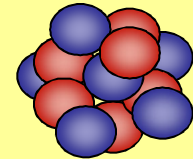


Introduction to Nuclear physics;

The nucleus a complex system



Héloïse Goutte
CEA, DAM, DIF

Heloise.goutte@cea.fr

I) Some features about the nucleus

- discovery
- radius
- binding energy
- nucleon-nucleon interaction
- life time

II) Modeling of the nucleus

- liquid drop
- shell model
- mean field

III) Examples of recent studies

- exotic nuclei
- isomers
- shape coexistence
- super heavy

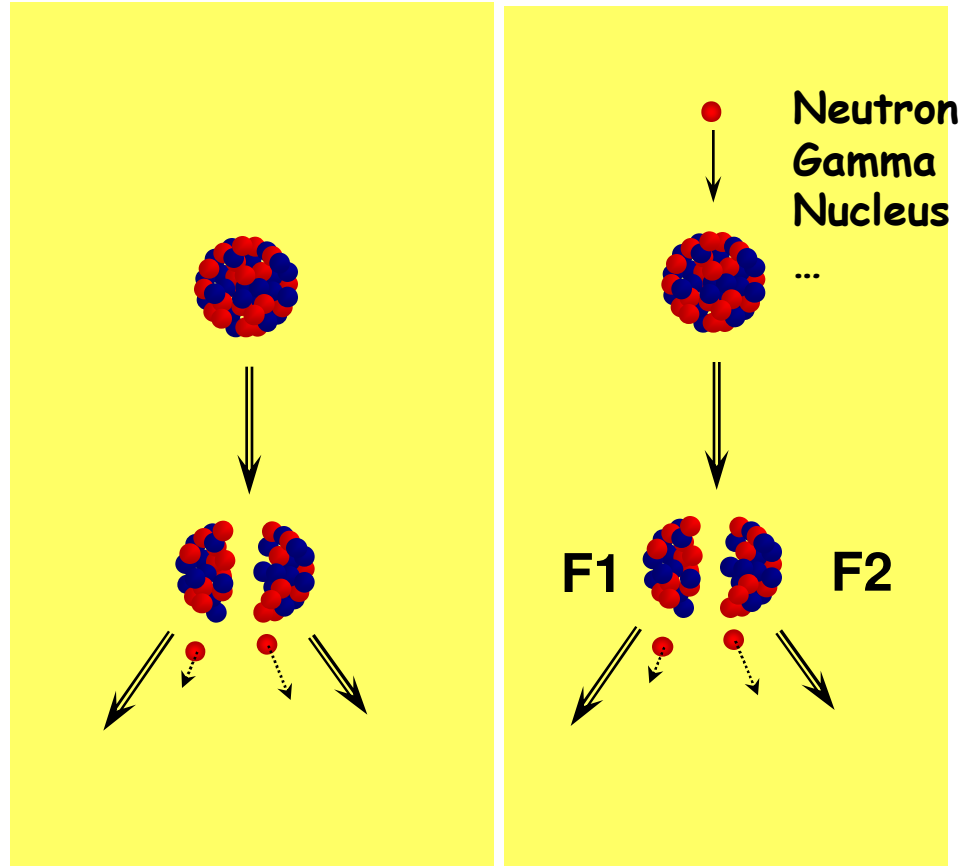
IV) Toward a microscopic description of the fission process

IV) Nuclear fission

The fission process

spontaneous

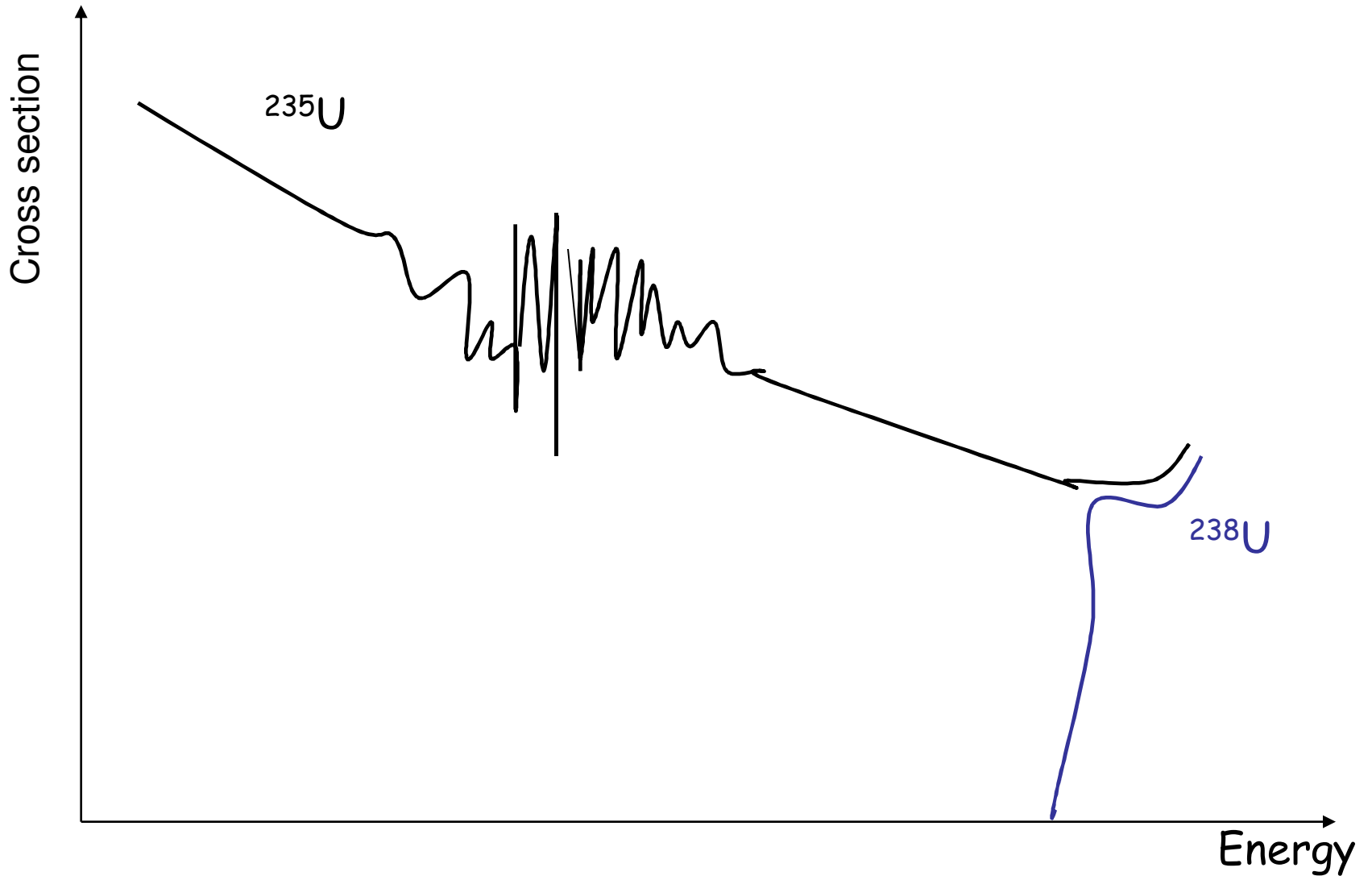
induced



From D. Goutte

Only 19 nuclei are known to fission spontaneously

Fission cross section



High energy released per fission ~ 200 MeV

to compare :

- combustion of 1 atom of carbon = 4 eV
- fission of 1 g of ^{235}U releases the same amount of energy than 2.55 tons of coal

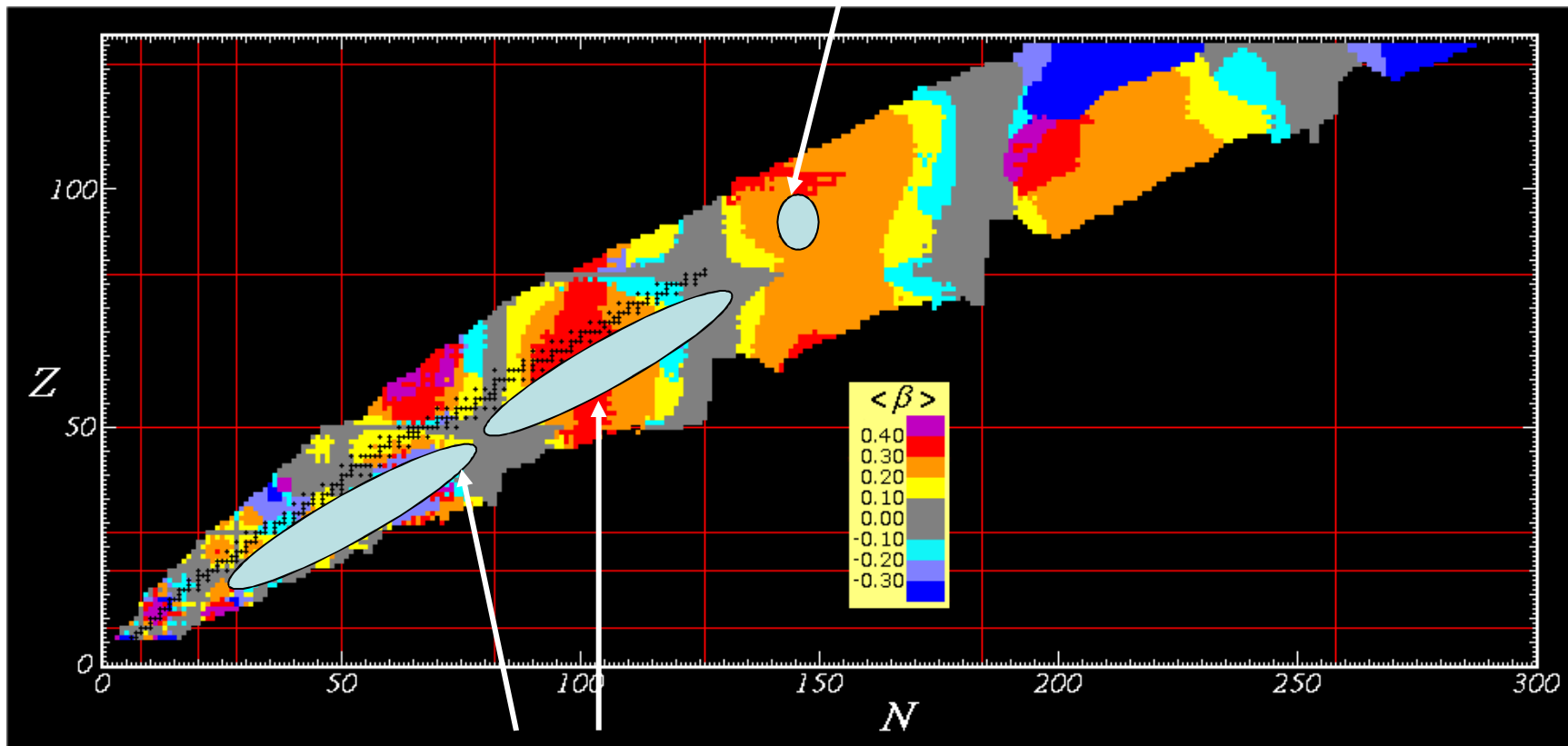
The ~ 200 MeV of energy release are shared as:

- | | |
|--|---------|
| • Kinetic energy of the fission products | 168 MeV |
| • Kinetic energy of the neutrons | 5 MeV |
| • Prompt γ emission | 7 MeV |
| • Delayed γ emission | 6 MeV |
| • Delayed β emission | 7 MeV |
| • Neutrinos | 10 MeV |

The importance of the fission process

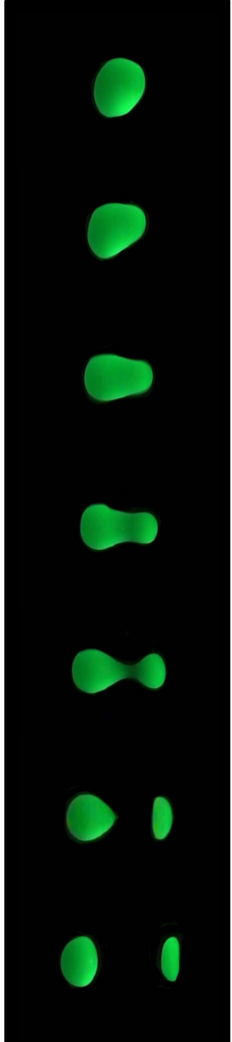
- Energy production
 - nuclear power plant
 - study of new fuel cycles
- Production of exotic nuclei
 - ALTO (IPN Orsay, France) , SPIRAL2 (GANIL, France)
- Astrophysics
 - r-process limitation
 - limitation in the production of Super Heavy Elements
 - Fission cycling
 - * depopulation of heavy region
 - * enhancement in fission-fragment region
 - * structure in nuclide distribution from fission fragments
 - Fission competition in beta-decay towards stability

Actinides (U, Pu...)



Fission fragments

A schematic description of the fission process

- 
- Competition between coulomb repulsion and the attractive nuclear interaction :
 - > oscillation of the nucleus due to this competition
 - > the system goes through **the saddle point** (a critical point) after which the potential energy decreases.

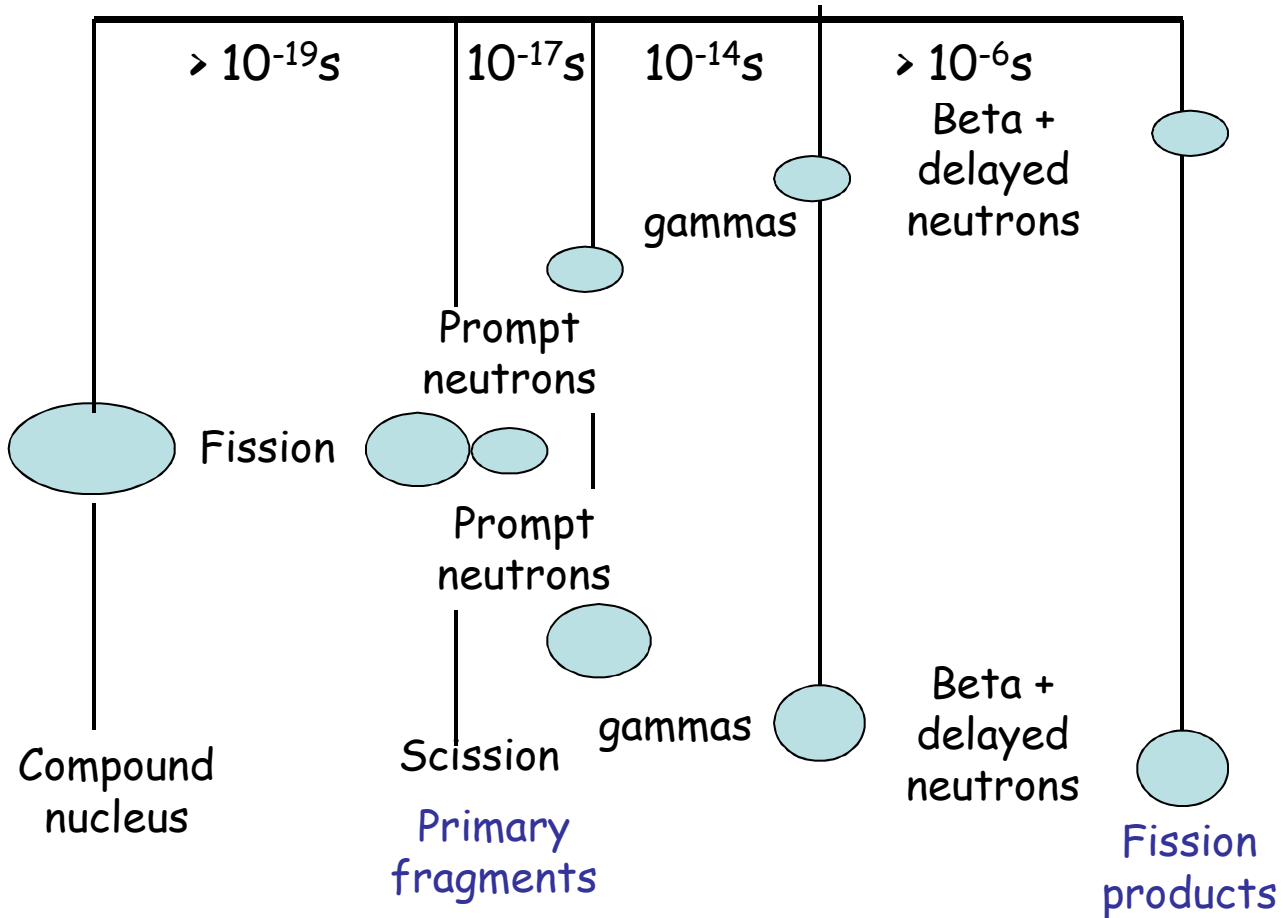
Then

- rapid increase of the deformation up to the **scission point** (break into two fragments)

