameter at the EW scale:

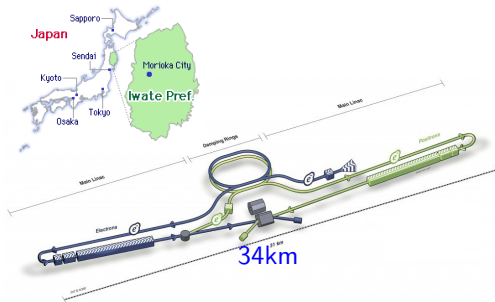
$$m_{\tilde{Z}}^2 = 2 \frac{m_{H_d}^2 + \Sigma_d^d - (m_{H_u}^2 + \Sigma_u^u) \tan^2 \beta}{\tan^2 \beta - 1} - 2\mu^2$$

- μ small \Rightarrow light higgsinos. Typical mass difference 10 - 20 GeV
- \Rightarrow challenging for LHC if other sparticles are heavy



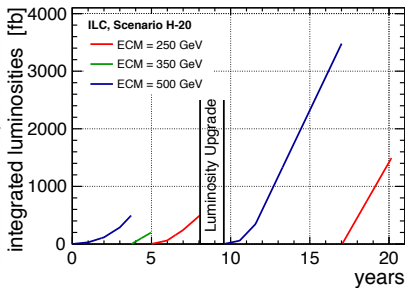
What is the International Linear Collider (ILC)

- Electron-positron collider at $\sqrt{s} = 250 - 500\text{GeV}$ (1TeV)
- Polarisation of electrons 80%, positrons 30%
- Well-defined initial state: 4-momentum and spin configuration.
- Clean and completely reconstructable final state
- Almost 4π detector coverage. **No trigger needed**
- Under political consideration in Japan



Typical 20yr running scenario

Integrated Luminosities [fb] arXiv:1506.07830



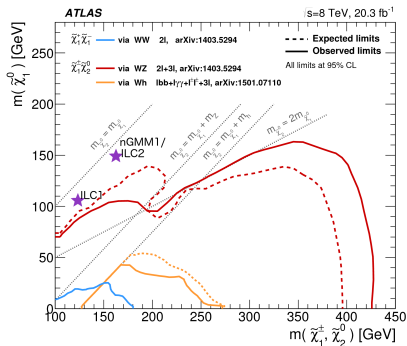
Benchmarks studied

- $\tilde{\chi}_1^0, \tilde{\chi}_2^0, \tilde{\chi}_1^\pm$ observable, in ILC1 $\tilde{\chi}_3^0$ accessible with a small cross section
- Other sparticles heavy
- Mass gaps $\sim 10 - 20$ GeV \Rightarrow higgsinos decay via a virtual Z/W

Masses (GeV) in three benchmarks

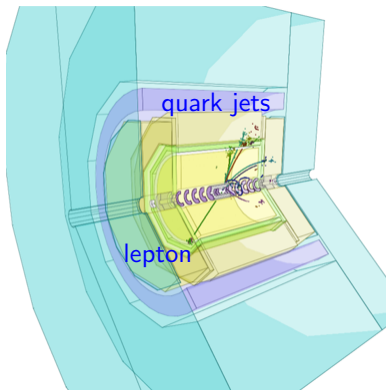
	ILC1	ILC2	nGMM1
$\tilde{\chi}_1^0$	103	148	151
$\tilde{\chi}_1^\pm$	117	157.8	159
$\tilde{\chi}_2^0$	124	158.3	156
$\tilde{\chi}_3^0$	267	539	1530
\tilde{g}	1560	2830	2860

Cross sections for production in e^+e^- at $\sqrt{s} = 500$ GeV several hundred fb



Detailed simulation study: 500 GeV, 500 fb⁻¹

$e^+e^- \rightarrow \tilde{\chi}_1^+ \tilde{\chi}_1^- \rightarrow \tilde{\chi}_1^0 q \bar{q}' \tilde{\chi}_1^0 e \nu_e$
 in the International Large Detector

