#### **Measurement of W-boson Mass in ATLAS**

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JG



- Motivation for W mass measurement
- Measurement Strategy

Method: Monte Carlo Templates Fits

- Event Selection and Calibration ATLAS 7TeV datasets in 2011
- Physics Modelling
- Measured Results arXiv:1701.07240



## Motivation

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- W boson mass is fundamental parameter of the Standard Model which is particularly sensitive to top and Higgs bosons' masses
- The measurement of the W boson mass provides a consistency test of the Standard Model and a probe of Beyond Standard Model physics
- The Standard Model prediction (arXiv:1608.01509): 80.360±0.008 GeV
   The world average experimental measurement: 80.385±0.015 GeV
   Improvement of W mass measurement allows to challenge the SM prediction

## **Measurement Strategy**



- \* Create Monte Carlo templates with different W mass values by re-weighting. Then perform Monte Carlo template fit to data with  $\chi^2$  minimisation to extract mass in data.
- Sensitive final state distributions: pT<sup>I</sup>, mT, pT<sup>miss</sup> are tested. (pT<sup>miss</sup> is only used as a cross check)

## **Measurement Strategy**



- Fits performed in categories to enhance the fit sensitivity
  - \* electron / muon decays (different detector effect)
  - \*  $p_T^I$  fit /  $m_T$  fit (different detector effect)
  - \* positive / negative lepton charges (different impact of physics modelling uncertainties)
  - different lepton pseudorapidity |η| ranges (different impact of physics modelling uncertainties)
- A blinding offset of W mass was applied throughout the measurement and removed when consistent results were found.

## **Event Selection**

- ATLAS 7TeV datasets in 2011
- Electron channel selection
  - |η| < 2.4</li>
     (exclude 1.2 < |η| < 1.82</li>
     due to large amount of passive material)
  - \* p<sub>T</sub> > 30 GeV
  - \* isolation requirements
  - 5.89×10<sup>6</sup> W-boson candidates,
     0.58×10<sup>6</sup> Z boson candidates
  - \* 4.6 fb<sup>-1</sup> of integrated luminosity
- Muon channel selection
  - \* |η| < 2.4 and p<sub>T</sub> > 30 GeV
  - isolation requirements
  - \* 7.84×10<sup>6</sup> W-boson candidates, 1.23×10<sup>6</sup> Z boson candidates
  - \* 4.1 fb<sup>-1</sup> of integrated luminosity (some data discarded due to a timing problem in the resistive plate chambers)
- Recoil
  - Vector sum of the transverse energy of all clusters measured in the calorimeters (range |η| < 4.9)</li>
  - \* u<sub>T</sub><30 GeV, m<sub>T</sub>>60 GeV



## **Detector Calibration - Leptons**

- Calibration of detector response to electrons and muons by using Z boson decays
  - momentum / energy scale and resolution
  - selection efficiencies
- Momentum calibration by using the Z peak



## **Detector Calibration - Recoil**

- Calibration of recoil
  - event activity correction
  - recoil response calibration
     using expected p<sub>T</sub> balance between lepton pairs and u<sub>T</sub> in Z boson decay events
- Recoil correction steps:
  - Equalise pile-up multiplicity distribution in data and MC (done directly in W events)
  - Correct for residual difference in the ΣE<sub>T</sub> distribution (done directly in W events) removes u<sub>T</sub> resolution discrepancy due to imperfect event activity mis-modelling
  - \* Residual corrections using  $p_T$  balance in Z events, mapped vs  $p_T^v$  and  $\Sigma E_T$ (done in Z events, uncertainties from Z statistics and Z to W extrapolation)





#### **Detector Calibration - Recoil**



| W-boson charge   | И                       | 7+               | И                       | 7-               | Com                     | bined            |
|--|-------------------------|------------------|-------------------------|------------------|-------------------------|------------------|
| Kinematic distribution                                 | $p_{\mathrm{T}}^{\ell}$ | $m_{\mathrm{T}}$ | $p_{\mathrm{T}}^{\ell}$ | $m_{\mathrm{T}}$ | $p_{\mathrm{T}}^{\ell}$ | $m_{\mathrm{T}}$ |
| $\delta m_W  [{ m MeV}]$                               |                         |                  |                         |                  |                         |                  |
| $\langle \mu \rangle$ scale factor                     | 0.2                     | 1.0              | 0.2                     | 1.0              | 0.2                     | 1.0              |
| $\Sigma \bar{E_{\mathrm{T}}}$ correction               | 0.9                     | 12.2             | 1.1                     | 10.2             | 1.0                     | 11.2             |
| Residual corrections (statistics)                      | 2.0                     | 2.7              | 2.0                     | 2.7              | 2.0                     | 2.7              |
| Residual corrections (interpolation)                   | 1.4                     | 3.1              | 1.4                     | 3.1              | 1.4                     | 3.1              |
| Residual corrections $(Z \to W \text{ extrapolation})$ | 0.2                     | 5.8              | 0.2                     | 4.3              | 0.2                     | 5.1              |
| Total  | 2.6                     | 14.2             | 2.7                     | 11.8             | 2.6                     | 13.0             |
|  |                         |                  |                         |                  |                         |                  |

