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Theory Meets Experiment at LHC

Spin Dependence in Proton- Nucleus Elastic Scattering

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Outline

- Motivation & introduction
- Spin asymmetry in pp
- Spin asymmetry in pA
- Results
- Conclusions

Motivation

Measurement of elastic (**CNI region**) scatterings at high energies used to be used for polarization measurement, e.g. in AGS, RHIC

Today it is interesting physics itself. Latest results show non-zero spin-flip hadronic part in pp collisions.

Origin of spin-flip hadronic part:

- **Spin-flip pomeron?**
- Reggeon (main source of the spin flip at medium energy)?
- **Odderon?**
- **Other mechanism?**

What is CNI region?

Elastic scattering = very low 4-momentum transfer squared, $-t$, = very small angles

CNI (Coulomb-nuclear interference) region = a kinematical region where the interference electromagnetic-hadron terms dominates

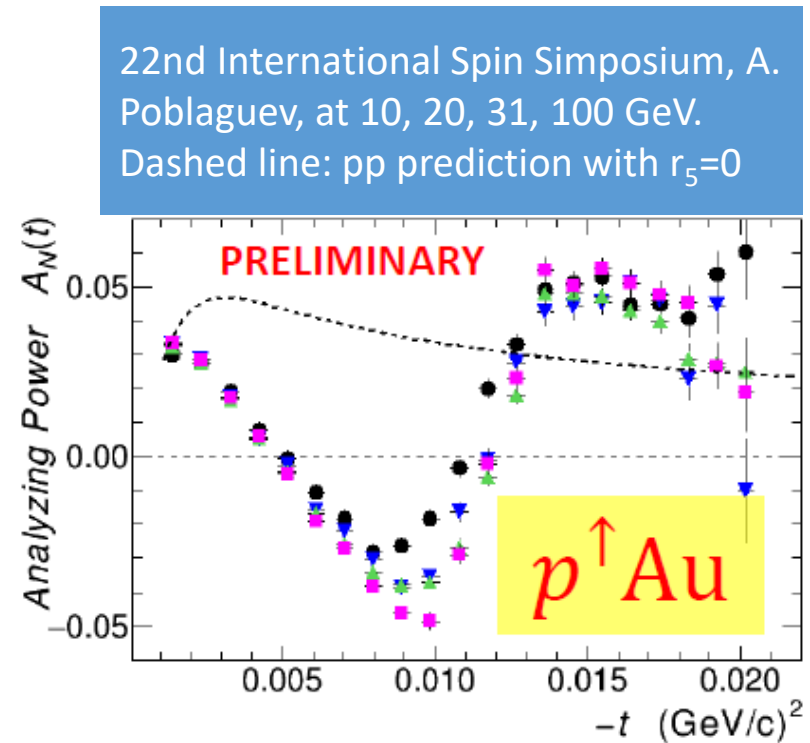
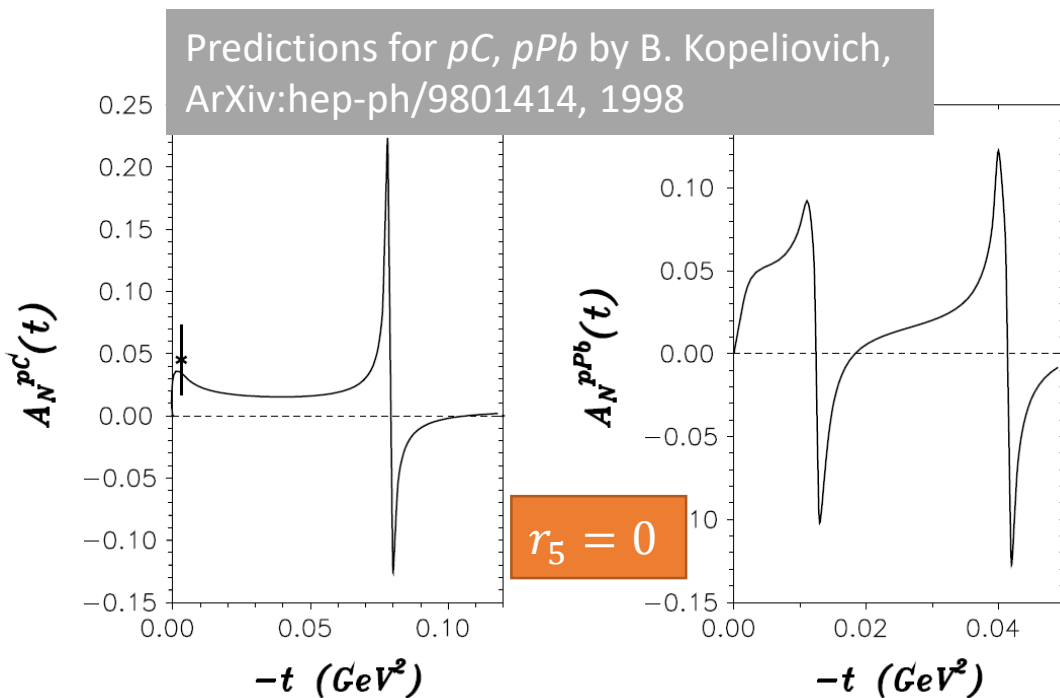
Measurable = single-spin asymmetry $A_N(t)$ = left-right asymmetry