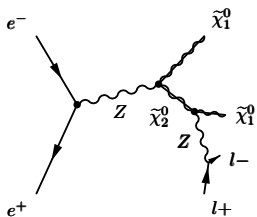


Soft tracks - no problem for ILC

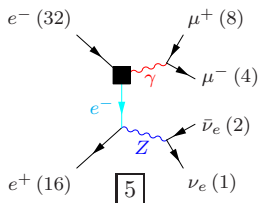
- Event generation Whizard 1.95, hadronisation Pythia 6.422
- Detailed ILD-specific software for simulation and reconstruction (Mokka & Marlin)
- Beam spectrum, ISR and $\gamma\gamma$ “pile-up” included

Neutralino measurement

- Neutralino signal: $e^+e^- \rightarrow \tilde{\chi}_1^0\tilde{\chi}_2^0 \rightarrow \tilde{\chi}_1^0\tilde{\chi}_1^0 e^+e^- (\mu^+\mu^-)$
- Characterised by large missing energy and two fermions in the final state
- Main background 4-fermion processes $\nu\nu ll$



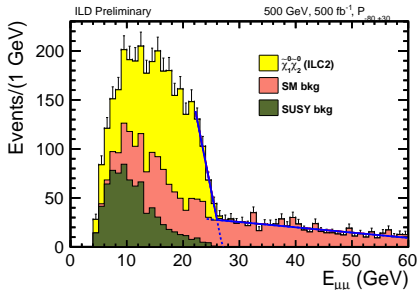
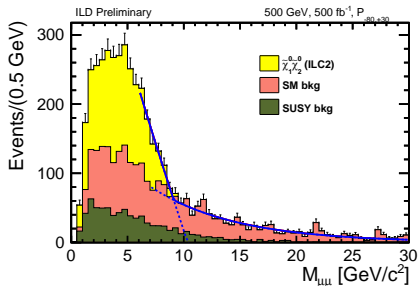
Neutralino signal



Background example

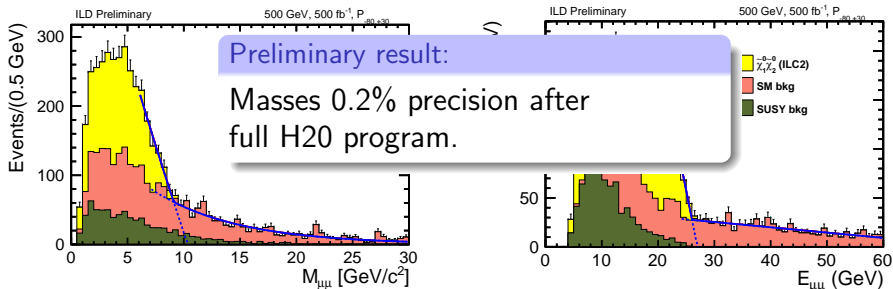
Mass extraction

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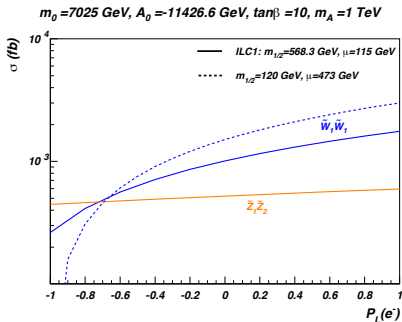
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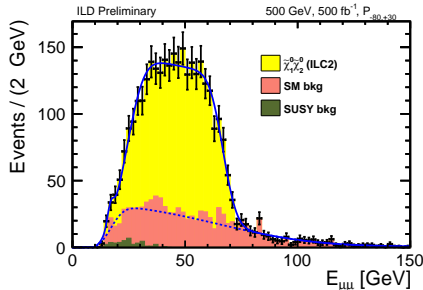
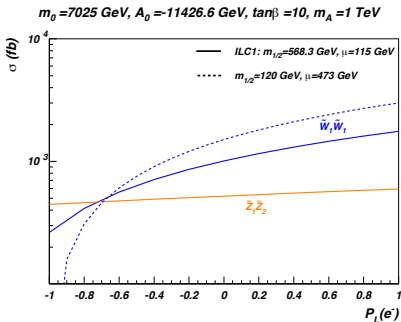
Cross section measurement

