Automated BSM at NLO

Celine Degrande CERN, 21 October 2016



Plan

- Framework : From FeynRules to Madgraph5_aMC@NLO
- Examples :
 - Charged Higgs production
 - Spin 2
 - Top FCNC
- Final remarks



FeynRules



FeynRules outputs



FeynRules outputs can be used directly by event generators

UFO : output with the full information used by several generators



FeynRules outputs



FeynRules outputs can be used directly by event generators

UFO : output with the full information used by several generators



UFO

- Generator independent output with full model information
- Contains the list of particles, parameters, vertices, decays (Ito 2), coupling orders
- vertices are split into Lorentz structures, colours and couplings and all are included in the model!

 $-ig_s T^a_{ij} \gamma_\mu$

• Used in MG5, Herwig, Gosam, Sherpa



Madgraph5_aMC@NLO

Automated NLO computation



shower 'à la' MC@NLO



MadLoop

$$\mathcal{A}^{1-loop} = \sum_{i} \frac{d_{i}}{d_{i}} \operatorname{Box}_{i} + \sum_{i} \frac{c_{i}}{r_{i}} \operatorname{Triangle}_{i} + \sum_{i} \frac{b_{i}}{b_{i}} \operatorname{Bubble}_{i} + \sum_{i} \frac{a_{i}}{r_{i}} \operatorname{Tadpole}_{i} + \frac{R}{r_{i}}$$

- Box, Triangle, Bubble and Tadpole are known scalar integrals
- Loop computation = find the coefficients
 - Tensor reduction (OPP)
- R : rational terms should be partially provided
- UV counterterm vertices have to be provided

To be provided : R₂

$$ar{A}(ar{q}) = rac{1}{\left(2\pi
ight)^4} \int d^d ar{q} rac{ar{N}(ar{q})}{ar{D}_0 ar{D}_1 \dots ar{D}_{m-1}}, \qquad ar{D}_i = (ar{q} + p_i)^2 - m_i^2$$



$$R_{2} \equiv \lim_{\epsilon \to 0} \frac{1}{\left(2\pi\right)^{4}} \int d^{d}\overline{q} \frac{\tilde{N}\left(\tilde{q}, q, \epsilon\right)}{\overline{D}_{0}\overline{D}_{1}\dots\overline{D}_{m-1}}$$

Finite set of vertices that can be computed once for all

R₂ example



$$\bar{Q}_{1} = \bar{q} + p_{1} = Q_{1} + \tilde{q}$$
$$\bar{Q}_{2} = \bar{q} + p_{2} = Q_{2} + \tilde{q}$$
$$\bar{D}_{0} = \bar{q}^{2}$$
$$\bar{D}_{1} = (\bar{q} + p_{1})^{2}$$
$$\bar{D}_{2} = (\bar{q} + p_{2})^{2}$$
't

't Hooft Veltman scheme $\overline{\eta}^{\overline{\mu}\,\overline{\nu}}\overline{\eta}_{\overline{\mu}\,\overline{\nu}} = d,$ $\overline{\gamma}^{\overline{\mu}}\overline{\gamma}_{\overline{\mu}} = d\mathbb{1},$

 $\bar{N}(\bar{q}) \equiv e^{3} \left\{ \bar{\gamma}_{\bar{\beta}} \left(\bar{Q}_{1} + m_{e} \right) \gamma_{\mu} \left(\bar{Q}_{2} + m_{e} \right) \bar{\gamma}^{\bar{\beta}} \right\}$ $= e^{3} \left\{ \gamma_{\beta} (Q_{1} + m_{e}) \gamma_{\mu} (Q_{2} + m_{e}) \gamma^{\beta} - \epsilon \left(Q_{1} - m_{e} \right) \gamma_{\mu} (Q_{2} - m_{e}) + \epsilon \tilde{q}^{2} \gamma_{\mu} - \tilde{q}^{2} \gamma_{\beta} \gamma_{\mu} \gamma^{\beta} \right\}$

Computed in MadLoop :R₁

Due to the \mathcal{E} dimensional parts of the denominators

Like for the 4 dimensional part but with a different set of integrals ~୨ · ୨ ୮

$$\int d^n \bar{q} \frac{\tilde{q}^2}{\bar{D}_i \bar{D}_j} = -\frac{i\pi^2}{2} \left[m_i^2 + m_j^2 - \frac{(p_i - p_j)^2}{3} \right] + \mathcal{O}(\epsilon) ,$$

$$\int d^n \bar{q} \frac{\tilde{q}^2}{\bar{D}_i \bar{D}_j \bar{D}_k} = -\frac{i\pi^2}{2} + \mathcal{O}(\epsilon) ,$$

$$\int d^n \bar{q} \frac{\tilde{q}^4}{\bar{D}_i \bar{D}_j \bar{D}_k \bar{D}_l} = -\frac{i\pi^2}{6} + \mathcal{O}(\epsilon) .$$

Only R = R_1 + R_2 is gauge invariant Check



UV

 $\bar{A}(\bar{q}) = \frac{1}{(2\pi)^4} \int d^d \bar{q} \frac{N(\bar{q})}{\bar{D}_0 \bar{D}_1 \dots \bar{D}_{m-1}} = K \frac{1}{\epsilon} + \mathcal{O}\left(\epsilon^0\right)$



Finite set of vertices that can be computed once for all

Renormalization



Internal parameters are renormalised by replacing the external parameters in their expressions

Renormalization conditions

On-shell scheme (or complex mass scheme):

Renormalized mass = Physical mass

Two-point function vanishes on-shell (No external bubbles)



$$i\delta_{ij} (\not p - m_i) + i \left[f_{ij}^L (p^2) \not p \gamma_- + f_{ij}^R (p^2) \not p \gamma_+ + f_{ij}^{SL} (p^2) \gamma_- + f_{ij}^{SR} (p^2) \gamma_+ \right]$$

$$\begin{split} \tilde{\Re} \left[f_{ij}^{L} \left(p^{2} \right) m_{i} + f_{ij}^{SR} \left(p^{2} \right) \right] \Big|_{p^{2} = m_{i}^{2}} &= 0 \\ \tilde{\Re} \left[f_{ij}^{R} \left(p^{2} \right) m_{i} + f_{ij}^{SL} \left(p^{2} \right) \right] \Big|_{p^{2} = m_{i}^{2}} &= 0 \\ \tilde{\Re} \left[2m_{i} \frac{\partial}{\partial p^{2}} \left[\left(f_{ii}^{L} \left(p^{2} \right) + f_{ii}^{R} \left(p^{2} \right) \right) m_{i} + f_{ii}^{SL} \left(p^{2} \right) + f_{ii}^{SR} \left(p^{2} \right) \right] + f_{ii}^{L} \left(p^{2} \right) + f_{ii}^{R} \left(p^{2} \right) \right] \Big|_{p^{2} = m_{i}^{2}} &= 0 \\ \\ \tilde{\Re} \left[Similar \text{ for the vectors and scalars} \right] \\ \end{split}$$

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$$\tilde{\mathfrak{K}}\left[f_{ij}^{L}\left(p^{2}\right)m_{i}+f_{ij}^{SR}\left(p^{2}\right)\right]\Big|_{p^{2}=m_{i}^{2}}=0$$
$$\tilde{\mathfrak{K}}\left[f_{ij}^{R}\left(p^{2}\right)m_{i}+f_{ij}^{SL}\left(p^{2}\right)\right]\Big|_{p^{2}=m^{2}}=0$$

