

Update on double Higgs analysis, and extraction of g_{HHH} and g_{WWHH} at CLIC

Boruo Xu^a, Rosa Simoniello^b, Philipp Roloff^b

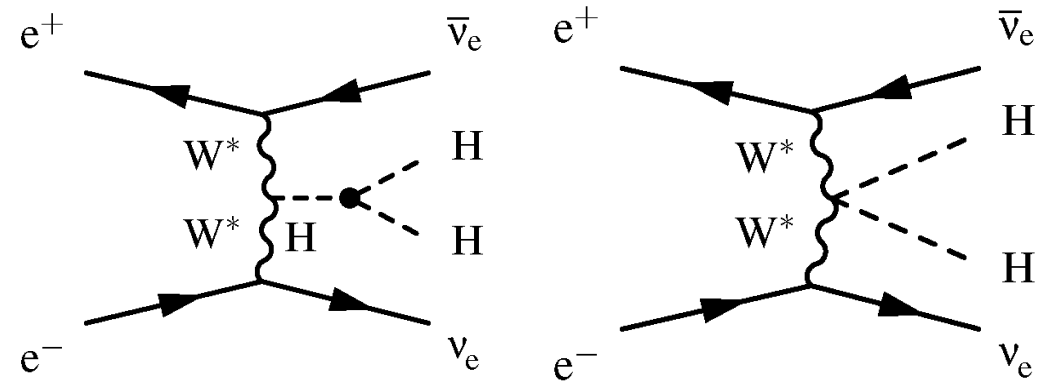
a: University of Cambridge; b: CERN

CLIC workshop 2017



Motivations

- To measure triple higgs self coupling, g_{HHH} , and quartic coupling, g_{HHWW} via double higgs production
- Divide analysis into sub-channels to increase significance
- Sub-channels: (Branching Ratio for $m_H=126\text{GeV}$)
 - $HH\nu\nu \rightarrow bbWW^*\nu\nu \rightarrow bbqqqq\nu\nu$
BR = 0.119 / $bbqq\nu\nu$ BR = 0.114 / $bb\nu\nu$ BR = 0.0274
 - $HH\nu\nu \rightarrow bb\nu\nu$ BR = 0.315
- Independent analysis at $\sqrt{s} = 1.4\text{ TeV}$ and 3 TeV



Strategy

- Veto events with isolated light lepton/tau
 - Light lepton and tau finders in MarlinReco
 - Boruo light lepton and tau finders
 - Simulate forward electron & photon veto for LumiCal and BeamCal
- χ^2 constraint for jet pairing; b-jet tagging
- Pre selection cuts
- MVA i.e.
 - $HH_{\nu\nu} \rightarrow bbWW^*_{\nu\nu} \rightarrow bbqqqq_{\nu\nu}$ / $HH_{\nu\nu} \rightarrow bbbb_{\nu\nu}$ is signal
 - $HH_{\nu\nu} \rightarrow$ other does not participate in MVA training

MC samples

- Many background channels, include $ee \rightarrow qqH\nu$ and $e\gamma \rightarrow qqH\nu$
 - $\gamma\gamma \rightarrow qqH\nu$ checked, negligible cross section
 - * and + represents generator cut $m(qq) > 50$ and 120 GeV
 - BS represents a real photon from beamstrahlung. EPA represents a “quasi-real” photon, simulated with Equivalent Photon Approximation

Channel	$\sigma(\sqrt{s} = 1.4 \text{ TeV}) / \text{fb}$	$\sigma(\sqrt{s} = 3 \text{ TeV}) / \text{fb}$
$e^-e^+ \rightarrow HH\nu\bar{\nu}$	0.149	0.588
$e^-e^+ \rightarrow q_1q_1H\nu\bar{\nu}$	0.86	1.78
$e^-e^+ \rightarrow c\bar{c}H\nu\bar{\nu}$	0.36	1.12
$e^-e^+ \rightarrow b\bar{b}H\nu\bar{\nu}$	0.31	1.91
$e^-e^+ \rightarrow qqqq$	1245.1	546.5*
$e^-e^+ \rightarrow qqqq\ell\ell$	62.1*	169.3*
$e^-e^+ \rightarrow qqqq\ell\nu$	110.4*	106.6*
$e^-e^+ \rightarrow qqqq\nu\bar{\nu}$	23.2*	71.5*
$e^-e^+ \rightarrow qq$	4009.5	2948.9
$e^-e^+ \rightarrow qq\ell\nu$	4309.7	5561.1
$e^-e^+ \rightarrow qq\ell\ell$	2725.8	3319.6
$e^-e^+ \rightarrow qq\nu\nu$	787.7	1317.5
$e^-\gamma(\text{BS}) \rightarrow e^-qqqq$	1160.7	1268.7*
$e^+\gamma(\text{BS}) \rightarrow e^+qqqq$	1156.3	1267.6*
$e^-\gamma(\text{EPA}) \rightarrow e^-qqqq$	287.1	287.9*
$e^+\gamma(\text{EPA}) \rightarrow e^+qqqq$	286.9	287.8*
$e^-\gamma(\text{BS}) \rightarrow \nu qqqq$	136.9†	262.5*
$e^+\gamma(\text{BS}) \rightarrow \bar{\nu} qqqq$	136.4†	262.3*
$e^-\gamma(\text{EPA}) \rightarrow \nu qqqq$	32.6†	54.2*
$e^+\gamma(\text{EPA}) \rightarrow \bar{\nu} qqqq$	32.6†	54.2*
$e^-\gamma(\text{BS}) \rightarrow qqH\nu$	15.8*	58.6*
$e^+\gamma(\text{BS}) \rightarrow qqH\nu$	15.7*	58.5*
$e^-\gamma(\text{EPA}) \rightarrow qqH\nu$	3.39*	11.7*
$e^+\gamma(\text{EPA}) \rightarrow qqH\nu$	3.39*	11.7*
$\gamma(\text{BS})\gamma(\text{BS}) \rightarrow qqqq$	21406.2*	13050.3*
$\gamma(\text{BS})\gamma(\text{EPA}) \rightarrow qqqq$	4018.7*	2420.6*
$\gamma(\text{EPA})\gamma(\text{BS}) \rightarrow qqqq$	4034.8*	2423.1*
$\gamma(\text{EPA})\gamma(\text{EPA}) \rightarrow qqqq$	753.0*	402.7*



