

# A new quark-hadron hybrid EOS for core-collapse supernovae and neutron star mergers

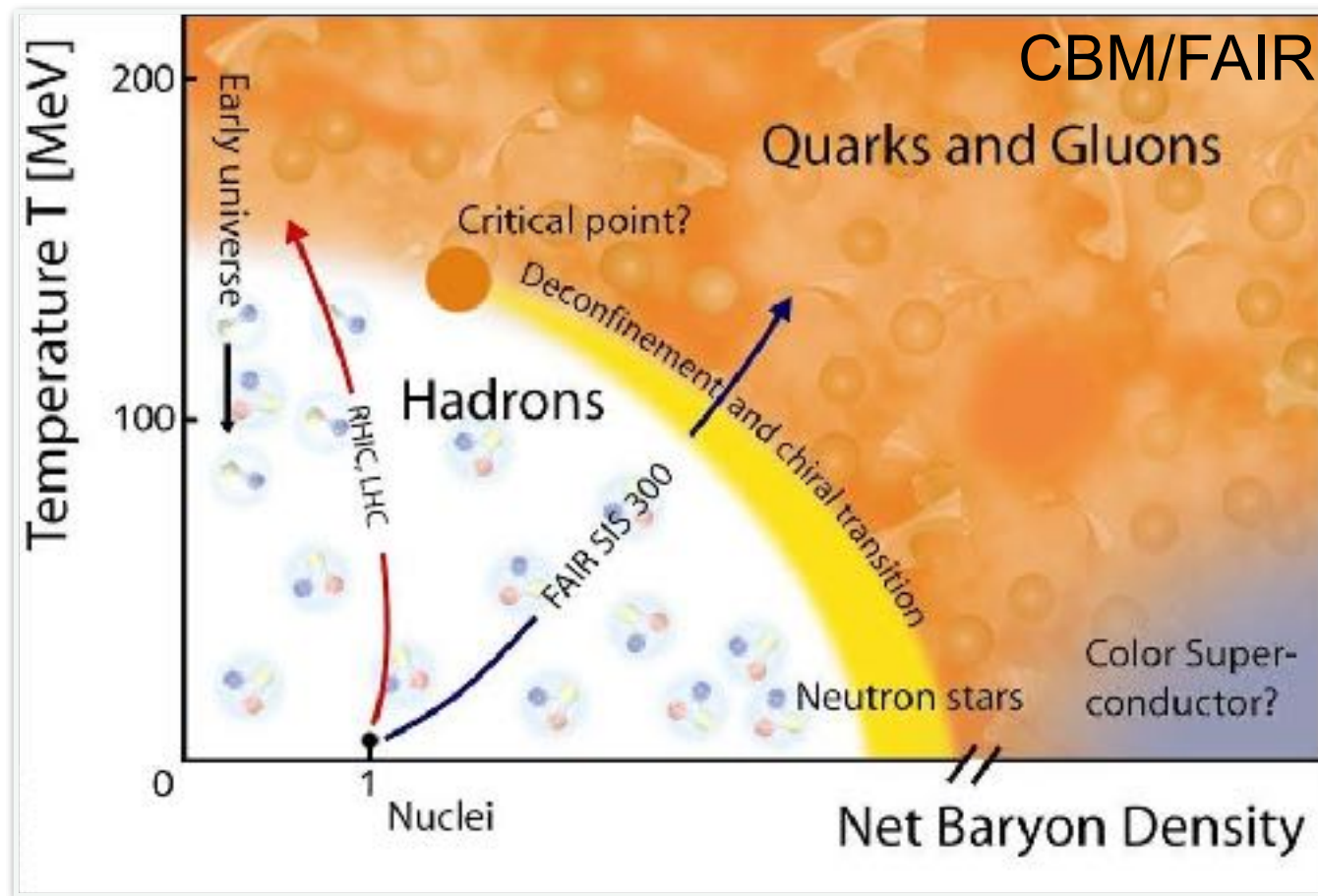
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Matthias Hempel, Basel University

*From quarks to gravitational waves, CERN, 6.12.2016*

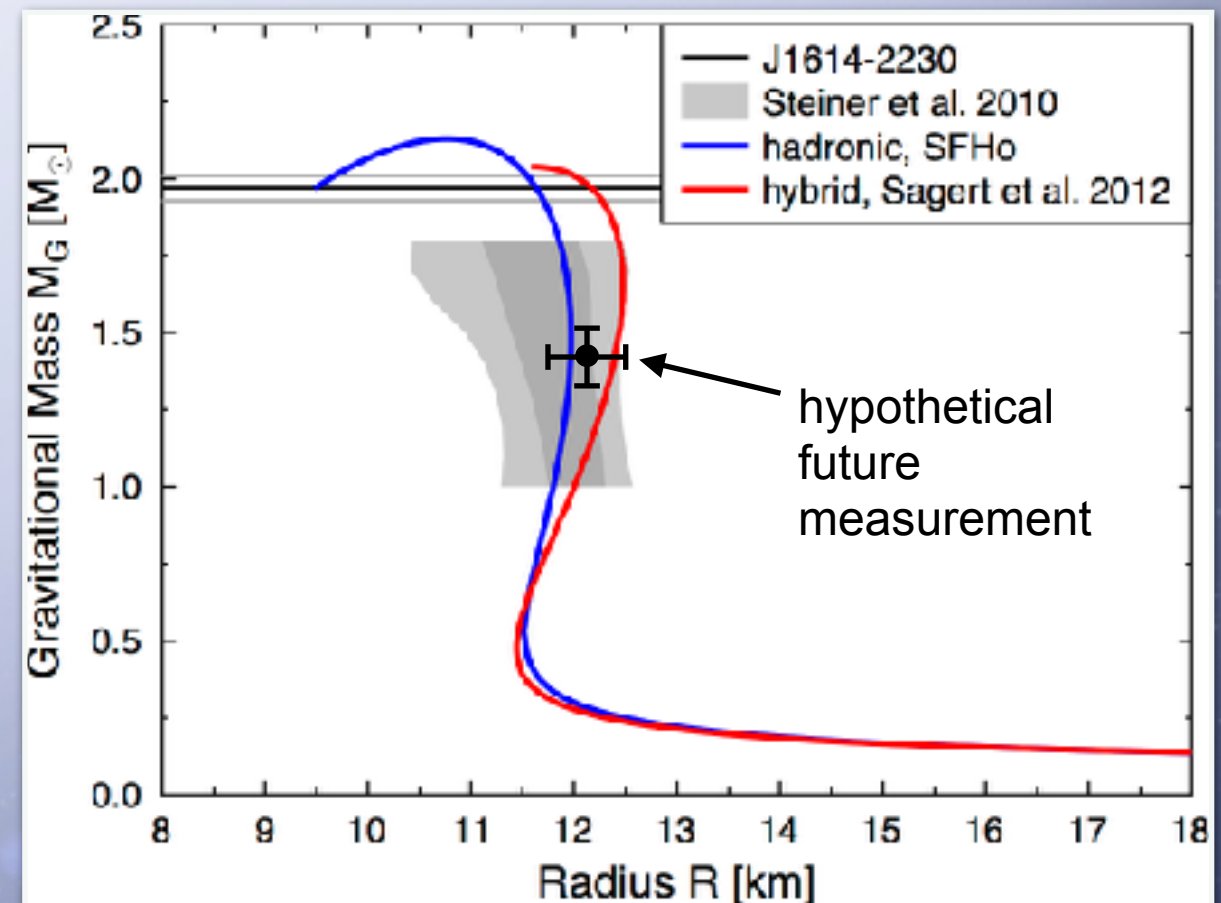


# QCD phase diagram



- M-R of neutron stars may not be sufficient to identify quark matter
- „masquerade“, Alford et al. 2005
- $\rightarrow$  cooling/transport properties, signatures in dynamic scenarios (see, e.g. Buballa et al. arXiv:1402.6911)

- what is the state of matter at extreme densities?
- is there a first-order phase transition to quark matter?



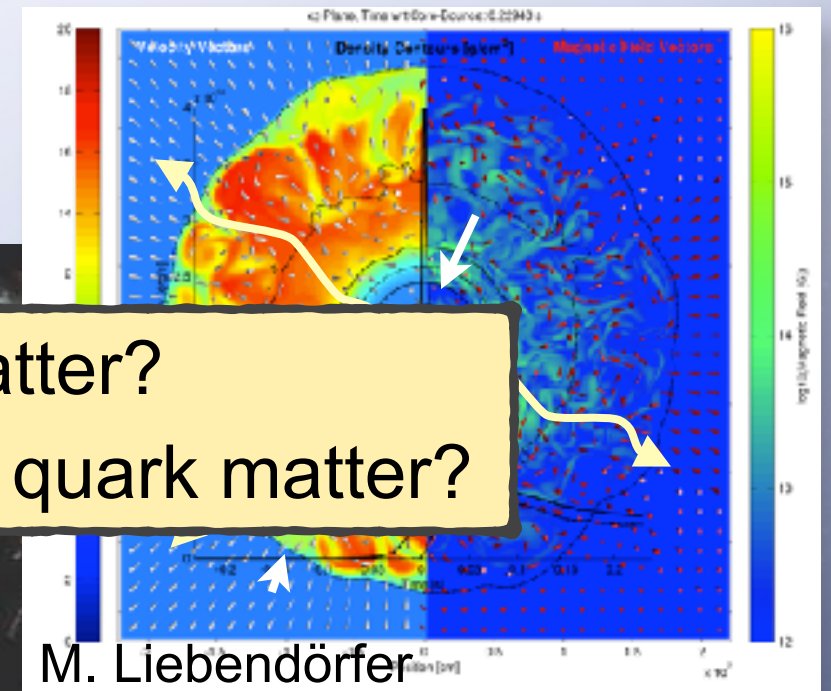


# Motivation: core-collapse supernovae

- how do massive stars explode?
- still many open questions in core-collapse supernova theory
- which progenitors end as black holes, which as neutron stars?
- what is their nucleosynthesis contribution, galactical chemical evolution?



→ what is the role of quark matter?  
→ are there clear observable signals of quark matter?