 $\tilde{\mathcal{X}}\left[2m_{i}\frac{\partial}{\partial p^{2}}\left[\left(f_{ii}^{L}\left(p^{2}\right)+f_{ii}^{R}\left(p^{2}\right)\right)m_{i}+f_{ii}^{SL}\left(p^{2}\right)+f_{ii}^{SR}\left(p^{2}\right)\right]+f_{ii}^{L}\left(p^{2}\right)+f_{ii}^{R}\left(p^{2}\right)\right]\right|_{p^{2}=m_{i}^{2}}=0$

Similar for the vectors and scalars

Renormalization conditions
Jero momentum scheme available for the gauge couplings

$$\Gamma_{FFV}^{\mu}(p_{1},p_{2}) = igT^{a}\delta_{f_{1},f_{2}} \left[\gamma^{\mu} \left(\frac{\delta g}{g} + \frac{1}{2} \delta Z_{VV} + \frac{1}{2} \delta Z_{FF}^{R} + \frac{1}{2} \delta Z_{FF}^{L} + \frac{g'_{V}}{2g} \delta Z_{V'V} \right) + \gamma^{\mu}\gamma_{5} \left(\frac{1}{2} \delta Z_{FF}^{R} - \frac{1}{2} \delta Z_{FF}^{L} + \frac{g'_{A}}{2g} \delta Z_{V'V} \right) + \left(\gamma^{\mu}h^{V}(k^{2}) + \gamma^{\mu}\gamma_{5}h^{A}(k^{2}) + \frac{(p_{1} - p_{2})^{\mu}}{2m}h^{S}(k^{2}) + \frac{k_{\mu}}{2m}h^{P}(k^{2}) \right) \right]$$

$$\frac{\delta g}{g} + \frac{1}{2} \delta Z_{VV} + \frac{1}{2} \delta Z_{FF}^{R} + \frac{1}{2} \delta Z_{FF}^{L} + \frac{g'_{A}}{2g} \delta Z_{V'V} + h^{V}(0) + h^{S}(0) = 0$$

$$\frac{1}{2} \delta Z_{FF}^{R} - \frac{1}{2} \delta Z_{FF}^{L} + \frac{g'_{A}}{2g} \delta Z_{V'V} + h^{A}(0) = 0.$$
By gauge invariance
$$\frac{\delta g}{g} + \frac{1}{2} \delta Z_{VV} + \frac{g'_{V}}{2g} \delta Z_{V'V} + \frac{g'_{A}}{2g} \delta Z_{V'V} = 0$$

$$\text{Only from two-point functions}$$

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$$MS \text{ scheme for everything else (option for all)}$$

6'



- Goal : Automate the one-loop computation for BSM models
- Required ingredients :



• Solution : UFO at NLO









FeynRules :

...

Lren = OnShellRenormalization[LSM , QCDOnly ->True]; WriteFeynArtsOutput[Lren , Output -> "SMrenoL", GenericFile -> False]

FeynArts / NLOCT :

WriteCT["SMrenoL/SMrenoL", "Lorentz", Output-> "SMQCDreno", QCDonly -> True]



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FeynRules :

```
...
Get["SMQCDreno.nlo"];
WriteUFO[ LSM , UVCounterterms -> UV$vertlist ,
R2Vertices -> R2$vertlist]
```

Degray

de

FeynRules :

...

Lren = OnShellRenormalization[LSM , QCDOnly ->True]; WriteFeynArtsOutput[Lren , Output -> "SMrenoL", GenericFile -> False]

FeynArts / NLOCT :

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FeynRules : ... Get["SMQCDreno.nlo"]; WriteUFO[LSM , UVCounterterms -> UV\$vertlist , R2Vertices -> R2\$vertlist]

Restrictions/Assumptions

- Renormalizable Lagrangian, maximum dimension of the operators is 4
- Feynman Gauge
- $\{\gamma_{\mu}, \gamma_5\} = 0$
- 't Hooft-Veltman scheme
- On-shell scheme for the masses and wave functions
- MS by default for everything else (zero-momentum possible for fermion gauge boson interaction)

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- On-shell scheme for the masses and wave functions
- MS by default for everything else (zero-momentum possible for fermion gauge boson interaction)
 MZ scheme for EW coupling egrande

EFT at NLO (QCD)

B. Grzadkowski et al, JHEP 1010 (2010) 085

	X^3		φ^6 and $\varphi^4 D^2$	$\psi^2 arphi^3$				
Q_G	$f^{ABC}G^{A\nu}_{\mu}G^{B\rho}_{\nu}G^{C\mu}_{\rho}$	Q_{φ}	$(arphi^\dagger arphi)^3$	$Q_{e\varphi}$	$(\varphi^{\dagger}\varphi)(\bar{l}_{p}e_{r}\varphi)$			
$Q_{\widetilde{G}}$	$f^{ABC} \widetilde{G}^{A\nu}_{\mu} G^{B\rho}_{\nu} G^{C\mu}_{\rho}$	$Q_{\varphi\Box}$	$(\varphi^{\dagger}\varphi)\Box(\varphi^{\dagger}\varphi)$	$Q_{u\varphi}$	$(\varphi^{\dagger}\varphi)(\bar{q}_{p}u_{r}\widetilde{\varphi})$			
Q_W	$\varepsilon^{IJK} W^{I\nu}_{\mu} W^{J\rho}_{\nu} W^{K\mu}_{\rho}$	$Q_{\varphi D}$	$\left(\varphi^{\dagger}D^{\mu}\varphi\right)^{\star}\left(\varphi^{\dagger}D_{\mu}\varphi\right)$	$Q_{d\varphi}$	$(\varphi^{\dagger}\varphi)(\bar{q}_{p}d_{r}\varphi)$			
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$X^2 \varphi^2$			$\psi^2 X \varphi$		$\psi^2 \varphi^2 D$			
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$Q_{arphi \widetilde{G}}$	$\varphi^{\dagger}\varphi\widetilde{G}^{A}_{\mu\nu}G^{A\mu\nu}$	Q_{eB}	$(\bar{l}_p \sigma^{\mu\nu} e_r) \varphi B_{\mu\nu}$	$Q_{\varphi l}^{(3)}$	$(\varphi^{\dagger}i\overleftrightarrow{D}_{\mu}^{I}\varphi)(\bar{l}_{p}\tau^{I}\gamma^{\mu}l_{r})$			
$Q_{\varphi W}$	$\varphi^{\dagger}\varphiW^{I}_{\mu\nu}W^{I\mu\nu}$	Q_{uG}	$(\bar{q}_p \sigma^{\mu\nu} T^A u_r) \widetilde{\varphi} G^A_{\mu\nu}$	$Q_{\varphi e}$	$(\varphi^{\dagger}i \overset{\leftrightarrow}{D}_{\mu} \varphi)(\bar{e}_{p} \gamma^{\mu} e_{r})$			
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$Q_{\varphi B}$	$\varphi^{\dagger}\varphiB_{\mu\nu}B^{\mu\nu}$	Q_{uB}	$(\bar{q}_p \sigma^{\mu\nu} u_r) \widetilde{\varphi} B_{\mu\nu}$	$Q^{(3)}_{\varphi q}$	$\left(\varphi^{\dagger}i\overleftrightarrow{D}_{\mu}^{I}\varphi)(\bar{q}_{p}\tau^{I}\gamma^{\mu}q_{r})\right)$			
$Q_{\varphi \widetilde{B}}$	$\varphi^{\dagger}\varphi\widetilde{B}_{\mu\nu}B^{\mu\nu}$	Q_{dG}	$(\bar{q}_p \sigma^{\mu\nu} T^A d_r) \varphi G^A_{\mu\nu}$	$Q_{\varphi u}$	$(\varphi^{\dagger}i\overleftrightarrow{D}_{\mu}\varphi)(\bar{u}_{p}\gamma^{\mu}u_{r})$			
$Q_{\varphi WB}$	$\varphi^{\dagger}\tau^{I}\varphiW^{I}_{\mu\nu}B^{\mu\nu}$	Q_{dW}	$(\bar{q}_p \sigma^{\mu\nu} d_r) \tau^I \varphi W^I_{\mu\nu}$	$Q_{\varphi d}$	$(\varphi^{\dagger}i\overleftrightarrow{D}_{\mu}\varphi)(\bar{d}_{p}\gamma^{\mu}d_{r})$			
$Q_{\varphi \widetilde{W}B}$	$\varphi^{\dagger}\tau^{I}\varphi\widetilde{W}^{I}_{\mu\nu}B^{\mu\nu}$	Q_{dB}	$(\bar{q}_p \sigma^{\mu\nu} d_r) \varphi B_{\mu\nu}$	$Q_{\varphi ud}$	$i(\widetilde{\varphi}^{\dagger}D_{\mu}\varphi)(\bar{u}_{p}\gamma^{\mu}d_{r})$			
	C. Degrande							