Expected very small, only few percent

$$A_N \frac{d\sigma^{pp}}{dt} = 2\text{Im}[(\phi_1 + \phi_2 + \phi_3 - \phi_4)\phi_5^*]$$
$$\frac{d\sigma^{pp}}{dt} = |\phi_1|^2 + |\phi_2|^2 + |\phi_3|^2 + |\phi_4|^2 + 4|\phi_5|^2$$

Current status

New data = from pC polarimeter & HJET (pp , pAu , pAl)
 @ RHIC (pAu at different energies from BES)



pp elastic scattering theory

Spin-flip EM amplitude – well known, caused by the proton's magnetic moment.

Spin-flip hadronic amplitude – nobody know.

Introduce **parameter r_5** that need to be **fit**

$$r_5 = \frac{m_p \phi_5}{\sqrt{-t} \operatorname{Im} \phi_+}$$

ϕ_+ - non-flip amplitude

ϕ_5 - single spin-flip amplitude

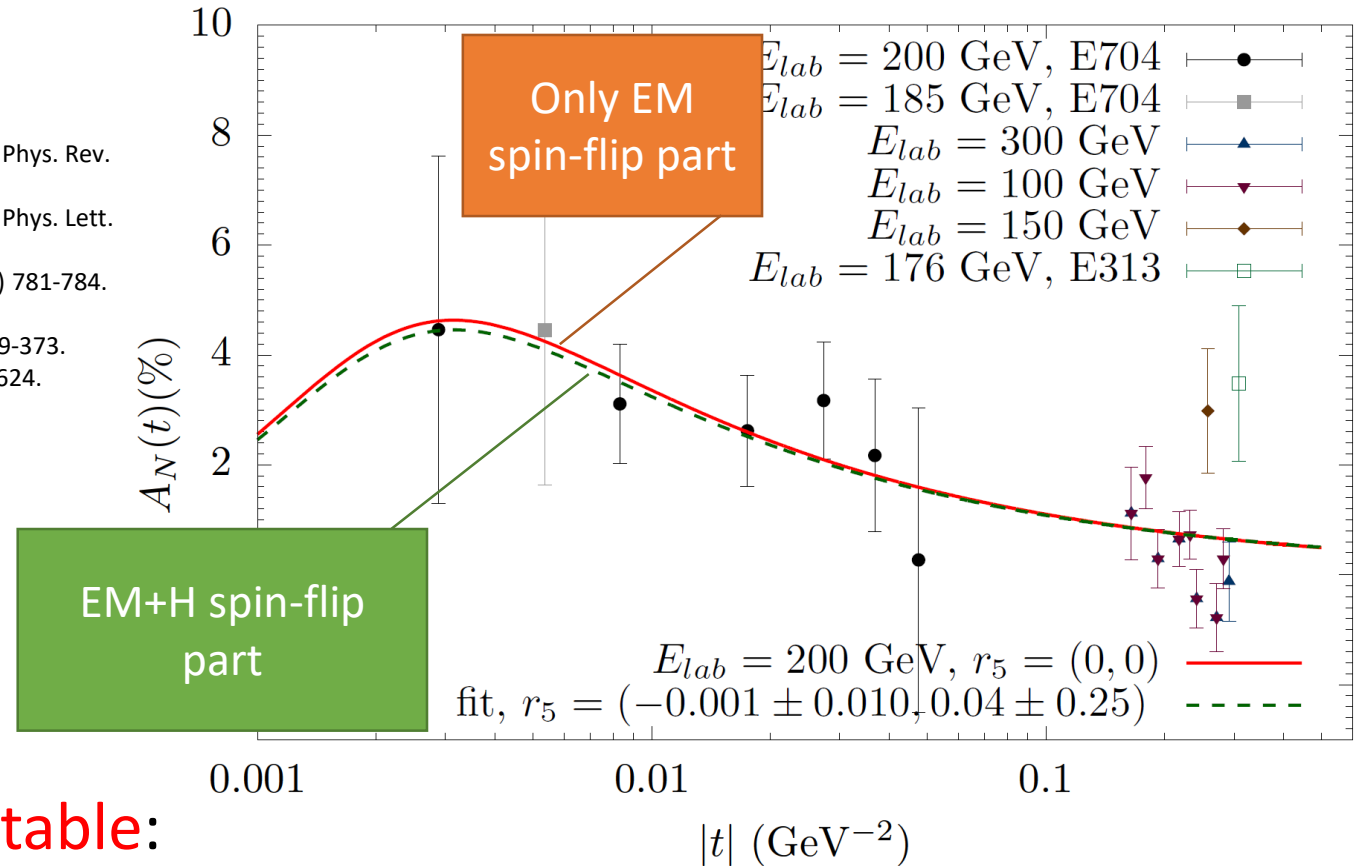
where

$$\phi_+ = \frac{1}{2}(\phi_1 + \phi_3)$$

$pp A_N(t)$ and old measurements

Data:

- E581/704 Collaboration, N. Akchurin et al., Phys. Rev. D48 (1993) 3026-3036.
- E581/704 Collaboration, N. Akchurin et al., Phys. Lett. B229 (1989) 299-303.
- J. H. Snyder et al., Phys. Rev. Lett. 41 (1978) 781-784. [Erratum: Phys. Rev. Lett.41,1256(1978)].
- G. Fidecaro et al., Phys. Lett. B76 (1978) 369-373.
- M. Corcoran et al., Phys. Rev. D22 (1980) 2624. [Erratum: Phys. Rev.D24,3010(1981)].

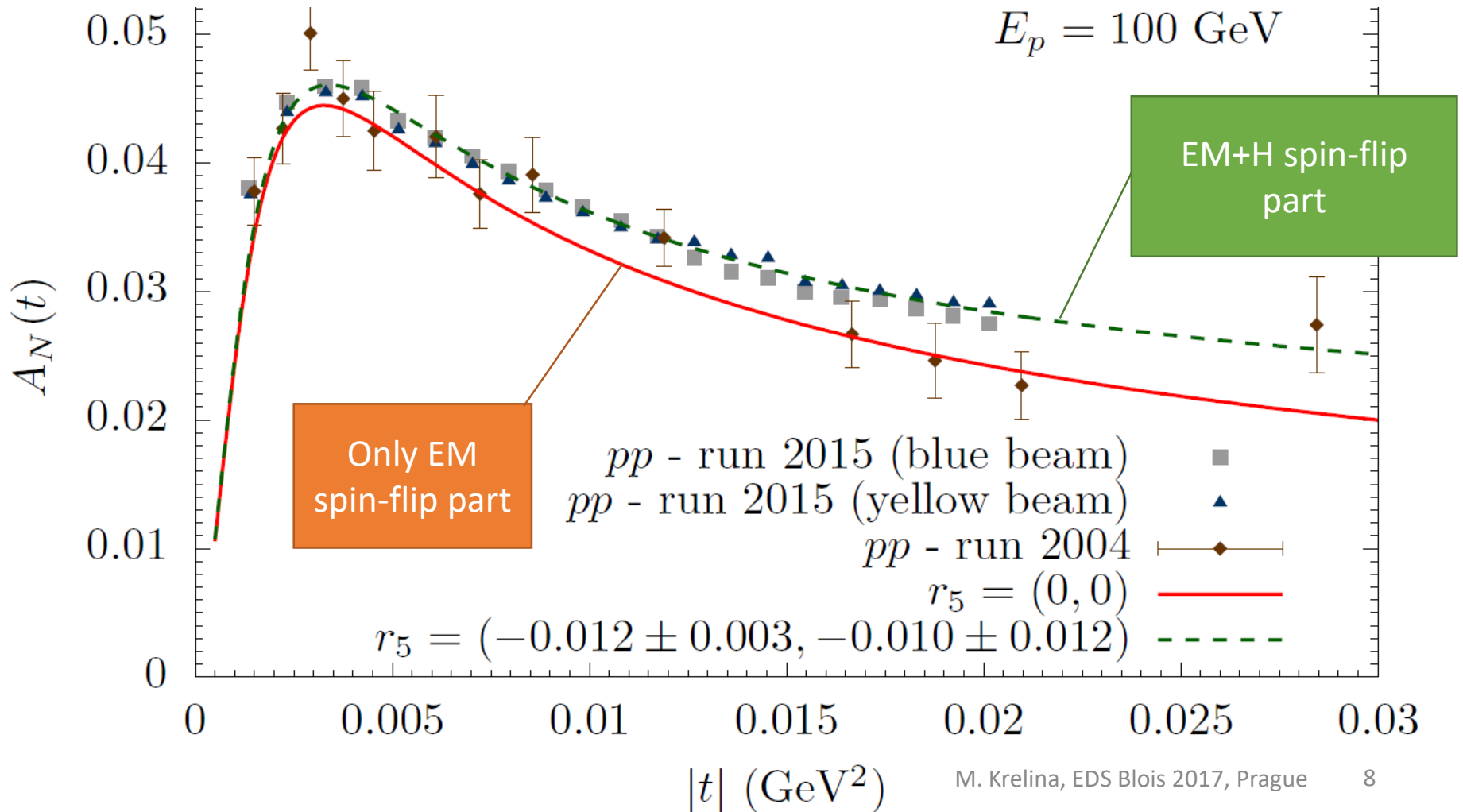


Fit of r_5 **not trustable**:

- **Neglected t dependence of r_5** (valid only for $tB \ll 1$, i.e. $t < 0.1 \text{ GeV}$)
- **Huge errors of small t data**

$pp A_N(t)$ @ RHIC

Situation has changed by measurement at RHIC. **Evidence of non-zero spin-flip hadronic amplitude**



Spin asymmetry in pA interactions

Spin asymmetry for elastic proton-nucleus interaction:

$$A_N \frac{d\sigma^{pA}}{dt} = 2\text{Im}[f_{++}^{pA} f_{+-}^{pA,*}]$$
$$\frac{d\sigma^{pA}}{dt} = |f_{++}^{pA}|^2 + |f_{+-}^{pA}|^2$$

Goal: predict pA $A_N(t)$ using r_5 from pp .

Theoretical predictions of $A_N(t)$ for pA done almost **20 years ago with no available data.**

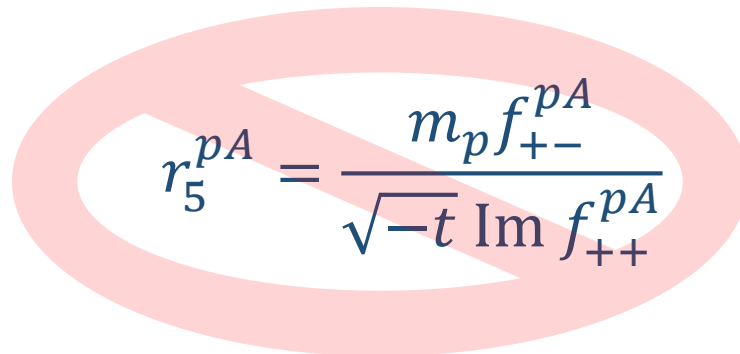
- *B. Z. Kopeliovich*, High-energy polarimetry at RHIC, in Workshop on Polarimetry at RHIC, (1998), arXiv:hep-ph/9801414 [hep-ph].
- *N. H. Buttimore, B. Z. Kopeliovich, E. Leader, J. Soer, and T. L. Trueman*, Phys. Rev. D59 (1999) 114010, arXiv:hep-ph/9901339 [hep-ph].
- *B. Z. Kopeliovich and T. L. Trueman*, Phys. Rev. D64 (2001) 034004, arXiv:hep-ph/0012091 [hep-ph].

Spin-flip hadronic amplitude in pA I.

Old papers:

Predicted that non-flip and spin-flip parts of hadronic amplitude **have the same nuclear form**

factor = r_5^{pA} is not subjected to any nuclear effects!


$$r_5^{pA} = \frac{m_p f_{+-}^{pA}}{\sqrt{-t} \operatorname{Im} f_{++}^{pA}}$$

Our statement: **r_5 is subjected to nuclear effects!**

Spin-flip hadronic amplitude in pA I.

Idea:

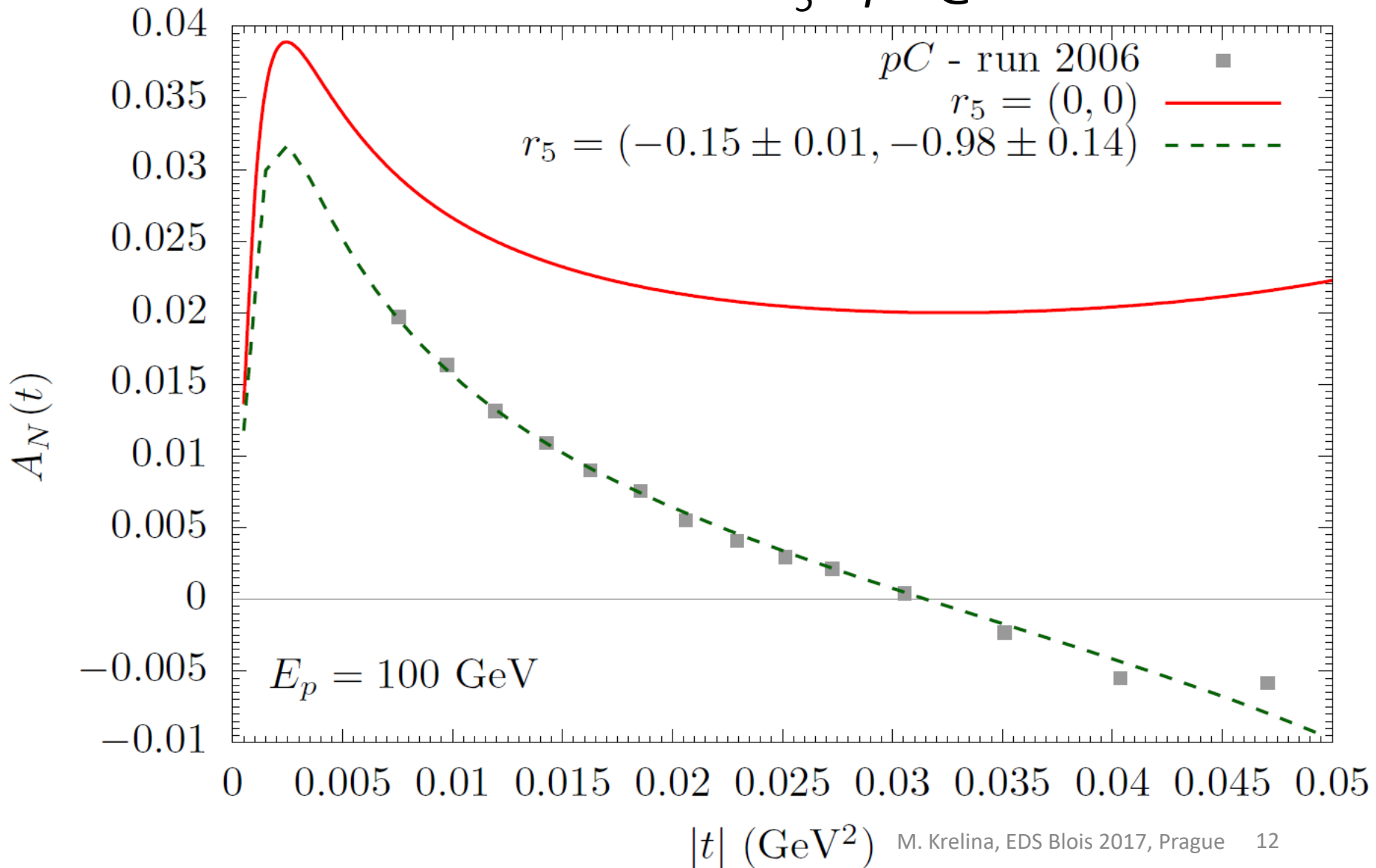
We factorize out **one spin-flip interaction** from Glauber elastic scattering amplitude

$$\begin{aligned}\tilde{F}(\vec{b}) &= 1 - \exp\left[-\int d^2s T_A(\vec{b})\Gamma(\vec{b} - \vec{s})\right] \\ &\quad + \mathbf{T}_A(\vec{b})\phi_5(\vec{q}) \exp\left[-\int d^2s T_A(\vec{b})\Gamma(\vec{b} - \vec{s})\right] \\ &= \tilde{F}^{++}(\vec{b}) + \tilde{F}^{+-}(\vec{b})\end{aligned}$$

Next: We can try to fit r_5 to existing pA data...

