



भारतीय प्रौद्योगिकी संस्थान हैदराबाद
Indian Institute of Technology Hyderabad



Measurement of Lepton Flavor Universality in B decays at Belle

S. Choudhury for the Belle collaboration

IIT Hyderabad, India

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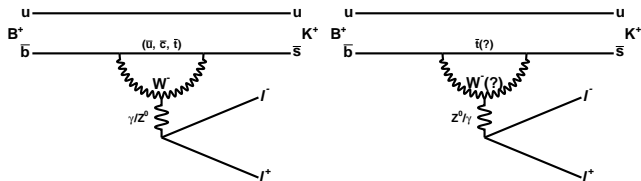
Test of LFU (R_K^*) in $B \rightarrow K^* \ell \ell$ decays [Belle, arXiv: 1904.02440]

Test of LFU (R_K) in $B \rightarrow K \ell \ell$ decays [New] [Conference paper to come]
(Preliminary)

Isospin asymmetry (A_I) in $B \rightarrow K \ell \ell$ decays [New] [Conference paper to come]
(Preliminary)

Introduction

- The rare decay $B \rightarrow K^{(*)} \ell \ell$ involves $b \rightarrow s$ quark level transition, which are flavor changing neutral currents (FCNCs). These processes occur through penguin loop and box diagrams in standard model (SM).



- Global analysis of B decays hints at lepton flavor non universality.
- These decays are highly suppressed and very small BR ($\mathcal{O}(10^{-7})$).
- These decays are very sensitive to new physics (NP).

New physics can contribute by:

- enhancing or suppressing decay rates.
- modifying the angular distribution of the final state particles.

Introduction

- The amplitude of a hadron decay process [arXiv: hep-ph/9806471] is described as:

$$A(M \rightarrow F) = \langle F | \mathcal{H}_{eff} | M \rangle = \frac{G_F}{\sqrt{2}} \sum_i V_{CKM}^i C_i(\mu) \langle F | O_i(\mu) | M \rangle$$

CKM couplings Wilson Coefficients Hadronic Matrix Elements

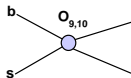
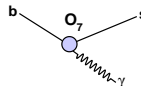
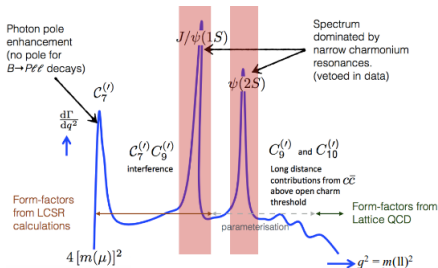
Wilson coefficients $C_i = \text{Perturbative short distance effects}$

Operators $O_i = \text{non-perturbative long distance effects.}$

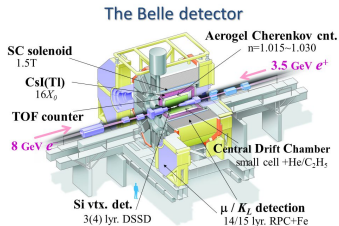
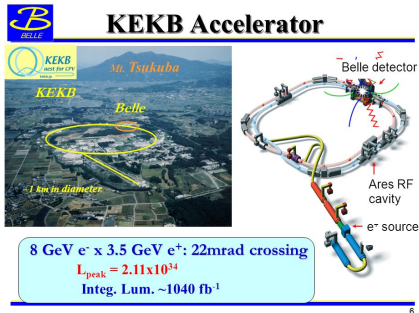
$i = 7$: Photon penguin

$i = 9, 10$: Electroweak penguin

- NP can affect SM operator contributions (Wilson coefficients) and/or enter through new operators.



- Contribution of C_7 , C_9 and C_{10} depends on q^2 (invariant mass square of two leptons).



- The Belle experiment is located at the KEBK accelerator in Tsukuba, Japan.
- Data taking from 1999 to 2010.
- Data collected: $711 \text{ fb}^{-1} = 772 \text{ million } B\bar{B} \text{ pairs}$.

$$e^+e^- \rightarrow \Upsilon(4S) \rightarrow B\bar{B}$$

Test of LFU ($R_{K^*}^*$) for $B \rightarrow K^* \ell \ell$

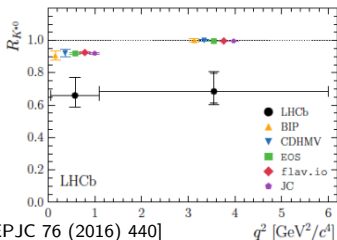
- LHCb measurement of

$$R_{K^*} = \frac{BR(B \rightarrow K^* \mu^+ \mu^-)}{BR(B \rightarrow K^* e^+ e^-)}$$
 shows deviations from SM expectation.