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X^3			φ^6 and $\varphi^4 D^2$		$\psi^2 arphi^3$		
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$Q_{\varphi W}$	$\varphi^{\dagger}\varphi W^{I}_{\mu u}W^{I\mu u}$	Q_{uG}	$(\bar{q}_p \sigma^{\mu\nu} T^A u_r) \widetilde{\varphi} G^A_{\mu\nu}$	$Q_{\varphi e}$	$(\varphi^{\dagger} i \tilde{D}_{\mu} \varphi) (\bar{e}_{p} \gamma^{\mu} e_{r})$		
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$Q_{\varphi \widetilde{B}}$	$arphi^\daggerarphi \widetilde{B}_{\mu u}B^{\mu u}$	Q_{dG}	$(\bar{q}_p \sigma^{\mu\nu} T^A d_r) \varphi G^A_{\mu\nu}$	$Q_{arphi u}$	$(\varphi^{\dagger}i\overleftrightarrow{D}_{\mu}\varphi)(\bar{u}_{p}\gamma^{\mu}u_{r})$	
$Q_{\varphi WB}$	$\varphi^{\dagger} F^{I} \varphi W^{I}_{\mu\nu} B^{\mu\nu}$	Q_{dW}	$(\bar{q}_p \sigma^{\mu\nu} d_r) \tau^I \varphi W^I_{\mu\nu}$	$Q_{arphi d}$	$(\varphi^{\dagger}i\overleftrightarrow{D}_{\mu}\varphi)(\bar{d}_{p}\gamma^{\mu}d_{r})$	
$Q_{\varphi \widetilde{W}B}$	$\varphi^{\dagger}\tau^{I}\varphi\widetilde{W}^{I}_{\mu\nu}B^{\mu\nu}$	Q_{dB}	$(\bar{q}_p \sigma^{\mu\nu} d_r) \varphi B_{\mu\nu}$	$Q_{\varphi ud}$	$i(\widetilde{\varphi}^{\dagger}D_{\mu}\varphi)(\bar{u}_{p}\gamma^{\mu}d_{r})$	
	<i>j</i>				C. Degra	ande



In the loop: same as SM



 $f^{ABC}G^{A\nu}_{\mu}G^{B\rho}_{\nu}G^{C\mu}_{\rho}$ $\varphi^{\dagger}\varphi G^{A}_{\mu\nu}G^{A\mu\nu}$

More momenta: higher rank of the integral numerator (NLOCT/MadLoop√)

Additional gamma algebra (NLOCT√)

 $(\bar{q}_p \sigma^{\mu\nu} T^A u_r) \widetilde{\varphi} G^A_{\mu\nu}$

$(\bar{L}L)(\bar{L}L)$		$(\bar{R}R)(\bar{R}R)$		$(\bar{L}L)(\bar{R}R)$		
Q_{ll}	$(\bar{l}_p \gamma_\mu l_r) (\bar{l}_s \gamma^\mu l_t)$	Q_{ee}	$(\bar{e}_p \gamma_\mu e_r) (\bar{e}_s \gamma^\mu e_t)$	Q_{le}	$(\bar{l}_p \gamma_\mu l_r) (\bar{e}_s \gamma^\mu e_t)$	
$Q_{qq}^{(1)}$	$(\bar{q}_p \gamma_\mu q_r) (\bar{q}_s \gamma^\mu q_t)$	Q_{uu}	$(\bar{u}_p \gamma_\mu u_r)(\bar{u}_s \gamma^\mu u_t)$	Q_{lu}	$(\bar{l}_p \gamma_\mu l_r)(\bar{u}_s \gamma^\mu u_t)$	
$Q_{qq}^{(3)}$	$(\bar{q}_p \gamma_\mu \tau^I q_r) (\bar{q}_s \gamma^\mu \tau^I q_t)$	Q_{dd}	$(\bar{d}_p \gamma_\mu d_r) (\bar{d}_s \gamma^\mu d_t)$	Q_{ld}	$(\bar{l}_p \gamma_\mu l_r) (\bar{d}_s \gamma^\mu d_t)$	
$Q_{lq}^{(1)}$	$(\bar{l}_p \gamma_\mu l_r)(\bar{q}_s \gamma^\mu q_t)$	Q_{eu}	$(\bar{e}_p \gamma_\mu e_r)(\bar{u}_s \gamma^\mu u_t)$	Q_{qe}	$(\bar{q}_p \gamma_\mu q_r) (\bar{e}_s \gamma^\mu e_t)$	
$Q_{lq}^{(3)}$	$(\bar{l}_p \gamma_\mu \tau^I l_r) (\bar{q}_s \gamma^\mu \tau^I q_t)$	Q_{ed}	$(\bar{e}_p \gamma_\mu e_r) (\bar{d}_s \gamma^\mu d_t)$	$Q_{qu}^{(1)}$	$(\bar{q}_p \gamma_\mu q_r)(\bar{u}_s \gamma^\mu u_t)$	
		$Q_{ud}^{(1)}$	$(\bar{u}_p \gamma_\mu u_r) (\bar{d}_s \gamma^\mu d_t)$	$Q_{qu}^{(8)}$	$(\bar{q}_p \gamma_\mu T^A q_r) (\bar{u}_s \gamma^\mu T^A u_t)$	
		$Q_{ud}^{(8)}$	$(\bar{u}_p \gamma_\mu T^A u_r) (\bar{d}_s \gamma^\mu T^A d_t)$	$Q_{qd}^{(1)}$	$(\bar{q}_p \gamma_\mu q_r) (\bar{d}_s \gamma^\mu d_t)$	
				$Q_{qd}^{(8)}$	$(\bar{q}_p \gamma_\mu T^A q_r) (\bar{d}_s \gamma^\mu T^A d_t)$	
$(\bar{L}R)(\bar{R}L)$ and $(\bar{L}R)(\bar{L}R)$			<i>B</i> -violating			
Q_{ledq}	$(\bar{l}_p^j e_r)(\bar{d}_s q_t^j)$	Q_{duq}	$\varepsilon^{\alpha\beta\gamma}\varepsilon_{jk}\left[(d_p^{\alpha})^T C u_r^{\beta}\right]\left[(q_s^{\gamma j})^T C l_t^k\right]$			
$Q_{quqd}^{(1)}$	$(\bar{q}_p^j u_r) \varepsilon_{jk} (\bar{q}_s^k d_t)$	Q_{qqu}	$\varepsilon^{\alpha\beta\gamma}\varepsilon_{jk}\left[(q_p^{\alpha j})^T C q_r^{\beta k}\right]\left[(u_s^{\gamma})^T C e_t\right]$			
$Q_{quqd}^{(8)}$	$(\bar{q}_p^j T^A u_r) \varepsilon_{jk} (\bar{q}_s^k T^A d_t)$	$Q_{qqq}^{(1)}$	$\varepsilon^{\alpha\beta\gamma}\varepsilon_{jk}\varepsilon_{mn}\left[(q_p^{\alpha j})^T C q_r^{\beta k}\right]\left[(q_s^{\gamma m})^T C l_t^n\right]$			
$Q_{lequ}^{(1)}$	$(\bar{l}_p^j e_r) \varepsilon_{jk} (\bar{q}_s^k u_t)$	$Q_{qqq}^{(3)}$	$\varepsilon^{\alpha\beta\gamma}(\tau^{I}\varepsilon)_{jk}(\tau^{I}\varepsilon)_{mn}\left[(q_{p}^{\alpha j})^{T}Cq_{r}^{\beta k}\right]\left[(q_{s}^{\gamma m})^{T}Cl_{t}^{n}\right]$			
$Q_{lequ}^{(3)} (\bar{l}_p^j \sigma_{\mu\nu} e_r) \varepsilon_{jk} (\bar{q}_s^k \sigma^{\mu\nu} u_t) $		Q_{duu}	$\varepsilon^{\alpha\beta\gamma}\left[(d_p^{\alpha})^T C u_r^{\beta}\right]\left[(u_s^{\gamma})^T C e_t\right]$			