Mass reconstruction

- $HH\nu\nu \rightarrow bb\bar{b}\bar{b}\nu\nu$, 4 jets in the final state

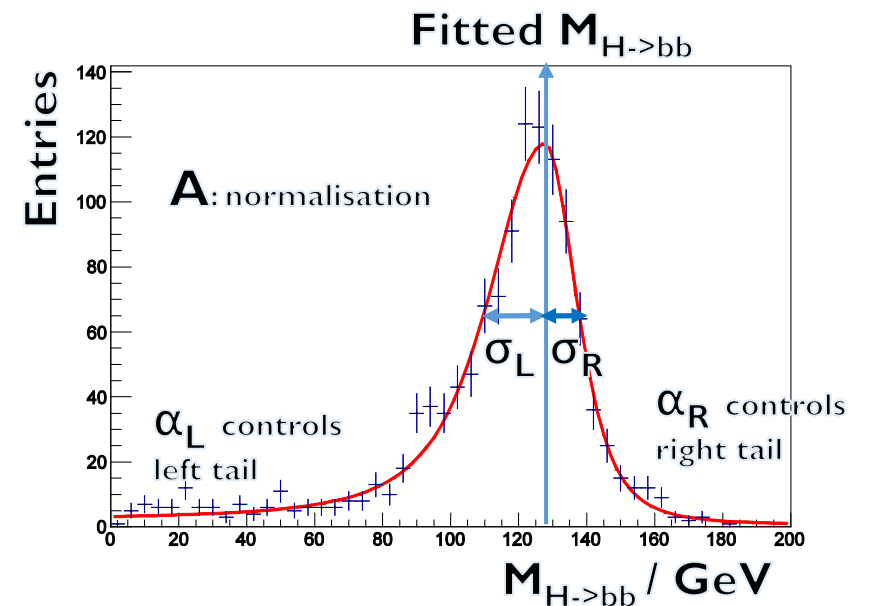
- Minimise $\chi_4^2 = |M_{12} - M_{34}|$

- $HH\nu\nu \rightarrow bbWW\nu\nu \rightarrow bbqqqq\nu\nu$, 6 jets in the final state

- Minimise $\chi_6^2 = \frac{(M_{12} - M_{Hbb})^2}{\sigma_{Hbb}^2} + \frac{(M_{3456} - M_{HWW})^2}{\sigma_{HWW}^2} + \frac{(M_{34} - M_{W^\pm})^2}{\sigma_{W^\pm}^2}$

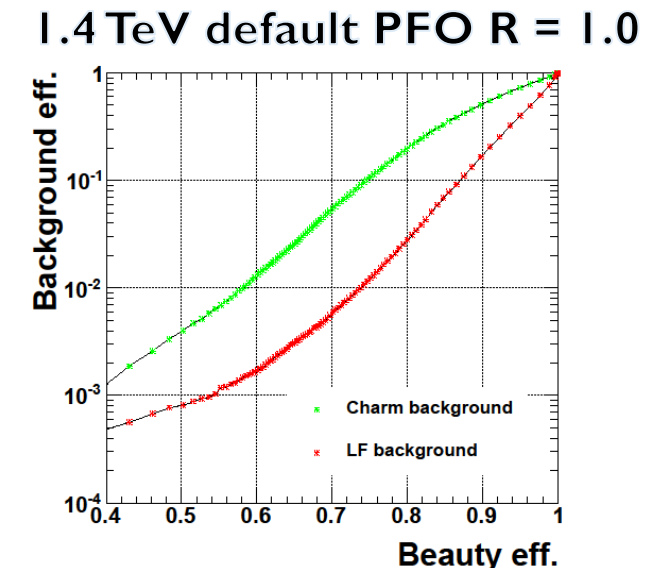
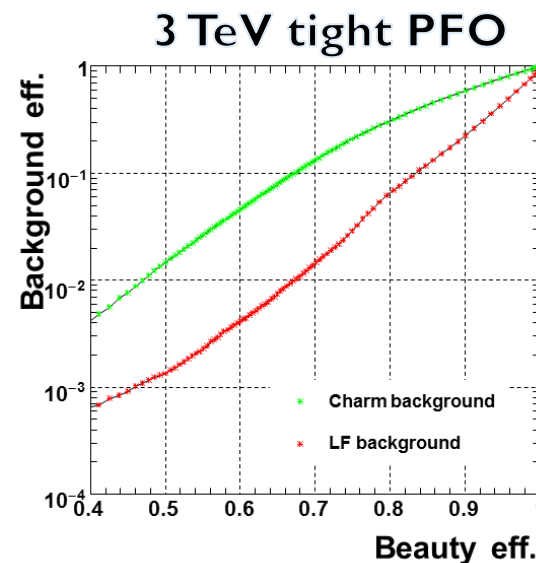
- M_{Hbb} , M_{HWW} , M_{W^\pm} , σ_{Hbb} , σ_{HWW} , σ_{W^\pm} are obtained from fitting of signal events, use $HH\nu\nu \rightarrow bbWW\nu\nu \rightarrow bbqqqq\nu\nu$ channel, cheated jet pairing

- $f = A \exp\left(\frac{-(x-\mu)^2}{g}\right) \begin{cases} g = 2\sigma_L^2 + \alpha_L(x-\mu)^2, & x < \mu \\ g = 2\sigma_R^2 + \alpha_R(x-\mu)^2, & x > \mu \end{cases}$



