

# Factorization of the Drell-Yan $q_T$ spectrum with massive quarks

Daniel Samitz

(University of Vienna)

based on arXiv:1703.09702

in collaboration with Piotr Pietrulewicz, Anne Spiering and Frank J. Tackmann

29th Rencontres de Blois

30 May 2017

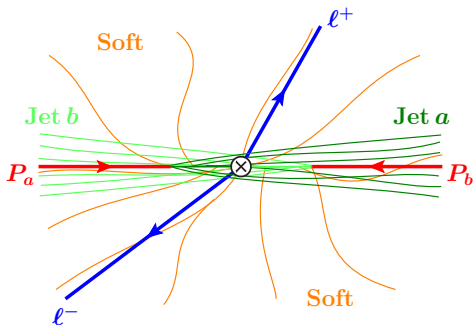


universität  
wien

$\int dk$   $\Pi$  Doktoratskolleg  
Particles and Interactions

# Motivation

- $p_T$  spectrum of Z-boson measured with high precision
- NNLL' analyses available
- no systematic theoretical description of b-quark mass effects yet can be relevant in  $m_W$  measurements
- discrepancies between MC and experiment in low  $p_T$  region

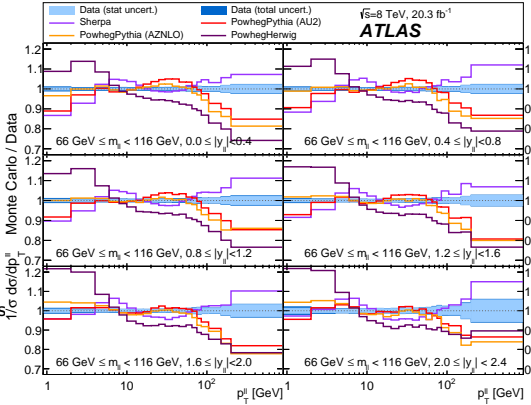


from: I.W.Stewart,F.J.Tackmann,W.J.Waalewijn, *Phys. Rev. D*81 (2010) 094035

goal: systematic treatment of quark mass effects at NNLL' accuracy  
for transverse momentum spectrum of the Z-boson

# Motivation

- $p_T$  spectrum of Z-boson measured with high precision
- NNLL' analyses available
- no systematic theoretical description of b-quark mass effects yet can be relevant in  $m_W$  measurements
- discrepancies between MC and experiment in low  $p_T$  region

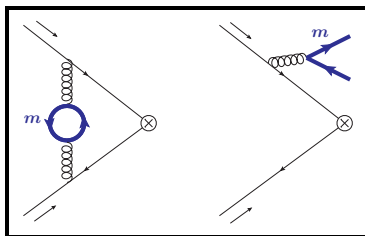
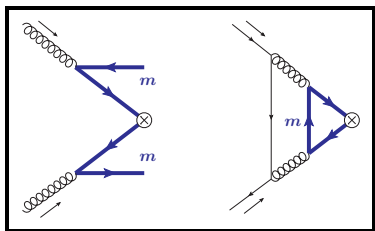


[ATLAS Collaboration (2015)]

goal: systematic treatment of quark mass effects at NNLL' accuracy for transverse momentum spectrum of the Z-boson

# Massive Quarks in DY

primary and secondary massive quarks.