$(\bar{L}L)(\bar{L}L)$		$(\bar{R}R)(\bar{R}R)$		$(\bar{L}L)(\bar{R}R)$		
Q_{ll}	$-\frac{(\overline{l}_{p}\gamma_{\mu}l_{r})(\overline{l}_{s}\gamma^{\mu}l_{t})}{(\overline{l}_{s}\gamma^{\mu}l_{t})}$	Q_{ee}	$(\bar{c}_p\gamma_\mu c_r)(\bar{c}_s\gamma^\mu c_t)$	Q_{le}	$-\frac{(\bar{l}_p\gamma_\mu l_r)(\bar{e}_s\gamma^\mu e_t)}{(\bar{e}_s\gamma^\mu e_t)}$	
$Q_{qq}^{(1)}$	$(\bar{q}_p \gamma_\mu q_r) (\bar{q}_s \gamma^\mu q_t)$	Q_{uu}	$(\bar{u}_p \gamma_\mu u_r)(\bar{u}_s \gamma^\mu u_t)$	Q_{lu}	$(\bar{l}_p \gamma_\mu l_r)(\bar{u}_s \gamma^\mu u_t)$	
$Q_{qq}^{(3)}$	$(\bar{q}_p \gamma_\mu \tau^I q_r) (\bar{q}_s \gamma^\mu \tau^I q_t)$	Q_{dd}	$(\bar{d}_p \gamma_\mu d_r) (\bar{d}_s \gamma^\mu d_t)$	Q_{ld}	$(\bar{l}_p \gamma_\mu l_r) (\bar{d}_s \gamma^\mu d_t)$	
$Q_{lq}^{(1)}$	$(\bar{l}_p \gamma_\mu l_r)(\bar{q}_s \gamma^\mu q_t)$	Q_{eu}	$(\bar{e}_p \gamma_\mu e_r)(\bar{u}_s \gamma^\mu u_t)$	Q_{qe}	$(\bar{q}_p \gamma_\mu q_r) (\bar{e}_s \gamma^\mu e_t)$	
$Q_{lq}^{(3)}$	$(\bar{l}_p \gamma_\mu \tau^I l_r) (\bar{q}_s \gamma^\mu \tau^I q_t)$	Q_{ed}	$(\bar{e}_p \gamma_\mu e_r) (\bar{d}_s \gamma^\mu d_t)$	$Q_{qu}^{(1)}$	$(\bar{q}_p \gamma_\mu q_r) (\bar{u}_s \gamma^\mu u_t)$	
		$Q_{ud}^{(1)}$	$(\bar{u}_p \gamma_\mu u_r) (\bar{d}_s \gamma^\mu d_t)$	$Q_{qu}^{(8)}$	$(\bar{q}_p \gamma_\mu T^A q_r) (\bar{u}_s \gamma^\mu T^A u_t)$	
		$Q_{ud}^{(8)}$	$(\bar{u}_p \gamma_\mu T^A u_r) (\bar{d}_s \gamma^\mu T^A d_t)$	$Q_{qd}^{(1)}$	$(\bar{q}_p \gamma_\mu q_r) (\bar{d}_s \gamma^\mu d_t)$	
				$Q_{qd}^{(8)}$	$(\bar{q}_p \gamma_\mu T^A q_r) (\bar{d}_s \gamma^\mu T^A d_t)$	
$(\bar{L}R)(\bar{R}L)$ and $(\bar{L}R)(\bar{L}R)$			<i>B</i> -violating			
Q_{ledq}	$(\bar{l}_p^j e_r)(\bar{d}_s q_t^j)$	Q_{duq}	$\varepsilon^{\alpha\beta\gamma}\varepsilon_{jk}\left[(d_p^{\alpha})^T C u_r^{\beta}\right]\left[(q_s^{\gamma j})^T C l_t^k\right]$			
$Q_{quqd}^{(1)}$	$(\bar{q}_p^j u_r) \varepsilon_{jk} (\bar{q}_s^k d_t)$	Q_{qqu}	$\varepsilon^{\alpha\beta\gamma}\varepsilon_{jk}\left[(q_p^{\alpha j})^T C q_r^{\beta k}\right]\left[(u_s^{\gamma})^T C e_t\right]$			
$Q_{quqd}^{(8)}$	$(\bar{q}_p^j T^A u_r) \varepsilon_{jk} (\bar{q}_s^k T^A d_t)$	$Q_{qqq}^{(1)}$	$\varepsilon^{\alpha\beta\gamma}\varepsilon_{jk}\varepsilon_{mn}\left[(q_p^{\alpha j})^T C q_r^{\beta k}\right]\left[(q_s^{\gamma m})^T C l_t^n\right]$			
$Q_{lequ}^{(1)}$	$(\bar{l}_p^j e_r) \varepsilon_{jk} (\bar{q}_s^k u_t)$	$Q_{qqq}^{(3)}$	$\varepsilon^{\alpha\beta\gamma}(\tau^{I}\varepsilon)_{jk}(\tau^{I}\varepsilon)_{mn}\left[(q_{p}^{\alpha j})^{T}Cq_{r}^{\beta k}\right]\left[(q_{s}^{\gamma m})^{T}Cl_{t}^{n}\right]$			
$Q_{lequ}^{(3)}$	$(\bar{l}_p^j \sigma_{\mu\nu} e_r) \varepsilon_{jk} (\bar{q}_s^k \sigma^{\mu\nu} u_t)$	Q_{duu}	$\varepsilon^{\alpha\beta\gamma} \left[(d_p^{\alpha})^T C u_r^{\beta} \right] \left[(u_s^{\gamma})^T C e_t \right]$			

