



Introduction to Particle Physics

(for non physics students)

3. FORCES



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UNIVERSITY OF OXFORD



FORCES

Gravity

Electromagnetic. Weak. Strong

 ep in H atom

$$\frac{\text{Gravity P.E.}}{\text{Electromag}} \approx 10^{-40}$$

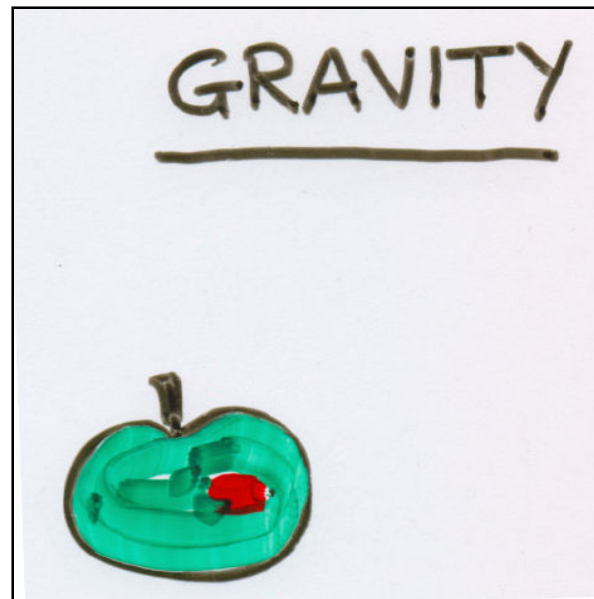
c.f. size of proton $\approx 10^{-15}$ m.

size of univ. $\leq 10^{10}$ yr. $\times 10^{16}$ m yr⁻¹
 $\leq 10^{26}$ m.

$$10^{-40} \approx \frac{\text{Radius of proton}}{\text{Radius of Universe}}$$

→ Ignore Gravity for individual particles at present energies

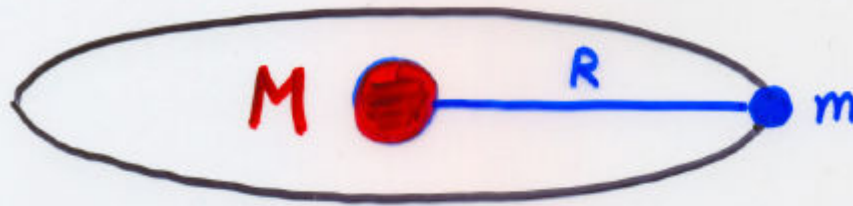
(10^{-35} m length or 10^{19} GeV grav. strong....)



Gravity
wins for
large bodies
and reveals
surprises
that may
link with
particles

DARK MATTER

Rotation speed via gravity
around a central mass



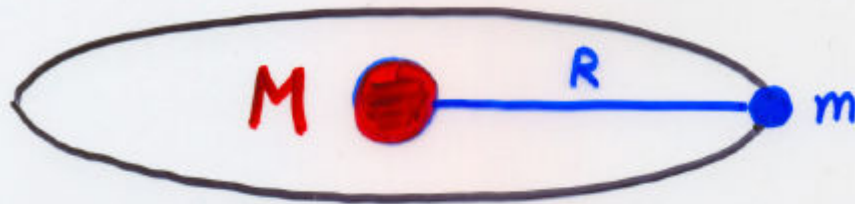
$$\text{Newton: } F = G \frac{Mm}{R^2} = \frac{mv^2}{R}$$

$$\Rightarrow v^2 = \frac{GM}{R}$$

speed goes down as \sqrt{R}

DARK MATTER

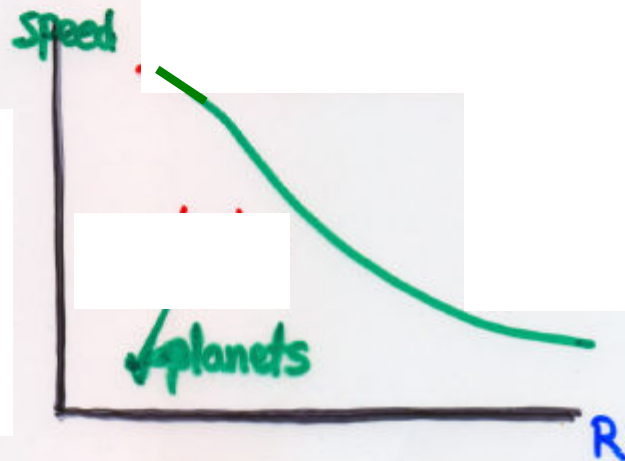
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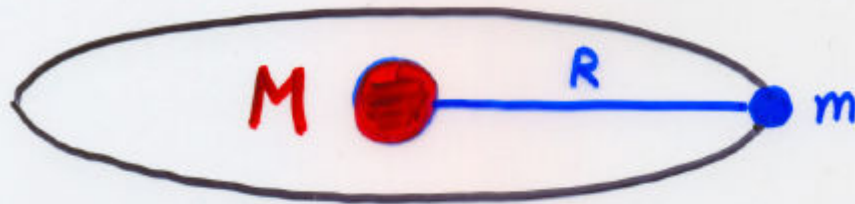
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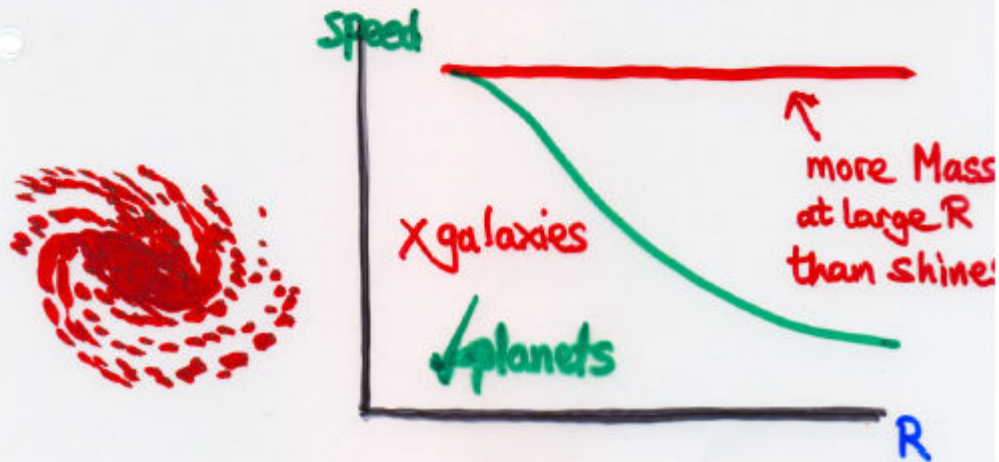
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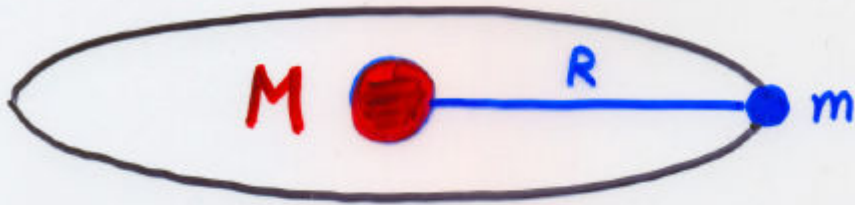
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DARK MATTER

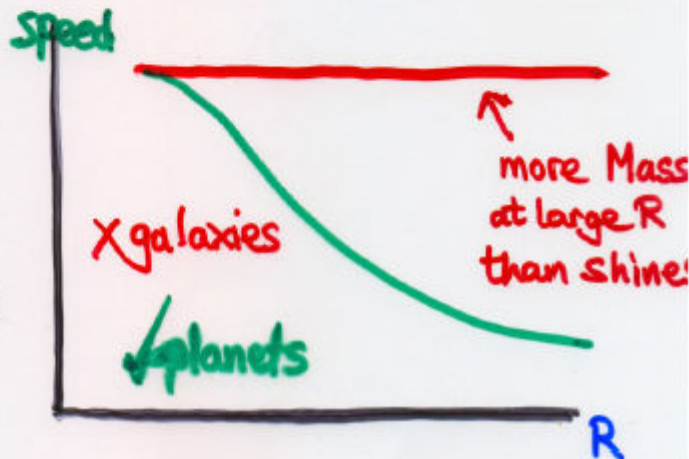
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$$\text{Newton: } F = G \frac{Mm}{R^2} = \frac{mv^2}{R}$$

$$\Rightarrow v^2 = \frac{GM}{R}$$

speed goes down as \sqrt{R}



What is dark matter?

Electrically neutral.

Hot DM – lightweight
like neutrinos

Cold DM – heavyweight
Maybe SUSY (next lecture)

Colour and the Strong Force

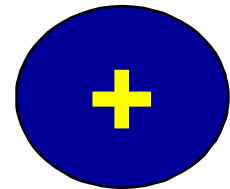
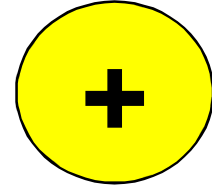
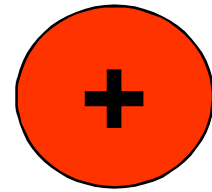
How quarks
work:

CHROMOSTATICS

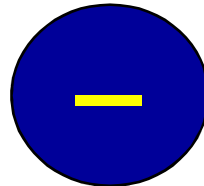
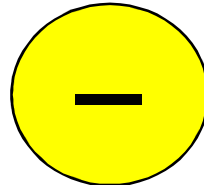
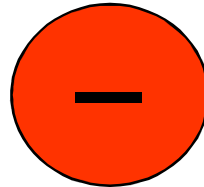
(like electrostatics but with three types of + (-) charges)

Three colour charges

Quarks “positive”



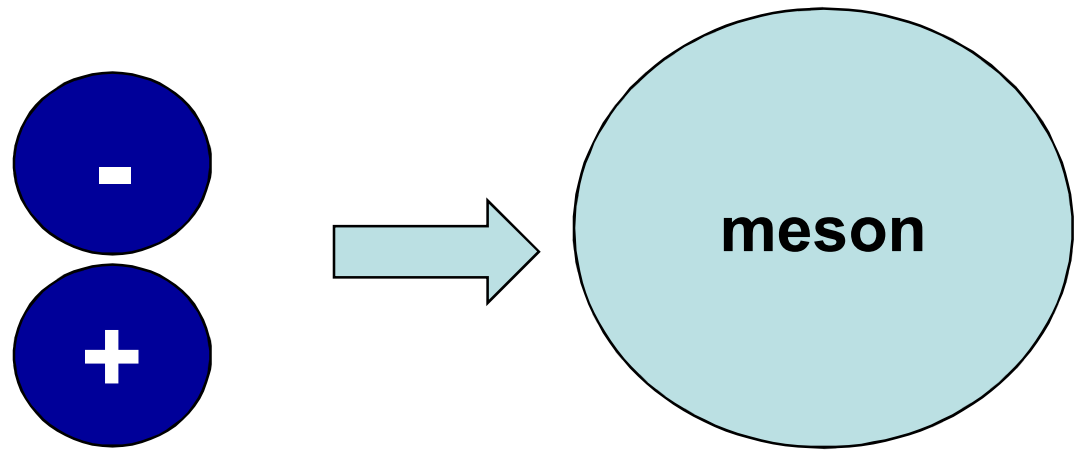
Antiquarks “negative”



Now use familiar rules

“Like charges (colours)
repel;
opposite (colours)
attract”

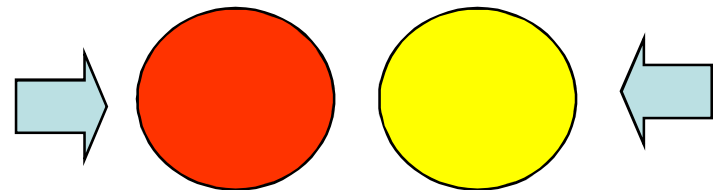
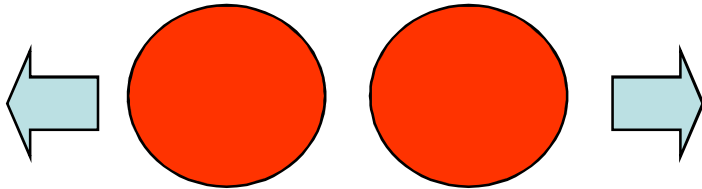
Simplest state: QQ^* Meson