- primary: massive quarks go into hard interaction
- secondary: massive quark corrections to light quark induced processes
- both start at  $\mathcal{O}(\alpha_s^2)$ , relevant for NNLL' resummation
- different hierarchies between  $p_T$  and  $m$  possible:

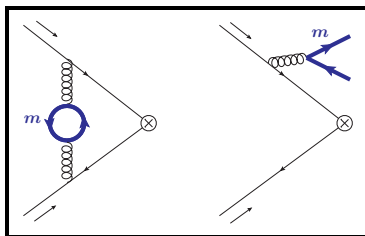
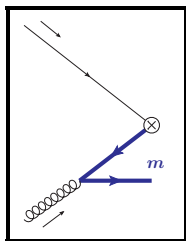
$$m \ll p_T$$

$$p_T \sim m$$

$$p_T \ll m$$

# Massive Quarks in W production

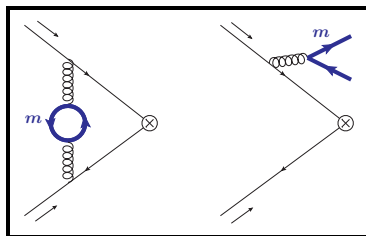
primary and secondary massive quarks.



- secondary massive quark effects the same as for Z production
- primary charm quarks already contribute at  $\mathcal{O}(\alpha_s)$
- primary bottom quarks CKM suppressed

# Massive Quarks in W production

primary and secondary massive quarks.



- secondary massive quark effects the same as for Z production
- primary charm quarks already contribute at  $\mathcal{O}(\alpha_s)$
- primary bottom quarks CKM suppressed

# W boson mass measurements

- experimentalists rely on ratio of W and Z boson spectrum

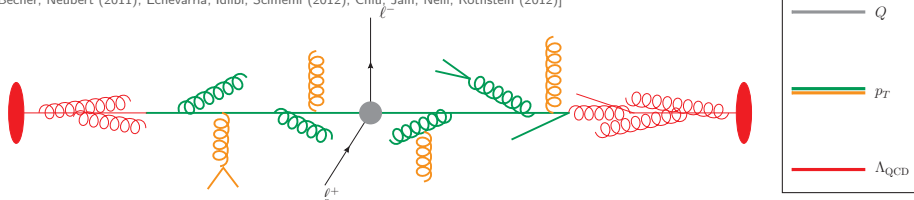
$$\left[ \frac{d\sigma^W}{dq_T} \right]_{\text{prediction}} = \left[ \frac{d\sigma^W}{dq_T} \times \left( \frac{d\sigma^Z}{dq_T} \right)^{-1} \right]_{\text{theory}} \times \left[ \frac{d\sigma^Z}{dq_T} \right]_{\text{measured}}$$

- Z boson spectrum measured with very high accuracy
  
- many things cancel to large extent in the ratio
  
- every difference between Z and W production can become relevant

# Massless Factorization for $p_T$ -spectrum in DY

[Collins, Soper, Sterman (1985)]

[Becher, Neubert (2011); Echevarria, Idilbi, Scimemi (2012); Chiu, Jain, Neill, Rothstein (2012)]

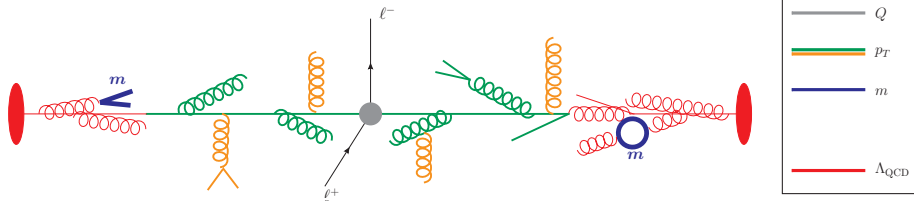


$$\frac{d\sigma}{dp_T} = \sum_{i \in \{q\}} H_i^{(n_f)}(Q) \times \left[ \sum_{j \in \{q, g\}} \mathcal{I}_{ij}^{(n_f)}(p_T, x) \otimes f_j^{(n_f)}(x) \right]^2 \otimes_{\perp} S^{(n_f)}(p_T) + \mathcal{O}\left(\frac{p_T}{Q}, \frac{\Lambda_{\text{QCD}}^2}{p_T^2}\right)$$

