



16 T $\cos\theta$ DIPOLE MECHANICAL ANALYSIS

STEFANIA FARINON

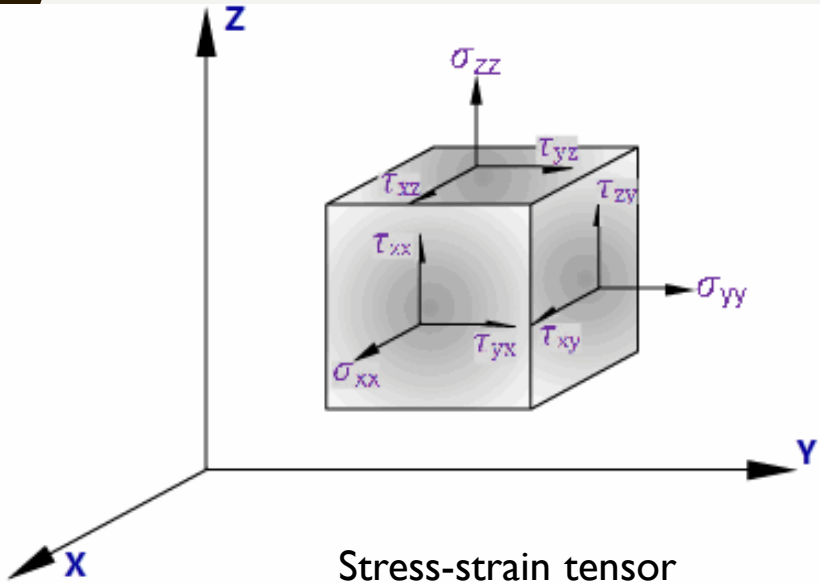
ON BEHALF OF INFN TEAM:

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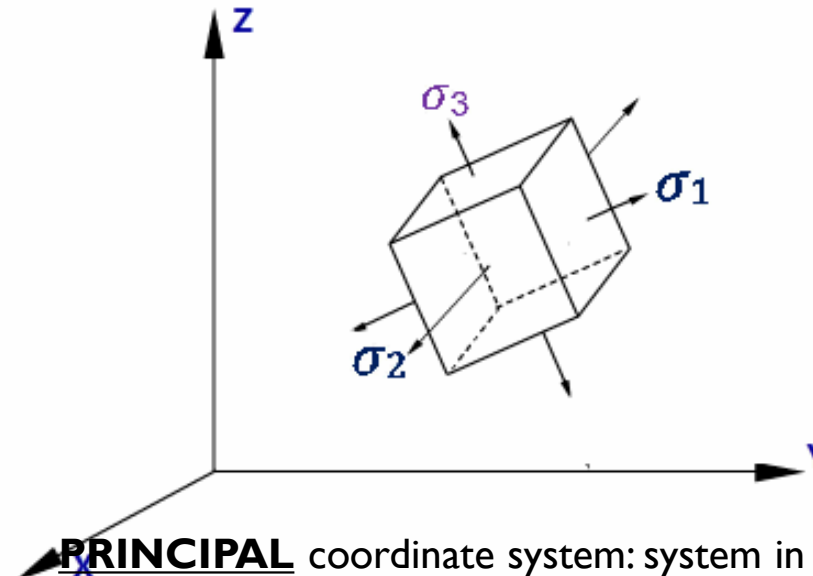
OVERVIEW

- Principal stresses and failure criteria
- 2D model: plain strain vs plain stress
- 2D mechanical optimization
- $\text{Cos}\theta$ 2D models:
- CONFIGURATION I – vertical cut
- CONFIGURATION II – horizontal cut
- CONFIGURATION III – hybrid
- CONCLUSIONS

PRINCIPAL STRESSES



Stress-strain tensor
In cartesian coordinate system



PRINCIPAL coordinate system: system in which the SS tensor is **DIAGONAL**

$$\sigma = \begin{Bmatrix} \sigma_{xx} & \tau_{xy} & \tau_{xz} \\ \tau_{yx} & \sigma_{yy} & \tau_{yz} \\ \tau_{zx} & \tau_{zy} & \sigma_{zz} \end{Bmatrix} = \begin{Bmatrix} \sigma_1 & 0 & 0 \\ 0 & \sigma_2 & 0 \\ 0 & 0 & \sigma_3 \end{Bmatrix}$$

- The principal stress σ_1 , σ_2 and σ_3 , defined for each single element, are those in which the stress-strain tensor is diagonal ($\sigma_3 < \sigma_2 < \sigma_1$).