Calibration uncertainties

m<sub>⊤</sub> and p<sub>⊤</sub><sup>l</sup> comb. 2.9 MeV Total

# **Physics Modelling**

- No available generator describes all observed distribution
   choose extensive re-weighting approach
- Re-weighted baseline MC (Powheg + Pythia 8) to more precise model
  - \* with higher order QCD effects
  - \* with electroweak corrections



# **Physics Modelling**

- The theoretical description of the angular coefficient A<sub>i</sub> are not described well by ResBos at NLO for fixed-order and resummed calculations but satisfactorily by DYNNLO
- \* Hadronic recoil parameter  $u_{\parallel}^{I}$  is sensitive to the Wp<sub>T</sub> DyRes and MiNLO do not describe data well, therefore not used



## **Results in Measurement Categories**

| Channel                                      | $m_W$   | Stat. | Muon  | Elec. | Recoil | Bckg. | QCD  | EWK  | PDF  | Total |
|--|---------|-------|-------|-------|--------|-------|------|------|------|-------|
| $m_{ m T}	ext{-}{ m Fit}$                    | [MeV]   | Unc.  | Unc.  | Unc.  | Unc.   | Unc.  | Unc. | Unc. | Unc. | Unc.  |
| $\overline{W^+ \to \mu\nu,  \eta  < 0.8}$    | 80371.3 | 29.2  | 12.4  | 0.0   | 15.2   | 8.1   | 9.9  | 3.4  | 28.4 | 47.1  |
| $W^+ \to \mu \nu, 0.8 <  \eta  < 1.4$        | 80354.1 | 32.1  | 19.3  | 0.0   | 13.0   | 6.8   | 9.6  | 3.4  | 23.3 | 47.6  |
| $W^+ \to \mu \nu, 1.4 <  \eta  < 2.0$        | 80426.3 | 30.2  | 35.1  | 0.0   | 14.3   | 7.2   | 9.3  | 3.4  | 27.2 | 56.9  |
| $W^+ \rightarrow \mu\nu, 2.0 <  \eta  < 2.4$ | 80334.6 | 40.9  | 112.4 | 0.0   | 14.4   | 9.0   | 8.4  | 3.4  | 32.8 | 125.5 |
| $W^-  ightarrow \mu  u,  \eta  < 0.8$        | 80375.5 | 30.6  | 11.6  | 0.0   | 13.1   | 8.5   | 9.5  | 3.4  | 30.6 | 48.5  |
| $W^- \rightarrow \mu\nu, 0.8 <  \eta  < 1.4$ | 80417.5 | 36.4  | 18.5  | 0.0   | 12.2   | 7.7   | 9.7  | 3.4  | 22.2 | 49.7  |
| $W^- \rightarrow \mu\nu, 1.4 <  \eta  < 2.0$ | 80379.4 | 35.6  | 33.9  | 0.0   | 10.5   | 8.1   | 9.7  | 3.4  | 23.1 | 56.9  |
| $W^- \rightarrow \mu\nu, 2.0 <  \eta  < 2.4$ | 80334.2 | 52.4  | 123.7 | 0.0   | 11.6   | 10.2  | 9.9  | 3.4  | 34.1 | 139.9 |
| $\overline{W^+ \to e\nu,  \eta  < 0.6}$      | 80352.9 | 29.4  | 0.0   | 19.5  | 13.1   | 15.3  | 9.9  | 3.4  | 28.5 | 50.8  |
| $W^+ \to e\nu, 0.6 <  \eta  < 1.2$           | 80381.5 | 30.4  | 0.0   | 21.4  | 15.1   | 13.2  | 9.6  | 3.4  | 23.5 | 49.4  |
| $W^+ \to e\nu, 1, 8 <  \eta  < 2.4$          | 80352.4 | 32.4  | 0.0   | 26.6  | 16.4   | 32.8  | 8.4  | 3.4  | 27.3 | 62.6  |