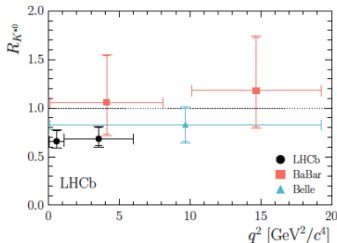
$$R_{K^*}(0.045 < q^2 < 1.1 \text{ GeV}^2/c^4) = 0.66^{+0.11}_{-0.07} \pm 0.03$$

$$R_{K^*}(1.1 < q^2 < 6 \text{ GeV}^2/c^4) = 0.69^{+0.11}_{-0.07} \pm 0.05$$

- Compatibility with the SM estimated to be at the level of $2.1 - 2.3\sigma$ for low q^2 and $2.4 - 2.5\sigma$ at central q^2 for a data sample of 3fb^{-1} .
- Belle [605 fb^{-1}] measurement for whole q^2 region, $R_{K^*} = 0.83 \pm 0.17 \pm 0.08$, is consistent with SM prediction.
- BaBar measured for low and high q^2 bins and are consistent with SM with large uncertainty.



- ▲ BIP [EPJC 76 (2016) 440]
- ▼ CDHVV [JHEP 04 (2017) 016]
- EOS [PRD 95 (2017) 035029]
- ◆ flav. io [EPJC 77 (2017) 377]
- JC [PRD 93 (2016) 014028]



- LHCb [JHEP 08(2017) 055]
- BaBar [PRD 86 (2012) 032012]
- ▲ Belle [PRL 103 (2009) 171801]

Test of LFU (R_{K^*}) in $B \rightarrow K^* \ell \ell$ decays at Belle [arXiv: 1904.02440]

- R_{K^*} measurement with 711 fb^{-1} data sample for different q^2 bins.

- The channels reconstructed for analysis are

$$\begin{aligned} B^0 &\rightarrow K^{*0} \mu^+ \mu^-, B^+ \rightarrow K^{*+} \mu^+ \mu^- \\ B^0 &\rightarrow K^{*0} e^+ e^-, B^+ \rightarrow K^{*+} e^+ e^- \end{aligned}$$

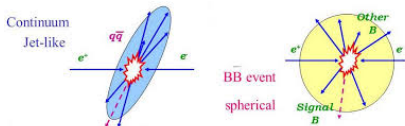
- K^* is reconstructed from:

$$\begin{aligned} K^{*0} &\rightarrow K^+ \pi^- \\ K^{*+} &\rightarrow K^+ \pi^0 \\ K^{*+} &\rightarrow K_S^0 \pi^+ \end{aligned}$$

- Multivariate analysis technique (NN) is used to identify each particle type in the decay chain.
- Kinematic variables which distinguish signal from background are

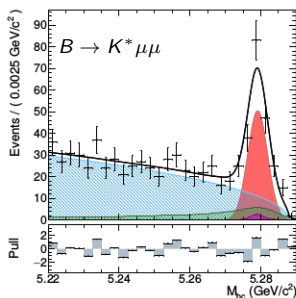
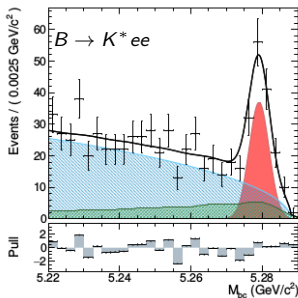
$$\begin{aligned} M_{bc} &= \sqrt{E_{beam}^2/c^4 - |p_B|^2/c^4} \\ \Delta E &= E_B - E_{beam} \end{aligned}$$