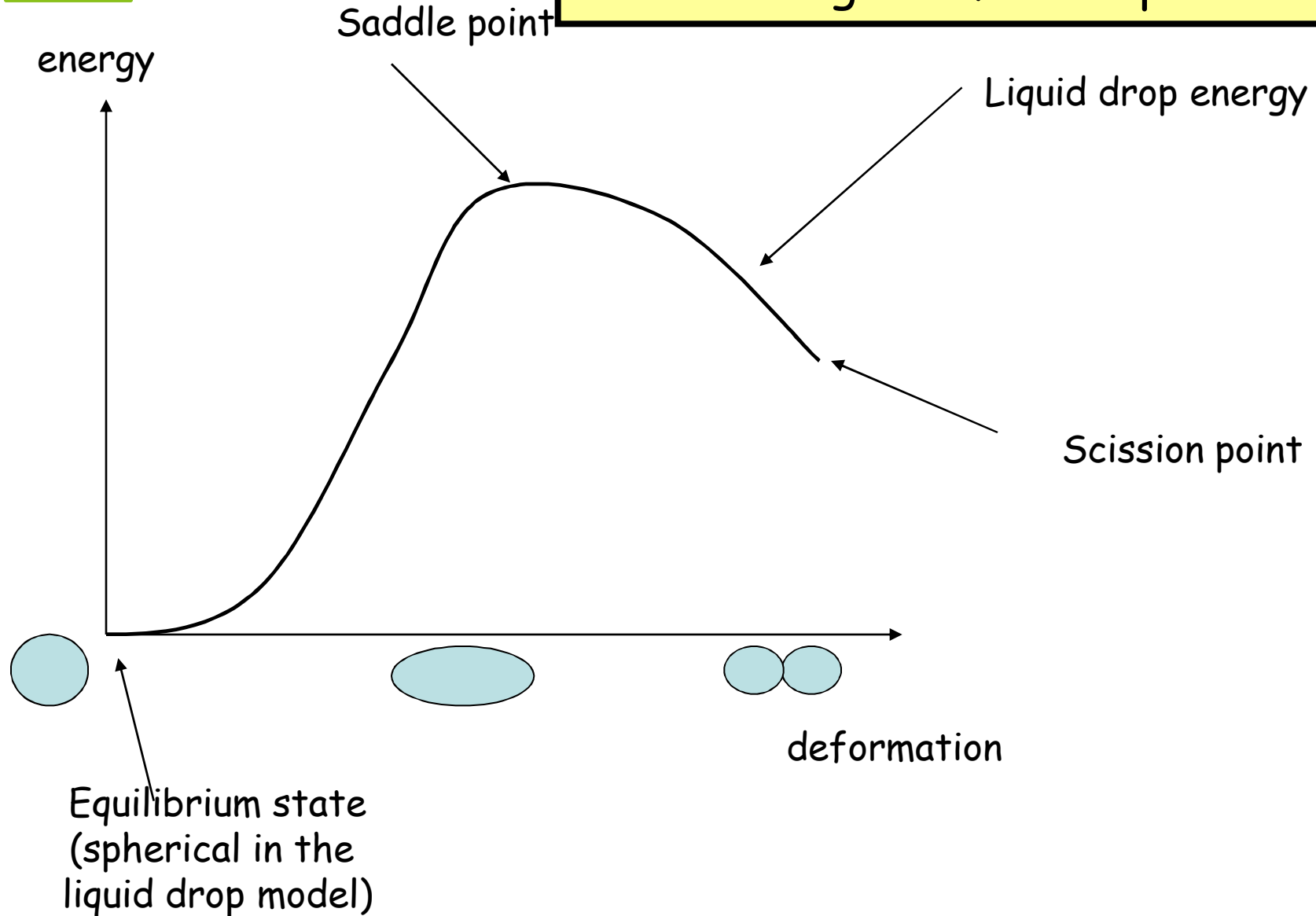
Then

- **separation** of the fragments
- **desexcitation** of the fragments

Time scale



Evolution of the liquid drop energy during the fission process



Liquid drop energy

energy

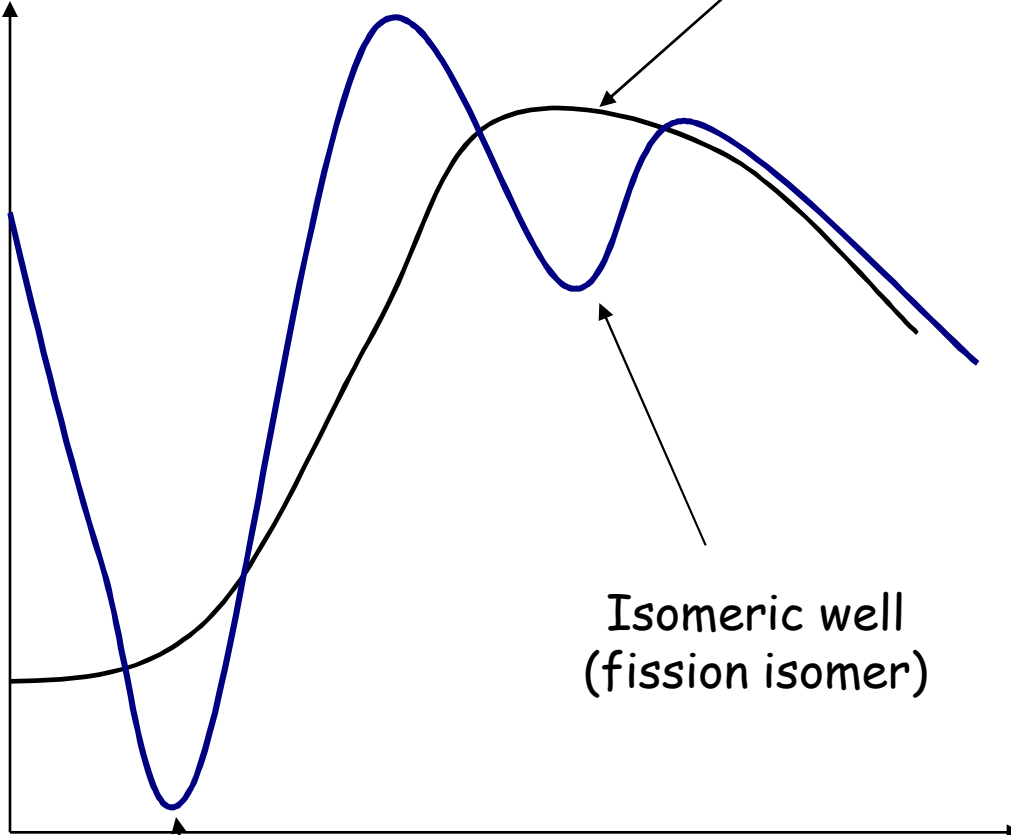
Structure effects

Liquid drop energy
+
Microscopic
shell corrections

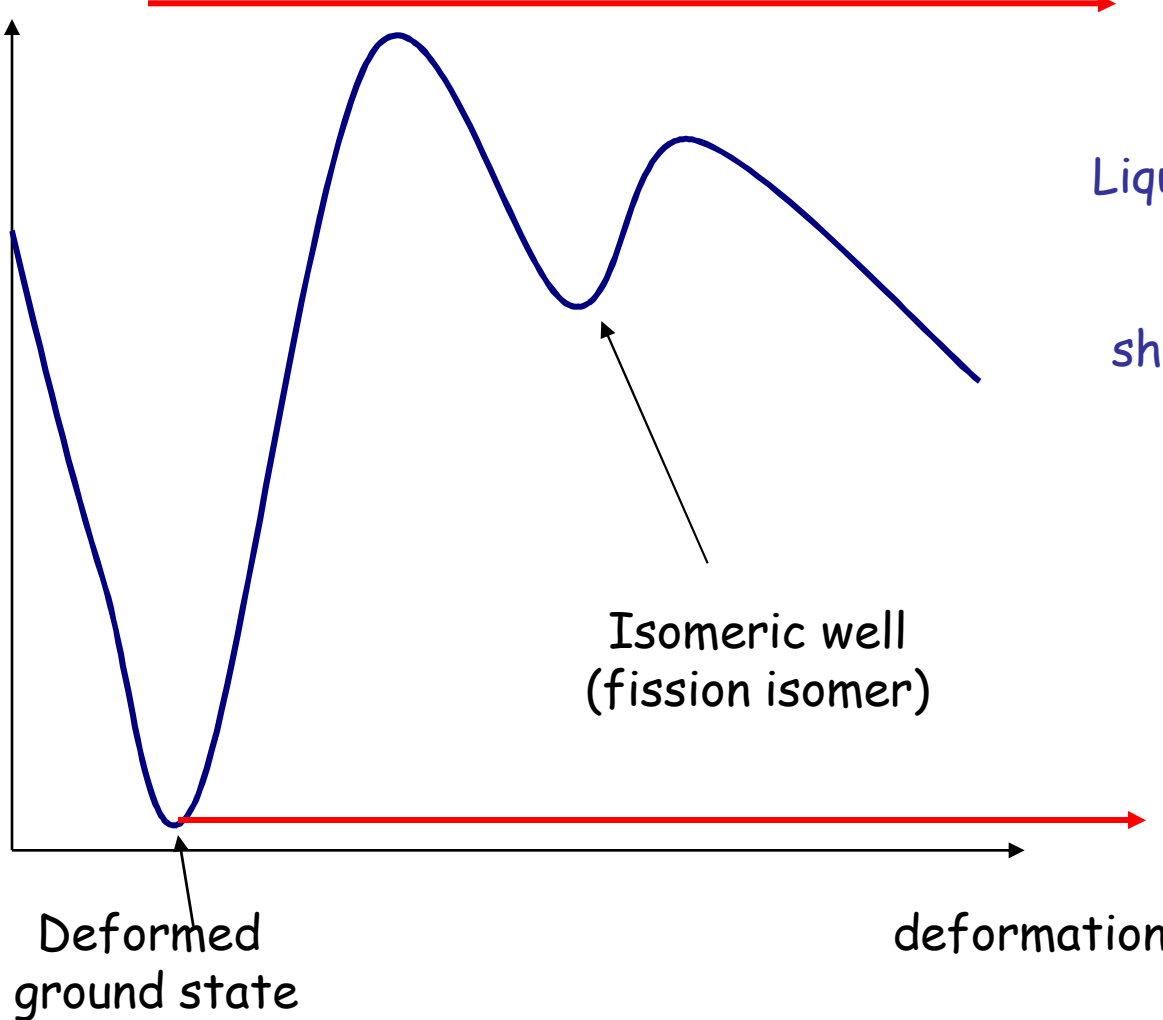
Isomeric well
(fission isomer)

Deformed
ground state

deformation



energy



Very favored induced fission

Liquid drop energy
+
Microscopic
shell corrections

Isomeric well
(fission isomer)

Deformed
ground state

deformation

Spontaneous fission
(tunneling through the
Barrier)
not favored (very long
fission lifetime)

Recent experimental studies: some examples

- Cross section measurements
 - absolute measurement for reference nuclei ($^{235-238}\text{U}$ and ^{239}Pu)
 - measurement of n-induced fission cross section for minor actinides from 1 eV to 1 GeV. (ex : n_Tof collaboration)
 - surrogate reactions ex: (t,pf) instead of (n,f)
- Fission fragment distributions
 - mass, charge, kinetic energy distributions
- Ternary fission
- Fission/quasi-fission, superheavy production
- Neutron emission (prompt and delayed)

To Study the fission of ${}^A Z_N$

Usual study : $n + {}^{A-1} Z_{N-1} \rightarrow {}^A Z_N \rightarrow \text{fission}$

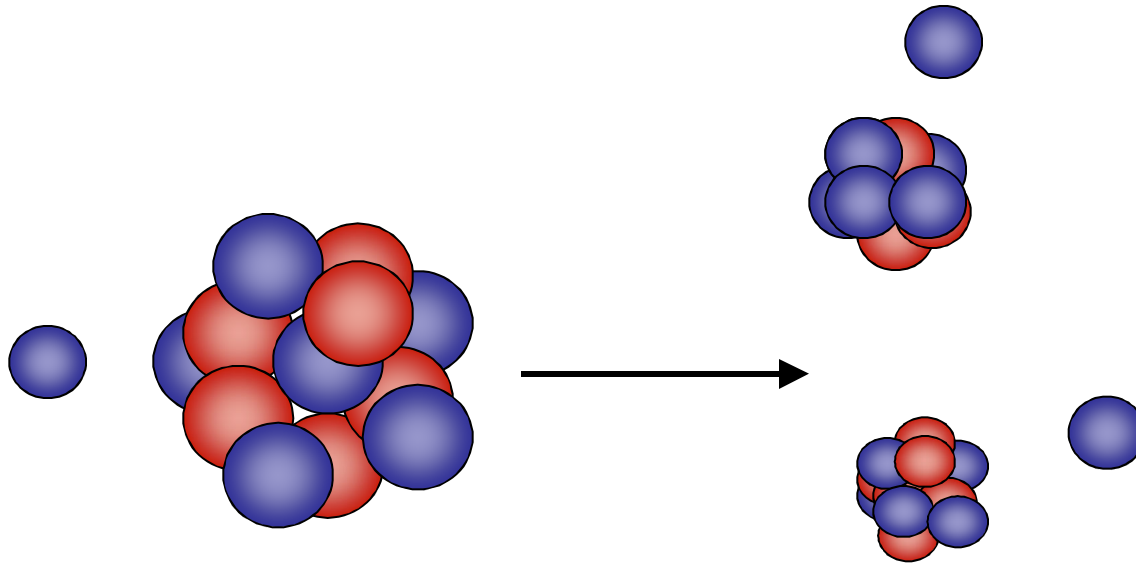


Not possible to make a target

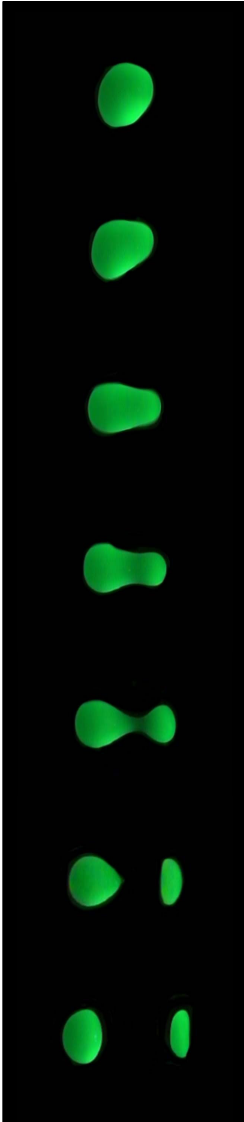

But a target which is possible is ${}^{A-2} Z_{N-2}$

Surrogate reaction : $t + {}^{A-2} Z_{N-2} \rightarrow {}^{A+1}(Z+1)_N \rightarrow p + {}^A Z_N \rightarrow \text{fission}$

What kind of problem can appear with this surrogate technique ?



The fission process : a challenge for the theory

- 
- * From a theoretical point of view, fission appears as a **large amplitude motion**, in which intervene:
 - * A large rearrangement of the internal structure of the nucleus with an important role played by the **shell effects** 
 - * Many types of **deformations** simultaneously
 - * **Dynamical effects**: couplings between collective modes, couplings between collective modes and intrinsic excitations.

