# Exclusive production of resonances in proton-proton collisions at high energies

#### Rainer Schicker (in coll. with R.Fiore, L.Jenkovszky)

Phys. Inst., Heidelberg

June 29, 2017

Central production at hadron colliders

Dual resonance model Pomeron-Pomeron scattering

Nonlinear, complex meson Regge trajectories

Pomeron-Pomeron cross section

Pomeron distribution in the proton

Cross sections at hadron level

Conclusions, outlook

#### Central production at hadron colliders I

mass spectra of exclusive pion pairs in proton-proton collisions



Fig. 2. The centrally produced  $\pi^+\pi^-$  effective mass spectrum at  $\sqrt{s} = a$ ) 12.7 GeV and b) 29 GeV using a LL trigger and c) at 29 GeV from a LR trigger.

Rainer Schicker (Heidelberg) Resonance production in Proton-Proton collisions June 29, 2017 3 / 24

## Central production at hadron colliders II

#### mass spectra of exclusive pion pairs in proton-proton collisions



## Central production event topologies

central production with/without diffractive dissociation



Pomeron-Pomeron-meson vertex in all three topologies



amplitude

 $\mathsf{Pomeron}\text{-}\mathsf{Pomeron}\to\mathsf{meson}$ 

• cross section Pomeron-Pomeron  $\rightarrow$  meson

#### Dual resonance model of Pomeron-Pomeron scattering

- many overlapping resonances at low masses  $M < 3 \text{ GeV}/c^2$
- transition into continuum
- Dual Amplitude with Mandelstam Analyticity (DAMA)

$$\left| \sum_{p}^{p} \left( X \right)^{2} = \sum_{\chi} \left( \sum_{u \text{ intarity}} = \sum_{u \text{ intarity}} \left( \sum_{u \in U} \left( X \right)^{2} \right) \left( X \right)^{2} \left( X \right)^$$

- DAMA requires the use of nonlinear, complex Regge traject.resonance widths are provided by imaginary part of DAMA
- direct-channel pole decomposition relevant for central prod.

$$A(M_X^2, t) = a \sum_{i=f, P} \sum_J \frac{[f_i(t)]^{J+2}}{J - \alpha_i(M_X^2)}.$$
 (1)

#### Nonlinear, complex meson trajectories

 real and imaginary part of trajectory are connected by dispersion relation

$$\Re e \,\alpha(s) = \alpha(0) + \frac{s}{\pi} PV \int_0^\infty ds' \frac{\Im m \,\alpha(s')}{s'(s'-s)}.$$
 (2)

imaginary part is related to the decay width

$$\Gamma(M_R) = \frac{\Im m \,\alpha(M_R^2)}{\alpha' M_R}.$$
(3)

imaginary part chosen as sum of single threshold terms

$$\Im m \alpha(s) = \sum_{n} c_n (s - s_n)^{1/2} \left(\frac{s - s_n}{s}\right)^{|\Re e \alpha(s_n)|} \theta(s - s_n). \quad (4)$$

- imaginary part of trajectory shown in Eq.(4) has correct threshold and asymptotic behaviour
- c<sub>n</sub> are expansion coefficients

#### Two f-trajectories

#### use the following f-resonances for fitting two f-trajectories

	IG Ibc	Traj.	M (GeV)	$\Gamma$ (GeV)
f <sub>0</sub> (980)	0+0++	$f_1$	$0.990 \pm 0.020$	$0.070 \pm 0.030$
$f_1(1420)$	0+1++	fi	$1.426 \pm 0.001$	$0.055 \pm 0.003$
$f_2(1810)$	0+2++	$f_1$	$1.815 \pm 0.012$	$0.197 \pm 0.022$
f4(2300)	0+4++	f1	$2.320 \pm 0.060$	$0.250 \pm 0.080$
$f_2(1270)$	0+2++	$f_2$	$1.275 \pm 0.001$	$0.185 \pm 0.003$
f4(2050)	0+4++	<b>f</b> 2	$2.018 \pm 0.011$	$0.237 \pm 0.018$
$f_6(2510)$	0+6++	$f_2$	$2.469 \pm 0.029$	$0.283 \pm 0.040$



Rainer Schicker (Heidelberg)