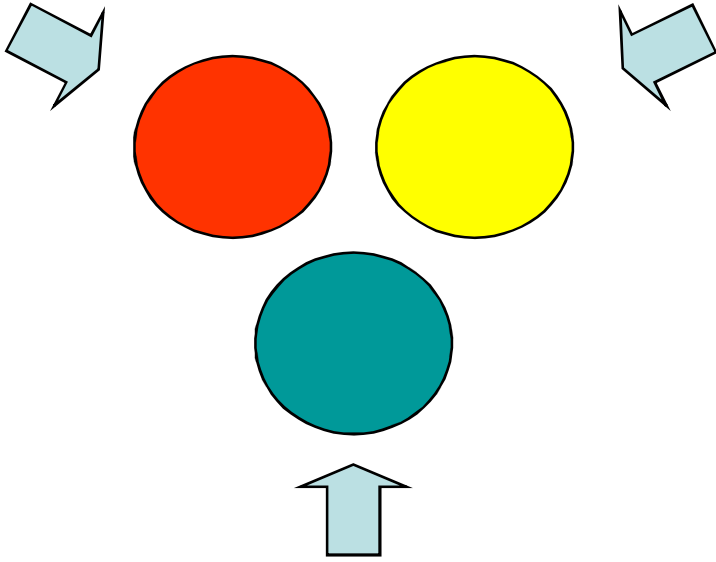


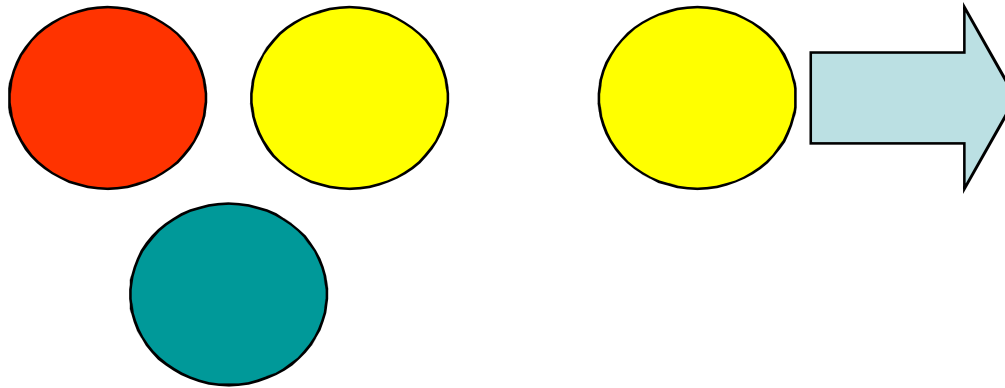
The **THREE** colours

enable quarks to attract one another

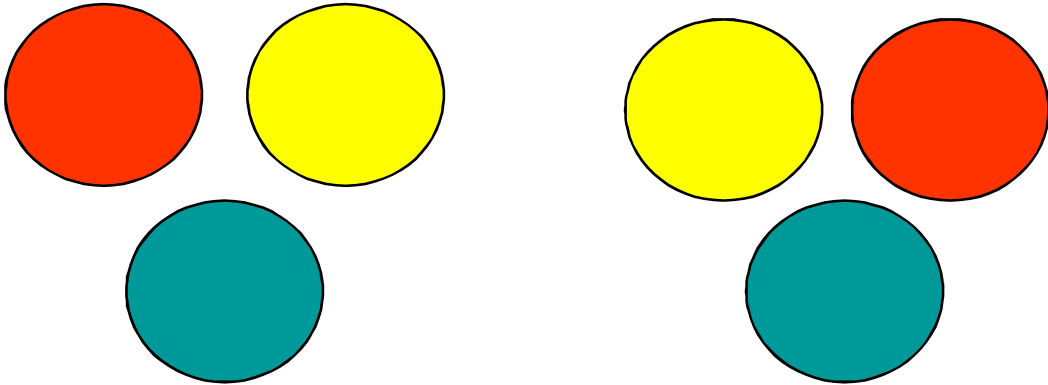
making **BARYONS** (e.g. the proton)







**Three colour charges neutralise
Makes baryon (e.g. proton)**



Simple nucleus (deuteron)

Electric charge → **Atoms** → **Molecules**

Colour charge → **Baryons** → **Nucleus**

Quantum Electrodynamics: QED

Electric charge  **Atoms**  **Molecules**

Quantum Chromodynamics: QCD

Colour charge  **Baryons**  **Nucleus**

Quantum Electrodynamics: QED

Electric charge  Atoms  Molecules

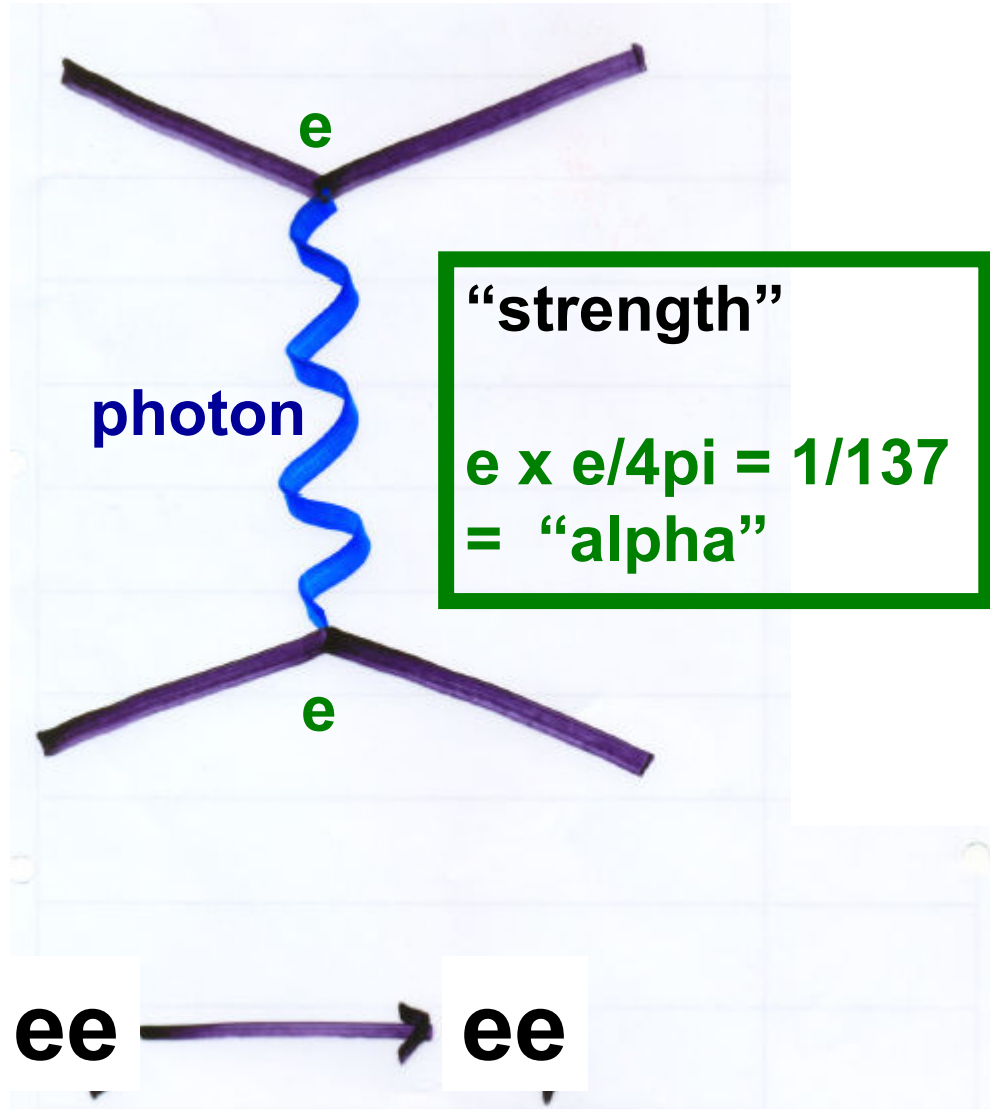
Interaction of electric charges and photons

Quantum Chromodynamics: QCD

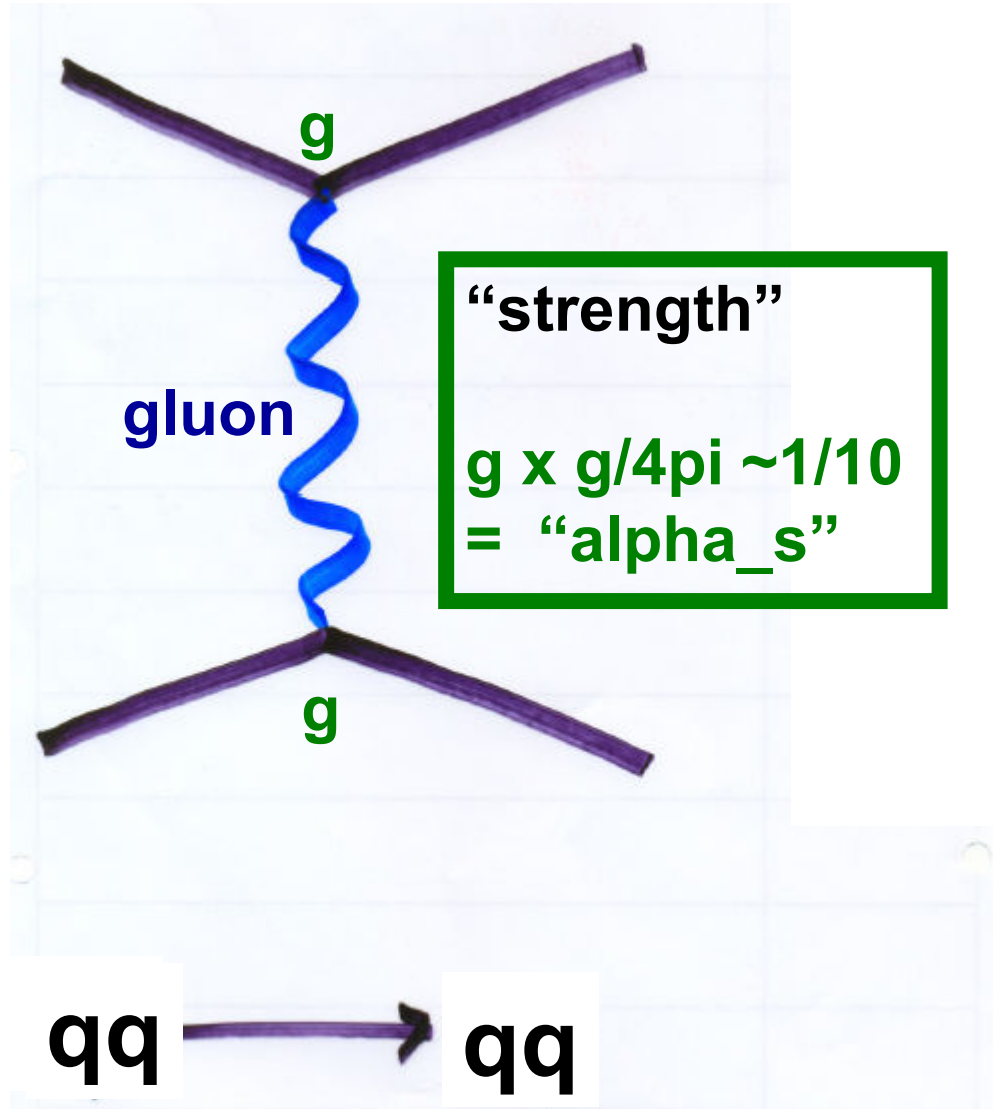
Colour charge  Baryons  Nucleus

Interaction of colour charges and gluons

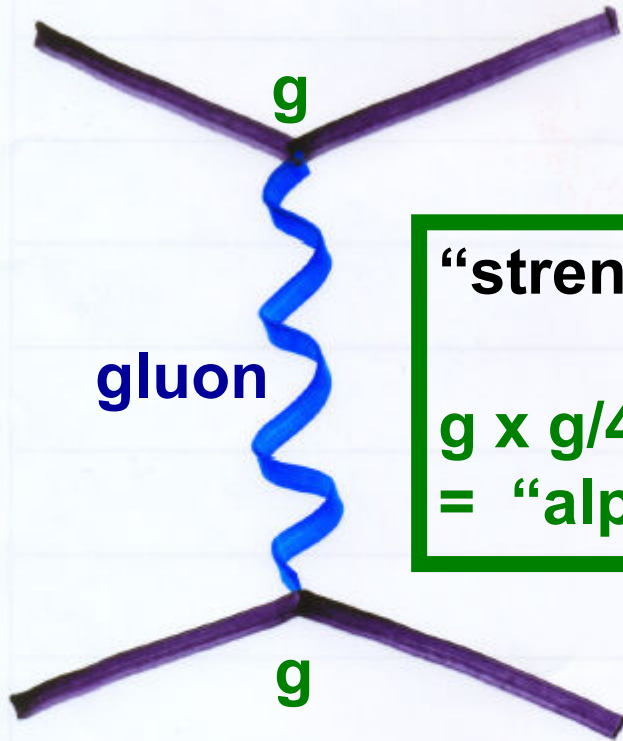
Feynman diagrams for electromagnetic interaction