- $H$ : hard function, scale  $Q$
- $\mathcal{I}$ : beam function, scale  $p_T$
- $S$ : soft function, scale  $p_T$
- $f$ : PDF, scale  $\Lambda_{\text{QCD}}$



# Factorization for $m \ll p_T$

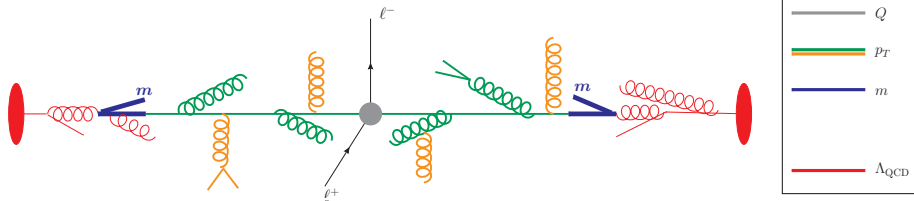


$$\frac{d\sigma}{dp_T} = \sum_{i \in \{q, Q\}} H_i^{(5)}(Q) \times \left[ \sum_{j \in \{q, Q, g\}} \mathcal{I}_{ij}^{(5)}(p_T, x) \otimes f_j^{(5)}(x) \right]^2 \otimes_{\perp} S^{(5)}(p_T)$$

Power Corrections:  $\mathcal{O}\left(\frac{m^2}{p_T^2}\right)$

- matching:  $f_j^{(5)}(x) = \sum_k \mathcal{M}_{jk}(x, m) \otimes f_k^{(4)}(x)$
- secondary  $\mathcal{M}_{qq}$  and primary  $\mathcal{M}_{Qg}$  heavy quarks  
[M. Buza, Y. Martinounine, J. Smith, W. van. Neerven (1998)]
- hard, beam and soft functions with 5 massless flavors

# Factorization for $m \ll p_T$

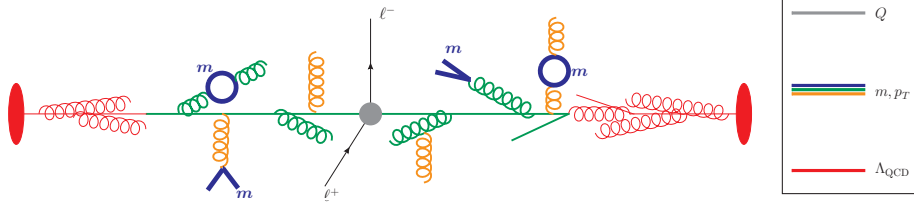


$$\frac{d\sigma}{dp_T} = \sum_{i \in \{q, Q\}} H_i^{(5)}(Q) \times \left[ \sum_{j \in \{q, Q, g\}} \mathcal{I}_{ij}^{(5)}(p_T, x) \otimes f_j^{(5)}(x) \right]^2 \otimes_{\perp} S^{(5)}(p_T)$$

Power Corrections:  $\mathcal{O}\left(\frac{m^2}{p_T^2}\right)$

- matching:  $f_j^{(5)}(x) = \sum_k \mathcal{M}_{jk}(x, m) \otimes f_k^{(4)}(x)$
- secondary  $\mathcal{M}_{qq}$  and primary  $\mathcal{M}_{Qg}$  heavy quarks  
[M. Buza, Y. Martinounine, J. Smith, W. van. Neerven (1998)]
- hard, **beam** and **soft** functions with **5** massless flavors