- Measure with different polarisation combinations
- Polarisation dependence reveals higgsino nature
- Strategy: Fit overall shape to count events



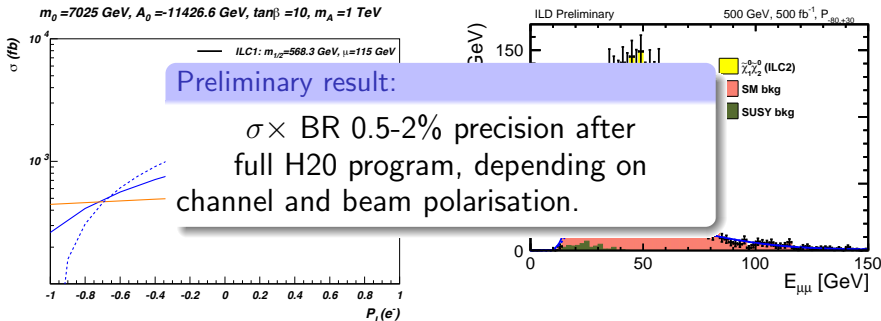
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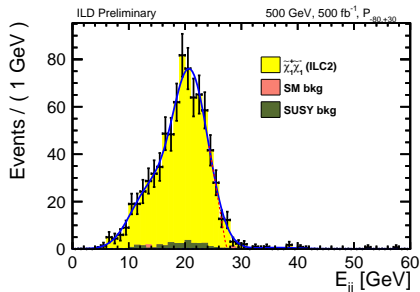
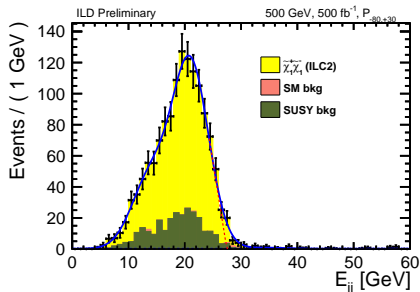
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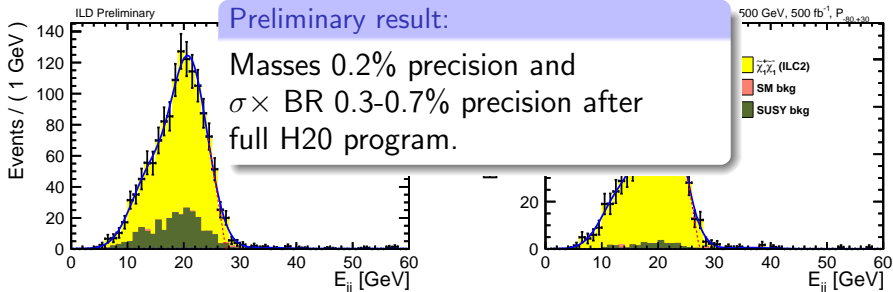
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Probing the GUT scale

So, we have three masses and four cross-section (two processes \times two beam-polarisations), with permit to percent precision.

- What can we say about **SUSY parameters** based on these observables?
- Which parameters are determined and how accurately?
- Can we test the **SUSY model type**?
- Can we make predictions about the **unobserved part** of the spectrum?
- Is there more to be used from the ILC data?

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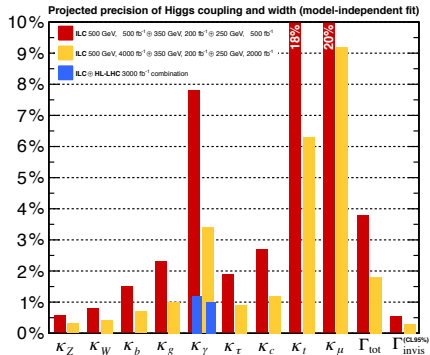
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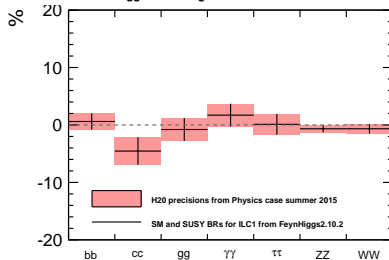
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Probing the GUT scale: Higgs is important!