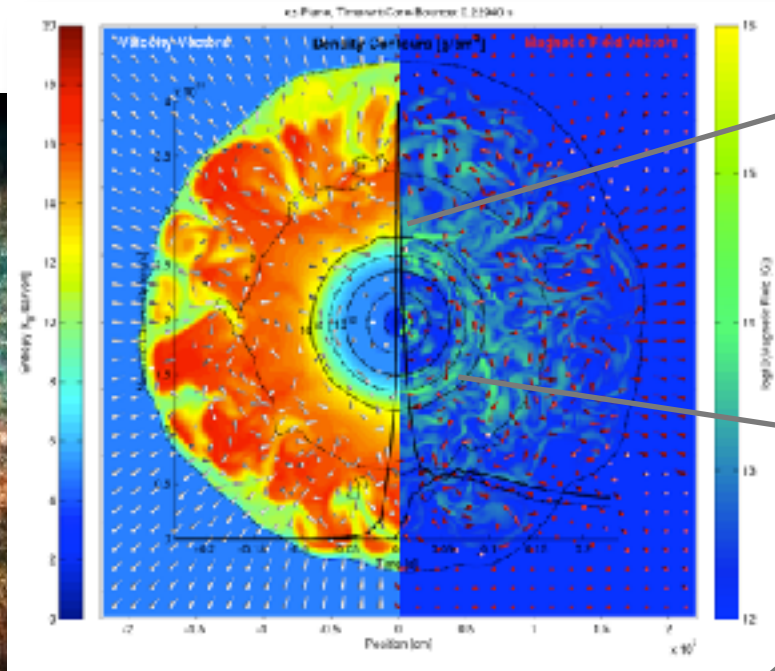
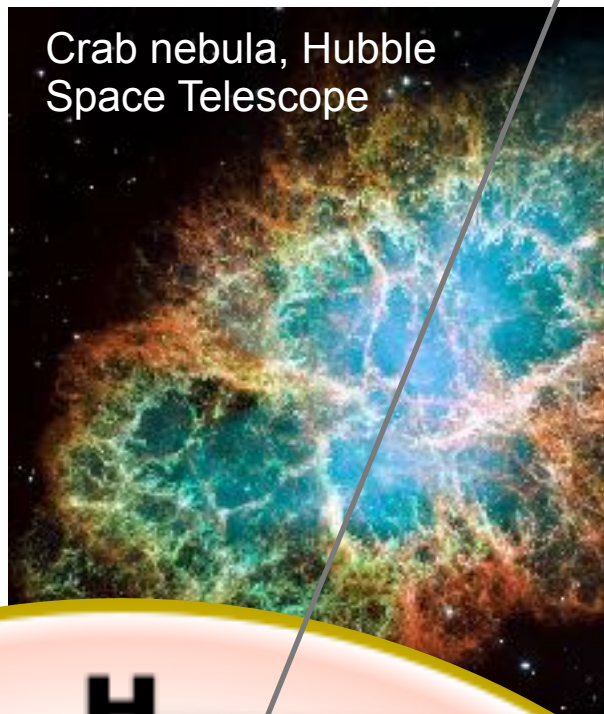
M. Liebendörfer





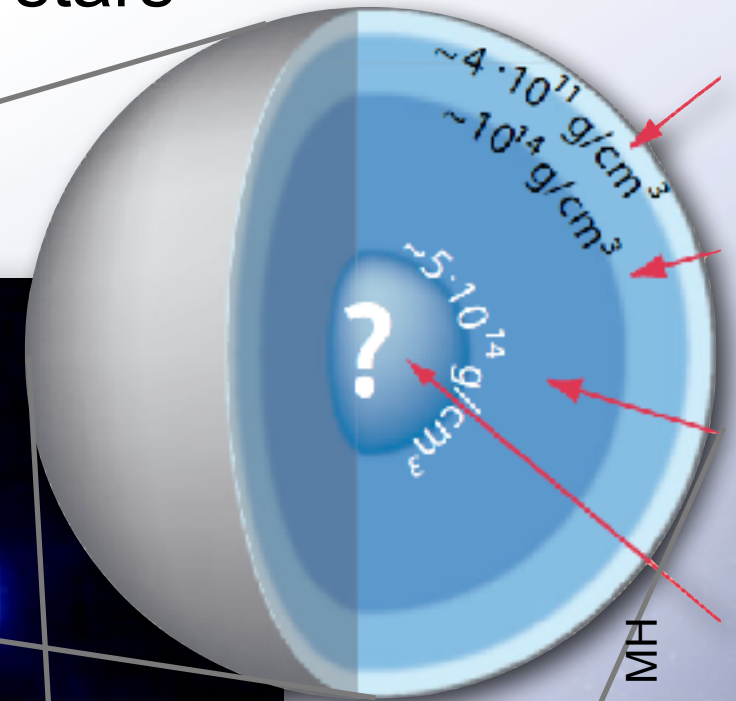
# The general purpose „supernova“ EOS

core-collapse supernovae

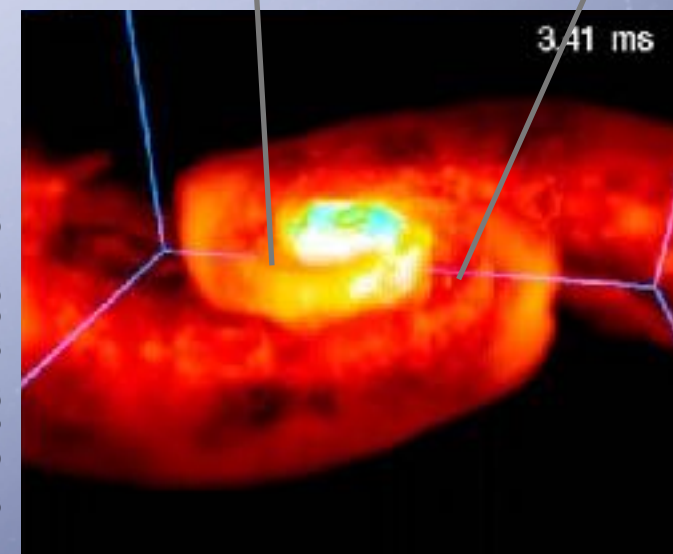


Liebrandt

neutron stars



neutron star mergers



Ruffert and Janka

- EOS tables with full density, temperature and asymmetry-dependence needed, „general purpose EOS“
- in total only 40 general purpose EOSs available (Oertel, MH, Klähn, Typel, Rev. Mod. Phys., accepted)

progenitor star at onset of collapse

Wikimedia

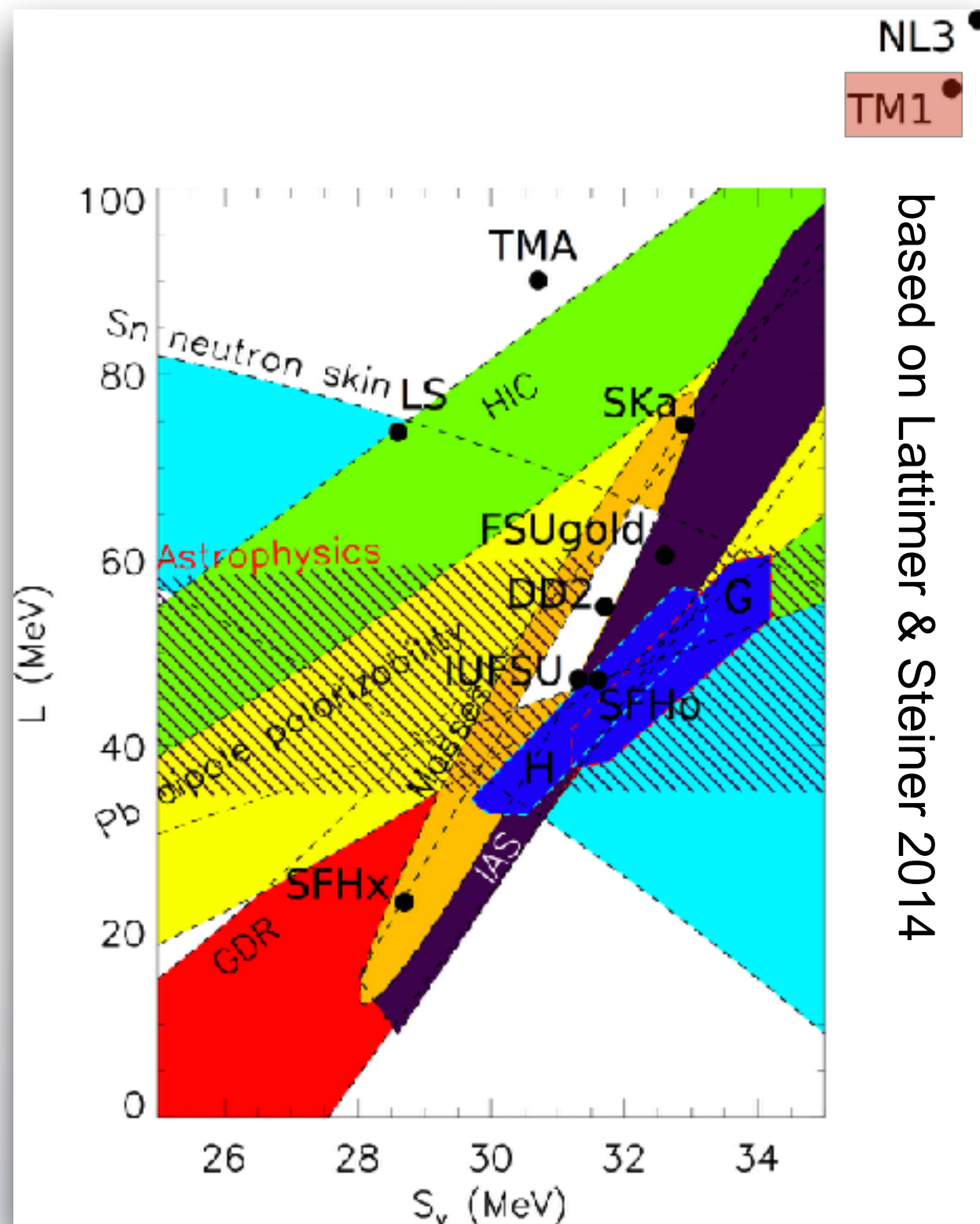
# Quark-hadron hybrid general purpose EOSs