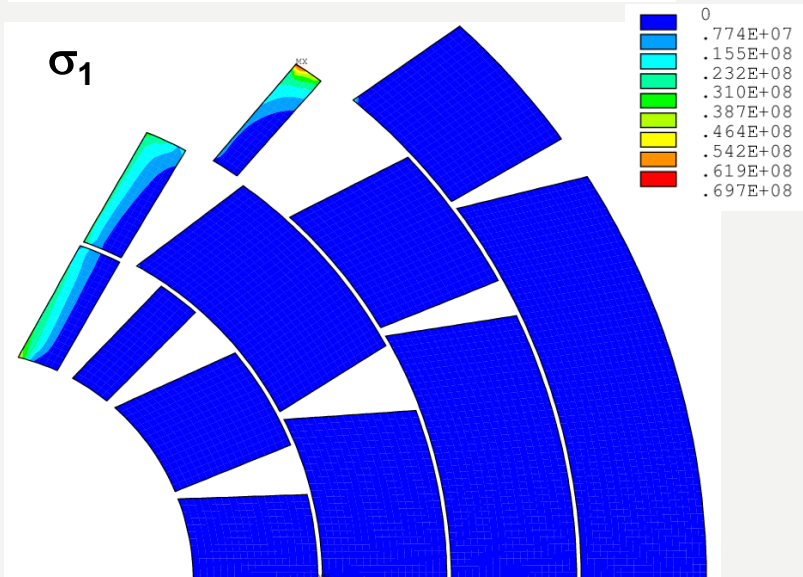
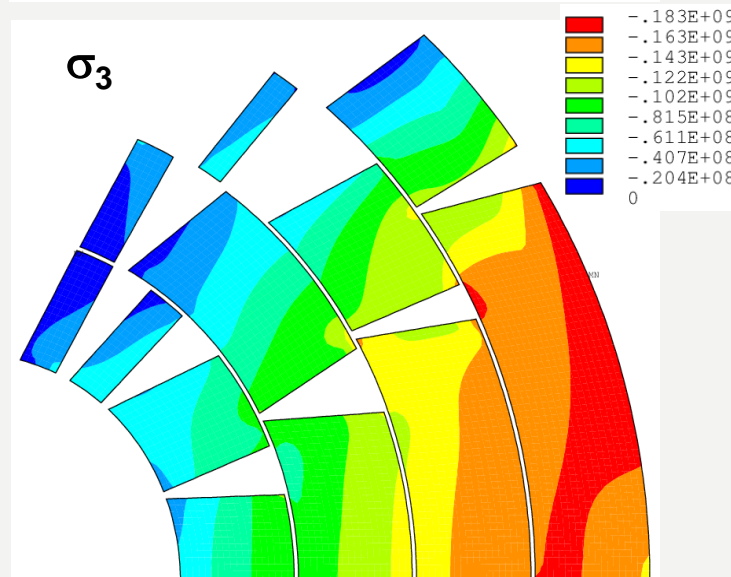
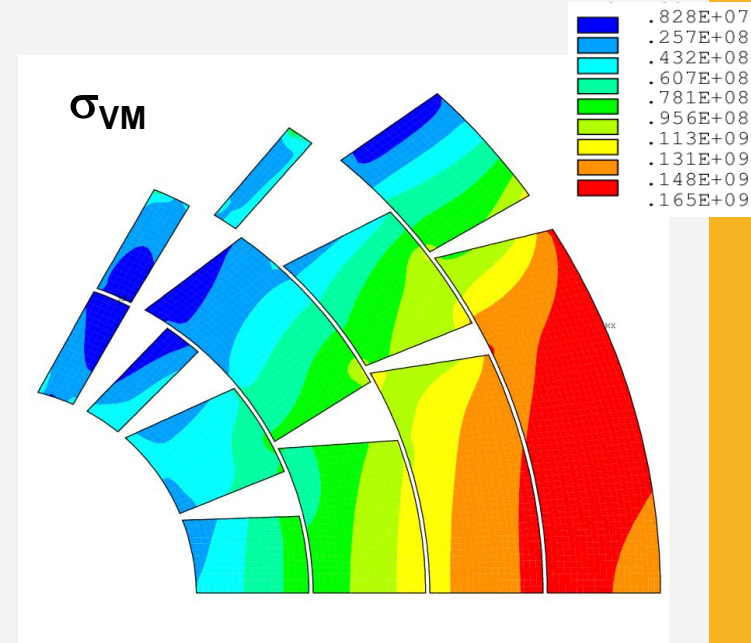
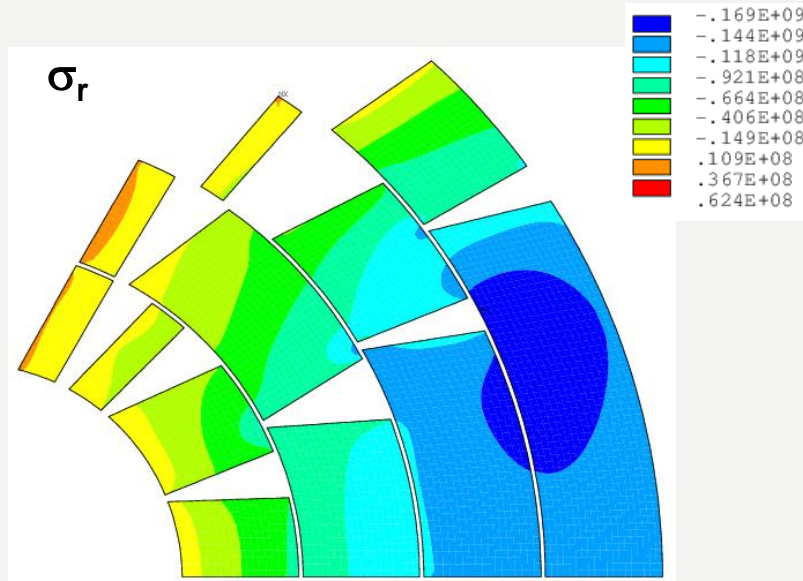
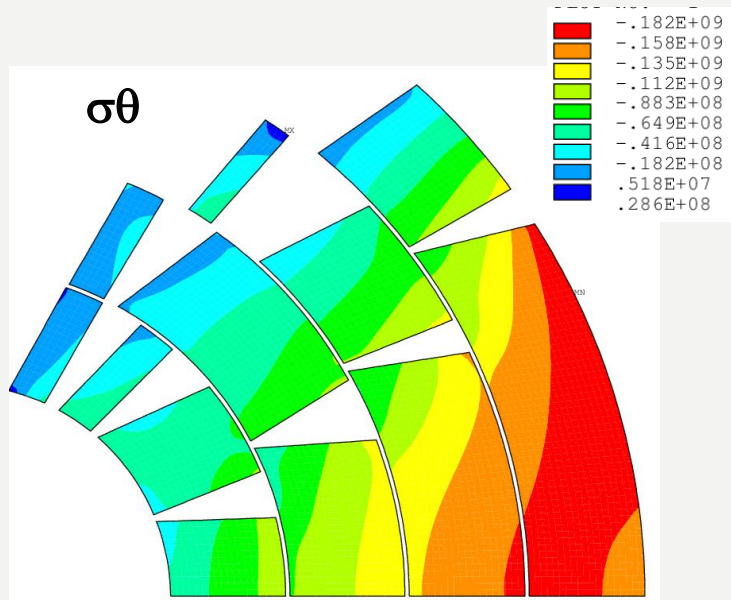
- $\sigma_3 \sim \sigma_x$ in block coil geometry

- $\sigma_3 \sim \sigma_\theta$ in $\cos\theta$ geometry

- Von Mises stress is defined as:

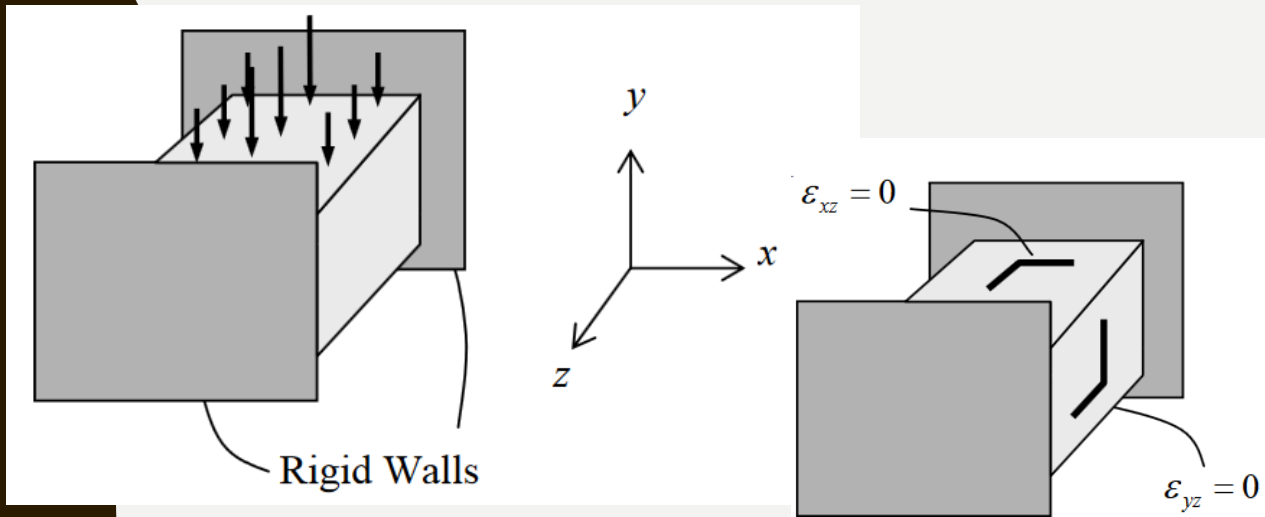
$$\sigma_v = \sqrt{\frac{(\sigma_1 - \sigma_2)^2 + (\sigma_2 - \sigma_3)^2 + (\sigma_3 - \sigma_1)^2}{2}}$$

STRESSES



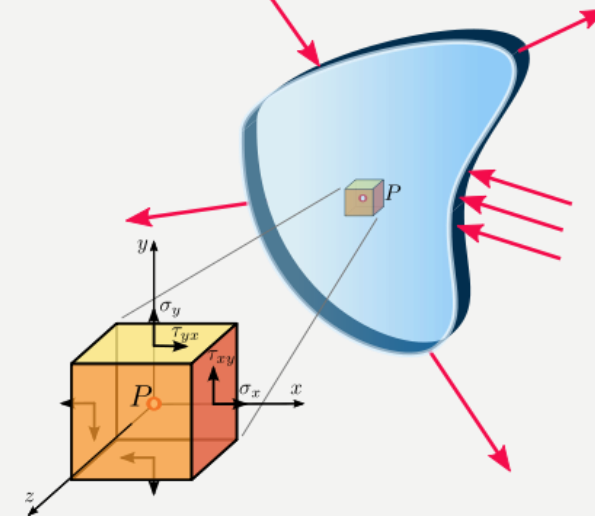
PLANE STRESS VS PLANE STRAIN

Plane strain



Plane strain is a stress state that varies only in the X and Y directions. The strain in the Z direction is always zero, as are the XZ and YZ shear strains, since the boundaries are fixed.

