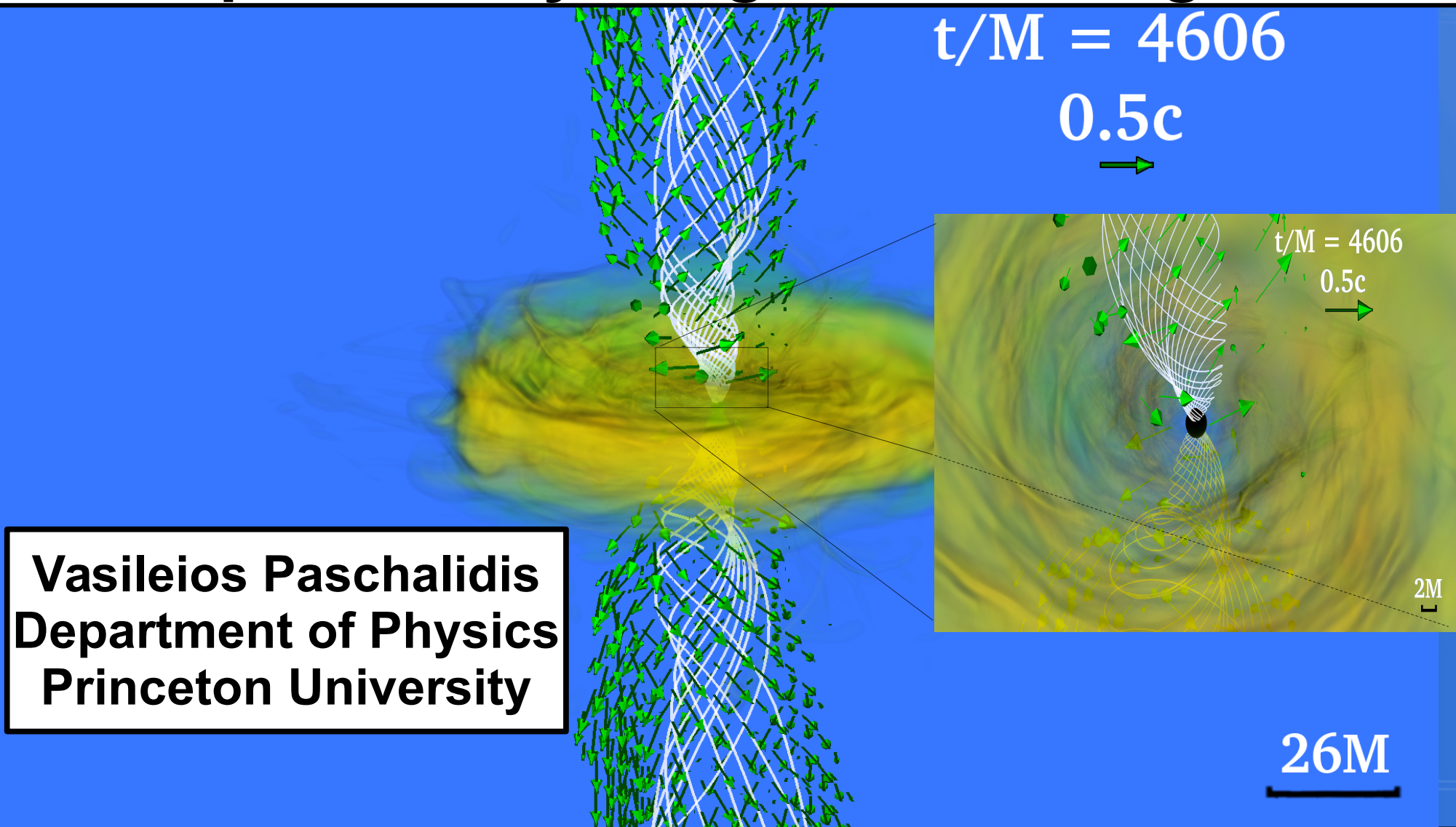


New paths to probing the nuclear equation of state via multimessenger signals from compact binary mergers involving NSs



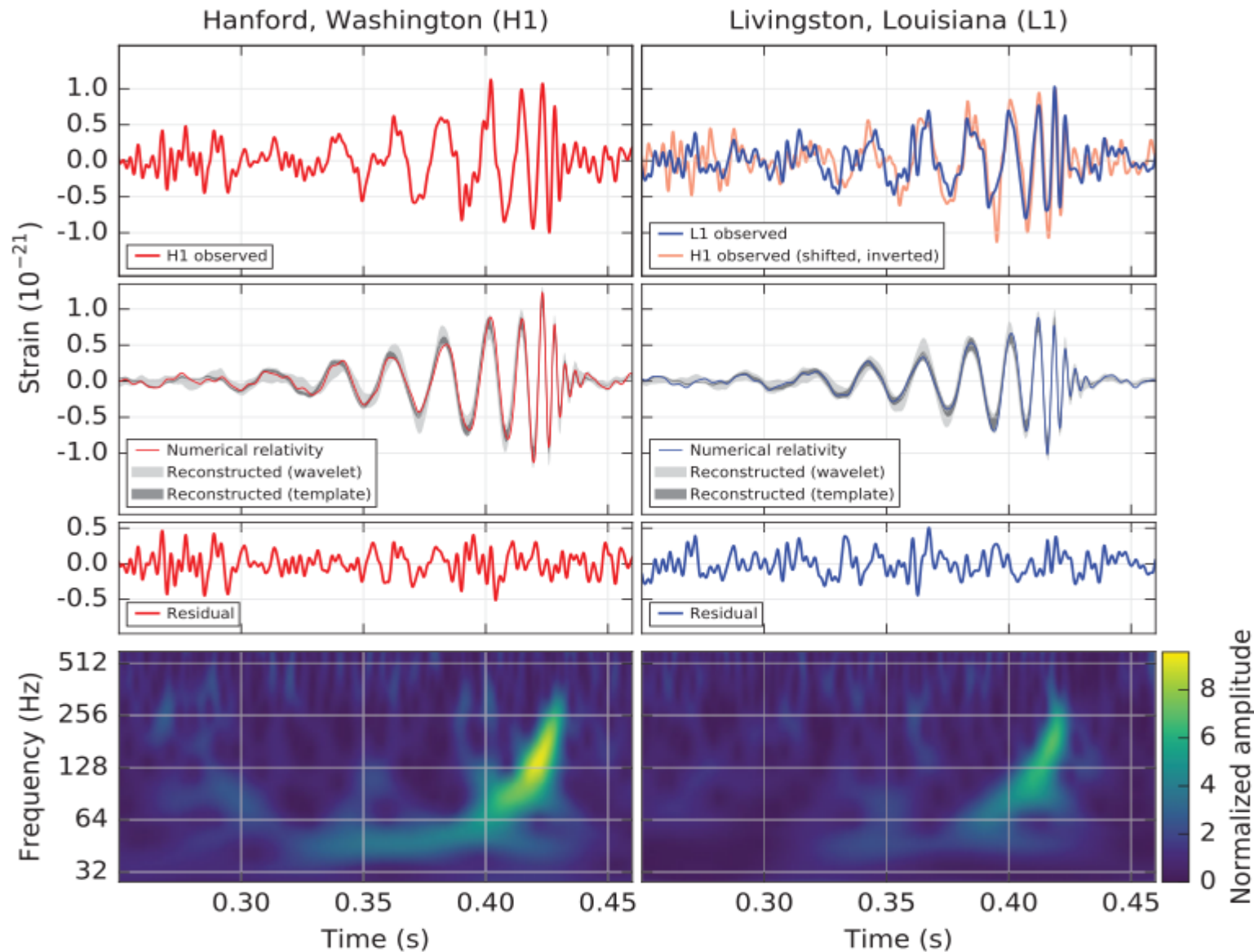
Vasileios Paschalidis
Department of Physics
Princeton University

SUMMARY

- Black hole – neutron star (BHNS) and neutron star- neutron star (NSNS) binaries are viable short gamma-ray burst (sGRB) progenitors
- Even one BHNS-generated gravitational wave (GW) signal coincident with a sGRB could potentially rule out a large number of (cold) nuclear equations of state (EOS) for $M_{\text{NS}} < 2M_{\text{sun}}$
- NSNS mergers form hypermassive NSs that generically undergo a one-arm ($m=1$) spiral instability; instability \rightarrow signal!
- GWs generated by the $m=1$ instability can constrain the finite-temperature nuclear EOS for $M_{\text{NS}} > 2M_{\text{sun}}$
- Numerical relativity is crucial for GW science and constraining the NS EOS

Gravitational waves exist!

GW150914



Gravitational waves exist!

GW150914

- GW150914:
 - Marked the birth of gravitational wave astronomy
 - Confirmed general relativity (GR) in the dynamical, strong-field regime
 - Best evidence for the existence of Bhs and binary BHBHs
 - Numerical relativity is crucial for GW science
 - Surprises await (LIGO was thought to be a NSNS detector)

Gravitational waves exist!

GW150914

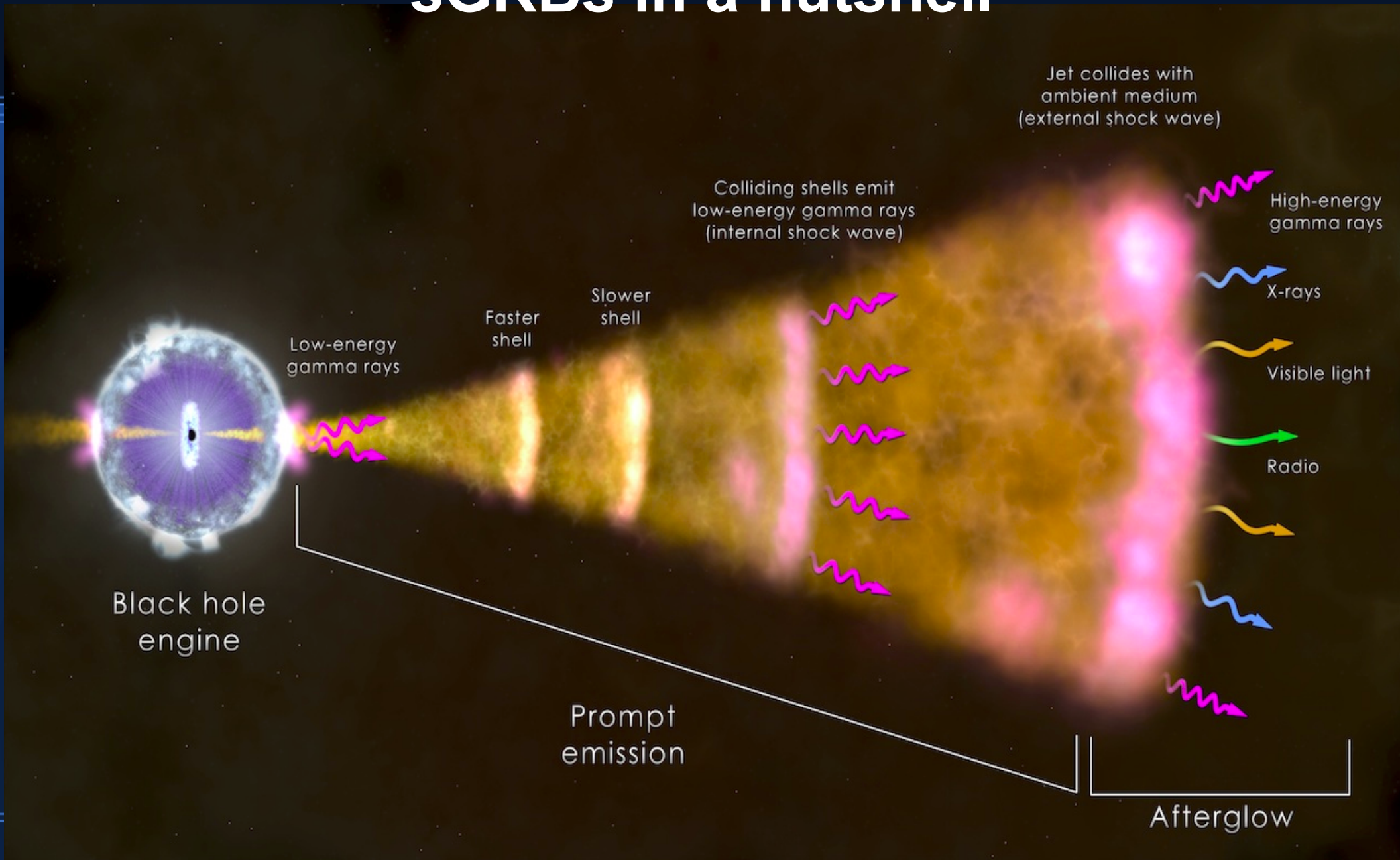
- GW150914:
 - Marked the birth of gravitational wave astronomy
 - Confirmed general relativity (GR) in the dynamical, strong-field regime
 - Best evidence for the existence of BHs and binary BHBHs
 - Numerical relativity is crucial for GW science
 - Surprises await (LIGO was thought to be a NSNS detector)
- In the next few years aLIGO/Virgo will routinely detect BHNS and NSNS
- BHNS and NSNS have are likely to be accompanied by a wealth of electromagnetic (EM) signals counterpart to the GWs, such as kilonovae, short gamma-ray bursts etc. (see also Luciano's talks)
- Coincident detection of GW and EM signals will mark the onset of multimessenger astronomy