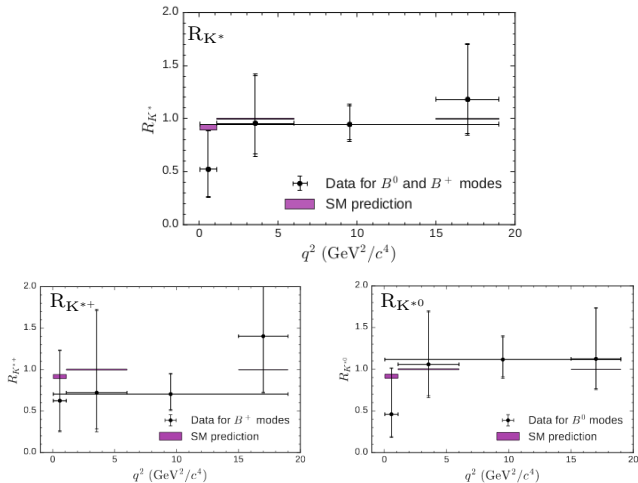
- Requirement on kinematic variables:
 $5.22 < M_{bc} < 5.30 \text{ GeV}/c^2$ and $-0.10 (-0.05) < \Delta E < 0.05 \text{ GeV}$ for $ee(\mu\mu)$
- Backgrounds:



- NN is used to suppress the backgrounds.

- Performed extended maximum likelihood fit in M_{bc} to extract the signal.
- Example fit for $q^2 > 0.045 \text{ GeV}^2/c^4$.
- $103.0^{+13.4}_{-12.7}$ and $139.9^{+16.0}_{-15.4}$ events for electron and muon modes, respectively.



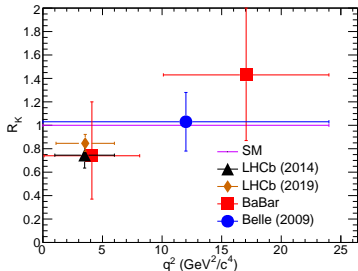


- First measurement of $R_{K^{*+}}$.
- All results are found to be compatible with SM prediction.

Test of LFU (R_K) for $B \rightarrow K\ell\ell$

- SM prediction is very accurate. $R_K^{(SM)} = 1 \pm \mathcal{O}(10^{-2})$
- LHCb [PRL 113, 151601(2014)] shows deviation from SM

$$R_K = \frac{BR(B^+ \rightarrow K^+ \mu^+ \mu^-)}{BR(B^+ \rightarrow K^+ e^+ e^-)} = 0.745^{+0.090}_{-0.074} \pm 0.036$$
 in $q^2 = [1 - 6] \text{ GeV}^2/c^4$: 2.6σ tension for 3fb^{-1} data sample (2011-12 data).
- LHCb [arXiv: 1903.09252] shows $R_K([1.1 - 6]) = 0.846^{+0.016}_{-0.054} {}^{+0.060}_{-0.014}$, 2.5σ deviation for 5 fb^{-1} data sample (2011 - 2016 data).
- The value of R_K for Belle [arXiv: 0904.0770] was consistent with unity within the uncertainty limit measured for a data sample of 605fb^{-1} .



Bin	R_K	Collaboration
$1 < q^2 < 6$	$0.745^{+0.090}_{-0.074} \pm 0.036$	LHCb (2014)
$1.1 < q^2 < 6$	$0.846^{+0.060+0.016}_{-0.054-0.014}$	LHCb (2019)
whole q^2	$1.03 \pm 0.19 \pm 0.06$	Belle
$0.10 < q^2 < 8.12$	$0.74^{+0.40}_{-0.31} \pm 0.06$	BaBar
$q^2 > 10.11$	$1.43^{+0.65}_{-0.44} \pm 0.12$	BaBar

Test of LFU (R_K) in $B \rightarrow K\ell\ell$ decays at Belle [New]

Introduction

- This measurement of R_K is with Belle full data sample of 711 fb^{-1} , while the previous measurement was with 605 fb^{-1} .
- We perform a multi-dimensional fit using M_{bc} , ΔE and background suppression variable to extract the signal yield.
- We calibrate the signal component with $B \rightarrow KJ/\psi$ sample and continuum ($e^+e^- \rightarrow q\bar{q}$) background with off-resonance data sample.

Particle Selection Criteria

- The decay mode reconstructed are $B^+ \rightarrow K^+\ell\ell$ and $B^0 \rightarrow K_S^0\ell\ell$, where $\ell\ell = \mu\mu$ or ee .
- K^\pm , μ^\pm and e^\pm particles satisfying PID are selected from tracks near IP. K_S^0 are selected using K_S^0 displaced vertex properties and with a mass window, 3σ about K_S^0 nominal mass.
- The requirement on kinematic variables are

$$5.2 < M_{bc} < 5.29 \text{ GeV}/c^2 \text{ and } -0.1 < \Delta E < 0.25 \text{ GeV}$$

Test of LFU (R_K) in $B \rightarrow K\ell\ell$ decays at Belle [New]

Background suppression and NN translation

- The irreducible peaking background coming from $B \rightarrow KJ/\psi(\rightarrow \ell\ell)$ and $B \rightarrow K\psi(2S)(\rightarrow \ell\ell)$ are removed by q^2 veto.
- The peaking background are reduced by applying invariant mass veto.