Model	Nuclear Interaction	Degrees of Freedom	$M_{\max}$ ( $M_{\odot}$ )	$R_{1.4M_{\odot}}$ (km)	References
STOS $\pi$ Q	TM1	$n, p, \alpha, (A, Z), \pi, q$	1.85	13.6	Nakazato <i>et al.</i> (2008)
STOSQ	TM1	$n, p, \alpha, (A, Z), q$	1.81	14.4	Nakazato <i>et al.</i> (2008)
STOSB139	TM1	$n, p, \alpha, (A, Z), q$	2.08	12.6	Fischer <i>et al.</i> (2014)
STOSB145	TM1	$n, p, \alpha, (A, Z), q$	2.01	13.0	Sagert <i>et al.</i> (2012)
STOSB155	TM1	$n, p, \alpha, (A, Z), q$	1.70	9.93	Fischer <i>et al.</i> (2011)
STOSB162	TM1	$n, p, \alpha, (A, Z), q$	1.57	8.94	Sagert <i>et al.</i> (2009)
STOSB165	TM1	$n, p, \alpha, (A, Z), q$	1.51	8.86	Sagert <i>et al.</i> (2009)

- hadronic phase: „STOS“, Shen, Toki, Oyamatsu and Sumiyoshi 1998, 2011
- quark phase: bag model (u,d,s), first-order strong interactions,  $\alpha_s$  (Farhi and Jaffe 1984)
- Gibbs conditions for phase equilibrium
- only two hybrid EOSs with sufficiently high  $M_{\max}$



# Characteristic properties of STOS („Shen“) EOS



- STOS: nucleons, alpha particles, representative heavy nucleus
- non-linear relativistic mean-field interactions (TM1)
- symmetry energy not compatible with various experimental constraints

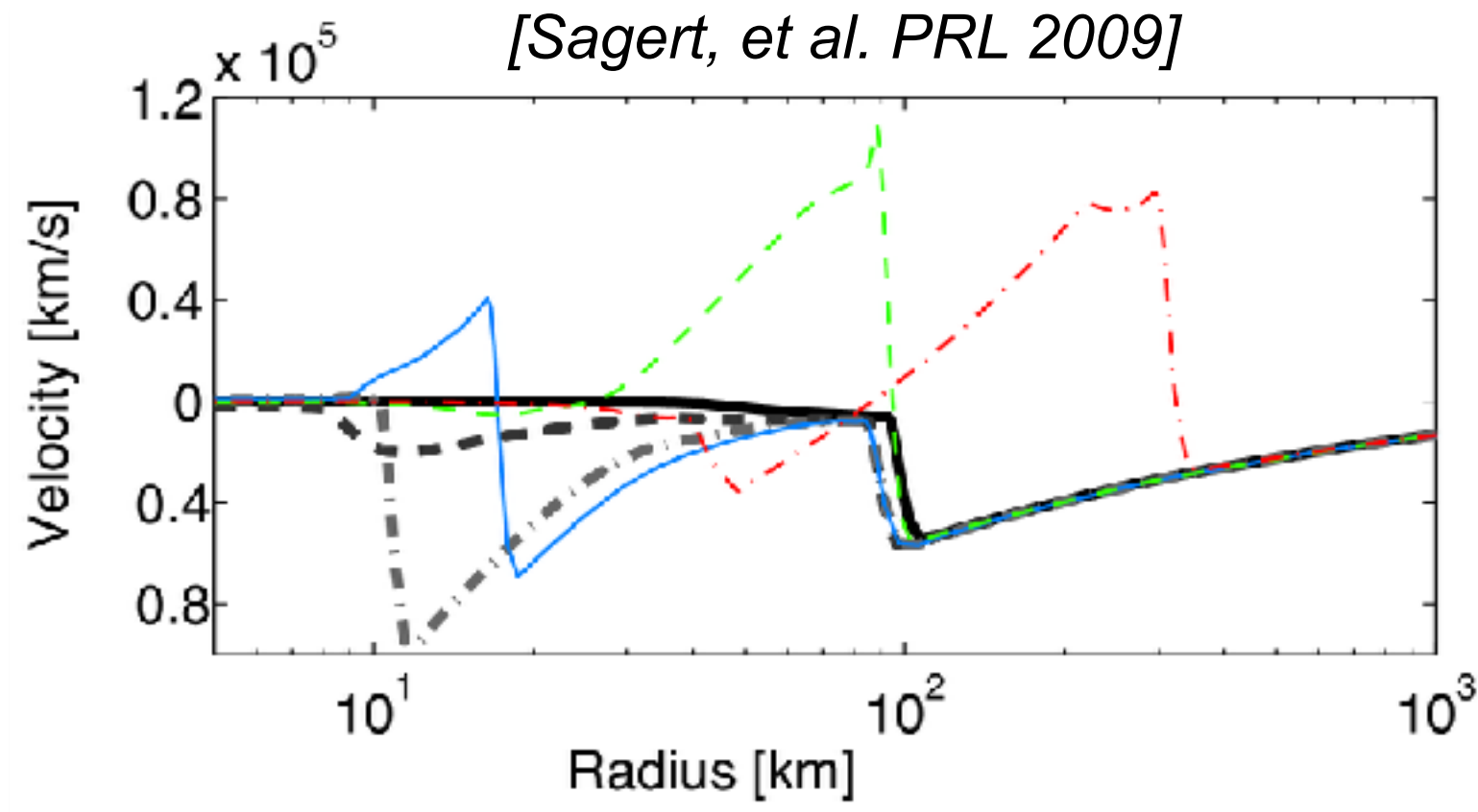
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- Gibbs conditions for phase equilibrium
- only two hybrid EOSs with sufficiently high  $M_{\max}$
- TM1: unrealistic symmetry energy

→ need for new hybrid EOSs  
which quark matter properties could be interesting?

# CCSN explosions by the QCD phase transition



$t_{pb} = 240.5$  ms

$t_{pb} = 255.2$  ms

$t_{pb} = 255.4$  ms

$t_{pb} = 255.5$  ms

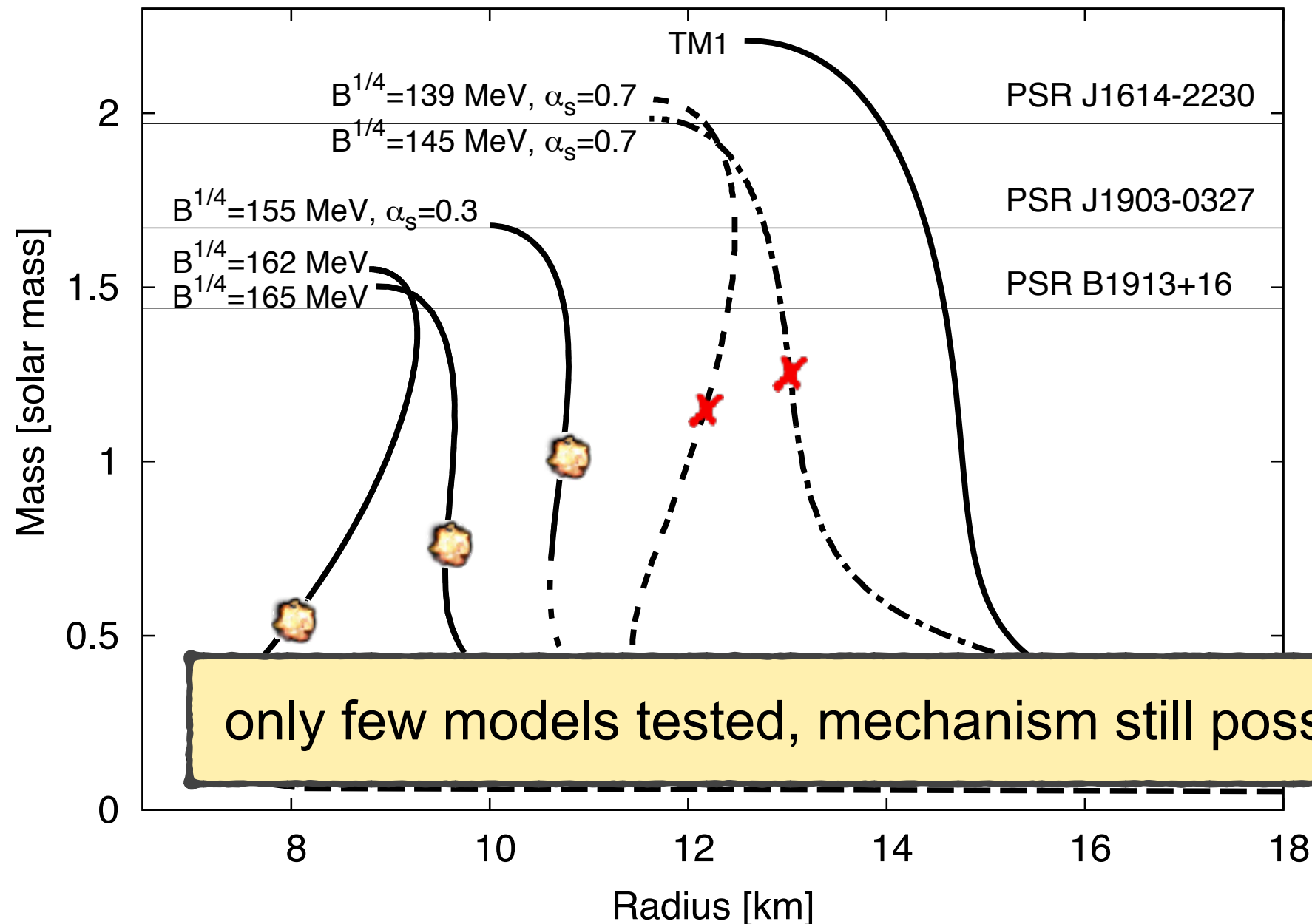
$t_{pb} = 256.3$  ms

$t_{pb} = 261.2$  ms

- phase transition induces collapse of the proto-neutron star
- collapse halts when pure quark matter is reached
- formation of a second shock, merges with standing accretion shock and triggers an explosion
- second neutrino burst as a clear observable signal (DasGupta et al. 2009)
- weak r-process (Nishimura et al. 2012)