- Assume ILC will measure m_h to 15 MeV precision
- No deviation from SM BRs but still important for the fit



Deviations of ILC1 Higgs branching ratios from SM



What does the model type mean?

Model type: which are the parameters of the model

- Two types of model: GUT scale and weak scale
- GUT scale model assumes a specific cause of SUSY breaking \implies few parameters (4-6)
- Weak scale model does not assume knowledge about the cause of SUSY breaking \implies lots of parameters
 - But some violate lepton number, violate CP in new ways, increase rates of FCNC...
 - Thus usually use only 10-19 parameters
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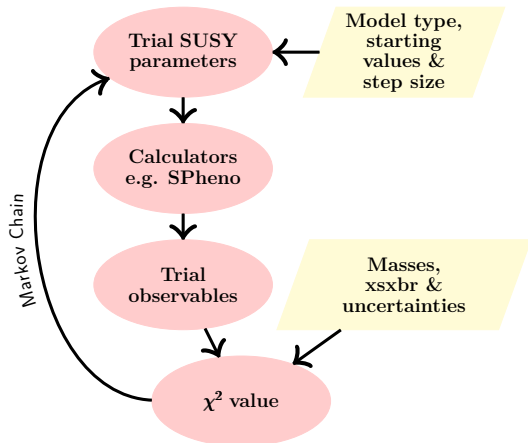
Probing the GUT scale: Fitting SUSY parameters

Fittino minimises

$$\chi^2 = \left(\frac{\mathcal{O}(ILC) - \mathcal{O}(theory)}{\Delta\mathcal{O}(ILC)} \right)^2$$

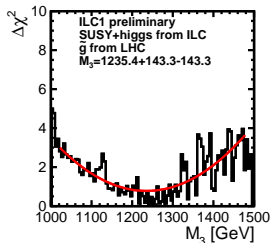
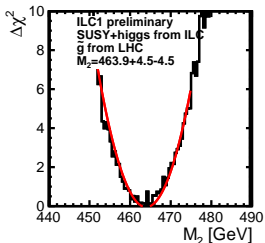
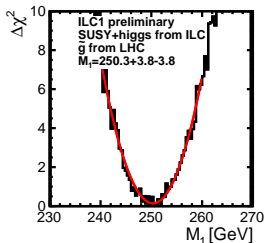
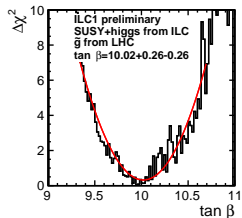
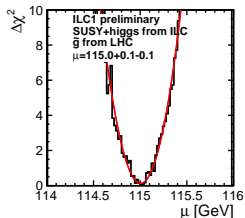
(arXiv:hep-ph/0412012)

SPheno 3.3.9beta,
Higgs mass and BRs
FeynHiggs2.10.2



Probing the GUT scale: Weak scale fits

- Purpose to test gaugino mass unification
- Input Higgs and SUSY obs. (incl \tilde{g} fr. LHC).
- M_1 , M_2 , M_3 , $\tan\beta$, and μ can be determined



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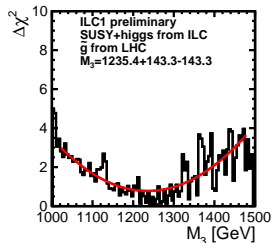
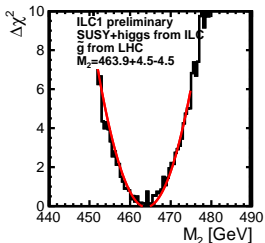
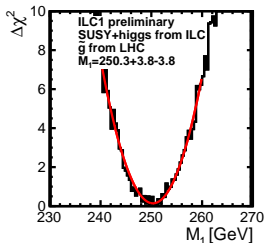
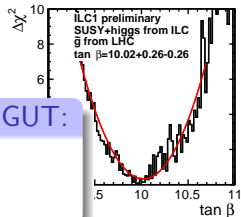
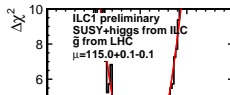
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Most important result for testing GUT:

$\delta(M_1) \approx 4 \text{ GeV}, \delta(M_2) \approx 11 \text{ GeV},$
 $\delta(M_3) \approx 130 \text{ GeV}.$



Probing the GUT-scale: Unification?