# Factorization for $p_T \sim m$

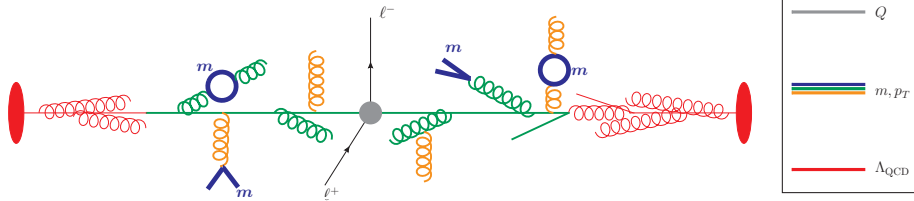


$$\frac{d\sigma_{\text{sec}}}{dp_T} = \sum_{i \in \{q\}} H_i^{(5)}(Q) \times \left[ \sum_{j \in \{q, g\}} \mathcal{I}_{ij}^{(5)}(p_T, x, m) \otimes f_j^{(4)}(x) \right]^2 \otimes_{\perp} S^{(5)}(p_T, m)$$

Power Corrections:  $\mathcal{O}\left(\frac{m^2}{Q^2}\right)$

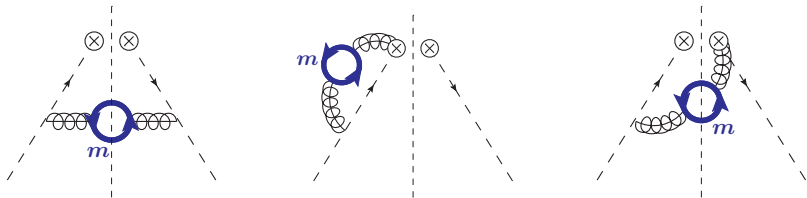
- secondary massive quarks in beam function  $\mathcal{I}_{qq}$  and soft function  $S$

# Factorization for $p_T \sim m$

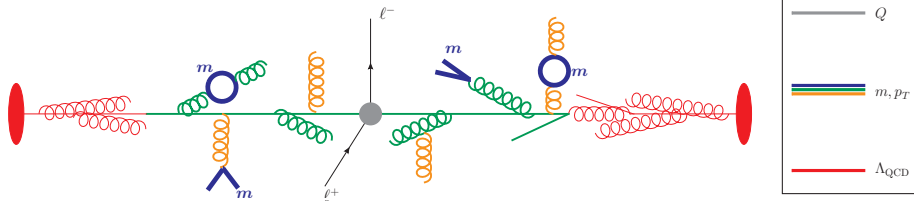


$$\frac{d\sigma_{\text{sec}}}{dp_T} = \sum_{i \in \{q\}} H_i^{(5)}(Q) \times \left[ \sum_{j \in \{q, g\}} \mathcal{I}_{ij}^{(5)}(p_T, x, m) \otimes f_j^{(4)}(x) \right]^2 \otimes_{\perp} S^{(5)}(p_T, m)$$

Power Corrections:  $\mathcal{O}\left(\frac{m^2}{Q^2}\right)$

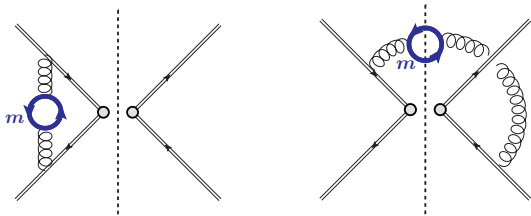


# Factorization for $p_T \sim m$

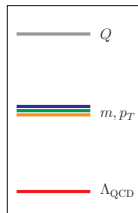
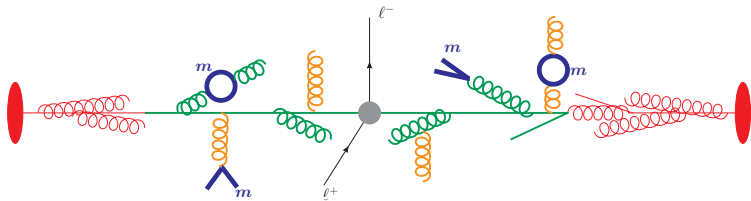


$$\frac{d\sigma_{\text{sec}}}{dp_T} = \sum_{i \in \{q\}} H_i^{(5)}(Q) \times \left[ \sum_{j \in \{q, g\}} \mathcal{I}_{ij}^{(5)}(p_T, x, m) \otimes f_j^{(4)}(x) \right]^2 \otimes_{\perp} S^{(5)}(p_T, m)$$

