



# Global properties of rotating neutron stars via matched QCD equations of state

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Tyler D. Gorda

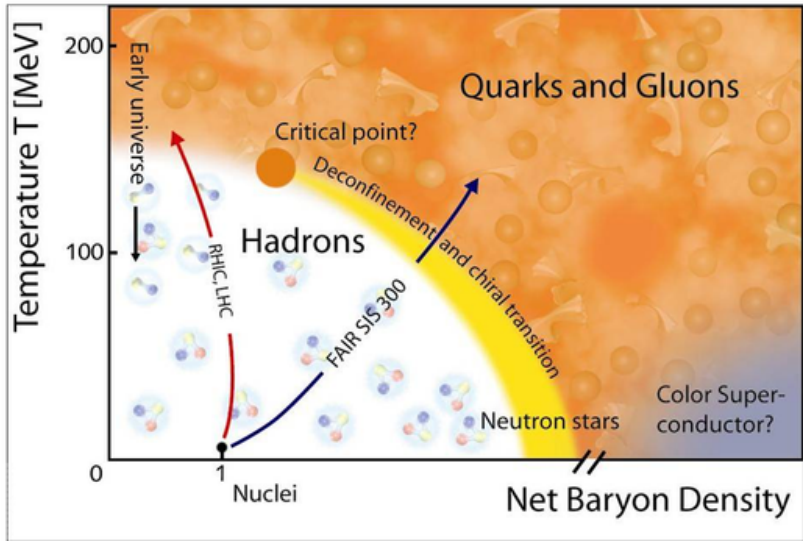
8 December 2016

University of Helsinki

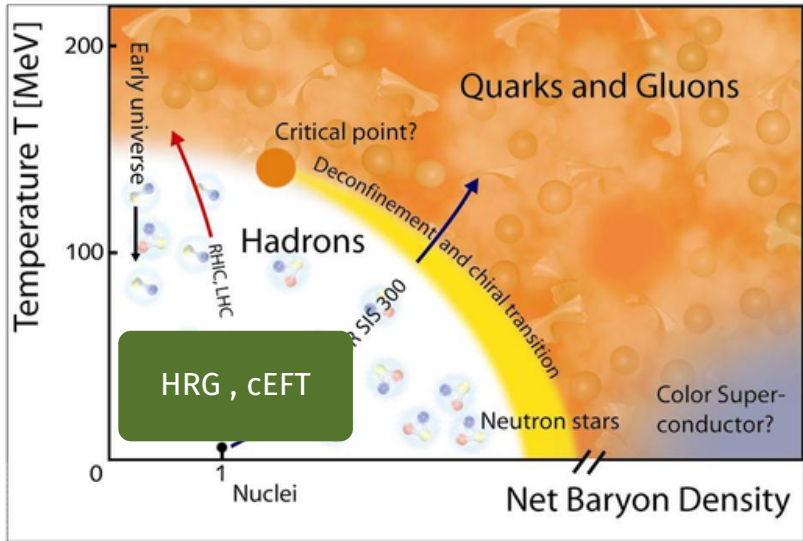
1. Matching: the idea
2. Kurkela et al. 2014 matched EOS band
3. Applications to rotating NSs