⇒ A laboratory for theoretical predictions

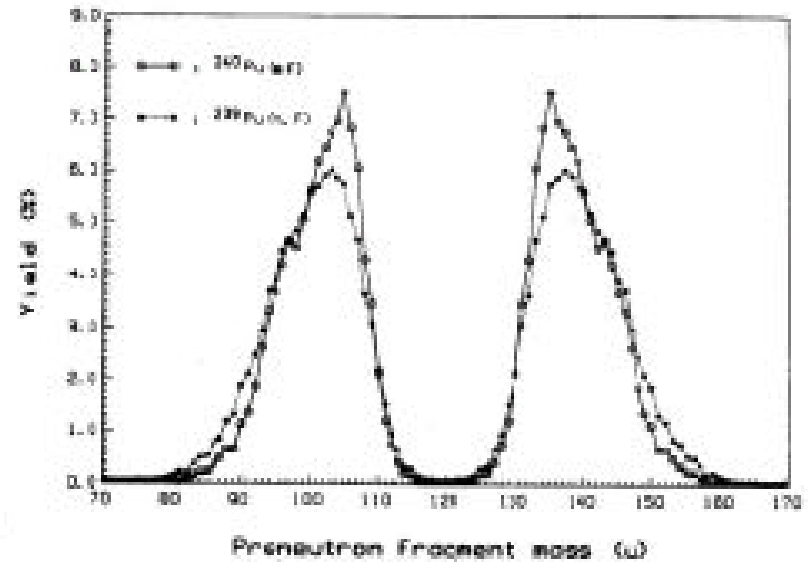
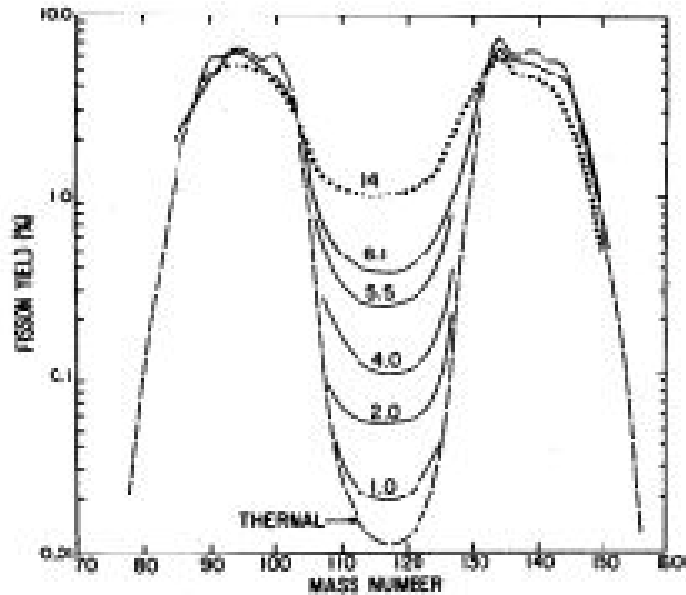
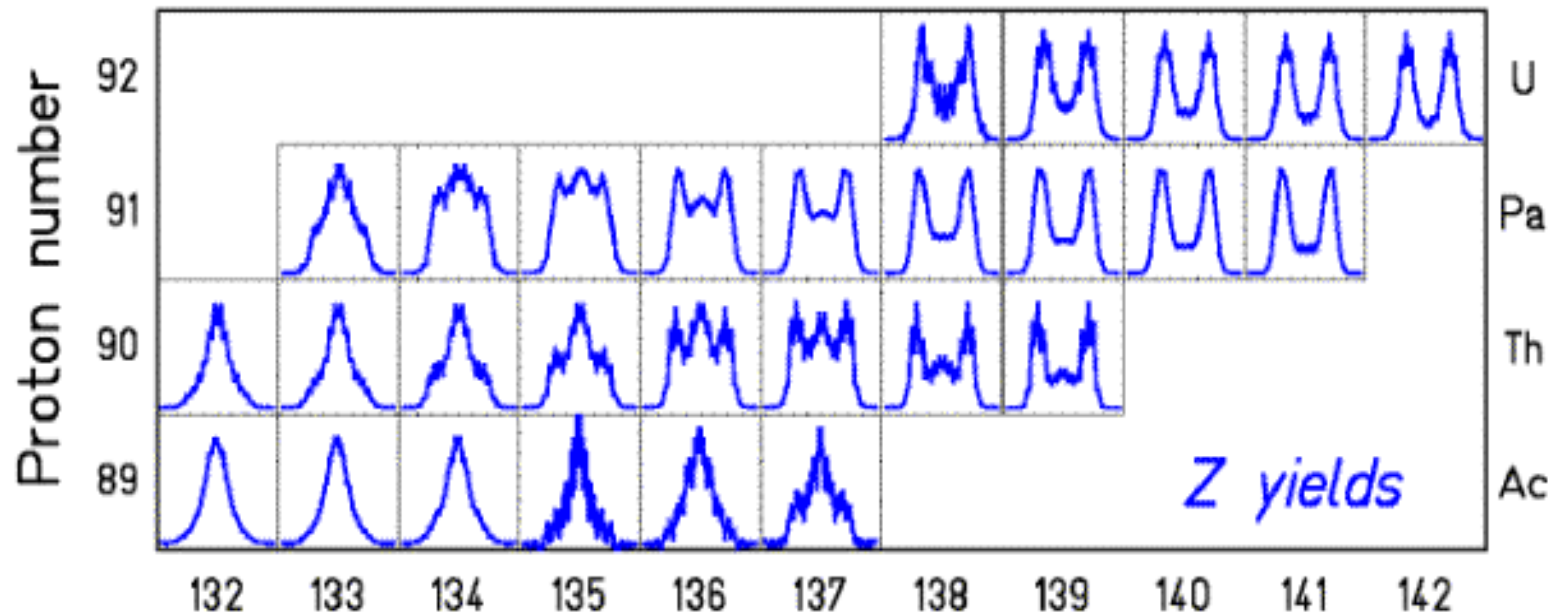


FIG. 6 A gauche, distributions en masse des fragments de la fission du noyau ^{236}U induite par des neutrons ayant des énergies comprises entre la valeur thermique (0.025 eV) et 14 MeV sur le noyau ^{235}U . A droite, comparaisons entre les distributions en masse des fragments du ^{240}Pu mesurées dans la fission spontanée du noyau et dans la fission induite par des neutrons thermiques sur le ^{239}Pu . Ces diagrammes sont tirés des Réfs. [82] et [83].

L.E. Glendenin, et al. Phys. Rev. C 24 (1981) 2600.
 C. Wagemans, et al. Phys. Rev. C 90 (1984) 218.

Fission fragment charge distributions



K-H Schmidt et al., Nucl. Phys. A665 (2000) 221

Theoretical studies of the fission process

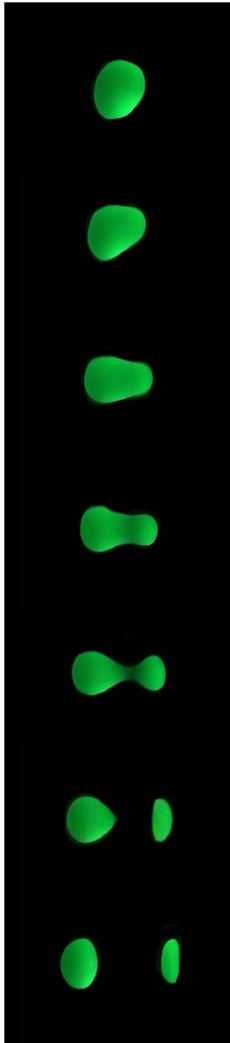
Why new studies now ?

- **Fundamental questions** : a process, not fully understood
- A large amount of new experimental results : fission in **new conditions** (exotic nuclei, super heavies, new energy range ...)
- Need for **predictions for nuclear data**
 - Energy production
 - Production of exotic nuclei : ALTO, SPIRAL2
- Progress made these last decades in the **microscopic description** of the atomic nuclei
- **New super-calculators**

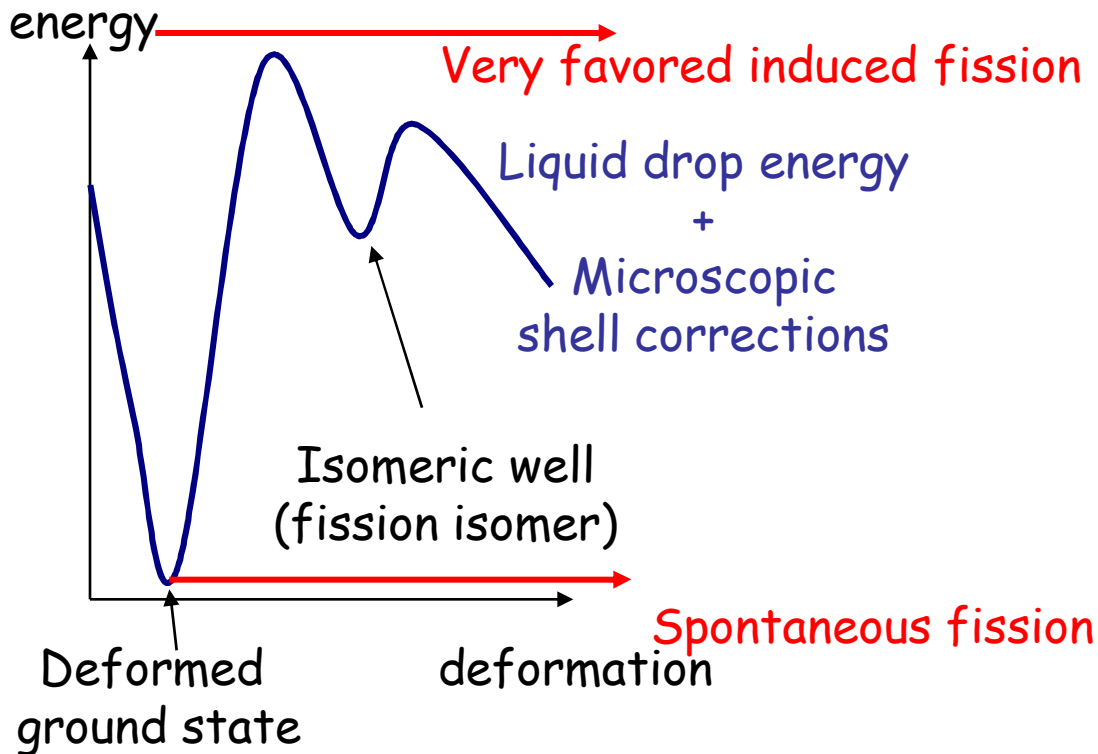
Recent microscopic fission studies

Towards a description :

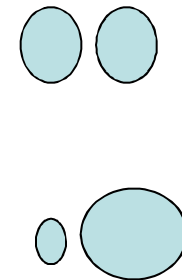
- as « *ab-initio* » as possible : microscopic description in terms of nucleons in interaction (mean field based approach)
 - applicable to the different aspects of the process :
 - * properties of the fissioning system (deformation of the ground state, fission isomer energy)
 - * dynamical evolution
 - * properties of the fragments (mass, charge, energy ...)
 - able to give quantitative results, which directly compared to experimental data.
- The ultimate goal is to have a coherent, quantum, microscopic, and time dependent description of the structure of the nucleus and of the dynamics of the process.