Mode	Peaking source	Veto
$B^+ \rightarrow K^+\mu^+\mu^-$	$B^+ \rightarrow \bar{D}^0(\rightarrow K^+\pi^-)\pi^+$	$M_{K^+\mu^-} \notin [1.8489 - 1.8810]$
$B^+ \rightarrow K^+\mu^+\mu^-$	$B^+ \rightarrow K^+J/\psi(\rightarrow \mu^+\mu^-)$	$M_{K^+\mu^-} \notin [3.06 - 3.13]$

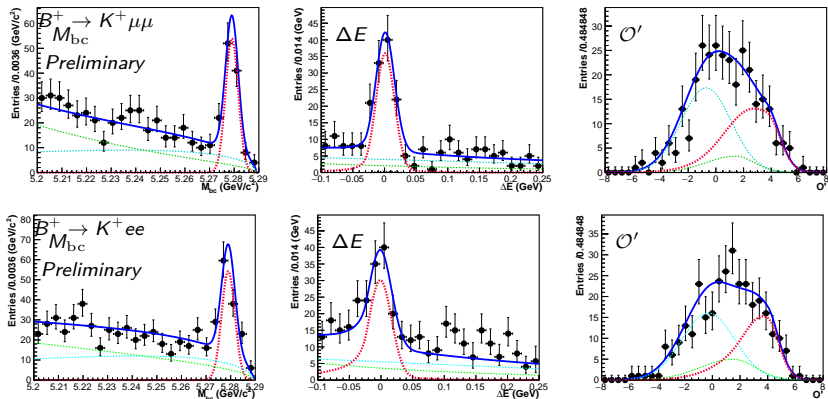
- B to charmless decays have negligible contribution in all modes.
- The NN is trained with some event shape, vertex quality and kinematic variables to suppress the background from continuum and generic B decays.
- The NN output (\mathcal{O}) is translated to \mathcal{O}' using the formula

$$\mathcal{O}' = \log \frac{\mathcal{O} - \mathcal{O}_{\min}}{\mathcal{O}_{\max} - \mathcal{O}}$$

- $NN_{\min} = -0.6$ reduces background $\sim 75\%$, with signal efficiency loss of 4 – 5%.

Fit results for $B \rightarrow K\ell\ell$ [New]

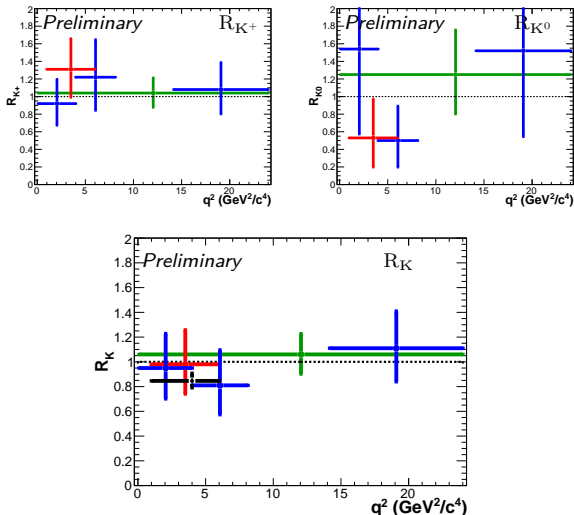
- Extended maximum likelihood fit is performed in 3-dimensions *i.e.*, M_{bc} , ΔE and \mathcal{O}' .
- $B \rightarrow KJ/\psi(\rightarrow \ell\ell)$ is used as a control sample to calibrate the signal PDF of $B \rightarrow K\ell\ell$.
- Example fit of $B^+ \rightarrow K^+ \mu\mu$ and $B^+ \rightarrow K^+ e^+ e^-$ for $q^2 > 0.1 \text{ GeV}^2/c^4$.