$(\bar{L}L)(\bar{L}L)$		$(\bar{R}R)(\bar{R}R)$		$(\bar{L}L)(\bar{R}R)$		
Q_{ll}	$- (\overline{l}_p \gamma_\mu l_r) (\overline{l}_s \gamma^\mu l_t) - $	Q_{ee}	$-(\bar{c}_p\gamma_\mu c_r)(\bar{c}_s\gamma^\mu c_t)$	Q_{le}	$- (\overline{l}_p \gamma_\mu l_r) (\overline{c}_s \gamma^\mu c_t) -$	
$Q_{qq}^{(1)}$	$(\bar{q}_p \gamma_\mu q_r) (\bar{q}_s \gamma^\mu q_t)$	Q_{uu}	$(\bar{u}_p \gamma_\mu u_r)(\bar{u}_s \gamma^\mu u_t)$	Q_{lu}	$(\bar{l}_p \gamma_\mu l_r) (\bar{u}_s \gamma^\mu u_t)$	
$Q_{qq}^{(3)}$	$(\bar{q}_p \gamma_\mu \tau^I q_r) (\bar{q}_s \gamma^\mu \tau^I q_t)$	Q_{dd}	$(\bar{d}_p \gamma_\mu d_r) (\bar{d}_s \gamma^\mu d_t)$	Q_{ld}	$(\bar{l}_p \gamma_\mu l_r) (\bar{d}_s \gamma^\mu d_t)$	
$Q_{lq}^{(1)}$	$(\bar{l}_p \gamma_\mu l_r)(\bar{q}_s \gamma^\mu q_t)$	Q_{eu}	$(\bar{e}_p \gamma_\mu e_r)(\bar{u}_s \gamma^\mu u_t)$	Q_{qe}	$(\bar{q}_p \gamma_\mu q_r) (\bar{e}_s \gamma^\mu e_t)$	
$Q_{lq}^{(3)}$	$(\bar{l}_p \gamma_\mu \tau^I l_r)(\bar{q}_s \gamma^\mu \tau^I q_t)$	Q_{ed}	$(\bar{e}_p \gamma_\mu e_r) (\bar{d}_s \gamma^\mu d_t)$	$Q_{qu}^{(1)}$	$(\bar{q}_p \gamma_\mu q_r) (\bar{u}_s \gamma^\mu u_t)$	
		$Q_{ud}^{(1)}$	$(\bar{u}_p \gamma_\mu u_r) (\bar{d}_s \gamma^\mu d_t)$	$Q_{qu}^{(8)}$	$(\bar{q}_p \gamma_\mu T^A q_r) (\bar{u}_s \gamma^\mu T^A u_t)$	
Same as SM		$Q_{ud}^{(8)}$	$(\bar{u}_p \gamma_\mu T^A u_r) (\bar{d}_s \gamma^\mu T^A d_t)$	$Q_{qd}^{(1)}$	$(\bar{q}_p \gamma_\mu q_r) (\bar{d}_s \gamma^\mu d_t)$	
				$Q_{qd}^{(8)}$	$(\bar{q}_p \gamma_\mu T^A q_r) (\bar{d}_s \gamma^\mu T^A d_t)$	
$(\bar{L}R)$	$(\bar{R}L)$ and $(\bar{L}R)(\bar{L}R)$		<i>B</i> -violating			
Q_{ledq}	$(\bar{l}_p^j e_r)(\bar{d}_s q_t^j)$	Q_{duq}	$\varepsilon^{\alpha\beta\gamma}\varepsilon_{jk}\left[(d_p^{\alpha})^T C u_r^{\beta}\right]\left[(q_s^{\gamma j})^T C l_t^k\right]$			
$Q_{quqd}^{(1)} \qquad (\bar{q}_p^j u_r) \varepsilon_{jk} (\bar{q}_s^k d_t)$		Q_{qqu}	$\varepsilon^{\alpha\beta\gamma}\varepsilon_{jk}\left[(q_p^{\alpha j})^T C q_r^{\beta k}\right]\left[(u_s^{\gamma})^T C e_t\right]$			
$Q_{quqd}^{(8)} \mid (\bar{q}_p^j T^A u_r) \varepsilon_{jk} (\bar{q}_s^k T^A d_t)$		$Q_{qqq}^{(1)}$	$\varepsilon^{\alpha\beta\gamma}\varepsilon_{jk}\varepsilon_{mn}\left[(q_p^{\alpha j})^T C q_r^{\beta k}\right]\left[(q_s^{\gamma m})^T C l_t^n\right]$			
$Q_{lequ}^{(1)}$	$(\bar{l}_p^j e_r) \varepsilon_{jk} (\bar{q}_s^k u_t)$	$Q_{qqq}^{(3)}$	$\varepsilon^{\alpha\beta\gamma}(\tau^{I}\varepsilon)_{jk}(\tau^{I}\varepsilon)_{mn}\left[(q_{p}^{\alpha j})^{T}Cq_{r}^{\beta k}\right]\left[(q_{s}^{\gamma m})^{T}Cl_{t}^{n}\right]$			
$Q_{lequ}^{(3)}$	$(\bar{l}_p^j \sigma_{\mu\nu} e_r) \varepsilon_{jk} (\bar{q}_s^k \sigma^{\mu\nu} u_t)$	Q_{duu}	$\varepsilon^{\alpha\beta\gamma}\left[(d_p^{\alpha})^T C u_r^{\beta}\right]\left[(u_s^{\gamma})^T C e_t\right]$			

$(\bar{L}L)(\bar{L}L)$		$(\bar{R}R)(\bar{R}R)$		$(\bar{L}L)(\bar{R}R)$		
Q_{ll}	$- (\overline{l}_p \gamma_\mu l_r) (\overline{l}_s \gamma^\mu l_t) - $	Q_{ee}	$-(\bar{c}_p\gamma_\mu c_r)(\bar{c}_s\gamma^\mu c_t) -$	Q_{le}	$- (\overline{l}_p \gamma_\mu l_r) (\overline{c}_s \gamma^\mu c_t) -$	
$Q_{qq}^{(1)}$	$(\bar{q}_p \gamma_\mu q_r) (\bar{q}_s \gamma^\mu q_t)$	Q_{uu}	$(\bar{u}_p \gamma_\mu u_r)(\bar{u}_s \gamma^\mu u_t)$	Q_{lu}	$(\bar{l}_p \gamma_\mu l_r) (\bar{u}_s \gamma^\mu u_t)$	
$Q_{qq}^{(3)}$	$(\bar{q}_p \gamma_\mu \tau^I q_r) (\bar{q}_s \gamma^\mu \tau^I q_t)$	Q_{dd}	$(\bar{d}_p \gamma_\mu d_r) (\bar{d}_s \gamma^\mu d_t)$	Q_{ld}	$(\bar{l}_p \gamma_\mu l_r) (\bar{d}_s \gamma^\mu d_t)$	
$Q_{lq}^{(1)}$	$(\bar{l}_p \gamma_\mu l_r)(\bar{q}_s \gamma^\mu q_t)$	Q_{eu}	$(\bar{e}_p \gamma_\mu e_r)(\bar{u}_s \gamma^\mu u_t)$	Q_{qe}	$(\bar{q}_p \gamma_\mu q_r) (\bar{e}_s \gamma^\mu e_t)$	
$Q_{lq}^{(3)}$	$(\bar{l}_p \gamma_\mu \tau^I l_r)(\bar{q}_s \gamma^\mu \tau^I q_t)$	Q_{ed}	$(\bar{e}_p \gamma_\mu e_r) (\bar{d}_s \gamma^\mu d_t)$	$Q_{qu}^{(1)}$	$(\bar{q}_p \gamma_\mu q_r) (\bar{u}_s \gamma^\mu u_t)$	
		$Q_{ud}^{(1)}$	$(\bar{u}_p \gamma_\mu u_r) (\bar{d}_s \gamma^\mu d_t)$	$Q_{qu}^{(8)}$	$(\bar{q}_p \gamma_\mu T^A q_r) (\bar{u}_s \gamma^\mu T^A u_t)$	
Same as SM		$Q_{ud}^{(8)}$	$(\bar{u}_p \gamma_\mu T^A u_r) (\bar{d}_s \gamma^\mu T^A d_t)$	$Q_{qd}^{(1)}$	$(\bar{q}_p \gamma_\mu q_r) (\bar{d}_s \gamma^\mu d_t)$	
				$Q_{qd}^{(8)}$	$(\bar{q}_p \gamma_\mu T^A q_r) (\bar{d}_s \gamma^\mu T^A d_t)$	
$(\bar{L}R)$	$(\bar{R}L)$ and $(\bar{L}R)(\bar{L}R)$		<i>B</i> -violating			
Q_{ledq}	$(\bar{l}_p^j e_r)(\bar{d}_s q_t^j)$	Q_{duq}	$\varepsilon^{\alpha\beta\gamma}\varepsilon_{jk}\left[(d_p^{\alpha})^T C u_r^{\beta}\right]\left[(q_s^{\gamma j})^T C l_t^k\right]$			
$Q_{quqd}^{(1)} \qquad (\bar{q}_p^j u_r) \varepsilon_{jk} (\bar{q}_s^k d_t)$		Q_{qqu}	$\varepsilon^{\alpha\beta\gamma}\varepsilon_{jk}\left[(q_p^{\alpha j})^T C q_r^{\beta k}\right]\left[(u_s^{\gamma})^T C e_t\right]$			
$\left \begin{array}{c} Q_{quqd}^{(8)} \\ q_{p}^{j}T^{A}u_{r} \\ \varepsilon_{jk} (\bar{q}_{s}^{k}T^{A}d_{t}) \end{array} \right $		$Q_{qqq}^{(1)}$	$\varepsilon^{\alpha\beta\gamma}\varepsilon_{jk}\varepsilon_{mn}\left[(q_p^{\alpha j})^T C q_r^{\beta k}\right]\left[(q_s^{\gamma m})^T C l_t^n\right]$			
$Q_{lequ}^{(1)}$	$(\bar{l}_p^j e_r) \varepsilon_{jk} (\bar{q}_s^k u_t)$	$Q_{qqq}^{(3)}$	$\varepsilon^{\alpha\beta\gamma}(\tau^{I}\varepsilon)_{jk}(\tau^{I}\varepsilon)_{mn}\left[(q_{p}^{\alpha j})^{T}Cq_{r}^{\beta k}\right]\left[(q_{s}^{\gamma m})^{T}Cl_{t}^{n}\right]$			
$Q_{lequ}^{(3)}$	$(\bar{l}_p^j \sigma_{\mu\nu} e_r) \varepsilon_{jk} (\bar{q}_s^k \sigma^{\mu\nu} u_t)$	Q_{duu}	$\varepsilon^{\alpha\beta\gamma}\left[(d_p^{\alpha})^T C u_r^{\beta}\right]\left[(u_s^{\gamma})^T C e_t\right]$			