# Mass-radius relation of hybrid EOS and SN explosions



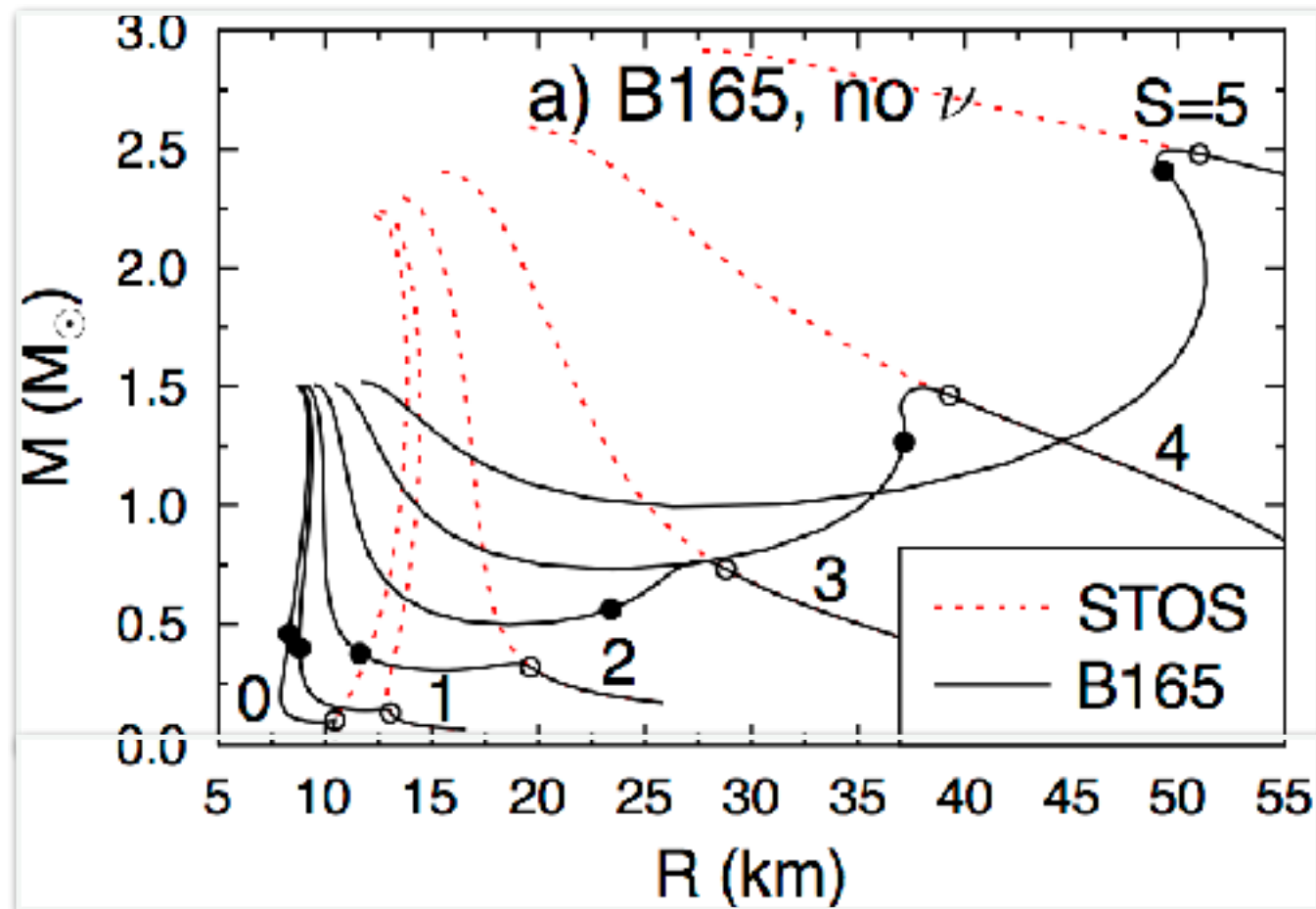
- no explosions for sufficiently high maximum mass
- weak phase transition

only few models tested, mechanism still possible for others?

 explosions in spherical symmetry  
(T. Fischer et al. ApJS 2011)

- see also: Fischer, Blaschke, et al. 2012: PNJL hybrid EOS

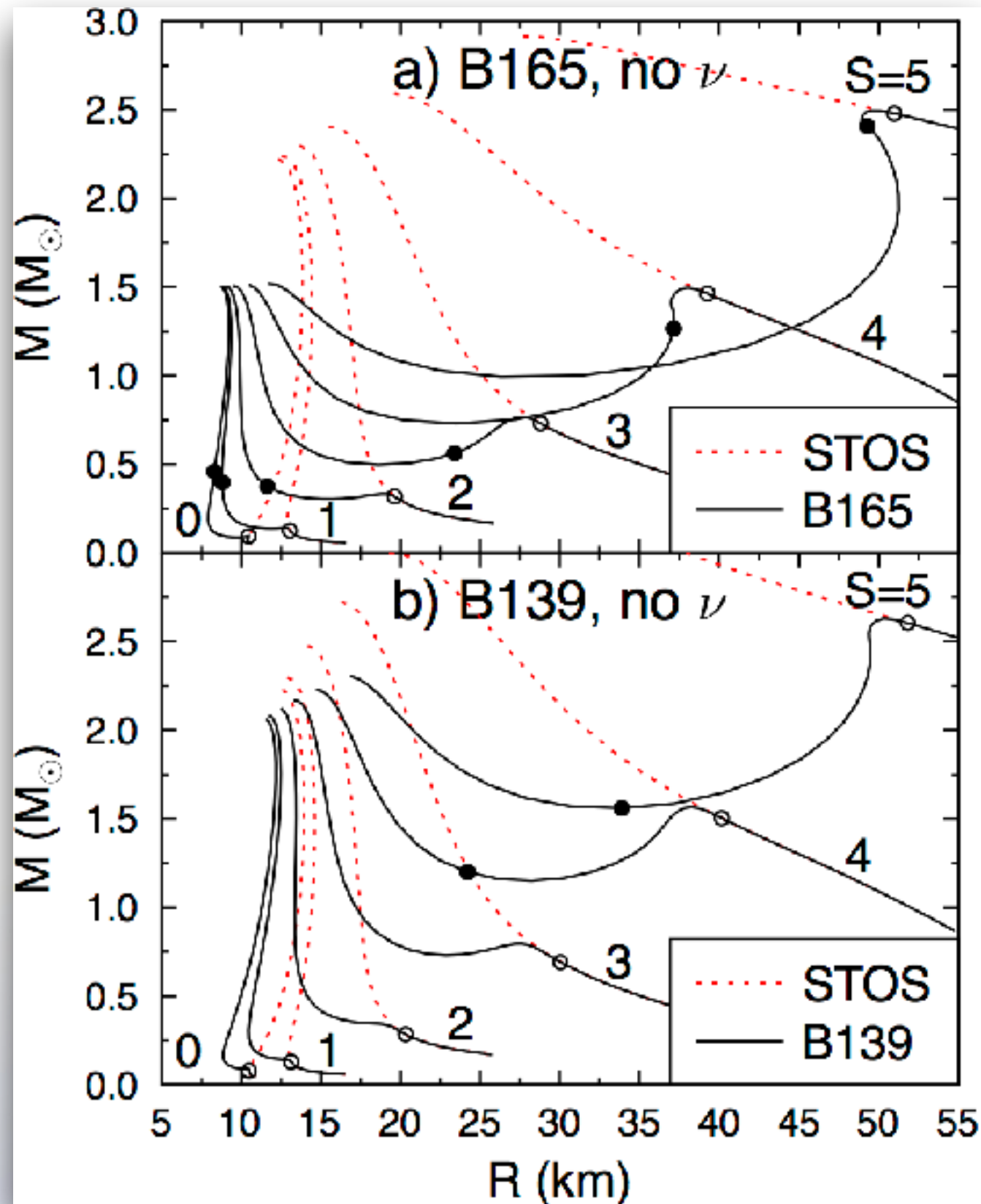
# A hot third family of proto-compact stars



- after onset of phase transition: loss of stability, regained for sufficiently large quark matter core
- third family feature („twins“) arises for high entropies
- novel aspect: a third family that exists only in the proto-neutron star stage

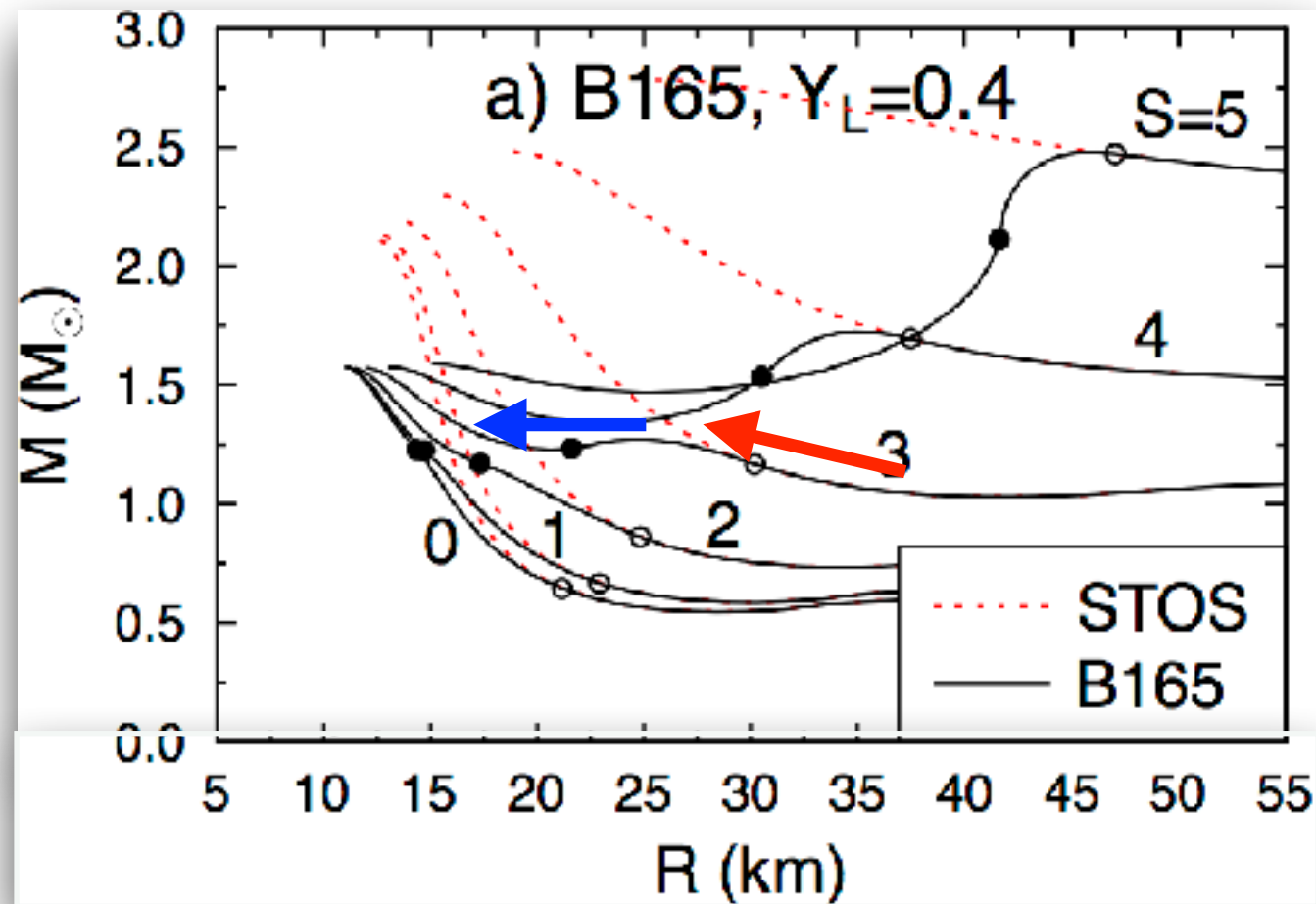


# A hot third family of proto-compact stars — EOS dependence



- for B139: third family arises only for very high entropies, much less pronounced