## Matching: the idea

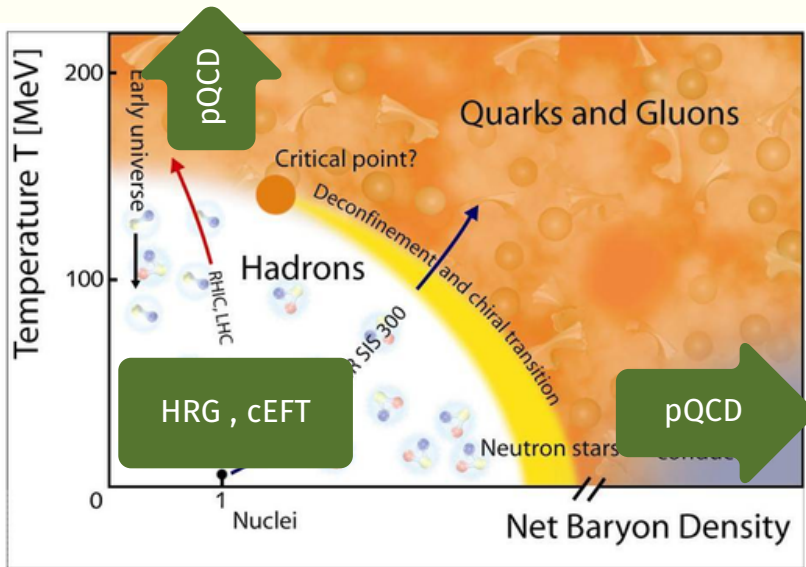
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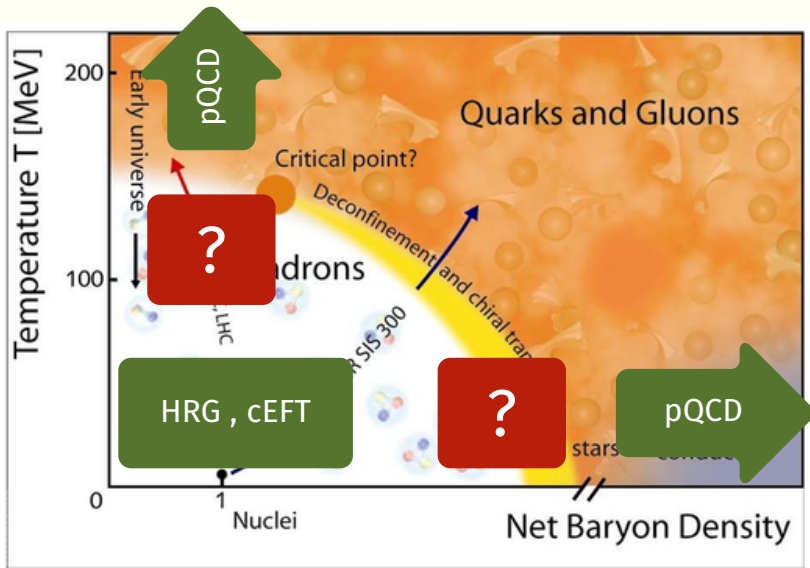
# QCD MATTER



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- Matching two (controlled) **perturbative** regimes can give us information about the complex, **nonperturbative** regime in between.



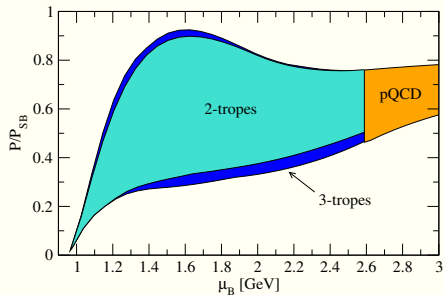
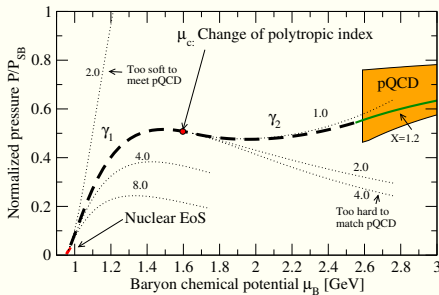
- Matching two (controlled) **perturbative** regimes can give us information about the complex, **nonperturbative** regime in between.
- This philosophy, applied to the QCD phase diagram at  $T = 0$  can shed light on NSs and their properties.

Kurkela et al. 2014 matched EOS  
band

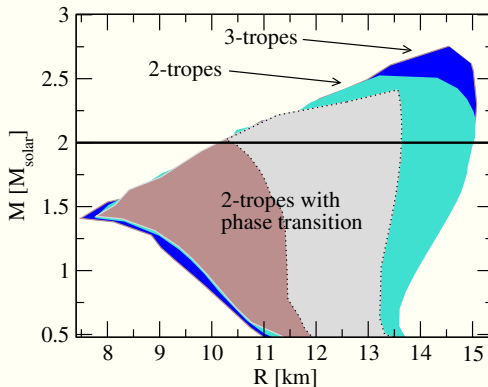
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- Kurkela et al. 2014 have matched **cEFT** (Tews et al. 2013) to **pQCD** (Fraga et al. 2014, Kurkela et al. 2010) with 2-3 interpolating polytropes:  $P(n) \propto n^\gamma$
- Thermodynamic consistency, subluminality, matching to pQCD, place stringent constraints on values of matching indices and locations.