 $\gamma^{\mu}\gamma^{\nu}\gamma^{\rho}P_{R}\otimes\gamma_{\mu}\gamma_{\nu}\gamma_{\rho}P_{R} = E + (16 - 4a\varepsilon)\gamma^{\mu}P_{R}\otimes\gamma_{\mu}P_{R}$ $\gamma^{\mu}\gamma^{\nu}\gamma^{\rho}P_{R}\otimes\gamma_{\rho}\gamma_{\nu}\gamma_{\mu}P_{R} = -E + [4 - (12 - 4a)\varepsilon]\gamma^{\mu}P_{R}\otimes\gamma_{\mu}P_{R}$

C. Degrande

Extra R2 (gauge invariant) Change the UV matching

EFT at NLO

- UV counterterms :
 - Basis reduction needed for the anomalous matrix (By Liam Moore)
 - Check (R.Alonso, E. E. Jenkins, A.V. Manohar, M.Trott, JHEP 1404 (2014) 159)
 - MSbar : I/ϵ from the amplitudes not from the renomalization
 - Running (UFO 2.0)



R2:Validation

- tested* on the SM (QCD:P. Draggiotis et al. +QED:M.V. Garzelli et al)
- tested* on MSSM (QCD:H.-S. Shao,Y.-J. Zhang) : test the Majorana

*Analytic comparison of the expressions

UV Validation

- SM QCD : tested* (W. Beenakker, S. Dittmaier, M. Kramer, B. Plumper)
- SM EW : tested* (expressions given by H.-S. Shao from A. Denner)

*Analytic comparison of the expressions

Tests in event generators

- aMC@NLO
- The SM QCD has been tested by V. Hirschi (Comparison with the built-in version)
- SM EW (MZ scheme): comparison to published results for ME by H.-S. Shao and V. Hirschi
- Various BSM
 - gauge invariance
 - pole cancelation



=== Finite === Stored ML5 opt ML5 opt ML5 default Process Relative diff. Result -1.2565695610e+01 -1.2565705416e+01 -1.2565696276e+01 3.9018817097e-07 Pass d d~ > w+ w- g === Born === Process ML5 default Stored ML5 opt ML5 opt Relative diff. Result d d~ > w+ w- g |.8518318521e-06 |.8518318521e-06 |.8518318521e-06 8.0617231411e-15 Pass === Single pole === Stored ML5 opt ML5 opt ML5 default Relative diff. Process Result d d~ > w+ w- g -1.9397426502e+01 -1.9397426502e+01 -1.9397426504e+01 5.5894073017e-11 Pass === Double pole === Stored ML5 opt ML5 opt ML5 default Relative diff. Result Process d d~ > w+ w- g === Summary === I/I passed, 0/I failed=== Finite === Stored MadLoop v4 ML5 opt ML5 default Relative diff. Process Result -5.3971186943e+01 -5.3971193753e+01 -5.3971189940e+01 6.3091071914e-08 Pass d~d>agg === Born === Stored MadLoop v4 ML5 opt ML5 default Relative diff. Result Process 6.4168774056e-05 6.4168764370e-05 6.4168764370e-05 7.5467680882e-08 Pass d~d>agg === Single pole === Stored MadLoop v4 ML5 opt ML5 default Process Relative diff. Result -3.7439549398e+01 -3.7439549398e+01 -3.7439549397e+01 6.8122965983e-12 Pass d~d>agg === Double pole === Stored MadLoop v4 ML5 opt Process ML5 default Relative diff. Result d~d>agg === Summary === I/I passed, 0/I failed=== Finite === Stored MadLoop v4 ML5 opt Process ML5 default Relative diff. Result -5.3769573669e+01 -5.3769573347e+01 -5.3769566412e+01 6.7475496780e-08 Pass d~d>zgg

=== Finite === Process Stored ML5 opt ML5 opt ML5 default Relative diff. Result d d~ > w+ w- g -1.2565695610e+01 -1.2565705416e+01 -1.2565696276e+01 3.9018817097e-07 Pass === Born === Stored ML5 opt ML5 opt ML5 default Relative diff. Result Process d d~ > w+ w- g |.8518318521e-06 |.8518318521e-06 |.8518318521e-06 8.0617231411e-15 Pass === Single pole === Process Stored ML5 opt ML5 opt ML5 default Relative diff. Result d d~ > w+ w- g -1.9397426502e+01 -1.9397426502e+01 -1.9397426504e+01 5.5894073017e-11 Pass === Finite === Process Stored ML5 opt ML5 opt ML5 default Relative diff. Result d d~ > w+ w- g -1.2565695610e+01 -1.2565705416e+01 -1.2565696276e+01 3.9018817097e-07 Pass === Born === Process Stored ML5 opt ML5 opt ML5 default Relative diff. Result d d~ > w+ w- g |.85|83|852|e-06 |.85|83|852|e-06 |.85|83|852|e-06 8.06|723|4||e-15 Pass === Single pole === Process Stored ML5 opt ML5 opt ML5 default Relative diff. Result d d~ > w+ w- g -1.9397426502e+01 -1.9397426502e+01 -1.9397426504e+01 5.5894073017e-11 Pass === Double pole === Process Stored ML5 opt ML5 opt ML5 default Relative diff. Result MLJ UEIAUIL rrocess Stored madeoop v+ MES opt Relative uni. Result -5.3769573669e+01 -5.3769573347e+01 -5.3769566412e+01 6.7475496780e-08 Pass d~d>zgg

