

Rare decays

A biased view...

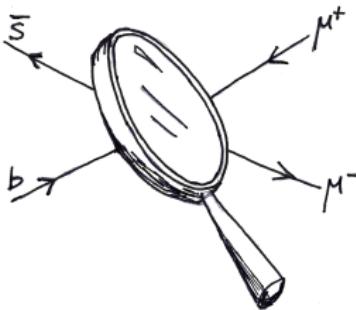
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University of Liverpool

29th Rencontres de Blois - May 28 - June 2, 2017
Blois, France

Why rare decays?

- Tiny effects in the SM \Rightarrow NP can be at the same level
- Virtual particles \Rightarrow High mass reach
- Precise predictions in SM
- Model independent searches
- Historically the laboratory of many particle physics discoveries



How are rare decays sensitive?

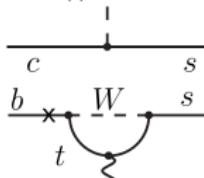
EFT, Wilson coefficients and other “boring” stuff

Complex interactions substituted with Fermi-like operators: couplings hide the high energy information



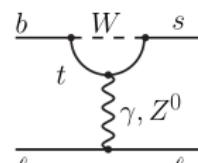
Charged current

$$G_F V_{cb} V_{cs}^* \textcolor{red}{C}_2 \bar{c}_L \gamma^\mu b_L \bar{s}_L \gamma_\mu c_L$$



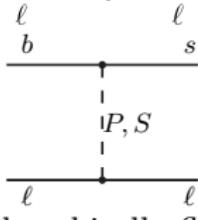
photon penguin

$$\frac{e}{4\pi^2} G_F V_{tb} V_{ts}^* m_b \textcolor{red}{C}_7 \bar{s}_L \sigma_{\mu\nu} b_R F^{\mu\nu}$$



EW penguin

$$G_F V_{tb} V_{ts}^* \textcolor{red}{C}_{9(10)} \bar{s}_L \gamma^\mu b_L \bar{\ell} \gamma_\mu (\gamma_5) \ell$$



NP (pseudo)-scalar

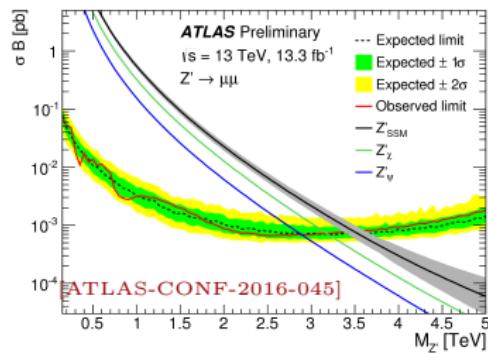
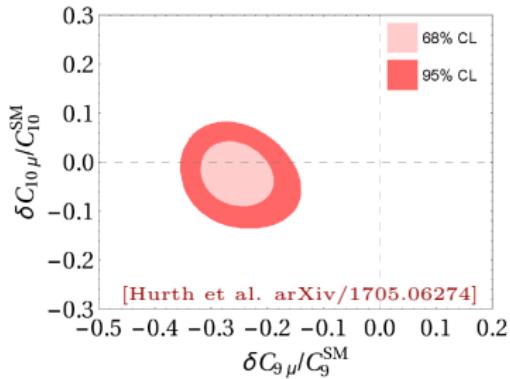
$$\propto \textcolor{red}{C}_{S(P)} \bar{s}_L b_L \bar{\ell} (\gamma_5) \ell$$

Plus chirally flipped operators...

How are rare decays sensitive?

EFT, Wilson coefficients and other “boring” stuff (2)

- New physics interactions can enter through new operators (S, P, \dots) or modifying the coefficients of SM operators
- If Wilson coefficients are thought of effective couplings with a NP scale (e.g. for C_9):
$$\sim G_F V_{tb} V_{ts}^* \frac{\alpha}{4\pi} C_9 = \frac{g^2}{\Lambda}$$
- Probing scales (masses!) up to hundreds of TeV (depending how large the coupling you allow to be)
- Not necessarily having the CKM flavour structure (MFV)



1. Branching fraction

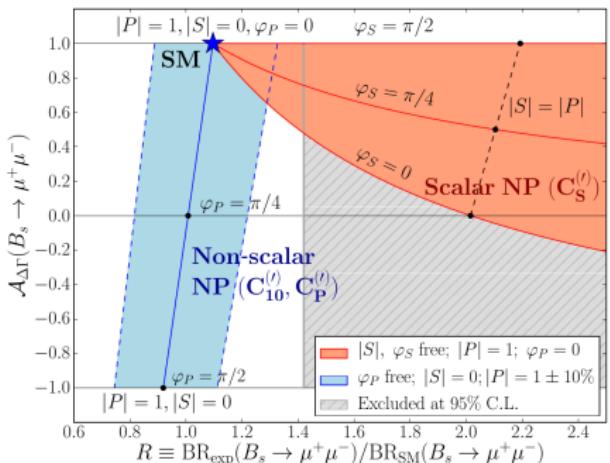
$$\mathcal{B}^{t=0}(B_s^0 \rightarrow \mu^+ \mu^-) = \frac{G_F^4 M_W^4}{\pi^2} \tau_{B_s^0} \textcolor{blue}{f}_{B_s}^2 m_{B_s}^3 \sqrt{1 - \frac{4m_\mu^2}{m_{B_s}^2}} |V_{tb} V_{ts}^*|^2 \left(|2 \frac{m_\mu}{m_{B_s}} (\textcolor{red}{C}_{10} - C'_{10}) + C_P - C'_P|^2 + |C_S - C'_S|^2 \right)$$

2. Ratio of branching fractions

$$\mathcal{R} = \frac{\mathcal{B}(B^0 \rightarrow \mu^+ \mu^-)}{\mathcal{B}(B_s^0 \rightarrow \mu^+ \mu^-)} = \frac{\tau_{B_d}}{\tau_{B_s}} \left(\frac{\textcolor{blue}{f}_{B_d}}{\textcolor{blue}{f}_{B_s}} \right)^2 \left| \frac{V_{td}}{V_{ts}} \right|^2 \frac{m_{B_d} \sqrt{1 - \frac{4m_\mu^2}{m_{B_d}^2}}}{m_{B_s} \sqrt{1 - \frac{4m_\mu^2}{m_{B_s}^2}}}$$