# Collapse to the third family in a supernova



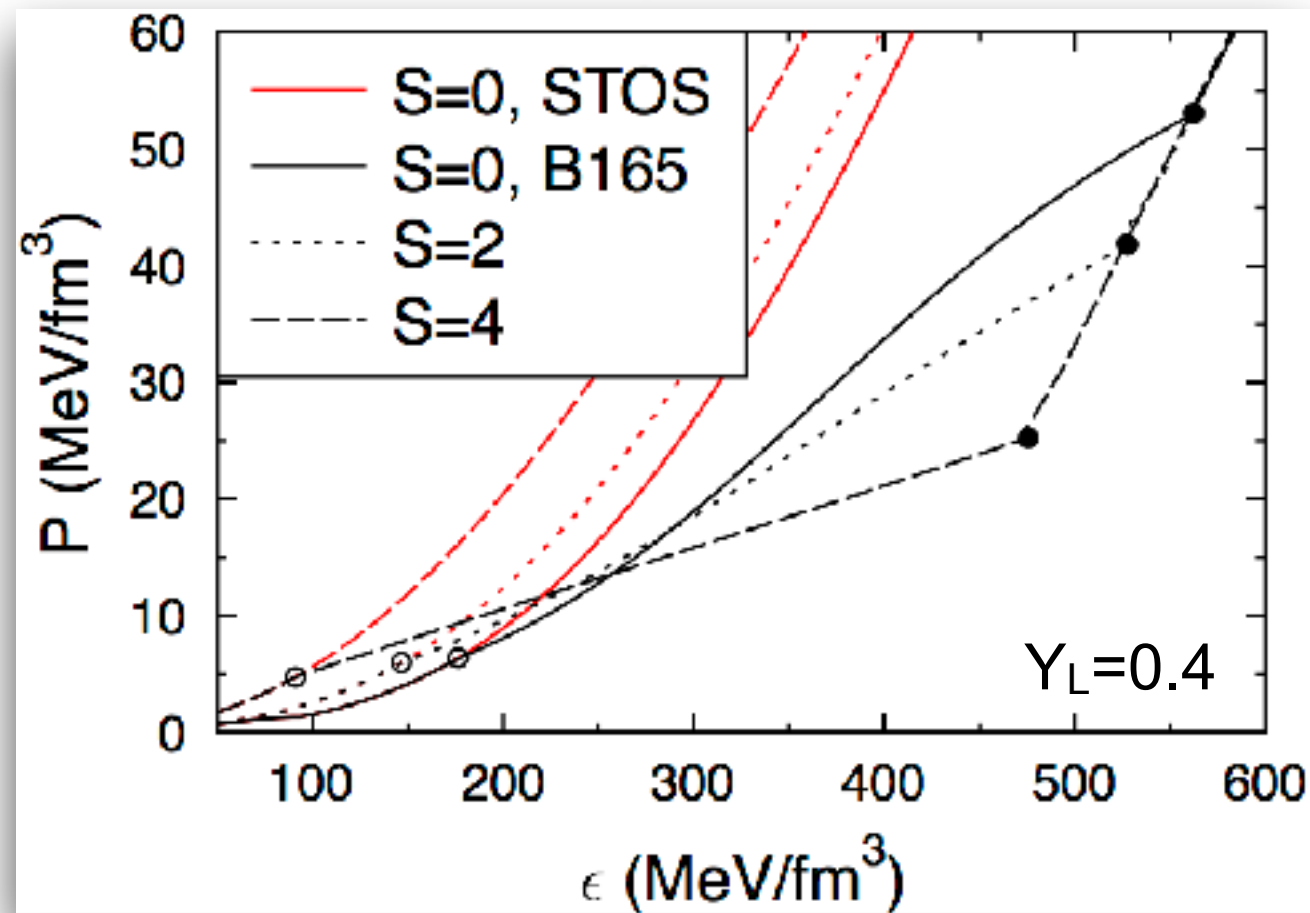
schematically:

- **accretion**: increase of the proto-neutron star mass from  $\sim 1 M_{\text{sun}}$  to  $\sim 1.5 M_{\text{sun}}$  in the first 200 ms
- **collapse** from the second to the third family with gravitational binding energy release

- exactly this was seen in the core-collapse supernova simulations by T. Fischer in 2009-2012
- results in an energetic explosion even in spherical symmetry
- new insight: the unusual thermal properties and the hot third family stand behind the explosion
- third family feature in cold neutron stars helpful, but not necessary

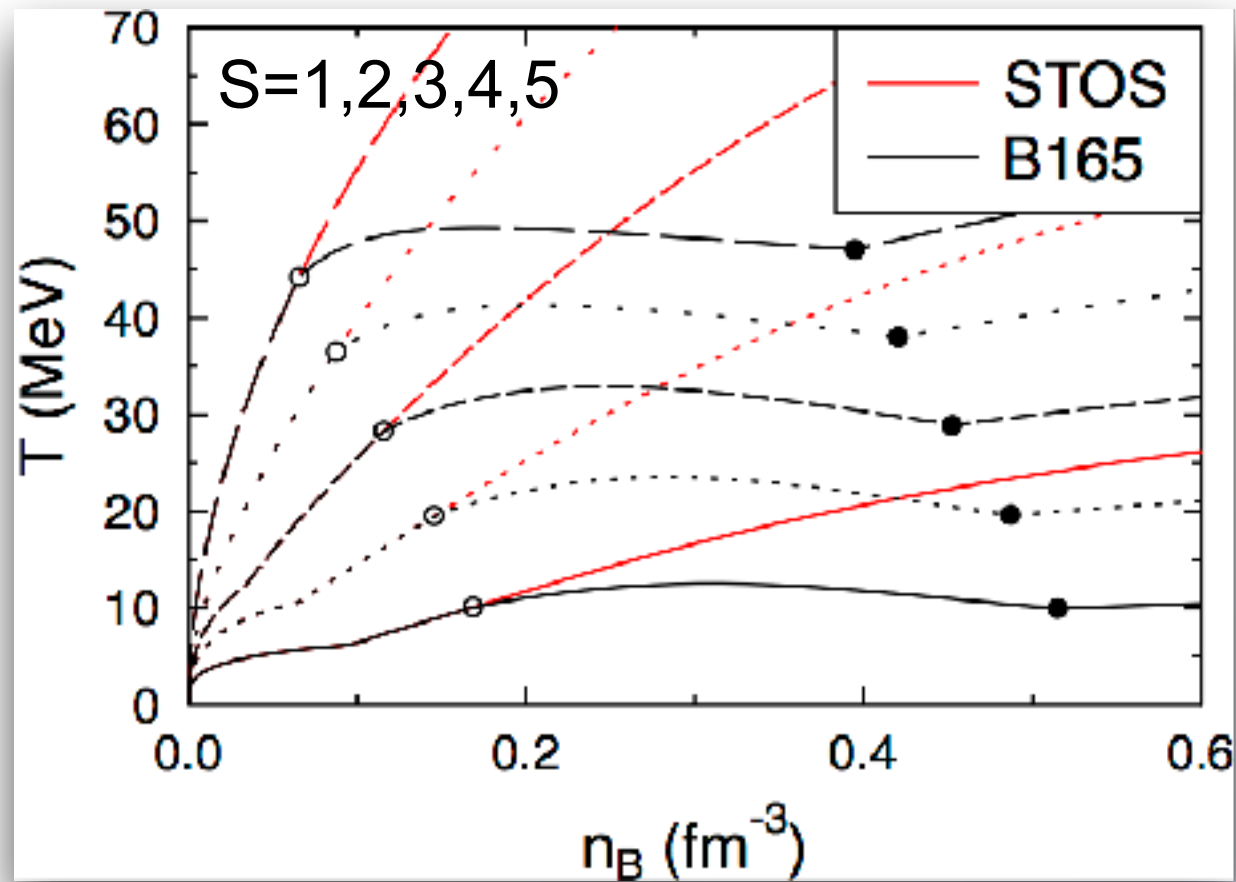


# Pressure-energy density relation



- hadronic and quark matter stiffens when it is heated
- in the phase coexistence region it softens