| $W^-  ightarrow e u,  \eta  < 0.6$           | 80415.8 | 31.3  | 0.0   | 16.4  | 11.8   | 15.5  | 9.5  | 3.4  | 31.3 | 52.1  |
| $W^- \rightarrow e\nu, 0.6 <  \eta  < 1.2$   | 80297.5 | 33.0  | 0.0   | 18.7  | 11.2   | 12.8  | 9.7  | 3.4  | 23.9 | 49.0  |
| $W^- \rightarrow e\nu, 1.8 <  \eta  < 2.4$   | 80423.8 | 42.8  | 0.0   | 33.2  | 12.8   | 35.1  | 9.9  | 3.4  | 28.1 | 72.3  |
| $p_{\mathrm{T}}	ext{-}\mathrm{Fit}$          |         |       |       |       |        |       |      |      |      |       |
| $W^+ 	o \mu \nu,  \eta  < 0.8$               | 80327.7 | 22.1  | 12.2  | 0.0   | 2.6    | 5.1   | 9.0  | 6.0  | 24.7 | 37.3  |
| $W^+ \to \mu \nu, 0.8 <  \eta  < 1.4$        | 80357.3 | 25.1  | 19.1  | 0.0   | 2.5    | 4.7   | 8.9  | 6.0  | 20.6 | 39.5  |
| $W^+ \to \mu \nu, 1.4 <  \eta  < 2.0$        | 80446.9 | 23.9  | 33.1  | 0.0   | 2.5    | 4.9   | 8.2  | 6.0  | 25.2 | 49.3  |
| $W^+ \to \mu \nu, 2.0 <  \eta  < 2.4$        | 80334.1 | 34.5  | 110.1 | 0.0   | 2.5    | 6.4   | 6.7  | 6.0  | 31.8 | 120.2 |
| $W^-  ightarrow \mu  u,  \eta  < 0.8$        | 80427.8 | 23.3  | 11.6  | 0.0   | 2.6    | 5.8   | 8.1  | 6.0  | 26.4 | 39.0  |
| $W^- \rightarrow \mu\nu, 0.8 <  \eta  < 1.4$ | 80395.6 | 27.9  | 18.3  | 0.0   | 2.5    | 5.6   | 8.0  | 6.0  | 19.8 | 40.5  |
| $W^- \rightarrow \mu\nu, 1.4 <  \eta  < 2.0$ | 80380.6 | 28.1  | 35.2  | 0.0   | 2.6    | 5.6   | 8.0  | 6.0  | 20.6 | 50.9  |
| $W^- \rightarrow \mu\nu, 2.0 <  \eta  < 2.4$ | 80315.2 | 45.5  | 116.1 | 0.0   | 2.6    | 7.6   | 8.3  | 6.0  | 32.7 | 129.6 |
| $W^+  ightarrow e u,  \eta  < 0.6$           | 80336.5 | 22.2  | 0.0   | 20.1  | 2.5    | 6.4   | 9.0  | 5.3  | 24.5 | 40.7  |
| $W^+ \to e\nu, 0.6 <  \eta  < 1.2$           | 80345.8 | 22.8  | 0.0   | 21.4  | 2.6    | 6.7   | 8.9  | 5.3  | 20.5 | 39.4  |
| $W^+ \rightarrow e\nu, 1,8 <  \eta  < 2.4$   | 80344.7 | 24.0  | 0.0   | 30.8  | 2.6    | 11.9  | 6.7  | 5.3  | 24.1 | 48.2  |
| $W^- \to e\nu,  \eta  < 0.6$                 | 80351.0 | 23.1  | 0.0   | 19.8  | 2.6    | 7.2   | 8.1  | 5.3  | 26.6 | 42.2  |
| $W^- \rightarrow e\nu, 0.6 <  \eta  < 1.2$   | 80309.8 | 24.9  | 0.0   | 19.7  | 2.7    | 7.3   | 8.0  | 5.3  | 20.9 | 39.9  |
| $W^- \rightarrow e\nu, 1.8 <  \eta  < 2.4$   | 80413.4 | 30.1  | 0.0   | 30.7  | 2.7    | 11.5  | 8.3  | 5.3  | 22.7 | 51.0  |
|  |         |       |       |       |        |       |      |      |      |       |