- 137 ± 14 , 138 ± 15 events in $B^+ \rightarrow K^+ \mu^+ \mu^-$, $B^+ \rightarrow K^+ e^+ e^-$ modes.
- $27.3^{+6.6}_{-5.8}$ and $21.8^{+7.0}_{-6.1}$ events in $B^0 \rightarrow K_S^0 \mu^+ \mu^-$ and $B^0 \rightarrow K_S^0 e^+ e^-$ modes.

R_K , R_{K^+} and R_{K^0} results from Belle [New]

- R_{K^+} , R_{K^0} and R_K are measured for [0.1 , 4.0], [4.0 , 8.12], [1.0 , 6.0], > 14.18 and > 0.1 q^2 bins.
- R_K is taken as weighted average of R_{K^+} and R_{K^0} .

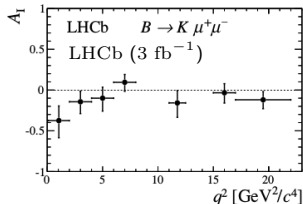
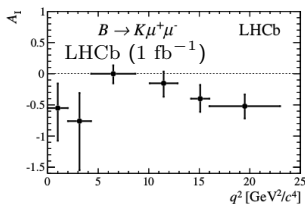


- The measurements are found to be consistent with SM prediction as well as LHCb result.

Isospin Asymmetry (A_I) in $B \rightarrow K\ell\ell$ decays

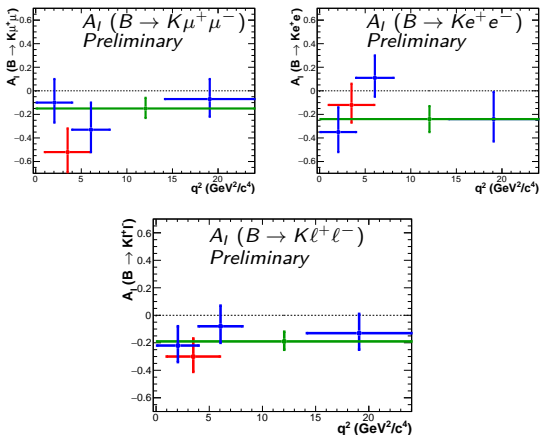
$$A_I = \frac{(\tau_{B^+}/\tau_{B^0}) \times \mathcal{B}(B^0 \rightarrow K^0\ell\ell) - \mathcal{B}(B^+ \rightarrow K^+\ell\ell)}{(\tau_{B^+}/\tau_{B^0}) \times \mathcal{B}(B^0 \rightarrow K^0\ell\ell) + \mathcal{B}(B^+ \rightarrow K^+\ell\ell)}$$

- BaBar [[arXiv:0807.4119](#)] has reported 3.2σ in $B \rightarrow K\ell\ell$ for low q^2 bin using 384 million $B\bar{B}$ pairs.
- Belle [[arXiv: 0904.0770](#)] measurement with 657 million $B\bar{B}$ pairs, show no significant deviation from null value, $\sigma = 1.75$.
- LHCb [[arXiv: 1205.3422](#)] show deviation in $A_I(B \rightarrow K\mu\mu)$ measured for 1 fb^{-1} data sample, the deviation below $q^2 < 4.3\text{ GeV}^2/c^4$ and above $q^2 > 16\text{ GeV}^2/c^4$ bin more significant. The significance of the deviation from zero integrated across q^2 is 4.4σ .
- LHCb [[arXiv: 1403.8044](#)] again show $A_I(B \rightarrow K\mu\mu)$ with 3 fb^{-1} data sample and found negative asymmetry but the results are more consistent with SM expectation.



A_I results from Belle [New]

- A_I is measured for $B \rightarrow K\mu^+\mu^-$, $B \rightarrow Ke^+e^-$ and $B \rightarrow K\ell^+\ell^-$ for $[0.1, 4.0]$, $[4.0, 8.12]$, $[1.0, 6.0]$, > 14.18 and > 0.1 q^2 bins.
- $A_I(B \rightarrow K\ell^+\ell^-)$ as weighted average of $A_I(B \rightarrow K\mu^+\mu^-)$ and $A_I(B \rightarrow Ke^+e^-)$.



- The isospin asymmetry is found for $B \rightarrow K\mu^+\mu^-$ at a level of $\sim 2.7\sigma$ for the bin of $1 < q^2 < 6$ GeV²/c⁴ and this deviation is $\sim 2.5\sigma$ for $B \rightarrow K\ell^+\ell^-$.