# Temperature for isentropes with B165 hybrid EOS



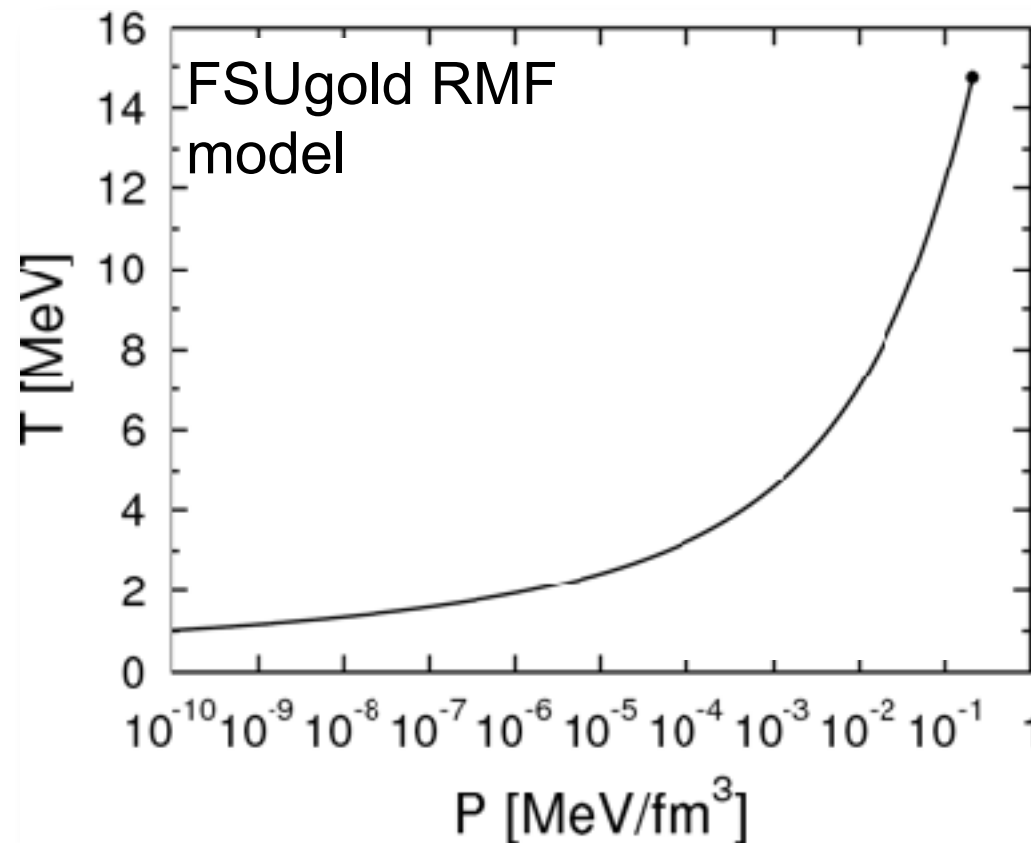
- $dT/dn_B < 0$  in parts of the phase coexistence region



# Pressure-temperature phase diagrams

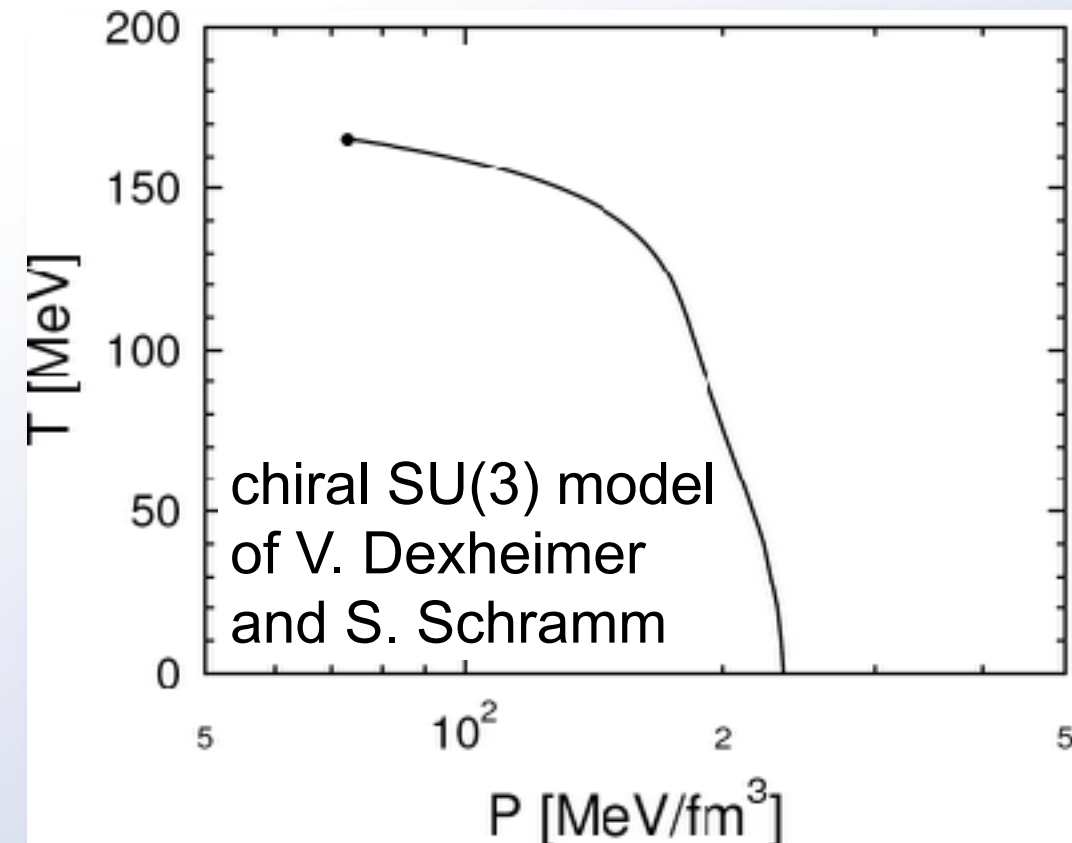
[MH, V. Dexheimer, S. Schramm, I. Iosilevskiy, PRC 88 (2013)]

liquid-gas phase transition



*enthalpic*

chiral/deconfinement phase transition



*entropic*

opposite slope in P-T as  
fundamental difference

see also:

[Satarov, Dmitriev, Mishustin, PAN72 (2009)]

[Bombaci et al., PLB680 (2009)]

[Wambach, Heckmann, Buballa, AIPC1441 (2011)]

[Steinheimer, Randrup, Koch, PRC89 (2014)]

[Iosilevskiy, arXiv:1403.8053]

# Unusual thermal properties of entropic phase transitions

- Clausius-Clapeyron equation

$$\left. \frac{dP}{dT} \right|_{\text{PT}} = \frac{S^I - S^{II}}{1/n_B^I - 1/n_B^{II}}$$

- for Maxwell phase transition

$$\left. \frac{dP}{dT} \right|_{\text{PT}} = \left. \frac{\partial P}{\partial T} \right|_{n_B} \quad \left. \frac{\partial P}{\partial T} \right|_{n_B} < 0 \Leftrightarrow \left. \frac{\partial T}{\partial n_B} \right|_S < 0$$

- mass-radius relation given by  $P(\epsilon, S)$
- to characterize thermal effects:  $dP/dS|_\epsilon$
- $dP/dS|_\epsilon > 0$ : stiffening,  $dP/dS|_\epsilon < 0$ : softening for increasing entropy

$$\left. \frac{\partial P}{\partial S} \right|_\epsilon = -T n_B \left( \frac{c_s}{c} \right)^2 + \frac{T}{C_V} \left. \frac{\partial P}{\partial T} \right|_{n_B}$$

- first term small, relativistic correction

entropic PT: unusual thermal properties, softening of the EOS with increasing entropy