Fit ranges : 32<p<sup>-1</sup><45 GeV; 66<m<sup>-</sup><99 GeV, minimizing total expected measurement uncertainty

Strongly

correlated

Strongly  $|\eta|$  comb.  $\rightarrow \sim 14$  MeV

correlated W+/W- comb  $\rightarrow \sim 8 \text{ MeV}$ 

 $|\eta| \text{ comb } e \rightarrow \sim 15 \text{ MeV}$ 

 $\mu \rightarrow \sim 11 \text{ MeV}$ 

## **Results in Measurement Categories**



- Measurements consistent
  - in each category
  - \* in combinations of categories
- Fulfils the requirement to be unblinded



## **Final Combined Results**



 $m_W = 80369.5 \pm 6.8 \text{ MeV(stat.)} \pm 10.6 \text{ MeV(exp. syst.)} \pm 13.6 \text{ MeV(mod. syst.)}$  $= 80369.5 \pm 18.5 \text{ MeV}$ 

- Final uncertainty dominated by physics modelling uncertainties
  - \* e.g. PDF uncertainty in fixed order prediction 8 MeV on  $p_T^{I}$  fit
  - parton shower factorisation scale 5 MeV
- ATLAS result competitive with previous measurements and consistent with SM prediction

#### W+ W- Mass Difference

 Auxiliary measurement: Mass difference between W+ and W-(zero difference in the SM)

 $m_{W^+} - m_{W^-} = -29.2 \pm 12.8 \text{ MeV(stat.)} \pm 7.0 \text{ MeV(exp. syst.)} \pm 23.9 \text{ MeV(mod. syst.)}$ = -29.2 ± 28.0 MeV,

Same measurement methodology but mass difference was not blinded

| Channel                 | $m_{W^+} - m_{W^-}$ [MeV] | Stat.<br>Unc. | Muon<br>Unc. | Elec.<br>Unc. | Recoil<br>Unc. | Bckg.<br>Unc. | QCD<br>Unc. | EW<br>Unc. | PDF<br>Unc.  | Total<br>  Unc. |
|-------------------------|---------------------------|---------------|--------------|---------------|----------------|---------------|-------------|------------|--------------|-----------------|
| $W \rightarrow e \nu$   | -29.7                     | 17.5          | 0.0          | 4.9           | 0.9            | 5.4           | 0.5         | 0.0        | <b>24.</b> 1 | 30.7            |
| $W \rightarrow \mu \nu$ | -28.6                     | 16.3          | 11.7         | 0.0           | 1.1            | 5.0           | 0.4         | 0.0        | 26.0         | 33.2            |
| Combined                | -29.2                     | 12.8          | 3.3          | 4.1           | 1.0            | 4.5           | 0.4         | 0.0        | 23.9         | 28.0            |

PDF uncertainties anti-correlated between W<sup>+</sup> and W<sup>-</sup>

- First W-boson mass measurement at the LHC
- Consistent and competitive with previous measurements
- In agreement with prediction from global electroweak fit
- \*\* arXiv:1701.07240