=== Born === Stored MadLoop v4 ML5 opt ML5 default Relative diff. Process Result d~ d > z g g 3.1531233900e-04 3.1531235770e-04 3.1531235770e-04 2.9654886777e-08 Pass === Single pole === Stored MadLoop v4 ML5 opt ML5 default Process Relative diff. Result -3.7464897007e+01 -3.7464897007e+01 -3.7464897007e+01 4.2333025503e-12 Pass d~d>zgg === Double pole === Stored MadLoop v4 ML5 opt ML5 default Process Relative diff. Result d~d>zgg === Summary === I/I passed, 0/I failed=== Finite === Stored MadLoop v4 ML5 opt ML5 default Process Relative diff. Result -5.9990384275e+00 -5.9990511729e+00 -5.9990379587e+00 1.1013604745e-06 Pass d~d>zzg === Born === Process Stored MadLoop v4 ML5 opt ML5 default Relative diff. Result 2.2616997126e-06 2.2617000449e-06 2.2617000449e-06 7.3450366526e-08 Pass d~d>zzg === Single pole === Stored MadLoop v4 ML5 opt ML5 default Relative diff. Result Process -1.5469587040e+01 -1.5469587040e+01 -1.5469587040e+01 1.52266666708e-11 Pass d∼ d > z z g === Double pole === Stored MadLoop v4 ML5 opt ML5 default Process Relative diff. Result d~d>zzg === Summary === I/I passed, 0/I failed=== Finite === Stored MadLoop v4 ML5 opt ML5 default Relative diff. Process Result 2.9740187004e+01 2.9740187005e+01 2.9740187036e+01 5.3265970697e-10 Pass gg>htt~

=== Born === Stored MadLoop v4 ML5 opt ML5 default Relative diff. Process Result 1.1079653971e-07 1.1079653974e-07 1.1079653974e-07 1.3190849004e-10 Pass g g > h t t~ === Single pole === Stored MadLoop v4 ML5 opt ML5 default Process Relative diff. Result -7.0825709000e+00 -7.0825709000e+00 -7.0825709000e+00 5.0901237085e-13 Pass g g > h t t~ === Double pole === Stored MadLoop v4 ML5 opt ML5 default Process Relative diff. Result -6.00000000e+00 -6.00000000e+00 -6.00000000e+00 1.7023419711e-15 Pass gg > htt~=== Summary === 1/1 passed, 0/1 failed=== Finite === ML5 default Stored MadLoop v4 ML5 opt Process Relative diff. Result 3.6409017466e+01 3.6409021125e+01 3.6409021117e+01 5.0242920154e-08 Pass g g > z t t~ === Born === ML5 default Process Stored MadLoop v4 ML5 opt Relative diff. Result 7.0723041711e-07 7.0723046101e-07 7.0723046101e-07 3.1039274206e-08 Pass g g > z t t~ === Single pole === Stored MadLoop v4 ML5 opt ML5 default Relative diff. Result Process -7.1948086812e+00 -7.1948086773e+00 -7.1948086773e+00 2.7349789963e-10 Pass g g > z t t~ === Double pole === Stored MadLoop v4 ML5 opt ML5 default Relative diff. Result Process -6.00000000e+00 -6.00000000e+00 -6.00000000e+00 2.5165055225e-15 Pass gg>ztt~ === Summary === 1/1 passed, 0/1 failed=== Finite === ML5 default Relative diff. Result Process Stored ML5 opt ML5 opt -1.2565695610e+01 -1.2565705416e+01 -1.2565696276e+01 3.9018817097e-07 Pass d d~ > w+ w- g

=== Born === Process Stored ML5 opt ML5 opt ML5 default Relative diff. Result d d~ > w+ w- g 1.8518318521e-06 1.8518318521e-06 1.8518318521e-06 8.0617231411e-15 Pass

=== Single pole ===

Process Stored ML5 opt ML5 opt ML5 default Relative diff. Result d ~ > w+ w- g -1.9397426502e+01 -1.9397426502e+01 -1.9397426504e+01 5.5894073017e-11 Pass

=== Double pole ===

 Process
 Stored ML5 opt
 ML5 opt
 ML5 default
 Relative diff.
 Result

 d d~ > w+ w- g
 -5.66666666667e+00
 -5.66666666667e+00
 -5.66666666667e+00
 -5.66666666667e+14
 Pass

=== Summary ===

I/I passed, 0/I failed=== Finite ===

 Process
 Stored ML5 opt
 ML5 default
 Relative diff.
 Result

 d~ d > a g g
 -1.1504816412e+01
 -1.1504816557e+01
 -1.1504815497e+01
 4.6089385415e-08
 Pass

=== Born ===

 Process
 Stored ML5 opt
 ML5 opt
 ML5 default
 Relative diff.
 Result

 d~ d > a g g
 2.3138920858e-06
 2.3138920858e-06
 2.3138920858e-06
 4.3012538015e-15
 Pass

=== Single pole === Process Stored ML5 opt ML5 opt ML5 default Relative diff. Result d~ d > a g g -2.8637049838e+01 -2.8637049838e+01 -2.8637049838e+01 1.5718407645e-13 Pass

=== Double pole === Process Stored ML5 opt ML5 opt ML5 default Relative diff. Result d~ d > a g g -8.6666666667e+00 -8.6666666667e+00 -8.66666666667e+00 1.7421961310e-15 Pass

=== Summary === I/I passed, 0/I failed=== Finite === Process Stored ML5 opt ML5 opt ML5 default Relative diff. Result d~ d > z g g -1.0306105482e+01 -1.0306105654e+01 -1.0306102645e+01 1.4600800434e-07 Pass

+7/3

C. Degrande

Massive and massless b

== a a > t t~ ['QED'] == == a a > t t~ a ['QED'] == == a a > w+ w- ['QED'] == == a b > t w- ['QED'] == $== d \sim d > w + w - ['QCD'] ==$ $== d \sim d > w + w - ['QED'] ==$ $== d \sim d > z z ['QCD'] ==$ $== d \sim d > z z ['QED'] ==$ == e+ e- > t t~ a ['QED'] == == e+ e- > t t~ g ['QED'] == == g b > t w- ['QED'] ==== g g > h h ['QCD'] ==== g g > t t~ ['QED'] == == g g > t t~ g ['QED'] == == g g > t t~ h ['QCD'] == == g g > t t~ h ['QED'] == == h h > h h ['QED'] ==== h h > h h h ['QED'] == $== t t \sim > w + w - ['QED'] ==$

== u b > t d ['QED'] == == u d~ > t b~ ['QED'] == == u g > t d b~ ['QED'] == == u u~ > a a ['QED'] == == u u~ > e+ e- ['OED'] == == u u~ > g a ['QCD QED'] == == u u~ > u u~ ['QCD QED'] ==== u u~ > u u~ a ['QCD QED'] == == u u~ > u u~ g ['QCD QED'] == $== u u \sim > w + w - ['QED'] ==$ == u u~ > z a ['QED'] == $== u u^{2} > z z ['QED'] ==$ $== u \sim d > w - z ['0CD'] ==$ $== u \sim d > w - z ['QED'] ==$ $== u \sim u > w + w - ['QCD'] ==$ $== u \sim u > w + w - ['QED'] ==$ $== u \sim u > z z ['QCD'] ==$ $== u \sim u > z z ['QED'] ==$ == ve ve~ > e+ e- ['OED'] == == w + w - > h h ['QED'] ==