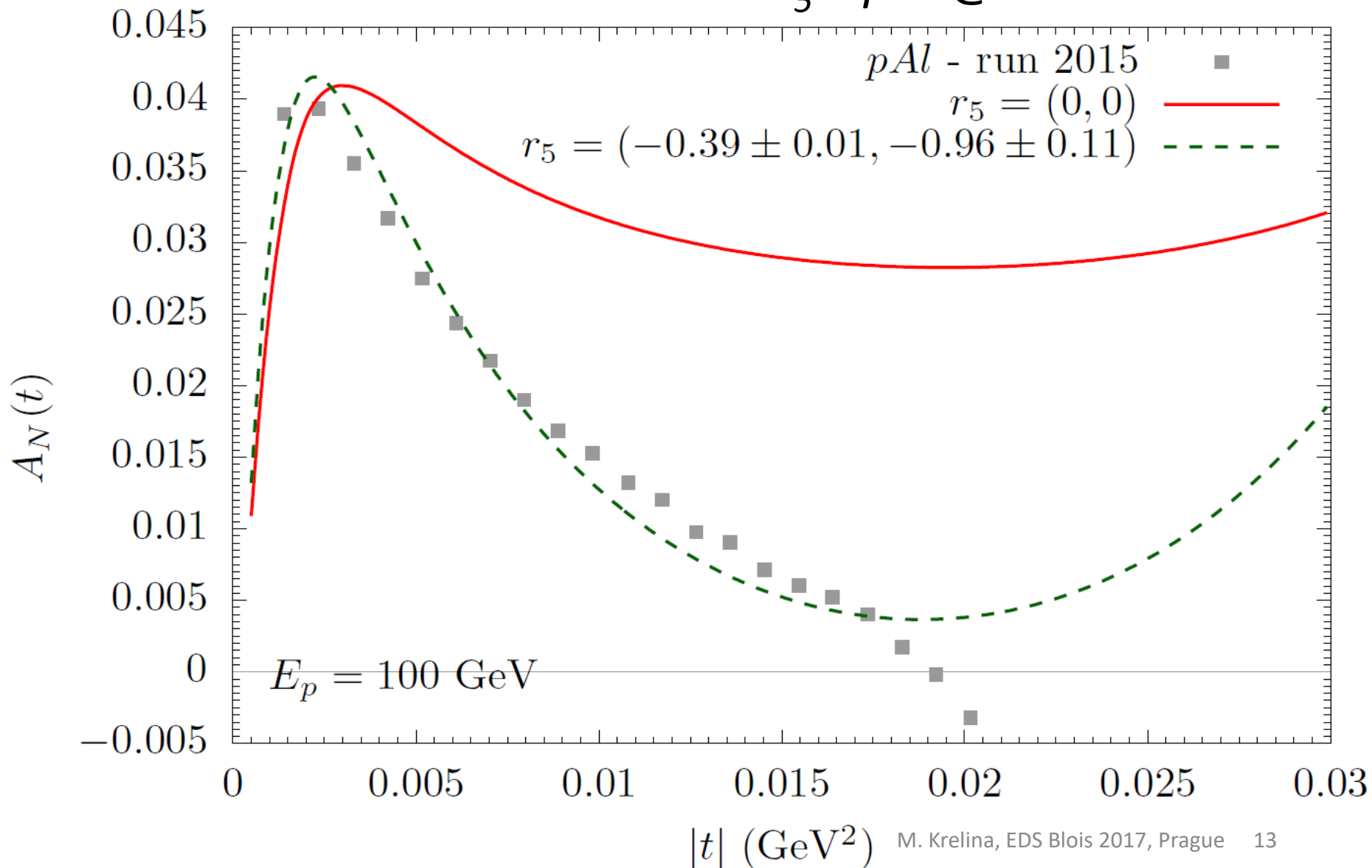
pC - fit

Fit – best r_5 - *pC* @ 100 GeV



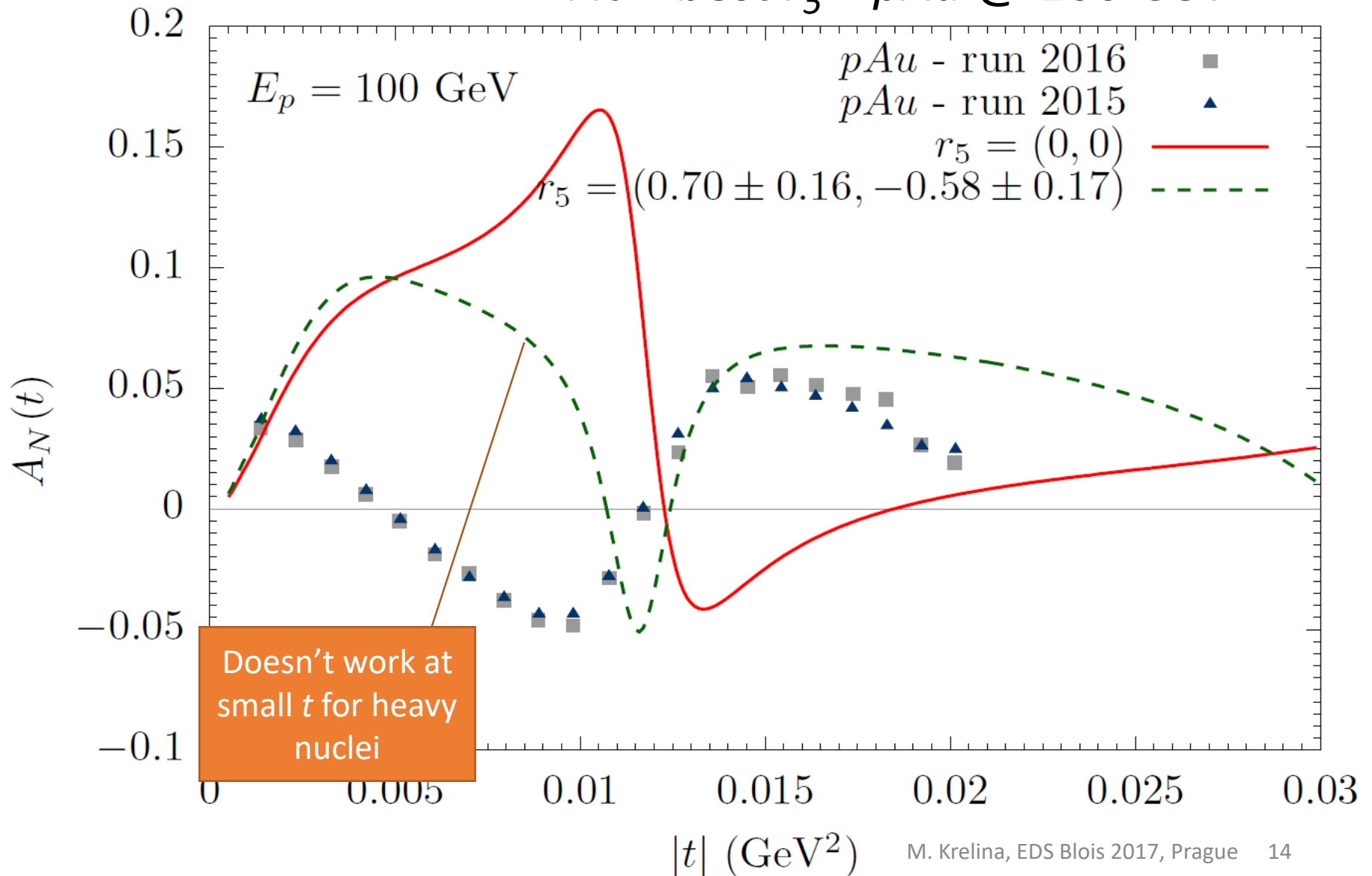
pAl - fit

Fit – best r_5 - *pAl* @ 100 GeV



pAu - fit

Fit – best r_5 - *pAu* @ 100 GeV



$pp - pA$ inconsistency

Fit of r_5 on pA is far from r_5 on pp .

- One would not expect so big a difference between pC and pp
 - Looks more like a problem with data
- This is the **main puzzle in pp/pA** for elastic spin-flip interactions

Why data on **heavy nuclei** are not in agreement?

- More tricky, more freedom in selecting of nuclear parametrizations, Coulomb phase, real part, ...
- Sensitivity on nuclear density
 - **Well studied** for Carbon
 - For **Gold** only one **parametrization from 1956!**

Conclusions

- pp data with **small errors available**, can fit r_5
- r_5 independent on t only for small t , approx. $t < 0.1$
- We fitted **significant real part of r_5** in pp
- **Formulation of r_5 dependence in pA is not right** → reformulation
 - Factorizing out one spin-flip interaction
 - This interaction dominates at the edge of the nucleus
- **r_5 fit for pC is not in correspondence with r_5 in pp**
 - *This inconsistency is independent on the r_5 formulation (old or new)*
- We see no **easy solution of this puzzle**
 - It looks to us more like an inconsistency in available data