Power Corrections:  $\mathcal{O}\left(\frac{m^2}{Q^2}\right)$



# Factorization for $p_T \sim m$

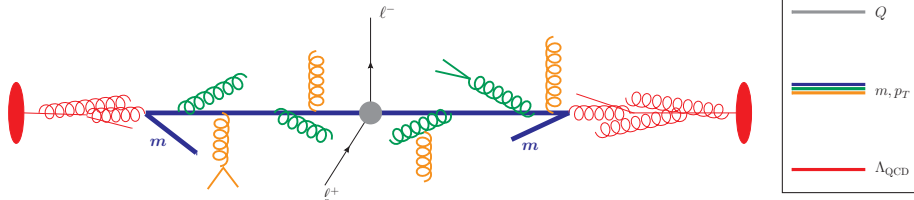


$$\frac{d\sigma_{\text{sec}}}{dp_T} = \sum_{i \in \{q\}} H_i^{(5)}(Q) \times \left[ \sum_{j \in \{q, g\}} \mathcal{I}_{ij}^{(5)}(p_T, x, m) \otimes f_j^{(4)}(x) \right]^2 \otimes_{\perp} S^{(5)}(p_T, m)$$

Power Corrections:  $\mathcal{O}\left(\frac{m^2}{Q^2}\right)$

- secondary massive quarks in beam function  $\mathcal{I}_{qq}$  and soft function S

# Factorization for $p_T \sim m$



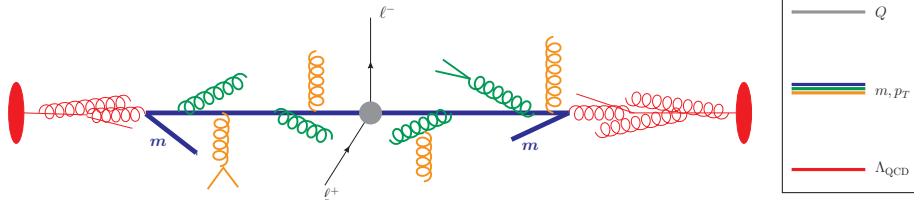
$$\frac{d\sigma_{\text{prim}}}{dp_T} = H_Q^{(5)}(Q) \times \left[ \sum_{j \in \{q, g\}} \mathcal{I}_{Qj}^{(5)}(p_T, x, m) \otimes f_j^{(4)}(x) \right]^2 \otimes_{\perp} S^{(5)}(p_T, m)$$

Power Corrections:  $\mathcal{O}\left(\frac{m^2}{Q^2}\right)$

- secondary **massive** quarks in **beam function**  $\mathcal{I}_{qq}$  and **soft function**  $S$
- primary **massive** quark **beam function**  $\mathcal{I}_{Qg}$

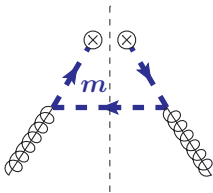
[A. Balyaev, P. Nadolsky, C.-P. Yuan (2005); S. Berge, P. Nadolsky, F. Olness (2005)]

# Factorization for $p_T \sim m$



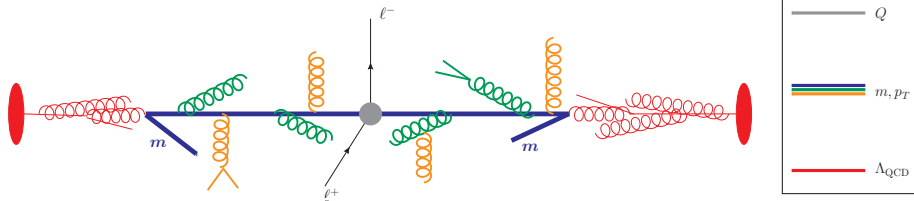
$$\frac{d\sigma_{\text{prim}}}{dp_T} = H_Q^{(5)}(Q) \times \left[ \sum_{j \in \{q, g\}} \mathcal{I}_{Qj}^{(5)}(p_T, x, m) \otimes f_j^{(4)}(x) \right]^2 \otimes_{\perp} S^{(5)}(p_T, m)$$