Resonance production in Proton-Proton collisions

June 29, 2017 8 / 24

#### Two f-trajectories

#### use the following f-resonances for fitting two f-trajectories

	IG Ibc	Traj.	M (GeV)	$\Gamma$ (GeV)
f <sub>0</sub> (980)	0+0++	fı	$0.990 \pm 0.020$	$0.070 \pm 0.030$
$f_1(1420)$	0+1++	fi	$1.426 \pm 0.001$	$0.055 \pm 0.003$
$f_2(1810)$	0+2++	$f_1$	$1.815 \pm 0.012$	$0.197 \pm 0.022$
f4(2300)	0+4++	fi	$2.320 \pm 0.060$	$0.250 \pm 0.080$
$f_2(1270)$	0+2++	$f_2$	$1.275 \pm 0.001$	$0.185 \pm 0.003$
f4(2050)	0+4++	f2	$2.018 \pm 0.011$	$0.237 \pm 0.018$
$f_6(2510)$	0+6++	$f_2$	$2.469 \pm 0.029$	$0.283 \pm 0.040$



#### The Pomeron trajectory

the following parameterisation is used

$$\alpha_P(M^2) = \frac{1 + \varepsilon + \alpha' M^2}{1 - c\sqrt{s_0 - M^2}}$$
(5)

 $\varepsilon = 0.08$ ,  $\alpha' = 0.25 \text{ GeV}^{-2}$ ,  $c = \alpha'/10 = 0.025$ , s<sub>0</sub> the two pion thresh. s<sub>0</sub> = 4m<sub>\pi</sub><sup>2</sup>.

# The $f_0(500)$ resonance

- $\blacksquare$  exclusive pion pair mass distribution at COMPASS shows broad continuum at  $m_{\pi^+\pi^-}<1~{\rm GeV/c^2}$
- this mass range attributed to  $f_0(500)$  resonance
- at hadron colliders, this mass range is seriously suffering from missing acceptance for pairs of low tranverse momentum
- $f_0(500)$  is of prime importance for understanding of
  - attractive part of nucleon-nucleon interaction
  - spontaneous breaking of chiral symmetry
- parameterised by Breit-Wigner form

$$A(M^{2}) = a \; \frac{-M_{0}\Gamma}{M^{2} - M_{0}^{2} + iM_{0}\Gamma} \tag{6}$$

# The Pomeron-Pomeron cross section

• the Pomeron-Pomeron cross section derived from imaginary part of trajectories  $(f_1, f_2, Pomeron)$  by the optical theorem

$$\sigma_t^{PP}(M^2) = \Im m A(M^2, t=0) =$$

$$\sum_{i=f,P} \sum_{J} \frac{[f_i(0)]^{J+2} \Im m \,\alpha_i(M^2)}{(J - \Re e \,\alpha_i(M^2))^2 + (\Im m \,\alpha_i(M^2))^2}.$$
 (7)

• the  $f_0(500)$  resonance contributes to the cross section

$$\sigma_{f_0(500)}^{PP}(M^2) = a\sqrt{1. - \frac{4 m_\pi^2}{M^2}} \frac{M_0^2 \Gamma^2}{(M^2 - M_0^2)^2 + M_0^2 \Gamma^2}, \qquad (8)$$

with the resonance mass of  $M_0=$  (0.40–0.55) GeV and a width  $\Gamma$  = (0.40–0.70) GeV

background term

$$\sigma_{backgr.}^{PP}(M^2) = c * (0.1 + \log(M^2)) \text{ mb},$$
 (9)

Rainer Schicker (Heidelberg) Resonance production in Proton-Proton collisions June 29, 2017 12 / 24

# The Pomeron-Pomeron cross section

- contributions of the  $f_0(500), f_1, f_2$  and Pomeron trajectory, and the background
- R.Fiore et al., Eur. Phys. J. C76 (2016) no.1., 38.



Rainer Schicker (Heidelberg) Resonance production in Proton-Proton collisions June 29, 2017 13 / 24

#### Cross section at hadron level

- differential cross section  $d\sigma = \frac{|\mathcal{M}|^2}{flux} dQ$  $\mathcal{M} = inv.$  amplitude,
  - dQ = Lorentz-invariant phase space

flux = flux factor

- $\blacksquare |\mathcal{M}|^2 dQ = \mathsf{flux}_{\mathsf{prot}} \ \mathsf{d}\sigma_{\mathsf{prot}} = \mathsf{flux}_{\mathsf{Pom}} \ \mathcal{F}_{\mathsf{prot}}^{\mathsf{Pom}} \ \mathsf{d}\sigma_{\mathsf{Pom}}$
- *F*<sup>Pom</sup><sub>prot</sub> = "Distribution of pomerons in the proton"