What is missing in this description ?



- Description of the dynamics (time evolution)
- Description of the different fragmentations



Assumptions of the present approach

- * fission dynamics is governed by the evolution of a few collective parameters q_i (elongation and asymmetry)

Why these two degrees of freedom are important ?




- * Internal structure is at equilibrium at each step of the collective movement


→ Assumption valid only for low-energy fission

$$|\Psi(t)\rangle = \int dq_i f(q_i, t) |\Phi_{q_i}\rangle$$

Fission dynamics results from a time evolution in a collective space

A two-steps formalism

- 1) **STATIC** calculations : determination of $|\Phi_{q_i}\rangle$
 Analysis of the nuclear properties as functions of the deformations 
 Constrained- Hartree-Fock-Bogoliubov method using the D1S Gogny
 effective interaction

- 2) **DYNAMICAL** calculations : determination of $f(q_i, t)$ 
 Time evolution in the fission channel
 Formalism based on the Time dependent Generator Coordinate Method
 (TDGCM+GOA)

Constrained Hartree-Fock-Bogoliubov approach

$$\delta \langle \Phi_{q_i} | \hat{H} - \sum_i \lambda_i \hat{Q}_i - \lambda_N \hat{N} - \lambda_Z \hat{Z} | \Phi_{q_i} \rangle = 0$$

with

$$\begin{cases} \langle \Phi_{q_i} | \hat{N}(\hat{Z}) | \Phi_{q_i} \rangle = N(Z) \\ \langle \Phi_{q_i} | \hat{Q}_i | \Phi_{q_i} \rangle = q_i \end{cases}$$

Most commonly used constraints : q_{20} , q_{30} , q_{22} , q_{40} and q_{10}



Time Dependent Generator Coordinate Method

$$\frac{\partial}{\partial f^*(q_i, t)} \int_{t_1}^{t_2} \langle \psi(t) | \hat{H} - i\hbar \frac{\partial}{\partial t} | \psi(t) \rangle dt = 0 \quad \text{with the same } \hat{H} \text{ than in HFB}$$

Using the Gaussian Overlap Approximation, it leads to a Schrödinger-type Equation :

$$H_{\text{coll}} g(q_i, t) = i\hbar \frac{\partial g(q_i, t)}{\partial t}$$

with

$$H_{\text{coll}} = -\frac{\hbar^2}{2} \sum_{i,j} \frac{\partial}{\partial q_i} B_{ij}(q_i) \frac{\partial}{\partial q_j} + \langle \Phi_{q_i} | \hat{H} | \Phi_{q_i} \rangle - \Delta V(q_i)$$

→ With this method the collective Hamiltonian is entirely derived by microscopic ingredients and the Gogny D1S force

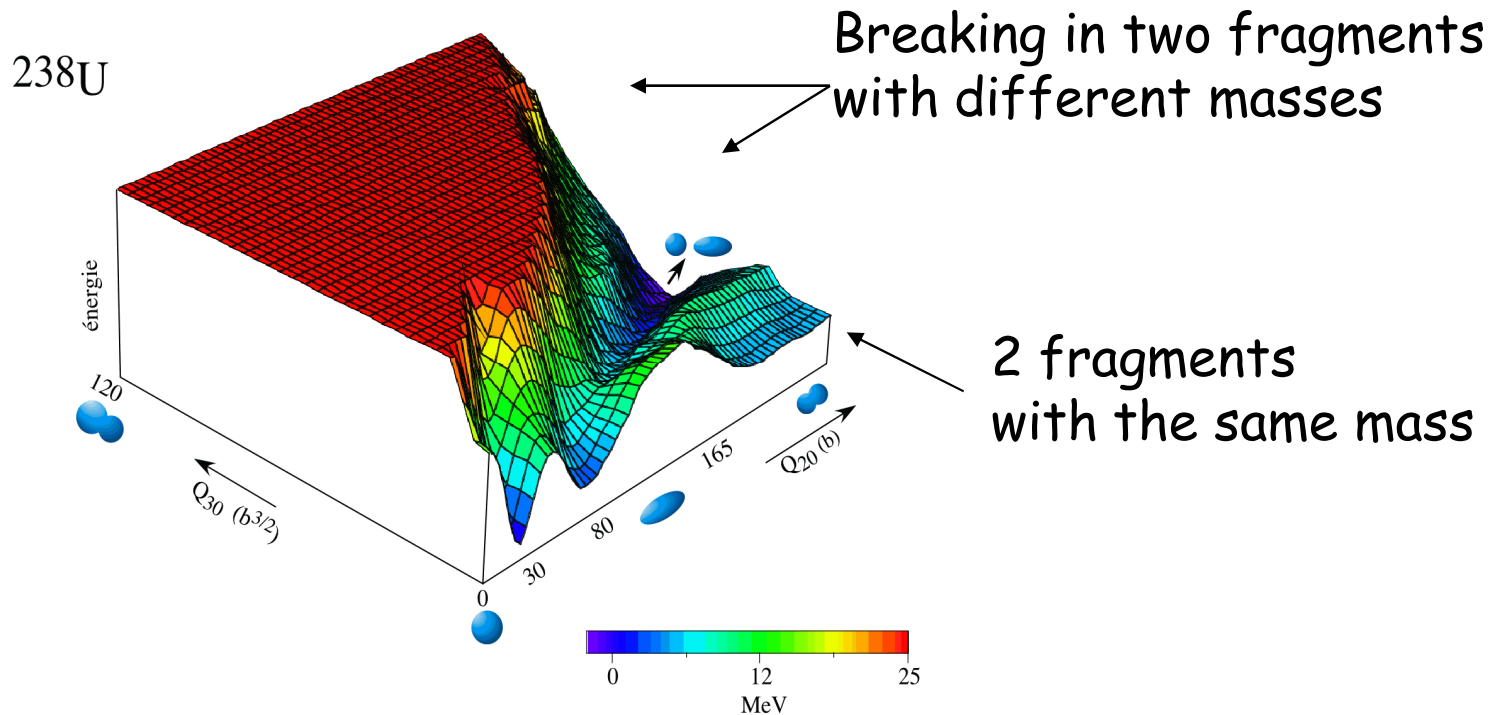
1) Static results:

- * Properties of the fissioning system
 - potential energy landscape of the fissioning system
- * Properties of the fragments
 - definition of the scission configurations
 - total kinetic energy
 - deformation
 - number of evaporated neutrons