3. Effective lifetime

$$\tau_{\mu\mu} = \frac{\tau_{B_s}}{(1 - y_s^2)} \frac{1 + 2y_s \mathcal{A}_{\Delta\Gamma} + y_s^2}{1 + y_s \mathcal{A}_{\Delta\Gamma}}$$



Most recent predictions (time integrated)

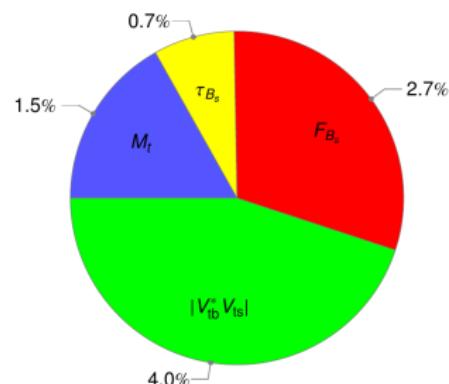
$$\mathcal{B}(B_s^0 \rightarrow \mu^+ \mu^-)^{\langle t \rangle} = (3.65 \pm 0.23) \cdot 10^{-9}$$

$$\mathcal{B}(B^0 \rightarrow \mu^+ \mu^-)^{\langle t \rangle} = (1.06 \pm 0.09) \cdot 10^{-10}$$

$$\mathcal{R} = 0.0287 \pm 0.0026$$

$$A_{\Delta\Gamma} = 1$$

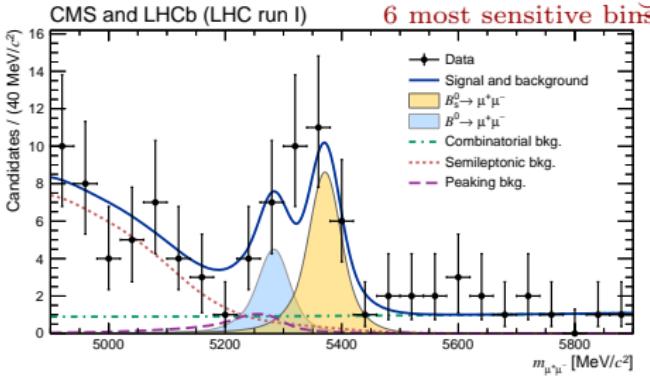
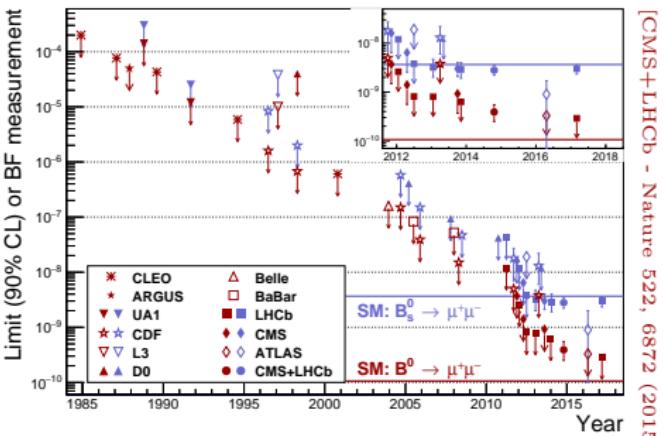
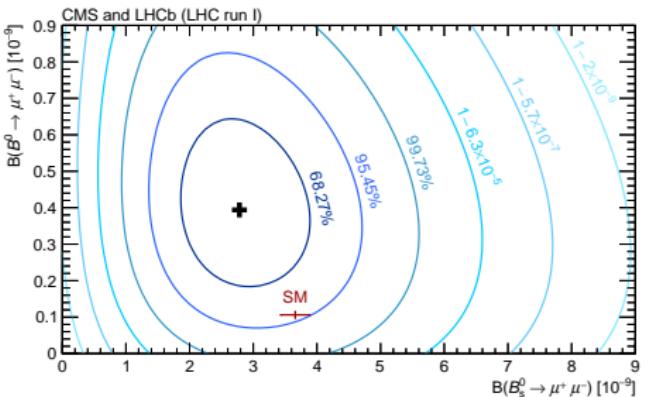
$$\mathcal{B}(B_s^0 \rightarrow \tau^+ \tau^-)^{\langle t \rangle} = (7.73 \pm 0.49) \times 10^{-7}$$



- Impressively precise predictions
- Any significant deviations from these values is sign of new interactions beyond the SM
- Main uncertainties are parametric, dominated by CKM matrix elements.

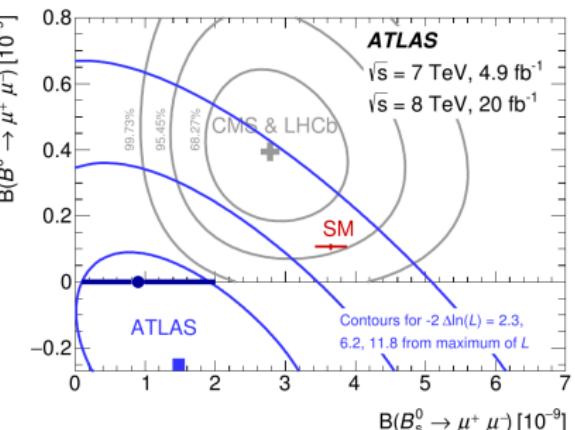
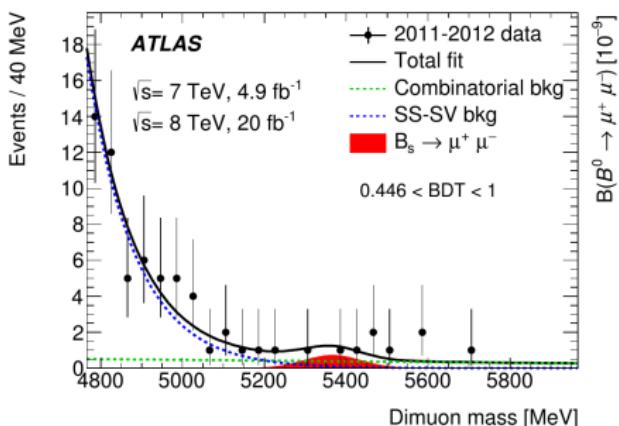
[Bobeth et al. PRL 112 (2014) 101801.] [Bobeth et al. PRD 89, 034023 (2014)] [Hermann et al. JHEP 1312 (2013) 097]

