pp Elastic Scattering at LHC

Proton Structure

Outer Cloud – Inner Shell – Gluon Core

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This proton structure leads to three main processes in elastic scattering



The first process occurs in the small |t| region. The outer cloud of $q\bar{q}$ condensed ground state of \leftarrow one proton interacts with that of the other.

Diffraction Amplitude

$$T_D(s,t) = i p W \int_0^\infty b \, db \, J_0(b,q) \, \Gamma_D(s,b)$$

Profile Function

$$\Gamma_D(s,b) = g(s) \left[\frac{1}{1 + e^{(b-R)/a}} + \frac{1}{1 + e^{-(b+R)/a}} - 1 \right]$$

where $R = R_0 + R_1 \left(\ln s - \frac{i \pi}{2} \right)$, $a = a_0 + a_1 \left(\ln s - \frac{i \pi}{2} \right)$ and g(s) is a complex crossing even function.

Our Diffraction Amplitude - Asymptotic Properties

$$\sigma_{tot}(s) \sim (a_0 + a_1 \ln s)^2 \qquad \checkmark \text{ (Froissart - Martin bound)}$$

$$\rho(s) \simeq \frac{\pi a_1}{a_0 + a_1 \ln s} \qquad \checkmark \text{ (derivative dispersion relation)}$$

$$T_D(s,t) \sim i s \ln^2 s \ f(|t| \ln^2 s) \checkmark \text{ (Auberson-Kinoshita-Martin scaling)}$$

$$T_D^{\overline{pp}}(s,t) = T_D^{pp}(s,t) \qquad \checkmark \text{ (crossing even)}$$

Beyond diffraction scattering –

The second process becomes important at $|t| \gtrsim 0.5 \ GeV^2$, when the baryonic charge core of one proton probes that for the other via multiple vector meson ω -exchanges.



Multiple $\boldsymbol{\omega}$ -exchanges accompanied by the cloud-cloud interaction

The **third** process also begins at $|t| \gtrsim 0.5 \ GeV^2$ (impact parameter $b \leq 0.3 \ fm$) with gluon exchanges between valence quarks.



The third process viewed in momentum space.

We combine our multiple ω -exchange amplitude with our low-x gluongluon interaction amplitude by using a joint eikonal:

$$\chi_{\omega}(s,b) + \chi_{gg}(s,b).$$

Our combined hard scattering amplitude is then

$$T_{\omega+gg}(s,t) \simeq \left[\left(\eta_0 + \frac{c_0}{\left(s \, e^{i\frac{\pi}{2}}\right)^{\sigma}} \right) + i \left(\lambda_0 - \frac{d_0}{s^2} \right) \right] \left[T_{\omega}(s,t) + e^{i \chi_{\omega}(s,\tilde{b})} T_{gg}(s,t) \right].$$

 $T_{\omega}(s,t)$: scattering amplitude due to multiple ω -exchanges $T_{gg}(s,t)$: gluon-gluon scattering amplitude

 $e^{i \chi_{\omega}(s,\tilde{b})}$: additional screening of $T_{gg}(s,t)$ by the baryonic-charge shell.

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Something was missing in our low- $|t| \frac{d\sigma}{dt}$ calculation...

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Polarization of the Quark-Antiquark Cloud





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Conclusions

Over four decades of collider experience by many groups...

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CERN ISR 23 - 62 \text{ GeV}(pp)

Fermilab 27.4 GeV (pp)

CERN SPS 546, 630 GeV (\overline{p}p)

Tevatron 1.8 TeV (\overline{p}p)

Tevatron 1.96 TeV (\overline{p}p)

CERN LHC 7, 8, 13...TeV (pp)
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and much theoretical development...

have led us envision the **Structure of the Proton**.



Structure of the **Proton**



References

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The scalar field $\zeta(r)$ as a function of r. $r_{\rm C}$: radius of the core, $r_{\rm B}$: radius of the baryonic charge density.