2) Dynamical results

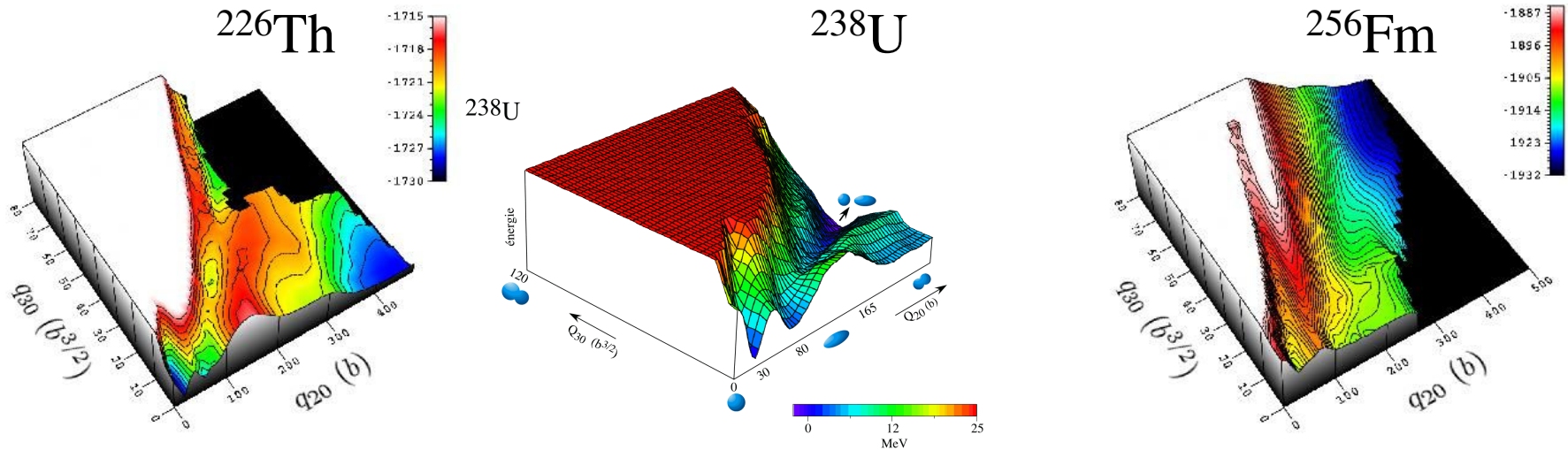
fission fragment mass distributions

Static results: 2D potential energy surface



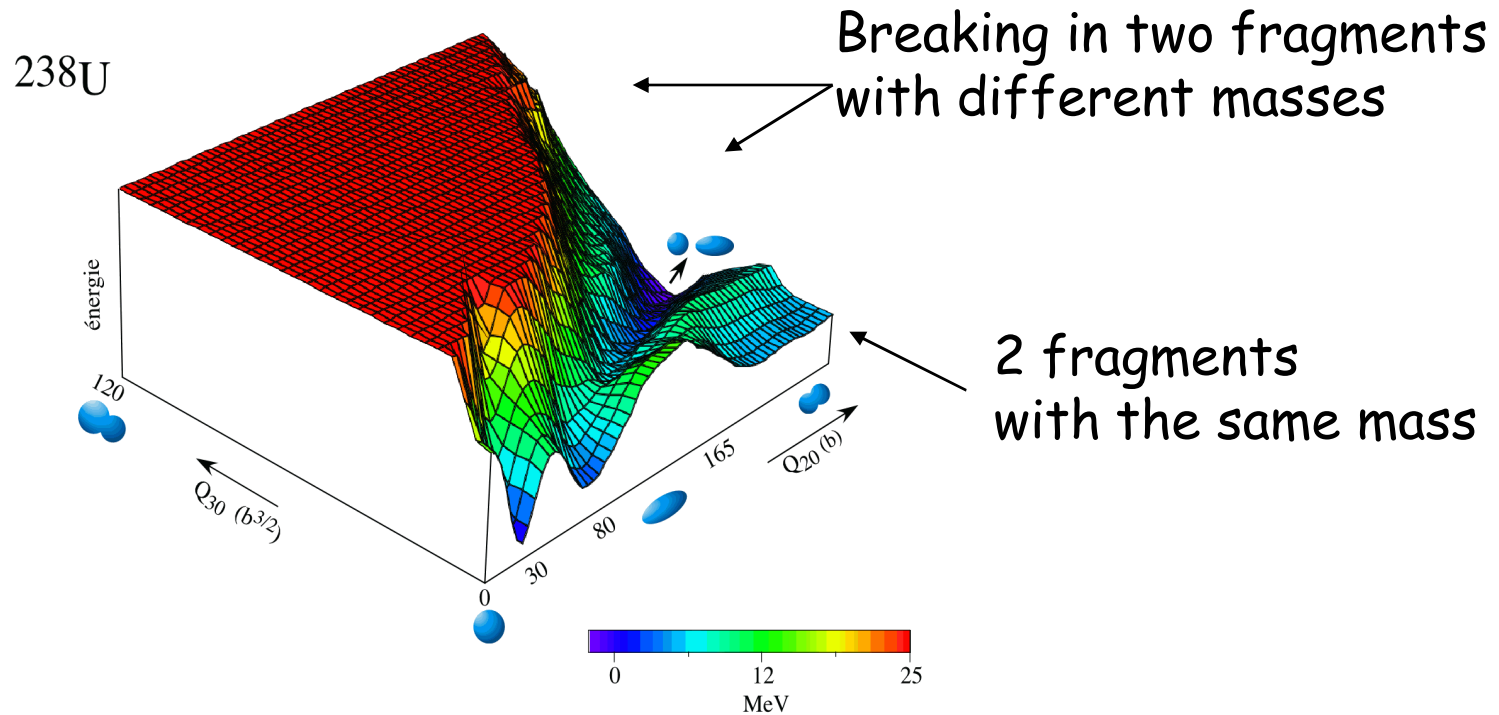
H. Goutte, P. Casoli, J.-F. Berger, Nucl. Phys. A 734, 217 (2004)

Topology of the surfaces



- * Superdeformed minima in ^{226}Th and ^{238}U
No SD minima for the systems with $N \geq 156$ (ex ^{256}Fm)
J.P. Delaroche, M. Girod, H. Goutte, J. Libert, NPA 771, 103 (2006)
- * Third minimum in ^{226}Th
- * Different topologies of the surfaces;
competitions between symmetric and asymmetric valleys

How can we determine the scission configurations ?



H. Goutte, P. Casoli, J.-F. Berger, Nucl. Phys. A 734, 217 (2004)

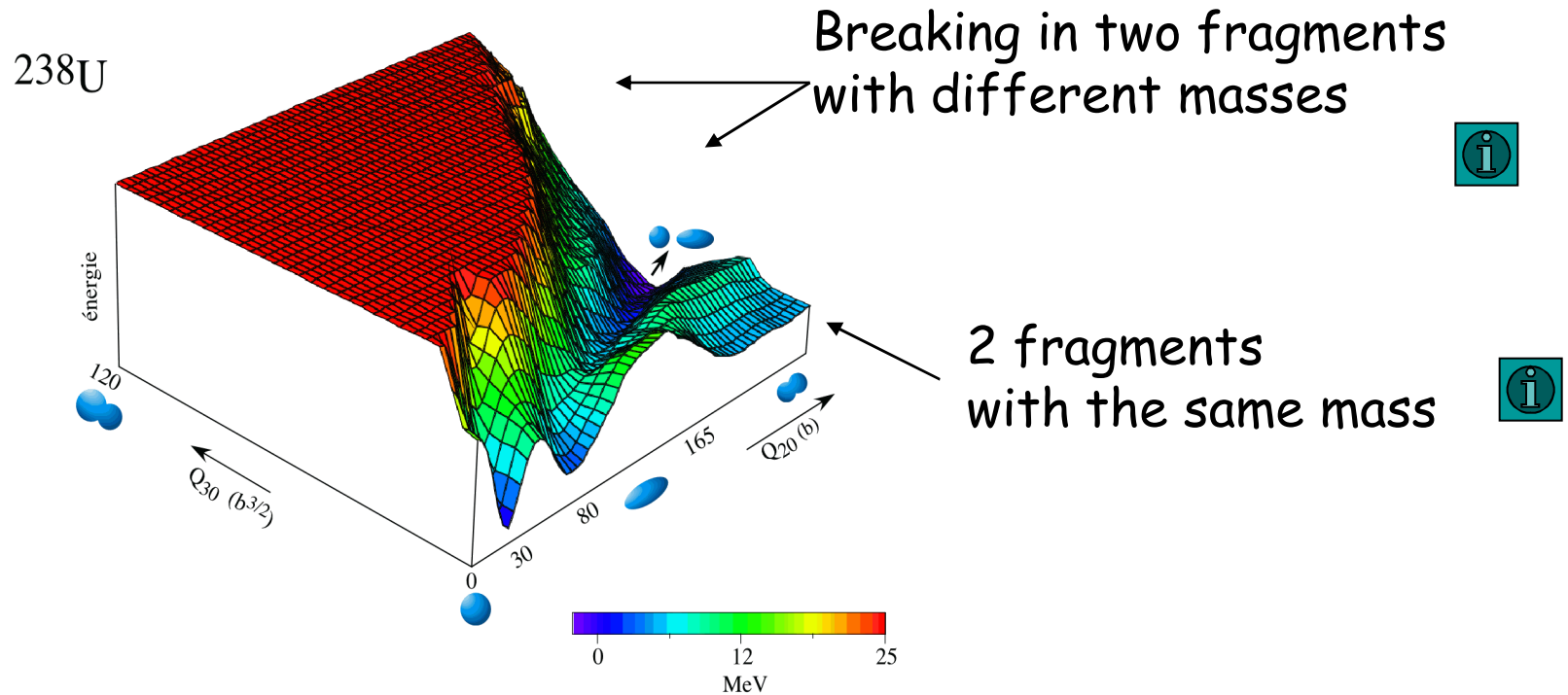
No topological definition of the exit points

Different prescriptions :

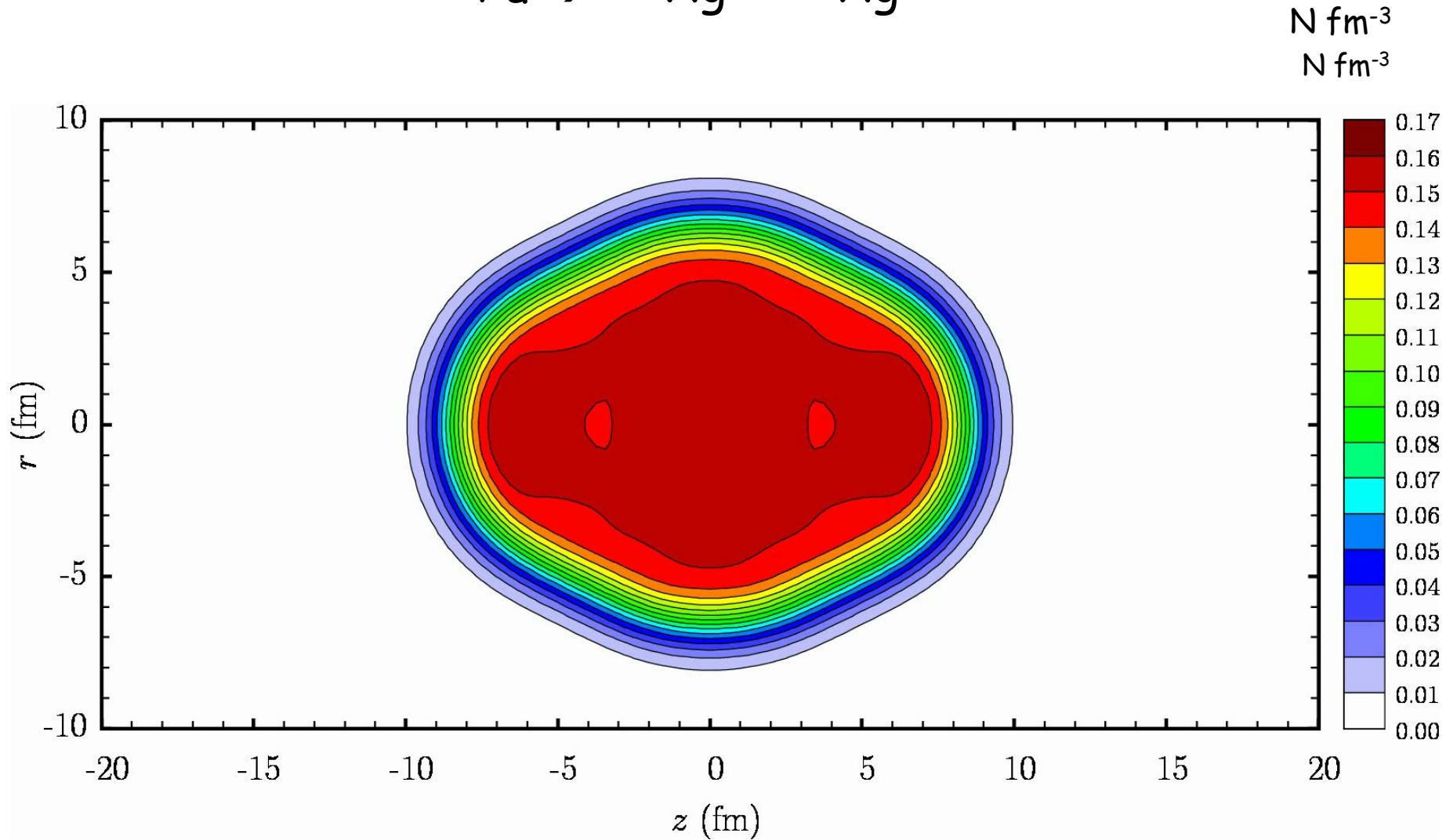
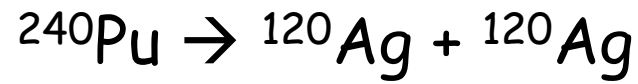
* E_{nucl} less than 1% of E_{coul}
L.Bonneau et al., PRC75 064313 (2007)