- 30 years search for $B_{d,s}^0 \rightarrow \mu^+ \mu^-$ decays
- First evidence in LHCb with 1 fb^{-1}
- Observation from CMS+LHCb combined analysis
- Good agreement with SM



$B_s^0 \rightarrow \mu^+ \mu^-$ in ATLAS

- 25 fb^{-1} of 7-8 TeV pp collisions
- Normalised to $B^+ \rightarrow J/\psi K^+$ events
- Search in three bins of a BDT operator



$$\mathcal{B}(B_s^0 \rightarrow \mu^+ \mu^-) = 0.9^{+1.1}_{-0.8} \times 10^{-9} \quad \mathcal{B}(B^0 \rightarrow \mu^+ \mu^-) < 4.2 \times 10^{-10} \text{ at } 95\% \text{ CL}$$

B_s^0 signal significance is 1.4σ

The 2D likelihood is compatible with SM at 2σ

Observation of $B_s^0 \rightarrow \mu^+ \mu^-$ at LHCb

And first measurement of the effective lifetime

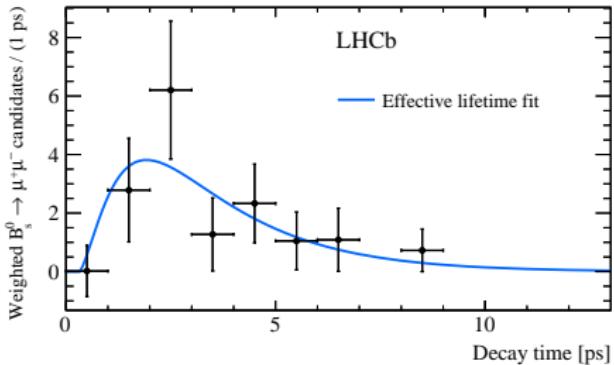
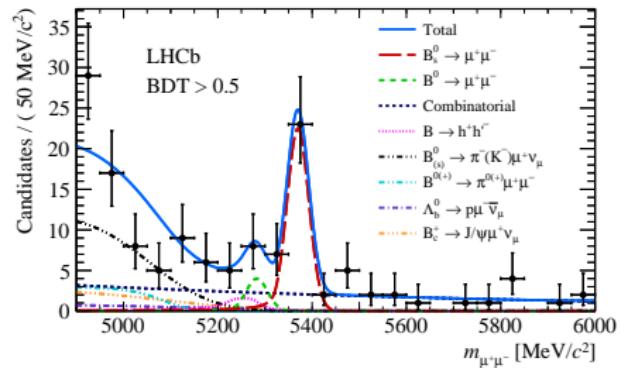
- 3fb^{-1} Run 1 + 2 fb^{-1} Run 2 data
- Re-optimized particle identification and multivariate operator

Results:

$$\begin{aligned}\mathcal{B}(B_s^0 \rightarrow \mu^+ \mu^-) &= (3.0 \pm 0.6^{+0.3}_{-0.2}) \times 10^{-9} \\ \mathcal{B}(B^0 \rightarrow \mu^+ \mu^-) &< 3.4 \times 10^{-10} (95\% \text{ CL})\end{aligned}$$

- First single-experiment observation of $B_s^0 \rightarrow \mu^+ \mu^-$ with 7.8σ
 - First measurement of effective lifetime
- $$\tau(B_s^0 \rightarrow \mu^+ \mu^-) = (2.04 \pm 0.44 \pm 0.05)\text{ps}$$

Compatible with $A_{\Delta\Gamma} = 1(-1)$ at the 1.0 (1.4) σ level



Search for $B_{(s)}^0 \rightarrow \tau^+\tau^-$ decays at LHCb

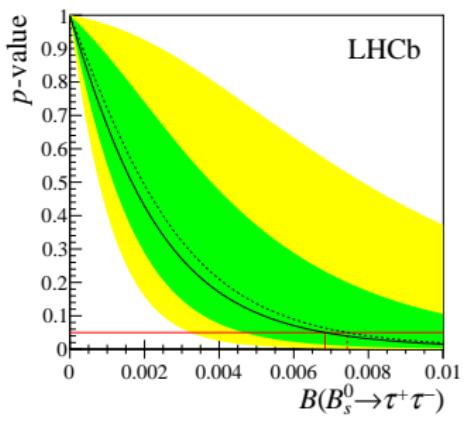
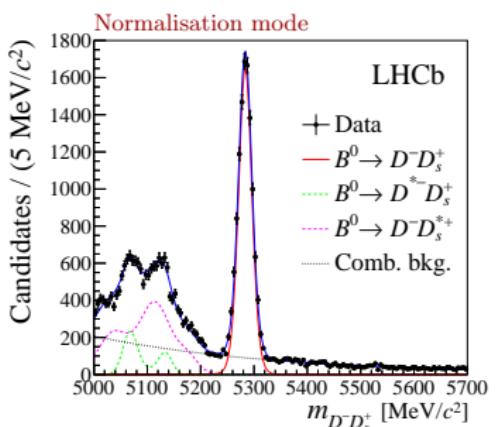
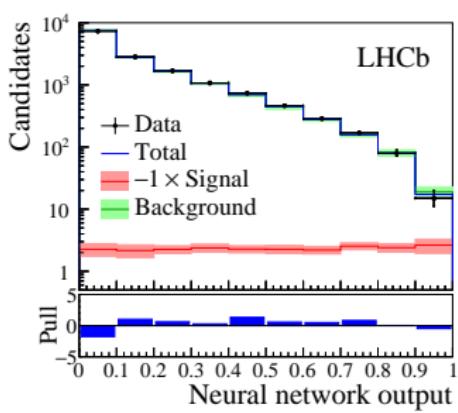
- Extremely difficult analyses
- Full Run 1 (3 fb^{-1})
- $\tau \rightarrow \pi\pi\pi\nu$ mode (10%)
- Search in NN output