- Solutions for  $\gamma_1 \in [2.23, 9.2]$ , and  $\gamma_2 \in [1.0, 1.5]$ , change in polytropic index at  $\mu^* \in [1.08, 2.05]$  GeV.



- Used EOS band to construct rotating NS. (With  $2M_{\odot}$  constraint.)



## Applications to rotating NSs

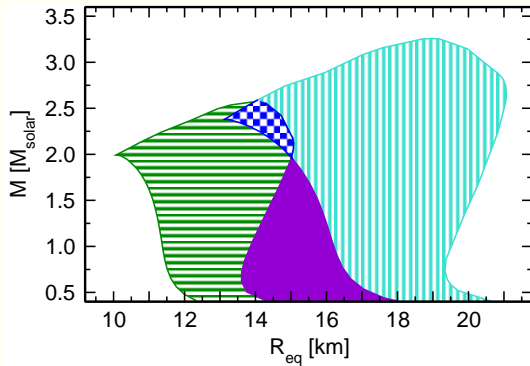
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- Used  $P(\epsilon)$  of Kurkela et al. 2014 with the publically-available RNS code to construct NSs with any  $\omega$  below the mass-shedding (Kepler) limit.
- Looked at various relations:
  - $M-R_e$
  - $M-f$
  - $R_e-f$  (for  $1.4M_\odot$  star)
  - $I-R_e$  (for the double pulsar PSR J0737-3039A)

# Plots

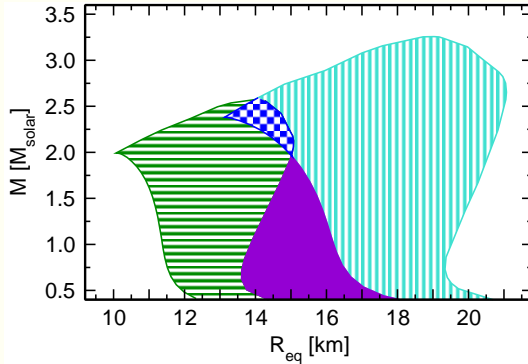


# MASS-EQUATORIAL RADIUS



Green region: nonrotating. Light blue region: mass shedding.

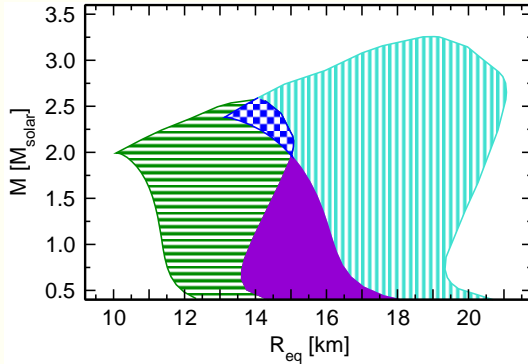
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Green region: nonrotating. Light blue region: mass shedding.

- Maximum nonrotating mass is  $2.5M_{\odot}$ ; rotating is  $3.25M_{\odot}$
- Maximum allowed radius is 21km.

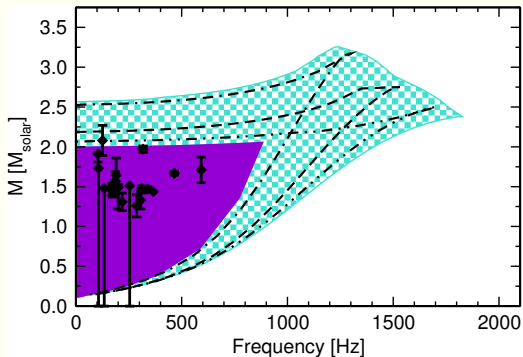
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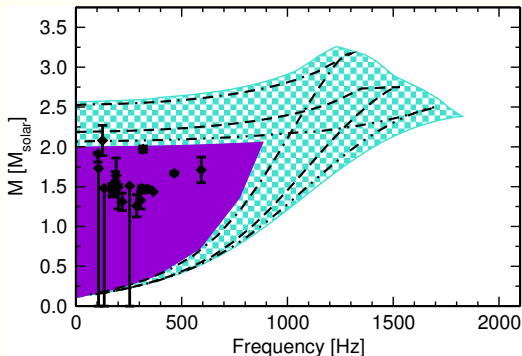
- Maximum nonrotating mass is  $2.5M_{\odot}$ ; rotating is  $3.25M_{\odot}$
- Maximum allowed radius is 21km.
- The same EOS forms the boundaries for both the rotating and nonrotating regions.