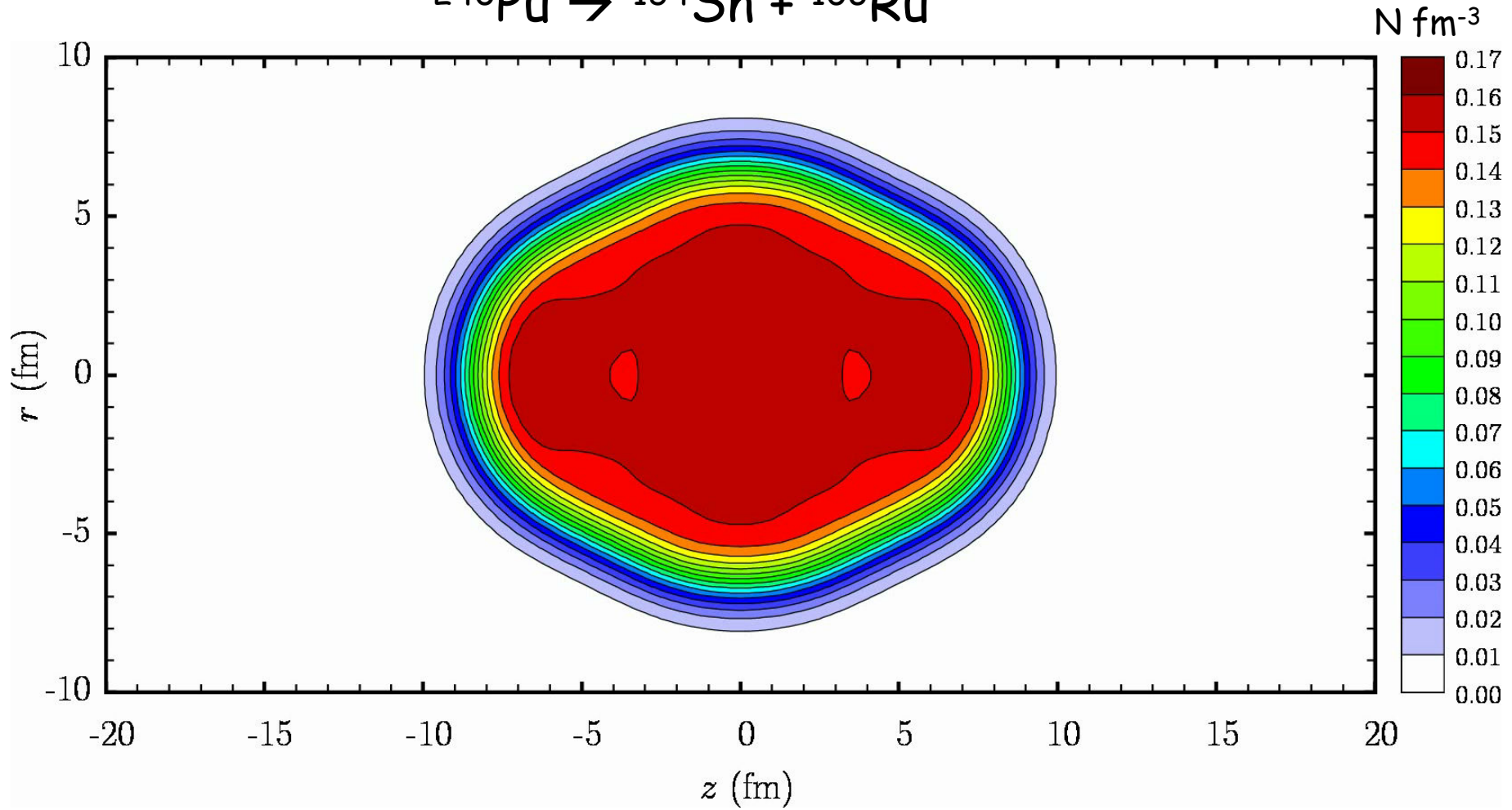
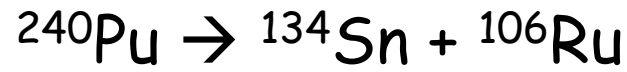
* "low density" in the neck

+ energy drop (≈ 15 MeV)
+ decrease of the hexadecapole ($\approx 1/3$)
J.-F. Berger et al., NPA428 23c (1984)



H. Goutte, P. Casoli, J.-F. Berger, Nucl. Phys. A 734, 217 (2004)





For the different scission configurations we determine :

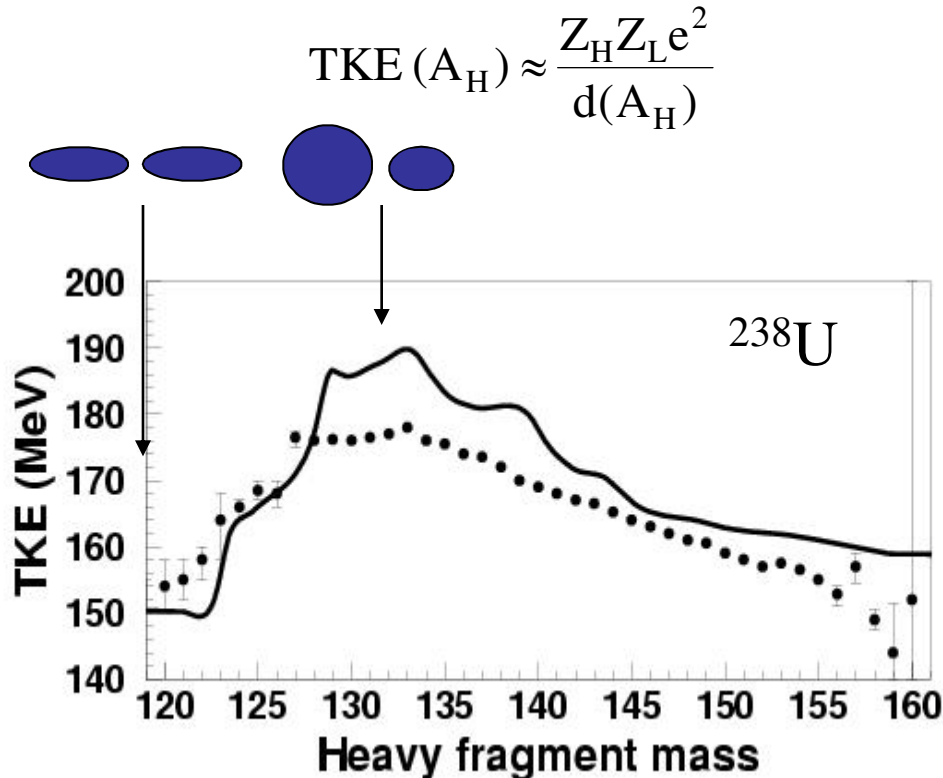
- masses and charges of the fragments,
- distance between the fragments
- deformations of the fragments,
- ...

We can derive :

- kinetic energy distributions
- « 1D static» mass and charge distributions,
- fragment deformation energy,
- polarisation of the fragments,
- ...

Total kinetic energy distribution

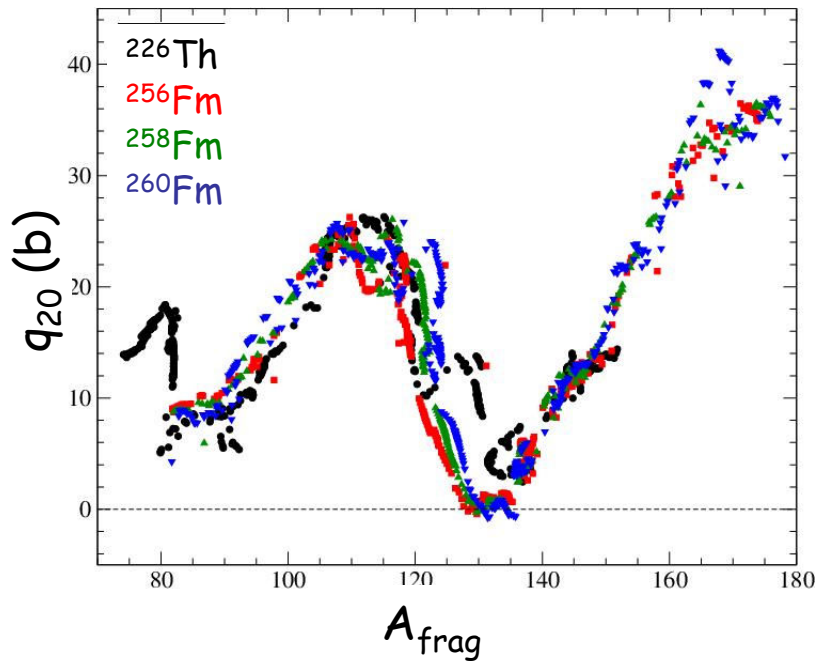
Exp: S. Pommé et al. Nucl. Phys. A572 (1994)



- Good overall agreement
- Over-estimation (up to 6%)

H. Goutte, J.-F. Berger, P. Casoli and D. Gogny, Phys. Rev. C 71, 024316 (2005)

Quadrupole deformation of the fission fragments at scission



The fragment deformation do not strongly depend upon the fissioning system

We find the well-known saw-tooth structure: minima for $A \sim 82$ and 130
 maxima for $A \sim 112$ and 170

Due to shell effects :