Limits at 95% CL

$$\mathcal{B}(B_s^0 \rightarrow \tau^+\tau^-) < 6.8 \times 10^{-3}$$

$$\mathcal{B}(B_d^0 \rightarrow \tau^+\tau^-) < 2.1 \times 10^{-3}$$

First (B_s^0) and world best (B^0) limits
Still very far from SM

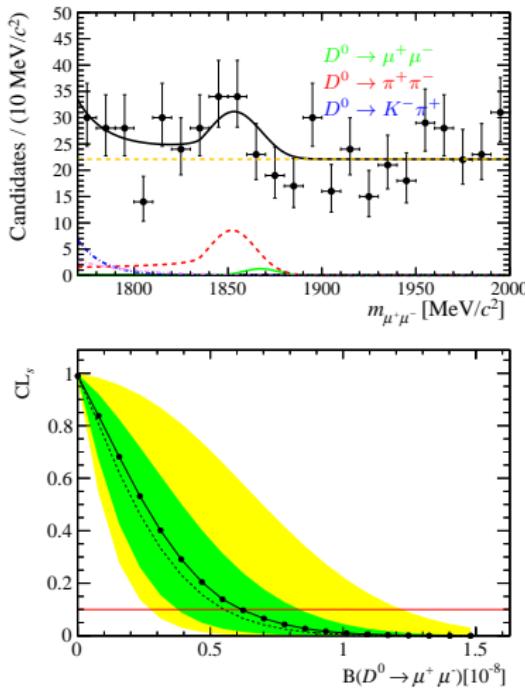


Search for $D^0 \rightarrow \mu^+ \mu^-$ at LHCb

- $D^0 \rightarrow \mu^+ \mu^-$ arises at tree levels in some leptoquarks model used for B decays: important complementary bounds! [Bauer et al. PRL116 (2016) no.14, 141802]
- $D^{*+} \rightarrow D^0(\rightarrow \mu^+ \mu^-)\pi^+$ search
- 0.9 fb^{-1} at 7 TeV

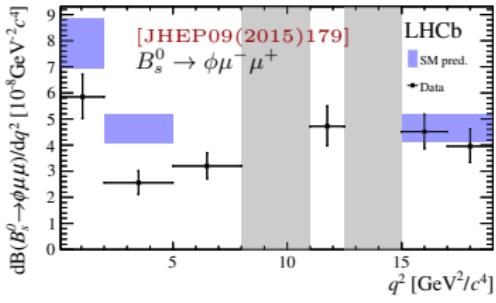
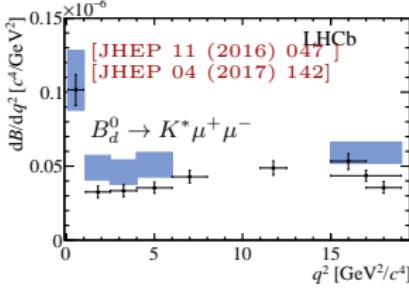
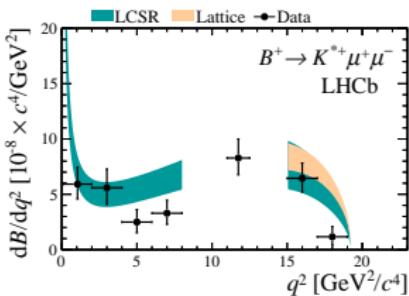
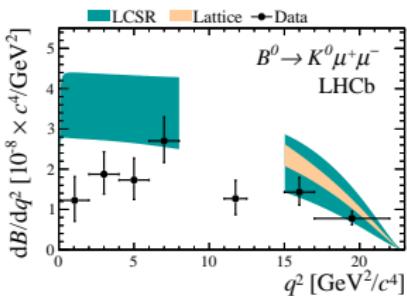
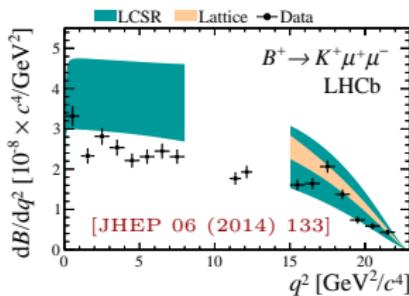
$$\mathcal{B}(D^0 \rightarrow \mu^+ \mu^-) < 7.6 \times 10^{-9}$$

- Similar complementary constraints from other rare charm decays



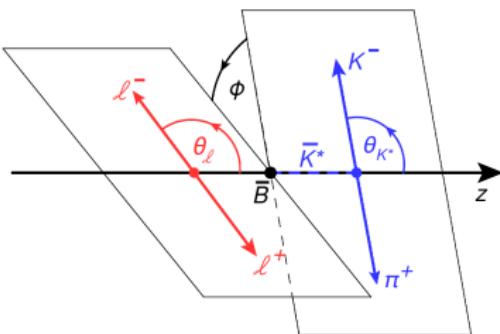
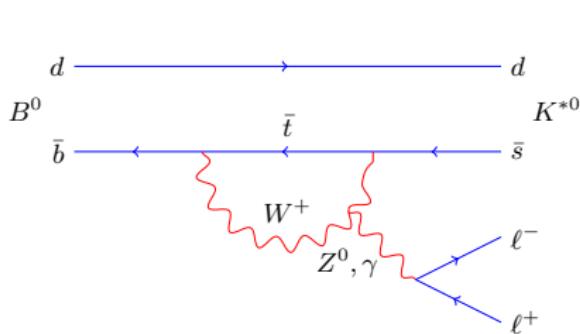
Branching fractions

- Measurements of various $b \rightarrow s$ transitions systematically below the SM:
- Might be all due to modification of C_9