- Not work for heavy nuclei – **more tricky**

Thank you for your attention

Acknowledgement

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pp elastic scattering theory I.

Five independent helicity
amplitudes:

$$\phi_1(s, t) = \langle ++ | M | ++ \rangle,$$

$$\phi_2(s, t) = \langle ++ | M | -- \rangle,$$

$$\phi_3(s, t) = \langle +- | M | +- \rangle,$$

$$\phi_4(s, t) = \langle +- | M | -+ \rangle,$$

$$\phi_5(s, t) = \langle ++ | M | +- \rangle,$$

**Cross section & single-spin
asymmetry $A_N(t)$:**

$$\frac{d\sigma}{dt} = \frac{2\pi}{s(s - 4m_p^2)} \{ |\phi_1|^2 + |\phi_2|^2 + |\phi_3|^2 + |\phi_4|^2 + |\phi_5|^2 \}$$

$$A_N \frac{d\sigma}{dt} = -\frac{4\pi}{s(s - 4m_p^2)} \text{Im} \{ (\phi_1 + \phi_2 + \phi_3 - \phi_4) \phi_5^* \}$$

pp amplitudes

$$\phi_1^h = \frac{\sigma_{tot}^{pp}}{8\pi} s(\rho_{pp} + i)e^{-\frac{1}{2}B|t|},$$

$$\phi_2^h = r_2 \frac{\sigma_{tot}^{pp}}{4\pi} s(\rho_{pp} + i)e^{-\frac{1}{2}B|t|} = r_2^2 \frac{t}{m_p^2} \frac{\sigma_{tot}^{pp}}{8\pi} s(\rho_{pp} + i)e^{-\frac{1}{2}B|t|} \approx 0,$$

$$\phi_3^h = \frac{\sigma_{tot}^{pp}}{8\pi} s(\rho_{pp} + i)e^{-\frac{1}{2}B|t|},$$

$$\phi_4^h = -r_4 \frac{t}{m_p^2} \frac{\sigma_{tot}^{pp}}{8\pi} s(\rho_{pp} + i)e^{-\frac{1}{2}B|t|} \approx 0,$$

$$\phi_5^h = r_5 \frac{\sqrt{-t}}{m_p} \frac{\sigma_{tot}^{pp}}{8\pi} s(\rho_{pp} + i)e^{-\frac{1}{2}B|t|},$$