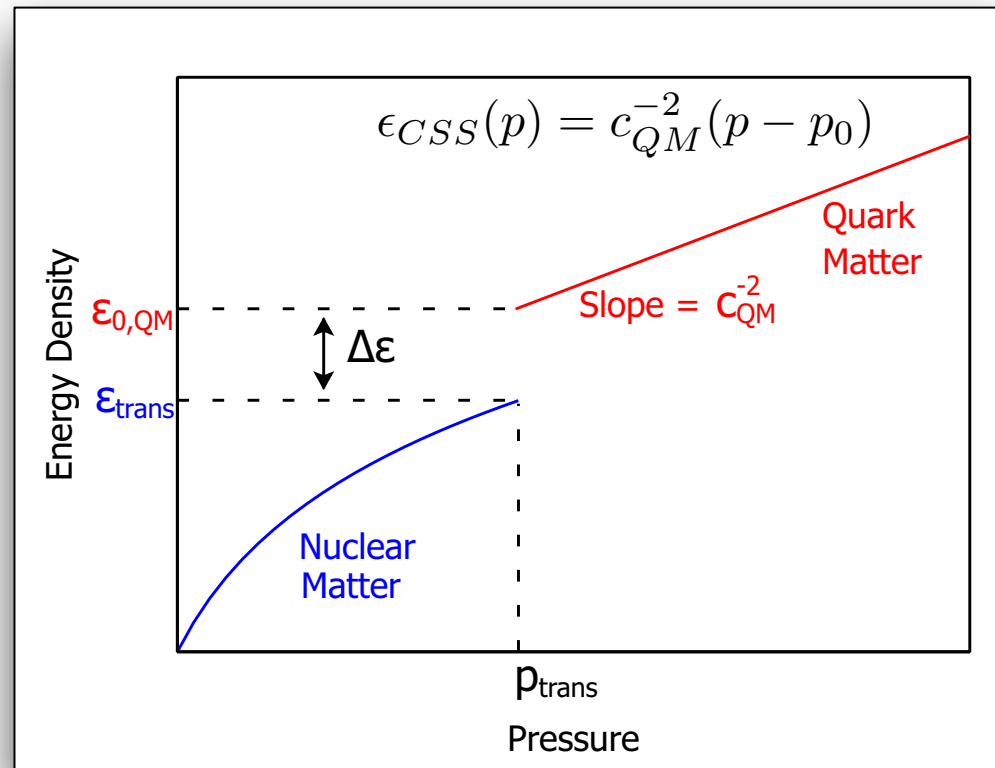


# Towards generating a new hybrid supernova EOS: A systematic analysis of cold hybrid stars

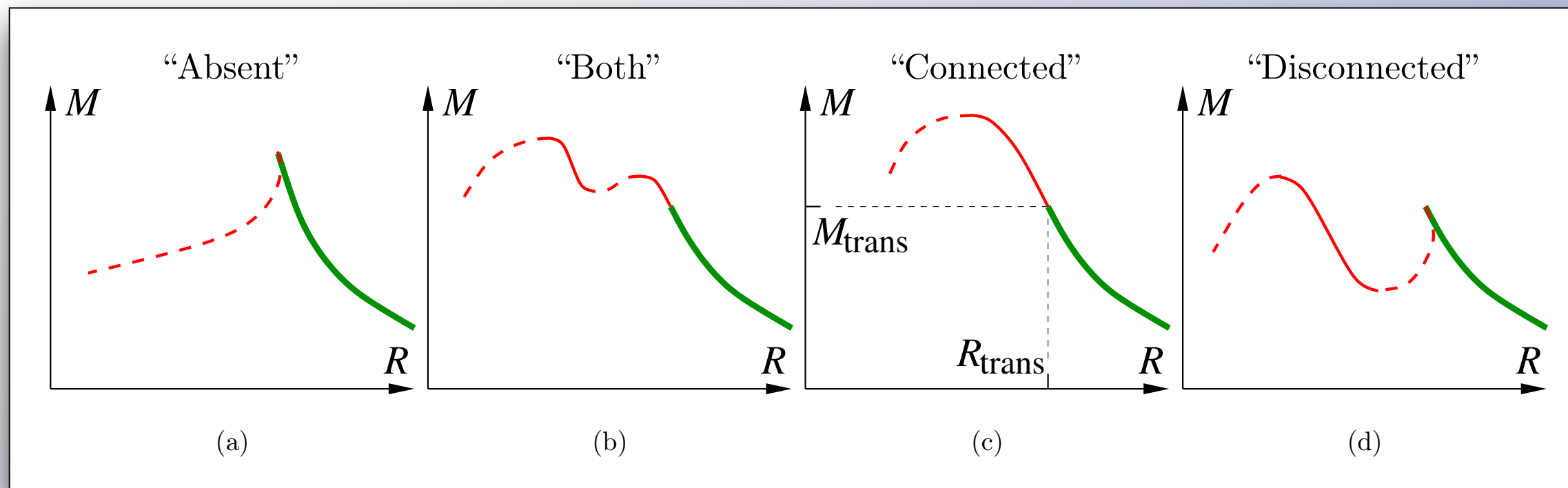
*[Oliver Heinemann, MH, Friedrich-Karl Thielemann, PRD 94 (2016)]*

# Alford's parameter scan

[Alford, Han, Prakash, PRD88 (2013)]



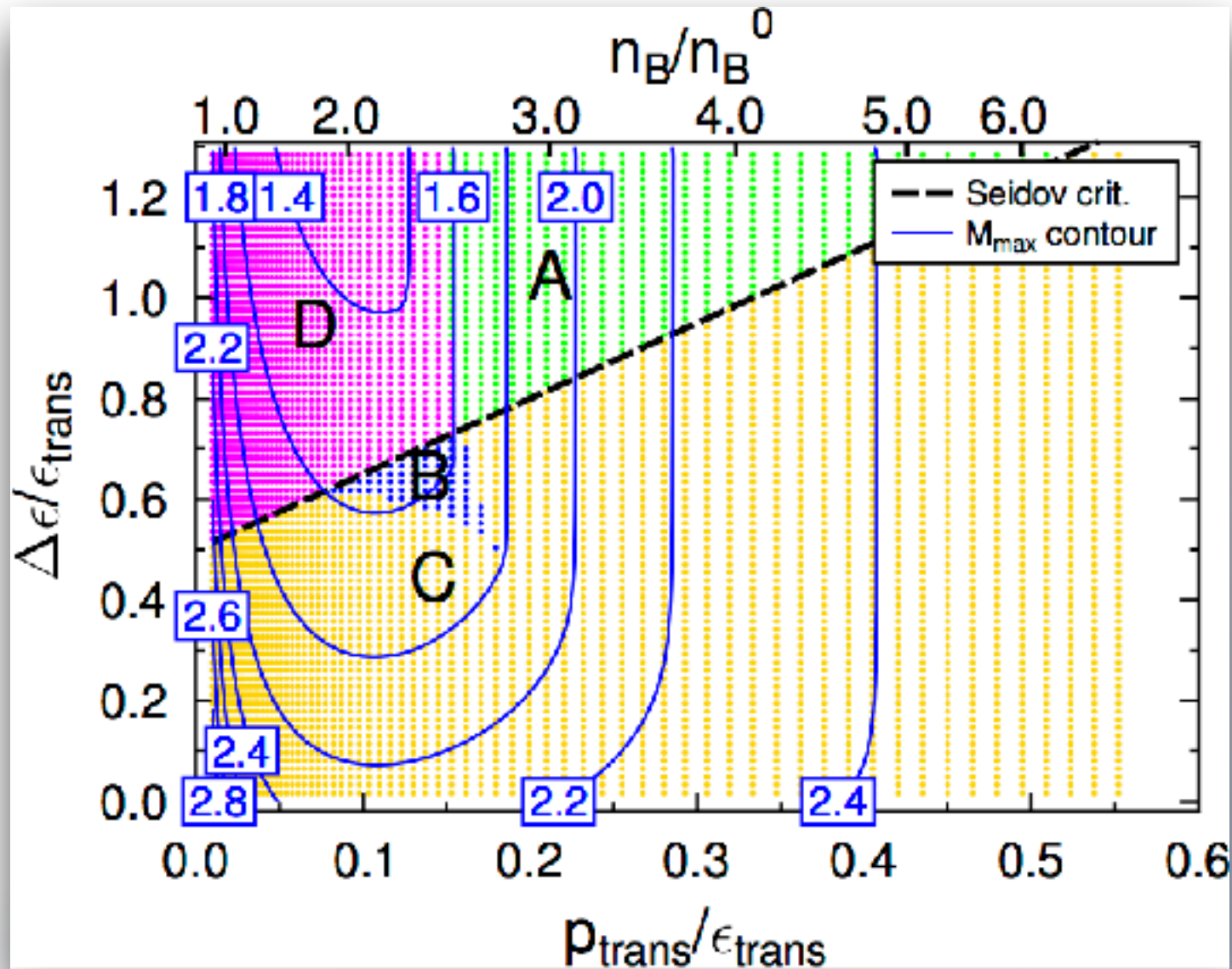
- quark matter: constant speed of sound
- systematic variation of transition pressure and energy density discontinuity
- maximum mass and classification of hybrid stars





# New parameter scan for HS(DD2) hadronic EOS

- HS(DD2): general purpose (supernova) EOS, good nuclear matter properties,  $M_{\text{max}} = 2.42 M_{\text{sun}}$

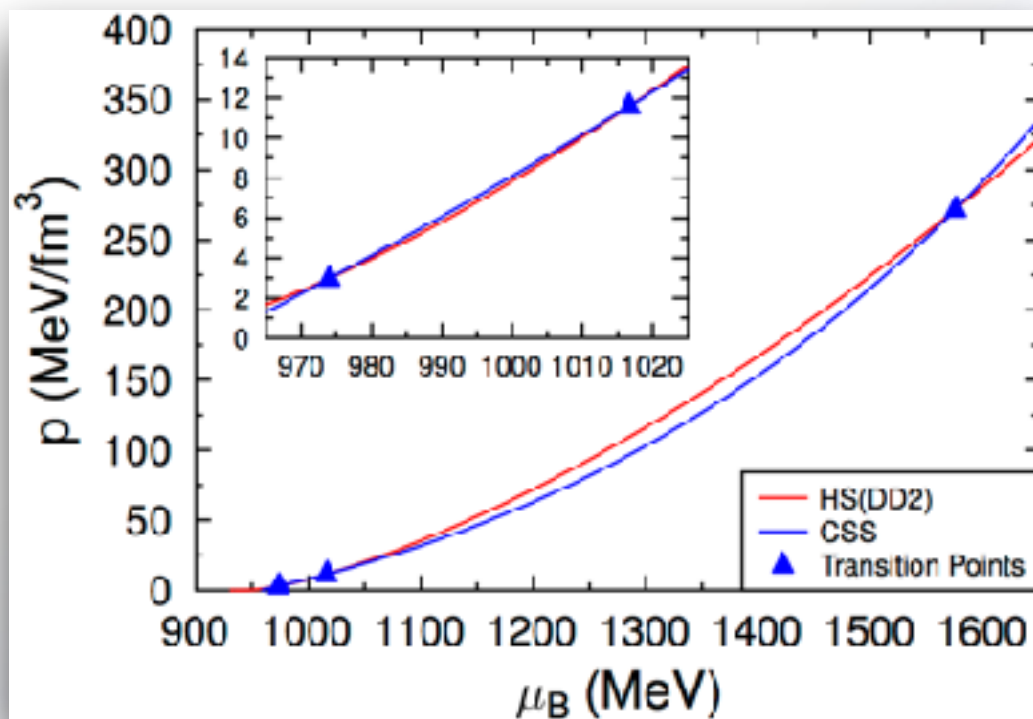


- $M_{\text{max}} > M_{\text{max}}(\text{HSDD2})$  possible
- limited parameter region with  $M_{\text{max}} > 2 M_{\text{sun}}$  and third family
- favorable region extended for  $c_s^2 > 1/3$