BHNS and NSNS binaries are
viable sGRB progenitors

sGRBs in a nutshell

- Flashes of gamma rays of extra-galactic origin
- Instruments: BATSE, Swift, HETE-2, Fermi, Hubble, Liverpool & Faulkes...
- Timescales: $T_{90} \leq 2\text{s}$; $\langle T_{90} \rangle = 0.2\text{s}$;
- Gamma ray luminosities: $10^{50} - 10^{52} \text{ erg/s}$ ($10\text{erg} = 1 \text{ joule}$)
- Host galaxies: spirals & gas depleted ellipticals \rightarrow (old stars) (Berger 2013)
- Popular model: relativistic jet (fireball); $\Gamma \geq 100$ (Piran 2004)
- Plausible engine: BH + accretion disk (with twin relativistic jets)

sGRBs in a nutshell



sGRBs in a nutshell

- Flashes of gamma rays of extra-galactic origin
- Instruments: BATSE, Swift, HETE-2, Fermi, Hubble, Liverpool & Faulkes...
- Timescales: $T_{90} \leq 2\text{s}$; $\langle T_{90} \rangle = 0.2\text{s}$;
- Gamma ray luminosities: $10^{50} - 10^{52} \text{ erg/s}$ ($10\text{erg} = 1 \text{ joule}$)
- Host galaxies: spirals & gas depleted ellipticals \rightarrow (old stars) (Berger 2013)
- Popular model: relativistic jet (fireball); $\Gamma \geq 100$ (Piran 2004)
- Plausible engine: BH + accretion disk (with twin relativistic jets)
- Progenitor: **NSNS?** Eichler et al. 1989; **BHNS?** Paczynski 1991

sGRBs in a nutshell

- Flashes of gamma rays of extra-galactic origin
- Instruments: BATSE, Swift, HETE-2, Fermi, Hubble, Liverpool & Faulkes...
- Timescales: $T_{90} \leq 2\text{s}$; $\langle T_{90} \rangle = 0.2\text{s}$;
- Gamma ray luminosities: $10^{50} - 10^{52}$ erg/s (10erg = 1 joule)
- Host galaxies: spirals & gas depleted ellipticals \rightarrow (old stars) (Berger 2013)
- Popular model: relativistic jet (fireball); $\Gamma \geq 100$ (Piran 2004)
- Plausible engine: BH + accretion disk (with twin relativistic jets)
- Progenitor: **NSNS?** Eichler et al. 1989; **BHNS?** Paczynski 1991
- Jet launching mechanism: magnetic fields or neutrinos

sGRBs in a nutshell

- Flashes of gamma rays of extra-galactic origin
- Instruments: BATSE, Swift, HETE-2, Fermi, Hubble, Liverpool & Faulkes...
- Timescales: $T_{90} \leq 2\text{s}$; $\langle T_{90} \rangle = 0.2\text{s}$;
- Gamma ray luminosities: $10^{50} - 10^{52}$ erg/s (10erg = 1 joule)
- Host galaxies: spirals & gas depleted ellipticals \rightarrow (old stars) (Berger 2013)
- Popular model: relativistic jet (fireball); $\Gamma \geq 100$ (Piran 2004)
- Plausible engine: BH + accretion disk (with twin relativistic jets)
- Progenitor: **NSNS?** Eichler et al. 1989; **BHNS?** Paczynski 1991
- Jet launching mechanism: magnetic fields or neutrinos

Motivation for simulating BH-NS and NS-NS mergers as sGRB engines

- Engine behind short-hard Gamma Ray Bursts (sGRBs) is not known!
- NSNS and BHNS mergers: favored progenitors for sGRBs
- But,
 - we do not know how these mergers may power sGRBs
 - it has never been shown theoretically that mergers of compact binaries can launch highly relativistic jets (until recently no jets at all)!
- Through a complete computational/theoretical model of sGRB engines → Infer the progenitor parameters from sGRB → crosscheck with GWs

Motivation for simulating BH-NS and NS-NS mergers as sGRB engines

The theoretical challenge:

Demonstrate from first principles that BH-NS/NS-NS mergers can launch jets (similar to core collapse SN).

Motivation for simulating BH-NS and NS-NS mergers as sGRB engines

The theoretical challenge:

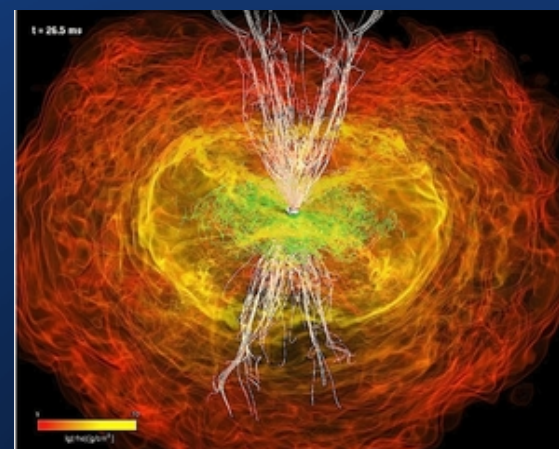
Demonstrate from first principles that BH-NS/NS-NS mergers can launch jets (similar to core collapse SN).

Simulations in full non-linear general relativity (GR), necessary to capture the dynamical inspiral, merger, disk formation and accretion onto the BH and to predict the gravitational wave signature → multimessenger astronomy!

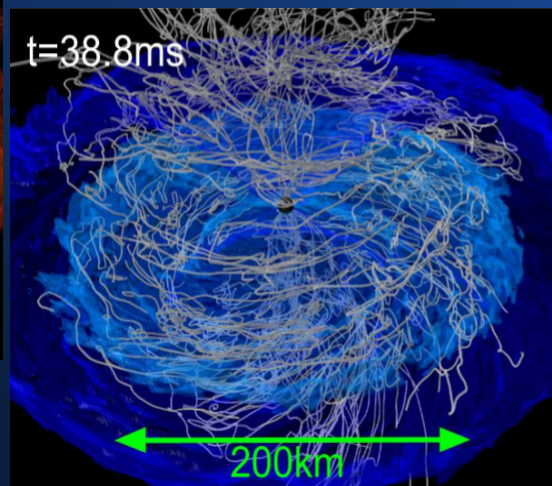
NS-NS mergers \rightarrow jets?

NS-NS mergers \rightarrow jets?

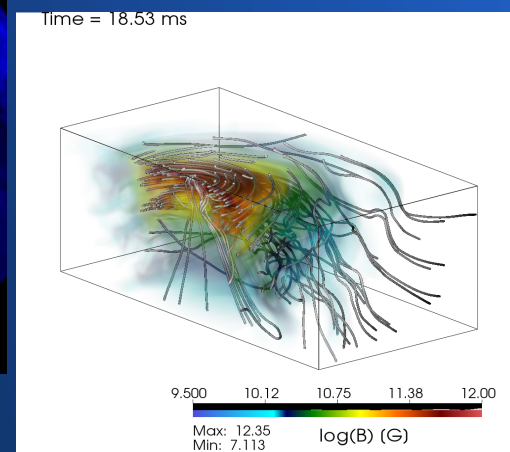
- MHD studies in full GR find with initial dipole magnetic fields confined to the NS interiors:



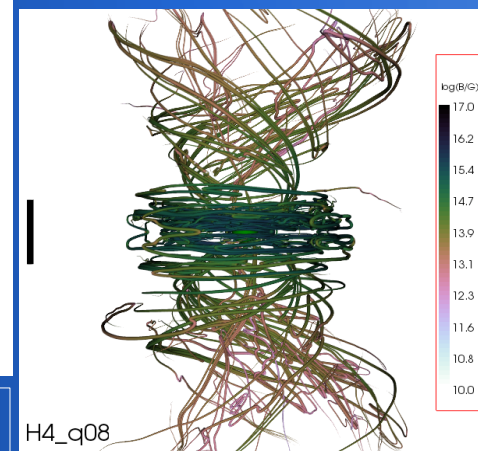
Rezzolla et al. 2011



Kiuchi et al. 2015



Dionysopoulou & Rezzolla 2016

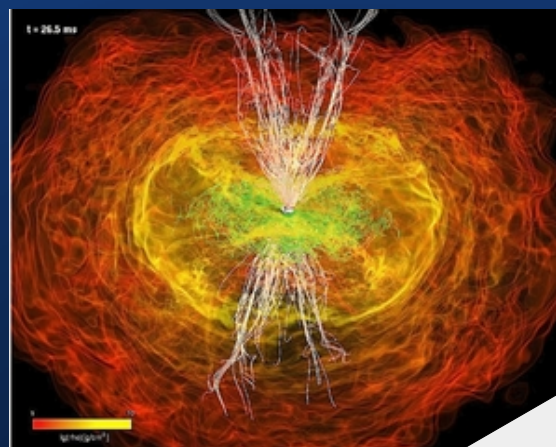


Kawamura et al. 2016

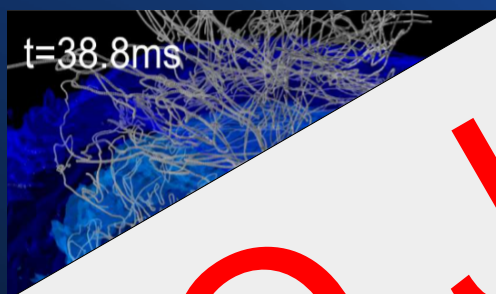
NS-NS mergers \rightarrow jets?

- MHD studies in full GR find with initial dipole magnetic field confined to the NS interiors:

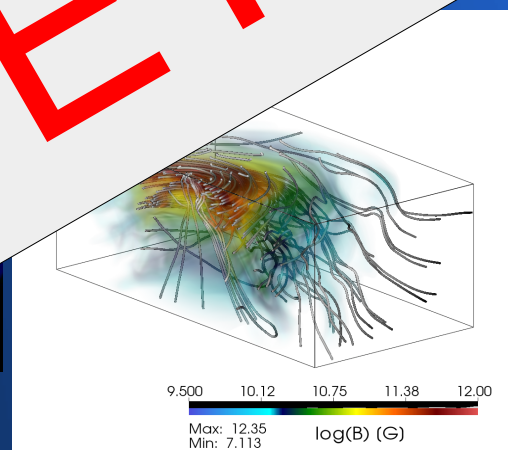
NO JETS!