$$N = 82 \text{ and } Z = 50$$

$$N = 50 \text{ and } Z = 28$$

N. Dubray, H. Goutte, J.-P. Delaroche, Phys. Rev. C 77, 014310 (2008)

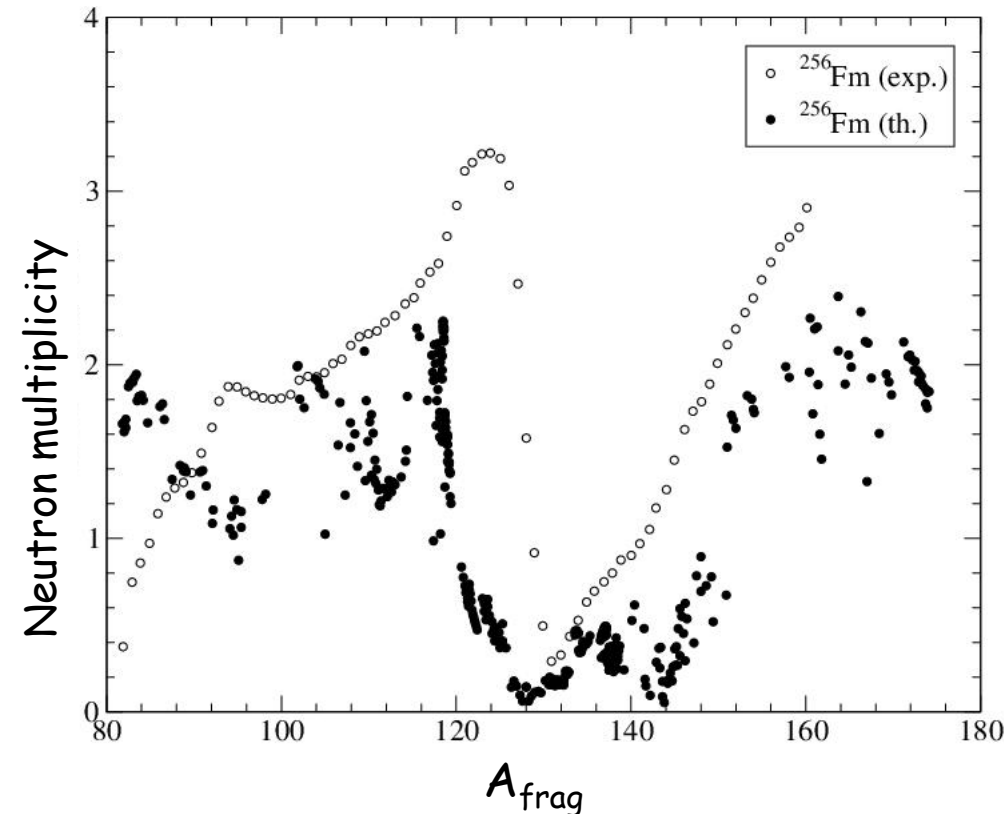
Prompt neutron emission

$$\nu(A) = \frac{E_{def}(A)}{E_k + B_n^*(A)}$$

Good qualitative agreement

but

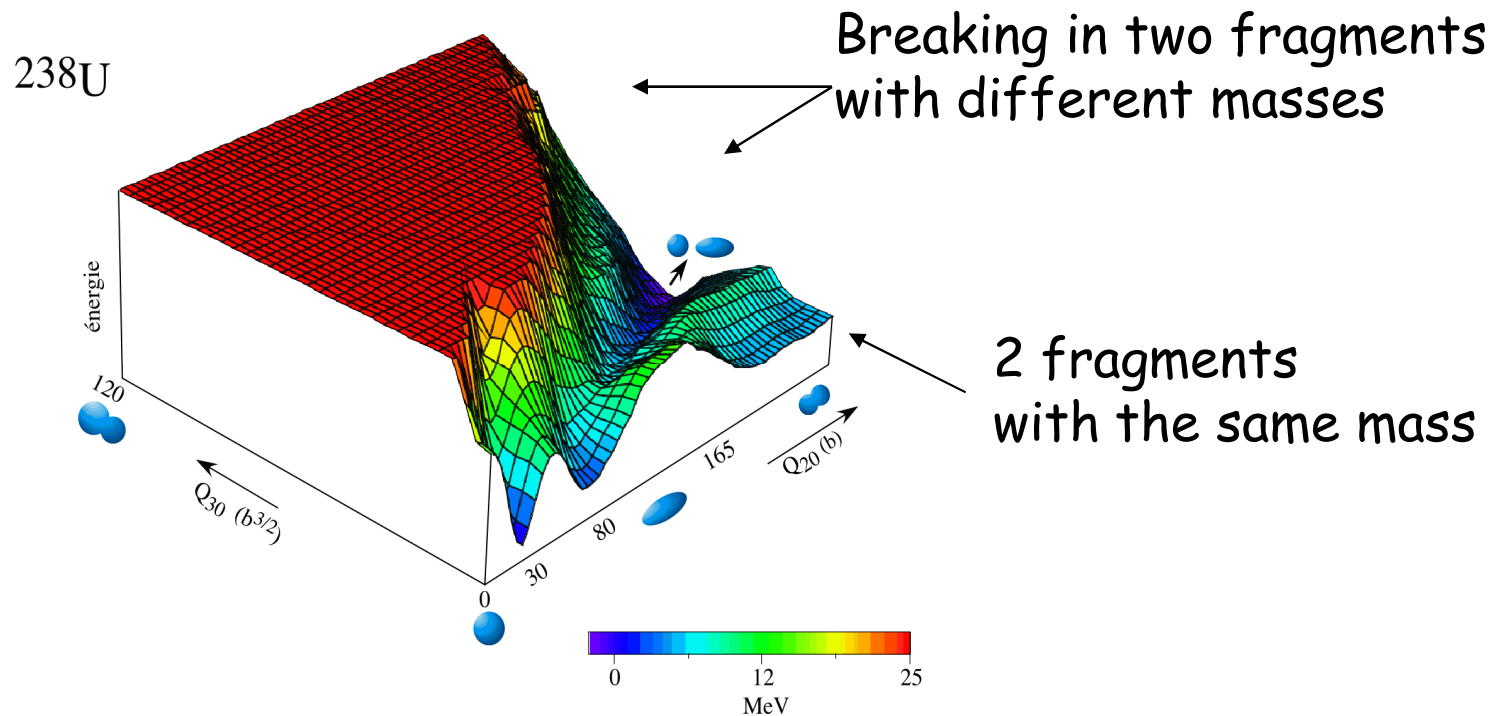
under estimation
probably due to the neglect of
intrinsic excitations of the
fission fragments



J.E. Gindler PRC 19, 1806 (1979)

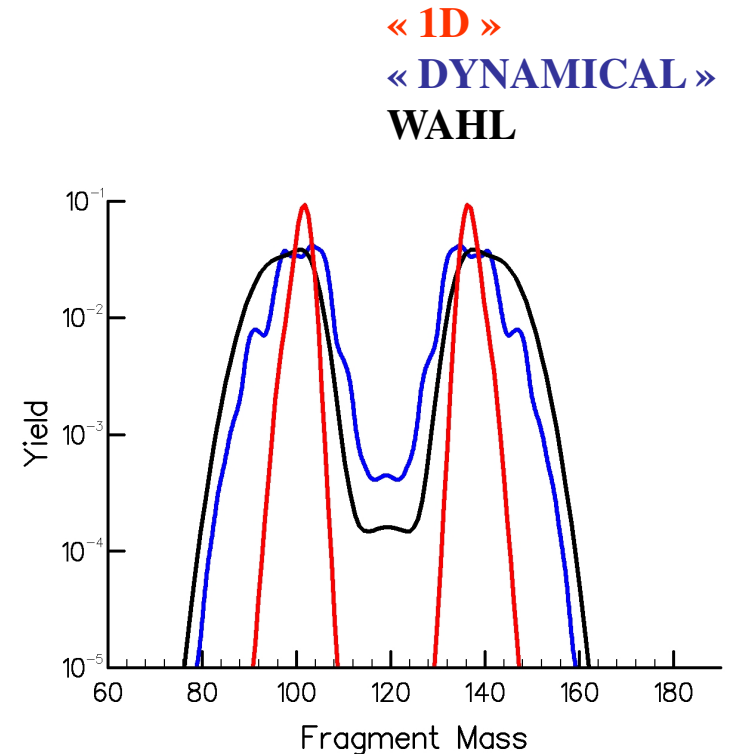
N. Dubray, H. Goutte, J.-P. Delaroche, Phys. Rev. C 77, 014310 (2008)

Time dependent propagation



Comparisons between 1D and « dynamical » distributions

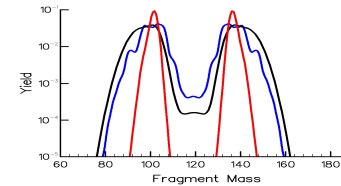
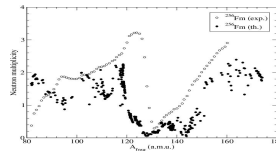
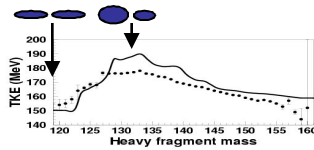
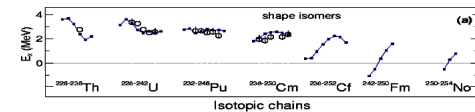
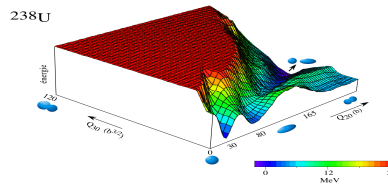
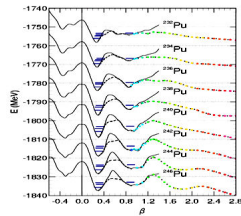
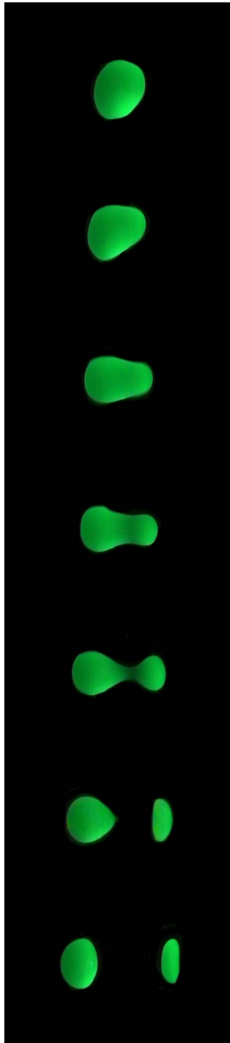
- Same location of the maxima
→ Due to properties of the potential energy surface (well-known *shell effects*)
- Spreading of the peaks
→ Due to *dynamical effects* :
(interaction between the 2 collective modes via potential energy surface and tensor of inertia)
- Good agreement with experiment



H. Goutte, J.-F. Berger, P. Casoli and D. Gogny, Phys. Rev. C71 (2005) 024316

Conclusion

« Coherent » determination of the properties of the fissioning system, the fission dynamics, and observables of the fragments.



-> good qualitative agreement with the exp. data, even if there are no free parameters

-> this strengthens our idea that microscopic approaches based on the mean field and the Gogny force are pertinent for the study of nuclear structure and fission.

Static properties of the fissioning systems

- * spectroscopy of heavy nuclei

R.D. Herzberg et al. Nature (London) 442 (2006), 896.

Collective dynamics

- * fission fragment distributions

(influence of the incident energy, of the mass of the fissioning system, fission modes, odd-even effects ...)

Properties of the fragments

- * measurements correlated in kinetic energy, mass, charge, neutron emission in which each fragment is identified in Z and A .
- * spectroscopy of the fission fragments

-> Need for existing facilities (CERN-nTOF, ISOLDE, SPIRAL, GSI, ILL, ...)
and future (FAIR, SPIRAL2, EURISOL, ...)

SOME GENERAL CONCLUSIONS ABOUT THE NUCLEAR PHYSICS

Current subjects under study in the community (non exhaustive list)

- * Structure of exotic nuclei
- * to improve the theoretical approaches for the many-body problem
- * to develop the same approach for both nuclear structure and nuclear reaction (ex: fission process)

*

To my opinion, nuclear physics both experimental and theoretical
is a very fantastic subject

Don't hesitate to contact me for PhD or post doc or any question
Heloise.goutte@cea.fr