- The LFU ratio is measured for several q^2 bins, including the bin of $1 < q^2 < 6 \text{ GeV}^2/c^4$.
- The new results of R_K with Belle full data sample of 711 fb^{-1} are consistent with SM prediction as well as LHCb result.
- R_{K^*} measurement for different q^2 bins are compatible with SM prediction for Belle full data sample.

- A_I shows $\sim 2.7\sigma$ deviation for $B \rightarrow K\mu\mu$ mode of $1 < q^2 < 6 \text{ GeV}^2/c^4$ bin.

- More results to come from Belle and Belle II.

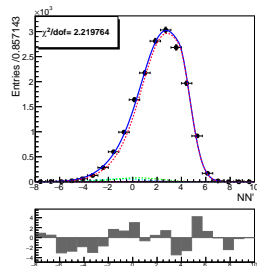
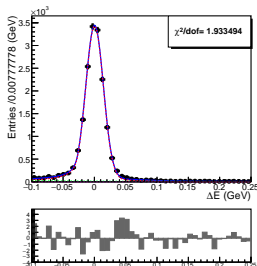
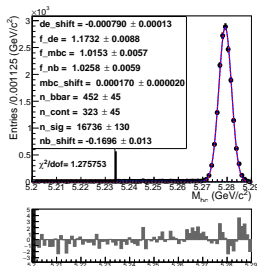
*Thank
you!*

Table: R_{K^+} , R_{K^0} and R_K for different q^2 bins.

Bin	R_{K^+}	R_{K^0}	R_K
$0.1 < q^2 < 4$	$0.92^{+0.27}_{-0.24} \pm 0.05$	$1.5^{+1.2}_{-1.0} \pm 0.1$	$0.95^{+0.27}_{-0.24} \pm 0.06$
$4 < q^2 < 8.12$	$1.22^{+0.42}_{-0.37} \pm 0.07$	$0.50^{+0.39}_{-0.30} \pm 0.03$	$0.81^{+0.28}_{-0.23} \pm 0.05$
$1 < q^2 < 6$	$1.31^{+0.34}_{-0.31} \pm 0.07$	$0.53^{+0.44}_{-0.33} \pm 0.03$	$0.98^{+0.27}_{-0.23} \pm 0.06$
$q^2 > 14.18$	$1.08^{+0.30}_{-0.27} \pm 0.06$	$1.52^{+1.23}_{-0.97} \pm 0.10$	$1.11^{+0.29}_{-0.26} \pm 0.07$
whole q^2	$1.04^{+0.16}_{-0.15} \pm 0.06$	$1.25^{+0.50}_{-0.44} \pm 0.08$	$1.06^{+0.15}_{-0.14} \pm 0.07$

Table: $A_I(B \rightarrow K\mu\mu)$, $A_I(B \rightarrow Kee)$ and $A_I(B \rightarrow K\ell\ell)$ for different q^2 bins.

Bin	$A_I(B \rightarrow K\mu\mu)$	$A_I(B \rightarrow Kee)$	$A_I(B \rightarrow K\ell\ell)$
$0.1 < q^2 < 4$	$-0.10^{+0.20}_{-0.17} \pm 0.01$	$-0.35^{+0.21}_{-0.17} \pm 0.01$	$-0.22^{+0.14}_{-0.12} \pm 0.01$
$4 < q^2 < 8.12$	$-0.33^{+0.23}_{-0.19} \pm 0.01$	$0.11^{+0.19}_{-0.16} \pm 0.01$	$-0.08^{+0.15}_{-0.12} \pm 0.01$
$1 < q^2 < 6$	$-0.52^{+0.20}_{-0.17} \pm 0.02$	$-0.12^{+0.18}_{-0.15} \pm 0.01$	$-0.30^{+0.13}_{-0.11} \pm 0.01$
$q^2 > 14.18$	$-0.07^{+0.17}_{-0.15} \pm 0.01$	$-0.24^{+0.23}_{-0.19} \pm 0.01$	$-0.13^{+0.14}_{-0.12} \pm 0.01$
whole q^2	$-0.15^{+0.09}_{-0.08} \pm 0.01$	$-0.24 \pm 0.11 \pm 0.01$	$-0.19^{+0.07}_{-0.06} \pm 0.01$



Condition	R_K
$R_K(B^+ \rightarrow K^+ J/\psi)$	0.992 ± 0.011
$R_K(B^0 \rightarrow K_S^0 J/\psi)$	1.048 ± 0.020