Feynman diagrams for chromomagnetic interaction

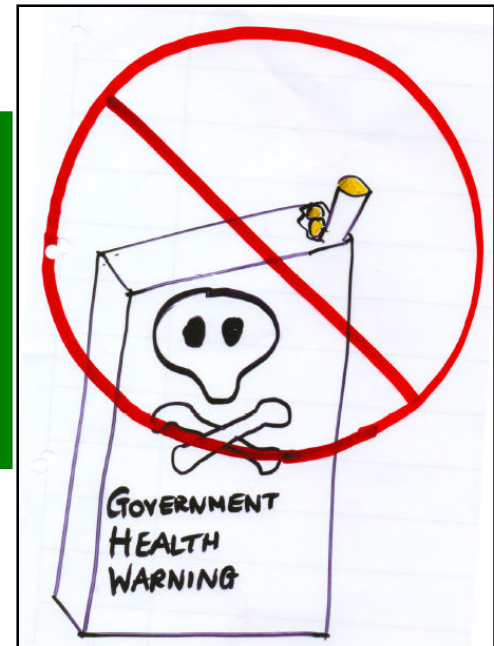


Feynman diagrams for chromomagnetic interaction



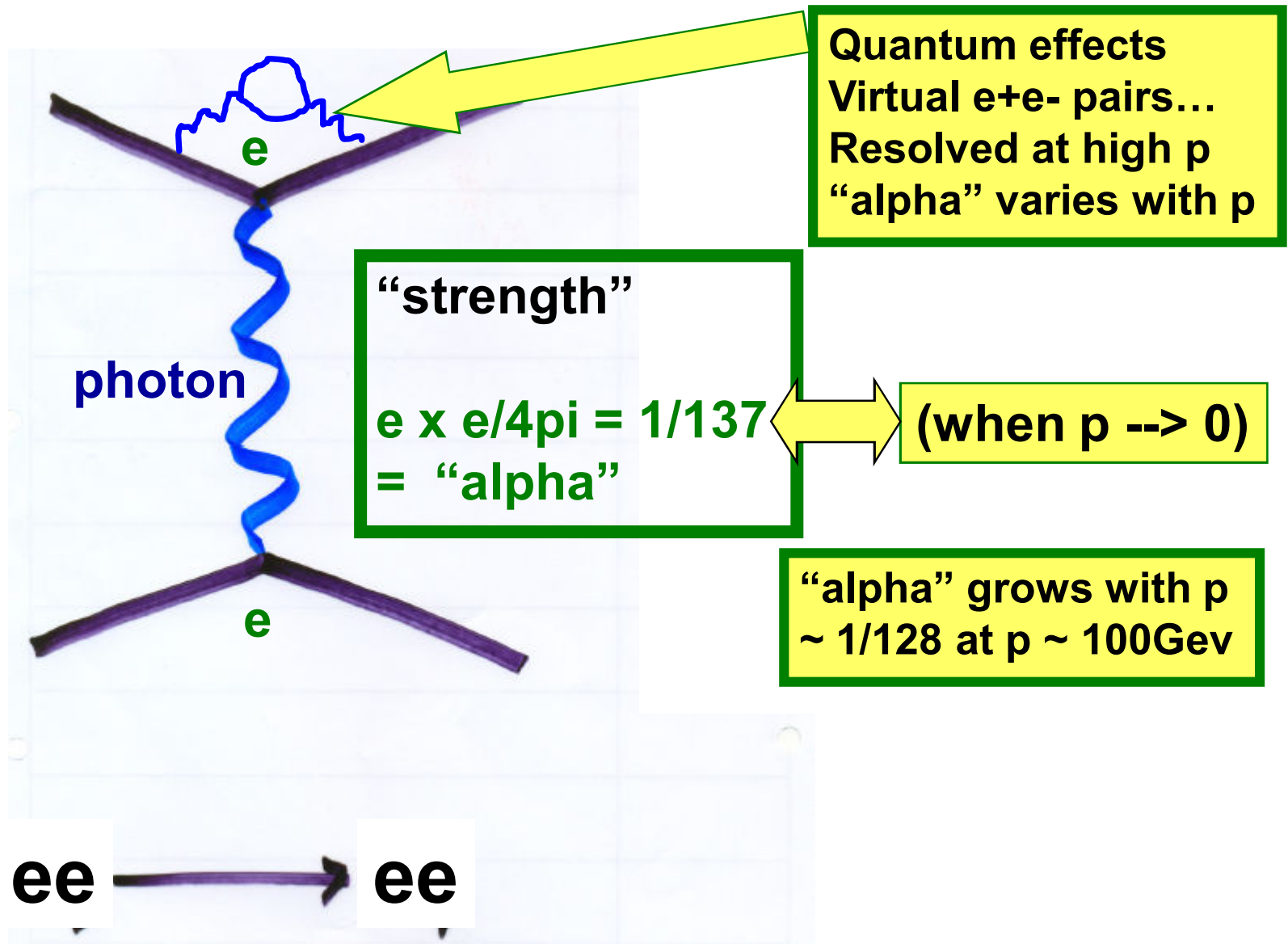
“strength”

$$g \times g/4\pi \sim 1/10 \\ = \text{“alpha}_s\text{”}$$

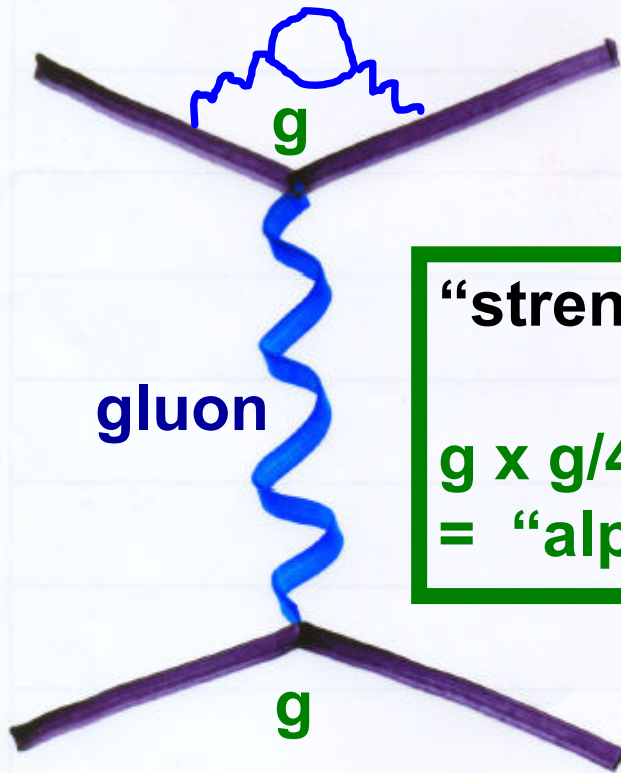


qq → qq

Feynman diagrams for electromagnetic interaction



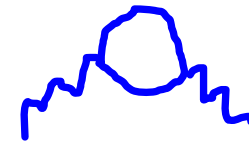
Feynman diagrams for chromomagnetic interaction



“strength”

$$g \times g/4\pi \sim 1/10 \\ = \text{“alpha}_s\text{”}$$

Like QED, QCD has



and also



qq → qq

“alpha_s” **falls** with p
= is **big** at **small** p
“STRONG” force
= **small** at **large** p
“pQCD” in HEPHys

Quantum Electrodynamics: QED

Electric charge  Atoms  Molecules

Interaction of electric charges and photons

“alpha” = $1/137$ small; perturbation; 12 places of decimals

Quantum Chromodynamics: QCD

Colour charge  Baryons  Nucleus

Interaction of colour charges and gluons

Quantum Electrodynamics: QED

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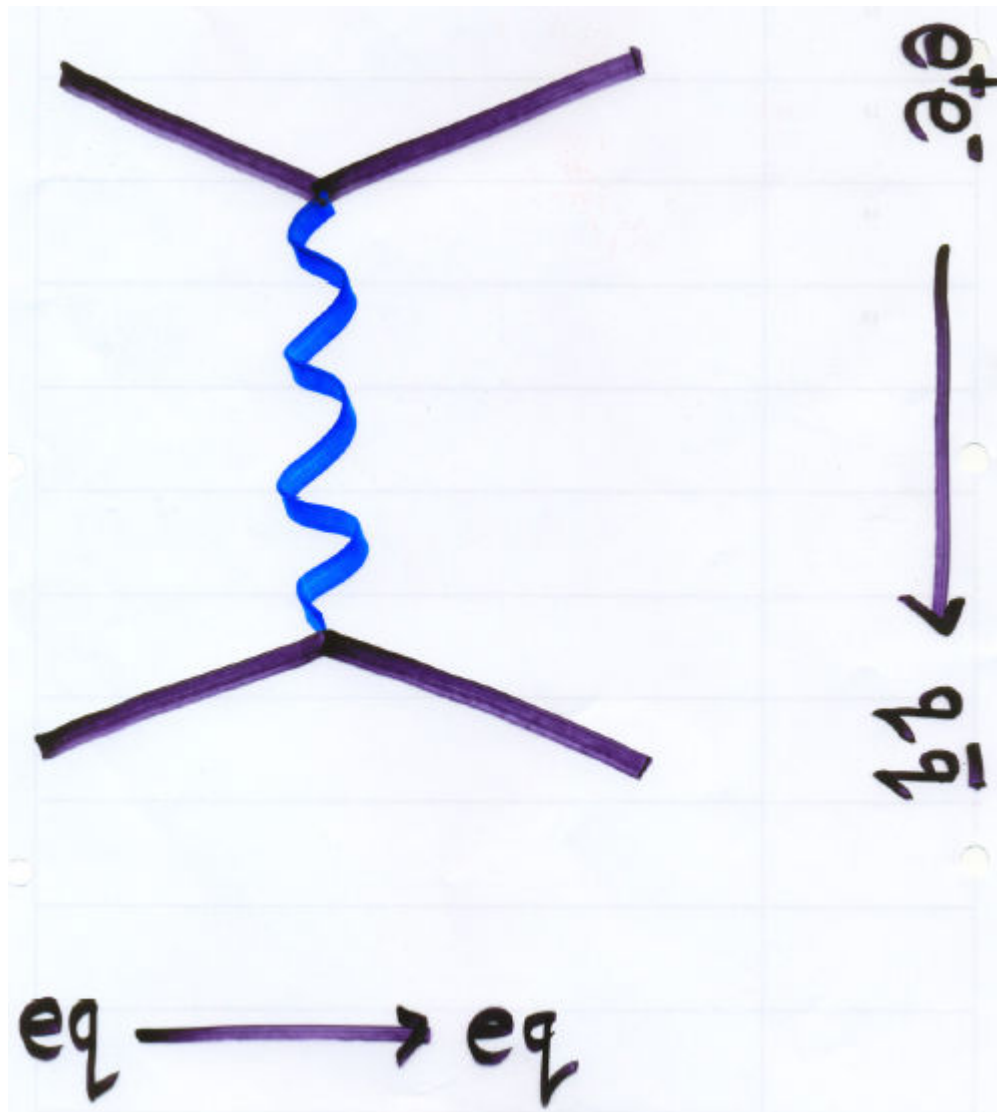
Interaction of colour charges and gluons