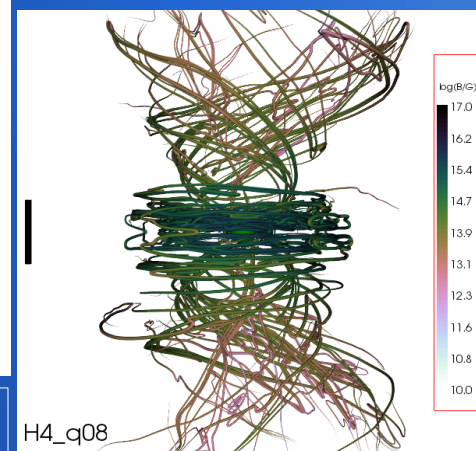
Rezzolla et al.



et al. 2015



Dionysopoulou &
Rezzolla 2016

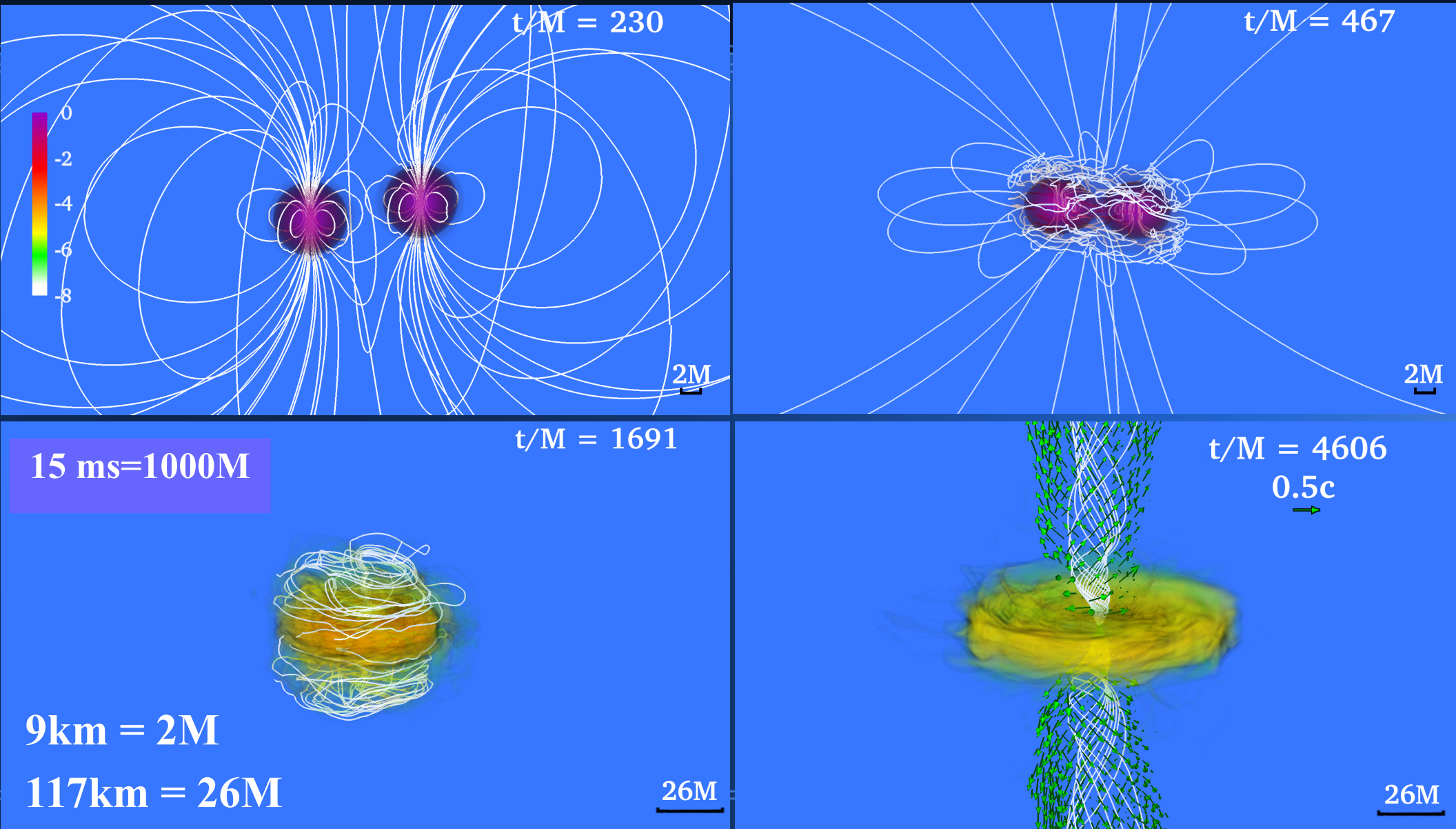


Kawamura et al. 2016

NS-NS mergers → jets?

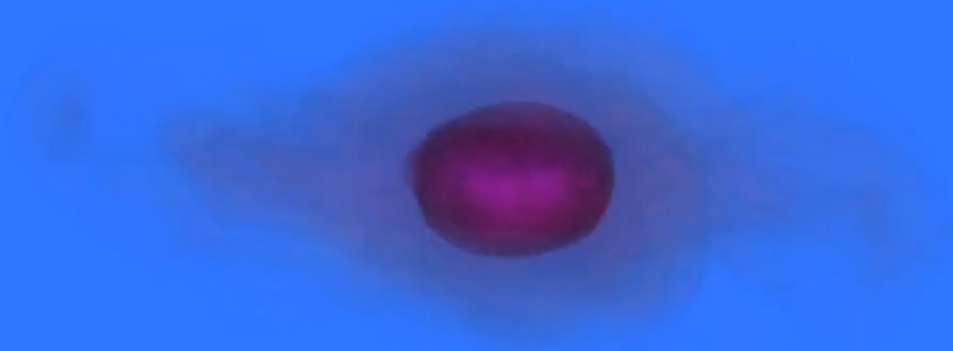
- Ruiz, Lang, Paschalidis, Shapiro, Ap. J. Lett. 824 (2016)
- Perform simulations with magnetized NSNS at reasonably high resolutions
- Initial data same as in Rezzolla et al (2011):
- Initial B field:
 - dipolar (interior + exterior), and interior only
 - Stronger than Rezzolla et al (2011), but still dynamically weak ($320 \leq P_{\text{gas}}/P_{\text{mag}}$)
 - Strength motivated by expectations of post-merger B-field amplification due to KHI and MRI → $\langle B \rangle \sim 10^{15.3-16}$ G (Price & Rosswog 2006, Zrake & MacFadyen 2013, Kiuchi et al. 2015)

NSNS mergers → incipient jets



NSNS mergers → incipient jets

$t/M = 665$



BH-NS mergers \rightarrow jets?

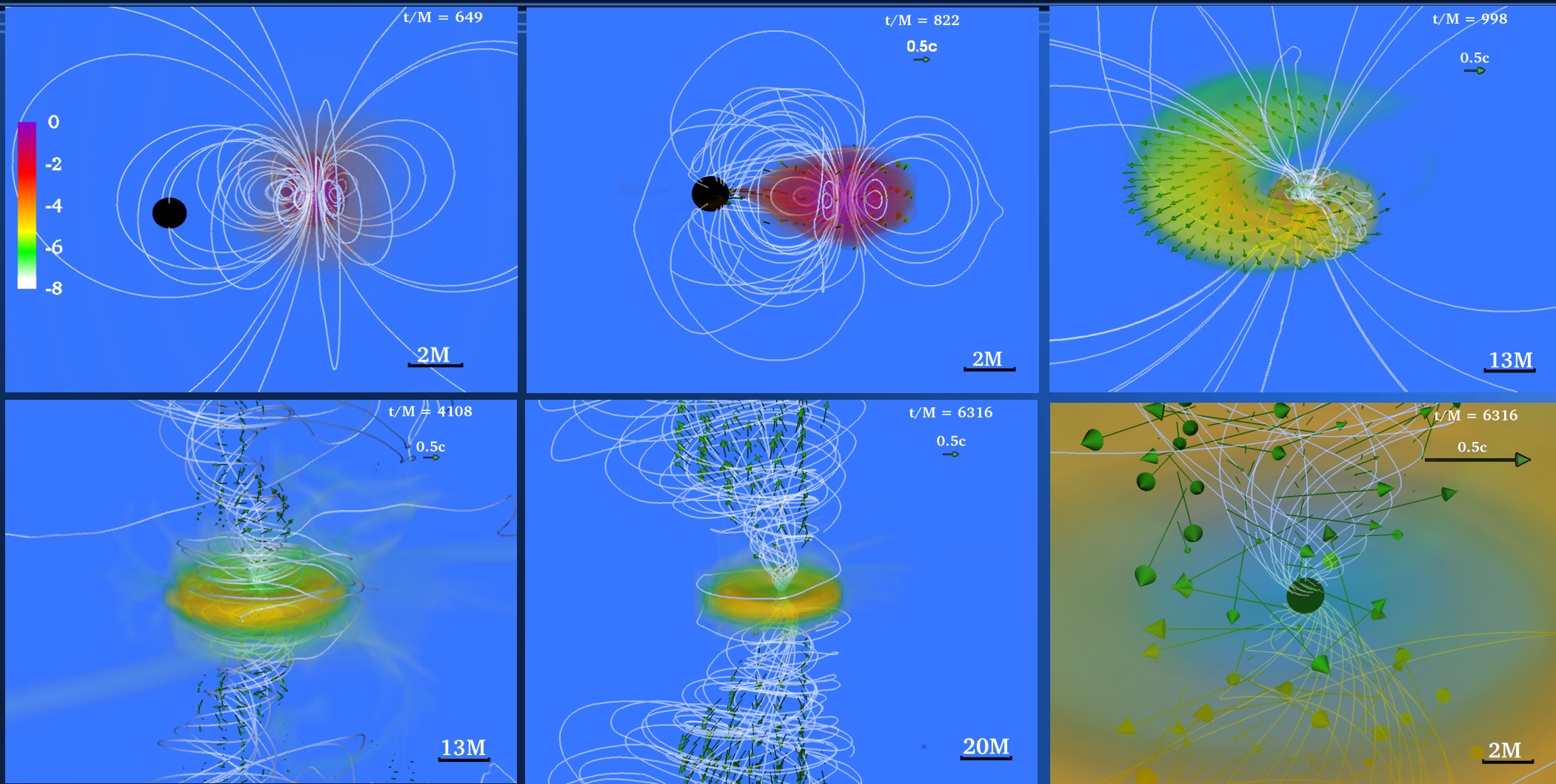
Previous works with purely interior dipole magnetic fields (BH spin \parallel L_{obs}):

- Chawla, Anderson, Besselman et al. (2010) \rightarrow No jet
- Etienne, Liu, Paschalidis, Shapiro (2012) \rightarrow No jet
- Etienne, Paschalidis, Shapiro (2012) \rightarrow No jet
- Kiuchi, Sekiguchi, Kyotoku, Shibata, Taniguchi, Wada (2014) \rightarrow No jet

BH-NS mergers \rightarrow No jets?

An incipient jet emerges

Paschalidis, Ruiz, Shapiro Ap. J. Lett. 806 (2015)



An incipient jet emerges

- $\frac{B^2}{8\pi\rho c^2} \sim 100$ ~ terminal Lorentz factor (Vlahakis & Konigl 2003)
- Disk lifetime: $t_{disk} \sim \frac{M_{disk}}{\dot{M}} \sim O(0.1 s)$ consistent with short sGRB $\langle T_{90} \rangle$
- Outgoing EM luminosity: $L_{EM} \sim 10^{51} \text{ erg/s}$ ~ consistent with typical sGRB
- BHNS and NSNS mergers are viable sGRB engines!
- Delay time between peak GW amplitude and jet launching $> 50 \text{ ms}$

Coincident detection of BHNS-generated GW signal and a sGRB can rule out a large number of (cold) nuclear EOS for $M_{\text{NS}} < 2M_{\text{sun}}$

BHNS mergers \rightarrow BH+disk? Not trivial!

BHNS mergers \rightarrow BH+disk? Not trivial!

- Why is it difficult to create an accretion disk following merger of a quasicircular BH-NS?

BHNS mergers \rightarrow BH+disk? Not trivial!

- Why is it difficult to create an accretion disk following merger of a quasicircular BH-NS?
- To have an appreciable disk, the NS must be tidally disrupted **outside** the (effective) innermost circular orbit (ISCO)

BHNS mergers \rightarrow BH+disk? Not trivial!

- Key parameters determining the interplay between ISCO and tidal disruption radius:
- $q = M_{\text{BH}}/M_{\text{NS}}$ and NS compaction, $C = GM_{\text{NS}}/R_{\text{NS}}c^2 \rightarrow$ tidal disruption radius

BHNS mergers \rightarrow BH+disk? Not trivial!

- Key parameters determining the interplay between ISCO and tidal disruption radius:
- $q = M_{\text{BH}}/M_{\text{NS}}$ and NS compaction, $C = GM_{\text{NS}}/R_{\text{NS}}c^2 \rightarrow$ tidal disruption radius

$$a_{\text{tidal}} = a_{g, \text{NS}} \Rightarrow r_{\text{tidal}} = 2 \left(\frac{q}{10} \right)^{-2/3} \left(\frac{C}{0.2} \right)^{-1} r_{g, \text{BH}}, \quad r_{g, \text{BH}} = \frac{GM_{\text{BH}}}{c^2}$$

BHNS mergers \rightarrow BH+disk? Not trivial!

