

Charm and tau loop effects in $B^+ \rightarrow K^+ \mu^+ \mu^-$

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based on ongoing work with G.Isidori, M.König, S. Liechti, P. Owen, N.Serra

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Can we use it to extract bounds on NP in $b \rightarrow s\tau\tau$?

Effective field theory description

EFT for
$$b \to s\mu\mu$$
: $\mathscr{L}_{eff} = \frac{4G_F}{\sqrt{2}} V_{tb} V_{ts}^* \sum_i C_i(\mu) O_i$,

$$SM \begin{cases} O_9^{\mu} = \frac{e^2}{16\pi^2} (\bar{s}\gamma_{\mu}P_L b)(\bar{\mu}\gamma^{\mu}\mu) & O_{10}^{\mu} = \frac{e^2}{16\pi^2} (\bar{s}\gamma_{\mu}P_L b)(\bar{\mu}\gamma^{\mu}\gamma_5\mu) \\ O_7 = \frac{e}{16\pi^2} m_b (\bar{s}\sigma_{\mu\nu}P_R b) F^{\mu\nu} & O_{1-6}, O_8 \end{cases}$$

NP
$$C_i^{\text{SM}} \rightarrow C_i^{\text{SM}} + \delta C_i^{NP}$$
 and/or new operators

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• C_i^{SM} • f_+, f_0, f_T for $B \to K$

Non-local effects: the charm loop

Non-local (long distance) effects arise via 4-quark + chromomagnetic operator, and are included via

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[Semi]perturbative approach valid at low q^2 : Pert. contribution + expansion in $\Lambda^2_{QCD}/(q^2 - 4m_c^2)$ [Khodjamirian et al., 1212.0234] cannot be applied in the full kinematical range : **Non-local (long distance)** effects arise via 4-quark + chromomagnetic operator, and are included via

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Goal: model long-distance effects at experiments, in the entire spectrum.





• Standard approach: exclude events close to resonances [Babar, Belle, CDF, CMS, LHCb...]



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- access long-distance info unaccessible from first principles [e.g. phases]
- extract reliable short-distance info [hence NP!]

We propose the following parametrisation of hadronic long-distance contributions:

$$C_9^{\text{eff}}(q^2) = C_9 + Y(q^2), \quad Y(q^2) = Y_0 + \Delta C_{q\bar{q}}^{1P}(q^2) + \Delta C_{c\bar{c}}^{1P}(q^2) + \Delta C_{c\bar{c}}^{2P}(q^2)$$

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constraint: $|\Delta C_{\bar{q}q}^{1P}(0)| = \mathcal{O}\left(\frac{\Lambda_{QCD}}{m_b}\right)$. CKM ≈ 0
suppression

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$$\rho(s) = \operatorname{Im} \left\{ \underbrace{\frac{\mathfrak{B}}{\rho}}_{\mu} \underbrace{\kappa}_{\mu} \right\} \sim \left\{ \begin{cases} \left(1 - \frac{4m_D^2}{s}\right)^{3/2} & DD \\ \left(1 - \frac{4m_D^2}{s}\right)^{3/2} & D^*D \end{cases} \right\} \\ \left(1 - \frac{4m_D^2}{s}\right)^{1/2} & D^*D \end{cases}$$

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Two-particle $\bar{c}c$ states (DD, D^*D^*, DD^*)

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constraint: $q^2 \ll m_c^2$ $\Delta C_{c\bar{c}}^{1P}(q^2) + \Delta C_{c\bar{c}}^{2P}(q^2) = \Delta C_{c\bar{c}}^{\text{pert}}(q^2)$

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Consider a NP scenario where a large $C_{9\tau}$ is generated:



 $O_{9}^{\tau} \sim (\bar{s}\gamma_{\mu}P_{L}b)(\bar{\tau}\gamma^{\mu}\tau) \qquad [e.g. \text{ combined expl. of} B \text{ anomalies...}]$

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Probing $b \rightarrow s\tau\tau$ directly is experimentally challenging...

 $\mathscr{B}_{\exp}(B^+ \to K^+ \tau^+ \tau^-) < 2.25 \cdot 10^{-3} \quad \text{[Babar]} \qquad \qquad \mathscr{B}_{\text{SM}}(B^+ \to K^+ \tau^+ \tau^-) = 1.2 \cdot 10^{-7}$

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...can we get a competitive bound from the $B^+ \rightarrow K^+ \mu^+ \mu^-$ spectrum?



Preliminary sensitivity @ LHCb [with Run 2 statistics]: $\mathscr{B}(B^+ \to K^+ \tau^+ \tau^-) \leq \mathscr{O}(10^{-4})$

The $\tau - \tau$ cusp



assuming $\mathscr{B}(B^+ \to K^+ \tau^+ \tau^-) =$ Babar upper limit (for illustration)

Conclusions and outlook

Preliminary studies of the expected sensitivity at LHCb with Run II statistics suggest the possibility of constraining NP in $b \rightarrow s\tau\tau$ through its imprint on the spectrum of $B^+ \rightarrow K^+\mu^+\mu^-$.

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In progress:

- detailed study on realistic sensitivity expected at LHCb with Run II statistics (and possibly beyond)
- extensions to other channels, e.g. $B \to K^* \mu^+ \mu^-$

Thank you!