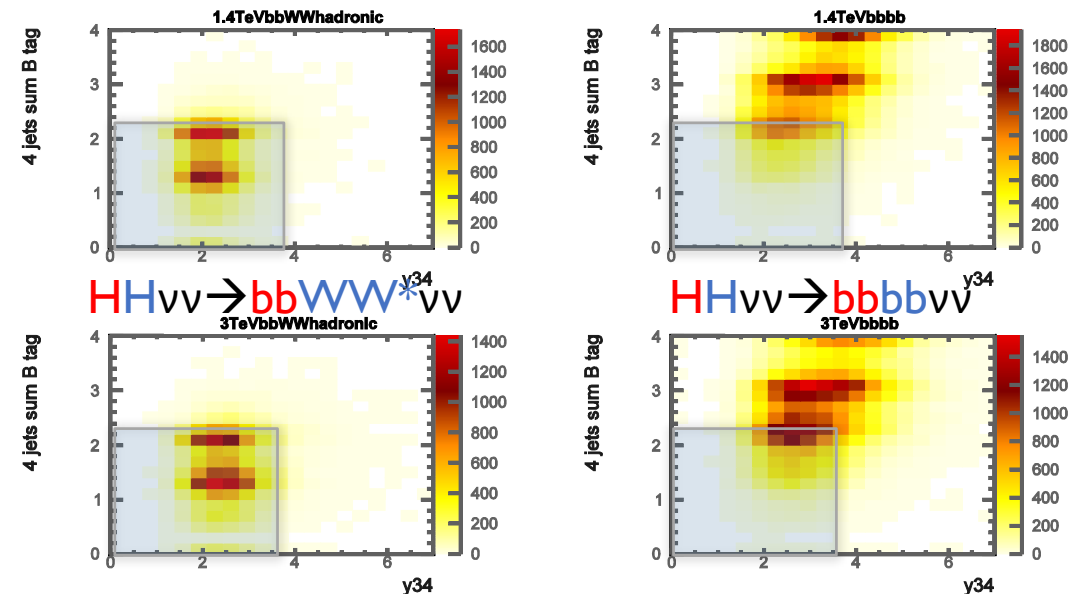
B,C jets tagging

- Want to find B jets as signal events contain $H \rightarrow bb$
- Based on LCFIPlus with root 5.28. Jet reconstruction, Vertexing and Durham algorithm in LCFIPlus
 - Samples $ee \rightarrow Z\nu\nu$, $Z \rightarrow cc/bb/uu/dd/ss$
- Primary and corresponding secondary vertices are forced into the same jet.



Mutually exclusive pre-selection cuts

- Mutually exclusive pre-selection cuts for $HH_{VV} \rightarrow b\bar{b}b\bar{b}VV$ and $HH_{VV} \rightarrow b\bar{b}WW^*VV$, to avoid double counting
- y -parameters and b-tag scanned for the best separation
- 1.4 TeV: $Y_{34} < 3.7$, sum b tag < 2.3 ;
 - bbWW 86%, bbbb 78%; Overall 67.06%
- 3TeV: $Y_{34} < 3.6$, sum b tag < 2.3
 - bbWW 89%, bbbb 82%; Overall 72.4%



MVA

- Optimised to avoid pairwise correlation whilst preserving significance
- $HH_{\nu\nu} \rightarrow bb_{bb\nu\nu}$, 10 variables
- $HH_{\nu\nu} \rightarrow bb_{WW^*\nu\nu}$, 32 variables
 - Smaller cross section. Harder to select signal

Process	σ/fb	ϵ_{preSel}	ϵ_{BDT}	N_{BDT}
$\text{HH}v_e\bar{v}_e; \text{HH} \rightarrow b\bar{b}b\bar{b}$	0.047	94 %	24 %	16
$\text{HH}v_e\bar{v}_e; \text{HH} \rightarrow \text{other}$	0.102	29 %	0.77 %	0.3
$e^+e^- \rightarrow q\bar{q}q\bar{q}v\bar{v}$	23	6.2 %	0.38 %	8
$e^+e^- \rightarrow q\bar{q}q\bar{q}lv$	110	16 %	0.03 %	7
$e^+e^- \rightarrow q\bar{q}Hv\bar{v}$	1.5	39 %	2.0 %	18
$e^\pm\gamma \rightarrow vq\bar{q}q\bar{q}$	154	13 %	0.01 %	3
$e^\pm\gamma \rightarrow qqHv$	30	28 %	0.01 %	1
$\text{HH}v_e\bar{v}_e; \text{HH} \rightarrow b\bar{b}WW^*; W^+W^- \rightarrow q\bar{q}q\bar{q}$	0.018	60 %	8.2 %	1.3
$\text{HH}v_e\bar{v}_e; \text{HH} \rightarrow b\bar{b}b\bar{b}$	0.047	15 %	0.5 %	0.1
$\text{HH}v_e\bar{v}_e; \text{HH} \rightarrow \text{other}$	0.085	20 %	1.7 %	0.5
$e^+e^- \rightarrow q\bar{q}q\bar{q}v\bar{v}$	23	17 %	0.002 %	0.1
$e^+e^- \rightarrow q\bar{q}q\bar{q}lv$	110	10 %	0.01 %	2
$e^+e^- \rightarrow q\bar{q}Hv\bar{v}$	1.5	35 %	0.1 %	0.8
$e^\pm\gamma \rightarrow vq\bar{q}q\bar{q}$	154	22 %	0.0045 %	2
$e^\pm\gamma \rightarrow qqHv$	30	27 %	0.02 %	3

Process	σ/fb	ϵ_{preSel}	ϵ_{BDT}	N_{BDT}
$\text{HH}v_e\bar{v}_e; \text{HH} \rightarrow b\bar{b}b\bar{b}$	0.19	66 %	24 %	61
$\text{HH}v_e\bar{v}_e; \text{HH} \rightarrow \text{other}$	0.40	5.4 %	3.2 %	1
$e^+e^- \rightarrow q\bar{q}q\bar{q}$	547	0.16 %	0.16 %	3
$e^+e^- \rightarrow q\bar{q}q\bar{q}v\bar{v}$	72	1.8 %	0.68 %	17
$e^+e^- \rightarrow q\bar{q}q\bar{q}lv$	107	1.8 %	0.15 %	6
$e^+e^- \rightarrow q\bar{q}Hv\bar{v}$	4.7	18 %	3.0 %	50
$e^\pm\gamma \rightarrow vq\bar{q}q\bar{q}$	523	1.2 %	0.09 %	11
$e^\pm\gamma \rightarrow qqHv$	116	2.7 %	0.14 %	9
$\text{HH}v_e\bar{v}_e; \text{HH} \rightarrow b\bar{b}WW^*; W^+W^- \rightarrow q\bar{q}q\bar{q}$	0.07	62 %	12 %	10
$\text{HH}v_e\bar{v}_e; \text{HH} \rightarrow b\bar{b}b\bar{b}$	0.19	19 %	1.5 %	1
$\text{HH}v_e\bar{v}_e; \text{HH} \rightarrow \text{other}$	0.34	20 %	3.6 %	5
$e^+e^- \rightarrow q\bar{q}q\bar{q}$	547	1.4 %	0.01 %	1
$e^+e^- \rightarrow q\bar{q}q\bar{q}v\bar{v}$	72	9.0 %	0.05 %	6
$e^+e^- \rightarrow q\bar{q}q\bar{q}lv$	107	7.3 %	0.05 %	8
$e^+e^- \rightarrow q\bar{q}Hv\bar{v}$	4.8	32 %	0.6 %	19
$e^\pm\gamma \rightarrow vq\bar{q}q\bar{q}$	523	15 %	0.04 %	67
$e^\pm\gamma \rightarrow qqHv$	116	27 %	0.2 %	140