Power Corrections:  $\mathcal{O}\left(\frac{m^2}{Q^2}\right)$





# Factorization for $p_T \sim m$

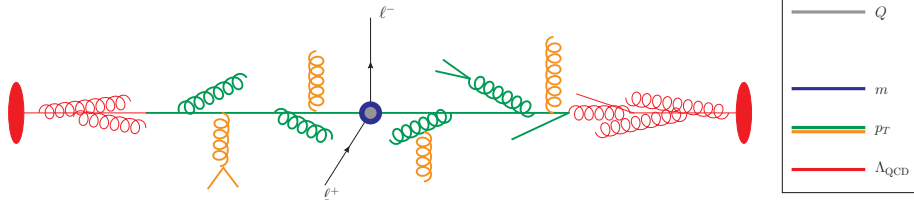


$$\frac{d\sigma_{\text{prim}}}{dp_T} = H_Q^{(5)}(Q) \times \left[ \sum_{j \in \{q, g\}} \mathcal{I}_{Qj}^{(5)}(p_T, x, m) \otimes f_j^{(4)}(x) \right]^2 \otimes_{\perp} S^{(5)}(p_T, m)$$

Power Corrections:  $\mathcal{O}\left(\frac{m^2}{Q^2}\right)$

- secondary massive quarks in beam function  $\mathcal{I}_{qq}$  and soft function  $S$
- primary massive quark beam function  $\mathcal{I}_{Qq}$   
[A. Balyaev, P. Nadolsky, C.-P. Yuan (2005); S. Berge, P. Nadolsky, F. Olnes (2005)]
- PDF with 4 and hard function with 5 massless flavors

# Factorization for $p_T \ll m$

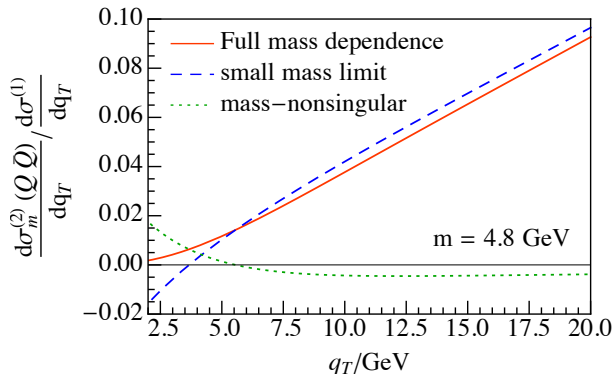


$$\frac{d\sigma}{dp_T} = \sum_{i \in \{q\}} H_i^{(5)}(Q) \times H_m(m) \times \left[ \sum_{j \in \{q, g\}} \mathcal{I}_{ij}^{(4)}(p_T, x) \otimes f_j^{(4)}(x) \right]^2 \otimes_{\perp} S^{(4)}(p_T)$$