Plane stress



Plane stress is a stress state that varies only in the X and Y directions. The stress in the Z direction is always zero, as are the XZ and YZ shear stresses. Plane stress is generally used on flat, thin structures, where the deformation is assumed to be solely in the plane of the structure.

Plain stress approximation is less conservative but more compatible with 3D simulation results.

2D MECHANICAL OPTIMIZATION

Cables undergo degradation if:

- stress on conductors > 150 MPa @room temperature;
- stress on conductors > 200 MPa @cold;
- stress on conductors > 150 MPa @cold after energization in the high field region \rightarrow attention must be given in particular to first layers.
- Tensile stress on the iron yoke at 4 K < 200 Mpa.
- Contact pressure Ti pole-conductors > 2 MPa after energization at 16T.

Critical Current Measurements of High- J_c Nb₃Sn Rutherford Cables under Transverse Compression

B. Bordini, P. Alknes, A. Ballarino, L. Bottura, L. Oberli

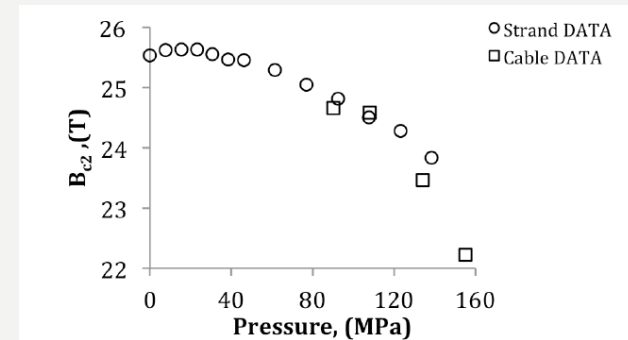
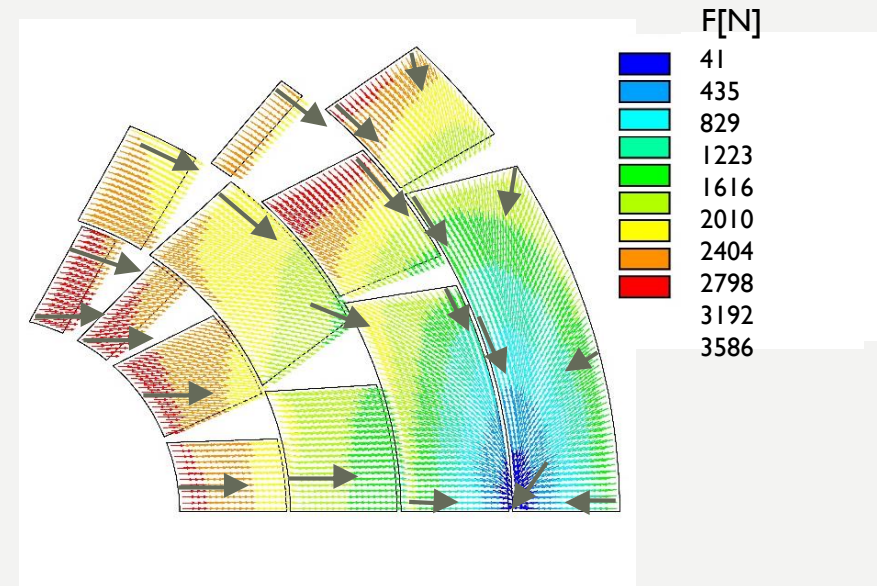


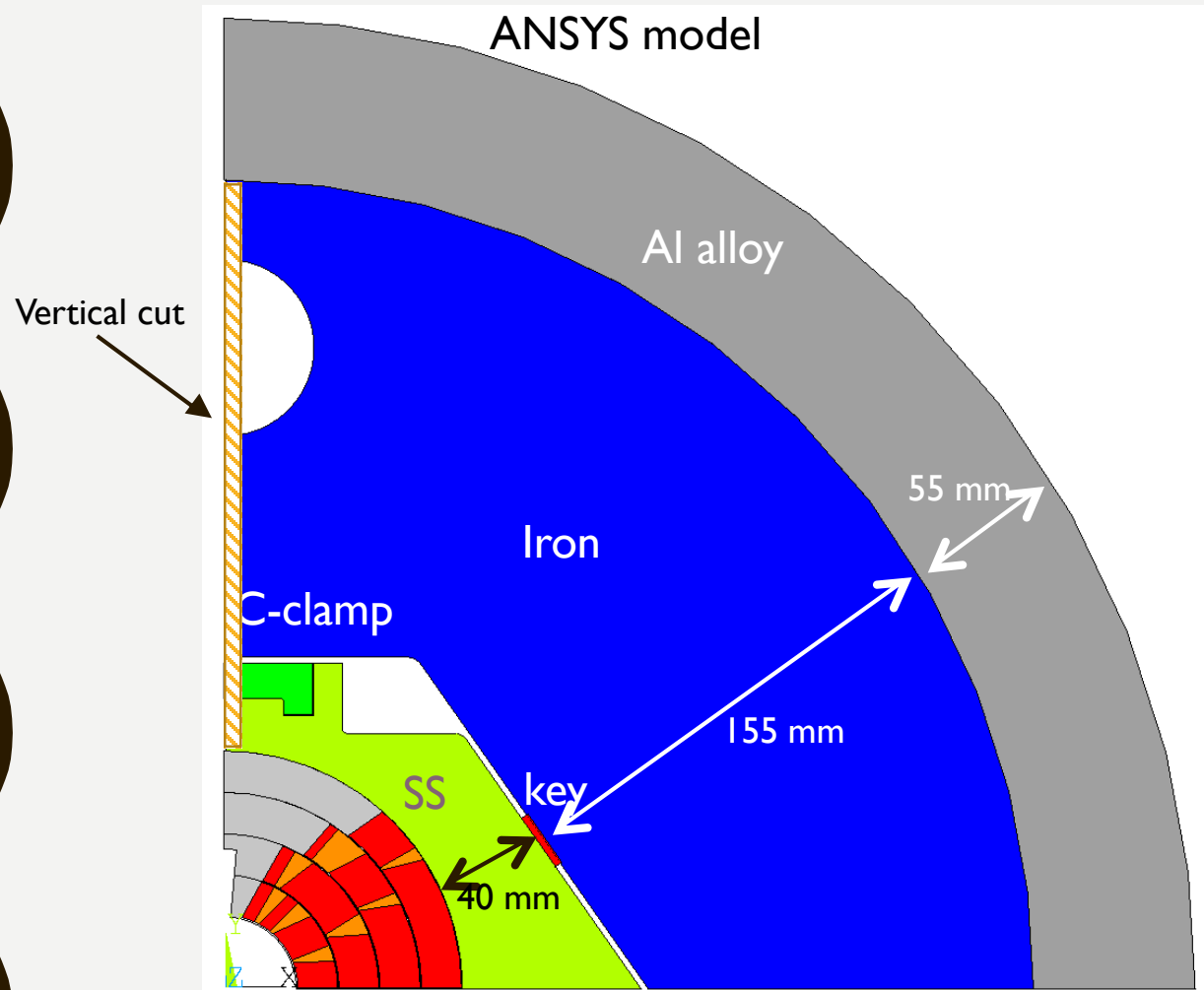
Fig. 6. Upper critical field at 4.2 K estimated from the critical current measurements under transversal pressure.