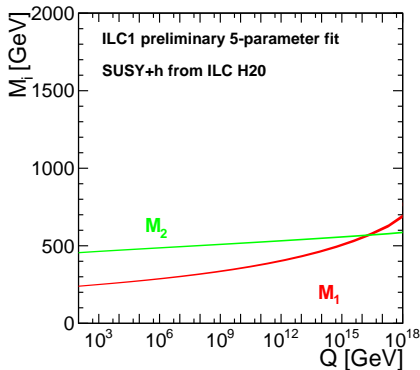
- This is at the 1 TeV scale.
- SUSY parameters change w/ scale governed by a system of coupled differential equations, the renormalisation group equations (RGEs).
- What happens if one inputs the fitted values and precisions into the RGEs for $M_{1,2,3}$?
 - Do gaugino masses unify?
 - Yes ...
 - ... and also M_3 : in ILC1 LHC will see the \tilde{g} .
 - ... or, conversely -in ILC2 - predict the gluino mass after just 5 years of ILC data:
 $m_{\tilde{g}} = 2870 \pm 210\text{GeV}$

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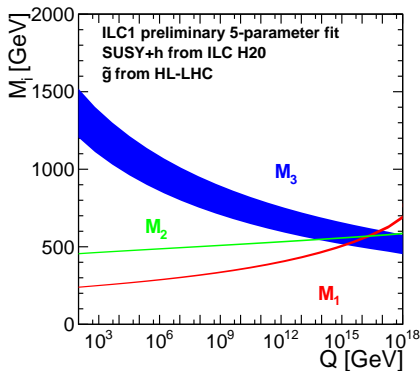
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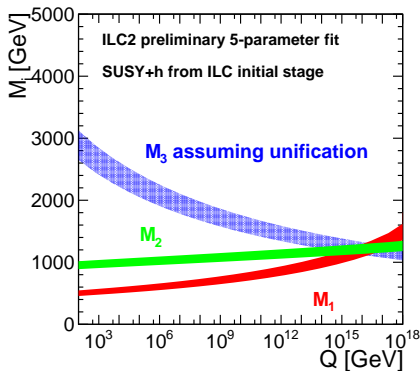
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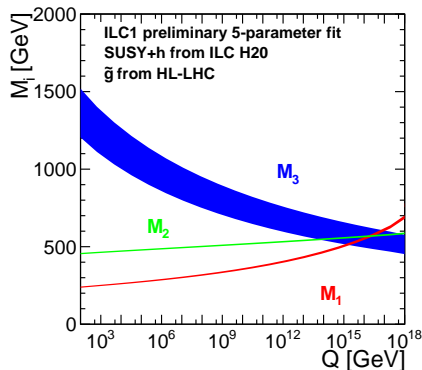


Probing the GUT-scale: Model discrimination?

- Can we see the difference between models ?
- Compare results from ...
 - ILC1 = radiatively driven natural SUSY, with ...
 - nGMM1 = mirage unification.
- Clearly distinguishable!