- Key parameters determining the interplay between ISCO and tidal disruption radius:
- $q = M_{\text{BH}}/M_{\text{NS}}$ and NS compaction, $C = GM_{\text{NS}}/R_{\text{NS}}c^2 \rightarrow$ tidal disruption radius

$$a_{\text{tidal}} = a_{g, \text{NS}} \Rightarrow r_{\text{tidal}} = 2 \left(\frac{q}{10} \right)^{-2/3} \left(\frac{C}{0.2} \right)^{-1} r_{g, \text{BH}}, \quad r_{g, \text{BH}} = \frac{GM_{\text{BH}}}{c^2}$$

- BH spin \rightarrow ISCO $r_{g, \text{BH}} \leq r_{\text{ISCO}} \leq 6 r_{g, \text{BH}}$

BHNS mergers \rightarrow BH+disk? Not trivial!

- Key parameters determining the interplay between ISCO and tidal disruption radius:
- $q=M_{\text{BH}}/M_{\text{NS}}$ and NS compaction, $C=GM_{\text{NS}}/R_{\text{NS}}c^2 \rightarrow$ tidal disruption radius

$$a_{\text{tidal}} = a_{g, \text{NS}} \Rightarrow r_{\text{tidal}} = 2 \left(\frac{q}{10} \right)^{-2/3} \left(\frac{C}{0.2} \right)^{-1} r_{g, \text{BH}}, \quad r_{g, \text{BH}} = \frac{GM_{\text{BH}}}{c^2}$$

- BH spin \rightarrow ISCO $r_{g, \text{BH}} \leq r_{\text{ISCO}} \leq 6 r_{g, \text{BH}}$
- For a given BH spin and mass ratio, there exists a **critical compaction**, such that following NS disruption no mass is left outside the BH to form a disk.

Probing the nuclear EOS with GW+sGRB observations

- Let us assume that we have a BHNS GW signal and an associated sGRB
- The inspiral GW signal will provide the NS mass, the BH mass and spin

Probing the nuclear EOS with GW+sGRB observations

- Let us assume that we have a BHNS GW signal and an associated sGRB
- The inspiral GW signal will provide the NS mass, the BH mass and spin
- Numerical relativity hydrodynamic simulations using the inferred binary parameters (plus their uncertainties) can be run for all plausible nuclear EOSs to determine which EOSs result in a disk-less BH remnant.
- EOSs forming such a remnant are ruled out by the existence of a sGRB!

Probing the nuclear EOS with GW+sGRB observations

- Let us assume that we have a BHNS GW signal and an associated sGRB
- The inspiral GW signal will provide the NS mass, the BH mass and spin
- Numerical relativity hydrodynamic simulations using the inferred binary parameters (plus their uncertainties) can be run for all plausible nuclear EOSs to determine which EOSs result in a disk-less BH remnant.
- EOSs forming such a remnant are ruled out by the existence of a sGRB!
- Equivalently, a large No. of numerical relativity hydrodynamic simulations adopting plausible EOSs can be run a priori to determine the critical compaction for a disk-less BH remnant for given binary parameters.

Probing the nuclear EOS with GW+sGRB observations

- Foucart (2012) compiled the results from many numerical relativity BHNS simulations and derived a fitting formula for disk mass predictions

$$\frac{M_{disk}}{M_{NS}} = 0.415 q^{1/3} (1 - 2C) - 0.148 q C \frac{R_{ISCO}}{M_{BH}}$$

- Critical compaction for $M_{disk} = 0$

$$C_{NS,crit} = \left(2 + 2.14 q^{2/3} \frac{R_{ISCO}}{M_{BH}} \right)^{-1}$$

Probing the nuclear EOS with GW+sGRB observations

- Foucart (2012) compiled the results from many numerical relativity BHNS simulations and derived a fitting formula for disk mass predictions

$$\frac{M_{disk}}{M_{NS}} = 0.415 q^{1/3} (1 - 2C) - 0.148 q C \frac{R_{ISCO}}{M_{BH}}$$

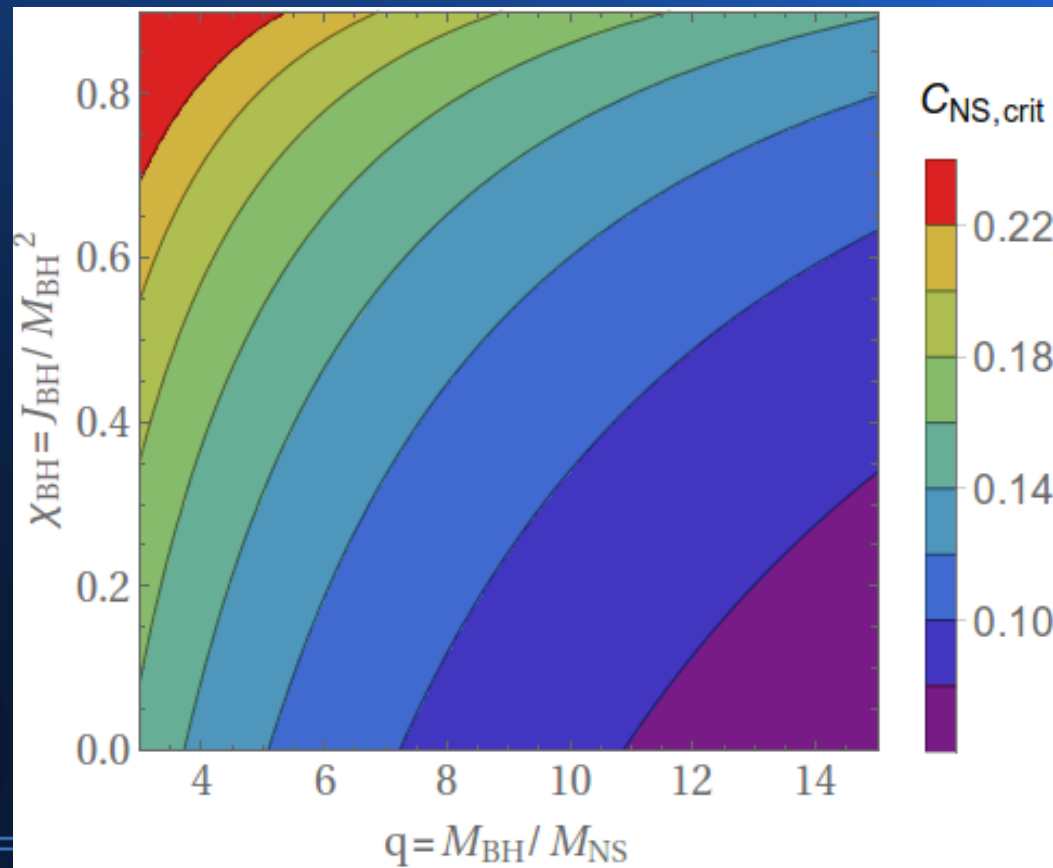
- Critical compaction for $M_{disk} = 0$

$$C_{NS,crit} = \left(2 + 2.14 q^{2/3} \frac{R_{ISCO}}{M_{BH}} \right)^{-1}$$

- Small q and large BH spin (small R_{ISCO}) increase the $C_{NS,crit}$

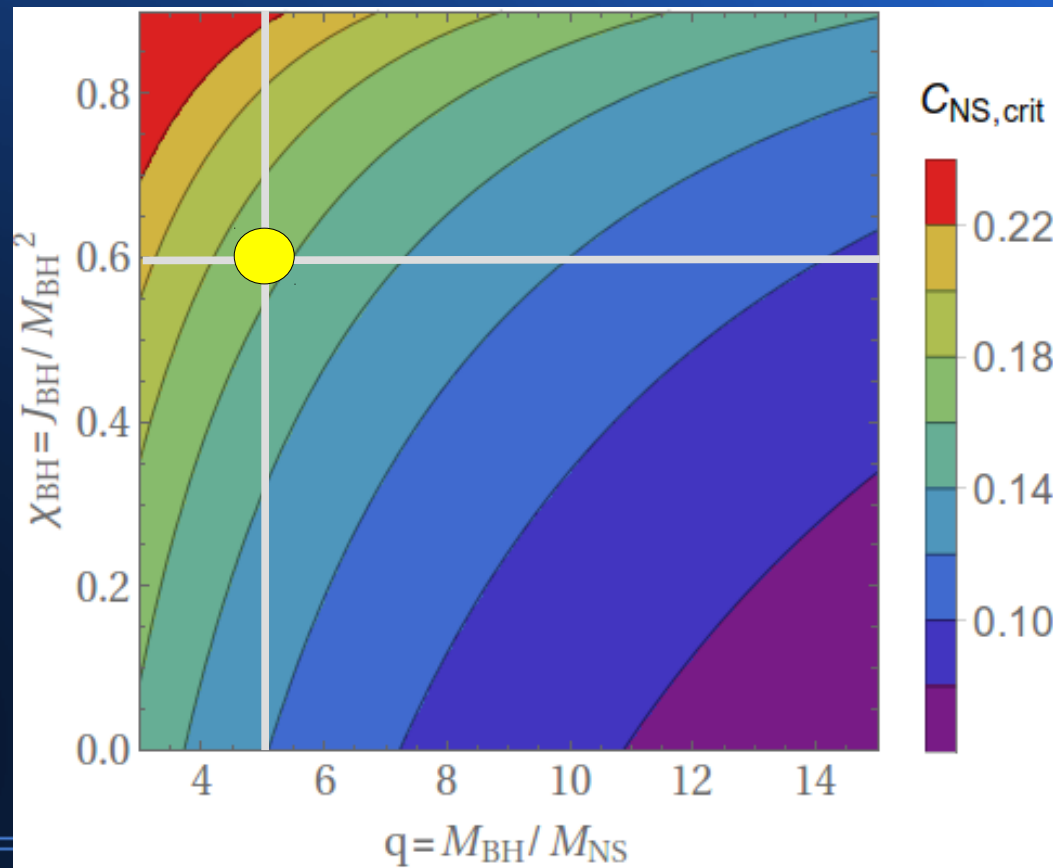
Probing the nuclear EOS with GW+sGRB observations

$$C_{NS,crit} = \left(2 + 2.14 q^{2/3} \frac{R_{ISCO}}{M_{BH}} \right)^{-1}$$



Probing the nuclear EOS with GW+sGRB observations

$$q=5, \chi_{BH}=0.6$$



Probing the nuclear EOS with GW+sGRB observations

- Advantages:
 - Practically model independent
 - Only two assumptions: I) GR, II) No disk \rightarrow no sGRB
 - Orbital parameters will be known from early inspiral – no need for finite size effects
 - Pure hydrodynamic simulations suffice: no need for complex physics, such as magnetic fields and neutrino transport
- Disadvantage:
 - if true EOS is soft (small NS radii), detection of a simultaneous sGRB + GW BHNS signal may never be realized

Probing the nuclear EOS with GW+sGRB observations

- Advantages:
 - Practically model independent
 - Only two assumptions: I) GR, II) No disk \rightarrow no sGRB
 - Orbital parameters will be known from early inspiral – no need for finite size effects
 - Pure hydrodynamic simulations suffice: no need for complex physics, such as magnetic fields and neutrino transport
- Disadvantage:
 - if true EOS is soft (small NS radii), detection of a simultaneous sGRB + GW BHNS signal may never be realized
- Pannarale & Ohm (2014) proposed a similar method, but assuming a finite, non-zero $M_{\text{thres}} = 0.03M_{\text{sun}}$ for no sGRB \rightarrow model dependent

NSNS mergers form hypermassive NSs that generically undergo a one-arm ($m=1$) instability

GWs generated by the $m=1$ instability can constrain the finite-temperature nuclear EOS for $M_{\text{NS}} > 2M_{\text{sun}}$

One-arm instability

- Shearing stellar instability (Corvino et al. 2010) → requires differential rotation
- Discovered by Centrella et al. (2001) in Newtonian hydrodynamic simulations of soft polytropic ($\Gamma=1.3$), differentially rotating stars