MATERIAL PARAMETERS

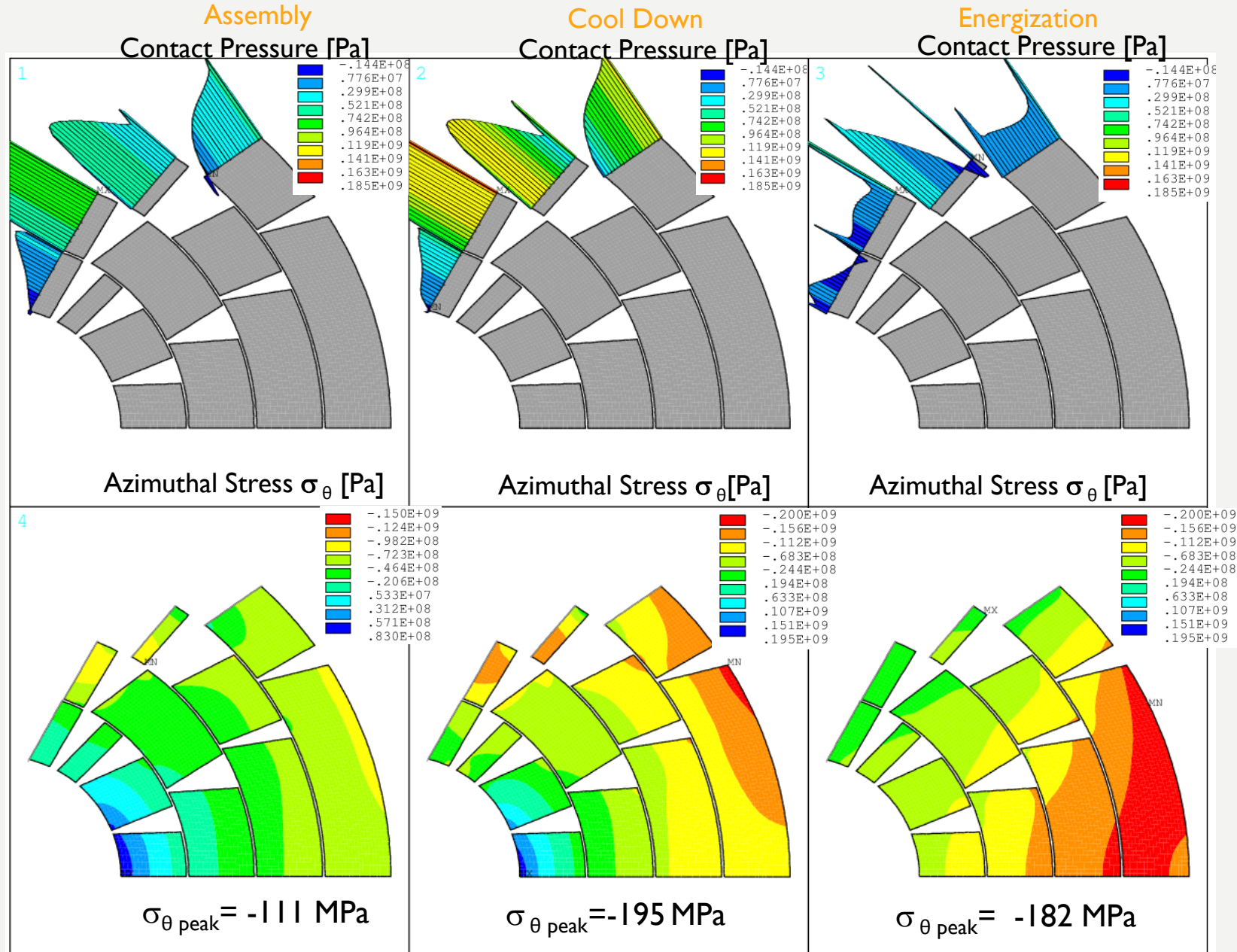
| | E modulus [GPa] (T=4K) | E modulus [GPa] (T=300K) | α (K ⁻¹) | ν_{xy} |
|-----------|------------------------|--------------------------|--|------------|
| Conductor | $E_x=33$ $E_y=27.5$ | $E_x=30$ $E_y=25$ | $\alpha_x=3.08E-3/296$ $\alpha_y=3.36E-3/296$ | 0.3 |
| Steel | 210 | 191 | $2.8e-3/296$ | 0.28 |
| Iron | 224 ← | 204 | $2.0e-3/296$ | 0.28 |
| Aluminum | 79 +10% | 72 | $4.2e-3/296$ | 0.3 |
| Copper | 110 | 100 | $3.4e-3/296$ | 0.3 |
| Resin | 27.5 | 25 | $2.5e-3/296$ | 0.2 |
| Titanium | 126.5 | 115 | $1.7e-3/296$ | 0.3 |

CONFIGURATION 1

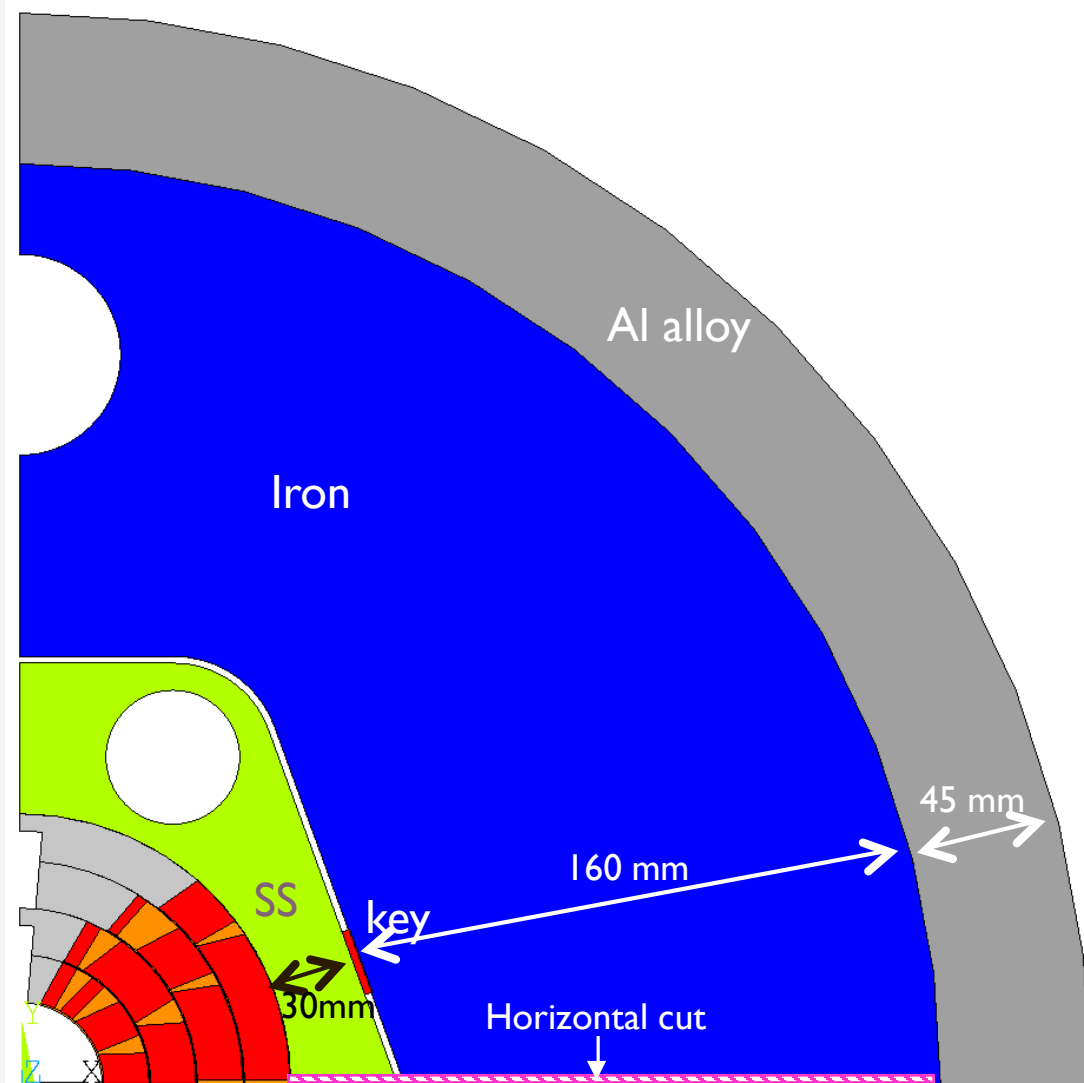


- Bladder & key configuration
Key length= 20 mm, interference= 0.6 mm
- Vertical cut both in the steel collar and in the iron yoke
- C-clamp mandatory to achieve enough contact pressure at the pole, interference= 0.15 mm