short distance: high momentum

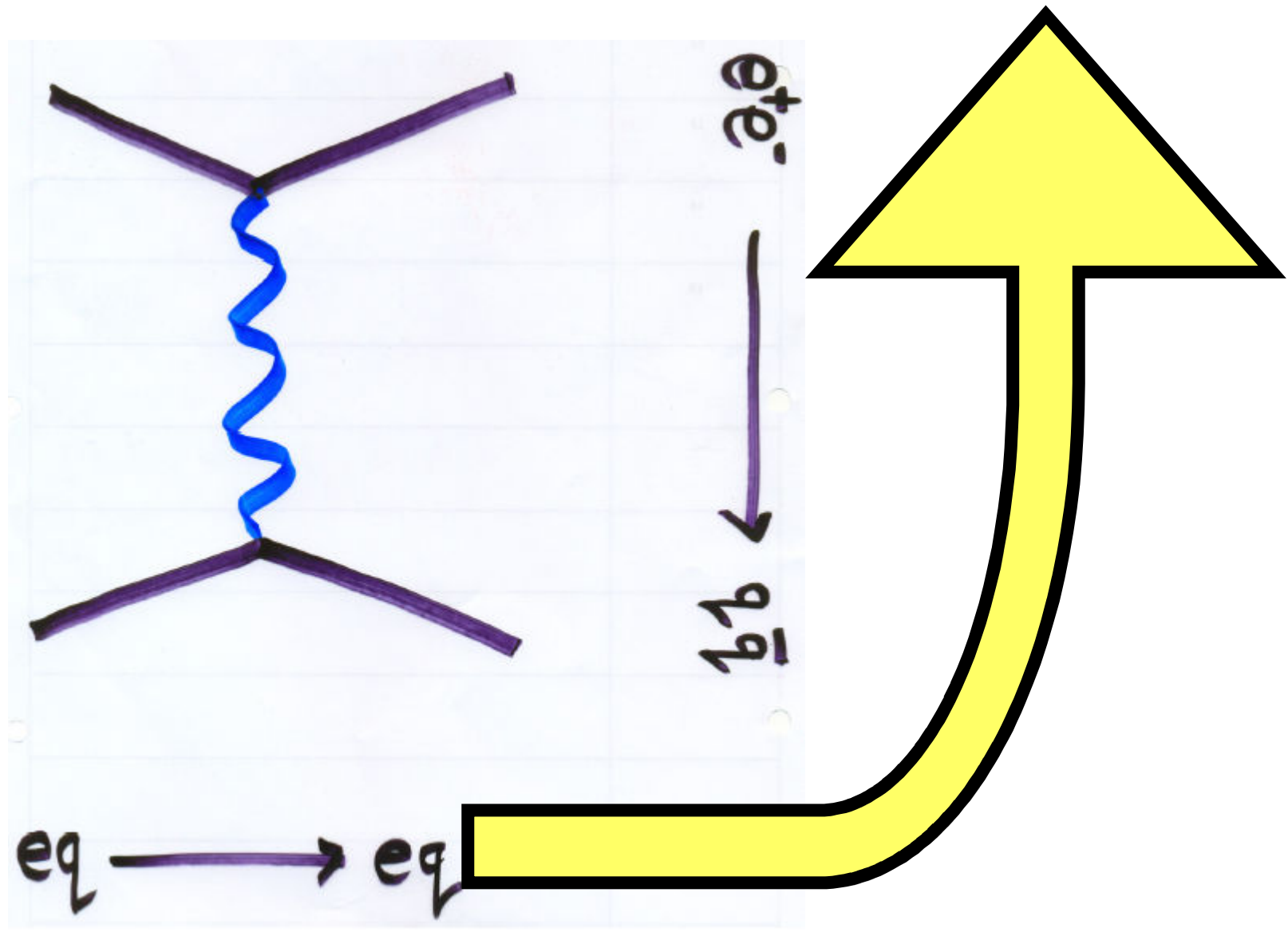
“alpha” = $1/10$ small; perturbation; “pQCD” v.precise

hadron size: low momentum “alpha” = large. lattice/models

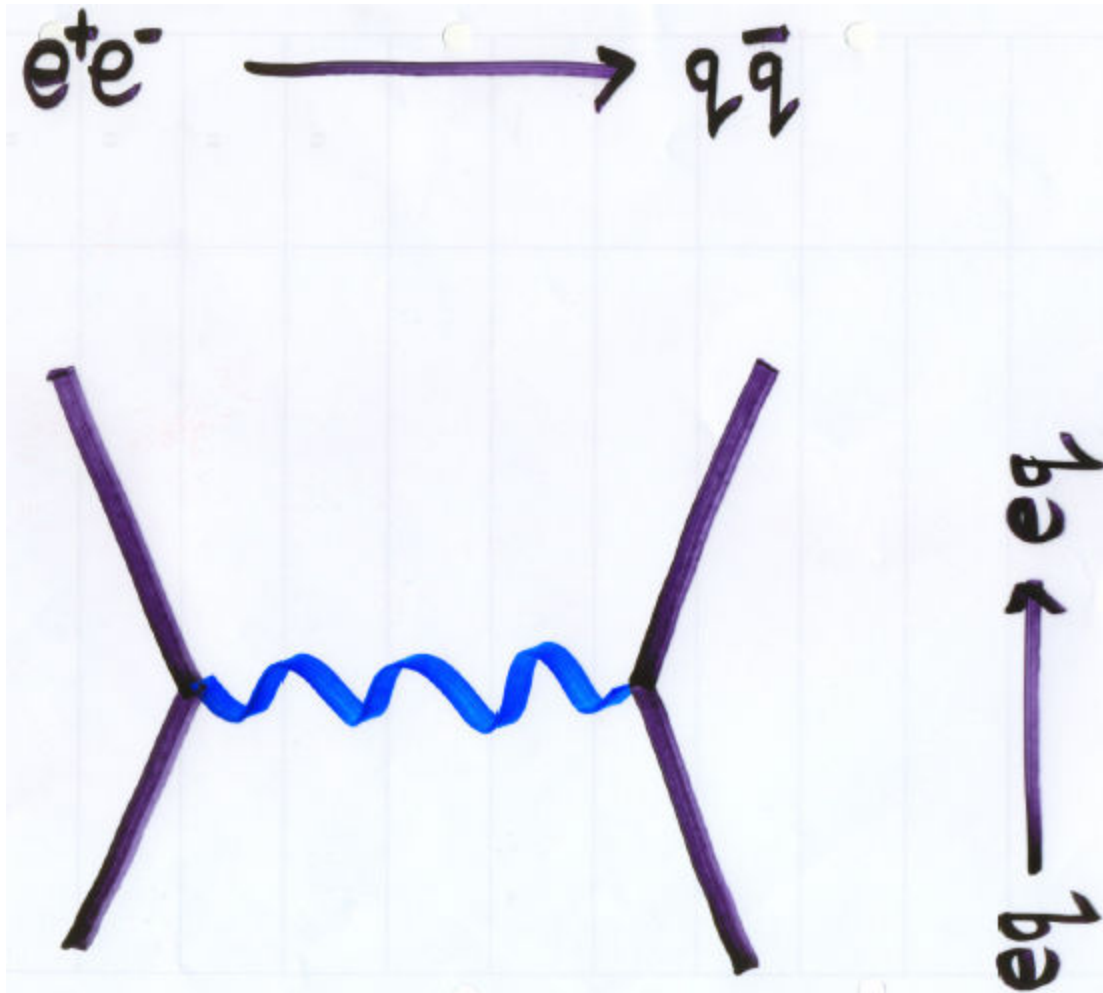
Feynman diagrams for electromagnetic interaction



Feynman diagrams for electromagnetic interaction



Feynman diagrams for electromagnetic interaction



FORCE CARRIERS



Photon

Emag

Gluon

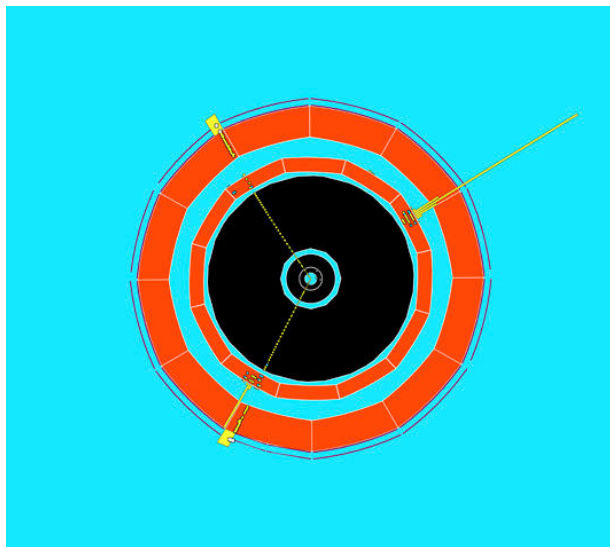
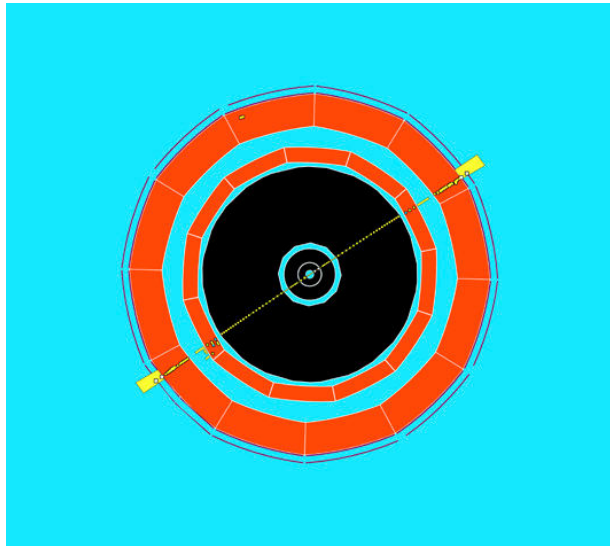
Strong

Feynman diagram for QCD analogous

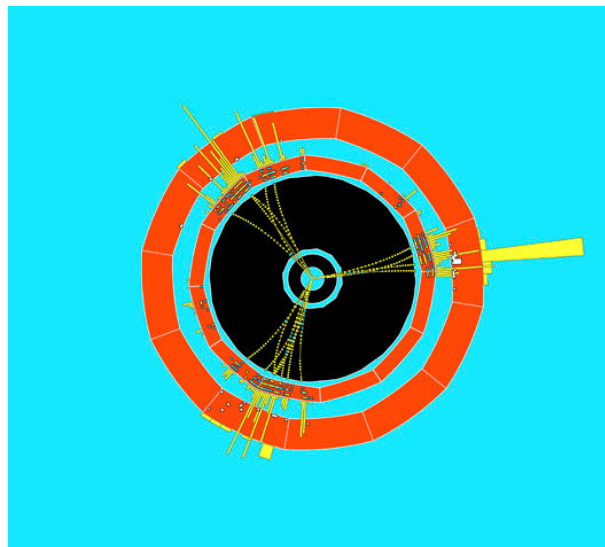
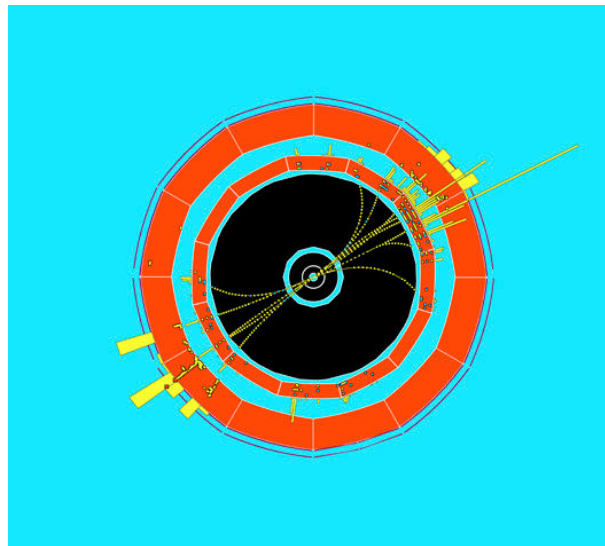
QED: electron; positron; photon