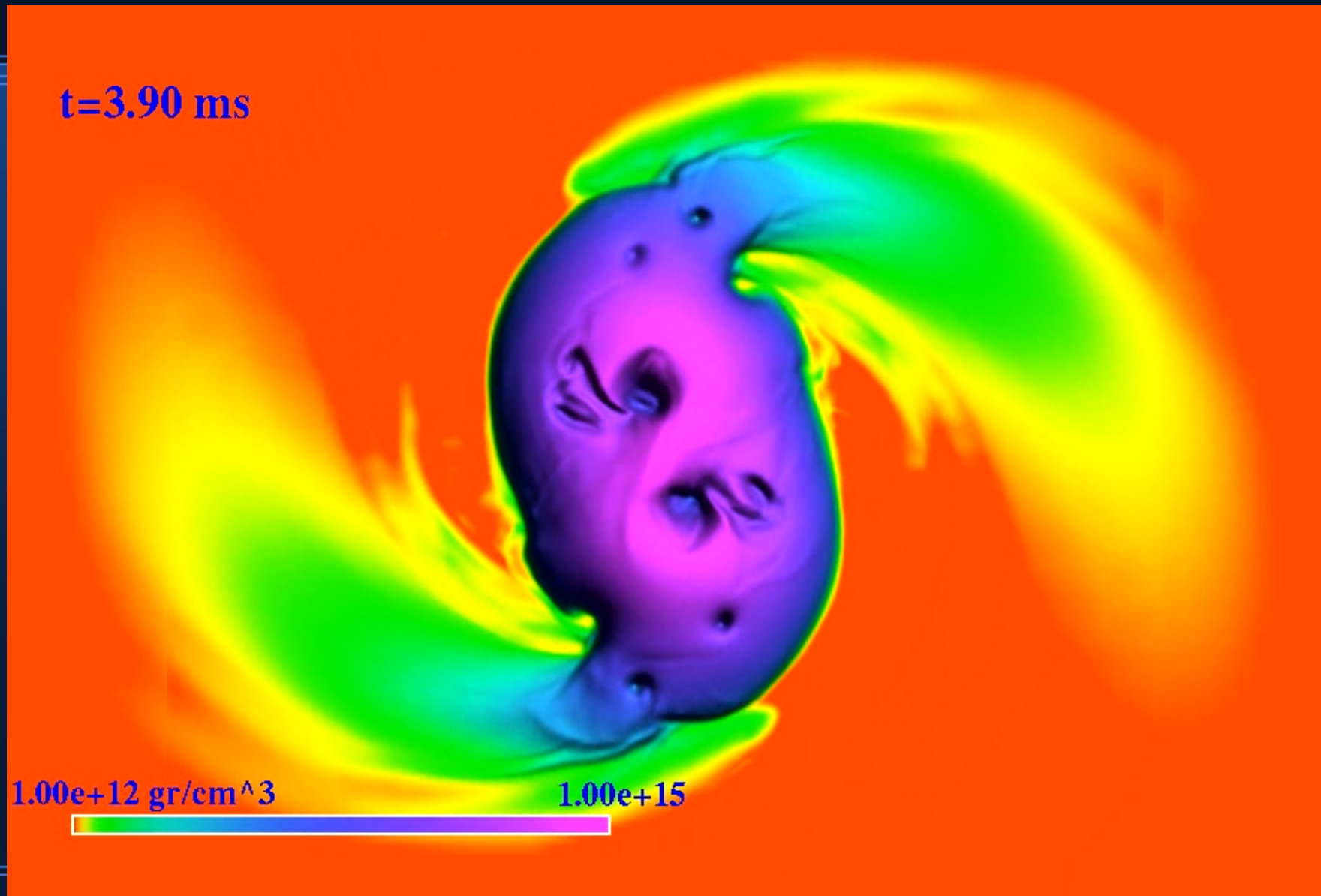
One-arm spiral instability

- Possible mechanism: (resonant excitation?) → corotation radius (Ou & Tohline 2006, Watts et al. 2003)
- Has been observed in Newtonian and GR core collapse simulations (Ott et al 2005, Ott et al. 2006, Kuroda et al. 2014)
- In over 15 years of NS-NS merger simulations, it has never been reported to occur in NS-NS mergers, until recently.

Eccentric NSNS mergers with NS spin

- Initial data (Paschalidis et al. 2015, East, Paschalidis et al. 2016 a, b):
 - adopt (phenom.) piecewise polytropic EOSs with a range of stiffness
 - Set two ($1.35M_{\odot}$) stars 200km away, on a marginally unbound orbit determined by a periapse distance r_p
 - Perform hydrodynamics simulations in full general relativity

Eccentric NSNS mergers with spin 0.025



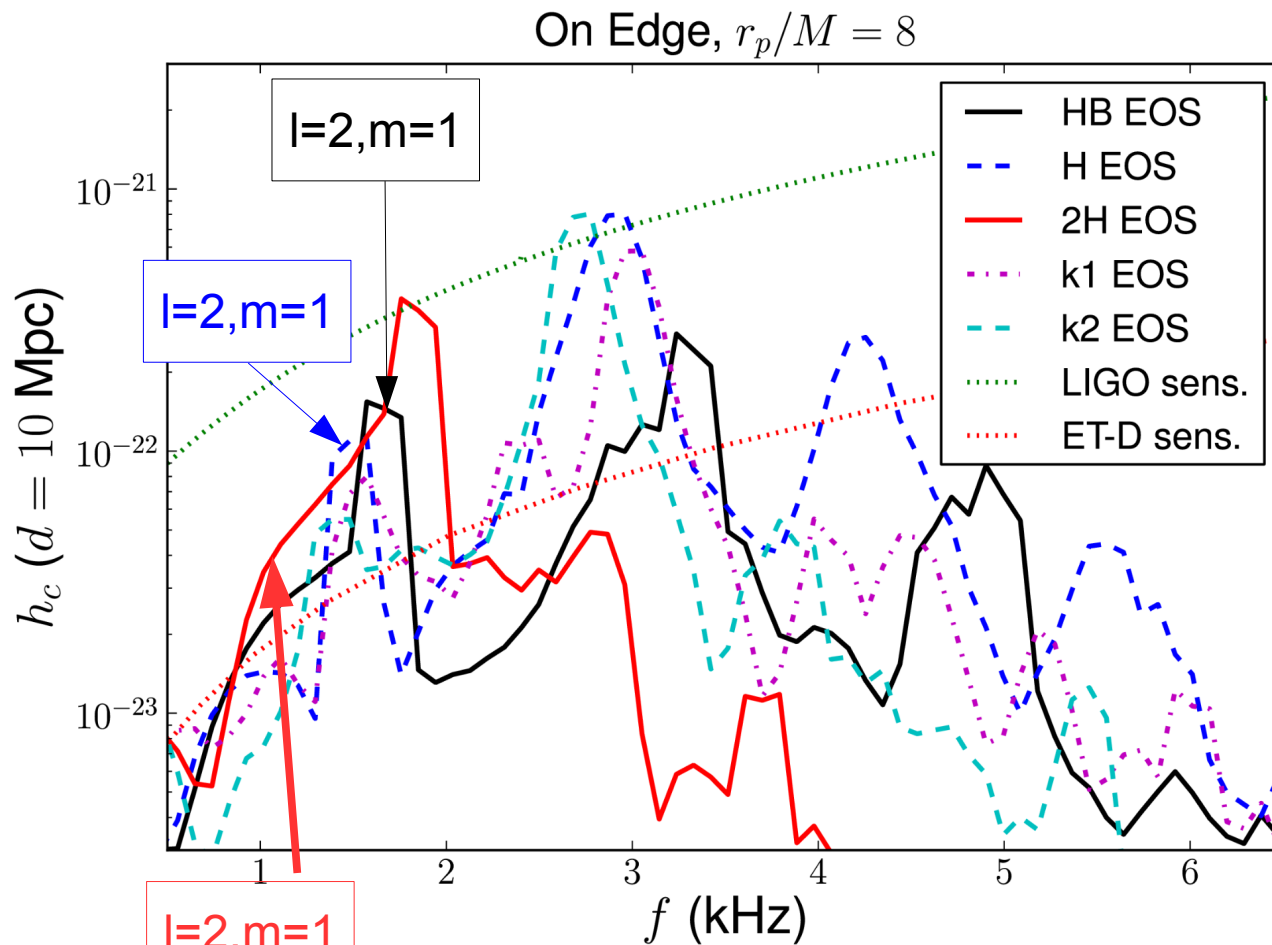
Significance

- Why should we care about this instability?

Significance

- Why should we care about this instability?
- Instability → Signal!

Gravitational Waves: Characteristic strain at 10Mpc, $r_p=8M$ for 10ms

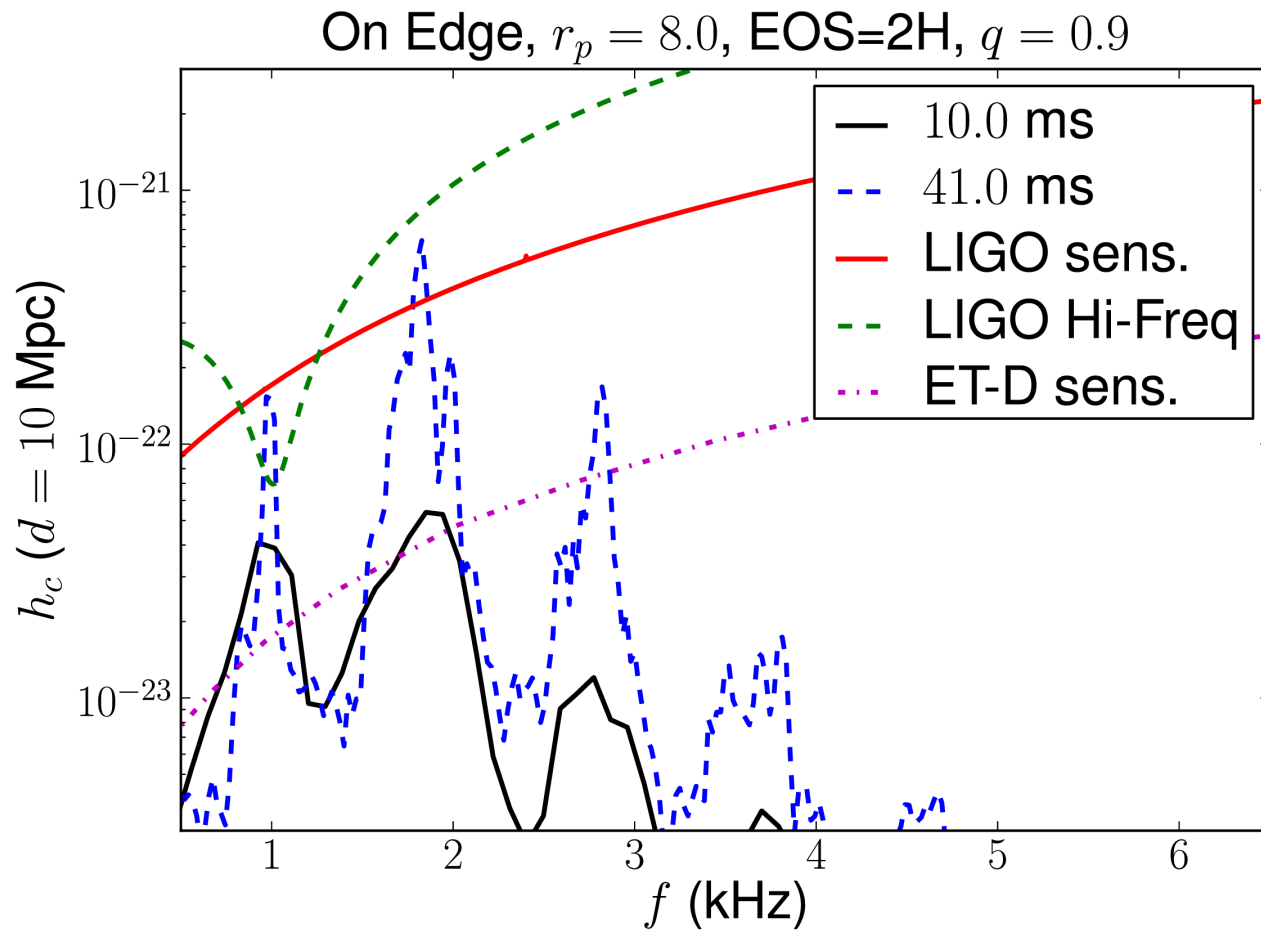


But, GW frequency and amplitude roughly constant with time, and hypermassive neutron star lifetime may be

$$J / \dot{J}_{GW} = 1 - 3s$$

Thus, h_c may be amplified by 100.