CONTACT PRESSURE AND PRINCIPAL STRESS

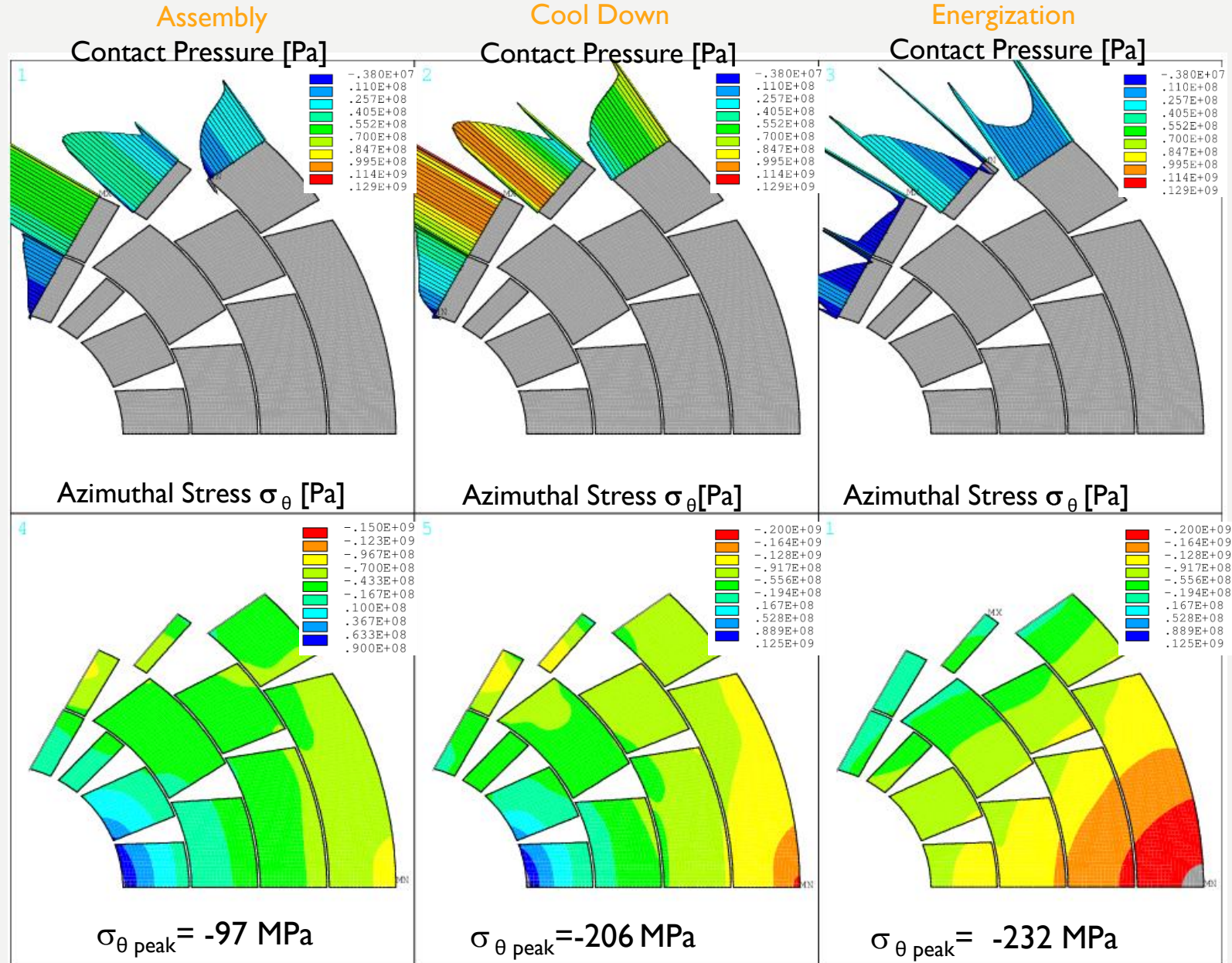


CONFIGURATION 2

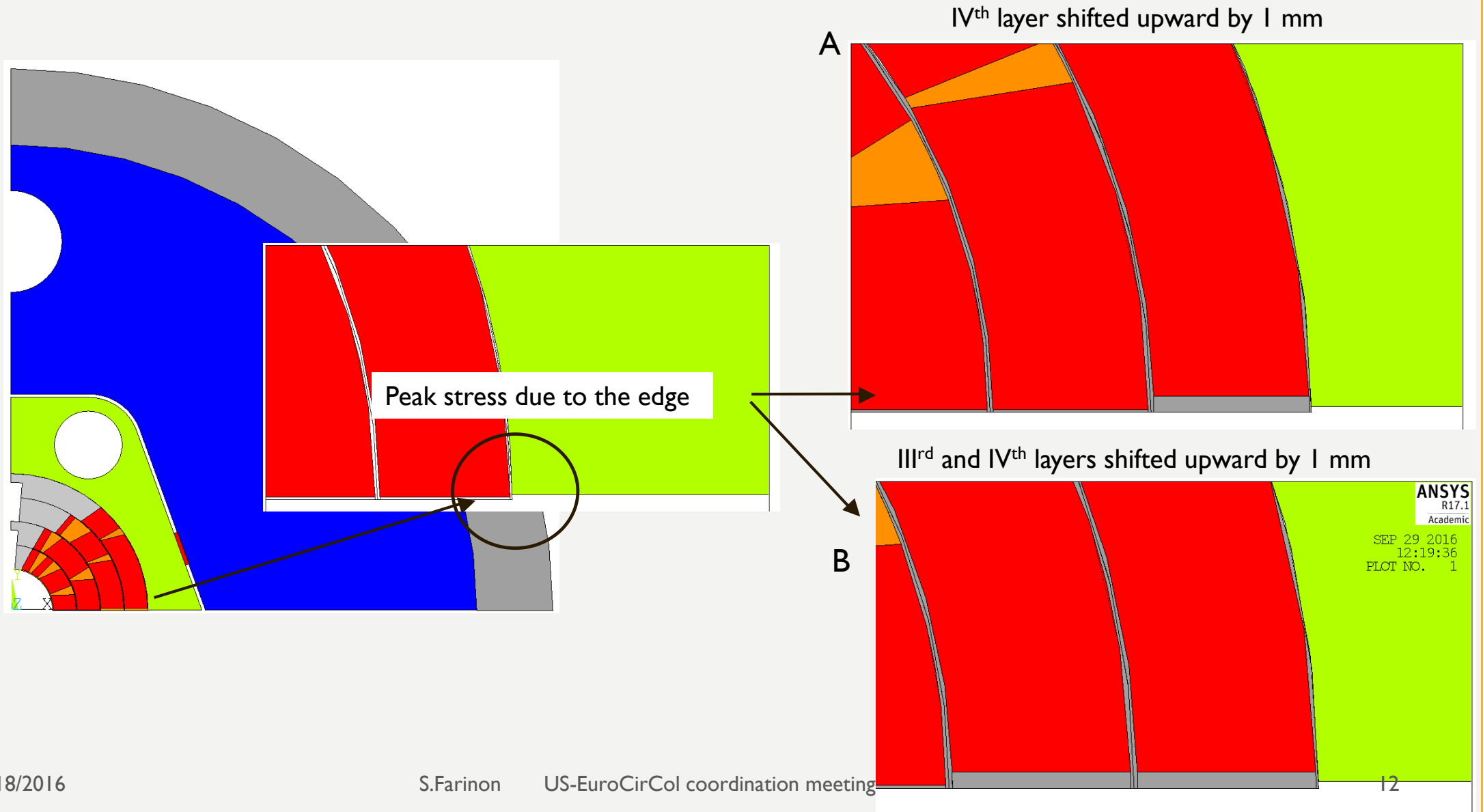


- Bladder & key configuration
Key length= 20 mm, interference= 0.4 mm
- Horizontal cut both in the steel collar and in the iron yoke