QCD: quark; antiquark; gluon

QED (electrons and photons)



QCD (quarks and gluons)



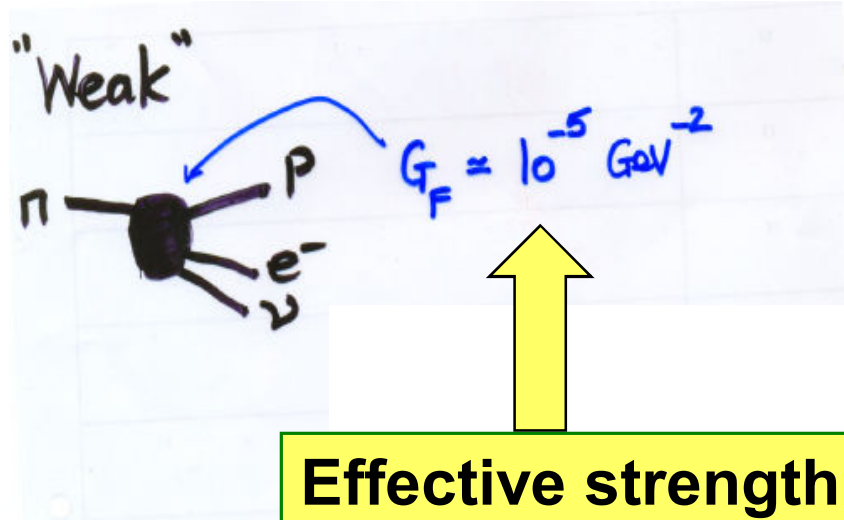
**LEP
@ CERN**

1989-2000

**The
Electroweak
Story**

Part 1: The WEAK Force

**Fermi model (1934)
of neutron
beta decay**



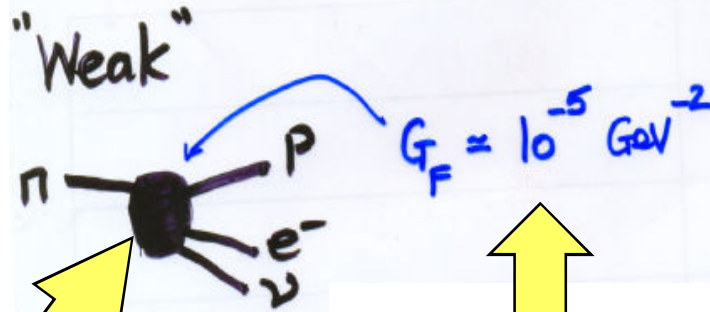
**Effective strength
“G_F” “Fermi constant”
deduced by observed
rate of beta decay.**

Empirical.

No theory (1934)

Small = feeble = “weak”

**Fermi model (1934)
of neutron
beta decay**



**Now look into the black box
with a modern high resolution
microscope and reveals
W-boson being exchanged**

**Effective strength
“G_F” “Fermi constant”
deduced by observed
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Empirical.

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FORCE CARRIERS



Photon

Emag

Gluon

Strong



p

Fermi
model

n

FORCE CARRIERS



Photon

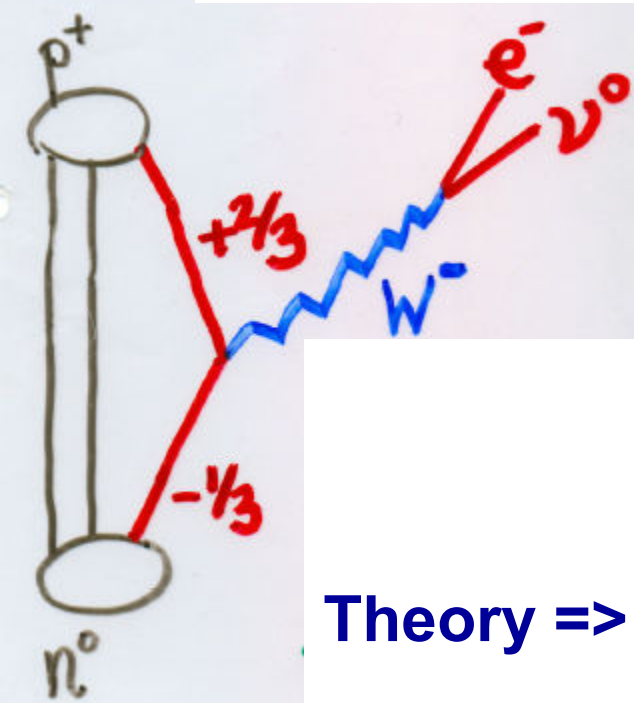
Emag

Gluon

Strong

W

Weak



Theory \Rightarrow Z; expt confirmed

FORCE CARRIERS



Photon

Emag

$m = 0$

Gluon

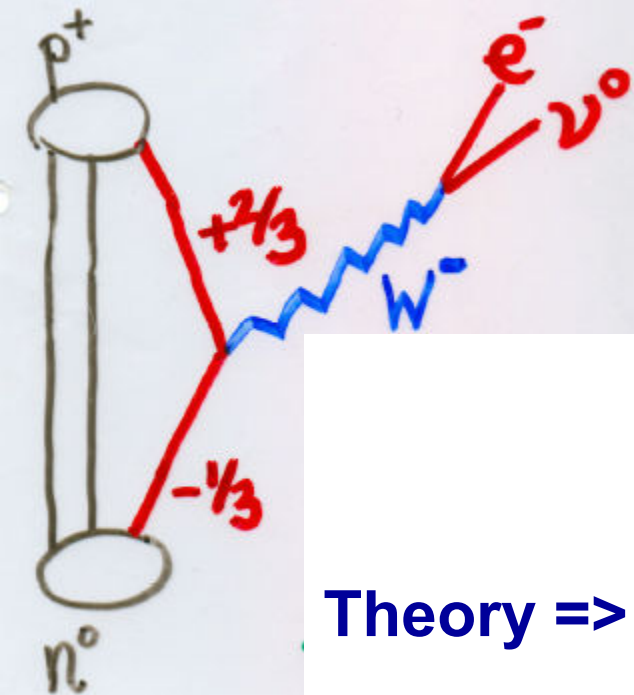
Strong

$m = 0$

W

Weak

$m = 80 \times \text{proton}$



Theory \Rightarrow Z; expt confirmed

FORCE CARRIERS



Photon

Emag

$m = 0$

Gluon

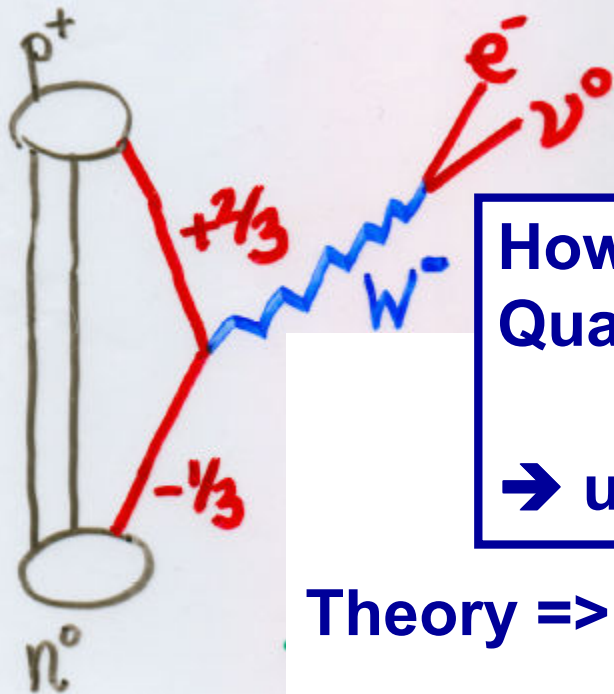
Strong

$m = 0$

W

Weak

$m = 80 \times \text{proton}$



How can 1 eject 80?

Quantum weirdness: Heisenberg uncertainty

→ unlikely → “weak”

Theory \Rightarrow Z; expt confirmed

**The
Electroweak
Story**

Part 2: History and Unity

“Weak force as Electromagnetism in disguise”

The Electroweak Story

1864

Maxwell unifies electricity and magnetism
→ electromagnetism

100 years later

Glashow Salam Weinberg propose
unification of Electromagnetic and weak
electro-weak

They use Higgs mechanism

→ predict force carriers

→ masses predicted. $W^+ W^- Z^0$ $(m_\gamma = 0)!$

1983-84

W and Z particles found by CERN
experiments UA1 + UA2



1984

Rubbia + van der Meer → Nobel Prize

1989-95



Tune $E_+ + E_- = M_Z c^2 = 91 \text{ GeV}$

LEP 4 experiments
20 million Z^0

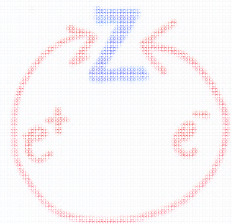
Z unstable. Decays "democratically" to
 $q\bar{q}$ e^+e^- $\mu^+\mu^-$ $\tau^+\tau^-$
 $\nu_e\bar{\nu}_e$ $\nu_\mu\bar{\nu}_\mu$ $\nu_\tau\bar{\nu}_\tau$



$\frac{1}{\text{Life}} \sim \# \text{ of holes}$
 $\Rightarrow \# \text{ of decay paths}$

Perfect match if $\# \nu = 3$

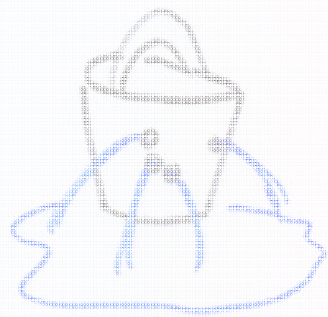
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life $\sim \frac{1}{\Gamma}$ of holes
 $\Rightarrow \frac{1}{\Gamma}$ of decay paths

Perfect match if $\frac{1}{\Gamma} = 3$

Z Lifetime

Heisenberg Uncertainty Principle

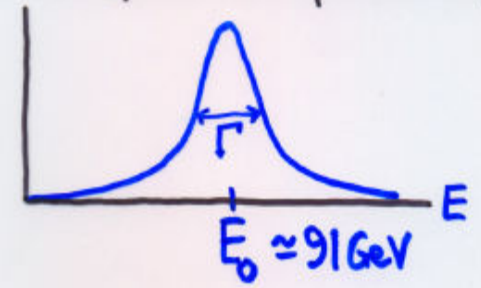
$$\Delta E \Delta t \approx \hbar \approx 6 \times 10^{-25} \text{ GeV sec}$$

example

$\Delta t =$ lifetime of unstable particle

$$\Rightarrow \Delta E = \Delta M c^2 = \frac{6 \times 10^{-25} \text{ GeV}}{\Delta t \text{ (sec)}}$$