# MASS-FREQUENCY



**Purple region:** allowed for all EOSs. **L. blue region:** allowed for only some EOSs. **Dashed lines:** sample EOSs. **Data points:** NSs with  $f > 100$  Hz, from Haensel, Bejger, Fortin, and Zdunik, 2016.

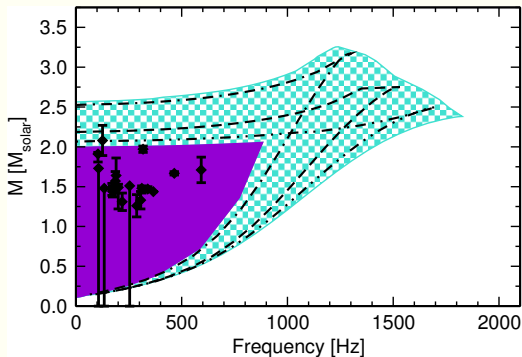
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- One star (B1516+02B) cuts slightly into the top band, though not really a rotation constraint.
- $f$  constraint: upper-right corner of purple region:  $f > 883$  Hz will start eliminating EOSs.

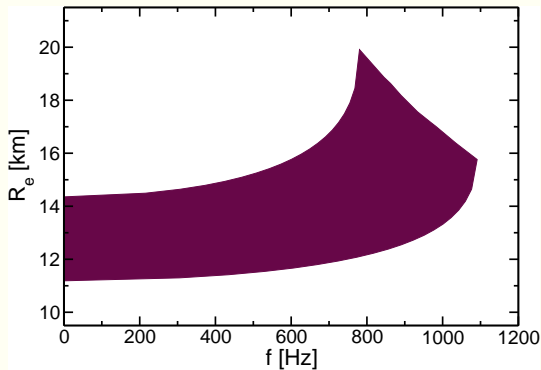
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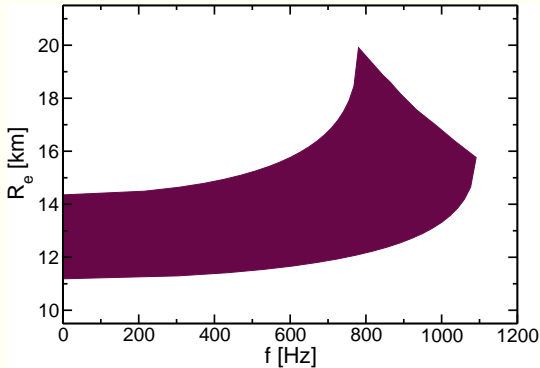
- One star (B1516+02B) cuts slightly into the top band, though not really a rotation constraint.
- $f$  constraint: upper-right corner of purple region:  $f > 883$  Hz will start eliminating EOSs.
- lower- $f$  NSs could also rule out EOSs if their masses were sufficiently low (e.g.,  $f = 716$  Hz starts constraining for  $M > 1M_{\odot}$ )

# EQUATORIAL RADIUS-FREQUENCY



Allowed region of  $R_e(f)$  curves for a  $1.4M_{\odot}$  star.

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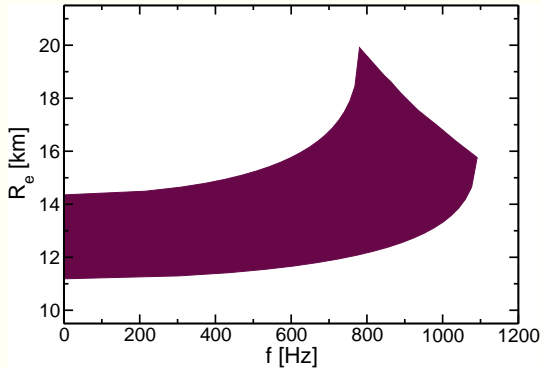


Allowed region of  $R_e(f)$  curves for a  $1.4M_\odot$  star.