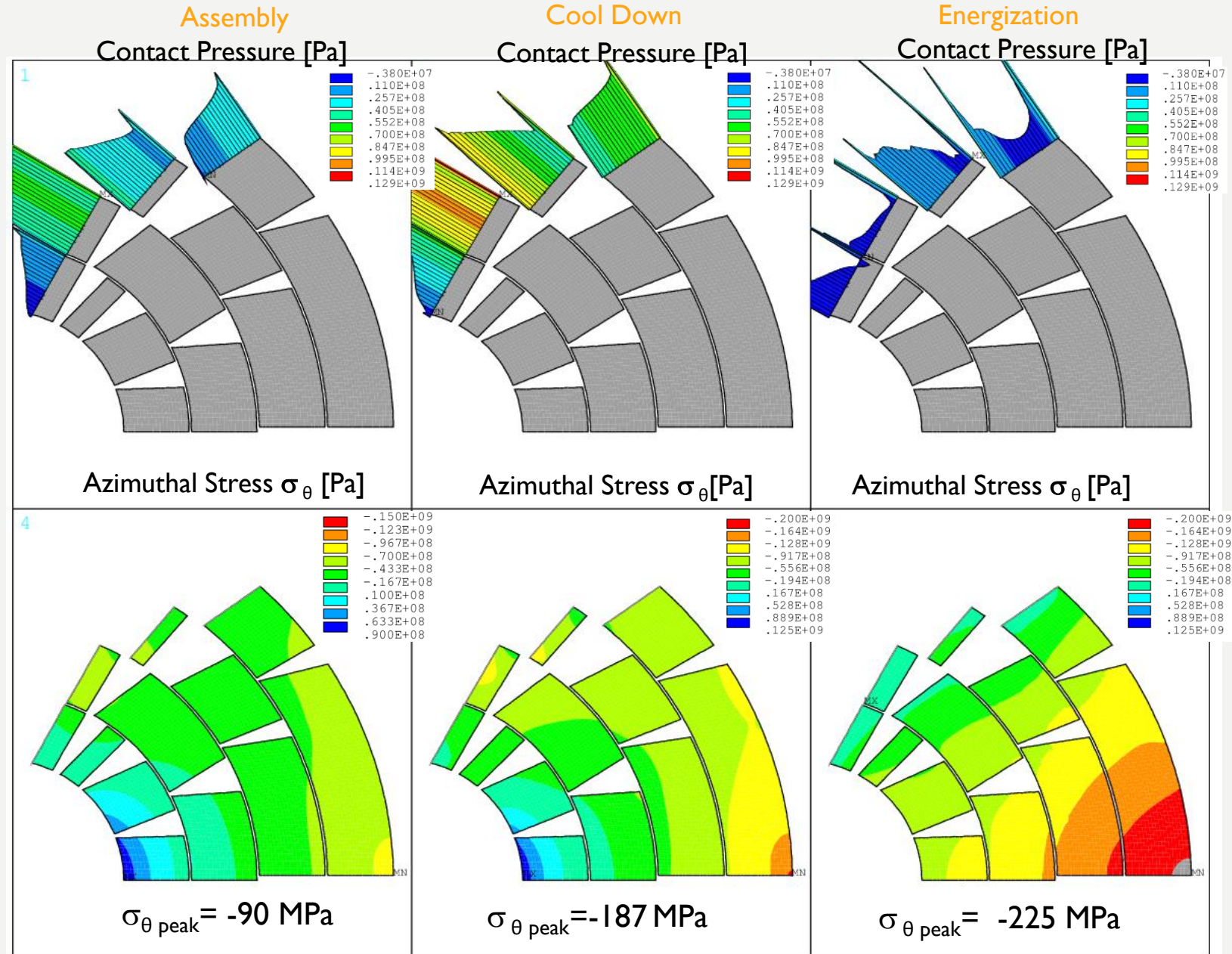
CONTACT PRESSURE AND PRINCIPAL STRESS



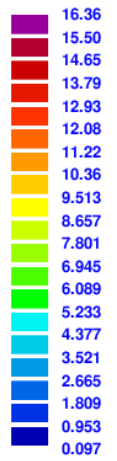
CONFIGURATION 2



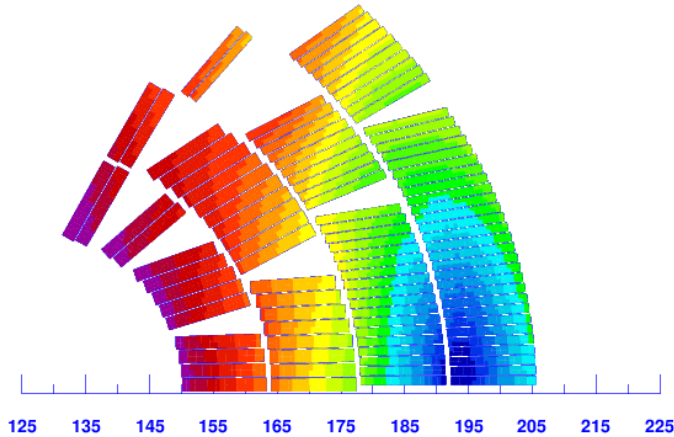
CONTACT PRESSURE AND PRINCIPAL STRESS



|B| (T)



I6T-22b-36-optd6f7



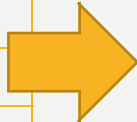
Turn number:
 Layer 1: 13
 Layer 2: 20
 Layer 3: 30
 Layer 4: 38
Tot: 202/ap.