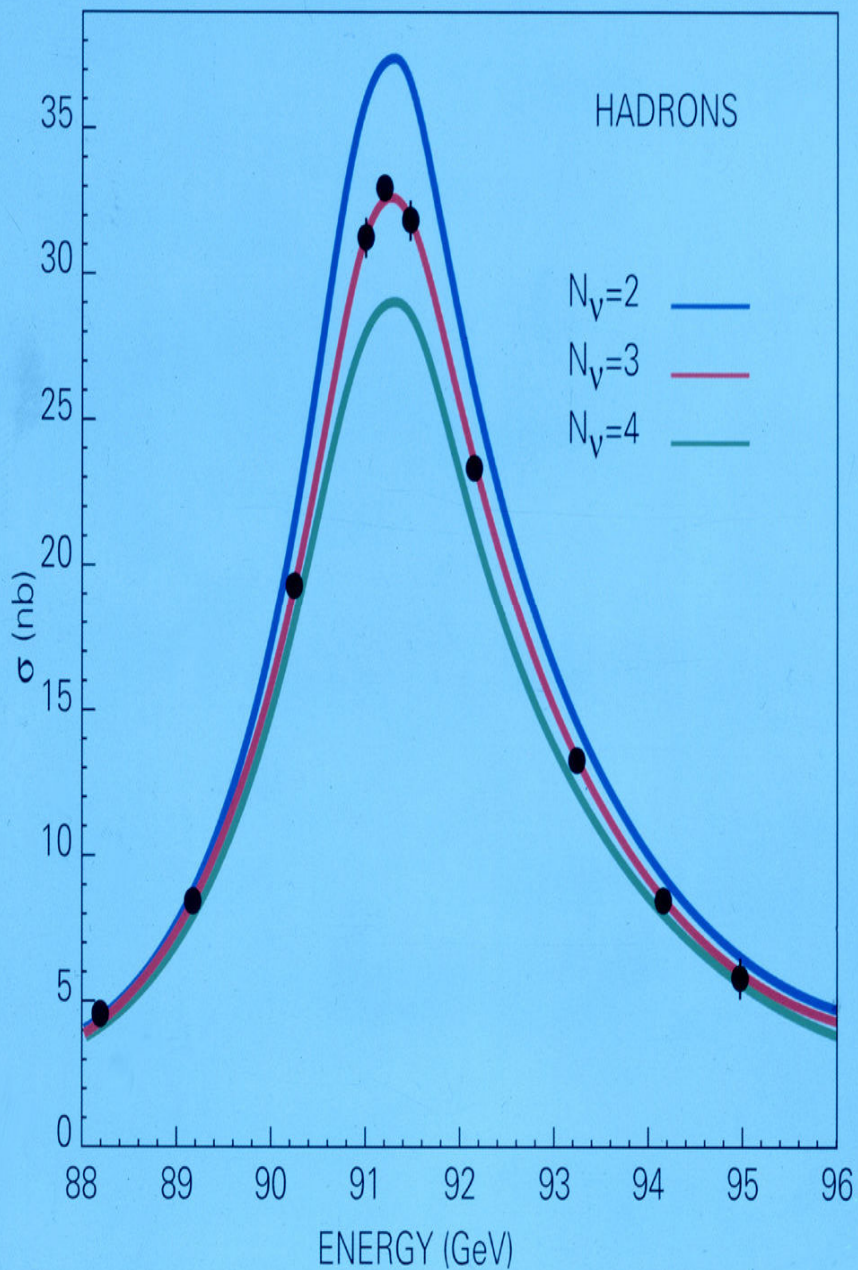
$e^+e^- \rightarrow Z$ (production probability)



$$\Gamma = \Delta E = 2.5 \text{ GeV}$$

$$\Rightarrow \text{Lifetime} = 10^{-25} \text{ sec}$$

ALEPH



Z Lifetime

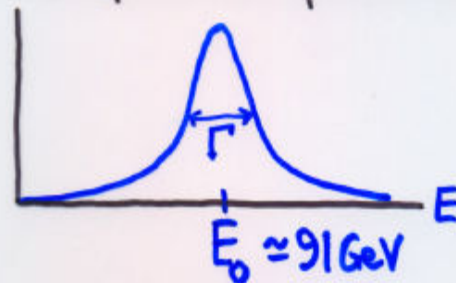
Heisenberg Uncertainty Principle

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example Δt = lifetime of unstable particle

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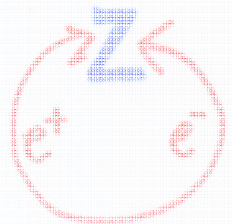
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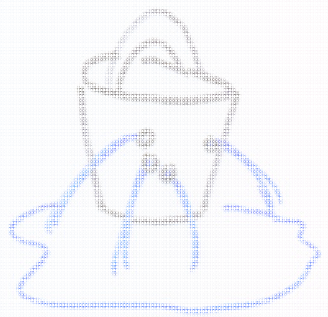
1989-95



Tune $E_+ + E_- = M_Z c^2 = 91 \text{ GeV}$

LEP 4 experiments
20 million Z^0

Z unstable. Decays "democratically" to
 $q\bar{q}$ e^+e^- $\mu^+\mu^-$ $\tau^+\tau^-$
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life $\sim \#$ of holes
 $\Rightarrow \#$ of decay paths

Perfect match if $\# \nu = 3$

Z Lifetime

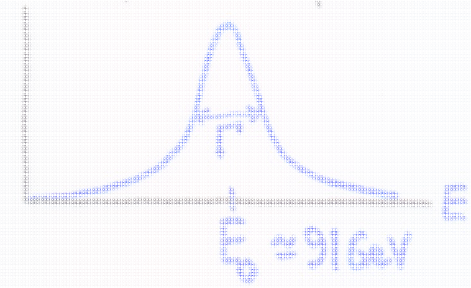
Heisenberg Uncertainty Principle

$$\Delta E \Delta t \approx \hbar = 6 \times 10^{-26} \text{ GeV sec}$$

example $\Delta t =$ lifetime of unstable particle

$$\Rightarrow \Delta E = \Delta M c^2 = \frac{6 \times 10^{-26} \text{ GeV}}{\Delta t (\text{sec})}$$

$e^+e^- \Rightarrow Z$ (production probability)



$$\Gamma = \Delta E = 2.5 \text{ GeV}$$

$$\Rightarrow \text{Lifetime} = 10^{-26} \text{ sec}$$

1996-2000

LEP $e^+(100 \text{ GeV}) + e^-(100 \text{ GeV}) \rightarrow W^+W^-$

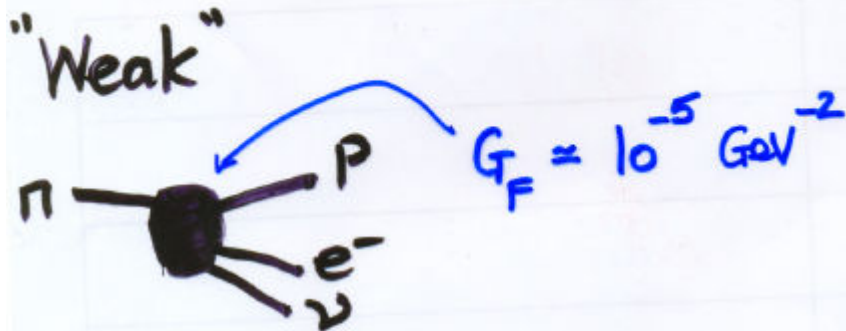
+ look for Higgs

The Electroweak Story

Part 3: Unity

“Weak force as Electromagnetism in disguise”

**Beta decay (weak interaction):
Feynman diagram for Fermi's original model**



"weak strength"

$1/100,000 \text{ GeV}^2$

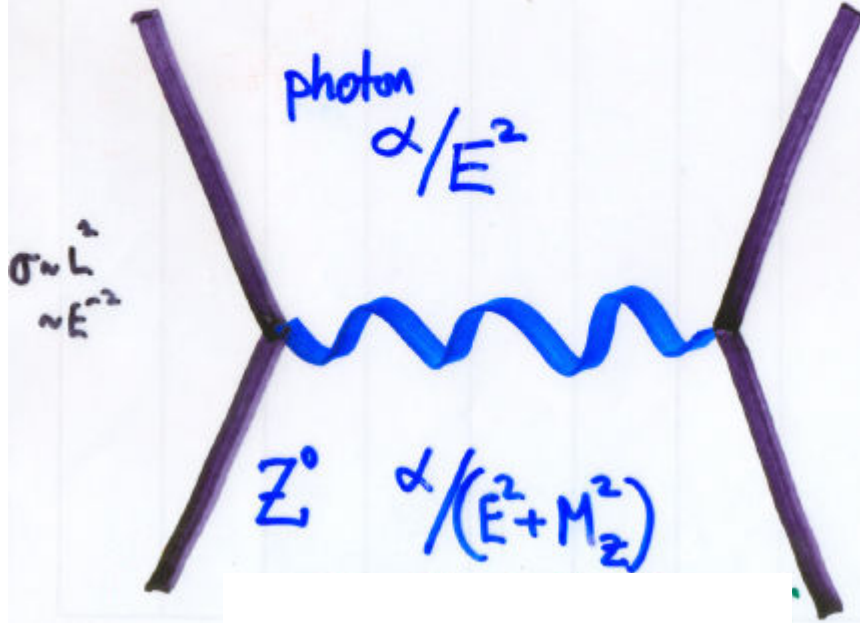


contrast with

"emag strength"

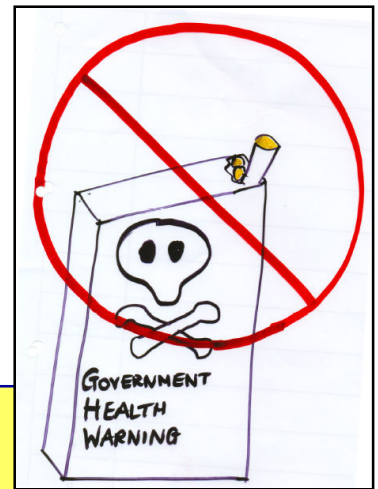
$e \times e/4\pi = 1/137$
 $= \text{"alpha"}$

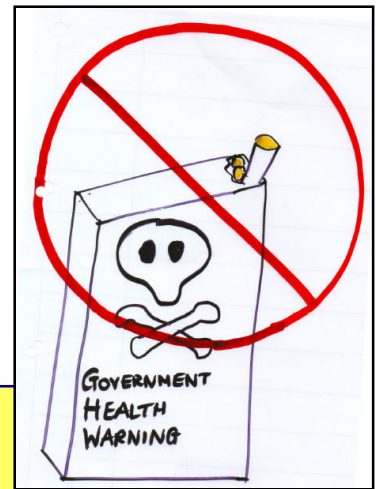
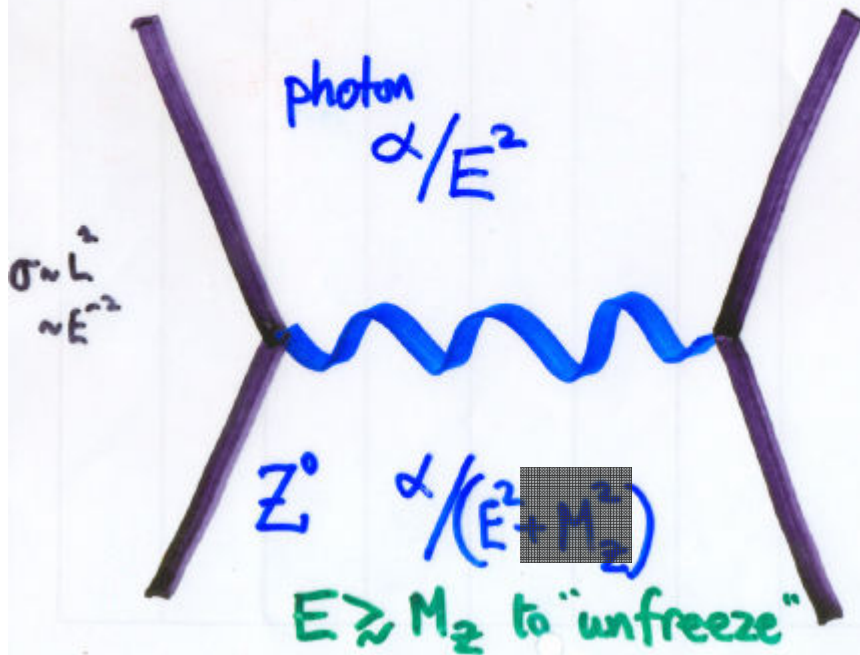
Notice a number (e.m.) but
dimensions of $1/\text{GeV}^2$ (weak).....