• 
$$d\sigma_{prot} = \frac{flux_{Pom}}{flux_{prot}} F_{prot}^{Pom} d\sigma_{Pom}$$

• flux factor for collinear two-body collision of A and B: flux =  $4.*((p_A \cdot p_B)^2 - m_A^2 m_B^2)^{1/2}$ 

#### Pomeron distribution in the proton

- "Distribution of pomerons in the proton" = F<sup>P</sup><sub>p</sub>(t, ξ)
   A.Donnachie, P.V.Landshoff, Nucl. Phys. B303 (1988) 634.
  - ▶ t = 4-momentum transfer to the proton (Mandelstam t)
  - $\xi = \text{fractional long.}$  momentum loss of proton = 1.-x<sub>F</sub>
- Pomeron couples to quarks rather like a C = +1 isoscalar photon
- $F_{\rho}^{P}(t,\xi) = \frac{9\beta_{0}^{2}}{4\pi^{2}} [F_{1}(t)]^{2}\xi^{1-2\alpha(t)}$ , integrated over azimuth
- $F_1(t)$  elastic form factor
- Pomeron traj.  $\alpha(t) = 1. + \varepsilon + \alpha' t$ ,  $\varepsilon \sim 0.085$ ,  $\alpha' = 0.25 \text{ GeV}^{-2}$

#### Resonance cross section at hadron level

$$\sigma_{pp} = \iiint \frac{f l u x_P}{f l u x_P} \cdot F_{p_A}^P(t_A, \xi_A, \phi_A) F_{p_B}^P(t_B, \xi_B, \phi_B) \sigma_{PP}(M_x, t_{A,B}) dt_A d\xi_A d\phi_A dt_B d\xi_B d\phi_B$$
(10)

kinematic transformation ( $\Delta \phi = \phi_A - \phi_B$ ): ( $t_A, \xi_A, t_B, \xi_B, \Delta \phi$ )  $\rightarrow u_+, u_-, v_-, M_x, p_{T,x}$  $M_x$ : mass of central system,  $P_{T,x}$ : trans. mom. of central system

$$\sigma_{pp} = \iiint \int \frac{f | ux_{p}}{f | ux_{p}} \cdot \tilde{F}_{p_{A}}^{P} \tilde{F}_{p_{B}}^{P} \frac{p_{T,x} dp_{T,x}}{\sqrt{F^{2} - (p_{T,x}^{2} - G)^{2}}} \frac{\sigma_{PP}(M_{x}, u_{+}, u_{-}) M_{x} J dM_{x} du_{+} du_{-} dv_{-}}{\sqrt{H^{2} - (\frac{p_{T,x}^{2} + M_{x}^{2}}{2\gamma^{2}})}}$$

$$\frac{d\sigma_{pp}}{dM_{x}dp_{T,x}} = \iiint \frac{flux_{p}}{flux_{p}} \cdot \tilde{F}_{pA}^{P} \tilde{F}_{pB}^{P} \frac{p_{T,x}}{\sqrt{F^{2} - (p_{T,x}^{2} - G)^{2}}} \frac{\sigma_{PP}(M_{x}, u_{+}, u_{-})M_{x}Jdu_{+}du_{-}dv_{-}}{\sqrt{H^{2} - (\frac{p_{T,x}^{2} + M_{x}^{2}}{2\gamma^{2}})}}$$
$$F = F(u_{+}, u_{-}, v_{-}), \quad G = G(u_{+}, u_{-}, v_{-}), \quad H = H(u_{+}, u_{-}, v_{-})$$

Rainer Schicker (Heidelberg) Resonance production in Proton-Proton collisions June 29, 2017 16 / 24

#### Differential hadronic cross sections

- QCD motivated t-dependence of PP cross section  $\propto \frac{1}{\sqrt{t_a \cdot t_B}}$
- convolute PP cross section with DL PP-dist. to get  $\frac{d\sigma}{dM_{\star}dp_{T,\tau}}$
- integration range  $\xi_{A,B} < 10^{-3}, |t_{A,B}| < 1.5 \text{ GeV}^2$ .