## Backup Results in Measurement Categories

| Combined  | Value   | Stat. | Muon | Elec. | Recoil | Bckg. | QCD  | $\mathbf{EW}$ | PDF  | Total | $\chi^2/{ m dof}$ |
|---|---------|-------|------|-------|--------|-------|------|---------------|------|-------|-------------------|
| categories  | [MeV]   | Unc.  | Unc. | Unc.  | Unc.   | Unc.  | Unc. | Unc.          | Unc. | Unc.  | of Comb.          |
| $m_{\rm T}, W^+, e^{-\mu}$  | 80370.0 | 12.3  | 8.3  | 6.7   | 14.5   | 9.7   | 9.4  | 3.4           | 16.9 | 30.9  | 2/6               |
| $m_{\rm T}, W^-, e$ - $\mu$   | 80381.1 | 13.9  | 8.8  | 6.6   | 11.8   | 10.2  | 9.7  | 3.4           | 16.2 | 30.5  | 7/6               |
| $m_{\mathrm{T}}, W^{\pm}, e$ - $\mu$                                | 80375.7 | 9.6   | 7.8  | 5.5   | 13.0   | 8.3   | 9.6  | 3.4           | 10.2 | 25.1  | 11/13             |
| $p_{\rm T}^{\ell}, W^+, e^{-\mu}$                                   | 80352.0 | 9.6   | 6.5  | 8.4   | 2.5    | 5.2   | 8.3  | 5.7           | 14.5 | 23.5  | 5/6               |
| $p_{\rm T}^{\ell}, W^{-}, e^{-\mu}$                                 | 80383.4 | 10.8  | 7.0  | 8.1   | 2.5    | 6.1   | 8.1  | 5.7           | 13.5 | 23.6  | 10/6              |
| $p_{\mathrm{T}}^{\bar{\ell}}, W^{\pm}, e$ - $\mu$                   | 80369.4 | 7.2   | 6.3  | 6.7   | 2.5    | 4.6   | 8.3  | 5.7           | 9.0  | 18.7  | 19/13             |
| $p_{\mathrm{T}}^{\ell}, W^{\pm}, e$                                 | 80347.2 | 9.9   | 0.0  | 14.8  | 2.6    | 5.7   | 8.2  | 5.3           | 8.9  | 23.1  | 4/5               |
| $m_{\mathrm{T}}, W^{\pm}, e$  | 80364.6 | 13.5  | 0.0  | 14.4  | 13.2   | 12.8  | 9.5  | 3.4           | 10.2 | 30.8  | 8/5               |
| $m_{\mathrm{T}}$ - $p_{\mathrm{T}}^{\ell}, W^{+}, e$                | 80345.4 | 11.7  | 0.0  | 16.0  | 3.8    | 7.4   | 8.3  | 5.0           | 13.7 | 27.4  | 1/5               |
| $m_{\rm T}$ - $p_{\rm T}^{\bar{\ell}}, W^{-}, e$                    | 80359.4 | 12.9  | 0.0  | 15.1  | 3.9    | 8.5   | 8.4  | 4.9           | 13.4 | 27.6  | 8/5               |
| $m_{\mathrm{T}}$ - $p_{\mathrm{T}}^{\bar{\ell}}, W^{\pm}, e$        | 80349.8 | 9.0   | 0.0  | 14.7  | 3.3    | 6.1   | 8.3  | 5.1           | 9.0  | 22.9  | 12/11             |
| $p_{\mathrm{T}}^{\ell}, W^{\pm}, \mu$                               | 80382.3 | 10.1  | 10.7 | 0.0   | 2.5    | 3.9   | 8.4  | 6.0           | 10.7 | 21.4  | 7/7               |
| $m_{\rm T}, W^{\pm}, \mu$   | 80381.5 | 13.0  | 11.6 | 0.0   | 13.0   | 6.0   | 9.6  | 3.4           | 11.2 | 27.2  | 3/7               |
| $m_{\mathrm{T}}$ - $p_{\mathrm{T}}^{\ell}, W^{+}, \mu$              | 80364.1 | 11.4  | 12.4 | 0.0   | 4.0    | 4.7   | 8.8  | 5.4           | 17.6 | 27.2  | 5/7               |
| $m_{\mathrm{T}}$ - $p_{\mathrm{T}}^{\ell},W^{-},\mu$                | 80398.6 | 12.0  | 13.0 | 0.0   | 4.1    | 5.7   | 8.4  | 5.3           | 16.8 | 27.4  | 3/7               |
| $m_{\mathrm{T}}$ - $p_{\mathrm{T}}^{\ell}, W^{\pm}, \mu$            | 80382.0 | 8.6   | 10.7 | 0.0   | 3.7    | 4.3   | 8.6  | 5.4           | 10.9 | 21.0  | 10/15             |
| $m_{\mathrm{T}}$ - $p_{\mathrm{T}}^{\ell}, W^{+}, e$ - $\mu$        | 80352.7 | 8.9   | 6.6  | 8.2   | 3.1    | 5.5   | 8.4  | 5.4           | 14.6 | 23.4  | 7/13              |
| $m_{\rm T}$ - $p_{\rm T}^{\ell}, W^{-}, e$ - $\mu$                  | 80383.6 | 9.7   | 7.2  | 7.8   | 3.3    | 6.6   | 8.3  | 5.3           | 13.6 | 23.4  | 15/13             |
| $m_{\mathrm{T}}$ - $p_{\mathrm{T}}^{\ell}, W^{\pm}, e$ - $\mu \mid$ | 80369.5 | 6.8   | 6.6  | 6.4   | 2.9    | 4.5   | 8.3  | 5.5           | 9.2  | 18.5  | 29/27             |