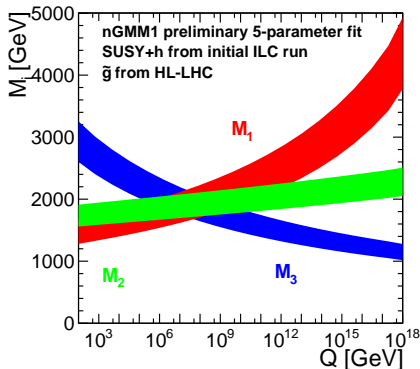
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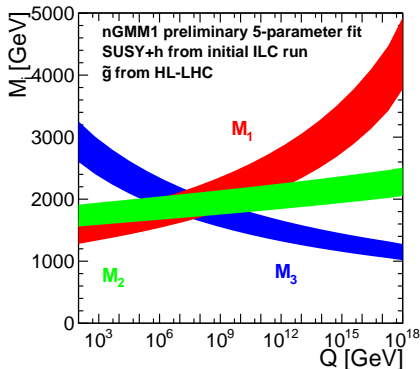
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Probing the GUT-scale: Predict rest of spectrum?

- Heavier neutralino/chargino masses

- $m_{\tilde{\chi}_3^0} = 263 \pm 4 \text{ GeV}$

- $m_{\tilde{\chi}_4^0} = 509 \pm 10 \text{ GeV}, m_{\tilde{\chi}_2^\pm} = 509 \pm 10 \text{ GeV}$

⇒ Motivation for ILC energy upgrade e.g. to $\sqrt{s} \sim 1 \text{ TeV}$

- Rough ranges for all other masses

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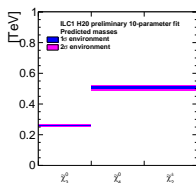
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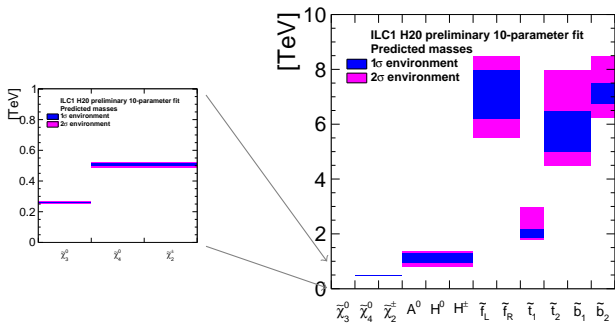
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Conclusions

- Light higgsinos motivated by **naturalness**, and are **not** excluded by LHC.
- ILC would probe higgsinos complementary to LHC reach
 - Either exclude masses up to $\sqrt{s}/2 = 500$ GeV for 1 TeV upgrade \rightarrow wide coverage of natural SUSY scenarios
 - or discover regardless of mass scale of heavier states
- ILC would measure properties of higgsinos to sub-percent-level precision.
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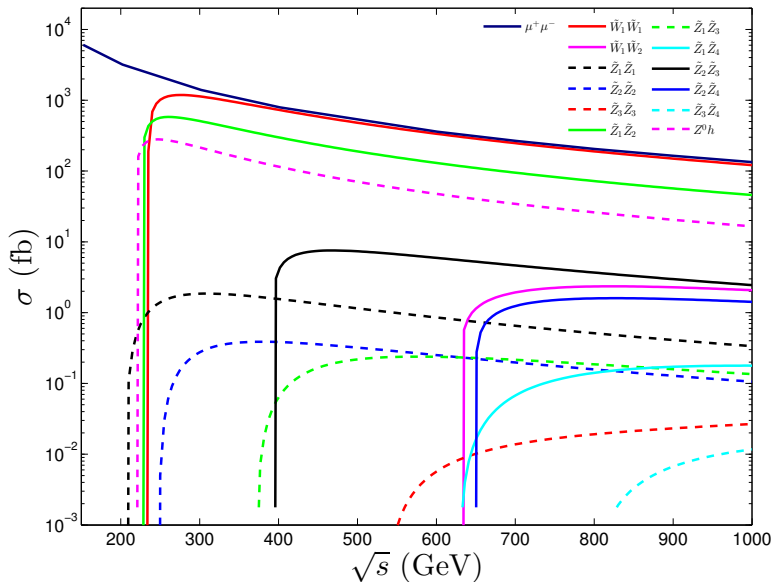
would provide clear motivation for ILC 1 TeV upgrade or other, even higher energy colliders

Thank You !