1.4TeV 1.5ab⁻¹



3TeV 2ab⁻¹

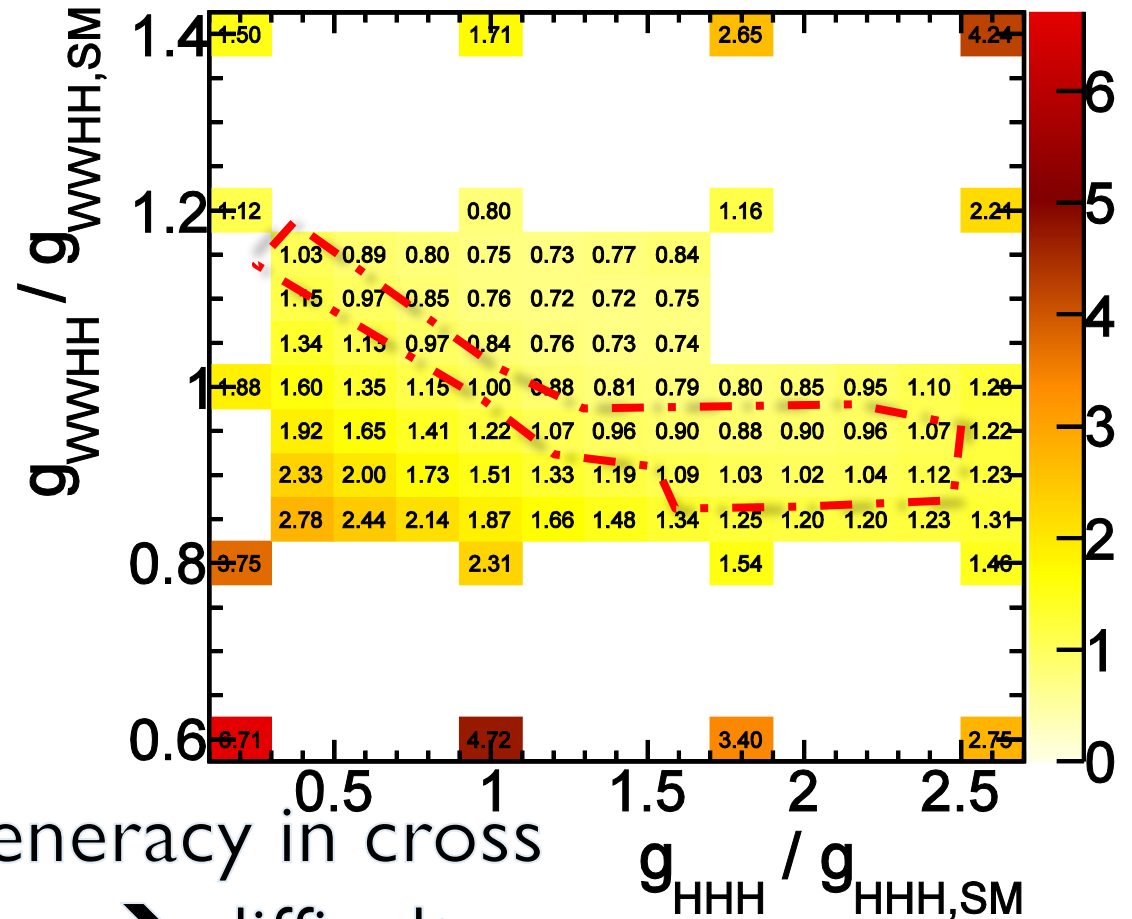
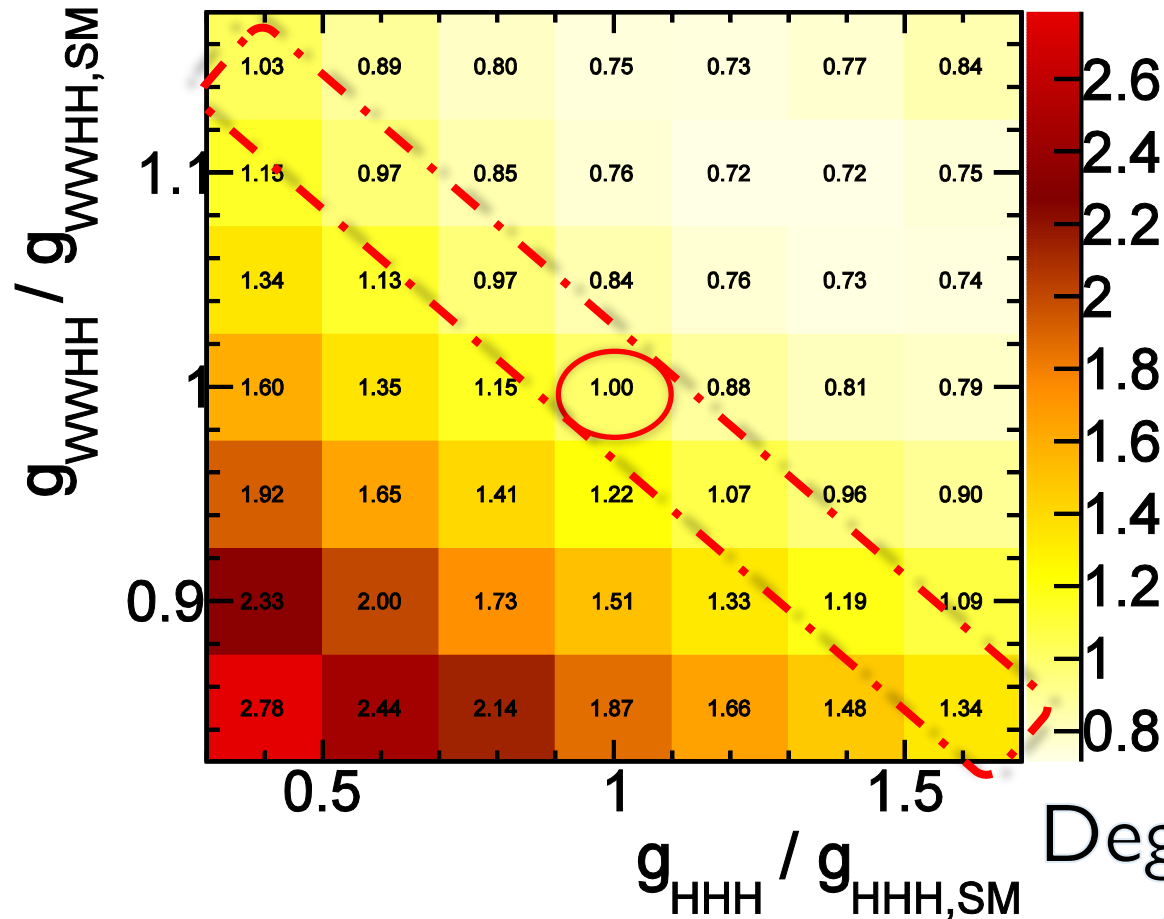