- Largest  $f$  that all EOSs can support is  $f = 780\text{Hz}$ .
- Plot serves as a prediction for observational astronomers.



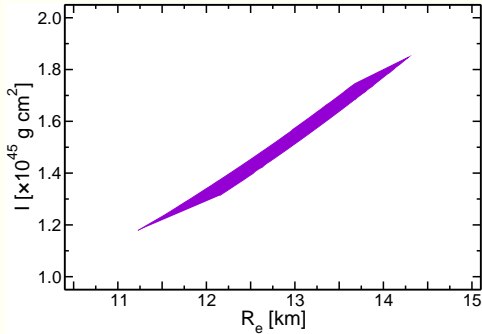
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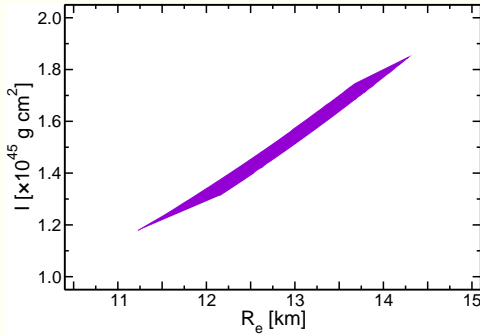
- Largest  $f$  that all EOSs can support is  $f = 780\text{Hz}$ .
- Plot serves as a prediction for observational astronomers.
- When consistent, reliable data of NS radii are available, plot could be overlaid with observational data to further constrain the QCD EOS.

# $I$ - $R_e$ FOR THE DOUBLE PULSAR PSR J0737-3039A



Allowed region of  $(I, R_e)$  points for PSR J0737-3039A.

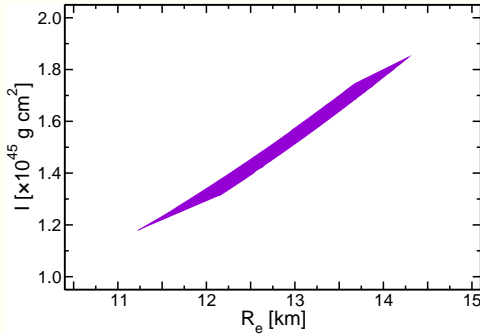
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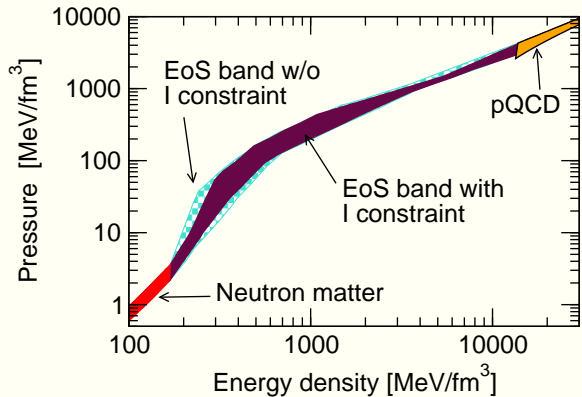


Allowed region of  $(I, R_e)$  points for PSR J0737-3039A.

- Strongly correlated: measuring  $I$  with 10% precision determines  $R_e$  to  $\pm 0.5$  km within this approach.
- All EOSs fall on “vertical” edges, so a measurement of  $I$ , even to low precision, would have large effect on EOS band.

e.g.  $I = (1.5 \pm 0.15) \times 10^{45} g \cdot cm^2$

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- Kurkela et al. 2014 matching can be applied to **rotating** NSs, and allows for other comparisons to observation:
  - **$M$ - $f$  regions** most directly connect to current observations and can lead to future EOS-constraint. (Future  $R_e$ - $f$  also?)
  - **Most stringent constraints** on EOS band would come from even a relatively imprecise measurement of  $I$  of the double pulsar PSR J0737-3039A.



Thank you!