Power Corrections:  $\mathcal{O}\left(\frac{p_T^2}{m^2}, \frac{m^2}{Q^2}\right)$

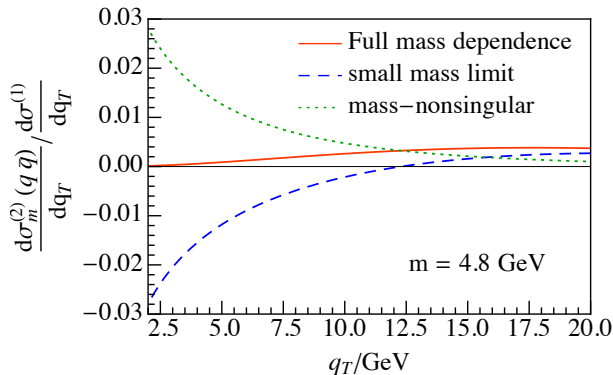
- mass mode matching function  $H_m$  from integrating out the heavy flavor from the current  
[S. Gritschacher, A. Hoang, I. Jemos, V. Mateu, P. Pietrulewicz (2014)]
- beam function, soft function, PDF with 4 massless flavors, hard function with 5 massless flavors

# Mass Effects - Primary



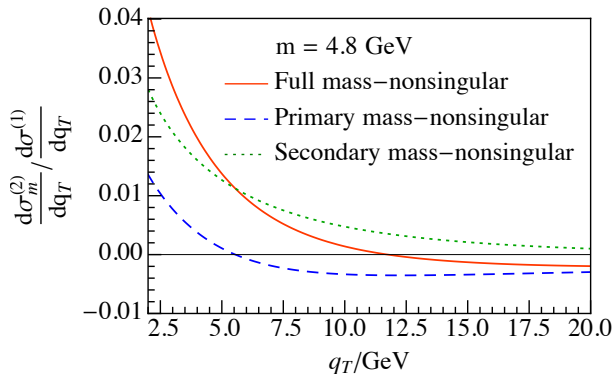
- $\mathcal{O}(\alpha_s^2)$  contributions from primary massive quarks at fixed order, normalized to the LO spectrum
- $E_{\text{cm}} = 13 \text{ TeV}$ ,  $m_b = 4.8 \text{ GeV}$ ,  $Q = m_Z$ ,  $Y = 0$ , MSTW NLO PDFs

# Mass Effects - Secondary



- $\mathcal{O}(\alpha_s^2)$  contributions from secondary massive quarks at fixed order, normalized to the LO spectrum
- $E_{\text{cm}} = 13 \text{ TeV}$ ,  $m_b = 4.8 \text{ GeV}$ ,  $Q = m_Z$ ,  $Y = 0$ , MSTW NLO PDFs

# Mass Effects



- $\mathcal{O}(\alpha_s^2)$  quark mass corrections to the Z-boson  $p_T$ -spectrum at fixed order, normalized to the LO spectrum
- $E_{\text{cm}} = 13 \text{ TeV}$ ,  $m_b = 4.8 \text{ GeV}$ ,  $Q = m_Z$ ,  $Y = 0$ , MSTW NLO PDFs

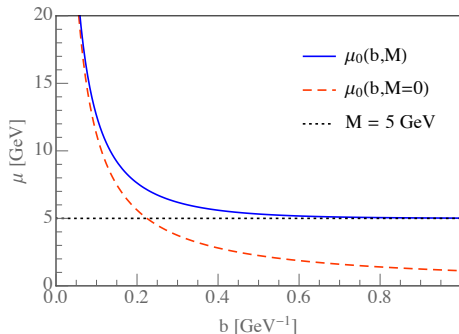
# Rapidity Logs from Massive Flavors

- secondary massive quarks lead to mass dependent rapidity anomalous dimension  $\tilde{\gamma}_\nu(b, m, \mu)$  (here in  $b$  space)

$$\tilde{\gamma}_\nu(b, m, \mu) \xrightarrow{b \rightarrow 0} = \left(\frac{\alpha_s(\mu)}{4\pi}\right)^2 C_F T_F \left(\frac{16}{3} L_b^2 + \frac{160}{9} L_b + \frac{224}{27}\right) \quad L_b = \ln\left(\frac{b^2 \mu^2 e^{2\gamma_E}}{4}\right)$$

$$\tilde{\gamma}_\nu(b, m, \mu) \xrightarrow{b \rightarrow \infty} = \left(\frac{\alpha_s(\mu)}{4\pi}\right)^2 C_F T_F \left(-\frac{16}{3} L_m^2 - \frac{160}{9} L_m - \frac{224}{27}\right) \quad L_m = \ln \frac{m^2}{\mu^2}$$