Angular analysis of $B_d^0 \rightarrow K^* \ell^+ \ell^-$ decays

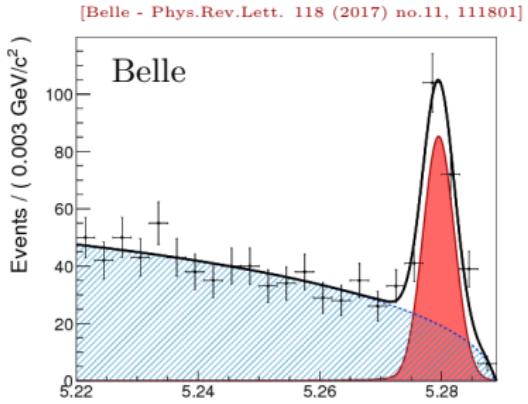
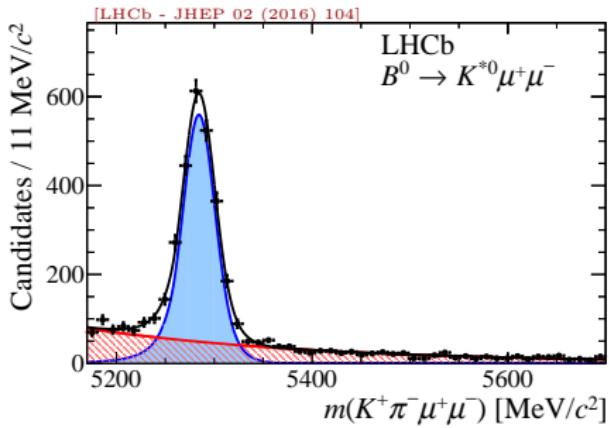
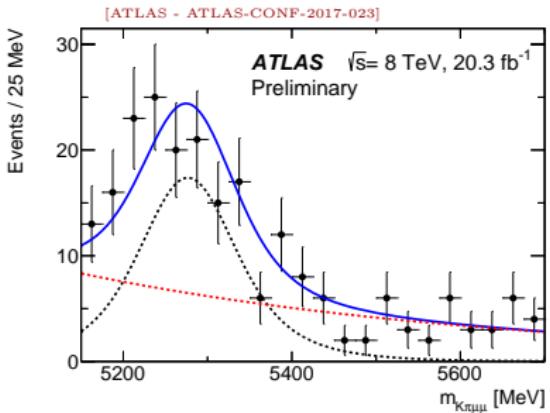
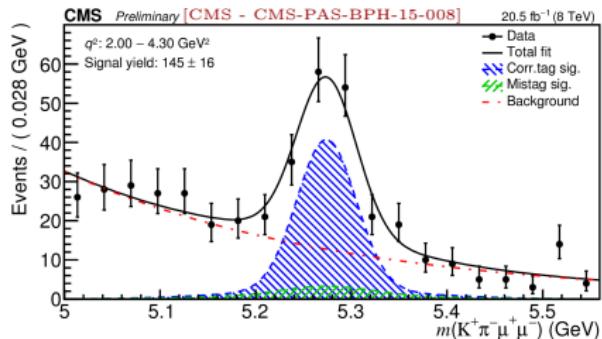
- $b \rightarrow s$ transition with vector in the final state
- Final state described by $q^2 = m_{\mu\mu}^2$ and three angles $\Omega = (\theta_\ell, \theta_K, \phi)$
- F_L, A_{FB}, S_i sensitive to $C_7^{(\prime)}, C_9^{(\prime)}, C_{10}^{(\prime)}$



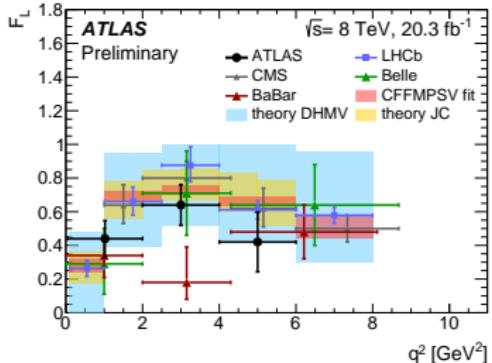
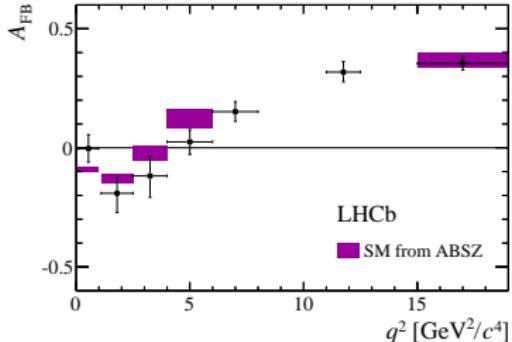
$$\frac{1}{d(\Gamma + \bar{\Gamma})/dq^2} \frac{d^3(\Gamma + \bar{\Gamma})}{d\vec{\Omega}} = \frac{9}{32\pi} \left[\frac{3}{4}(1 - F_L) \sin^2 \theta_K + F_L \cos^2 \theta_K + \frac{1}{4}(1 - F_L) \sin^2 \theta_K \cos 2\theta_\ell - F_L \cos^2 \theta_K \cos 2\theta_\ell + S_3 \sin^2 \theta_K \sin^2 \theta_\ell \cos 2\phi + S_4 \sin 2\theta_K \sin 2\theta_\ell \cos \phi + S_5 \sin 2\theta_K \sin \theta_\ell \cos \phi + \frac{4}{3} A_{FB} \sin^2 \theta_K \cos \theta_\ell + S_7 \sin 2\theta_K \sin \theta_\ell \sin \phi + S_8 \sin 2\theta_K \sin 2\theta_\ell \sin \phi + S_9 \sin^2 \theta_K \sin^2 \theta_\ell \sin 2\phi \right]$$