# Thermodynamic stability

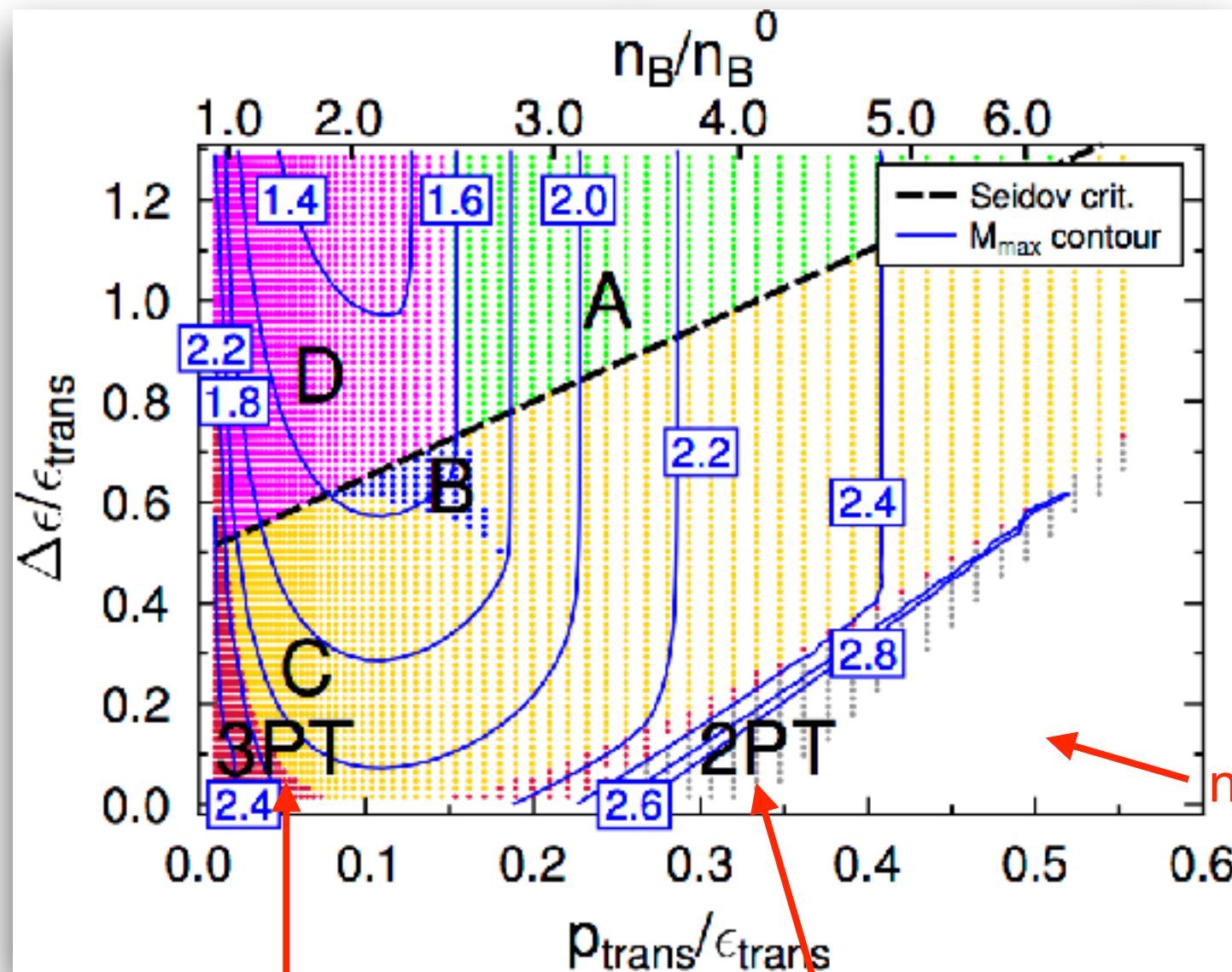
- previous parameter scans: only pressure and temperature equilibrium ( $T=0$ )
- $p(\mu)$  relation can be derived from  $p(\epsilon)$

$$p^{\text{CSS}}(\mu) = \frac{c_{QM}^2}{1 + c_{QM}^2} p_0 \left[ \left( \frac{\mu}{\mu_0} \right)^{\frac{1+c_{QM}^2}{c_{QM}^2}} + \frac{1}{c_{QM}^2} \right]$$





# Effect of thermodynamic stability



negative energy densities

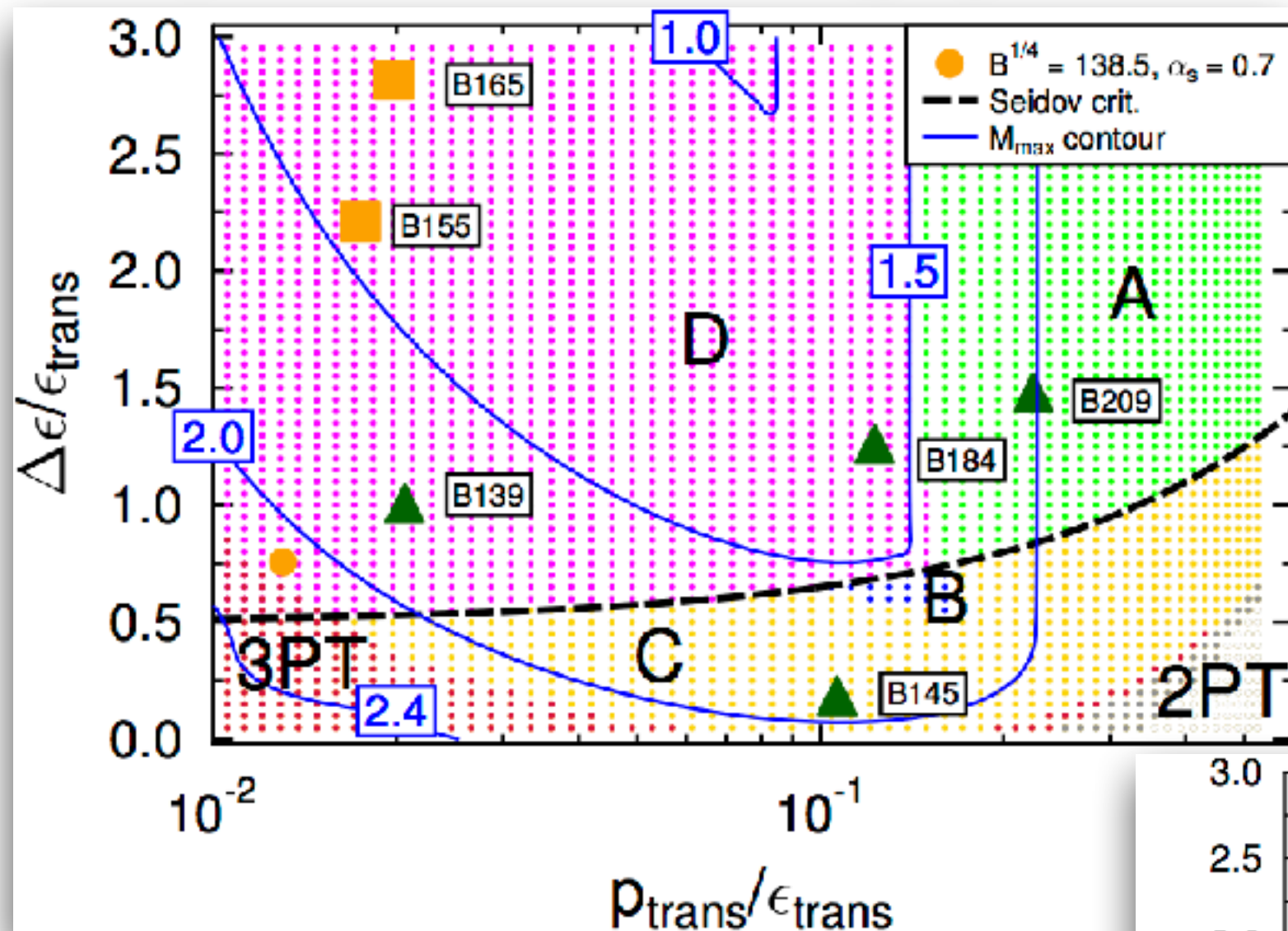
reconfinement (HQHQ)

absolutely stable quark matter (QHQQ)

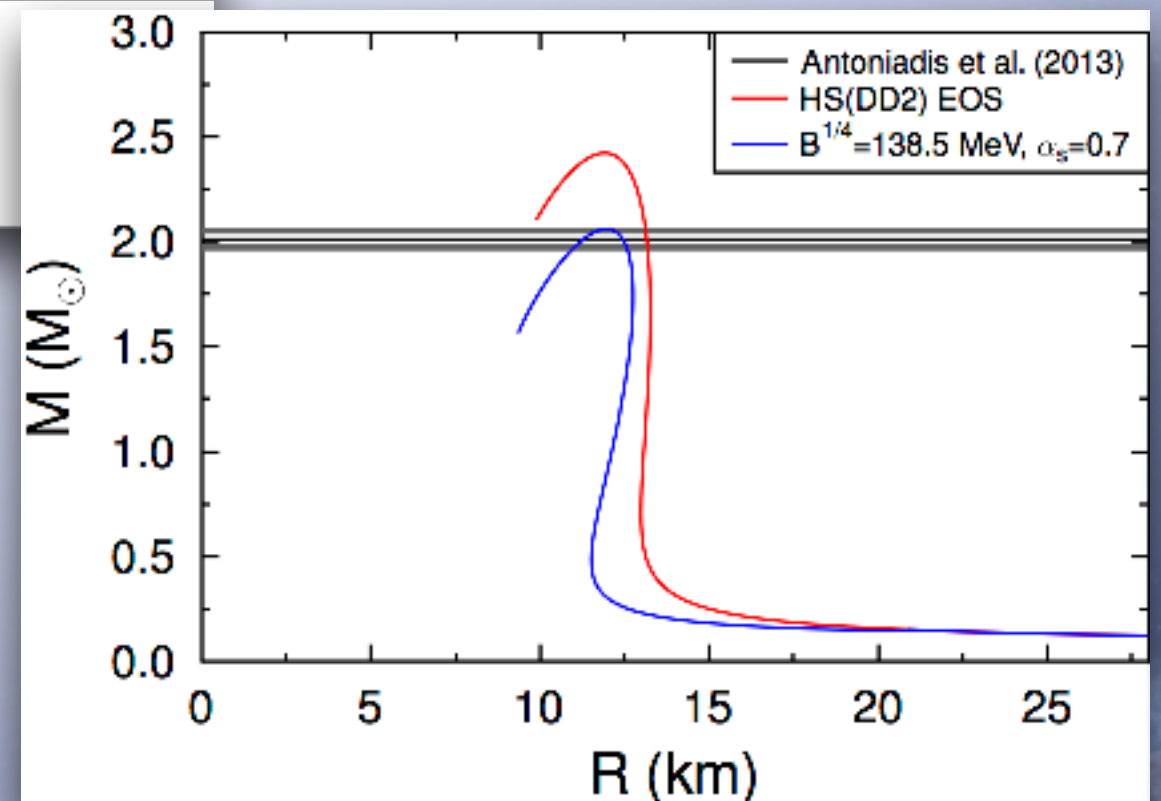
- reconfinement for low transition pressures and weak phase transitions
- (almost pure) quark stars appear
- $M_{\text{max}} > M_{\text{max}}(\text{HSDD2})$  only possible for quark stars



# Comparison with existing hybrid EOSs



- constant-speed of sound EOS can be transferred to bag model
- expectations confirmed, third family favorable for explosions
- new quark-hadron hybrid general purpose EOS just finished



# Summary and conclusions

- the QCD phase transition is *entropic* ( $dP/dT|_{PT} < 0$ ) and leads to unusual thermal properties
- possible consequences:
  - inverted convection in proto-neutron stars (Yudin et al. MNRAS 2016)
  - hot third family of compact stars
  - core-collapse supernova explosions (?)
- systematic analysis of quark matter properties, reconfinement problem
- new hybrid EOS with interesting properties just finished
- work in progress: spherically symmetric and multi-D CCSN simulations
- compare prediction for neutron star and black hole birth mass distribution with observations
- effects of quark matter in NS mergers?