- Corrected higgs decay branching ratio with LHC results

Extraction of g_{HHH} and g_{WWHH}

- Full analysis for $HH\nu\nu \rightarrow bbWW^*\nu\nu \rightarrow bbqqqq\nu\nu$ and $HH\nu\nu \rightarrow bb\nu\nu$ at $\sqrt{s} = 1.4$ and 3 TeV completed. Simple scaling for g_{HHH} sensitivity presented **in higgs paper**
- Simultaneous extraction of g_{HHH} and g_{WWHH} using template fitting method is **work in progress**

Cross section plots, normalised to nominal SM



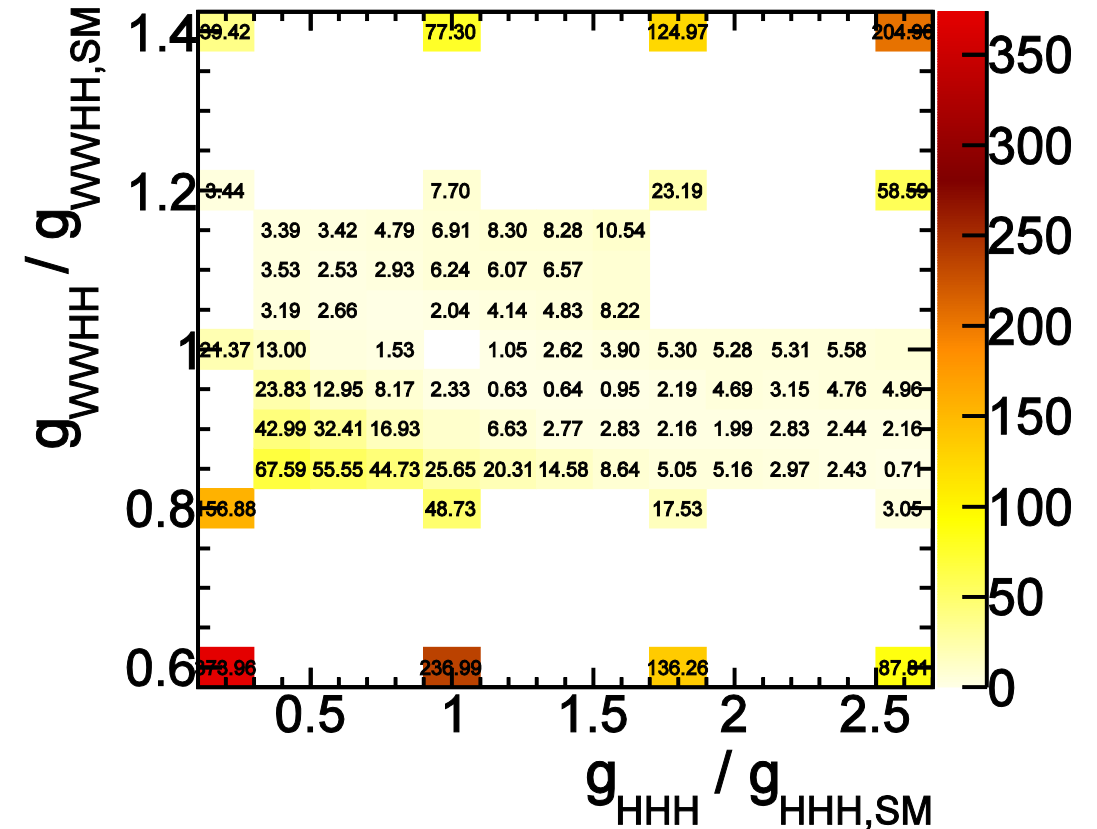
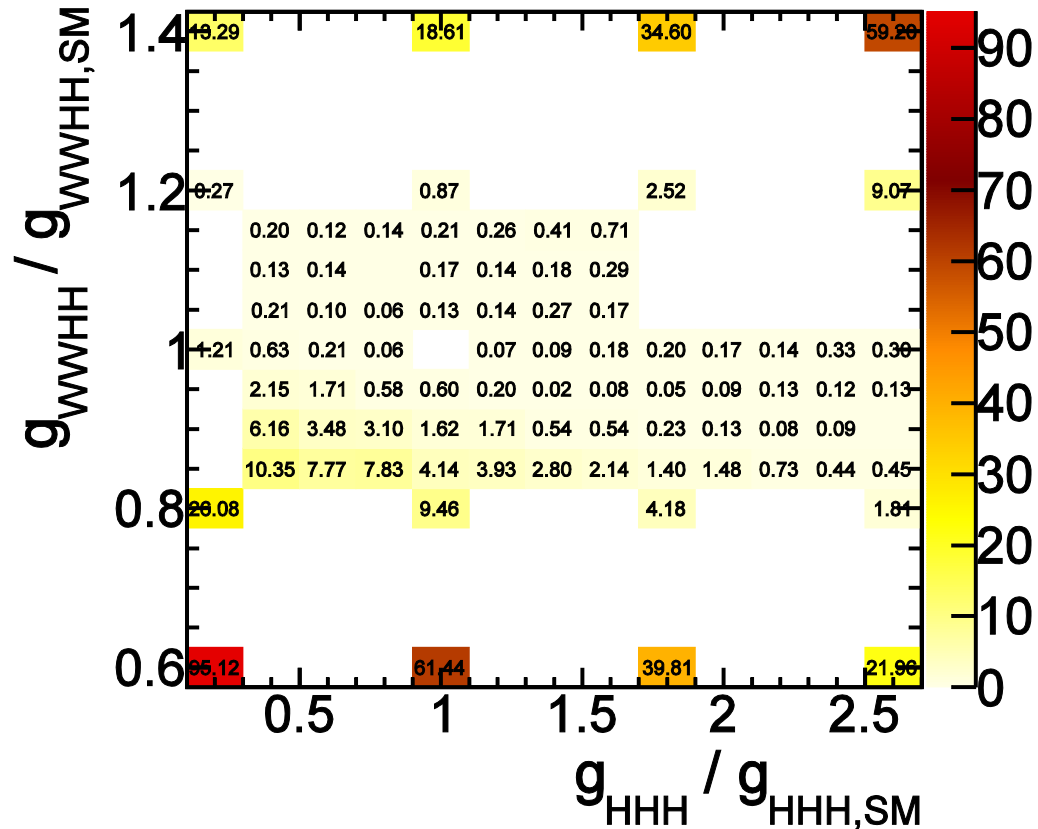
Degeneracy in cross section \rightarrow difficult