Gravitational Waves II: Characteristic strain at 10Mpc, 2H EOS $q=0.9$ for $>10\text{ms}$



Almost perfect
monochromatic source

Correlation of GW 2,1 mode frequency with EOS

The stiffer the EOS, the lower the 2,1 GW mode frequency ($f_{\text{GW},21}$) for a given total mass

Run multiple NSNS simulations varying total mass, and EOS to develop a fitting formula correlating the EOS with $f_{\text{GW},21}$ (much like $l=2, m=2$ mode see Roberto's & Luciano's talk)

Gravitational Waves: detectability

- A figure of merit for detectability is the GW signal-to-noise (SNR) ratio
- East et al. (2016)

$$SNR_{LIGO} \approx 5.6 \left(\frac{T_{m=1}}{400 \text{ ms}} \right)^{1/2} \left(\frac{r}{10 \text{ Mpc}} \right)^{-1} \quad SNR_{ET} \approx 5.0 \left(\frac{T_{m=1}}{400 \text{ ms}} \right)^{1/2} \left(\frac{r}{100 \text{ Mpc}} \right)^{-1}$$

$$J / J_{GW}^{\cdot} = 1 - 3s$$

- But magnetic fields, neutrinos play a role on these timescales

SUMMARY

- BHNS and NSNS binaries are viable sGRB progenitors
- Even one coincident detection of GW signal and a sGRB from a BHNS inspiral and merger can potentially rule out a large number of (cold) nuclear EOSa
- NSNS mergers form hypermassive NSs that generically undergo a $m=1$ instability and GWs generated can constrain the finite-temperature nuclear EOS
- Numerical relativity is crucial for GW science and constraining the NS EOS

Probing the nuclear EOS with GW+sGRB observations

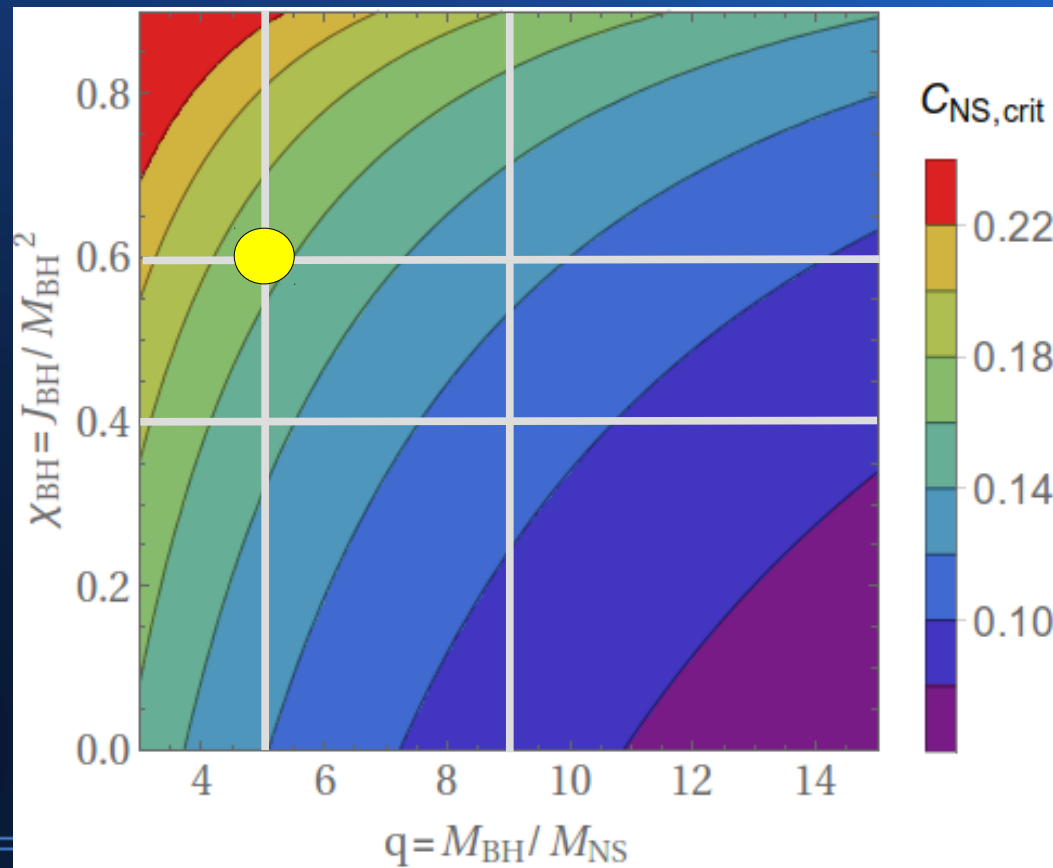
- sGRBs with determined redshifts lies at $r > 460 \text{ Mpc} = 1.42 \times 10^{22} \text{ km}$
- The NSNS aLIGO horizon is $r_{\text{NSNS}} \lesssim 400 \text{ Mpc}$
- The BHNS ($M_{\text{BH}} = 10 M_{\text{sun}}$, $M_{\text{NS}} = 1.4 M_{\text{sun}}$) aLIGO horizon is $r_{\text{NSNS}} \lesssim 900 \text{ Mpc}$
- It is a matter of time until we detect GWs from a inspiralling and merging BHNS binary

Probing the nuclear EOS with GW+sGRB observations

- sGRBs with determined redshifts lies at $r > 460 \text{ Mpc} = 1.42 \times 10^{22} \text{ km}$
- The NSNS aLIGO horizon is $r_{\text{NSNS}} \lesssim 400 \text{ Mpc}$
- The BHNS ($M_{\text{BH}} = 10 M_{\text{sun}}$, $M_{\text{NS}} = 1.4 M_{\text{sun}}$) aLIGO horizon is $r_{\text{NSNS}} \lesssim 900 \text{ Mpc}$
- It is a matter of time until we detect GWs from a inspiralling and merging BHNS binary
- If sGRBs are indeed associated with BHNS mergers, then it is plausible that we will detect a GW BHNS inspiral signal accompanied by a sGRB.

Probing the nuclear EOS with GW+sGRB observations

$$q = 7 \pm 2, \chi_{BH} = 0.5 \pm 0.1$$



What is a hypermassive neutron star (HMNS)?

- NSs can be non-rotating, uniformly rotating or differentially rotating. The amount of rotation determines how much mass the NS can support.

What is a hypermassive neutron star (HMNS)?

- NSs can be non-rotating, uniformly rotating or differentially rotating. The amount of rotation determines how much mass the NS can support.
- For a given equation of state:

The maximum mass that can be supported by a non-spinning NS is known as the Tolman-Oppenheimer-Volkoff (TOV or OV) limit denoted by M_{TOV}

The maximum mass that can be supported by a NS when allowing for maximal uniform rotation is known as the supramassive limit (M_{SUP})

What is a hypermassive neutron star (HMNS)?

- NSs can be non-rotating, uniformly rotating or differentially rotating. The amount of rotation determines how much mass the NS can support.
- For a given equation of state:

The maximum mass that can be supported by a non-spinning NS is known as the Tolman-Oppenheimer-Volkoff (TOV or OV) limit denoted by M_{TOV}

The maximum mass that can be supported by a NS when allowing for maximal uniform rotation is known as the supramassive limit (M_{SUP})

- A NS with mass M_{NS} satisfying $M_{\text{TOV}} < M_{\text{NS}} < M_{\text{SUP}}$ is called **supramassive**
- A NS with mass M_{NS} satisfying $M_{\text{SUP}} < M_{\text{NS}}$ is called **hypermassive**

One-arm instability vs EOS

- East, Paschalidis & Pretorius (2016) focusing on eccentric mergers consider 6 equations of state with fixed total mass at $2.7 M_{\odot}$, and spins 0.05, 0.075, $r_p=8M$

B EOS	$M_{TOV} = 2.06 M_{\odot}$	→ Forms BH → No one-arm instability
HB EOS	$M_{TOV} = 2.12 M_{\odot}$	→ Toroidal HMNSs → Develop $m=1$ inst.
H EOS	$M_{TOV} = 2.25 M_{\odot}$	→ Ellipsoidal HMNSs → Develop $m=1$ inst.
2H EOS	$M_{TOV} = 2.83 M_{\odot}$	→ Ellipsoidal HMNSs → “Develop” $m=1$ inst.
$\Gamma=3, k_1$	$M_{TOV} = 2.06 M_{\odot}$	→ Double core HMNSs → Develop $m=1$ inst.
$\Gamma=3, k_2$	$M_{TOV} = 2.22 M_{\odot}$	→ Double core HMNSs → Develop $m=1$ inst.

One-arm instability vs EOS

- East, Paschalidis & Pretorius (2016) focusing on eccentric mergers consider 6 equations of state with fixed total mass at $2.7 M_{\odot}$, and spins 0.05, 0.075, $r_p=8M$

B EOS	$M_{TOV} = 2.06 M_{\odot}$	→ Forms BH → No one-arm instability
HB EOS	$M_{TOV} = 2.12 M_{\odot}$	→ Toroidal HMNSs → Develop $m=1$ inst.
H EOS	$M_{TOV} = 2.25 M_{\odot}$	→ Ellipsoidal HMNSs → Develop $m=1$ inst.
2H EOS	$M_{TOV} = 2.83 M_{\odot}$	→ Ellipsoidal HMNSs → “Develop” $m=1$ inst.
$\Gamma=3, k_1$	$M_{TOV} = 2.06 M_{\odot}$	→ Double core HMNSs → Develop $m=1$ inst.
$\Gamma=3, k_2$	$M_{TOV} = 2.22 M_{\odot}$	→ Double core HMNSs → Develop $m=1$ inst.

- $m=1$ instability does not depend on the background about which it develops
- $m=1$ instability should be generic in nature.

Eccentric NS-NS mergers (azimuthal modes)

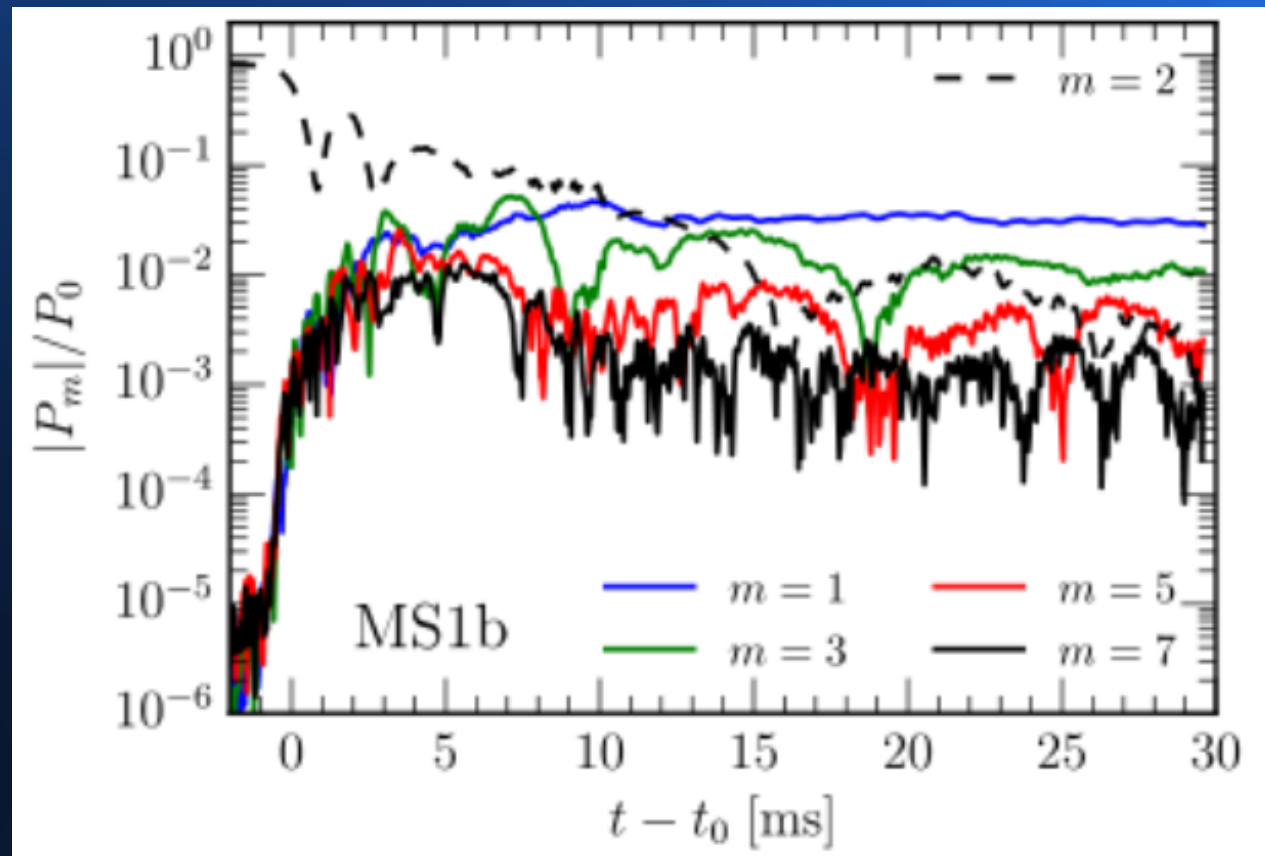
- In all cases where the instability appears

$$J_{\text{merger}} / M^2 \approx 0.9 - 1.0$$

- This is precisely the regime of interest for quasi-circular NSNS mergers!
- Does the instability arise in quasi-circular NSNS mergers?