BACKUP

ILC1 unpolarised cross sections

ILC1: $m_0 = 7025$ GeV, $m_{1/2} = 568.3$ GeV, $A_0 = -11426.6$ GeV, $\tan\beta = 10$, $\mu = 115$ GeV, $m_A = 1000$ GeV



Fit observables

- mass $\tilde{\chi}_1^0, \tilde{\chi}_2^0, \tilde{\chi}_1^\pm$ (1%)
- xsxbr of $\tilde{\chi}_1^+ \tilde{\chi}_1^- \rightarrow q\bar{q}' l\nu_l$ ($l=e, \mu$) (3%)
for $\mathcal{P}(e^- = \mp 80\%, e^+ = \pm 30\%)$
- xsxbr of $\tilde{\chi}_1^0 \tilde{\chi}_2^0 \rightarrow \tilde{\chi}_1^0 \tilde{\chi}_1^0 ll$ ($l=e, \mu$) (3%)
for $\mathcal{P}(e^- = \mp 80\%, e^+ = \pm 30\%)$
- Higgs mass $\Delta = 30$ MeV
- Higgs BRs $h \rightarrow bb, h \rightarrow cc, h \rightarrow \tau\tau, h \rightarrow gg, h \rightarrow \gamma\gamma,$
 $h \rightarrow ZZ^*, h \rightarrow WW^*$

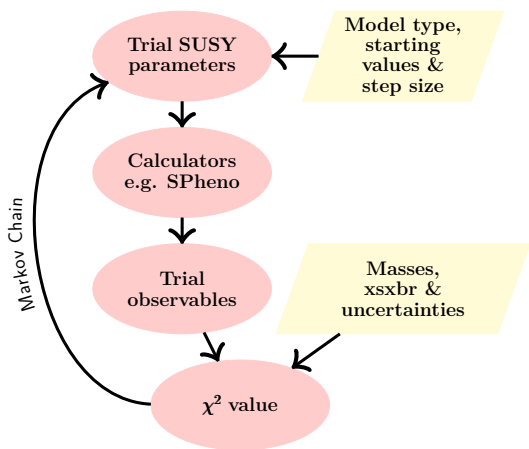
Probing the GUT scale: Fitting SUSY parameters

Fittino minimises

$$\chi^2 = \left(\frac{\mathcal{O}(ILC) - \mathcal{O}(theory)}{\Delta\mathcal{O}(ILC)} \right)^2$$

(arXiv:hep-ph/0412012)

SPheno 3.3.9beta,
Higgs mass and BRs
FeynHiggs2.10.2



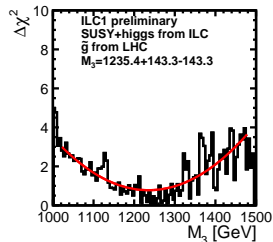
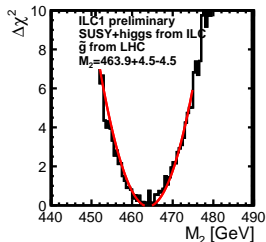
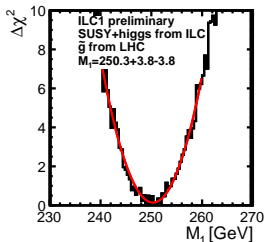
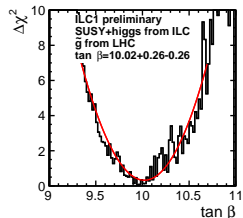
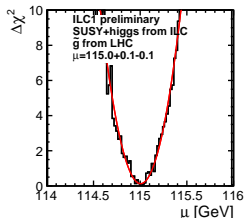
Fitted parameters of ILC1