Simultaneous extraction of g_{HHH} and g_{WWHH}

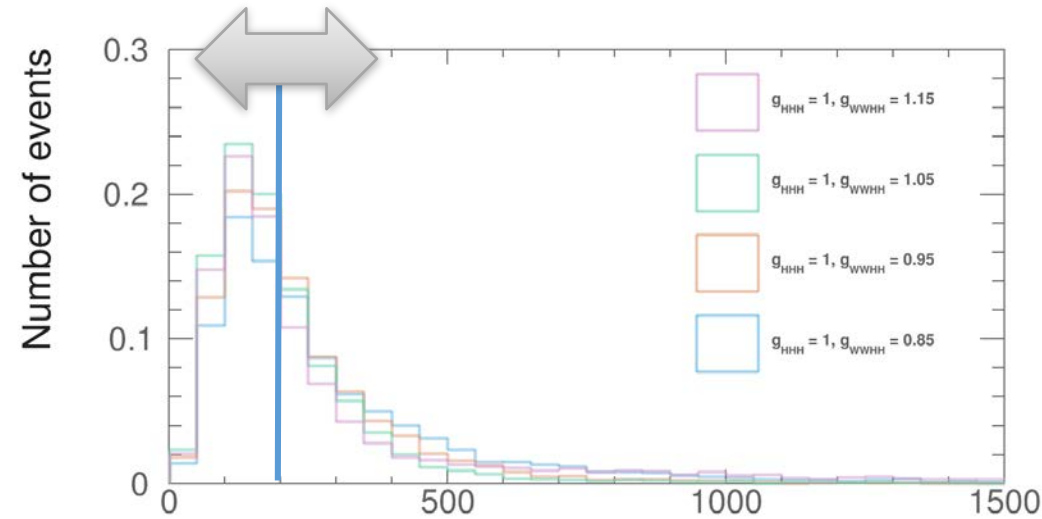
- **Template fitting**
- Samples with modified g_{HHH} and g_{WWHH}
- Apply MVA trained with nominal SM couplings
- Perform Chi-Square calculation on the template
- $\chi^2 = \sum_{i=1}^4 \frac{(\text{Expected} - \text{Observed})^2}{\text{Expected}}$, index i is for kinematic bins, expected is the template distribution, observed is the poisson fluctuated nominal coupling distribution
 - Event numbers normalised to 3ab^{-1} luminosity

Chi-Square template

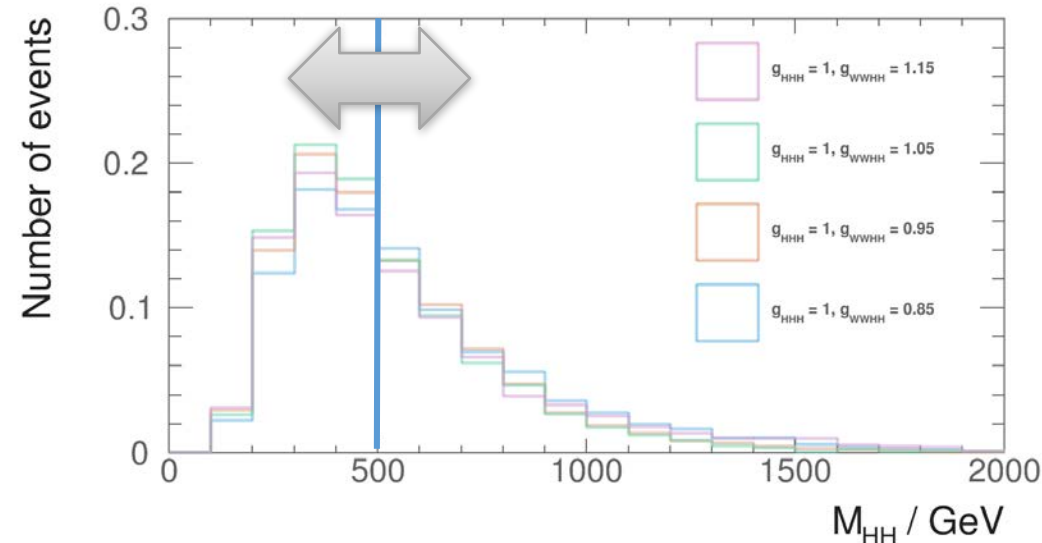


Kinematic bins: H_T and M_{HH}

- Kinematic bins: H_T , sum of P_T of two Higgs; M_{HH} , invariant mass of two Higgs system
 - Motivated by theory paper CERN-PH-TH-2013-161
- One example: H_T : cut at 200 GeV; m_{HH} : cut at 500 GeV
- Another example: H_T : cut at 150, 250, 350 GeV; m_{HH} : cut at 500 GeV
 - Modified couplings samples, plotted $ee \rightarrow HH\nu\nu \rightarrow bbWW\nu\nu$ after pre-selection cuts. Normalised integrated area to 1