Wedge minimum thickness: **0.86 mm**

 In LHC: 0.70 mm
 In DII: 0.98 mm

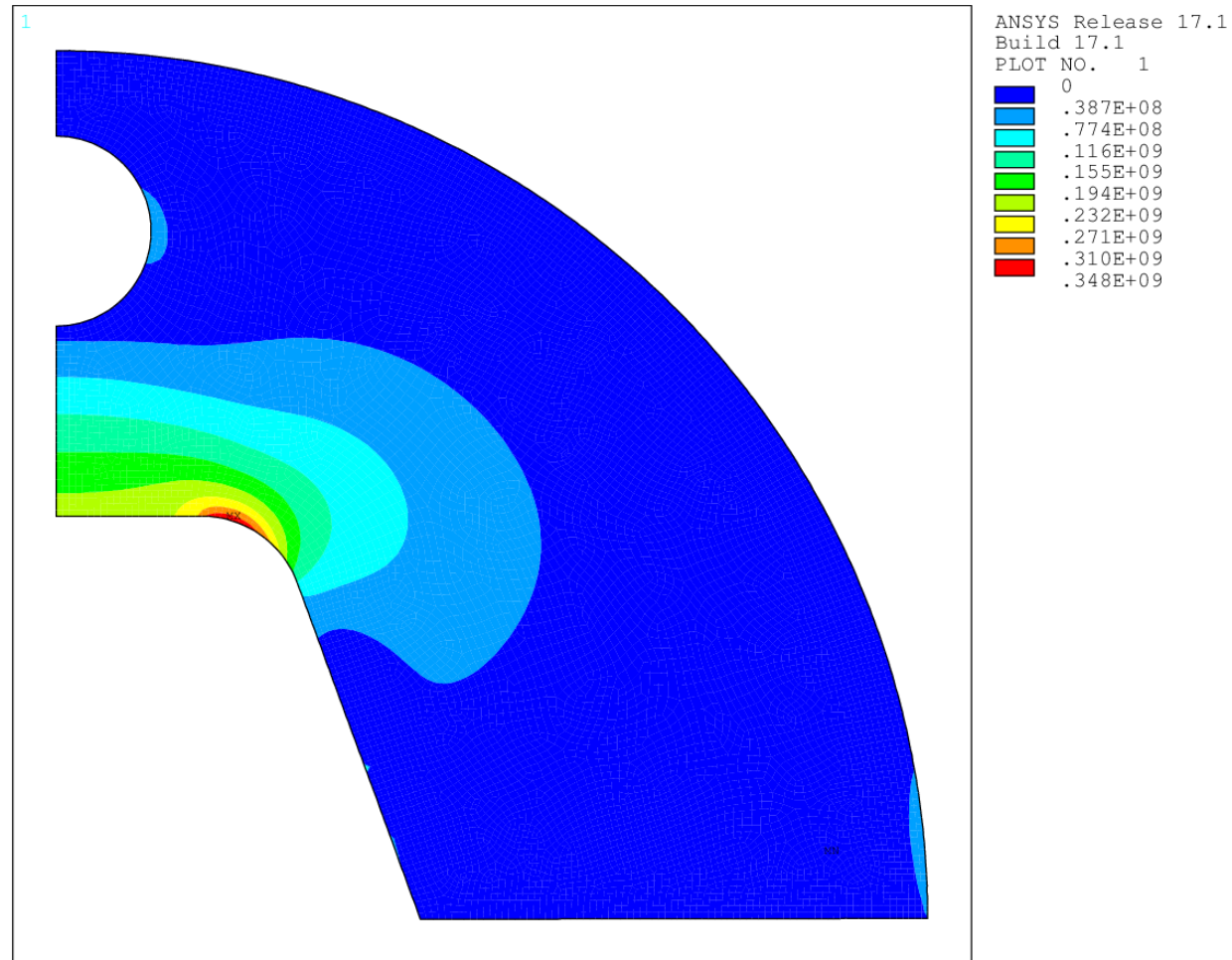
Field harmonics < 1 unit

| | Cable 1 (inner) | Cable 2 (outer) |
|--------------------------------------|------------------------|------------------------|
| Strand number | 22 | 36 |
| Strand diameter | 1.1 mm | 0.712 mm |
| Bare width | 13.2 mm | 13.5mm |
| Bare inner thickness | 1.892 mm | 1.225 mm |
| Bare outer thickness | 2.072 mm | 1.343 mm |
| Insulation | 0.15 mm | 0.15 mm |
| Keystone angle | 0.5° | 0.5° |
| Cu/NCu | 0.85 | 2.15 |
| Operating current | 11180 A | 11180A |
| Copper current density | 1165 A/mm ² | 1143 A/mm ² |
| Operating point on LL (1.9 K) | 86% | 86% |



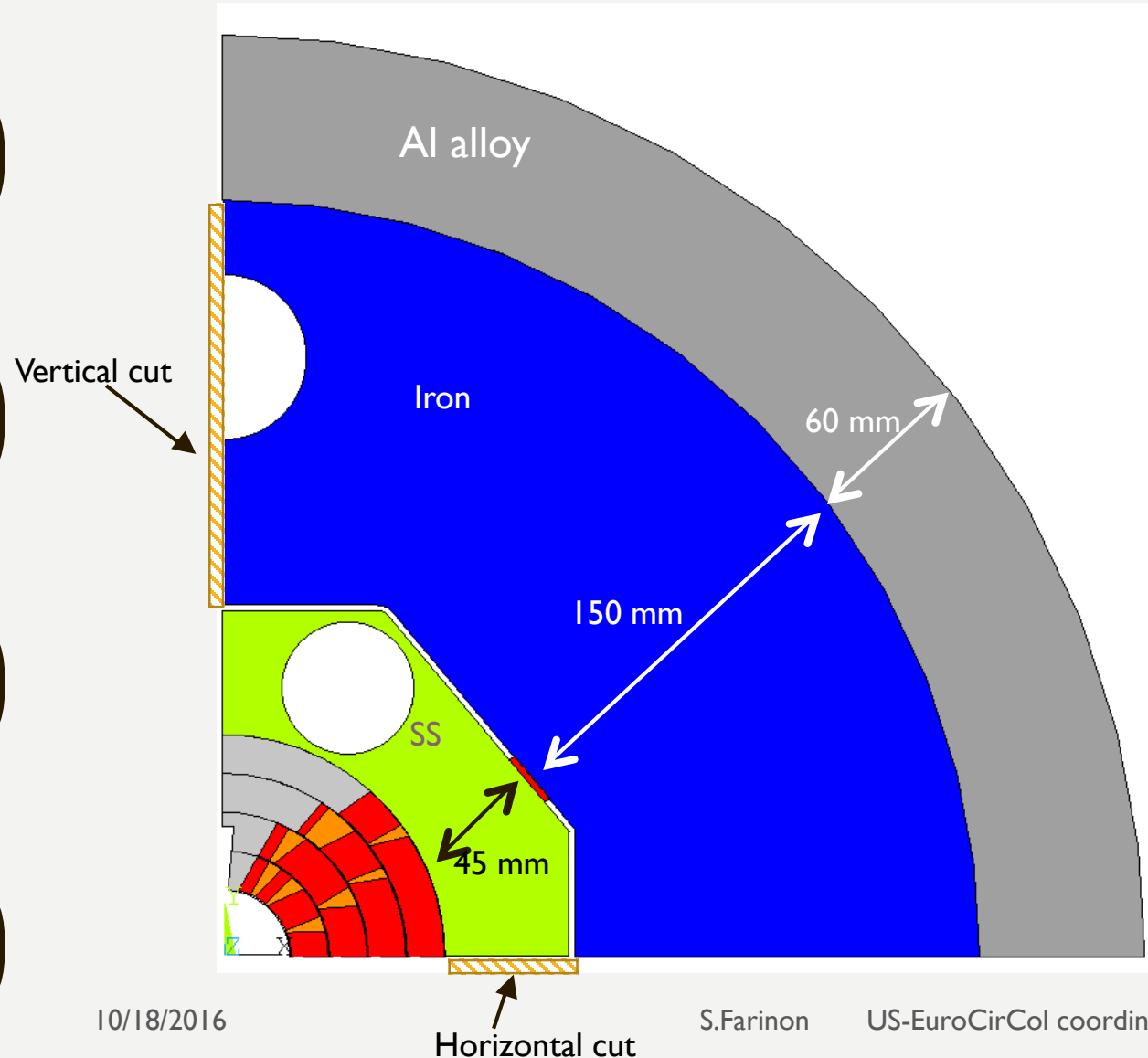
| Cable 1 (inner) | Cable 2 (outer) |
|------------------------------|------------------------------|
| 22 | 36 |
| 1.1 mm | 0.712 mm |
| 13.2 mm | 13.5mm |
| 1.892 mm | 1.225 mm |
| 2.072 mm | 1.343 mm |
| 0.15 mm | 0.15 mm |
| 0.5° | 0.5° |
| 0.85 | 2.1 |
| 11200 A | 11200 A |
| 1167 A/mm² | 1154 A/mm² |
| 86% | 86% |