Angular analysis of $B_d^0 \rightarrow K^*\mu^+\mu^-$ decays

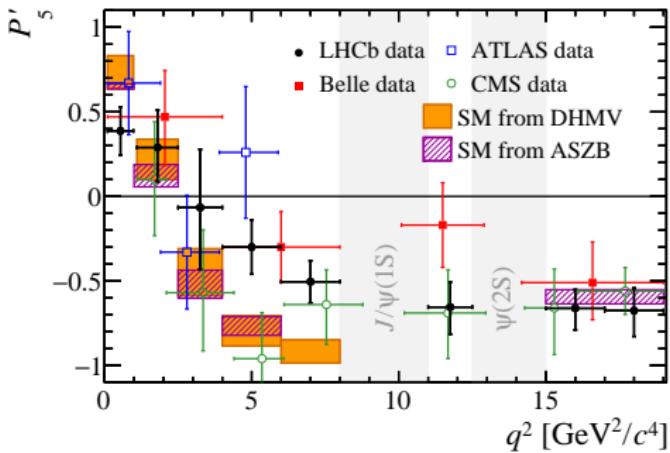
Many recent measurements



$B_d^0 \rightarrow K^* \mu^+ \mu^-$ results

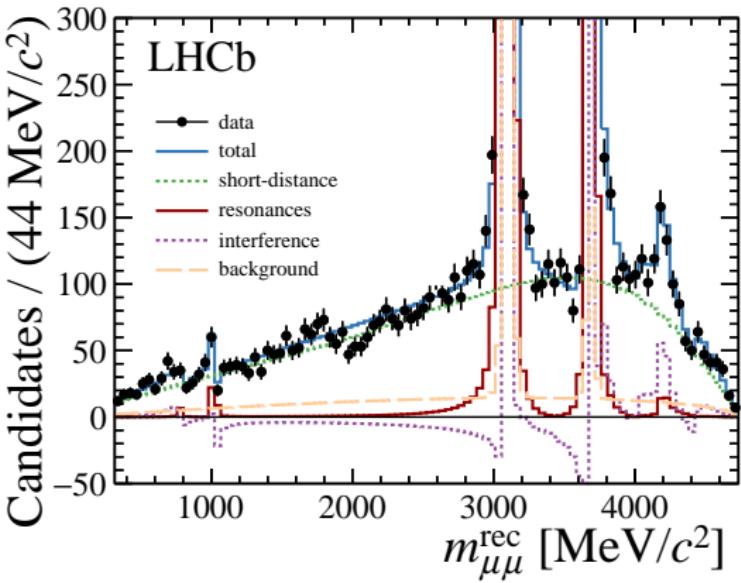
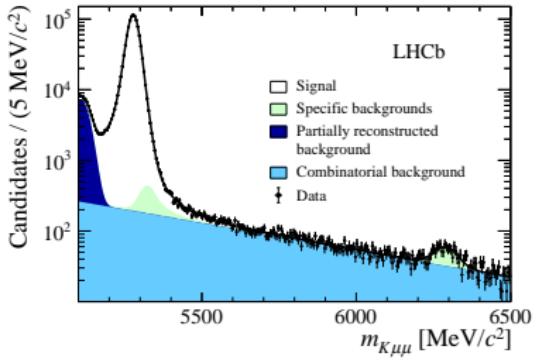


- Several observables appear different than SM
- In particular P'_5 has significant discrepancy
- Global fits show large disagreement



Phase space difference in $B^+ \rightarrow K^+ \mu^+ \mu^-$ decays

- Fit to full dimuon mass distribution
 - Resonances: ρ , ω , ϕ , J/ψ , $\psi(2S)$
 - Broad charmonium states: $\psi(3770)$, $\psi(4040)$, $\psi(4160)$, $\psi(4415)$,
- Four-fold ambiguity in J/ψ and $\psi(2S)$ phase signs:
Compatible with $\pi/2$, hence low interference with non-resonant



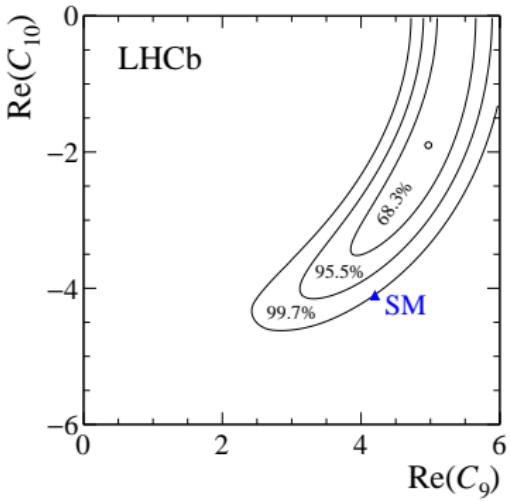
$$\frac{d\Gamma}{dq^2} = \frac{G_F^2 \alpha^2 |V_{tb} V_{ts}^*|^2}{128\pi^5} |\mathbf{k}| \beta \left\{ \frac{2}{3} |\mathbf{k}|^2 \beta^2 \left| \mathcal{C}_{10} f_+(q^2) \right|^2 + \frac{4m_\mu^2 (m_B^2 - m_K^2)^2}{q^2 m_B^2} \left| \mathcal{C}_{10} f_0(q^2) \right|^2 \right. \\ \left. + |\mathbf{k}|^2 \left[1 - \frac{1}{3} \beta^2 \right] \left| \mathcal{C}_9 f_+(q^2) + 2\mathcal{C}_7 \frac{m_b + m_s}{m_B + m_K} f_T(q^2) \right|^2 \right\},$$

[Bailey et al. Phys. Rev. D 93, 025026 (2016)]

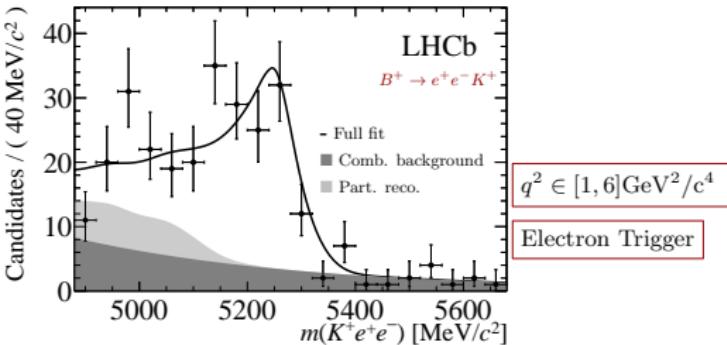
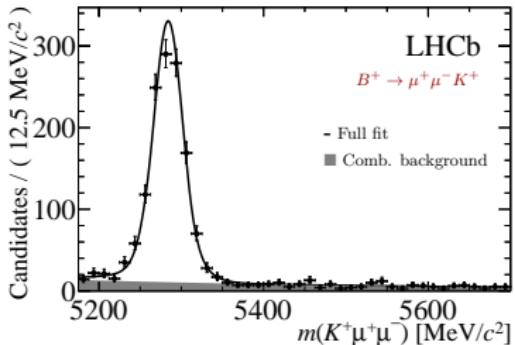
- Fit to Wilson coefficients
- Non resonant sensitive to C_9 and C_{10}
- Deviation of 3.0σ from SM
- Low $B^+ \rightarrow K^+\mu^+\mu^-$ BR not explained by resonance interferences

$$\mathcal{B}(B^+ \rightarrow K^+\mu^+\mu^-) = (4.37 \pm 0.15 \pm 0.23) \times 10^{-7}$$

in agreement with previous measurement



Test of lepton universality using $B^+ \rightarrow K^+ \ell^+ \ell^-$ decays



The combination of the various trigger channels gives:

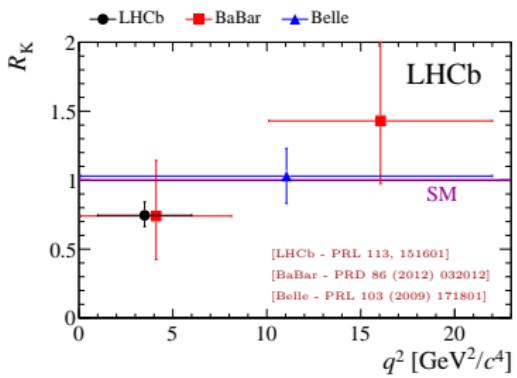
$$R_K = 0.745^{+0.090}_{-0.074}(\text{stat}) \pm 0.036(\text{syst})$$

Most precise measurement to date,
compatible with SM at 2.6σ level

The branching fraction of $B^+ \rightarrow e^+ e^- K^+$
is measured as

$$\mathcal{B}(B^+ \rightarrow e^+ e^- K^+) = 1.56^{+0.19}_{-0.15}(\text{stat})^{+0.06}_{-0.05}(\text{syst}) \times 10^{-7}$$

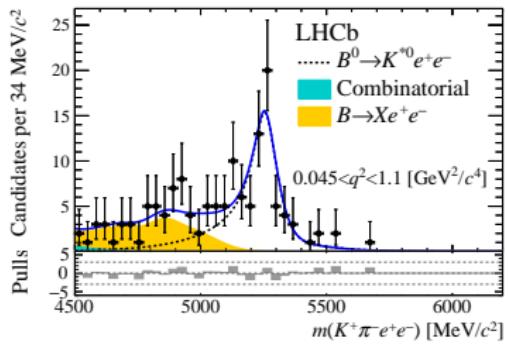
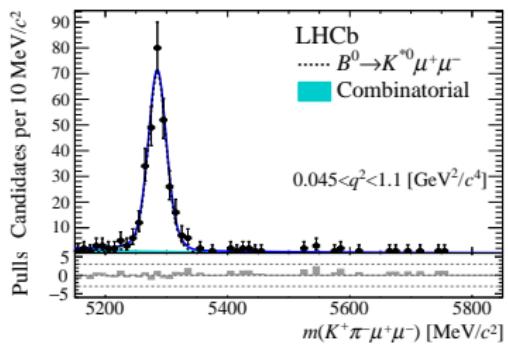
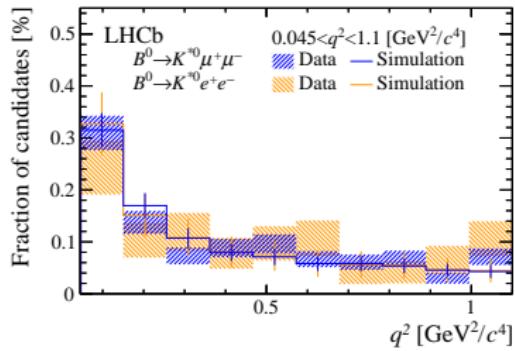
well compatible with SM predictions



Lepton Universality Test in $B_d^0 \rightarrow K^* \ell^+ \ell^-$

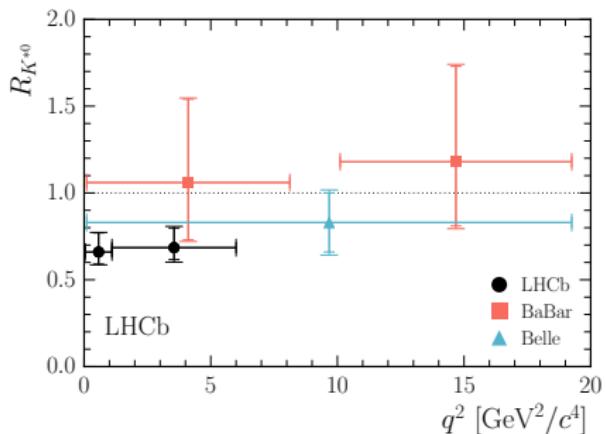
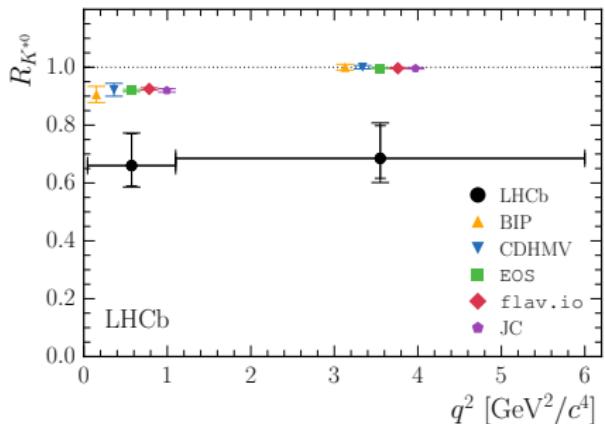
$$R_{K^*} = \frac{\mathcal{B}(B_d^0 \rightarrow K^* \mu^+ \mu^-)}{\mathcal{B}(B^+ \rightarrow J/\psi(\rightarrow \mu^+ \mu^-) K^{*+})} / \frac{\mathcal{B}(B_d^0 \rightarrow K^* e^+ e^-)}{\mathcal{B}(B^+ \rightarrow J/\psi(\rightarrow e^+ e^-) K^{*+})}$$

- Very clean theoretical predictions
- Double ratio to cancel systematics
- Two q^2 bins and three independent triggers
- Excluded low q^2 region (dominated by photons)



Lepton Universality Test in $B_d^0 \rightarrow K^* \ell^+ \ell^-$

$$R_{K^*} = \begin{cases} 0.66^{+0.11}_{-0.07} \text{ (stat)} \pm 0.03 \text{ (syst)} & \text{for } 0.045 < q^2 < 1.1 \text{ GeV}^2/c^4 \\ 0.69^{+0.11}_{-0.07} \text{ (stat)} \pm 0.05 \text{ (syst)} & \text{for } 1.1 < q^2 < 6.0 \text{ GeV}^2/c^4 \end{cases}$$



- Statistically dominated
- SM compatibility: $[2.1 - 2.3]\sigma$ and $[2.4 - 2.5]\sigma$ for the two bins respectively

Summary of B anomalies

Are we there yet?