$$G^2(t) = e^{-\frac{1}{2}B|t|}$$

$$e^{i\delta_{pp}} \phi_1^{em} = -\frac{s\alpha_{EM}}{|t|} G^2(t) e^{i\delta_{pp}},$$

$$e^{i\delta_{pp}} \phi_2^{em} = \frac{s\alpha_{EM}(\mu - 1)^2}{|t|} G^2(t) e^{i\delta_{pp}} \approx 0,$$

$$e^{i\delta_{pp}} \phi_3^{em} = -\frac{s\alpha_{EM}}{|t|} G^2(t) e^{i\delta_{pp}},$$

$$e^{i\delta_{pp}} \phi_4^{em} = -\frac{s\alpha_{EM}(\mu - 1)^2}{|t|} G^2(t) e^{i\delta_{pp}} \approx 0,$$

$$e^{i\delta_{pp}} \phi_5^{em} = -\frac{s\alpha_{EM}(\mu - 1)}{2m_p\sqrt{-t}} G^2(t) e^{i\delta_{pp}},$$

pp amplitude parameters

\sqrt{s} (GeV)	σ_{tot}^{pp} (mb)	ρ_{pp}	B (GeV ⁻²) [6]
6.56 (22 GeV in LAB) AGS	39.015	-0.241	10.48
20	39.193	-0.021	11.7
40	41.346	0.051	12.57
62.3	43.482	0.082	12.97
200	51.688	0.126	14.47
7000	97.283	0.137	19.90

Spin-flip hadronic nuclear form factor

Our statement: r_5 is subjected to nuclear effects!

Non-flip hadronic form factor:

$$\tilde{F}(\vec{b}) = 1 - \exp \left[- \int d^2 s T_A(\vec{s}) \Gamma(\vec{b} - \vec{s}) \right]$$

Now, let's factorize out one interaction:

$$\begin{aligned} \tilde{F}(\vec{b}) &= 1 - \int \prod_{j=1}^A d^3 q_j \rho_j(\vec{q}_j) (1 - \Gamma_j(\vec{b} - \vec{s}_j)) \\ &= 1 - \left[\int d^3 q \rho_j(\vec{q}) (1 - \Gamma(\vec{b} - \vec{s})) \right] \left[\int \prod_{j=2}^A d^3 q_j \rho_j(\vec{q}_j) (1 - \Gamma_j(\vec{b} - \vec{s}_j)) \right] \\ &= 1 - \exp \left[- \int d^2 s T_A(\vec{s}) \Gamma(\vec{b} - \vec{s}) \right] + T_A(b) f^{pp,5}(\vec{q}) \exp \left[- \int d^2 s T_A(\vec{s}) \Gamma(\vec{b} - \vec{s}) \right] \\ &= \tilde{F}^{nf}(\vec{b}) + \tilde{F}^{sf}(\vec{b}) \end{aligned}$$

pA amplitudes I.

All pA amplitudes:

$$f_{++}^{pA,h} = \frac{\sigma_{tot}^{pA}}{4\sqrt{\pi}} F_A^h(q^2),$$

$$f_{+-}^{pA,h} = r_5 \frac{\sqrt{-t}}{m_p} \frac{\sigma_{tot}^{pp}}{8\sqrt{\pi}} (\rho_{pp} + i) F_A^{h,5}(q^2, r_5),$$

$$e^{i\delta_{pA}} f_{++}^{pA,em} = \frac{2\sqrt{\pi} Z \alpha_{EM}}{q^2} F_A^{em}(q^2) e^{i\delta_{pA}},$$

$$e^{i\delta_{pA}} f_{+-}^{pA,em} = \frac{\sqrt{\pi} Z \alpha_{EM}}{m_N q} (\mu_p - 1) F_A^{em}(q^2) e^{i\delta_{pA}},$$

pA amplitudes II.

Form factors:

$$F_A^{em}(q^2) = \frac{1}{A} \int d^2b e^{i\vec{q}\cdot\vec{b}} T_A(b)$$

$$F_A^h(q^2) = \frac{2i}{\sigma_{tot}^{pA}} \int d^2b e^{i\vec{q}\cdot\vec{b}} \left[1 - e^{-\frac{1}{2}\sigma_{tot}^{NN} (1-i\rho_{pp}) T_A(b)} \right]$$

$$F_A^{h,5}(q^2, r_5) = \int d^2b e^{i\vec{q}\cdot\vec{b}} T_A^h(b) e^{-\frac{1}{2}\sigma_{tot}^{NN} (1-i\rho_{pp}) T_A(b)}$$

Other factors:

$$\delta_{pA} = \alpha_{EM} Z_1 Z_2 e^{2\omega} [2E_1(2\omega) - E_1(\omega)],$$

$$\omega = \frac{1}{4} q^2 B_{pA},$$