- large logarithms in  $\tilde{\gamma}_\nu$  can be avoided e.g. by  $b$  space setting of  $\mu$



$$\mu_0(b, m) \xrightarrow{b \rightarrow 0} \frac{2e^{-\gamma_E}}{b}$$

$$\mu_0(b, m) \xrightarrow{b \rightarrow \infty} m$$

$\Rightarrow$  mass introduces IR cutoff

$\Rightarrow$  no non-pert. regime for  $b \rightarrow \infty$

# Summary

- achieved resummation of all mass-related logarithms for  $p_T$ -spectrum in Drell-Yan at NNLL'
- calculated one-loop primary and two-loop secondary massive quark corrections to beam and soft functions
- with these ingredients also NNLL' resummation for bottom mass effects in  $W$  production (for charm only NNLL)
- mass effects estimated to be at percent level

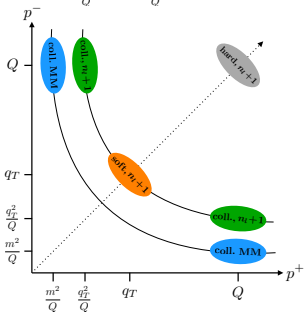
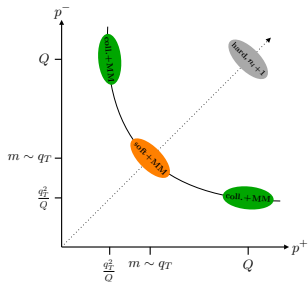
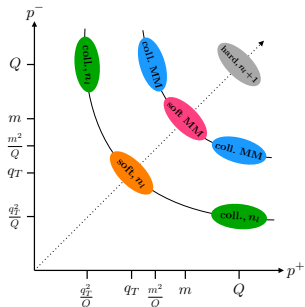
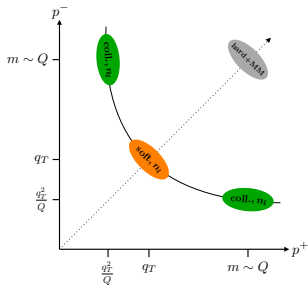
# Summary

- achieved resummation of all mass-related logarithms for  $p_T$ -spectrum in Drell-Yan at NNLL'
- calculated one-loop primary and two-loop secondary massive quark corrections to beam and soft functions
- with these ingredients also NNLL' resummation for bottom mass effects in  $W$  production (for charm only NNLL)
- mass effects estimated to be at percent level

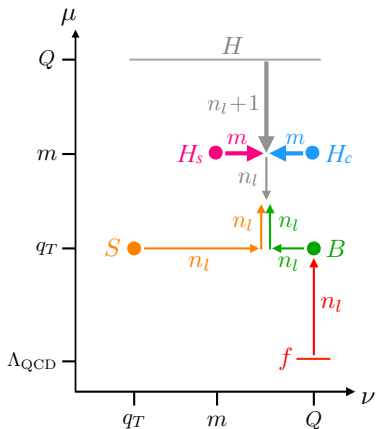
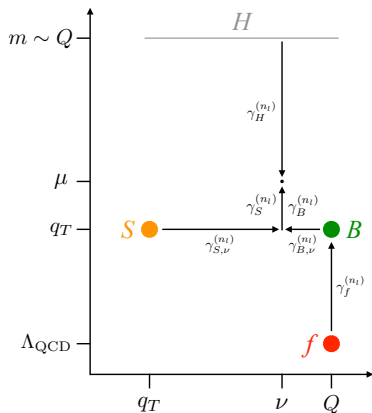
Thank you for your attention



# Modes



# Evolution 1



# Evolution 2