Rainer Schicker (Heidelberg) Resonance production in Proton-Proton collisions June 29, 2017 17 / 24

#### Fractional longitudinal momentum loss



Fract. longitudinal momentum loss  $\xi$  in  $\frac{d\sigma(pp \rightarrow ppf_0(980))}{dy}|_{y=0}$ 

#### Conclusions and outlook

- Model presented for Pomeron-Pomeron cross section in resonance region M < 5 GeV.</li>
- Cross section at hadron level derived by convoluting Pomeron-Pomeron cross section with Pomeron distribution and scaling by Pomeron/proton flux.
- Cross section at hadron level calculable for event topologies of single/double diffractive dissociation (work in progress).
- Model can be extended to lower energies where Reggeon exchanges contribute.
- To do: absorptive corrections, multi Pomeron exchanges.

Central production Dual resonance model Regge trajectories PP-cross section Pomeron flux Hadr. cross section Outlook

# Backup

Rainer Schicker (Heidelberg) Resonance production in Proton-Proton collisions June 29, 2017 20 / 24

#### Nonlinear, complex meson trajectories

real and imag. part of traj. are related by dispersion relation

$$\Re e \,\alpha(s) = \alpha(0) + \frac{s}{\pi} PV \int_0^\infty ds' \frac{\Im m \,\alpha(s')}{s'(s'-s)}. \tag{11}$$

imaginary part chosen as sum of single threshold terms

$$\Im m \alpha(s) = \sum_{n} c_n (s - s_n)^{1/2} \left(\frac{s - s_n}{s}\right)^{|\Re e \ \alpha(s_n)|} \theta(s - s_n).$$
(12)

real part of trajectory given by

$$\Re e \,\alpha(s) = \alpha(0) + \frac{s}{\sqrt{\pi}} \sum_{n} c_n \frac{\Gamma(\lambda_n + 3/2)}{\Gamma(\lambda_n + 2)\sqrt{s_n}} \,_2F_1(1, 1/2; \lambda_n + 2\frac{s}{s_n})\theta(s_n - s)$$

$$+\frac{2}{\sqrt{\pi}}\sum_{n}c_{n}\frac{\Gamma(\lambda_{n}+3/2)}{\Gamma(\lambda_{n}+1)}\sqrt{s_{n}} {}_{2}F_{1}(-\lambda_{n},1;3/2;\frac{s_{n}}{s})\theta(s-s_{n}).$$
(13)

#### Lorentz-invariant phase space

- 2  $\rightarrow$  3 body reaction:  $A + B \rightarrow 1 + 2 + X$
- Lorentz-invariant three-particle phase space:

$$\frac{d^{3}\vec{P_{1}}}{(2\pi)^{3}2E_{1}}\frac{d^{3}\vec{P_{2}}}{(2\pi)^{3}2E_{2}}d^{4}P_{x}(2\pi)^{4}\delta^{4}(P_{A}+P_{B}-P_{1}-P_{2}-P_{X})$$

$$= J \cdot dt_A d\xi_A d\phi_A dt_B d\xi_B d\phi_B \tag{14}$$

with  $\mathsf{J}=\mathsf{Jacobian}$  determinant of the transformation

$$(\vec{P_{1}},\vec{P_{2}},P_{X})(2\pi)^{4}\delta^{4}(P_{A}+P_{B}-P_{1}-P_{2}-P_{X}) \rightarrow (t_{A},\xi_{A},\phi_{A},t_{B},\xi_{B},\phi_{B})$$

#### The Pomeron trajectory I

$$\alpha_P(M^2) = 1. + \varepsilon + \alpha' M^2 - c \sqrt{s_0 - M^2}, \qquad (15)$$

Linear term in Eq. 14 is replaced by heavy threshold mimicking linear behaviour in mass region M < 5 GeV.

$$\alpha_{P}(M^{2}) = \alpha_{0} + \alpha_{1} \left( 2m_{\pi} - \sqrt{4m_{\pi}^{2} - M^{2}} \right) + \alpha_{2} \left( \sqrt{M_{H}^{2}} - \sqrt{M_{H}^{2} - M^{2}} \right) (16)$$

with  $M_H$  an effective threshold set at  $M_H = 3.5$  GeV



Rainer Schicker (Heidelberg) Resonance production in Proton-Proton collisions June 29, 2017 23 / 24

#### The Pomeron trajectory II

Pomeron trajectory parameterised as

$$\alpha_P(M^2) = \frac{1 + \varepsilon + \alpha' M^2}{1 - c\sqrt{s_0 - M^2}}$$
(17)

with resulting cross section