One-arm instability in quasicircular mergers

- D. Radice et al. (2016) → hydro simulations in full GR with piecewise polytropic EOS (MS1b) and equal-mass, irrotational NSNS



One-arm instability in quasicircular mergers

- Lehner et al. (2016) → hydro simulations in full GR with realistic EOS (MS1b) treating equal-mass and unequal mass, irrotational NSNS
- They find that the one-arm instability operates for realistic EOSs and that the larger the binary mass ratio the easier the $m=1$ density mode dominates following merger.

Gravitational Waves: detectability

- A figure of merit for detectability is the GW signal-to-noise (SNR) ratio
- East et al. (2016)

$$SNR_{LIGO} \approx 2.8 \left(\frac{T_{m=1}}{100 \text{ ms}} \right)^{1/2} \left(\frac{r}{10 \text{ Mpc}} \right)^{-1} \quad SNR_{ET} \approx 2.5 \left(\frac{T_{m=1}}{100 \text{ ms}} \right)^{1/2} \left(\frac{r}{100 \text{ Mpc}} \right)^{-1}$$

- Radice et al. (2016)

$$SNR_{LIGO} \approx 2.0 \left(\frac{T_{m=1}}{100 \text{ ms}} \right)^{1/2} \left(\frac{r}{10 \text{ Mpc}} \right)^{-1} \quad SNR_{ET} \approx 2.0 \left(\frac{T_{m=1}}{100 \text{ ms}} \right)^{1/2} \left(\frac{r}{100 \text{ Mpc}} \right)^{-1}$$

Gravitational Waves: detectability

- A figure of merit for detectability is the GW signal-to-noise (SNR) ratio
- East et al. (2016)

$$SNR_{LIGO} \approx 2.8 \left(\frac{T_{m=1}}{100 \text{ ms}} \right)^{1/2} \left(\frac{r}{10 \text{ Mpc}} \right)^{-1} \quad SNR_{ET} \approx 2.5 \left(\frac{T_{m=1}}{100 \text{ ms}} \right)^{1/2} \left(\frac{r}{100 \text{ Mpc}} \right)^{-1}$$

- Radice et al. (2016)

$$SNR_{LIGO} \approx 2.0 \left(\frac{T_{m=1}}{100 \text{ ms}} \right)^{1/2} \left(\frac{r}{10 \text{ Mpc}} \right)^{-1} \quad SNR_{ET} \approx 2.0 \left(\frac{T_{m=1}}{100 \text{ ms}} \right)^{1/2} \left(\frac{r}{100 \text{ Mpc}} \right)^{-1}$$

- Lehner et al. (2016)

$$SNR_{LIGO} \approx 6.0 \left(\frac{T_{m=1}}{100 \text{ ms}} \right)^{1/2} \left(\frac{r}{10 \text{ Mpc}} \right)^{-1} \quad SNR_{ET} \approx 6.0 \left(\frac{T_{m=1}}{100 \text{ ms}} \right)^{1/2} \left(\frac{r}{100 \text{ Mpc}} \right)^{-1}$$

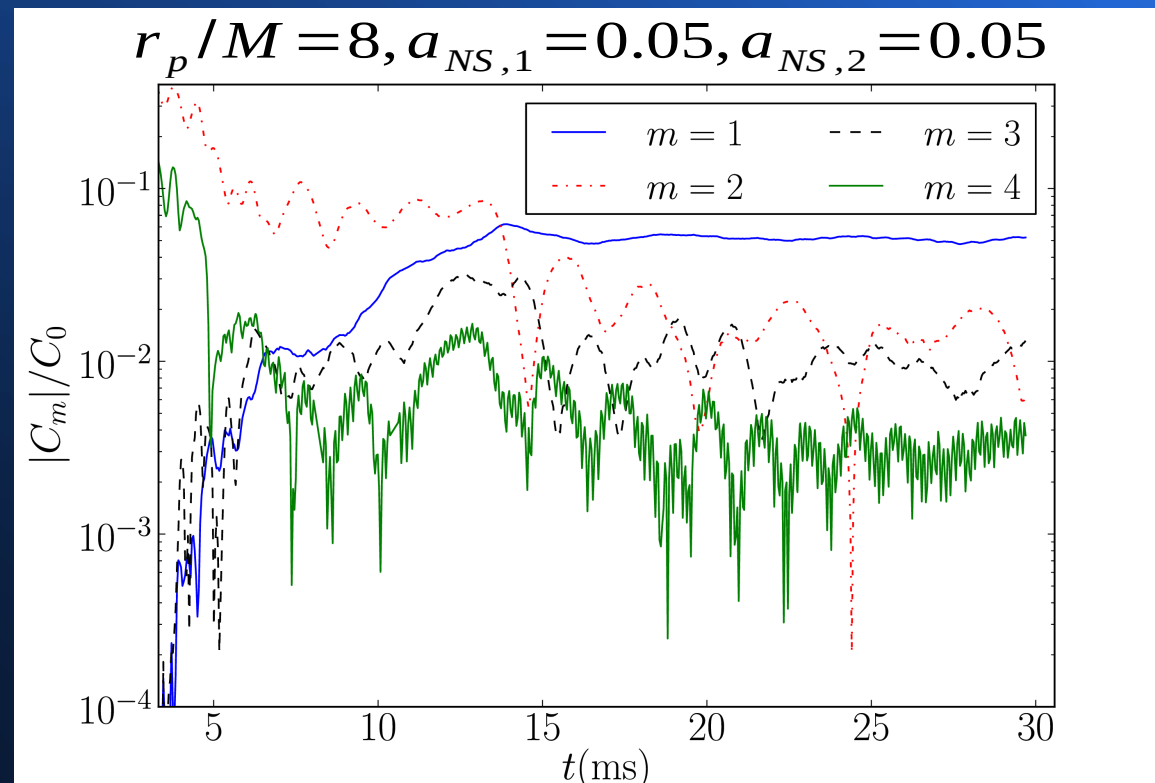
Eccentric NSNS mergers (azimuthal modes)

- Volume azimuthal mode decomposition of the rest-mass density in a center-of-mass frame

$$C_m = \int \rho e^{im\varphi} d^3x$$

- If axisymmetric $C_m = 0, m > 0$

Eccentric NSNS mergers (azimuthal modes)



Numerical relativity: equations

- Equations:

$$G_{\mu\nu} = 8\pi T_{\mu\nu}$$

→ Einstein

10, 2nd-order highly
Non-linear partial differential
equations (PDEs)

Numerical relativity: equations

- Equations:

$$G_{\mu\nu} = 8\pi T_{\mu\nu} \rightarrow \text{Einstein}$$

$$\nabla_{\alpha} (T^{\alpha\beta} + R^{\alpha\beta}) = 0$$

$$\nabla_{\alpha} R^{\alpha\beta} = -G^{\alpha\beta}$$

energy-momentum & radiation

8 PDEs

Numerical relativity: equations

- Equations:

$$G_{\mu\nu} = 8\pi T_{\mu\nu} \rightarrow \text{Einstein}$$

$$\nabla_{\alpha} (T^{\alpha\beta} + R^{\alpha\beta}) = 0$$

$$\nabla_{\alpha} R^{\alpha\beta} = -G^{\alpha\beta}$$

energy-momentum & radiation

$$\nabla_{\mu} F^{\mu\nu} = -J^{\nu}$$

$$\nabla_{\mu} {}^* F^{\mu\nu} = 0$$

Maxwell

8 PDEs

Numerical relativity: equations

- Equations:

$$G_{\mu\nu} = 8\pi T_{\mu\nu} \rightarrow \text{Einstein}$$

$$\nabla_{\alpha} (T^{\alpha\beta} + R^{\alpha\beta}) = 0$$

$$\nabla_{\alpha} R^{\alpha\beta} = -G^{\alpha\beta}$$

energy-momentum & radiation

$$\nabla_{\mu} F^{\mu\nu} = -J^{\nu}$$

$$\nabla_{\mu} {}^* F^{\mu\nu} = 0$$

Maxwell

$$\nabla_{\alpha} (\rho_0 u^{\alpha}) = 0$$

Baryon conservation

1 PDE

Numerical relativity: equations

- Equations:

$$G_{\mu\nu} = 8\pi T_{\mu\nu}$$

$$\nabla_{\alpha}(T^{\alpha\beta} + R^{\alpha\beta}) = 0$$

$$\nabla_{\alpha} R^{\alpha\beta} = -G^{\alpha\beta}$$

$$\nabla_{\mu} F^{\mu\nu} = -J^{\nu}$$

$$\nabla_{\mu} {}^* F^{\mu\nu} = 0$$

$$\nabla_{\alpha}(\rho_0 u^{\alpha}) = 0$$

Need to solve a total of > 27 coupled non-linear PDEs in 3+1 dimensions!

Numerical relativity: unique challenges

- Black hole singularities → blow ups both in MHD and gravity sectors
- Coordinates: meaningless, only gauge invariant quantities are meaningful
→ extracting physics not trivial

Single BH accretion \rightarrow jets!

- For ~ 15 years fixed-spacetime GRMHD accretion flows \rightarrow jets
- What is the problem with BH-NS?

Single BH accretion \rightarrow jets!

- For ~ 15 years fixed-spacetime GRMHD accretion flows \rightarrow jets
- What is the problem with BH-NS?
- Fixed-spacetime GRMHD accretion does NOT always launch jets

BH-NS mergers → jets?

- What is the problem?

THE ASTROPHYSICAL JOURNAL, 678:1180–1199, 2008 May 10
© 2008. The American Astronomical Society. All rights reserved. Printed in U.S.A.

THE INFLUENCE OF MAGNETIC FIELD GEOMETRY ON THE EVOLUTION OF BLACK HOLE ACCRETION FLOWS: SIMILAR DISKS, DRASTICALLY DIFFERENT JETS

KRIS BECKWITH AND JOHN F. HAWLEY

Astronomy Department, University of Virginia, P.O. Box 400325, Charlottesville, VA 22904-4325; krb3u@virginia.edu, jh8h@virginia.edu

AND

JULIAN H. KROLIK

Department of Physics and Astronomy, Johns Hopkins University, Baltimore, MD 21218; jhk@pha.jhu.edu

Received 2007 September 24; accepted 2008 January 10

BH-NS mergers → jets?

- What is the problem?

THE ASTROPHYSICAL JOURNAL, 678:1180–1199, 2008 May 10
© 2008. The American Astronomical Society. All rights reserved. Printed in U.S.A.

THE INFLUENCE OF MAGNETIC FIELD GEOMETRY ON THE EVOLUTION OF BLACK HOLE ACCRETION FLOWS: SIMILAR DISKS, DRASTICALLY DIFFERENT JETS

KRIS BECKWITH AND JOHN F. HAWLEY

Astronomy Department, University of Virginia, P.O. Box 400325, Charlottesville, VA 22904-4325; krb3u@virginia.edu, jh8h@virginia.edu

AND

JULIAN H. KROLIK

Department of Physics and Astronomy, Johns Hopkins University, Baltimore, MD 21218; jhk@pha.jhu.edu

Received 2007 September 24; accepted 2008 January 10

- Initially toroidal B-fields (confined in the disk) → no jets
- Accretion of a net poloidal magnetic flux is essential to support of strong jets

BH-NS mergers → jets?

- What is the problem?

THE ASTROPHYSICAL JOURNAL, 678:1180–1199, 2008 May 10
© 2008. The American Astronomical Society. All rights reserved. Printed in U.S.A.

THE INFLUENCE OF MAGNETIC FIELD GEOMETRY ON THE EVOLUTION OF BLACK HOLE ACCRETION FLOWS: SIMILAR DISKS, DRASTICALLY DIFFERENT JETS

KRIS BECKWITH AND JOHN F. HAWLEY

Astronomy Department, University of Virginia, P.O. Box 400325, Charlottesville, VA 22904-4325; krb3u@virginia.edu, jh8h@virginia.edu

AND

JULIAN H. KROLIK

Department of Physics and Astronomy, Johns Hopkins University, Baltimore, MD 21218; jhk@pha.jhu.edu

Received 2007 September 24; accepted 2008 January 10

- Initially toroidal B-fields (confined in the disk) → no jets
- Accretion of a net poloidal magnetic flux is essential to support of strong jets
- The conclusions apply to B-fields initially confined in the disk

BH-NS mergers \rightarrow jets?