Feynman rules:

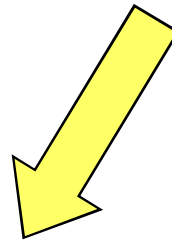
If energy E flows through
 the transmitted "virtual"
 particle (photon; Z)
 it costs $1/(E^2+M^2)$



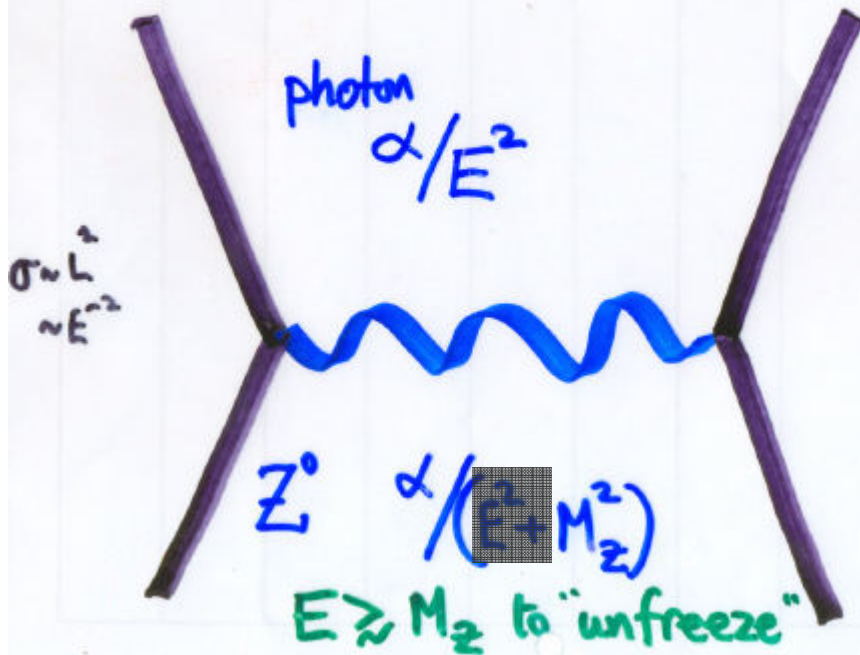


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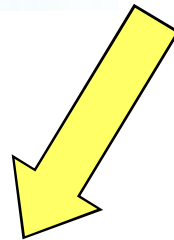


If $E \gg M$ the cost is $1/E^2$like the case of the photon



Feynman rules:

If energy E flows through
 the transmitted "virtual"
 particle (photon; Z)
 it costs $1/(E^2 + M^2)$



If $E \gg M$ the cost is $1/E^2$...like the case of the photon

If $E \ll M$ the cost is $1/M^2$

$$\sigma \sim L^2$$
$$\sim E^{-2}$$

Fermi model

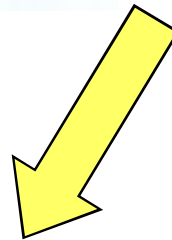
photon
 $\propto 1/E^2$

$Z^0 \propto 1/(E^2 + M_Z^2)$

$E \gg M_Z$ to "unfreeze"

Feynman rules:

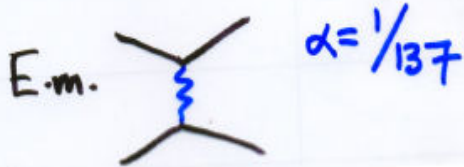
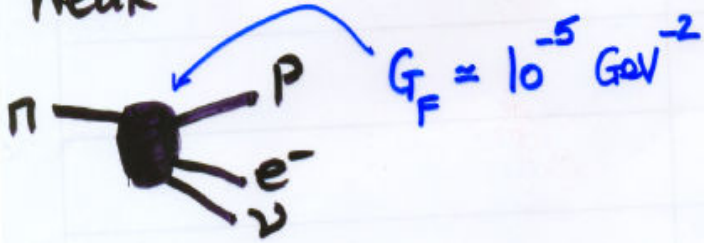
If energy E flows through the transmitted "virtual" particle (photon; Z) it costs $1/(E^2 + M^2)$



If $E \gg M$ the cost is $1/E^2$...like the case of the photon

If $E \ll M$ the cost is $1/M^2$

"Weak"

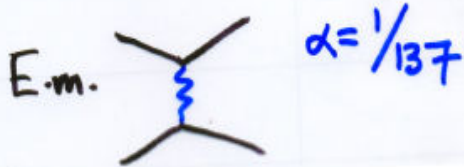
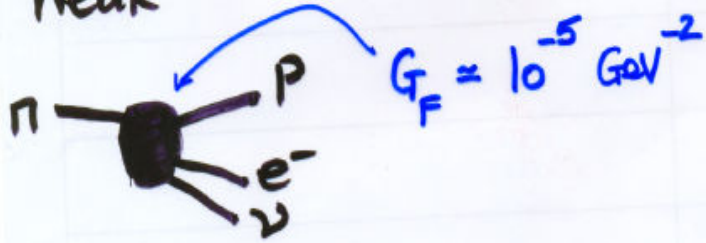


"weak strength"

$$1/100,000 \text{ GeV}^2$$

$$= 1/137 \times 1/(28 \text{ GeV})^2$$

"Weak"

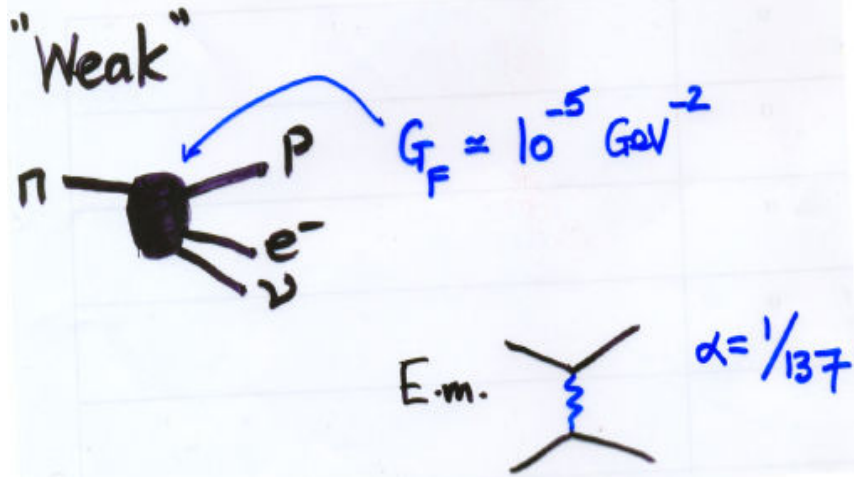


"weak strength"

$$1/100,000 \text{ GeV}^2$$

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"weak" has fundamentally electromagnetic strength if $m \sim 30 \text{ GeV}$



"weak strength"

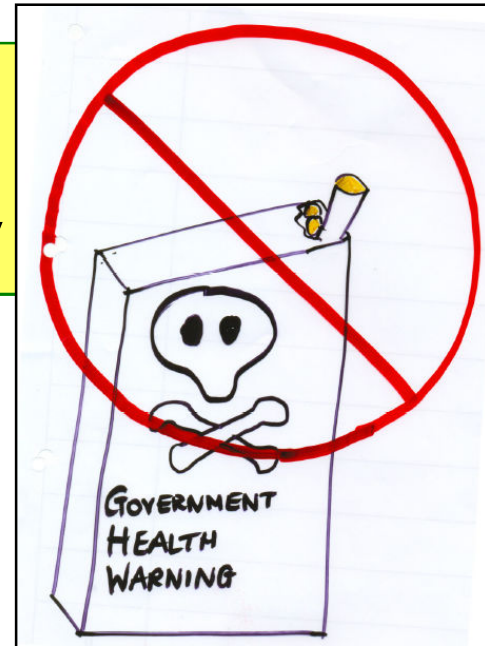
$1/100,000 \text{ GeV}^2$

$= 1/137 \times 1/(28 \text{ GeV})^2$

"weak" has fundamentally electromagnetic strength if $m \sim 30 \text{ GeV}$

More carefully: root 2; parity violation;
 SU2 x U1; Weinberg angle..
 requires $m(W) \sim 80 \text{ GeV}$; $m(Z) \sim 90 \text{ GeV}$

Experimentally verified!!



At the heart of the Sun:



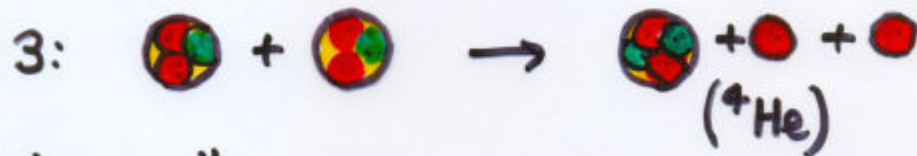
 **Proton**

 **neutron**

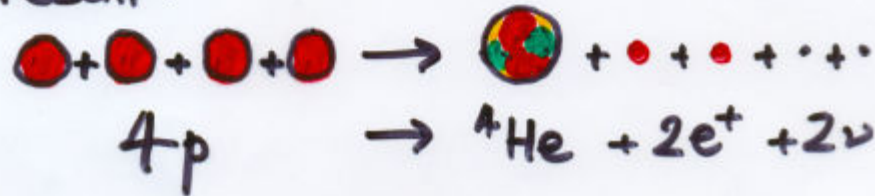
 **positron**

 **neutrino**

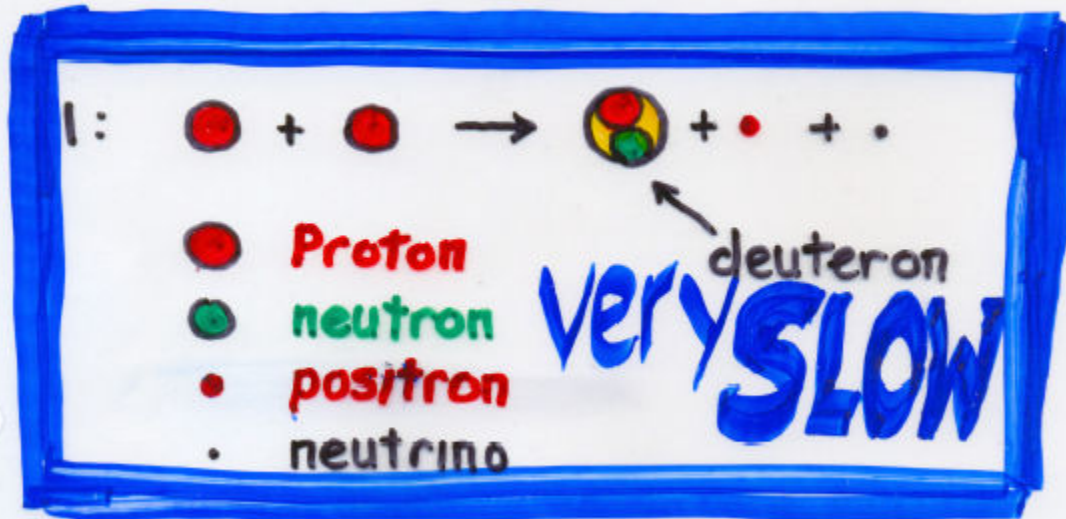
 deuteron



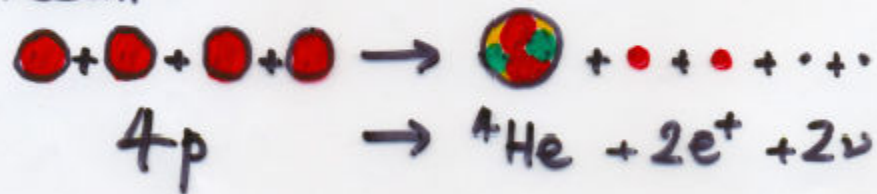
Net result:



At the heart of the Sun:

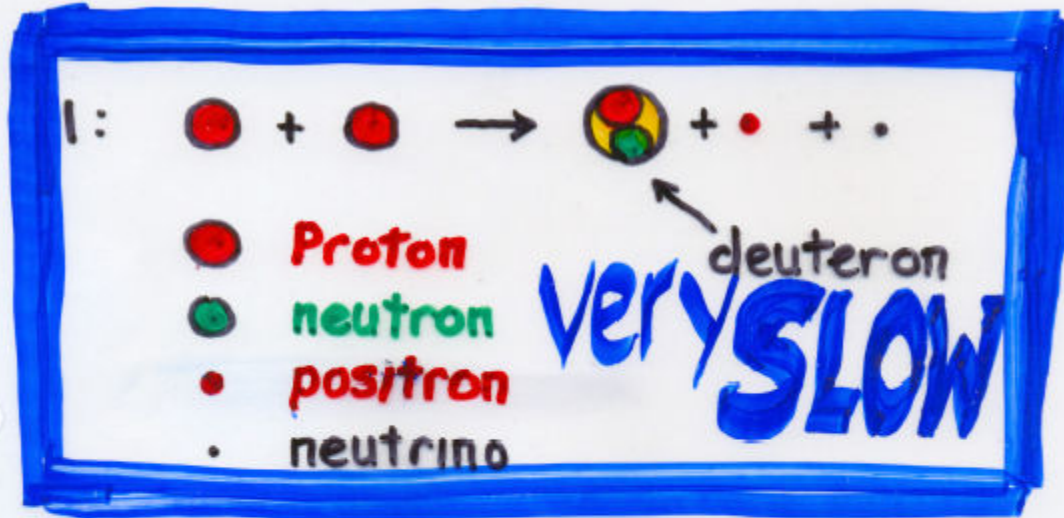


Net result:

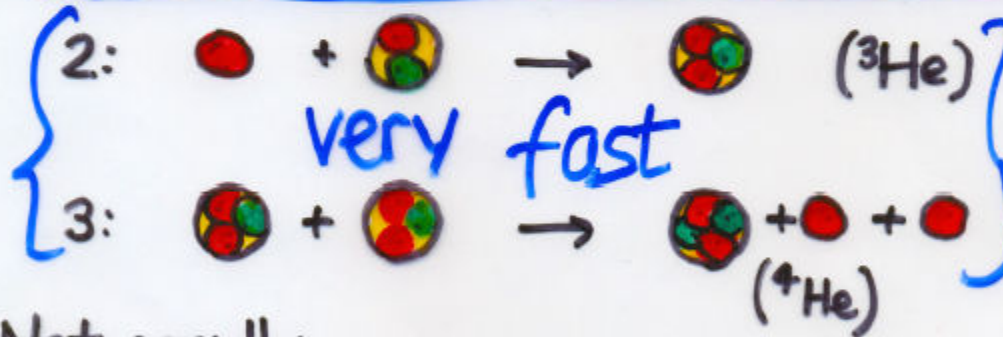


$\Delta E = \Delta M c^2: {}^4\text{He} + 4p \approx 28\text{MeV}$

At the heart of the Sun:

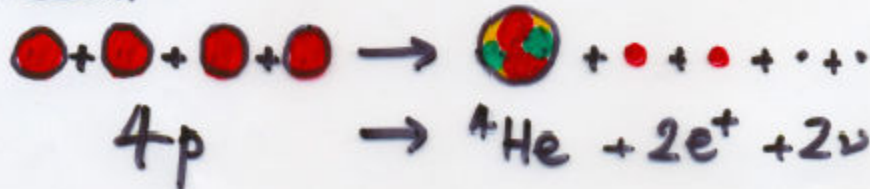


WEAK



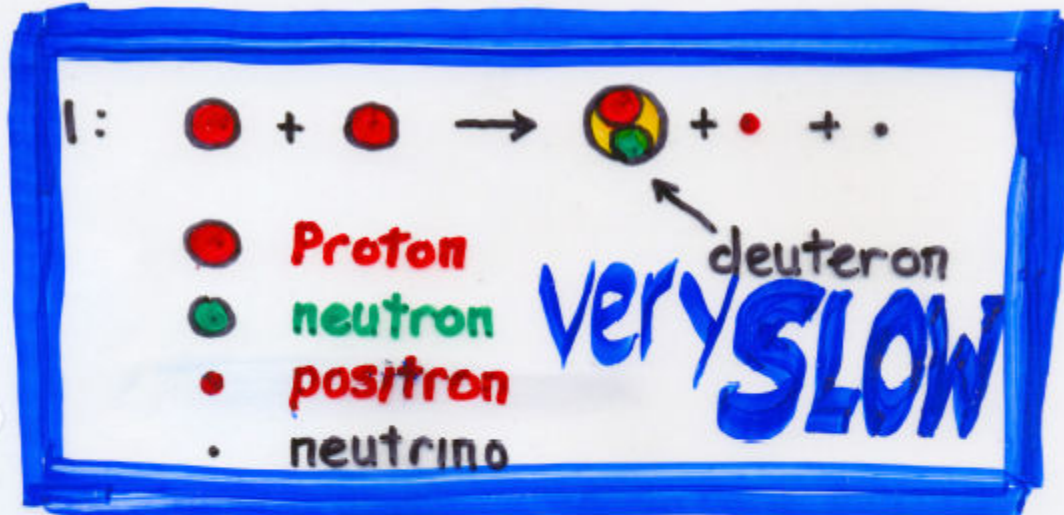
STRONG

Net result:



$\Delta E = \Delta M c^2: {}^4\text{He} + 4p \approx 28\text{MeV}$

At the heart of the Sun:

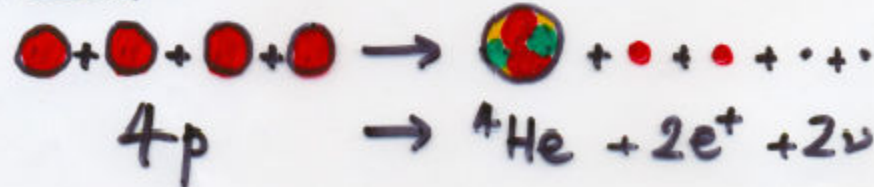


WEAK



STRONG

Net result:



$\Delta E = \Delta M c^2: {}^4\text{He} + 4p \approx 28\text{MeV}$

→ why sun has shone for 5 Byr...
→ Intelligent life developed

The weak force is feeble in the Sun ..

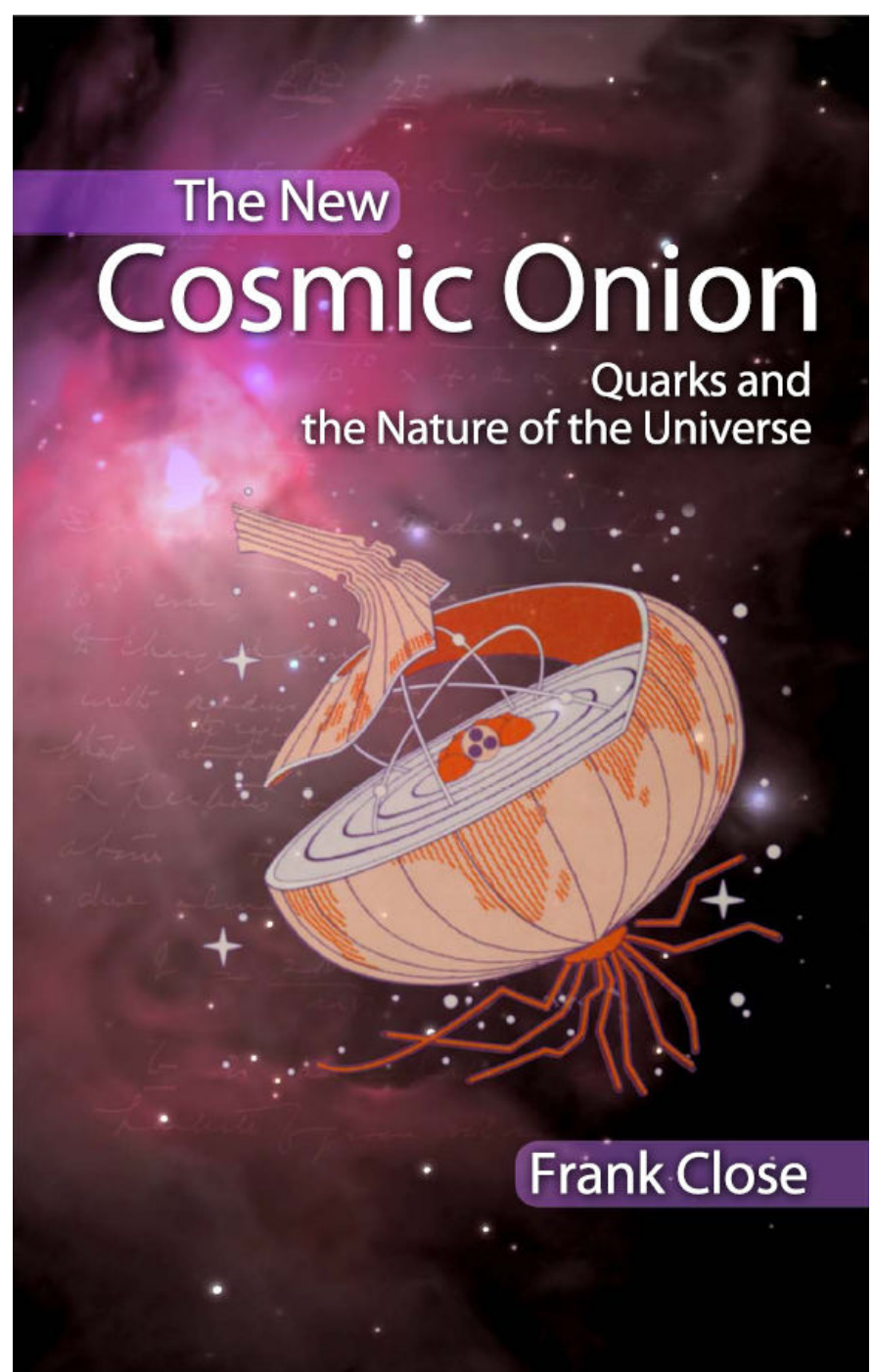
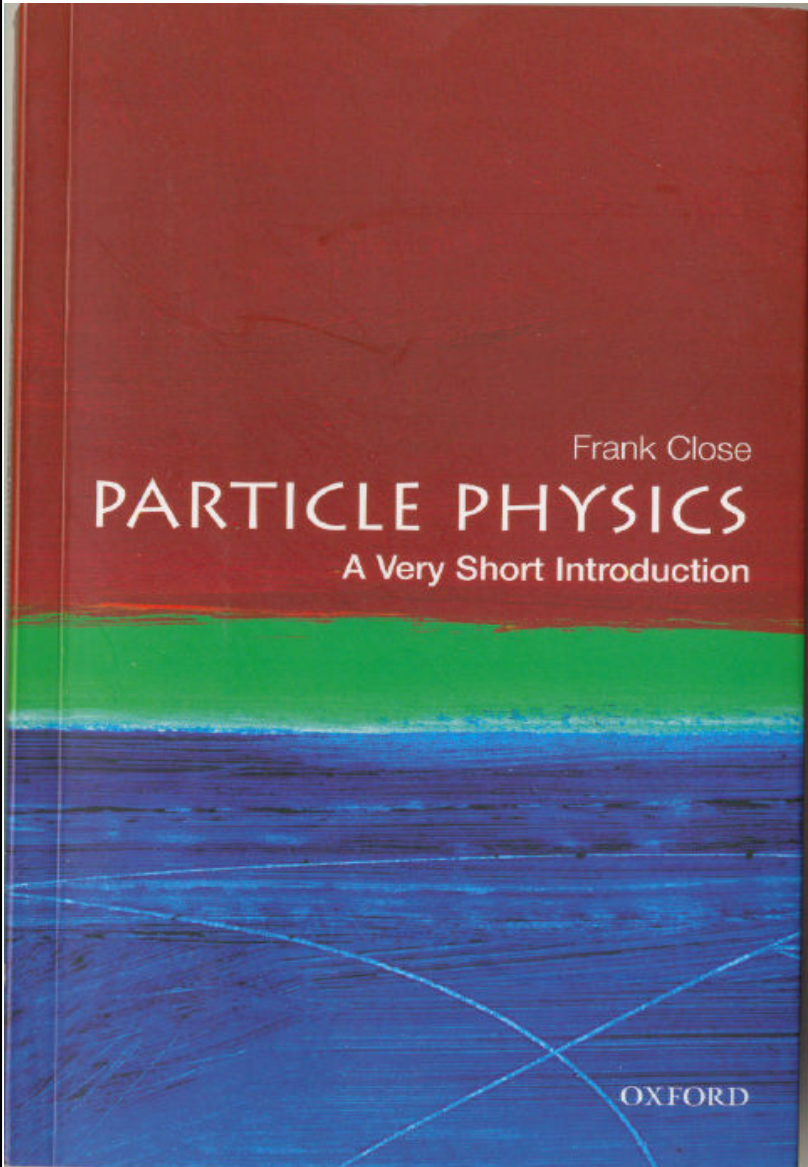
..because $10,000,000\text{K} \sim 1 \text{ keV} \ll 80 \text{ GeV}$

...this is why the sun has stayed active long enough for us to have evolved and be having this conversation.

→ We exist because $m(W)$ is not zero

→ Mass matters

A Very Short Introduction



1960s QUARKS

STRONG force gives them

n^0



p^+