1. Low $b \rightarrow s\mu\mu$ branching fractions
 2. Discrepancies in angular observables of $B_d^0 \rightarrow K^*\mu^+\mu^-$
 3. Signs of lepton non-universality in: $B^+ \rightarrow K^+\mu^+\mu^-$ and $B_d^0 \rightarrow K^*\mu^+\mu^-$
- All seems to be related to a change in the C_9 coefficient (or maybe C_9 and C_{10} , but V-A)
 - Global fits start to exhibit several standard deviations of discrepancy
 - $c\bar{c}$ interference explanation seems not justified
 - Additional discrepancies in tree-level $B \rightarrow D^{(*)}\ell\nu$ decays (See Victor Renaudin's talk)
 - Many NP explanations: Z' , leptoquarks, low mass resonances etc

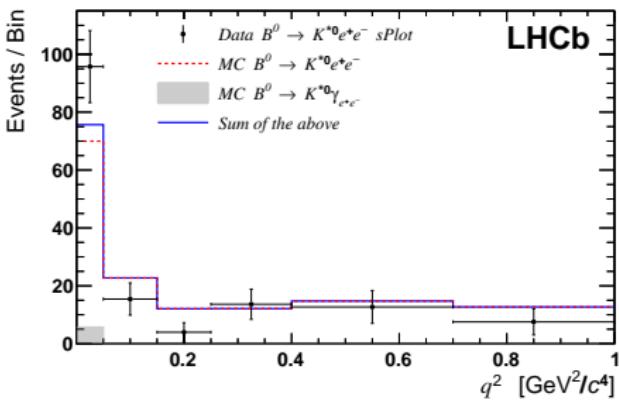
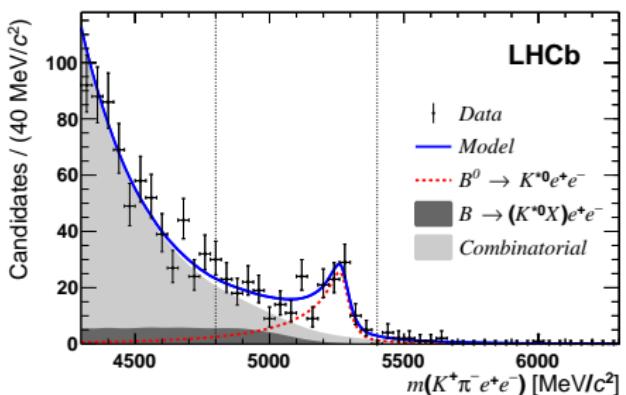
See following talk by Joaquim Matias!

- Rare heavy flavour decays are a great laboratory to test the SM: precise predictions and clean experimental observables
- Model independent sensitivity to NP:
 - ★ New (pseudo)-scalar interactions tightly constrained by $B_s^0 \rightarrow \mu^+ \mu^-$ decays
 - ★ Possible new vector (or V-A) interactions seem to explain several B anomalies
- Variety of complementary observables
- For some decays: healthy competition between 4 experiments!
- Vibrant field: many new results will come soon to confirm or disprove this tantalising results!

Backup

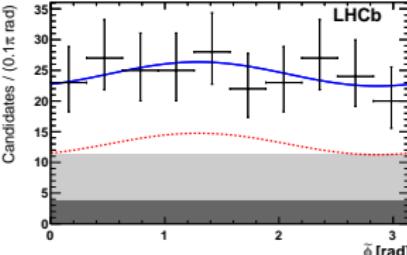
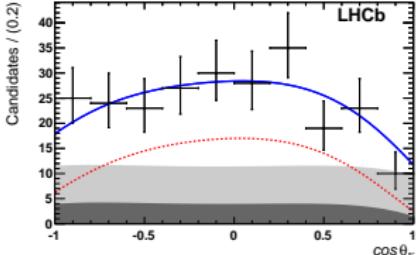
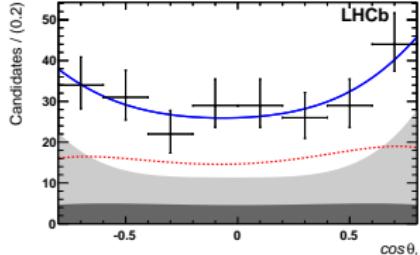
Angular analysis of $B_d^0 \rightarrow K^* e^+ e^-$ decays

- Angular analysis of $B_d^0 \rightarrow K^* e^+ e^-$ at very low q^2 ($\in [0.002, 1.120] \text{GeV}^2/c^4$)
- Folded angular observables ($\phi = \phi + \pi$ if $\phi < 0$)
- Measurement of F_L , $A_T^{(2)}$, $A_T^{(\text{Im})}$, $A_T^{(\text{Re})}$, * sensitive to C'_7 as $q^2 \rightarrow 0$



$$* A_T^{(\text{Re})} = \frac{4}{3} A_{FB}/(1 - F_L), A_T^{(2)} = \frac{1}{2} S_3/(1 - F_L) \text{ and } A_T = \frac{1}{2} S_9/(1 - F_L)$$

Angular analysis of $B_d^0 \rightarrow K^* e^+ e^-$ decays



- † Data
- Model
- $B^0 \rightarrow K^{*0} e^+ e^-$
- $B \rightarrow (K^{*0} X) e^+ e^-$
- Combinatorial

Observable	Measurement	SM prediction [†]
F_L	$+0.16 \pm 0.06 \pm 0.03$	$+0.10^{+0.11}_{-0.05}$
$A_T^{(2)}$	$-0.23 \pm 0.23 \pm 0.05$	$0.03^{+0.05}_{-0.04}$
A_T^{Re}	$+0.10 \pm 0.18 \pm 0.05$	$-0.15^{+0.04}_{-0.03}$
A_T^{Im}	$+0.14 \pm 0.22 \pm 0.05$	$(-0.2^{+1.2}_{-1.2}) \times 10^{-4}$

- Measurements well in agreement with SM predictions
- Constraints on $C_7^{(\prime)}$ competitive with radiative decays

[†]S. Jäger, J. M. Camalich [[arXiv/1412.3283](https://arxiv.org/abs/1412.3283)]

Search for $K_S^0 \rightarrow \mu^+ \mu^-$ decays at LHCb

- NP can be orders of magnitude the SM
- Full Run 1 statistics
- Normalisation and main background:
 $K_S^0 \rightarrow \pi^+ \pi^-$
- $\mathcal{B}(K_S^0 \rightarrow \mu^+ \mu^-) < 1.0 \times 10^{-9}$ at 95% CL