TENSILE STRESS IN THE IRON



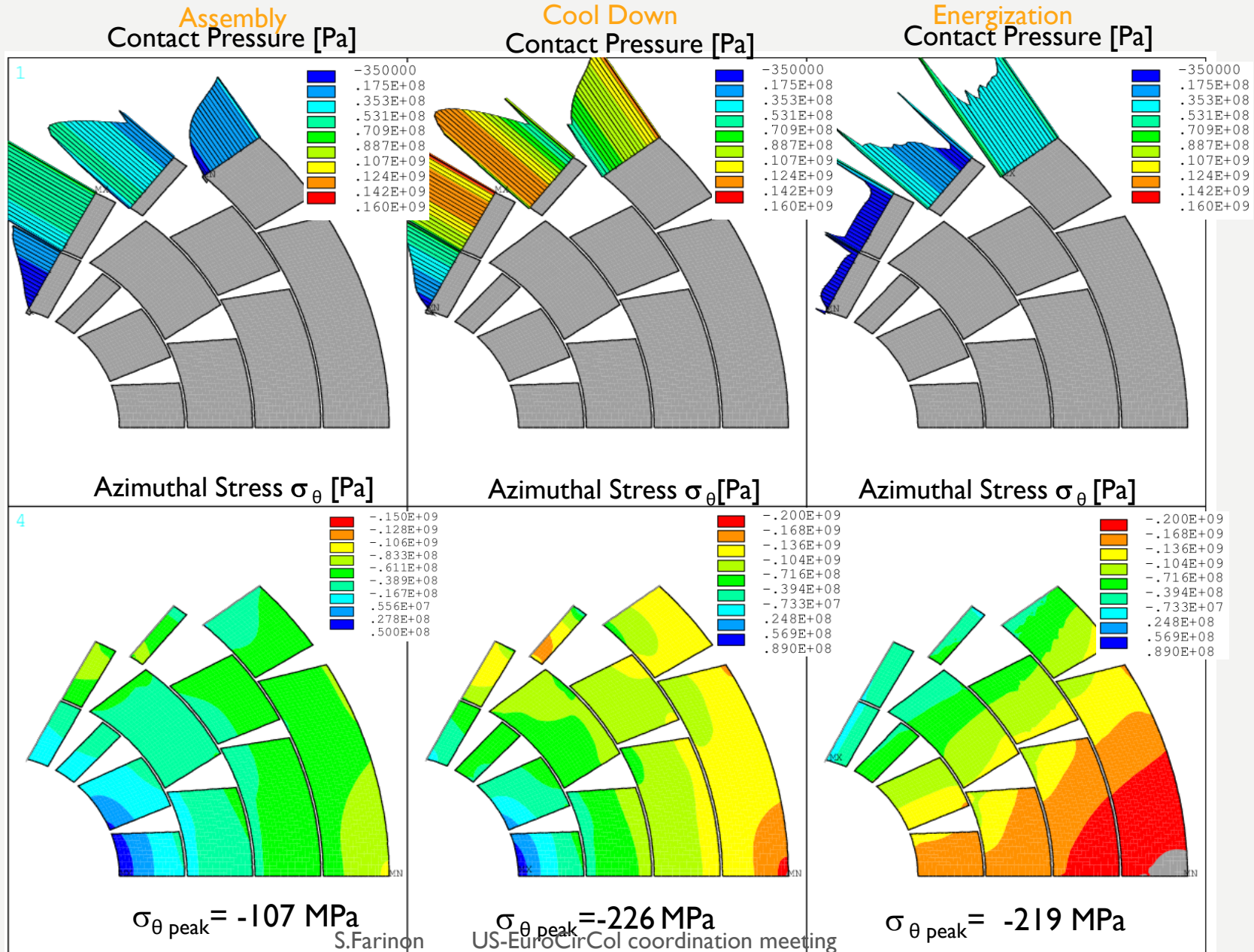
Tensile stress peak in the iron ($\sigma_{I \text{ peak}}$) \sim 350 MPa

CONFIGURATION 3

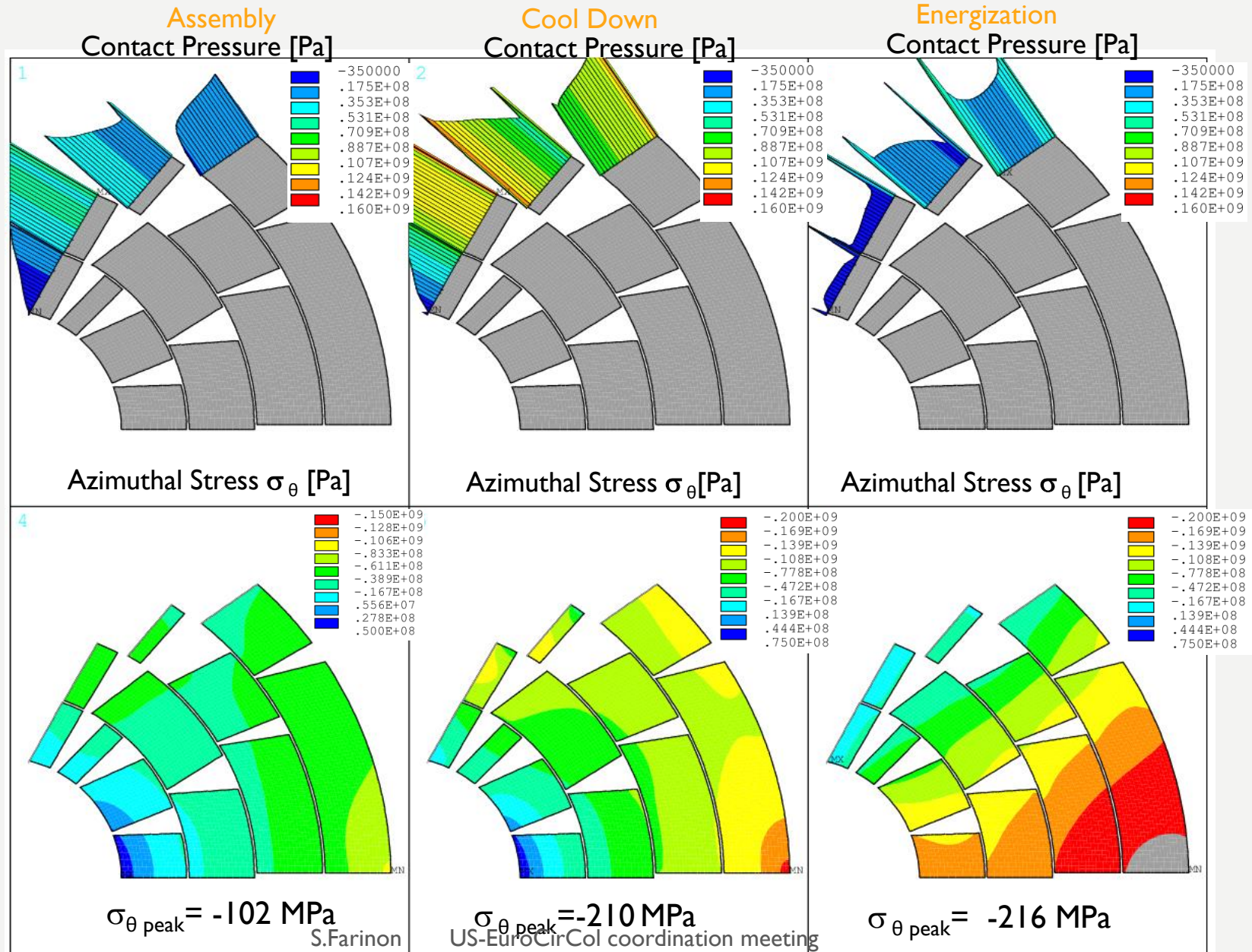


- Bladder & key configuration
Key length= 20 mm, interference= 0.5 mm
- Horizontal cut in the steel collar
→greater contact pressure at the pole
- Vertical cut in the iron yoke
→smaller tensile stress on the iron

CONTACT PRESSURE AND PRINCIPAL STRESS



CONTACT PRESSURE AND PRINCIPAL STRESS



CONCLUSIONS

- The mechanics of the 16T costheta dipole has been investigated, giving particular importance to the fulfillment of the following requirements: stress on conductors < 150 MPa @room temperature, stress on conductors < 200 MPa @cold and contact pressure Ti pole-conductors > 2 MPa after energization.
- Different configurations were considered, among those the more promising were presented:
- CONFIGURATION I- vertical cut in the steel collar and the in the iron yoke
 - Bladder&Key + C-clamp mandatory to achieve contact pressure at the pole
 - Almost fulfill stress limits on the conductor
 - Good contact pressure at the pole for all the layers
- CONFIGURATION II – horizontal cut in the steel collar and in the iron yoke
 - Almost fulfill stress limits on the conductor
 - Good contact pressure at the pole for all the layers
 - Very high values for tensile stress on the iron (350 MPa)
- CONFIGURATION III- hybrid solutions, horizontal cut in the steel collar and vertical cut in the iron yoke
 - Almost fulfill stress limits on the conductor
 - Good contact pressure at the pole for all the layers