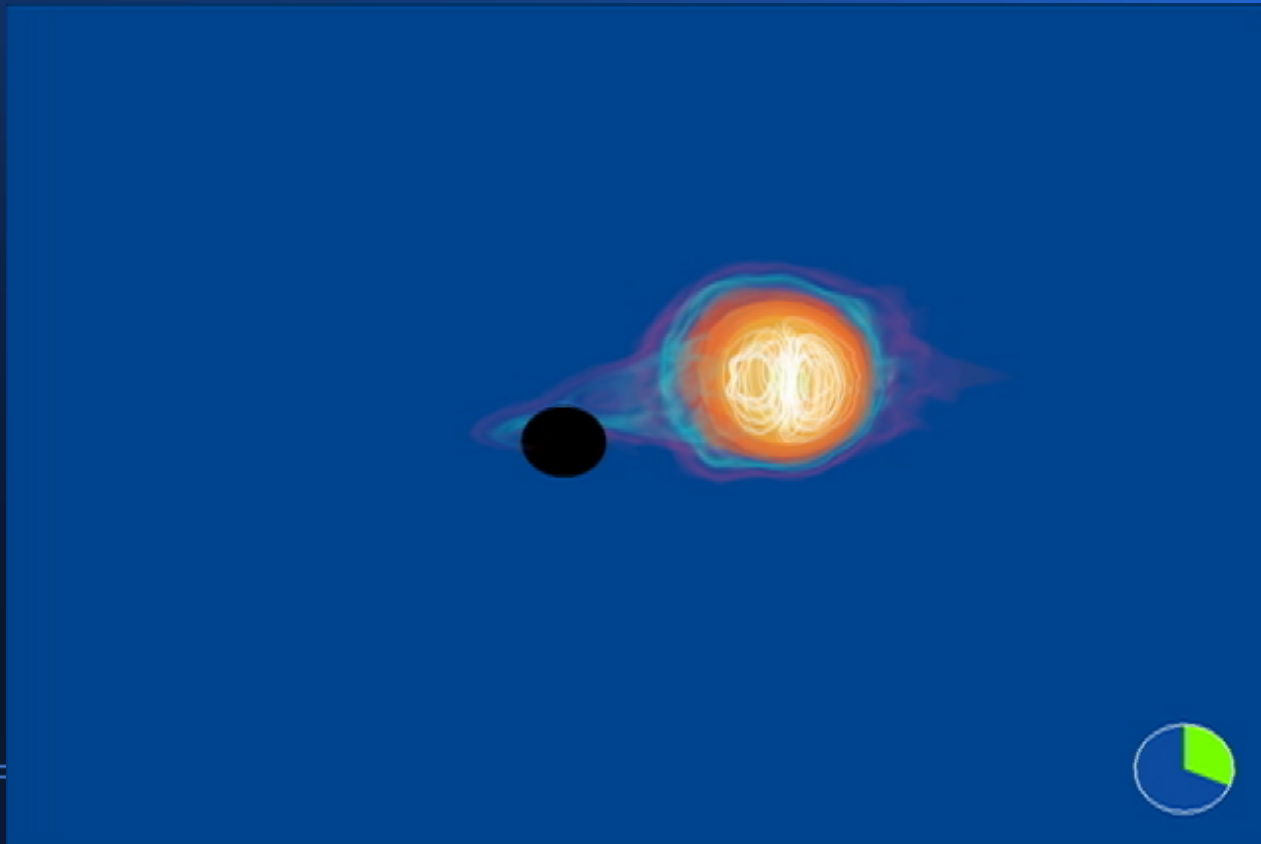
- How can we get a consistent, large scale, vertical field in a BH-NS merger, since the interior B-field inevitably becomes predominantly toroidal?
- What special initial B-field configuration prior to tidal disruption \rightarrow jets?

BH-NS mergers \rightarrow jets?

- How can we get a consistent, large scale, vertical field in a BH-NS merger, since the interior B-field inevitably becomes predominantly toroidal?
- What special initial B-field configuration prior to tidal disruption \rightarrow jets?
- Recall: pulsars suggest that NSs are likely endowed with dipole B-fields extending from the stellar interior out to the exterior.
- Could an initial dipole field give rise to conditions that favor jet formation?

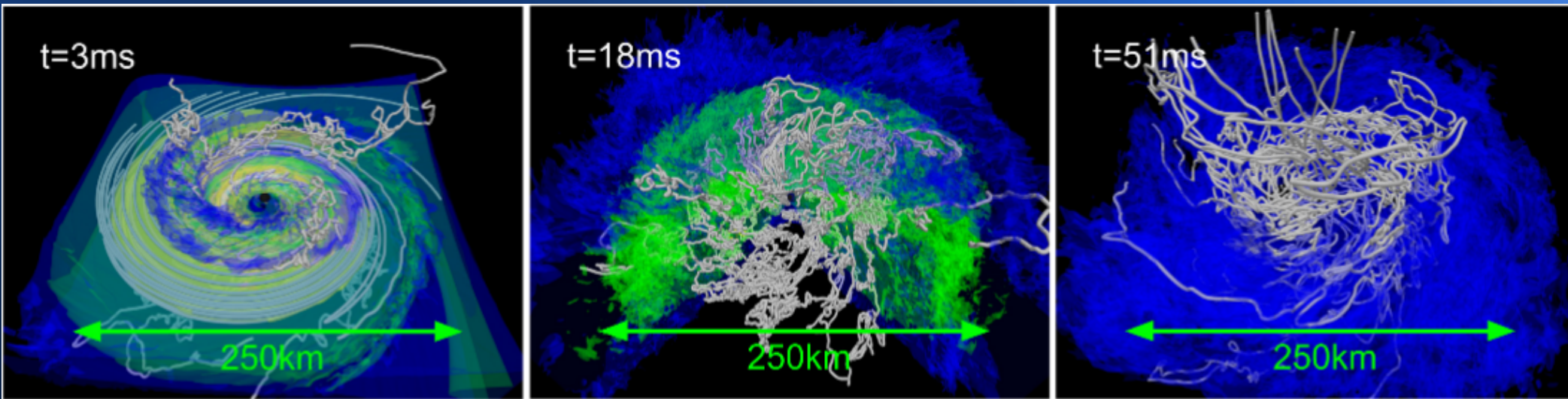
BH-NS mergers \rightarrow jets?

- A common result of all mag. BHNS simulations until Fall 2014 (Etienne, Liu, Paschalidis, Shapiro (2012), Etienne, Paschalidis, Shapiro (2013):



BH-NS mergers \rightarrow No jets?

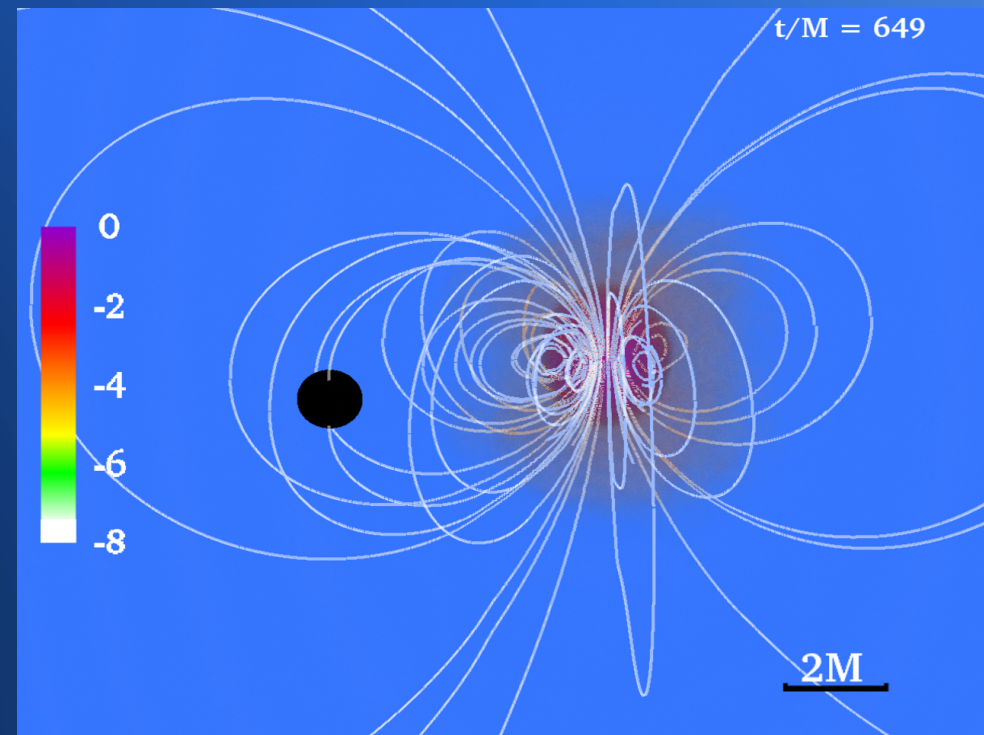
- Same outcome in recent very high resolution MHD simulations in full general relativity by Kiuchi et al 2015



BH-NS \rightarrow no jets!!!!?????????

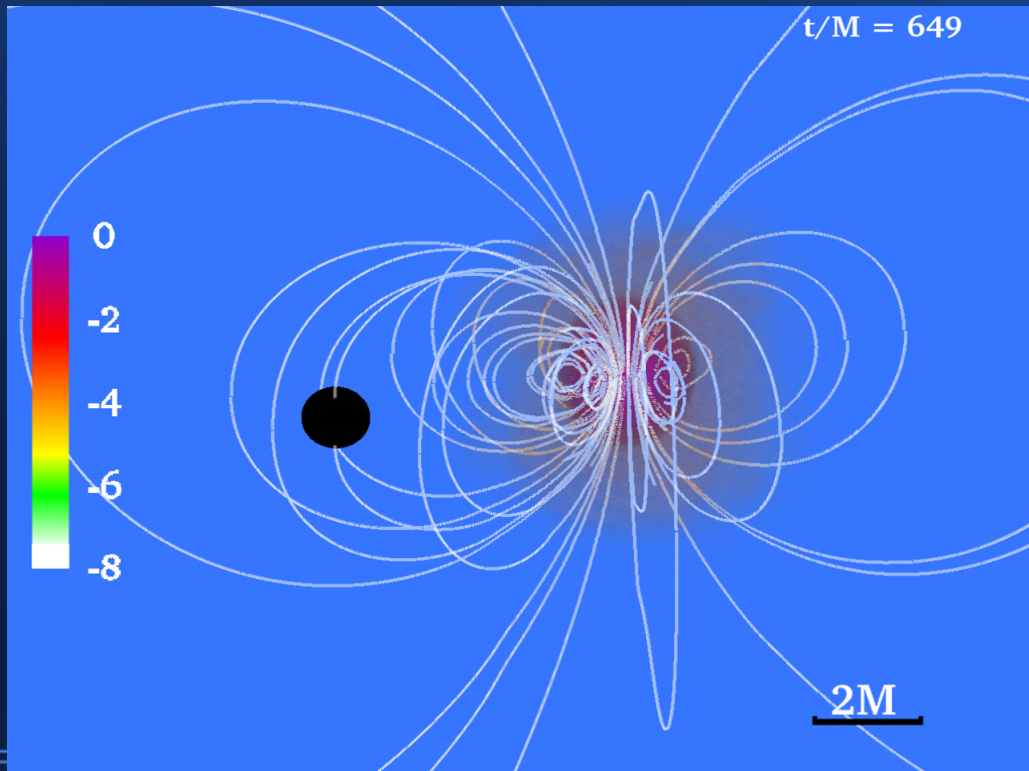
BH-NS mergers \rightarrow jets?

- Seed interior+exterior B-field
- Problem: How to evolve exterior force-free (B-field energy density dominated) with ideal MHD code?
- Solution: Mimic force-free exterior at $t=0$, by considering B-field pressure dominated



BH-NS mergers → jets?

- Perform simulations with a NS initially endowed with a dynamically weak dipolar magnetic field $P_{gas}/P_{mag} \geq 20$ (VP et al 2014)
- Metric and fluid initial data: $q=3:1$; $a/M=0.75$; $n=1$ polytropic NS



NS: expected to have a low-density force-free (B-energy-density-dominated) exterior magnetosphere.

Set initial exterior atmospheric rest-mass density such that

$$\beta = \frac{P_{gas}}{P_{mag}} = 0.1, 0.05, 0.01$$