Future development

- UFO@NLO in Gosam (N. Greiner)
- DRED (asked by Gosam)
- UFO 2.0



Plan

- Framework : From FeynRules to Madgraph5_aMC@NLO
- Examples :
 - Charged Higgs production
 - Spin 2
 - Top FCNC
- Final remarks



The Higgs discovery







The Higgs discovery



C. D., M.Ubiali, M.Wiesemann and M.Zaro, JHEP 1510 (2015) 145

C. Degrande

- Motivations :
 - needed for the LHC current and future runs
 - First searches in the high mass region
 - Threshold region (With R. Frederix)
- 4F NLO fully differential matched with parton shower



Shape comparison with the 5F

5 Flavours

- m_b=0 (but m_b^y>0)
- In the PDF
- In the running of α_s
- Handle collinear logarithms



4 Flavours

- m_b>0
- Not in the PDF
- Not in the running of α_s
- Contribution to b observable at LO

Type-II 2HDM
$$V_{t\bar{b}H^-} = -i\left(y_t P_R \frac{1}{\tan\beta} + y_b P_L \tan\beta\right) \qquad P_{R/L} = (1 \pm \gamma_5)/2$$
$$y_{t/b} \equiv \sqrt{2} \frac{m_{t/b}^y}{v}$$

$$\delta y_{t/b} = \sqrt{2} \frac{\delta m_{t/b}}{v} \qquad \underbrace{\text{On-shell sc.}}_{v} \quad \delta m_{t/b} = -\frac{g_s^2}{12\pi^2} m_{t/b} \left(\frac{3}{\bar{\epsilon}} + 4 - 6\log\frac{m_{t/b}}{\mu_R}\right)$$
$$\underbrace{\text{MS sc.}}_{\delta y_b} = -\frac{\sqrt{2}}{v} \frac{g_s^2 m_b^y}{4\pi^2 \bar{\epsilon}}$$

Input : -FR model -running of the b yukawa mass

Validation : -Comparison with S. Dittmaier, M. Kramer, M. Spira and M. Walser, PRD 83 (2011) 055005 -Recover ttH









Example I: Charged Higgs production 4F vs 5F







Only LO in 5F



Shower dependent in 5F

H⁺ production : m_H~m_t

1607.05291 : C. D., R. Frederix, V. Hirschi, M.Ubiali, M.Wiesemann and M.Zaro

NLO in QCD Complex Mass Scheme (Top)



scalars (≲7%)

H⁺ production : m_H~m_t



H⁺ production : m_H~m_t



Spin-2

$$\begin{aligned} \mathcal{L}_{V,f}^{Y_2} &= -\frac{\kappa_{V,f}}{\Lambda} T_{\mu\nu}^{V,f} Y_2^{\mu\nu} \\ T_{\mu\nu}^f &= -g_{\mu\nu} \left[\bar{\psi}_f \left(i\gamma^{\rho} D_{\rho} - m_f \right) \psi_f - \frac{1}{2} \partial^{\rho} \left(\bar{\psi}_f i\gamma_{\rho} \psi_f \right) \right] \\ &+ \left[\frac{1}{2} \bar{\psi}_f i\gamma_{\mu} D_{\nu} \psi_f - \frac{1}{4} \partial_{\mu} \left(\bar{\psi}_f i\gamma_{\nu} \psi_f \right) + (\mu \leftrightarrow \nu) \right], \\ T_{\mu\nu}^{\Phi} &= D_{\mu} \Phi^{\dagger} D_{\nu} \Phi + D_{\nu} \Phi^{\dagger} D_{\mu} \Phi - g_{\mu\nu} (D^{\rho} \Phi^{\dagger} D_{\rho} \Phi - V(\Phi)) \end{aligned}$$

$$\begin{aligned} T_{\mu\nu}^{Y_2} &= -g_{\mu\nu} \left[-\frac{1}{4} F^{\rho\sigma} F_{\rho\sigma} + \delta_{m\nu,0} \left((\partial^{\rho} \partial^{\sigma} V_{\sigma}) V_{\rho} + \frac{1}{2} \left(\partial^{\rho} V_{\rho} \right)^2 \right) \right] \\ -F_{\mu\nu}^{\rho} F_{\nu\rho} + \delta_{m\nu,0} \left[\left(\partial_{\mu} \partial^{\rho} V_{\rho} \right) V_{\nu} + \left(\partial_{\nu} \partial^{\rho} V_{\rho} \right) V_{\mu} \right], \\ T_{\mu\nu}^{FP} &= -g_{\mu\nu} \left[(\partial^{\rho} \bar{\omega}^a) \left(\partial_{\rho} \omega^a \right) - g_s f^{abc} \left(\partial^{\rho} \bar{\omega}^a \right) \omega^b V_{\rho}^c \right] \\ + \left[\left(\partial_{\mu} \bar{\omega}^a \right) \left(\partial_{\nu} \omega^a \right) - g_s f^{abc} \left(\partial_{\mu} \bar{\omega}^a \right) \omega^b V_{\nu}^c + (\mu \leftrightarrow \nu) \right] \end{aligned}$$

- Simplified model for new resonance search
- Motivated by Extra Dimension
- Check : Known UV (P.Artoisenet et al, JHEP 1311 (2013) 043)

$$\delta \kappa_{g} = \frac{\alpha_{s}}{3\pi} T_{F} \sum_{q} \left(\kappa_{g} - \kappa_{q} \right) \left(\frac{1}{\epsilon} - \gamma_{E} + \log 4\pi + \log \frac{\mu_{R}^{2}}{m_{Y_{2}}^{2}} \right),$$

$$\delta \kappa_{q} = \frac{2\alpha_{s}}{3\pi} C_{F} \left(\kappa_{q} - \kappa_{g} \right) \left(\frac{1}{\epsilon} - \gamma_{E} + \log 4\pi + \log \frac{\mu_{R}^{2}}{m_{Y_{2}}^{2}} \right),$$
No running

 Production at the LHC (G. Das, CD, V. Hirschi, F. Maltoni, H.-S. Shao, arXiv:1605.09359 [hep-ph])
 C. Degrande



Spin-2



Y2+H is LO (Loop-induced)

Spin-2: Non-universal





Decay the top with the CMS with flavour mixing

Top FCNC




Plan

- Framework : From FeynRules to Madgraph5_aMC@NLO
- Examples :
 - Charged Higgs production
 - Spin 2
 - Top FCNC
- Final remarks



Final remarks

- Automatic BSM@NLO
 - Renormalizable (Public)
 - For EFT (Private)
- Pheno
 - Top EFT
 - Full EFT



 Jointly by FeynRules and Madgraph_aMC@NLO teams

C. Degrande





Example I: Charged Higgs production

- $m_{H^{\pm}} = 200 \,\text{GeV}$ and $[m_{H^{\pm}} = 600 \,\text{GeV}]$
- $\tan \beta = 8$ **but** y_b^2, y_t^2 and $y_b y_t$

NNPDF2.3 at NLO/ NNPDF3.0 at LO with 4/5F

- $\alpha_s(M_Z) = 0.118 \text{ (5F)} \qquad \alpha_s(M_Z) = 0.1226 \text{ (4F)}$
- $m_b^{\text{pole}} = 4.75 \,\text{GeV}$ $m_t^{\text{pole}} = 172.5 \,\text{GeV}$ $\bar{m}_b(\bar{m}_b) = 4.3377 \,\text{GeV}$.

$$\mu_{R,F} = H_T/3 \equiv \frac{1}{3} \sum_i \sqrt{m(i)^2 + p_T(i)^2}$$

Anti-k_T $\Delta R = 0.4$ $p_T(j) \ge 25 \,\text{GeV}, \quad |\eta(j)| \le 2.5.$

C. Degrande