## Backup

- \* Samples of inclusive vector-boson production are produced using the Powheg MC generator interfaced to Pythia 8
- EW Corrections
  - QED final-state radiation simulated with Photos (dominant correction)
  - \* The effect of QED initial-state radiation (ISR) is also included through the Pythia 8 parton shower.
  - The effect of NLO EW corrections are estimated using Winhac
- Rapidity distribution and angular coefficients

  - An optimised version of DYNNLO is used
- Transverse momentum distribution
  - Modelled with Pythia 8
  - <sup>∞</sup> QCD parameters used in Pythia 8 were determined from fits to the Z-boson transverse momentum distribution measured with the ATLAS detector at a centre-of-mass energy of  $\sqrt{s}$  = 7 TeV (AZ tune)

| Decay channel                 | $W \rightarrow e\nu$  |                  | $W \rightarrow \mu \nu$ |                  | W-boson charge   |      | $W^+$            |                       | -                | Combined              |                  |
|-------------------------------|-----------------------|------------------|-------------------------|------------------|--|------|------------------|-----------------------|------------------|-----------------------|------------------|
| Kinematic distribution        | $p_{\mathrm{T}}^\ell$ | $m_{\mathrm{T}}$ | $p_{\mathbf{T}}^{\ell}$ | $m_{\mathrm{T}}$ | Kinematic distribution p                                     |      | $m_{\mathrm{T}}$ | $p_{\mathrm{T}}^\ell$ | $m_{\mathrm{T}}$ | $p_{\mathrm{T}}^\ell$ | $m_{\mathrm{T}}$ |
|                               | 11                    | -                | - 1                     | -                | $\delta m_W  [{ m MeV}]$                                     |      |                  |                       |                  |                       |                  |
| $\delta m_W  [{ m MeV}]$      |                       |                  |                         |                  | Fixed-order PDF uncertainty                                  | 13.1 | 14.9             | 12.0                  | 14.2             | 8.0                   | 8.7              |
| FSP (real)                    | < 0.1                 | < 0.1            | < 0.1                   | < 0.1            | AZ tune  | 3.0  | 3.4              | 3.0                   | 3.4              | 3.0                   | 3.4              |
| ron (real)                    | < 0.1                 | < 0.1            | < 0.1                   | < 0.1            | Charm-quark mass   | 1.2  | 1.5              | 1.2                   | 1.5              | 1.2                   | 1.5              |
| Pure weak and IFI corrections | 3.3                   | 2.5              | 3.5                     | 2.5              | Parton shower $\mu_{\rm F}$ with heavy-flavour decorrelation | 5.0  | 6.9              | 5.0                   | 6.9              | 5.0                   | 6.9              |
| FSB (pair production)         | 3.6                   | 0.8              | 4.4                     | 0.8              | Parton shower PDF uncertainty                                | 3.6  | 4.0              | 2.6                   | 2.4              | 1.0                   | 1.6              |
| ron (pan production)          | 0.0                   | 0.0              | 7.7                     | 0.8              | Angular coefficients   | 5.8  | 5.3              | 5.8                   | 5.3              | 5.8                   | 5.3              |
| Total                         | 4.9                   | 2.6              | 5.6                     | 2.6              | Total  | 15.9 | 18.1             | 14.8                  | 17.2             | 11.6                  | 12.9             |

#### Backup



$$\frac{d\sigma}{dp_{\rm T}^2 \,dy \,dm \,d\cos\theta \,d\phi} = \frac{3}{16\pi} \frac{d\sigma}{dp_{\rm T}^2 \,dy \,dm} \times \left[ (1 + \cos^2 \theta) + A_0 \frac{1}{2} (1 - 3\cos^2 \theta) + A_1 \sin^2 \theta \cos\theta \,d\phi + A_1 \sin^2 \theta \cos\phi + A_2 \frac{1}{2} \sin^2 \theta \cos^2 \phi + A_3 \sin^2 \theta \cos\phi + A_4 \cos\theta + A_5 \sin^2 \theta \sin^2 \phi + A_6 \sin^2 \theta \sin\phi + A_7 \sin\theta \sin\phi \right].$$
(3)

The angular coefficients depend in general on  $p_T$ , y and m. The  $A_5-A_7$  coefficients are non-zero only at order  $O(\alpha_s^2)$  and above. They are small in the  $p_T$  region relevant for the present analysis, and are not considered further. The angles  $\theta$  and  $\phi$  are defined in the Collins–Soper (CS) frame [82].

## Backup