- Underlying theory is a 6-parameter GUT model (NUHM2)
- A priori do not know it is a GUT model so fit weak scale pMSSM-10 (at 1 TeV)

parameter	ILC1 pMSSM-10	Fitted values (higgsinos, Higgs, $m_{\tilde{g}}$)
M_1	250	$247 \pm 4\text{GeV}$
M_2	463	$452 \pm 11\text{GeV}$
M_3	1270	$1280 \pm 130\text{GeV}$
μ	115	$[115, 122]\text{GeV}$
$\tan \beta$	10	$[8, 18]$
$M_{\tilde{t}_L}$	4820	$[4500, 8000]\text{GeV}$
$M_{\tilde{t}_R}$	1670	$[1500, 2000]\text{GeV}$
$M_{\text{other sfermions}}$	7150	$[5500, 8500]\text{GeV}$
$A_{t=b=\tau}$	-4400	$[-6600, -4200]\text{GeV}$
m_A	1000	$1110 \pm 116\text{GeV}$

Probing the GUT scale: Weak scale fits

- Purpose to test gaugino mass unification
- Input Higgs and SUSY obs. (incl \tilde{g} fr. LHC).
- M_1 , M_2 , M_3 , $\tan\beta$, and μ can be determined



Probing the GUT-scale: Predict rest of spectrum?

- Can we predict more from these data ?
- Do 10-parameter fit of ILC1 SUSY+higgs.
- Measurements/predictions for all of SUSY.
 - Quite precise for the rest of the gauginos.
 - Very preliminary 95% CL ranges:
 - $0.1 < M_2 < 0.2$ TeV
 - $0.1 < M_3 < 0.2$ TeV
 - $0.1 < M_{H_u} < 0.2$ TeV
 - $0.1 < M_{H_d} < 0.2$ TeV
 - $0.1 < M_{H_1} < 0.2$ TeV
 - $0.1 < M_{H_2} < 0.2$ TeV
 - $0.1 < M_{H_3} < 0.2$ TeV
 - $0.1 < M_{H_4} < 0.2$ TeV
 - $0.1 < M_{H_5} < 0.2$ TeV
 - $0.1 < M_{H_6} < 0.2$ TeV
 - $0.1 < M_{H_7} < 0.2$ TeV
 - $0.1 < M_{H_8} < 0.2$ TeV
 - $0.1 < M_{H_9} < 0.2$ TeV
 - $0.1 < M_{H_{10}} < 0.2$ TeV
 - $0.1 < M_{H_{11}} < 0.2$ TeV
 - $0.1 < M_{H_{12}} < 0.2$ TeV
 - $0.1 < M_{H_{13}} < 0.2$ TeV
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 - $0.1 < M_{H_{98}} < 0.2$ TeV
 - $0.1 < M_{H_{99}} < 0.2$ TeV
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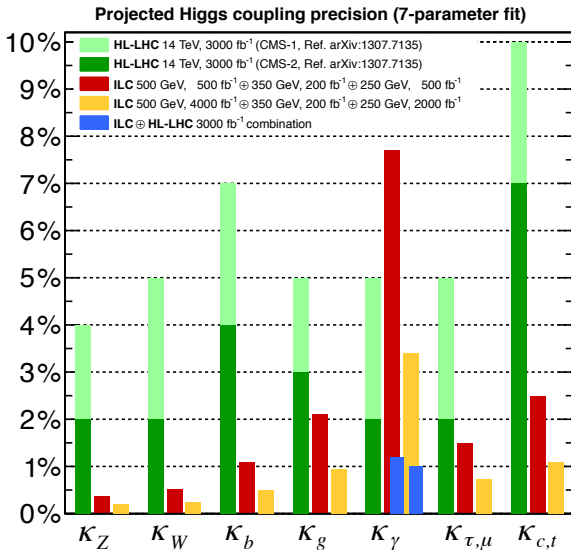
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Model *dependent* Higgs measurements at ILC and LHC



Dark matter predictions

- Dark matter relic density $\Omega_{ILC1}/\Omega_{Planck} = 0.054 \pm 0.001$
 \implies Strong hint that non-SUSY DM or non-thermal production of higgsinos exists
- Spin-independent WIMP-nucleon scattering cross section
 $\sigma^{SI} = 1.5 \times 10^{-8} \text{ pb}$
- WIMP annihilation cross section
 $\langle \sigma v \rangle = 2.6 \times 10^{-25} \text{ cm}^3 \text{ s}^{-1}$