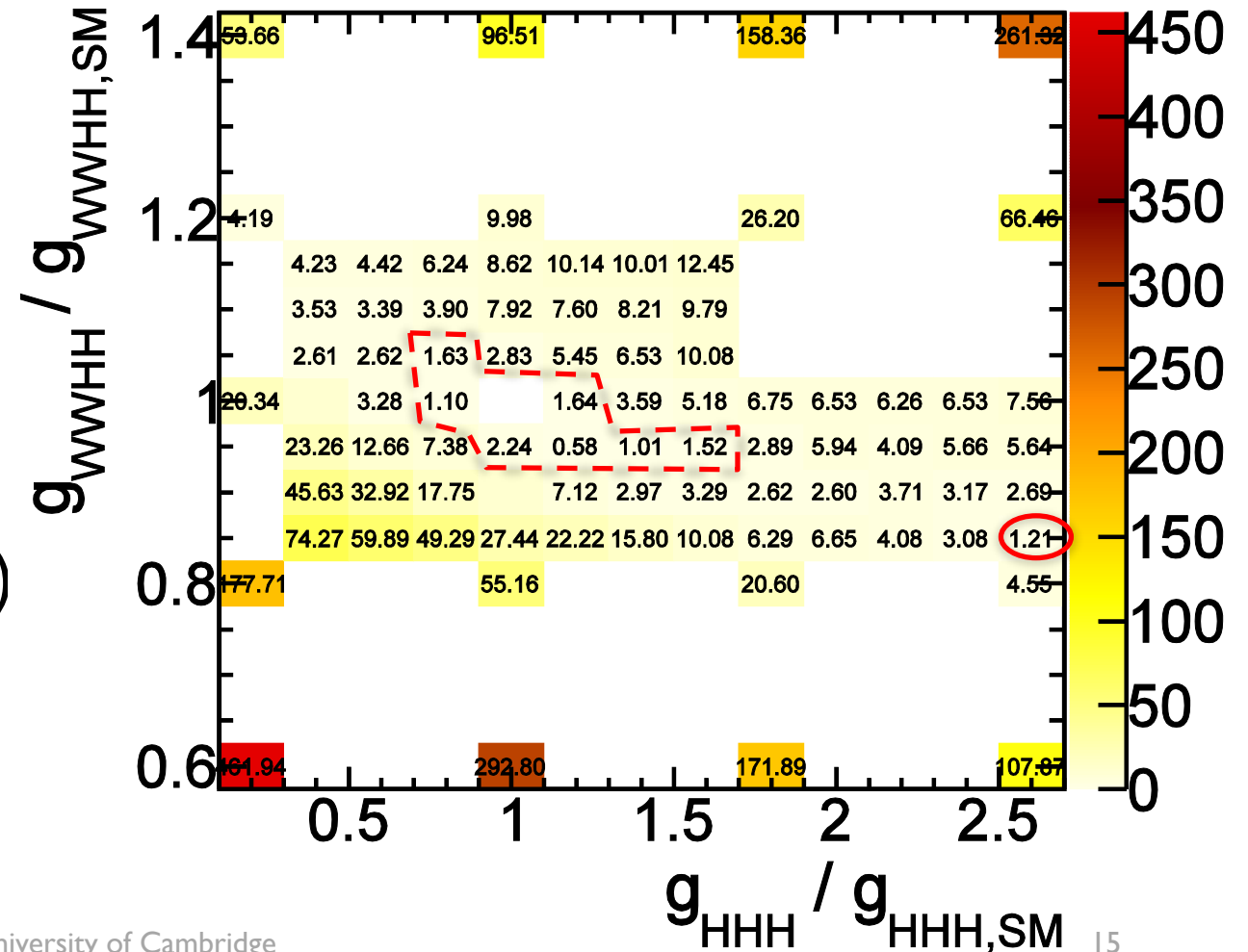


Trends reverse H_T / GeV



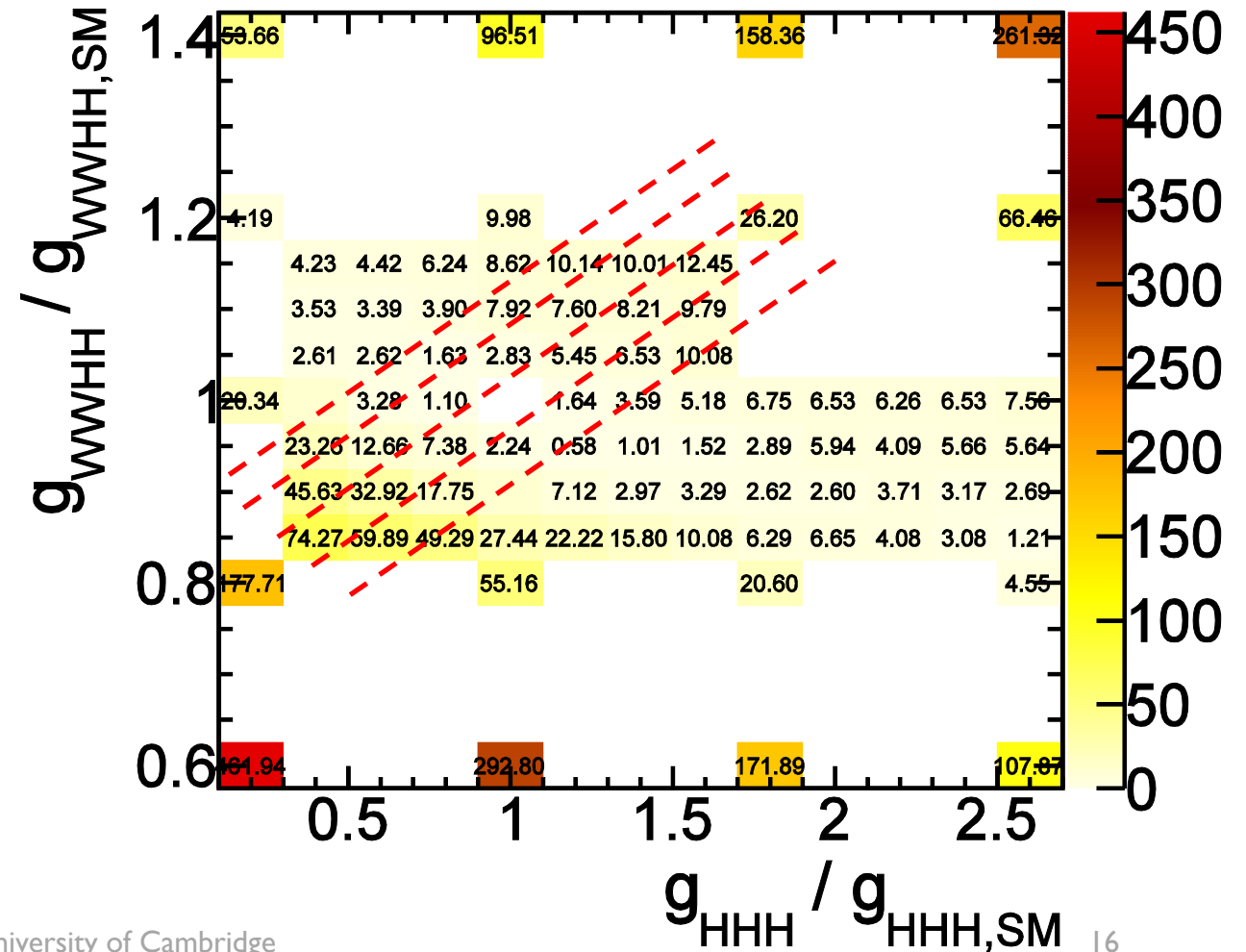
Toy MC, Chi-square average

- 100,000 toy MC experiments, averaged χ^2 template for combined channel
- More stable template
- Extract contour with 2 degrees of freedom
- Dotted line shows 1σ ($\chi^2 = 2.3$)
- More samples generating



Toy MC, Chi-square average, interpolation

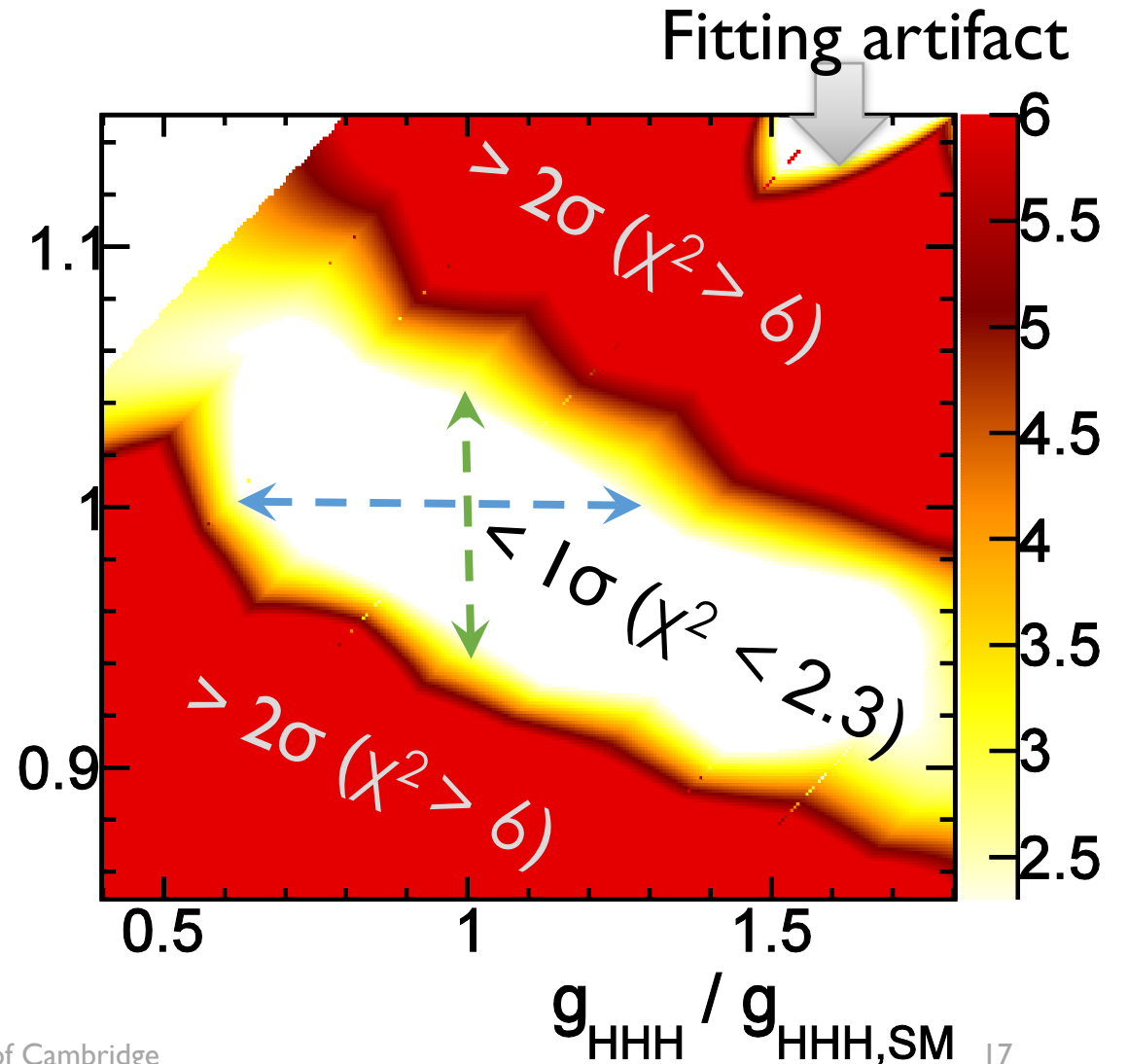
- Slice the template diagonally.
- Fit a cubic function, 4 degrees of freedom, for each slice
- Smooth transition between slices
- Fitting works well close to the minimum points



Toy MC, Chi-square average, interpolation

- Central white: $<1\sigma (\chi^2 < 2.3)$
- Outer red: $>2\sigma (\chi^2 > 6)$
- $g_{HHH} = 1$, $\% \Delta g_{WWHH} \sim 5\%$
- $g_{WWHH} = 1$, $\% \Delta g_{HHH} \sim 33\%$
 - Higgs paper, $2ab^{-1}$, only extract g_{HHH} , crude assumption, $\% \Delta g_{HHH} = 29\%$

Work in progress



Conclusion

- $HH\nu\nu \rightarrow bb\nu\nu$ and $HH\nu\nu \rightarrow bbWW^*\nu\nu$ selection at $\sqrt{s} = 1.4$ and 3 TeV finalised and presented in the higgs paper. A CLIC note in writing.
- For g_{HHH} and g_{WWHH} extraction, on-going work.
- Optimising kinematic bins cuts: Try to increase bins, different cuts.
- More template points being generated